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Mechanism of lithium ion selectivity through membranes: a brief review

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The recycling and reuse of lithium resources from spent lithium-ion batteries have become a major research area to address the contradiction between limited resources and increasing market demand. Membrane separation, as a highly efficient and easy-to-operate process, has attracted more attention among various lithium recycling technologies. However, the complicated ion migration process results in an insufficient understanding of the lithium ion diffusion mechanism in membrane separation. In this review, recent research efforts on membrane separation technology for lithium recovery are summarized, with the mechanism of ion selectivity through membranes being emphasized. To illustrate the ion diffusion mechanism, the ion transportation process through a membrane is divided into 3 sequential stages: the entering of ions into the channel openings of the membrane, the diffusion of ions within the channels, and the returning of ions to the solution on the other side of the membrane. In each stage, the main factors that affect lithium ion selectivity through membranes are discussed, including the ion charge, hydration energy, channel size and functional groups. It is found that the selectivity of the membrane separation process is highly correlated to the ion hydration energy and the interaction between the ion and the functional groups. In particular, the ion hydration energy is the key factor affecting the entry stage, while the anchoring strength between the ion and the functional groups of the channel wall dominates the diffusion stage within the channel. We conclude with a discussion of the challenges and future development trends of membrane separation technology for lithium recovery.

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The continuous expansion of the lithium-ion battery market gives rise to a rapid increase in lithium prices. In this review, we focus on recent research efforts on membrane separation technology for lithium recovery to further elucidate the mechanism of ion selectivity through membranes. This review would help researchers to understand the mechanism of ion selectivity through membranes and achieve lithium ion separation efficiently.

1. Introduction

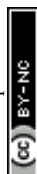
Lithium-ion batteries are widely used in our daily life due to their high energy density, wide voltage range, long cycle period, light weight and other advantages.^{1,2} Consequently, it is expected that the global lithium-ion battery market size will steadily increase from \$40.5 billion in 2020 to \$116.6 billion by 2030.³ However, the continuous expansion of the lithium-ion battery market gives rise to a rapid increase in lithium prices. By June 2023, the price of Li_2CO_3 per ton has increased to 43 000 USD. Lithium exists mostly in the form of compounds in nature, mainly distributed in minerals, salt lake brine, seawater, *etc.*^{4,5} To reconcile the contradiction between the limited lithium resources in nature and the

increasing market demand, people are now turning their attention to searching for new lithium sources.

Recycling and reusing lithium from waste lithium-ion batteries is widely recognized as the most feasible and promising solution to cope with the shortage of lithium. It is believed that the number of waste lithium-ion batteries that can be recycled worldwide will reach 641 595 tons by 2025. Especially in China, this value will reach 417 165 tons.⁶ Extracting lithium resources from waste lithium-ion batteries can not only meet the huge demand for lithium in the market but also achieve waste utilization, which is a very economical green chemical process. Therefore a lot of efforts have been made to develop more efficient separation and enrichment technologies, such as chemical precipitation,^{7,8} solvent extraction,^{9,10} and membrane separation.^{11,12}

In particular, the chemical precipitation method is mainly based on the solubility difference between various metal

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salts, where a large amount of precipitant is usually required.¹³ The solvent extraction method takes advantage of the difference in the partition coefficients of lithium ions in two immiscible solvents for separation. However, the extraction process is time-consuming, environmentally unfriendly and requires a lot of organic solvents.¹⁴

Compared to other separation and enrichment methods, the membrane separation method has the advantages of convenience, high separation purity and low energy consumption.^{15,16} Therefore, the membrane separation method has a wide range of applications, which can be used not only to extract lithium from waste lithium-ion batteries but also for the separation of other substances and seawater desalination.^{17,18} Generally, the reported membranes include thin film composite (TFC) membranes,^{19,20} covalent organic framework (COF) membranes,^{21,22} metal-organic framework (MOF) membranes²³ and so on. The TFC membrane features an ultrathin selective layer above a support in cross-sectional structure with different chemical compositions, while the MOF and COF membranes usually present a large number of pores. To simplify the description, both the selective layer and the pores are referred to as channels hereafter.

