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Electron correlation effects on uranium isotope fractionation in $\text{U(VI)}-\text{U(VI)}$ and $\text{U(IV)}-\text{U(VI)}$ equilibrium isotopic exchange systems†

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Uranium isotope fractionation has been extensively investigated in the fields of nuclear engineering and geochemical studies, yet the underlying mechanisms remain unclear. This study assessed isotope fractionations in $\text{U(VI)}-\text{U(VI)}$ and $\text{U(IV)}-\text{U(VI)}$ systems by employing various relativistic electron correlation methods to explore the effect of electron correlation and to realize accurate calculations of isotope fractionation coefficients (ϵ). The nuclear volume term, $\ln K_{\text{nv}}$, the major term in ϵ , was estimated using the exact two-component relativistic Hamiltonian in conjunction with either HF, DFT(B3LYP), MP2, CCSD, CCSD(T), FSCCD, CASPT2, or RASPT2 approaches for small molecular models with high symmetry. In contrast, chemical species studied in prior experimental work had moderate sizes and were asymmetrical. In such cases, electron correlation calculations other than DFT calculations were not possible and so only the HF and B3LYP approaches were employed. For closed-shell $\text{U(VI)}-\text{U(VI)}$ systems, the MP2, CCSD and CCSD(T) methods yielded similar $\ln K_{\text{nv}}$ values that were intermediate between those for the HF and B3LYP methods. Comparisons with experimental results for $\text{U(VI)}-\text{U(VI)}$ systems showed that the B3LYP calculations gave results closer to the experimental data than the HF calculations. Because of the open-shell structure of U(IV) , multireference methods involving the FSCCD, CASPT2 and RASPT2 techniques were used for $\text{U(IV)}-\text{U(VI)}$ systems, but these calculations exhibited instability. The average-of-configuration HF method showed better agreement with the experimental ϵ values for $\text{U(IV)}-\text{U(VI)}$ systems than the B3LYP method. Overall, electron correlation improved the description of ϵ for the $\text{U(VI)}-\text{U(VI)}$ systems but challenges remain with regard to open-shell U(IV) calculations because an energy accuracy of 10^{-6} – $10^{-7} E_{\text{h}}$ is required for $\ln K_{\text{nv}}$ calculations.

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Introduction

Uranium possesses two abundant isotopes having long half-lives, these being ^{235}U and ^{238}U . These isotopes generally exist in two dominant oxidation states (OSs) with differing mobilities: hexavalent U (U(VI)), which is highly soluble in water, and tetravalent U (U(IV)), which is sparingly soluble. The $^{238}\text{U}/^{235}\text{U}$ ratio can be significantly affected by redox processes, such as the reduction of U(VI) to U(IV) mediated by abiotic reducing agents or microbial enzymatic activities.^{1–9} The range of U isotope ratios observed in natural samples, including minerals, sediments and seawater, is quite broad.^{4,10–14} Hence, these

differences in U isotope ratios are expected to be utilized for assessing the redox evolution in Earth's oceans and atmosphere, as well as for enhancing our understanding of the evolution of life on Earth and ongoing subsurface processes. However, the underlying mechanisms governing variations in the isotope ratio (*i.e.*, isotope fractionation) during geochemical processes remain incompletely understood, necessitating further research.

In aqueous solution, U(VI) typically adopts the uranyl structure (UO_2^{2+}) while coordinating with H_2O molecules and various anions along the equatorial plane of the cation. The isotope fractionation coefficients (ϵ) for $\text{U(VI)}-\text{U(VI)}$ species involving carbonate, chloride, perchlorate and certain carboxylates (such as acetate, lactate and malate) were experimentally determined using ion exchange chromatography.^{15,16} In such prior work, ϵ was calculated as the difference in the $^{238}\text{U}/^{235}\text{U}$ ratio between a U(VI) species in solution and the hydrated UO_2^{2+} bound to a strongly acidic cation exchange resin packed into a column. These experiments were conducted at 298 K and the largest ϵ value obtained was 0.34‰ between the carbonate and

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resin-bound hydrated species, showing enrichment of ^{235}U in the former and ^{238}U in the latter. Such prior studies also demonstrated a proportional relationship between ε and the harmonic frequency of the $\text{U}=\text{O}$ asymmetric stretching mode (ν_3).^{15,16}

In other work, ε was determined for a $\text{U(IV)}-\text{U(VI)}$ system in low pH media containing either hydrochloric acid (HCl)^{17–19} or sulfuric acid (H_2SO_4).²⁰ These acidic conditions promoted the solubility of U(IV) and facilitated the appearance of an isotopic exchange equilibrium on a reasonable timescale. Previous studies by Fukuda *et al.* and Fujii *et al.* reported ε values ranging from 0.9 to 1.4‰ with a measurement error on the order of 20% at temperatures in the range of 303–433 K.^{17,18} Florence *et al.* reported an ε value of 1.3 ± 0.8 (2 σ)‰ for a direct isotopic exchange reaction in an H_2SO_4 solution at 308 K.²⁰ More recently, Wang *et al.* achieved isotopic exchange equilibrium through a direct isotopic exchange reaction in an HCl solution at 298 K.¹⁹ Based on the resulting data, ε could be estimated to be 1.65 ± 0.16 (2 σ)‰. The consistently positive ε values obtained for these $\text{U(IV)}-\text{U(VI)}$ systems provided evidence for ^{238}U enrichment in the U(IV) at isotopic equilibrium for the $\text{U(IV)}-\text{U(VI)}$ system.

The ε value can be theoretically approximated by the sum of the nuclear mass term ($\ln K_{\text{nm}}$), which arises from variations in vibrational energy levels resulting from differences in the reduced masses of isotopologues,²¹ and the nuclear volume term ($\ln K_{\text{nv}}$). Please refer to the section entitled “Theory of isotope fractionation in equilibrium” for the definitions of these terms. The latter originates from the difference in the ground-state electronic energies of isotopologues stemming from variations in the volume and shape of the atomic nucleus.^{22–26} In the case of the isotopic fractionation of heavy elements such as Hg, Tl, Pb and U, $\ln K_{\text{nv}}$ makes the predominant contribution to ε .^{22–26} This term is, in turn, greatly affected by relativistic effects because the electron density in the vicinity of a heavy nucleus is correlated with the magnitude of $\ln K_{\text{nv}}$.^{21,24–29} Consequently, the four-component Dirac–Coulomb (DC) Hamiltonian, one of the most accurate relativistic Hamiltonians, has been widely employed to compute $\ln K_{\text{nv}}$ together with the Hartree–Fock (HF) wave function, representing the DCHF method.^{25,26,30–35} Previously, the $\ln K_{\text{nv}}$ value for the chloride $\text{U(IV)}-\text{U(VI)}$ system was theoretically estimated by Abe *et al.* using UO_2Cl_3^- and $\text{UO}_2\text{Cl}_4^{2-}$ as molecular models for U(VI) together with UCl_4 as the U(IV) model, employing the DCHF method.³² The $\ln K_{\text{nv}}$ values calculated for UO_2Cl_3^- and $\text{UO}_2\text{Cl}_4^{2-}$ were both 1.90‰, in reasonable agreement with the experimental $\ln K_{\text{nv}}$ value of 2.24‰ at 303 K reported by Fujii *et al.*¹⁸ Nemoto *et al.* performed $\ln K_{\text{nv}}$ calculations for the same system using the infinite-order two-component Douglas–Kroll–Hess relativistic Hamiltonian,^{36–38} based on the HF formalism, and demonstrated that this level of theory yields $\ln K_{\text{nv}}$ results nearly equivalent to those generated by the DCHF method but with approximately 30 times faster computational speed.³⁹ Nemoto also suggested the possibility of using the exact two-component (X2C) relativistic Hamiltonian^{38,40–42} as an alternative. In recent studies, the present authors conducted

relativistic calculations of $\ln K_{\text{nv}}$ utilizing the X2C Hamiltonian within the density functional theory (DFT) formalism, which can incorporate electron correlation to some extent while maintaining computational efficiency comparable to that of the HF technique.^{43–45} However, the effect of employing DFT on the results was not examined in detail in this prior research. To the best of our knowledge, the effects of electron correlation on $\ln K_{\text{nv}}$ have been examined only with regard to the $\text{Hg(0)}-\text{Hg(II)}$ systems in work by Wiederhold *et al.* and Schable.^{46,47} In prior studies, employing second-order Møller–Plesset perturbation (MP2) theory⁴⁸ and coupled cluster singles, doubles and perturbative triples (CCSD(T))^{49,50} provided better agreement with experimental data (within a 6% error) and up to a 29% difference compared with HF results. Notably, in the case of U, the close energy levels of the valence orbitals (that is, the 5f, 6d and 7s orbitals)⁵¹ highlight the potential importance of static electron correlation in the theoretical treatment of U and suggest the necessity of an extensive investigation into the role of such orbitals in U isotope fractionation.

