


Cite this: *RSC Adv.*, 2021, 11, 10253

Theoretical study of the H/D isotope effect of CH₄/CD₄ adsorption on a Rh(111) surface using a combined plane wave and localized basis sets method

Hiroki Sakagami,^a Masanori Tachikawa^b and Takayoshi Ishimoto^{*acd}

We analysed the H/D isotope effect of CH₄/CD₄ adsorption on a Rh(111) surface using our combined plane wave and localized basis sets method, that we proposed for the consideration of delocalized electrons on a surface and the quantum effect of protons (deuterons) in metal–molecule interactions. We observed that the adsorption distance and energy of CD₄ were larger and lower than those of CH₄, respectively. This is in reasonable agreement with the corresponding experimental results of cyclohexane adsorption. We clearly found that the trend of the H/D isotope effect in the geometrical and energetic difference was similar to that of the hydrogen-bonded systems.

Received 24th December 2020
Accepted 1st March 2021

DOI: 10.1039/d0ra10796d

rsc.li/rsc-advances

Introduction

The behaviour of atoms and molecules on various surfaces has attracted attention in various fields, including materials science, material physics, and catalytic chemistry. In particular, the interaction between hydrogen (H) and transition metals is a crucial factor in chemical and physical processes. The H in the molecules that are adsorbed on metal surfaces determines important phenomena for not only fundamental physics but also for catalytic activity.^{1,2} It has been reported that the differences in adsorption energy, diffusion coefficient, and catalytic activity depend on various metals and surface orientations.^{3–5} Despite these studies, the interaction mechanism between H and metal surfaces is still not clearly understood due to the difficulty in the direct analysis of H on the metal surface from only the experimental side.

The interaction between H and metal surfaces is often analysed by deuterium (D) substitution for H. This helps in understanding the details of molecular adsorption on metal surfaces from the viewpoint of H/D isotope effects. Thus, understanding the H/D isotope effect is one of the key factors for surface design. For example, using a high-vacuum

microbalance, Jin *et al.* observed that the adsorption energy of D₂ (0.302 eV) is larger than that of H₂ on the surface of a Pd–Pt alloy.⁶ Zheng *et al.* observed that the diffusion coefficient of H (0.027 cm² s^{−1}) is larger than that of D on Pd(111) surfaces.⁴ These experimental results clearly indicate that the adsorption of D on metal surfaces is stronger than that of H. Moreover, H/D isotope effects in the chemical reactions of the adsorbed molecules on metal surfaces, such as oxygen reduction and hydrogen exchange reactions, were reported.^{7–9} However, it is difficult to directly analyse the H/D isotope effects in detail in the structural parameters of the adsorbed molecules on the metal surfaces.

Recently, Koitaya *et al.* observed the H/D isotope effects on the adsorption energy and adsorption distance of the molecules of cyclohexane (C₆H₁₂) and its deuterium substituent (C₆D₁₂) on Rh(111) surface.¹⁰ To the best of our knowledge, this is the first report discussing the H/D isotope effects on the geometrical differences of molecules adsorbed on a metal surface. Interestingly, they clearly elucidated that the adsorption energy of C₆H₁₂ was 0.084 eV higher than that of C₆D₁₂. This result shows an opposite trend of the H/D isotope effects on H/D atomic adsorption on the metal surfaces. However, the mechanism of this inverse isotope effect is still unclear. Therefore, it is necessary to understand the mechanism of the geometrical H/D isotope effects of adsorbed molecules on metal surfaces.