Currently, membrane separation processes mainly include forward osmosis (FO),^{24,25} nanofiltration (NF),^{26,27} reverse osmosis (RO),^{28,29} electrodialysis (ED)^{30,31} and membrane capacitive deionization (MCDI).^{32,33} FO technology is not very selective in solutions containing high concentrations of lithium, and RO technology is known for its high energy consumption. The ED and MCDI processes mainly rely on selective anion exchange membranes (AEMs) and cation exchange membranes (CEMs). Although ED and MCDI exhibit very rapid separation rates, the performance of ion exchange membranes can be influenced by several factors, such as membrane price and operating temperature. In contrast, NF is the most promising approach for lithium separation due to its low cost, process sustainability and low footprint.^{34,35}

For a typical membrane separation process, the different rates at which different ions pass through the membrane contribute to the ion selectivity of the membrane.³⁶ The current explanation for membrane separation mainly includes the ion dehydration mechanism³⁷ and ion-channel wall interaction mechanism.^{38,39} Many factors, such as channel size, hydration energy and the interaction between ions and channel walls, may affect ion selectivity through membranes.⁴⁰ In fact, ion migration across a membrane is a very complicated process, which could be influenced simultaneously by the factors mentioned above. However, there are few papers summarizing these influencing issues today, especially in the lithium recycling process. Therefore, this review will focus on recent research efforts on membrane separation technology for lithium recovery to further elucidate the mechanism of ion selectivity through membranes. Firstly, the three main stages of ion selectivity through membranes will be summarized, followed by the main factors affecting ion selectivity through membranes in

each stage. Finally, the existing main problems and possible solutions in this field will be highlighted.

2. Mechanism of ion selectivity through membranes

The entire process of ions passing through a membrane can be divided into three successive stages: (i) the first stage is the entering process of ions into the membrane, during which partial dehydration occurs; (ii) the second stage is the ion diffusion inside the membrane, during which ions may interact with functional groups on the membrane; (iii) the third stage is the returning of ions from the membrane to the solution on the other side, during which rehydration of ions may occur^{41,42} (Fig. 1). In particular, the ion selectivity resulting from the first stage is called partition selectivity, while the ion selectivity generated in the second stage is called diffusion selectivity.⁴² For the third stage, due to its symmetrical relationship with the first stage in the free energy curve, it can be considered that the third stage is the inverse process of the first stage.⁴⁰ In practical research, the third stage is rarely utilized to achieve ion selective passage through channels. Therefore, the following discussion will focus only on the first and second stages.

2.1. The entering process of ions into the membrane

The entering process refers to the entry of ions from the solution environment into the channel opening of the membrane under a certain driving force. Generally, the driving forces for ions passing through the membrane are mainly divided into osmotic pressure driving ($\Delta\pi$), hydraulic driving (ΔP) and electric potential driving (ΔV).³⁶

Among them, osmotic pressure driving corresponds to FO technology.^{43,44} As shown in Fig. 2(a), the device consists of a solution with lower concentration on the left side (feed solution), a membrane and a solution with higher concentration on the right side (draw solution). The membrane is composed of a support layer and a selective layer. Here, the role of the support layer is to maintain the mechanical stability of the membrane, while the role of the selective layer is to hinder the migration of solutes to the solution on the other side. The different concentrations between the two sides of the membrane will lead to osmotic pressure, which drives water molecules to migrate from the left solution through the membrane to the right solution. Meanwhile, the solute ions are blocked by the selective layer on the membrane. As the permeation time increases, the volume of the left solution decreases and the solute is enriched.

Hydraulic driving corresponds to NF technology⁴⁵ and RO technology.^{46,47} The difference between these two technologies mainly lies in the size of the particles being filtered. NF is used to filter particles of 8 to 50 Å size from its fluid.⁴⁸ In contrast, RO is increasingly applied for water desalination and can separate contaminations of size 12 Å and less.⁴⁸ As shown in