The present work employed various relativistic electron correlation methods to explore the impact of electron correlation on uranium isotope fractionation and to allow the calculations of accurate ε values. Given the computational complexity of advanced electron correlation methods, this study examined only highly symmetrical small molecules. Thus, we employed $\text{UO}_2\text{X}_4^{2-}$ ($\text{X}^- = \text{F}^-, \text{Cl}^-, \text{Br}^-$) (D_{4h}), $\text{UO}_2(\text{CO}_3)_2^{2-}$ (D_{2h}), $\text{UO}_2(\text{NO}_3)_2$ (D_{2h}) and $\text{UO}_2(\text{H}_2\text{O})_4^{2+}$ (D_{4h}) as hypothetical molecular models for U(VI) and UX_4 ($\text{X}^- = \text{F}^-, \text{Cl}^-, \text{Br}^-$) (T_d) as the U(IV) counterparts (as illustrated in Fig. 1). Note that the point group symmetry of each molecule is indicated in parentheses above. The HF, B3LYP, MP2,^{48,52} CCSD, CCSD(T),^{49,50} Fock-space CCSD (FSCCD),⁵³ complete active-space configuration interaction (CASCI), CAS second-order perturbation theory (CASPT2),^{54–56} restricted active-space CI (RASCI) and RAS second-order perturbation theory (RASPT2)⁵⁷ techniques were employed along with the X2C Hamiltonian for the purpose of calculating $\ln K_{\text{nv}}$. In addition, HF and B3LYP calculations were carried out to estimate ε values using more realistic asymmetrical large molecular models based on previous experimental studies of $\text{U(VI)}-\text{U(VI)}$ ^{15,16} and $\text{U(IV)}-\text{U(VI)}$ ^{17–20} systems. These estimated ε values were subsequently compared with experimental data to evaluate the suitability of the HF and B3LYP formalisms.

Theory of isotope fractionation in equilibrium

An isotope exchange reaction is generally represented as

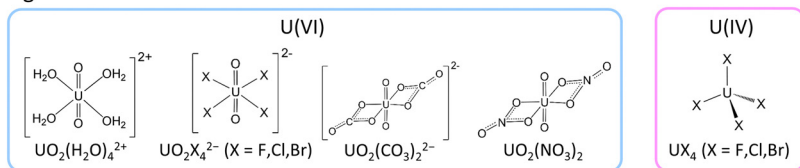


where A and A' refer to heavy and light isotopes, respectively, and AX and AY represent chemical compounds. The isotope fractionation coefficient, ε , can then be defined as

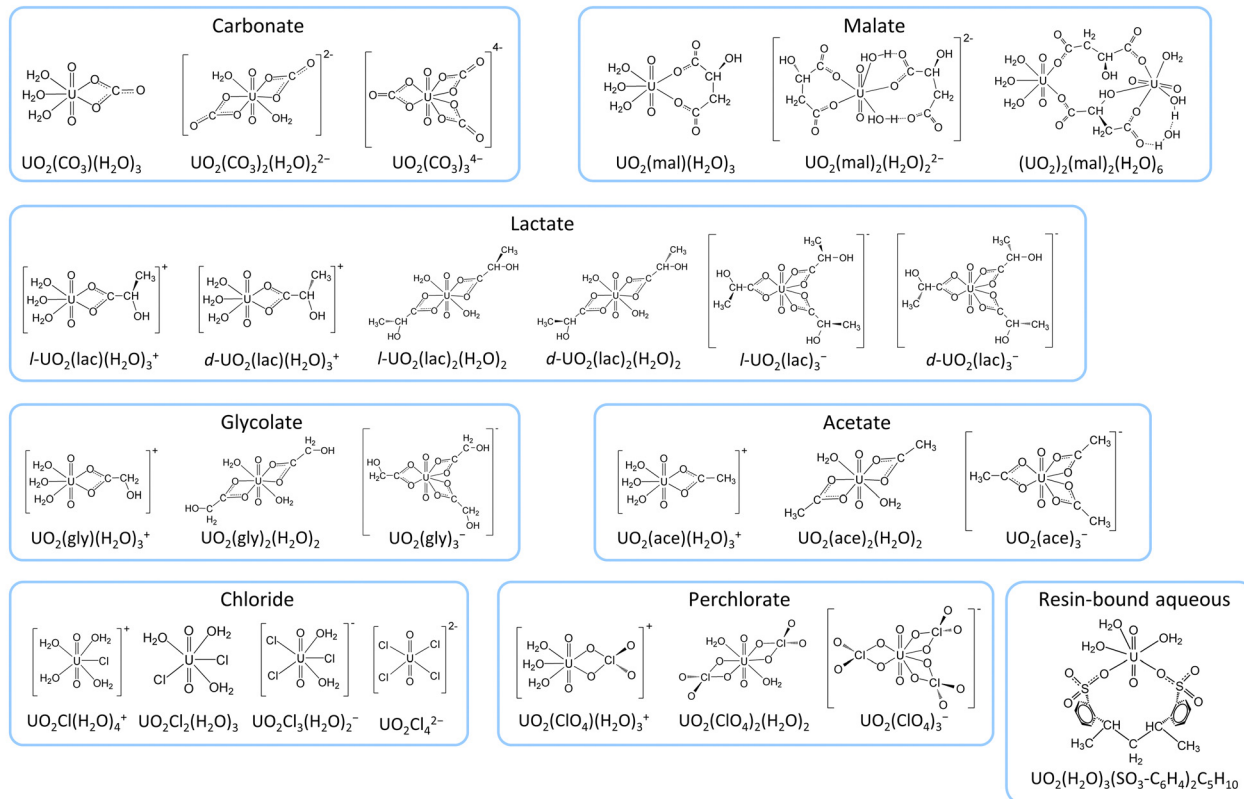
$$\varepsilon = \frac{[\text{A}'\text{X}]/[\text{AX}]}{[\text{A}'\text{Y}]/[\text{AY}]} - 1, \quad (2)$$



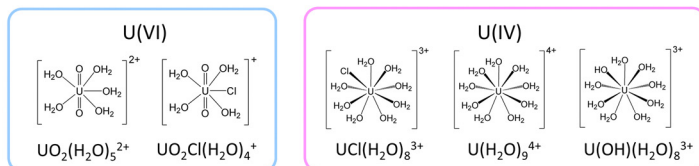
(a) High-level electron-correlation calculations



(b) U(VI)-U(VI) system



(c) U(IV)-U(VI) chloride system



(d) U(IV)-U(VI) sulfate system

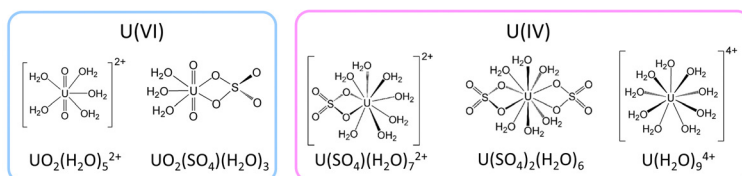


Fig. 1 Molecular structures utilized for (a) high-level electron correlation calculations and for comparisons with the experimental (b) U(vi)–U(vi), (c) U(IV)–U(vi) chloride and (d) U(IV)–U(vi) sulfate systems.