It is well known that the electronic structure calculation is one of the most powerful approaches for elucidating the detailed mechanism of adsorbed molecules on the metal surfaces. The plane wave (PW) approach using periodic boundary conditions (PBCs) is an effective tool for understanding physical and chemical phenomena on the metal surfaces. There are also many studies on H adsorption on the

^aGraduate School of Nanobioscience, Yokohama City University, 22-2 Seto, Kanazawa-ku, Yokohama 236-0027, Japan

^bGraduate School of Data Science, Yokohama City University, 22-2 Seto, Kanazawa-ku, Yokohama 236-0027, Japan

^cDepartment of Applied Chemistry, Graduate School of Advanced Science and Engineering, Hiroshima University, 1-3-2 Kagamiyama, Higashihiroshima 739-8511, Japan. E-mail: tishimo@hiroshima-u.ac.jp

^dDivision of Materials Model-Based Research, Digital Monozukuri (Manufacturing) Education and Research Center, Hiroshima University, Higashi-Hiroshima 739-0046, Japan


metal surfaces.^{11–14} Since the nuclear quantum effects (NQE) of protons and deuterons are treated as a difference of nuclear mass in the framework of the Born–Oppenheimer approximation in the conventional electronic structure calculation, the H/D isotope effects are discussed using the vibrational zero-point energy under harmonic oscillator approximation.¹⁵ However, reproducing the geometrical differences under the above treatment of protons and deuterons is difficult. Thus, it is essential to analyse the geometrical differences in the metal–hydrogen interaction that are induced by the difference in the NQE of protons and deuterons. Although the direct treatment of the NQE of protons and deuterons is important in electronic structure calculations for discussing the H/D isotope effects, PW embedded NQE have not yet been developed. It is also difficult to describe small geometrical and electronic structure differences in H and D by the PW approach.

For the direct treatment of the difference of the NQE of protons and deuterons, we developed multicomponent molecular orbital and density functional theory (MC_MO and MC_DFT) approaches, which are based on localized orbitals (LOs).^{16–18} Using these approaches, it is possible to describe the geometrical and electronic structure changes that are induced by H and D.^{17,19} Although these approaches are useful in investigating the H/D isotope effects for adsorbed molecules on metal surfaces, the calculation of large systems, such as those defined by PBCs, is not realistic due to high computational cost. Moreover, the addition of LO-based MC_MO and MC_DFT to the PW approach is challenging due to the high cost of program modification and computational accuracy. Thus, to achieve sufficient accuracy for analysing the H/D isotope effects for adsorbed molecules on metal surfaces, we proposed the combined plane wave and localized basis sets (CPLB) method.²⁰ In the CPLB method, the electronic structure of the surface system is calculated using the PW approach. Conversely, a highly accurate LO calculation that is based on the MC_MO or MC_DFT approach is used for cluster model to describe the NQE of protons and deuterons directly. The combination of both the PW- and LO-based approaches facilitates a detailed analysis of the H/D isotope effects for molecular adsorption on metal surfaces. We have already reported the efficiency of the CPLB method in analysing the H/D isotope effects of H/D atomic adsorption on the Pd(111) surface.²¹

In this study, we calculated the CH₄/CD₄ adsorption on the Rh(111) surface, which is a model of C₆H₁₂/C₆H₁₂ adsorption on Rh(111) surface experimentally,¹⁰ using the CPLB method to analyse and understand the geometrical and energetic changes induced by the H/D isotope effect.

CPLB method

Herein, we explain the framework of our proposed CPLB method. The CPLB method is developed by extending it to a periodic system that is based on the ONIOM-like scheme.²² The procedure for the calculation of adsorption energy for the CH₄ adsorption on the Rh(111) surface is illustrated in Fig. 1. The total energy of the surface system ($E(\text{PW, surface})$) consisting of the Rh(111) surface with adsorbed CH₄ was calculated

using the PW-based electronic structure calculations. The total energy of adsorbed CH₄ on the Rh cluster model, *i.e.*, $E(\text{PW, cluster})$ and $E(\text{LO, cluster})$, were calculated using both the PW- and LO-based electronic structure calculations, respectively. Based on these values, the total energy of the surface ($E(\text{CPLB, surface})$) is calculated by the CPLB method using eqn (1), which provides sufficient accuracy by including both delocalized electronic structure in PW and accurate metal–hydrogen interaction in the LO. In addition, by selecting the appropriate calculation method as PW or LO calculation, it is also possible to further analyse. In this study, we calculated these systems including the NQE of proton and deuteron by selecting the MC approach for the LO calculation.