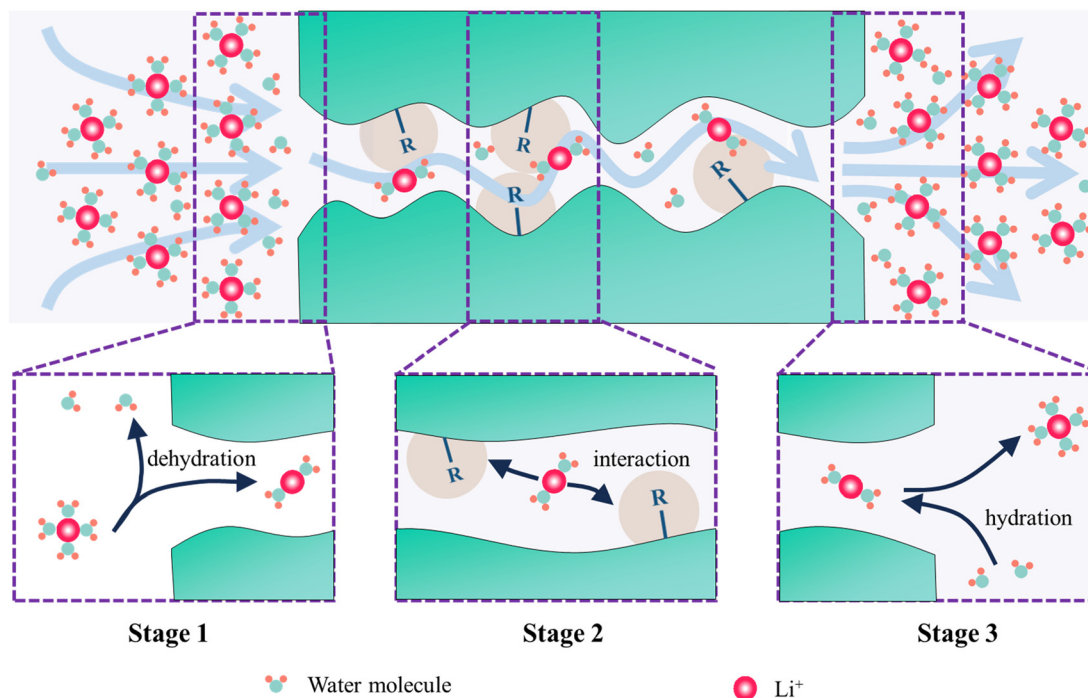


Fig. 1 The three stages of ion passing through the membrane. Stage 1 is the entering process of ions into the membrane, during which partial dehydration occurs. Stage 2 is the ion diffusion inside the membrane, during which ions may interact with functional groups on the membrane. Stage 3 is the returning of ions from the membrane to the solution on the other side, during which hydration of ions may occur.

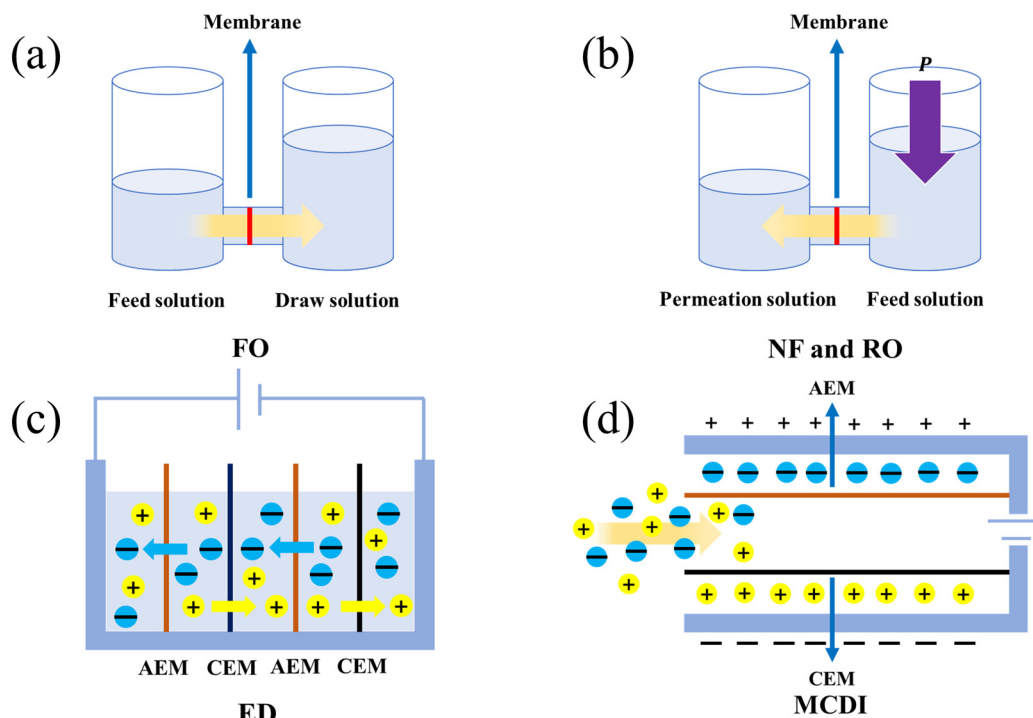


Fig. 2 Schematic diagram of different driving forces corresponding to technology. (a) FO technology (osmotic pressure driving); (b) NF and RO technology (hydraulic driving); (c) ED technology (electric potential driving); (d) MCDI technology (electric potential driving).