where the quantities in bracket represent concentrations and a positive value of ε indicates enrichment of the heavier isotope in the AY molecule compared with AX. Note that, in the case of the equilibrium shown in eqn (1), ε will equal $K - 1$, where K is the equilibrium constant. Because K for an

isotope exchange reaction is typically close to 1, ε can be approximated as $\ln K$. The latter may be expressed as the sum of two major terms, these being the nuclear mass term, $\ln K_{\text{nm}}$,²¹ and nuclear volume term, $\ln K_{\text{nv}}$.^{22–26} This expression is



$$\varepsilon = K - 1 \cong \ln K \approx \ln K_{\text{nm}} + \ln K_{\text{nv}} \quad (3)$$

$\ln K_{\text{nm}}$ can, in turn, be calculated as the difference of the logarithms of the reduced partition function ratio (β) between AX and AY, as

$$\ln K_{\text{nm}} = \ln \beta(\text{AY}) - \ln \beta(\text{AX}), \quad (4)$$

where $\ln \beta$ can be defined based on the harmonic vibrational frequencies (ν_i) as

$$\ln \beta = \ln \left[\prod_i \frac{u_i}{u'_i} \frac{e^{-u_i/2} / (1 - e^{-u_i})}{e^{-u'_i/2} / (1 - e^{-u'_i})} \right]; \quad u_i = \frac{h\nu_i}{k_B T} \quad (5)$$

Here, h is the Planck constant, k_B is the Boltzmann constant, T is the absolute temperature in degrees Kelvin and a prime symbol denotes values for the light isotopologues.

In contrast, $\ln K_{\text{nv}}$ is calculated based on the electronic energy difference between the two isotopologues (ΔE_{nv}) using finite-size nuclear charges. The associated equation is

$$\ln K_{\text{nv}} = [\Delta E_{\text{nv}}(\text{AX}) - \Delta E_{\text{nv}}(\text{AY})] / k_B T = [\{E(\text{AX}) - E(\text{A}'\text{X})\} - \{E(\text{AY}) - E(\text{A}'\text{Y})\}] / k_B T, \quad (6)$$

where the prime symbols indicate values for the light isotopologues (as in eqn (5)). Substituting 3.17×10^{-6} (E_{h}/K) for k_B and 298 K for T in eqn (6) demonstrates that a 1‰ change in $\ln K_{\text{nv}}$ will result from an electronic energy variance of approximately $1 \times 10^{-6} E_{\text{h}}$. Because of the significant effect of this minute energy change on $\ln K_{\text{nv}}$, it is crucial to exercise caution to avoid numerical errors when optimizing electronic energies.

Computational details

The ground state geometry optimizations and vibrational analyses associated with the $\ln K_{\text{nm}}$ calculations were conducted using the Gaussian16 software package.⁵⁸ The initial structures of the perchlorate and carboxylate ligands used for geometry optimization were taken from the database generated by the PubChemQC project.^{59,60} The DFT approach with the B3LYP functional, which combines Becke's three-parameter non-local hybrid exchange potential with Lee–Yang–Parr non-local functionals,^{61–63} was employed. The electronic structure of the U atom was described by utilizing the Stuttgart small-core relativistic effective core potential (RECP) referred to as ECP60MWB⁶⁴ together with a contracted Gaussian basis set [10s, 9p, 5d, 4f, 3g].⁶⁵ In the case of calculations involving Br, the ECP28MWB⁶⁶ RECP was used along with a contracted Gaussian basis set [4s, 4p, 3d, 2f]⁶⁷ while the 6-31++G(d,p) basis set was employed for all other atoms.^{68–76} When employing the polarizable continuum model (PCM)⁷⁷ during geometry optimization calculations, convergence was not achieved for certain molecules. Hence, this work reports $\ln K_{\text{nv}}$ and $\ln K_{\text{nm}}$ values only for optimized gas phase geometries for all molecules. In the case of those molecules for which geometry optimization was possible regardless of whether or not the PCM was used, employing this model did not greatly affect the

$\ln K_{\text{nv}}$ or $\ln K_{\text{nm}}$ values that were obtained, as shown in Section S1 in the ESI.†

Electronic energy calculations were performed using the X2C relativistic Hamiltonian^{38,40–42} implemented in the DIRAC16 software package^{78,79} with the HF and DFT formalisms to obtain $\ln K_{\text{nv}}$. In the case of the DFT calculations, we employed the B3LYP hybrid exchange–correlation functional.^{61–63} In a previous study by the authors,⁴³ the Perdew–Burke–Ernzerhof (PBE) approach⁸⁰ and Coulomb-attenuating method (CAM)-B3LYP⁸¹ were evaluated and minimal differences from the B3LYP results were observed for the majority of molecules. However, unlike the B3LYP method, these functionals produced unusual $\ln K_{\text{nv}}$ values for some large molecules. Consequently, the present work used only the B3LYP functional in DFT calculations. Restricted HF calculations were performed for the U(vi) closed-shell systems whereas calculations involving U(iv) open-shell systems employed the average-of-configuration (AOC) method in which the energy was averaged over all possible configurations in the active space formed by open-shell molecular orbitals (MOs).⁸² Six spinors were selected for the AOC method, primarily comprising U 5f_{5/2} as the open-shell. In contrast, during the DFT calculations, fractional occupation of the open-shell MOs was employed while calculating the energy for a configuration in which the occupation number of each open-shell MO was the same fractional value.

In the case of small highly symmetric molecules, $\ln K_{\text{nv}}$ was computed using the advanced electron correlation methods MP2,^{48,52} CCSD, CCSD(T)^{49,50} or FSCCD⁵³ implemented in the DIRAC21 software package.^{78,83} MP2 calculations were conducted only for the closed shell U(vi) species because the MP2 program implemented in DIRAC21 assumed canonical orbitals, which may not have been correct for open-shell calculations. As an alternative, the CASPT2^{54–56} approach was used for calculations concerning open-shell U(iv), using an active space defined by two electrons in six 5f_{5/2} spinors and with a reference function based on the CASCI technique. The effect of expanding the active space was assessed by performing RASCI-RASPT2 calculations employing different RAS1–RAS3 spaces, as detailed in subsequent sections and in the ESI.† Improved virtual orbital (IVO) methods^{84,85} were also introduced in conjunction with the CAS/RAS calculations. Because many MOs were nearly degenerate relative to the highest occupied MO (HOMO) and lowest unoccupied MO (LUMO) in UO₂Br₄^{2–} and in UBr₄, RASPT2 calculations were not carried out for these molecules. The MOs extending from the occupied orbital comprising the U 6s orbital to the virtual orbital below the orbital energy of 20.0 E_{h} were considered in these electron correlation calculations, based on a prior survey of the virtual cut-off threshold energy values as described in Section S2 in the ESI.† Those MOs were determined at the HF or HF(AOC) level. Specifically, in the case of the FSCCD calculations for U(iv) species, the electronic state of UX₄²⁺ was initially calculated as a closed shell system by removing two electrons from the 5f orbitals. Following this, two electrons were added to seven MOs (*i.e.*, fourteen spinors) ranging from the LUMO to the LUMO+6 to form the Fock



space. The basis sets consisted of Dyal's double-zeta basis set (Dyall.cv2z) for U,⁸⁶ Dyall.cv2z with the diffuse functions (Dyall.lacv2z) for Br^{87–89} and 6-31++G(d,p) for the remaining atoms.^{68–76} Note that the effect of the basis set on the $\ln K_{\text{nv}}$ value is described in Section S3 in the ESI.† A Gaussian-type finite nucleus model⁹⁰ incorporating root-mean-square nuclear charge radii of 5.8571 fm and 5.8337 fm for ²³⁸U and ²³⁵U, respectively,⁹¹ was utilized.

In the case of the HF and B3LYP calculations, the MOs were optimized solely for ²³⁸U isotopologues and then used to determine the electronic energy values for the ²³⁵U isotopologues without self-consistent-field (SCF) iterations, which was considered a suitable approximation.^{43,92–94} However, utilizing the identical MOs for the MP2, CASPT2 and RASPT2 calculations produced $\ln K_{\text{nv}}$ values nearly identical to those obtained from the HF, CASCI and RASCI calculations, respectively. This outcome is attributed to the dependence of the second-order correlation energy on both the two-electron integrals and the differences in orbital energies. In the case that the same MOs are used for two different isotopologues, the two-electron integrals will be unaffected by the nuclear volume difference whereas the orbital energies will be modified. However, this effect of the nuclear volume difference on the two orbital energies may not be significant. Hence, employing the MP2 method should have only a minimal effect on $\ln K_{\text{nv}}$. Consequently, orbital relaxation effects had a greater impact in these calculations. To address this phenomenon, the MOs for both isotopologues were optimized through high-level theory calculations as well as in the HF and B3LYP calculations for comparison.