$$E(\text{CPLB, surface}) = E(\text{PW, surface}) - E(\text{PW, cluster}) + E(\text{LO, cluster}) \quad (1)$$

The $\text{grad} E(\text{CPLB, surface})$ can be obtained by using the gradient with respect to the nuclear coordinates for each energy, as follows:

$$\text{grad} E(\text{CPLB, surface}) = \text{grad} E(\text{PW, surface}) - \text{grad} E(\text{PW, cluster}) - \text{grad} E(\text{PW, cluster}) \quad (2)$$

Using this scheme, we developed a geometry optimisation algorithm for the CPLB method. The adsorption energy and various other properties of CH₄ were also calculated using the same procedure.

Computational details

The computational details of each calculation are as follows: for the PW-based electronic structure calculations, we used the Vienna *ab initio* simulation package (VASP)^{23,24} with the projector-augmented wave method.^{25,26} The Perdew–Burke–Ernzerhof approximation with a generalized gradient approximation²⁷ was used for the exchange and correlation functionals. The cut-off energy was set to 800 eV. The structure of the Rh(111) surface was modelled based on three atomic layers with 16 atoms in each layer since the energy difference between 3 and 4 or 5 atomic layers was less than 0.005 eV for CH₄

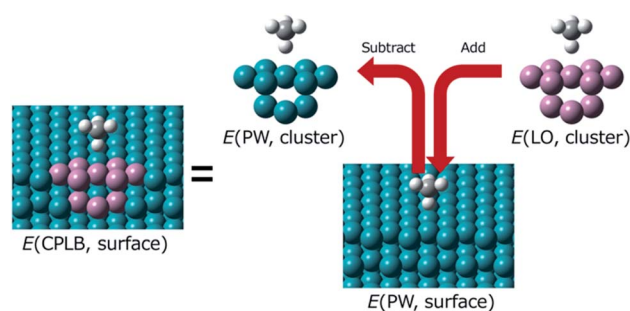


Fig. 1 Schematic illustration of the CPLB approach for CH₄ adsorption on a Rh(111) surface. The green and pink balls are Rh atom. These were treated using the PW and LO methods, respectively.



Table 1 The optimised parameters (Å) for adsorbed CH₄/CD₄ at the on-top site on Rh(111) surface using the CPLB method. X indicates H or D in CH₄/CD₄. $r(\text{C}-\text{X}[\text{upper}])$ is the average value of three C–H/C–D distances pointing upward

	CH ₄	CD ₄	$\Delta(\text{CD}_4-\text{CH}_4)$
$r(\text{C}\cdots\text{Rh})$	3.190	3.226	0.036
$r(\text{X}\cdots\text{Rh})$	2.071	2.111	0.040
$r(\text{C}-\text{X})$	1.119	1.115	−0.004
$r(\text{C}-\text{X}[\text{upper}])$	1.112	1.105	−0.007

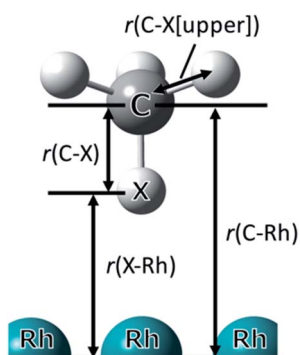


Fig. 2 Optimised adsorption structure of CH₄ on Rh(111) surface. The symbols used in Table 1 are also illustrated here. X indicates H or D in CH₄/CD₄.

Table 2 Adsorption energy (E_{ads}) (eV) of CH₄/CD₄ on Rh(111) surface

	CH ₄	CD ₄	$\Delta(\text{CD}_4-\text{CH}_4)$
$E_{\text{ads}}(\text{CPLB, surface})$	−0.402	−0.396	0.006

Table 3 The NBO charges of the interacting H/D atom in CH₄/CD₄ with Rh(111) and the total charges of CH₄/CD₄