Fig. 2(b), both NF and RO use a membrane to separate the left (permeation solution) and right (feed solution) solution.^{47,49}

Applying hydraulic pressure above the right solution will cause the solute to pass through the membrane and enter the left



The migration of ions from the solution to the channels also involves a process similar to concentration polarization in electrochemistry. There is an external concentration polarization phenomenon in the FO and RO processes.⁵⁶ The diffusion speed of ions from the solution to the channels is greater than the speed of ions entering the channels. As a result, ions will accumulate at the opening of channels. Consequently, there may be a difference between the ion concentration at the bulk phase of the solution and the opening of channels. Two different calculation methods for ion repulsion have been proposed. Ion repulsion is a measurable parameter to evaluate the selectivity of certain ions to pass through the membrane. The greater the ion repulsion of a membrane towards a certain ion, the less likely it is for that ion to pass through the membrane. Ion repulsion can be divided into observed ion repulsion (R_{obs}) and real ion repulsion (R_{real}). Between them, R_{obs} is based on the concentration of ions in the bulk phase of the solution, while R_{real} is based on the concentration of ions at the opening of channels. The calculation formula for the two ion repulsions is as follows:

$$\text{Real ion repulsion: } R_{\text{real}} = 1 - c_p/c_m \quad (2)$$

Lu *et al.* studied the selectivity of different cations passing through the MXene@PSS membrane (Fig. 3(a and b)).⁶¹ In their work, the sizes of hydrated Li^+ and Mg^{2+} ions are 7.64 Å and 8.56 Å, respectively. Since the interlayer spacing of the membrane is 6 Å, the dehydration process should occur for ions to pass through the channels. Mg^{2+} (-1922 kJ mol⁻¹) has a more negative hydration energy than Li^+ (-515 kJ mol⁻¹). Thus, Mg^{2+} is less prone to dehydration and less likely to enter the channels. Therefore, a relatively high $\text{Li}^+/\text{Mg}^{2+}$ selectivity of 28 was achieved. Li *et al.* also observed a similar separation efficiency of $\text{Li}^+/\text{Mg}^{2+}$ by PEI/Cyclen-TMC (Fig. 3(c)).⁶² Pang *et al.* used quaternization reaction to study the passage of Li^+ and Mg^{2+} through different hydrophobic membranes (Fig. 3(d)).⁶³ For membranes with different hydrophobicity, the experimental results show that the ion flux of Li^+ is greater than that of Mg^{2+} . The reason for this result is that the hydration energy of Mg^{2+} is more negative than that of Li^+ . Liang *et al.* encapsulated sulfurized spiropyran (SSP) into ZIF-8 crystal and prepared a membrane to separate Li^+ ions from other cations (Fig. 3(e)).⁶⁴ The order of hydration strength is $\text{Mg}^{2+} > \text{Li}^+ > \text{Na}^+ > \text{K}^+$, which results in electrochemical impedance spectroscopy showing that the ion transfer resistance of Mg^{2+} is the highest and Mg^{2+} is the least likely to pass through the membrane. Wu *et al.* studied the separation of monovalent and multivalent metal ions through MOF (HKUST-1) channels (Fig. 3(f)).⁶⁵ In this study, the selectivity of the membrane for $\text{Li}^+/\text{Zr}^{4+}$ can reach 3930 ± 373 owing to the more negative hydration energy and larger hydration diameter of Zr^{4+} .