A temperature of 298 K was adopted for all calculations, unless otherwise specified. The OS of U was confirmed from the Mulliken spin density⁹⁵ in the RECP-B3LYP calculations and the Mulliken population⁹⁵ of U 5f orbitals in the open-shell MOs during the X2C calculations, following the methodology employed in a previous study.⁴³ The compositions of molecular species under the experimental conditions of the sulfate U(vi)–U(vi) system²⁰ were predicted by conducting speciation simulations using the Visual MINTEQ 3.1 software package.⁹⁶ These simulations assumed a pH of 0.456 and a temperature of 308 K as reported in the literature.²⁰ This pH corresponded to an H⁺ concentration of 0.35 M. The concentrations of UO₂²⁺, U⁴⁺ and SO₄^{2–} were set to 0.1, 0.1 and 0.175 M, respectively. In contrast, calculations involving the chloride system employed the proportions of molecular species reported by Wang *et al.*, as predicted using the MINEQL software package.¹⁹

Results and discussion

(1) Impact of electron correlation on $\ln K_{\text{nv}}$ for small, highly symmetrical molecules

(a) **General overview of U(vi)–U(vi) and U(iv)–U(vi) systems.** The effect of electron correlation on U isotope fractionation was explored by computing $\ln K_{\text{nv}}$ values using various correlation methods within the X2C Hamiltonian framework. As a

consequence of computational limitations, this work focused on the small, highly symmetrical molecules UO₂X₄^{2–} (X[–] = F[–], Cl[–], Br[–]), UO₂(CO₃)₂^{2–}, UO₂(NO₃)₂ and UO₂(H₂O)₄²⁺ for U(vi) and UX₄ (X[–] = F[–], Cl[–], Br[–]) for U(iv) (Fig. 1). A U(iv) state in which two electrons occupied U 5f as an open-shell structure was successfully obtained, as confirmed by spin density analysis and the occupation numbers of U 5f orbitals (see Section S4 in ESI†). The $\ln K_{\text{nv}}$ values obtained for U(vi)–U(vi) and U(iv)–U(vi) are summarized in Tables 1 and 2, respectively. The isotope fractionations of U(vi)–U(vi) species occur *via* ligand exchange reactions without changing the main uranyl structure (O=U=O²⁺). In contrast, isotope fractionation of U(iv)–U(vi) involves the exchange of isotopes between different OSs such that the magnitude of $\ln K_{\text{nv}}$ for a U(iv)–U(vi) system is generally larger than for a U(vi)–U(vi) system.

(b) **Dependence of $\ln K_{\text{nv}}$ on molecular orbitals in U(vi)–U(vi) systems.** From Table 1 it is apparent that the two $\ln K_{\text{nv}}$ values obtained using optimized MOs for a single isotopologue (²³⁸U) and for individual isotopologues (²³⁵U and ²³⁸U) were nearly identical at the HF and B3LYP levels, consistent with prior reports.^{93,94} Using the MP2 method while employing identical MOs produced results close to those obtained from the HF technique. As discussed in the preceding section, using individual MOs yielded outcomes similar to those from the CCSD and CCSD(T) methods. The CCSD and CCSD(T) results demonstrate that switching between identical MOs and individual MOs has a minimal effect on $\ln K_{\text{nv}}$, suggesting that orbital rotation effects are appropriately incorporated through single excitation operators in the exponential ansatz.

(c) **Summary of results for U(vi)–U(vi) systems.** The overall results for the U(vi)–U(vi) system as shown in Fig. 2 and Table 1 establish that the MP2, CCSD and CCSD(T) methods all yield similar $\ln K_{\text{nv}}$ values if individual MOs are used in the MP2 calculations. In all cases, CCSD(T) values are intermediate between those derived from the HF and B3LYP methods. Consequently, it appears that the HF technique typically provides an overestimation whereas B3LYP calculations

Table 1 $\ln K_{\text{nv}}$ values for the U(vi)–U(vi) systems obtained using the HF, B3LYP, MP2, CCSD and CCSD(T) methods. The upper part of the table displays results obtained using MOs optimized for ²³⁸U for both isotopologues, whereas the lower part presents the results obtained using individually optimized MOs for ²³⁵U and ²³⁸U. All values are referenced to UO₂(H₂O)₄²⁺ and are presented in units of permil (‰)

MO optimization only for ²³⁸ U	HF	B3LYP	MP2	CCSD	CCSD(T)
UO ₂ F ₄ ^{2–}	1.31	0.86	1.30	1.18	1.12
UO ₂ (CO ₃) ₂ ^{2–}	0.90	0.39	0.90	0.71	0.65
UO ₂ Cl ₄ ^{2–}	0.66	0.34	0.66	0.59	0.56
UO ₂ Br ₄ ^{2–}	0.56	0.24	0.57	0.50	0.48
UO ₂ (NO ₃) ₂	0.06	–0.14	0.07	0.00	–0.01
Individual MO optimizations	HF	B3LYP	MP2	CCSD	CCSD(T)
UO ₂ F ₄ ^{2–}	1.31	0.86	1.14	1.20	1.14
UO ₂ (CO ₃) ₂ ^{2–}	0.90	0.39	0.68	0.75	0.67
UO ₂ Cl ₄ ^{2–}	0.66	0.34	0.55	0.61	0.58
UO ₂ Br ₄ ^{2–}	0.55	0.23	0.46	0.52	0.50
UO ₂ (NO ₃) ₂	0.05	–0.14	–0.01	0.02	0.00



Table 2 $\ln K_{\text{nv}}$ values for U(IV)–U(VI) systems obtained using the HF(AOC), B3LYP, CCSD, CCSD(T), FSCCSD, CASCI, CASPT2, RASCI and RASPT2 methods. The upper part of the table displays the results obtained using MOs optimized for ^{238}U for both isotopologues whereas the lower part presents the results obtained using individually optimized MOs for ^{235}U and ^{238}U . All values are expressed in units of ‰

MO optimization only for ^{238}U	HF(AOC)	B3LYP	CCSD	CCSD(T)	FSCCSD	CASCI	CASPT2	RASCI	RASPT2
$\text{UO}_2\text{F}_4^{2-}-\text{UF}_4$	3.64	2.26	2.98	2.79	2.49	3.76 ^b	3.70 ^b	3.76 ^c	3.69 ^c
$\text{UO}_2\text{Cl}_4^{2-}-\text{UCl}_4$	2.71	1.82	2.04	1.91	1.39	2.78 ^b	2.73 ^b	2.77 ^c	2.75 ^c
$\text{UO}_2\text{Br}_4^{2-}-\text{UBr}_4$	2.54	1.77	1.87	1.75	N/A ^a	2.60 ^b	2.53 ^b	—	—
Individual MO optimizations	HF(AOC)	B3LYP	CCSD	CCSD(T)	FSCCSD	CASCI	CASPT2	RASCI	RASPT2
$\text{UO}_2\text{F}_4^{2-}-\text{UF}_4$	3.64	2.27	3.08	2.94	1.93	3.85 ^b	2.73 ^b	3.80 ^c	2.68 ^c
$\text{UO}_2\text{Cl}_4^{2-}-\text{UCl}_4$	2.72	1.83	2.14	2.01	1.85	2.86 ^b	1.67 ^b	2.84 ^c	1.66 ^c
$\text{UO}_2\text{Br}_4^{2-}-\text{UBr}_4$	2.79	1.83	1.97	1.82	N/A ^a	2.67 ^b	1.58 ^b	—	—

^a Because the FSCCSD calculations for UBr_4 did not converge, calculated values are not provided. ^b In the case of the CASCI and CASPT2 calculations, CAS(2e,10s) was used for $\text{UO}_2\text{F}_4^{2-}$ and $\text{UO}_2\text{Cl}_4^{2-}$ whereas CAS(2e,6s) was used for UF_4 , UCl_4 and UBr_4 . Here, CAS(2e,6s) indicates that the CAS consisted of two electrons in six spinors. However, due to the degeneracy of a large number of the MOs relative to the LUMO of $\text{UO}_2\text{Br}_4^{2-}$, the MP2 energy was instead used in calculations involving this molecule. ^c The RAS1, RAS2 and RAS3 calculations used 12, 0 and 8 spinors for $\text{UO}_2\text{F}_4^{2-}$, respectively, and 4, 6 and 8 for UF_4 , respectively. Similarly, for $\text{UO}_2\text{Cl}_4^{2-}$, these values were 8, 0 and 8 while the values for UCl_4 were 4, 6 and 8, respectively. The numbers of active electrons were 12, 6, 8 and 6 for $\text{UO}_2\text{F}_4^{2-}$, UF_4 , $\text{UO}_2\text{Cl}_4^{2-}$ and UCl_4 , respectively.