	CH ₄	CD ₄	$\Delta(\text{CD}_4-\text{CH}_4)$
Interacting H/D	0.249	0.242	−0.008
CH ₄ /CD ₄	0.053	0.049	−0.004

adsorption. In the surface model calculation of the PBCs, $4 \times 4 \times 1$ k -points were sampled using the Monkhorst–Pack grid method.²⁸ For the LO-based electronic structure calculations, the modified Gaussian16 program package²⁹ embedded with the MC_DFT method¹⁸ was used to take into account the NQEs of protons and deuterons. For electrons, the LanL2DZ basis set with an effective core potential^{30–32} was used for Rh atoms, and the 6-31G(d,p) basis set was used for other atoms in the APFD method.³³ For the nucleus, the single s-type Gaussian-type function, $\exp\{-\alpha(r - R)^2\}$, was used for each protonic and deuteronic basis function. The α values for protons and deuterons were set to the standard values of 24.1825 and 35.6214, respectively.³⁴

The on-top site on the Rh(111) surface was found to be the most stable site for CH₄ adsorption compared to face-centered cubic and hexagonal close-packed sites. Based on these results, a H/D atom in CH₄/CD₄ was placed at the on-top site on the Rh(111) surface as initial structure obtained by conventional PW approach. The geometry of this system was optimised as follows. First, the position of the surface atoms in the top (1st) layer was optimised using the PW approach. Then, CH₄ was placed at the on-top site, and CH₄ and Rh atoms in the top layer were optimised using the PW approach. Finally, the atomic coordinates of CH₄/CD₄ were optimised using the CPLB method including the MC_DFT approach as an LO part under the condition of fixed Rh atoms on the surface.

Results and discussion

In this study, we show and discuss the results of the optimised geometry parameters, adsorption energy, and charges for CH₄/CD₄ adsorption on Rh(111) surface. The optimised parameters for adsorbed CH₄/CD₄ are listed in Table 1. The symbols used in Table 1 are illustrated in Fig. 2.

In Table 1, $\Delta(\text{CD}_4-\text{CH}_4)$ is the difference in the optimised parameters between CH₄ and CD₄. A positive value indicates that the bond distance of CD₄ was longer than that of CH₄. Since $r(\text{C}\cdots\text{Rh})$ is the distance between C the nearest neighbour (just below) Rh atom, its value was considered as the adsorption distance of the CH₄/CD₄ molecule on the Rh(111) surface. The $r(\text{C}\cdots\text{Rh})$ of CD₄ was longer than that of CH₄.

Looking at the geometrical parameters of $r(\text{X}\cdots\text{Rh})$, the $r(\text{D}\cdots\text{Rh})$ in the CD₄ adsorption was longer than that in the CH₄ adsorption as well as $r(\text{C}\cdots\text{Rh})$. Furthermore, both $r(\text{X}\cdots\text{Rh})$ and $r(\text{C}\cdots\text{Rh})$ are shorter than the values using the conventional PW approach (2.322, 3.429 Å), because of the NQEs. These $r(\text{C}\cdots\text{Rh})$ and $r(\text{X}\cdots\text{Rh})$ geometrical H/D isotope effect for the CH₄/CD₄ adsorption showed the similar trend as the difference of adsorption distance of C₆H₁₂/C₆D₁₂ that is observed in the experiments by Koitaya *et al.*¹⁰ In contrast, the $r(\text{C}-\text{D})$ of CD₄ was shorter than that of CH₄. Compared to the C–X distance in isolated CH₄/CD₄ (1.113/1.106 Å), which is calculated by the MC_DFT method, we clearly observed the same trend of geometrical H/D isotope effect. The H/D isotope effect that the covalent bond distance of the C–D bond is shorter than that of the C–H bond was due to the anharmonicity of the potential. Furthermore, both $r(\text{C}-\text{D})$ and $r(\text{C}-\text{H})$ are longer than the C–H/C–D distance in isolated CH₄/CD₄ owing to the interaction between CH₄/CD₄ and the Rh(111) surface. These results indicate that the geometrical changes due to D substitution for H were opposite in the $r(\text{C}\cdots\text{Rh})$ and covalent $r(\text{C}-\text{X})$ cases and H/D atomic adsorption on the Pd(111) surface.²¹ The difference in $r(\text{C}\cdots\text{Rh})$ is similar to the Ubbelohde effect observed in typical hydrogen-bonded systems.^{35,36} Hence, the C $\cdots$ Rh interaction was considered to be different from H/D atomic adsorption and essentially the same as the typical hydrogen-bonded systems.³⁷ In addition, this result indicates that the interaction between CD₄ and Rh(111) was weaker than in CH₄ case.