2.1.2. The channel size and hydration radius. The size of channels can affect the passage of ions through them. Steric

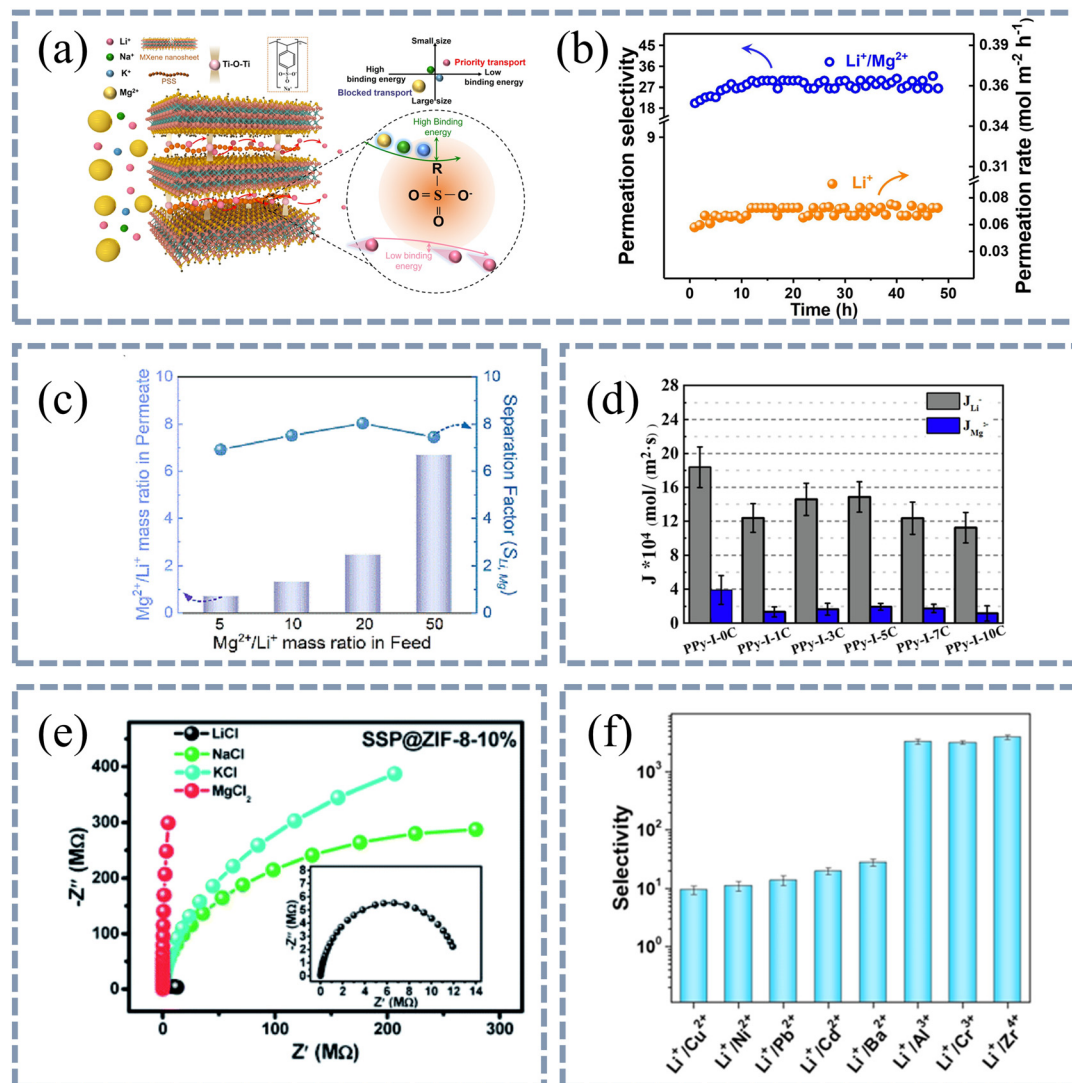
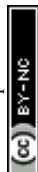


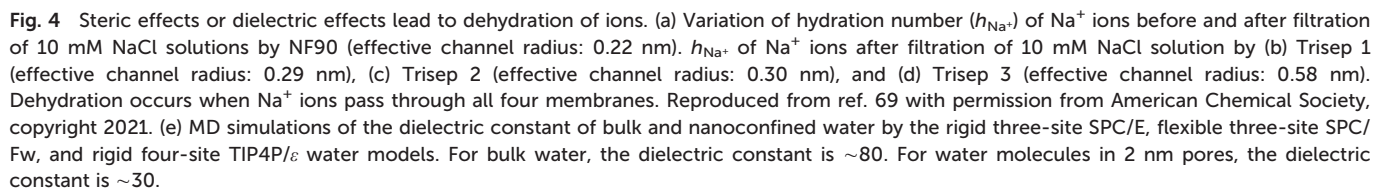
Fig. 3 The difference in hydration energy of ions results in selective passage of ions through the membranes. (a) Schematic diagram of channels for fast transport of Li^+ ions in MXene@PSS membranes. (b) Long-term stability of the MXene@PSS composite membrane. $\text{Li}^+/\text{Mg}^{2+}$ permeation selectivity reaches 28 due to the more negative hydration energy of Mg^{2+} ions. Reproduced from ref. 61 with permission from John Wiley and Sons, copyright 2021. (c) $\text{Mg}^{2+}/\text{Li}^+$ mass ratio in the permeate and separation factor ($S_{\text{Li,Mg}}$) of PEI/Cyclen-TMC composite membrane with various $\text{Mg}^{2+}/\text{Li}^+$ mass ratios in the feed. $S_{\text{Li,Mg}}$ can reach 8.0 owing to the more negative hydration energy of Mg^{2+} ions. Reproduced from ref. 62 with permission from Elsevier, copyright 2023. (d) The flux of PPY-I- n C membranes in diffusion dialysis experiment of single salt after 1 h: Li^+ and Mg^{2+} . n in PPY-I- n C is the carbon chain length of the quaternary ammonium reagent used in the membrane preparation process. The flux of Li^+ ions is faster than that of Mg^{2+} ions because the hydration energy of lithium ions is less. Reproduced from ref. 63 with permission from Elsevier, copyright 2021. (e) Ion selectivity of the SSP@ZIF-8-10% membrane. The order of hydration strength is $\text{Mg}^{2+} > \text{Li}^+ > \text{Na}^+ > \text{K}^+$. Electrochemical impedance spectroscopy results show that the ion transfer resistance of Mg^{2+} is the largest. Reproduced from ref. 64 with permission from Royal Society of Chemistry, copyright 2020. (f) Ion selectivity of Li^+ to various metal ions of the MOF membrane. The selectivity of the membrane for $\text{Li}^+/\text{Zr}^{4+}$ can reach 3930 ± 373 owing to the more negative hydration energy and larger hydration diameter of Zr^{4+} . Reproduced from ref. 65 with permission from John Wiley and Sons, copyright 2023.