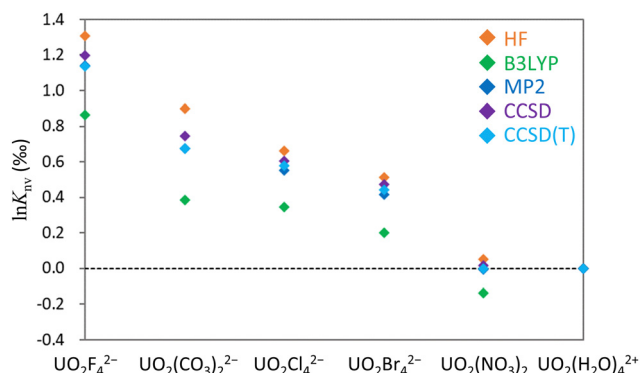


Fig. 2 $\ln K_{\text{nv}}$ values for the U(VI)–U(VI) system generated using the HF, B3LYP, MP2, CCSD and CCSD(T) methods. The horizontal axis indicates the molecule under consideration while the vertical axis shows $\ln K_{\text{nv}}$ values in permil (‰). $\text{UO}_2(\text{H}_2\text{O})_4^{2+}$ served as the reference for all calculations.

underestimate the values relative to those produced by the CCSD(T) method. The MP2 technique is evidently a cost-effective approach to predicting $\ln K_{\text{nv}}$ for closed-shell U(VI) states, although it remains computationally intensive in the case of calculations involving asymmetric medium-sized molecules. In such cases, it is likely that the true theoretical value lies between the outcomes of the HF and B3LYP calculations. The largest difference between the HF and CCSD(T) results of 0.23‰ was observed for calculations involving $\text{UO}_2(\text{CO}_3)_2^{2-}$ and $\text{UO}_2(\text{H}_2\text{O})_4^{2+}$. This outcome demonstrates that electron correlation can affect the $\ln K_{\text{nv}}$ of a U(VI)–U(VI) system by approximately 0.2‰.

(d) Dependence of $\ln K_{\text{nv}}$ on molecular orbitals in U(IV)–U(VI) systems. In calculations involving the U(IV)–U(VI) systems shown in Table 2, the use of either identical MOs or individual MOs did not affect the $\ln K_{\text{nv}}$ values at the HF, B3LYP, CCSD and CCSD(T) levels, similar to the results obtained for the U(VI)–U(VI) system that are shown in Table 1. At the MP2, CASPT2 and RASPT2 levels, employing identical MOs produced results

similar to those generated using the HF, CASCI and RASCI methods, respectively, as discussed in the preceding section. Hence, it is important to employ individual MOs so as to incorporate electron correlation effects when using these perturbation methods. In addition, using identical MOs gave quite different $\ln K_{\text{nv}}$ values from those produced with individual MOs at the FSCCSD levels, suggesting that orbital rotation effects may not be sufficient to account for the relaxation of MOs for different nuclear radii in FSCCSD calculations.

(e) Numerical instability and uncertainty in multireference calculations for U(IV)–U(VI) Systems. To accurately describe $\ln K_{\text{nv}}$ using individual MOs, it is crucial to obtain two sets of subtly distinct MOs solely as a consequence of differences in the nuclear volume. However, optimizing individual MOs through different SCF procedures can lead to more significant disparities in virtual MOs compared with the differences resulting solely from nuclear volume variations. This phenomenon can, in turn, produce numerical instability when applying the CASPT2, RASPT2 and FSCCSD methods to describe $\ln K_{\text{nv}}$. The appearance of such instability may be confirmed by calculating additional $\ln K_{\text{nv}}$ values using different nuclear radii and assessing the linearity of the correlation between $\ln K_{\text{nv}}$ and nuclear radius. Particularly in the case of the CASPT2 approach, significant instabilities appeared when the CASCI reference states were completely degenerate within the same irreducible representation. Calculations involving UX_4 molecules as U(IV) species generated three completely degenerate states in the ground state at the CASCI level. One such state had A symmetry while the others had B symmetry in the case that the C_2 double group was used as the Abelian group. In this scenario, a unique set of CI coefficients for the CASCI process could not be determined during the matrix diagonalization for each nuclear radius calculation. This may have produced small numerical errors in the CASPT2 energies (on the order of 10^{-6} – 10^{-7} E_{h}) that prevented a precise comparison of the energy values associated with the different nuclear radii, which is a prerequisite for the calculation of $\ln K_{\text{nv}}$. Interestingly, the CASPT2 calculations for



the non-degenerate state with A symmetry did not indicate numerical instability, and so the data related to the ground state of UX_4 are considered reliable. Employing the RASCI/RASPT2 method was shown to remove the degeneracy found in the CASCI results although greater numerical instability appeared in the RASPT2 results obtained without using the IVO technique. Even in the case that the IVO process was combined with the RASPT2 method, nonlinear trends with respect to the nuclear radii values sometimes emerged, depending on the choice of RAS. A more detailed discussion concerning the effect of the RAS technique, numerical instability and other factors is provided in Section S5 in the ESI†. It should be noted that the RASPT2 data in Table 2 do not show such numerical instability. The UCl_4 calculations using the FSCCD method with independent MOs generated $\ln K_{nv}$ values that did not exhibit instability, although the ground state was obtained as a non-degenerate system. Similarly, the CCSD and CCSD(T) calculations for A and B symmetries did not show any degeneration of the ground state (see Section S6 in the ESI†).

(f) Summary of results for $U(IV)$ – $U(VI)$ systems. As described earlier, UX_4 has an open-shell ground state in which two electrons occupy six degenerate $5f_{5/2}$ spinors. The MOs optimized using the HF(AOC) method were employed for all the post-Hartree–Fock calculations except for those involving FSCCD calculations. The HF(AOC) and CASCI approaches provided similar $\ln K_{nv}$ values, suggesting that the treatment of open-shell MOs *via* the AOC or CASCI procedures does not significantly affect $\ln K_{nv}$. Analogous to the $U(VI)$ – $U(VI)$ results, the $\ln K_{nv}$ values obtained through the CCSD and CCSD(T) methods were intermediate between those obtained from HF and B3LYP calculations. The FSCCD, CASPT2 and RASPT2 methods all produced comparable $\ln K_{nv}$ values that were either equivalent to or less than the values obtained from B3LYP calculations.

(g) Comparative analysis of calculated $\ln K_{nv}$ with experimental data in the $UO_2Cl_4^{2-}$ – UCl_4 system (for reference only). The molecular models used for $UO_2Cl_4^{2-}$ and UCl_4 in the present work may align with those reported by Fujii *et al.* based on experiments employing high HCl concentrations.¹⁸ Under these HCl-rich conditions, hexavalent uranyl can potentially coordinate with three or four Cl^- ions and water molecules whereas tetravalent uranium forms neutral UCl_4 and also undergoes coordination with water. Even so, attempts to simulate these species using Visual MINTEQ 3.1 did not converge, likely because of the very high HCl concentration used in the experimental work. Below, the present results are compared with the experimental data published by Fujii *et al.*, although it should be noted that uncertainty regarding the molecular structures and a reported large experimental error in ε ($\sim 20\%$) may make accurate comparisons challenging.