Further, we analysed the adsorption energy of CH₄/CD₄ on the Rh(111) surface, and the results are listed in Table 2. The



adsorption energy of CH₄ on the Rh(111) surface was defined as follows;

$$E_{\text{ads}} = E_{\text{tot}} - (E_{\text{surf}} + E_{\text{CH}_4}) \quad (3)$$

where E_{ads} is the adsorption energy of CH₄ on the Rh(111) surface, E_{tot} is the total energy of CH₄ adsorbed on the Rh(111) surface, and E_{surf} and E_{CH_4} are the total energies of the Rh(111) surface model and CH₄ molecule, respectively. A negative E_{ads} value indicates stable adsorption of CH₄ on the Rh(111) surface. The E_{ads} of CD₄ was lower than that of CH₄. The E_{ads} difference of CH₄/CD₄ showed the same trend as C₆H₁₂/C₆D₁₂ adsorption, which was observed in the experiments performed by Koitaya *et al.*¹⁰ We also confirmed that CD₄ has a weaker interaction with the Rh(111) surface than CH₄.

Finally, we performed a natural bond orbital (NBO) analysis³⁸ during the LO calculation. The NBO charges of the interacting H/D atom with the Rh(111) surface and the total charges of CH₄/CD₄ are listed in Table 3. Different NBO charges were observed in the interacting H/D atom and the total charges of CH₄/CD₄. The charges around the H atom (0.249) were larger than those around the D atom (0.242). This observation suggests that the number of electrons around the proton is lower than that around the deuteron. In the CH₄/CD₄ molecule, the total charge around the CH₄ molecule (0.053) was larger than around CD₄ (0.043), which showed a similar trend of interacting H/D atoms. In fact, the magnitude of the dipole moment of CH₄ (0.465 D) was slightly larger than that of CD₄ (0.415 D) expectedly. These results suggest that the number of electrons transferred to the Rh(111) surface was larger in CH₄ than that in CD₄, and CH₄ has a stronger interaction with the Rh(111) surface than CD₄.

Conclusions

We studied CH₄/CD₄ adsorption on Rh(111) surface to analyse and understand the H/D isotope effect on the molecules that are adsorbed on metal surfaces. We developed the CPLB method for highly accurate calculation for analysis of molecular adsorption on metal surfaces, which is difficult to calculate using conventional methods. Consequently, we observed the H/D isotope effects in terms of adsorption distance, adsorption energy, and charge. Our results suggest that the mechanism of molecular adsorption on metal surfaces differs from that of atomic adsorption. Furthermore, the molecular adsorption shows the H/D isotope effects that are similar to those observed in conventional hydrogen-bonded systems. Based on these observations, we confirm that our developed CPLB approach is effective in reproducing the H/D isotope effects on CH₄/CD₄ adsorption on metal surfaces. The extension to other atomic or molecular adsorption on various types of surface would be possible in the framework of CPLB approach. Moreover, the CPLB approach is expected to be a powerful tool for analysing H/D isotope effects on various phenomena, such as adsorption, desorption, absorption, and catalysis, that involve atoms/molecules on heterogeneous systems such as surfaces and bulk systems.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

This work was supported by JSPS KAKENHI Grant Numbers JP18K05035 and JP19H05062 "HYDROGENOMICS" (TI), and JP18H01945 and JP19H05063 "HYDROGENOMICS" (MT). The computations were carried out using the computer resources offered under the category of General Projects by the Research Institute for Information Technology, Kyushu University and Research Center for Computational Science (RCCS), Okazaki, Japan.

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