effects will occur when they pass through the same channel because of different hydration and bare sizes of ions. According to the relative size between the channel size and the ion hydration size, the situation of ions passing through channels can be divided into three types:⁶⁶ (i) the channel size is greater than the hydration size of the ions. In this case, ions can enter the channels as a complete hydrated layer with the smallest energy barrier. (ii) The channel size is between the hydrated size of ions and that of bare ions. In

this case, ions need to undergo partial dehydration to enter the channels, where the ions need to overcome a moderate energy barrier during the entering process. (iii) The bare size of ions is close to the channel size. In this case, the ions may undergo a deep dehydrating process, leading to the largest energy barrier when entering channels. Obviously, if the channel size is further reduced to be smaller than the bare size of the ions, the ions will not be able to pass through channels.



recently published study showed that in addition to steric effects, other factors can also affect ion dehydration. When the hydration size of ions is smaller than the channel size, dehydration may also occur (Fig. 4(a-d)).⁶⁹ Lu *et al.* used *in situ* TOF-SIMS technology to measure the number of water molecules coordinated with ions before and after they entered the channels. In their experiments, four membranes of NF90 (Fig. 4(a)), Trisep 1 (Fig. 4(b)), Trisep 2 (Fig. 4(c)), Trisep 3 (Fig. 4(d)) with the effective channel radius of 0.22 nm, 0.29 nm, 0.30 nm and 0.58 nm, respectively, were employed to understand the dehydration behavior of Na⁺ (average hydration radius: 3.58 Å). From the perspective of steric effect alone, Na⁺ ions will undergo dehydration



to electrostatic repulsion, which lowers their diffusion barrier. In contrast, if the ion carries different charges from that of the groups of channels, it would be strongly attracted by the wall group of channels, leading to facile entrance in the channel openings but slow diffusion inside channels. Therefore, the apparent ion selectivity is a comprehensive reflection of these two processes. Labbez *et al.* summarized two types of retention (*i.e.* ion repulsion) behaviors, the quasi-symmetric curves and the asymmetric S-shaped curves, in the nanofiltration process at different pH values (Fig. 5(a)).⁸⁰ Quasi-symmetric curves are suitable for symmetric salts such as KCl, LiCl and MgSO₄, while asymmetric S-shaped curves are suitable for asymmetric salts such as K₂SO₄ and MgCl₂. For symmetric salts, the channel walls are positively charged at low pH and are repulsive to cations. At high pH, the channel walls are negatively charged and are repulsive to anions. When the pH is close to the isoelectric point (IEP) of the channel wall, the channels are almost uncharged, leading to significantly reduced repulsion to both anions and cations. However, the retention is determined by the ions with higher valence in the asymmetric salt (for example, SO₄²⁻ in K₂SO₄, Mg²⁺ in

2.1.3. The charge of ions. The charge of ions can also affect the selective passage of ions through channels *via* electrostatic interactions.^{76,77} If the channel carries the same charge as the ion, the strong electrostatic repulsion between the channel and the ion would prevent the ion from entering the channel. In contrast, when the channel wall and ions have opposite charges, the entrance process of ions into the channel could be significantly promoted.