The $\ln K_{nv}$ value when converted to 298 K using the temperature-dependent equation reported by Fujii *et al.* was found to be 2.32‰. It was also evident that the HF(AOC) and CASCI methods tended to overestimate the experimental $\ln K_{nv}$ while the B3LYP technique provided an underestimate. Theoretically, the multireference electron correlation methods (that

is, the FSCCD, CASPT2 and RASPT2 methods) have the potential to precisely describe the electronic state of $U(IV)$, which comprises a degenerate open-shell system. However, these methods collectively underestimated the experimental value. The FSCCD approach might have yielded a smaller $\ln K_{nv}$ because of the lower occupation number of U 5f orbitals in the MOs specified as the Fock space for UCl_4^{2+} (see Section S7 in the ESI†). This lower occupation number could potentially reduce the shielding effect of open-shell 5f electrons on valence s orbitals (that is, those in 6s and 7s orbitals). The numerical instability associated with certain computational settings may impede the CASPT2 and RASPT2 methods from accurately estimating the electronic energy values required for $\ln K_{nv}$ calculations. Even though the CCSD and CCSD(T) approaches are generally not suitable for degenerate or open-shell systems, the present calculations exhibit moderate values of single or double-excitation amplitudes (see Section S8 in the ESI†), suggesting the absence of serious collapse of the numerical simulations. However, it remains unclear from this analysis whether the theoretically correct electronic state was obtained. Despite this uncertainty, the CCSD and CCSD(T) methods yielded the $\ln K_{nv}$ values closest to the experimental value reported by Fujii *et al.* when compared with the results from the other methodologies.

(2) Comparison between experimental and theoretical ε obtained using the HF and B3LYP methods

(a) $U(VI)$ – $U(VI)$ ligand exchange systems. $\ln K_{nv}$, $\ln K_{nm}$ and ε values for $U(VI)$ species with anionic ligands such as carbonate, malate, lactate, glycolate, acetate, chloride and perchlorate were calculated and compared with existing experimental ε values for $U(VI)$ – $U(VI)$ systems.^{15,16} In these calculations, $UO_2(H_2O)_3(SO_3-C_6H_4)_2C_5H_{10}$, which has a hydrated uranyl structure when attached to a cation exchange resin (Fig. 1), was used as a reference for calculations of ε . In the case of the nonsymmetric medium-size systems, only the HF and DFT methods have sufficiently low computational costs to be employed for $\ln K_{nv}$ calculations. Because the $\ln K_{nm}$ values were solely derived from the RECP-B3LYP technique, these values were used uniformly in all ε calculations, regardless of whether $\ln K_{nv}$ was obtained from X2C-HF or X2C-B3LYP calculations. Given the unknown coordination numbers of the ligands in the actual experiments, all conceivable patterns of coordination numbers were used in these computations. The resulting data are summarized in Table 3 and plotted in Fig. 3.

From Table 3, it is evident that $\ln K_{nv}$ exceeded $\ln K_{nm}$ for both the HF and B3LYP calculations for most species. This finding suggests that differences in electronic states, not vibrational levels, make the primary contribution to isotope fractionation, even in ligand exchange systems. Even among those species having identical ligands, the calculated ε values were greatly affected by the coordination number of the anionic ligand. As an example, the ranges of ε values for carbonate species were 0.44‰ and 0.46‰ for the HF and B3LYP methods.

Fig. 3 provides the ranges of ε values obtained from the HF and B3LYP computations, which reflect the wide variety of



Table 3 $\ln K_{nv}$, $\ln K_{nm}$ and ε values for the U(vi)–U(vi) systems. The values of $\ln K_{nv}$ calculated using the X2C-HF and X2C-B3LYP techniques are shown separately in the HF and B3LYP columns, respectively. The Expt. column presents the experimental ε values for each species.^{42,43} All values are in units of ‰

	Species	$\ln K_{nv}$		$\ln K_{nm}$	ε		
		HF	B3LYP		HF	B3LYP	Expt.
Carbonate	$\text{UO}_2(\text{CO}_3)(\text{H}_2\text{O})_3$	0.66	0.17	−0.04	0.62	0.13	0.34
	$\text{UO}_2(\text{CO}_3)_2(\text{H}_2\text{O})_2^{2-}$	0.86	0.29	−0.03	0.83	0.26	
	$\text{UO}_2(\text{CO}_3)_3^{4-}$	0.94	0.47	0.12	1.05	0.58	
Malate	$\text{UO}_2(\text{mal})(\text{H}_2\text{O})_3$	0.66	0.23	−0.08	0.58	0.15	0.22
	$\text{UO}_2(\text{mal})_2(\text{H}_2\text{O})_2^{2-}$	0.75	0.34	−0.07	0.68	0.27	
	$(\text{UO}_2)_2(\text{mal})_2(\text{H}_2\text{O})_6$ U1	0.68	0.24	−0.08	0.61	0.16	
	$(\text{UO}_2)_2(\text{mal})_2(\text{H}_2\text{O})_6$ U2	0.59	0.18	−0.08	0.51	0.10	
Lactate	L- $\text{UO}_2(\text{lac})(\text{H}_2\text{O})_3^+$	0.40	0.11	−0.08	0.32	0.03	0.14
	D- $\text{UO}_2(\text{lac})(\text{H}_2\text{O})_3^+$	0.43	0.05	−0.08	0.36	−0.03	
	L- $\text{UO}_2(\text{lac})_2(\text{H}_2\text{O})_2$	0.49	0.18	−0.09	0.40	0.09	
	D- $\text{UO}_2(\text{lac})_2(\text{H}_2\text{O})_2$	0.64	0.36	−0.09	0.55	0.27	
	L- $\text{UO}_2(\text{lac})_3^-$	0.51	0.30	−0.02	0.49	0.28	
	D- $\text{UO}_2(\text{lac})_3^-$	0.57	0.23	−0.02	0.55	0.21	
Glycolate	$\text{UO}_2(\text{gly})(\text{H}_2\text{O})_3^+$	0.42	0.08	−0.08	0.35	0.00	0.10
	$\text{UO}_2(\text{gly})_2(\text{H}_2\text{O})_2$	0.64	0.13	−0.09	0.54	0.03	
	$\text{UO}_2(\text{gly})_3^-$	0.63	0.36	−0.02	0.61	0.34	
Acetate	$\text{UO}_2(\text{ace})(\text{H}_2\text{O})_3^+$	0.42	0.21	−0.08	0.34	0.13	0.09
	$\text{UO}_2(\text{ace})_2(\text{H}_2\text{O})_2$	0.54	0.20	−0.10	0.44	0.11	
	$\text{UO}_2(\text{ace})_3^-$	0.67	0.32	−0.03	0.64	0.29	
Chloride	$\text{UO}_2\text{Cl}(\text{H}_2\text{O})_4^+$	0.34	−0.04	−0.02	0.32	−0.06	0.03
	$\text{UO}_2\text{Cl}_2(\text{H}_2\text{O})_3$	0.39	0.06	0.00	0.39	0.06	
	$\text{UO}_2\text{Cl}_3(\text{H}_2\text{O})_2^-$	0.46	0.10	0.06	0.52	0.16	
	$\text{UO}_2\text{Cl}_4^{2-}$	0.63	0.19	0.13	0.76	0.32	
Perchlorate	$\text{UO}_2(\text{ClO}_4)(\text{H}_2\text{O})_3^+$	0.20	−0.05	−0.10	0.11	−0.14	0.00
	$\text{UO}_2(\text{ClO}_4)_2(\text{H}_2\text{O})_2$	−0.08	−0.14	−0.09	−0.17	−0.23	
	$\text{UO}_2(\text{ClO}_4)_3^-$	0.02	−0.17	−0.05	−0.03	−0.22	
Resin-bound aqueous	$\text{UO}_2(\text{H}_2\text{O})_3(\text{SO}_3\text{-C}_6\text{H}_4)_2\text{C}_5\text{H}_{10}$	0.00	0.00	0.00	0.00	0.00	0.00

coordination numbers for the various ligands. The $y = x$ line represents an identical match between computational and experimental data. In this figure, the area occupied by the B3LYP results aligns more closely with the experimental line compared with the HF region. The HF values also exhibit overestimation similar to that described in the previous section regarding electron correlations calculations, in which the HF results were higher than the CCSD(T) values.