Regarding free ions in the solution, the chemical environment around the ions will undergo significant changes after entering the channels. In particular, in small channels, ions are likely to interact with the inner wall of the channel, thereby affecting the selective permeability of the membrane to different ions.^{78,79} The following focuses on the main issues influencing ion migration in the membrane, such as the charge of ions, the length and size of channels, and the interaction between the groups in the channel and the ion.

Figure 10 consists of two plots, (a) and (b), showing the limiting retention and rejection percentages as a function of pH for various salts.

Plot (a) shows the limiting retention (%) versus pH for four salts: KCl (filled circles), LiCl (filled triangles), K_2SO_4 (filled squares), and $MgSO_4$ (open squares). The x-axis ranges from 2 to 10, and the y-axis ranges from -20 to 100. The retention generally decreases with increasing pH for most salts, with $MgSO_4$ showing the highest retention at low pH and KCl showing the lowest retention at high pH.

Plot (b) shows the rejection (%) versus pH for four salts: Fluoride (filled circles), Chloride (filled triangles), Bromide (filled squares), and Iodide (open squares). The x-axis ranges from 3 to 9, and the y-axis ranges from 0 to 60. The rejection generally increases with increasing pH for all salts. An inset plot shows the rejection (%) versus pH for the same four salts, with the x-axis ranging from 3 to 9 and the y-axis ranging from 0 to 90. The inset shows that rejection increases with pH for all salts, with Fluoride showing the highest rejection and Iodide showing the lowest rejection at high pH.

Fig. 5 The effect of charge carried by ions on their passage through pores. (a) Relationship curve of retention with pH change during the nanofiltration process. There are two types of retention behaviors, the quasi-symmetric curves (KCl, LiCl and MgSO_4) and the asymmetric S-shaped curves (K_2SO_4 and MgCl_2). Reproduced from ref. 80 with permission from Elsevier, copyright 2002. (b) Relationship between ion rejection of LiCl (purple), NaCl (red), KCl (olive green), and CsCl (brown) through a polyamide membrane and pH changes. Inset: rejection of monovalent anions-fluoride (blue), chloride (orange), bromide (gray), and iodide (green), as sodium salts-at different pH values. All curves exhibit the characteristics of the quasi-symmetric curve. Reproduced from ref. 81 with permission from American Chemical Society, copyright 2021.

MgCl₂). For instance, the retention of K₂SO₄ is determined by SO₄²⁻, which would obviously increase the retention at high pH values by the strong repulsion toward the negatively charged channels. The same conclusion was also validated in Shefer's study.⁸¹ Fig. 5(b) shows the relationship between ion repulsion of LiCl (purple), NaCl (red), KCl (olive green) and CsCl (brown) under various pH values. Typical quasi-symmetric curves with the IEP of ~4.5 were observed for all the above symmetric salts.

2.2.2. The interaction between groups on the channel wall and ions. Similar to the groups at the channel opening, the

channel wall groups will also interact with ions. Therefore, strong ion-group interactions will cause the ions to be firmly anchored by the channel wall, which in turn reduces the ion transportation rate in the channels. Sheng *et al.* investigated the permeation rate and selectivity between K⁺ and Mg²⁺ on the TpBDMe₂ membrane (Fig. 6(a-c)).⁸² Because of the strong affinity between Mg²⁺ and the channel wall, a relatively small permeation rate of Mg²⁺ was observed with a high K⁺/Mg²⁺ selectivity of 1000. Guo *et al.* studied the selective passage of Li⁺ ions through a membrane made by adding polystyrene sulfonate to HKUST-1 MOF material (Fig. 6(d and e)).⁸³ Since