Because the B3LYP values for certain coordination numbers were close to the experimental data, one might expect that such information could be used to predict coordination numbers associated with experimental work. However, the precision of the present ε calculations did not exceed 0.01‰ (corresponding to an electronic energy accuracy of $10^{-8} E_h$), rendering the calculated data inadequate for such predictive purposes. Furthermore, achieving convergence to the exact global minimum of electronic states becomes increasingly challenging as molecules grow in size. As an example, in the case of the lactate calculations, there is a deviation of 0.18‰ in the B3LYP results (0.15‰ in the HF results) for the L- and D-enantiomers, which ideally should yield identical values. This discrepancy implies potential convergence to local minima in the SCF for either the L- or D-enantiomer, or even both. Notably, the ε values for the

U(vi)–U(vi) systems are smaller than those for the U(iv)–U(vi) systems involving changes in OS. Hence, it should be noted that U(vi)–U(vi) isotopic fractionation coefficients computed through the present *ab initio* methods might be less accurate.

Intriguingly, previous experimental studies have indicated robust negative linear correlations between the U=O antisymmetric stretching frequency, ν_3 , and ε .^{15,16} The plot in Fig. 4 includes calculated ν_3 value generated using the RECP-B3LYP method along with ε acquired from B3LYP or HF calculations and experimental data. The calculated results qualitatively replicate the experimental trend and demonstrate a negative linear correlation between ν_3 and ε . However, the associated R^2 values are 0.78 (B3LYP), 0.74 (HF) and 0.99 (experimental), confirming that the calculated results are more scattered than the experimental data. This scattering can possibly be attributed to the use of the RECP-B3LYP method to calculate the vibrational frequencies, whereas $\ln K_{nv}$ was determined with the X2C Hamiltonian. As previously noted, achieving convergence to the global minimum of the electronic state becomes increasingly challenging for larger molecules in X2C relativistic calculations. Although the R^2 value for the B3LYP results was marginally better than that for the HF values, the former method notably approached the experimental values more



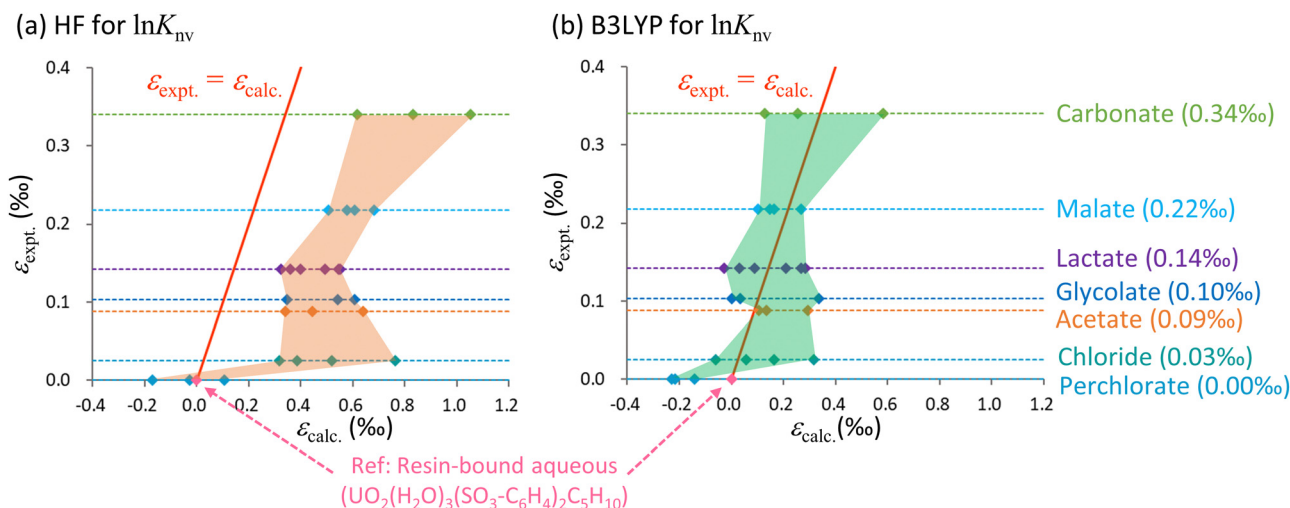


Fig. 3 Calculated ε values based on $\ln K_{nv}$ obtained using the (a) HF and (b) B3LYP methods along with experimental data for the $U(vi)$ – $U(vi)$ system. The horizontal axis shows the calculated values relative to $UO_2(H_2O)_3(SO_3-C_6H_4)_2C_5H_{10}$ while the vertical axis shows the experimental values relative to the aqueous UO_2^{2+} complex bound to the cation exchange resin. The red solid line indicates the scenario in which the calculated and experimental values are equal. The areas bounded by the values calculated using the HF and B3LYP methods are shaded orange and green, respectively. The dotted lines parallel to the horizontal axis represent the experimental values for each species as described on the right while the quantities in parentheses indicate the experimental data. The numerical data are also summarized in Table 3.

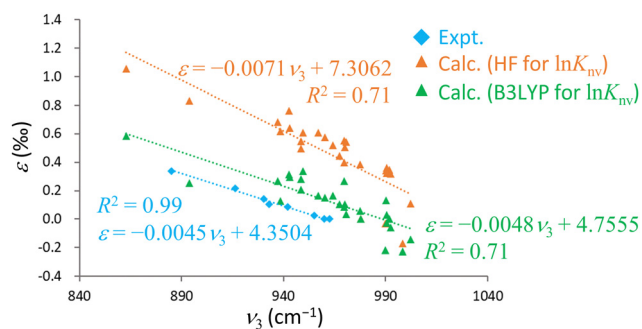


Fig. 4 Relationships between ν_3 and ε . The horizontal axis shows ν_3 in units of cm^{-1} while the vertical axis shows ε in units of ‰. The dotted lines are linear regressions and R^2 is the coefficient of determination in each case.

closely in terms of both slope and intercept in the ν_3 – ε plot. This outcome demonstrates the remarkable reproducibility that can be obtained from this technique, not just with regard to direct comparisons with experimental ε values but also in terms of the correlation between ν_3 and ε . Hence it is evident that the B3LYP method effectively incorporates the electron correlation effect for the $U(vi)$ – $U(vi)$ system.

(b) $U(iv)$ – $U(vi)$ systems in hydrochloric and sulfuric acid media. HF and B3LYP calculations were carried out to determine $\ln K_{nv}$, $\ln K_{nm}$ and ε for the $U(iv)$ – $U(vi)$ systems in hydrochloric and sulfuric acid media, aligning with the experiments conducted by Wang *et al.* (who determined an ε of 1.65‰ at 298 K)¹⁹ and Florence *et al.* (ε = 1.3‰ at 308 K).²⁰ In the recent HCl media experimentation by Wang *et al.*, the experimental error (0.16‰, 2σ) was approximately one-fourth the magnitude of the error in the experiments using sulfuric acid performed by

Florence (0.8‰, 2σ). Table 4 summarizes a plausible list of chemical species present in these experiments and the relative percentages of each. The data for the HCl system were sourced from a paper written by Wang *et al.*¹⁹ while those for the sulfuric system were determined from our own simulations. Based on coordinating the appropriate number of water molecules and optimizing geometries using the RECP-B3LYP method, $\ln K_{nv}$ and $\ln K_{nm}$ were calculated for each species, employing $U(H_2O)_9^{4+}$ as a reference. The final ε values were derived through weighted averaging based on the proportion of each species (refer to Table 4). In both the chloride and sulfate systems, the primary $U(vi)$ species was $UO_2(H_2O)_5^{2+}$. In the case of $U(iv)$, the primary species differed between the chlorine-coordinated and sulfate-coordinated configurations but exhibited similar ε values, resulting in similar calculated ε values for the chloride and sulfate systems. Two previous experiments showed a 0.35‰ difference in ε but agreed with each other within the associated experimental errors. The experimental ε values can be seen to fall between the ε values obtained by the HF and B3LYP methods for both the chloride and sulfate systems. Hence, the HF and B3LYP methods tended to overestimate and underestimate the experimental values, respectively. These trends are consistent with the observations discussed in the previous section concerning the effect of electron correlation on the $U(vi)$ – $U(vi)$ system based on a comparison with the CCSD(T) method. However, the deviation between the experimental data and B3LYP results is notably more significant in the case of the $U(iv)$ – $U(vi)$ systems compared with the $U(vi)$ – $U(vi)$ systems, particularly in the case of the chloride species. Considering the successful use of the B3LYP method to describe the $U(vi)$ – $U(vi)$ systems, as discussed earlier, this discrepancy suggests that predicting the open-shell



Table 4 $\ln K_{nv}$, $\ln K_{nm}$ and ε values for the U(IV)–U(VI) chloride and sulfate systems along with the oxidation state (OS) and speciation for each. For $\ln K_{nv}$ and ε , separate entries are provided for cases in which $\ln K_{nv}$ was computed using the X2C–HF(AOC) and X2C–B3LYP methods in the HF(AOC) and B3LYP columns, respectively. The reference for both chloride and sulfate systems was $\text{U}(\text{H}_2\text{O})_9^{4+}$. The proportion of speciation is displayed as a percentage (%) while $\ln K_{nv}$, $\ln K_{nm}$ and ε are presented in units of ‰

Chloride	OS	Proportion of speciation (%)	$\ln K_{nv}$		$\ln K_{nm}$	ε		Averaged ε among speciation		Experimental ε	Temperature (K)
			HF(AOC)	B3LYP		HF(AOC)	B3LYP	HF(AOC)	B3LYP		
$\text{UO}_2(\text{H}_2\text{O})_5^{2+}$	VI	51.7	2.59	1.76	−1.03	1.56	0.73	1.73	0.89	1.65	298
$\text{UO}_2\text{Cl}(\text{H}_2\text{O})_4^+$	VI	48.3	2.88	1.83	−0.98	1.90	0.85				
$\text{UCl}(\text{H}_2\text{O})_8^{3+}$	IV	95.4	−0.02	−0.12	0.01	−0.01	−0.11				
$\text{U}(\text{H}_2\text{O})_9^{4+}$	IV	3.3	0.00	0.00	0.00	0.00	0.00				
$\text{U}(\text{OH})(\text{H}_2\text{O})_8^{3+}$	IV	1.3	−0.04	−0.01	−0.14	−0.17	−0.14				

Sulfate	OS	Proportion of speciation (%)	$\ln K_{nv}$		$\ln K_{nm}$	ε		Averaged ε among speciation		Experimental ε	Temperature (K)
			HF(AOC)	B3LYP		HF(AOC)	B3LYP	HF(AOC)	B3LYP		
$\text{UO}_2(\text{H}_2\text{O})_5^{2+}$	VI	87.8	2.50	1.70	−0.98	1.52	0.72	1.75	0.94	1.3	308
$\text{UO}_2(\text{SO}_4)(\text{H}_2\text{O})_3$	VI	11.9	3.01	1.87	−0.97	2.05	0.90				
$\text{U}(\text{SO}_4)(\text{H}_2\text{O})_7^{2+}$	IV	52.2	0.15	−0.17	−0.12	0.03	−0.28				
$\text{U}(\text{SO}_4)_2(\text{H}_2\text{O})_6$	IV	45.6	−0.31	0.00	−0.10	−0.41	−0.10				
$\text{U}(\text{H}_2\text{O})_9^{4+}$	IV	1.8	0.00	0.00	0.00	0.00	0.00				

electronic states of U(IV) is more challenging than predicting the closed-shell U(VI) states when employing DFT calculations.

Conclusions

To the best of our knowledge, this work is the first to elucidate the effect of electron correlation on U isotope fractionation using various methods (specifically, the HF, HF(AOC), B3LYP, MP2, CCSD, CCSD(T), FSCCSD, CASCI, RASCI, CASPT2 and RASPT2 methods) with the X2C relativistic Hamiltonian. With the exception of the HF and B3LYP techniques, the use of these electron correlation methods was restricted to the analysis of small, highly symmetric molecular models. In calculations involving closed-shell U(VI)–U(VI) systems, the MP2, CCSD and CCSD(T) methods yielded comparable $\ln K_{nv}$ values that were intermediate between those obtained from the HF and B3LYP methods. A comparison of the HF and CCSD(T) results indicated that electron correlation modified the $\ln K_{nv}$ value by approximately 0.2‰.

In the case of U(IV)–U(VI) systems, an assessment of the effect of electron correlation was more challenging because of the triplet-like open-shell structure of U(IV). The CCSD and CCSD(T) approaches yielded $\ln K_{nv}$ values in between those generated by HF and B3LYP calculations, similar to the U(VI)–U(VI) results, while the FSCCSD, CASPT2 and RASPT2 calculations yielded values similar to those obtained from the B3LYP method. Several issues arose in conjunction with the CASPT2, RASPT2 and FSCCSD calculations. Specifically, the CASPT2 and RASPT2 methods sometimes exhibited numerical instability with regard to the $\ln K_{nv}$ values while the FSCCSD technique showed insufficient orbital rotation effects and lower occupation of 5f spinors. Assuming the present calculated models involving chlorides are comparable to the experimental work of Fujii *et al.*, the CCSD and CCSD(T) calculations provided the best agreement with the experimental data. However, it remains

uncertain whether the CCSD and CCSD(T) methods can describe open-shell U(IV) electronic states correctly.

HF and B3LYP calculations were performed using more experimentally realistic molecular models, and the results were compared with previous experimental results. In the case of the U(VI)–U(VI) systems, the HF approach overestimated the experimental ε values^{15,16} while the B3LYP results showed good agreement. The linear correlation observed between the U=O antisymmetric stretching frequency ν_3 and ε in the experimental results¹⁶ was reproduced by our HF and B3LYP calculations and the B3LYP values showed better agreement with the experimental trend than those obtained from the HF method. Currently, the number and variety of DFT functionals implemented in the DIRAC software are limited. However, it would be interesting to explore whether using other functionals, such as double hybrid functionals, could further improve the results obtained with B3LYP.

In contrast, calculations involving U(IV)–U(VI) systems with chloride and sulfate indicated that the HF(AOC) technique provided results closer to the experimental values,^{19,20} whereas the B3LYP method underestimated these values. This outcome highlights the difficulty in accurately describing the open-shell electronic state of U(IV). In principle, DFT methods are not suitable for describing such open-shell degenerate states, although the results obtained may seem correct coincidentally. Multireference electron correlation methods should offer more promising approaches; however, their application to large real systems is currently hindered by computational resource limitations. It is worth noting that similar results were observed for small U(IV)–U(VI) models using B3LYP, CASPT2, and FSCCSD calculations. Assuming this trend extends to larger realistic models, CASPT2 and FSCCSD methods might also underestimate experimental values in these larger scenarios. To address these discrepancies more effectively in future studies, the following calculations may be crucial: (i) employing



CASSCF-CASPT2 calculations to improve molecular orbitals, rather than HF(AOC)-CASCI-CASPT2. (ii) Utilizing multi-reference configuration interaction (CI) calculations to surpass the accuracy provided by second-order perturbation theory. (iii) Directly computing large realistic models using massively parallelized multireference programs on supercomputers.

Overall, this work demonstrated that reliable calculation results could be obtained for closed-shell $U(VI)$ – $U(VI)$ systems although determining the electronic state of $U(IV)$ remains challenging. It is also difficult to determine if the $U(IV)$ electronic state has been accurately computed based on $\ln K_{nv}$ because the experimental data must be assumed to be reliable, and the molecular model must be credible. In addition, it may be difficult to accurately produce $\ln K_{nv}$ values based on electron correlation calculations because this requires an energy accuracy on the order of 10^{-6} – 10^{-7} E_h . To address this issue, future work will need to validate and verify the present calculations using other properties that are more readily comparable between the experimental and computational domains, such as spectroscopic properties or thermodynamic properties.

Author contributions

A. S., M. H. and M. A. designed the research; A. S. performed the work and analyzed the data; A. S., M. H. and M. A. wrote the paper.

Conflicts of interest

There are no conflicts to declare.

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