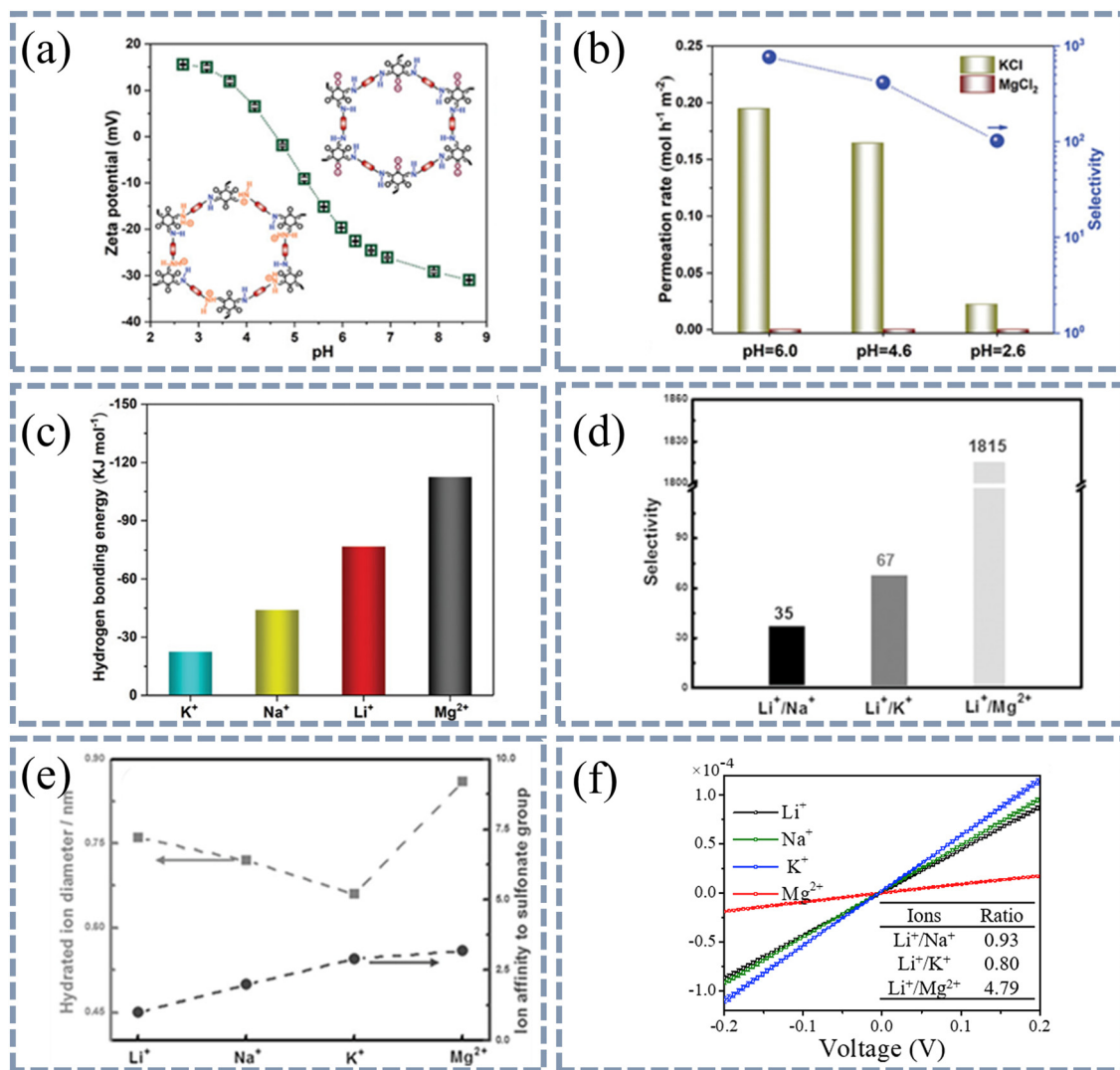


Fig. 6 The interaction between groups on the channel wall and ions affects the transport of ions in the membrane. (a) Zeta potential of TpBDMe₂ membranes as a function of pH. (b) Effects of pH on mono-/divalent cation permeation rate and selectivity of TpBDMe₂ membranes. (c) The hydrogen bonding energy between hydrated ions and the channel wall of TpBDMe₂ membranes. Because of the strong affinity between Mg²⁺ and the channel wall, a relatively low permeation rate of Mg²⁺ was observed with a high K⁺/Mg²⁺ selectivity of 1000. Reproduced from ref. 82 with permission from John Wiley and Sons, copyright 2021. (d) Binary ion selectivity of PSS@HKUST-1-6.7 in 0.5 M LiCl and 0.5 M Mⁿ⁺Cl_n electrolytes. (e) Relative strength of affinity between sulfonated group and ions (circles) and the hydrated ion diameters (squares). The selectivity of Li⁺/Na⁺, Li⁺/K⁺, and Li⁺/Mg²⁺ can reach 35, 67, and 1825, respectively, because the binding affinity between ions and the sulfonic group follow the sequence Mg²⁺ > K⁺ > Na⁺ > Li⁺. Reproduced from ref. 83 with permission from John Wiley and Sons, copyright 2016. (f) I-V curves of HSO₃-UiO-66-0.6@PVC membranes. The strong affinity between Mg²⁺ and -SO₃⁻ results in the highest separation ratio of Li⁺/Mg²⁺. Reproduced from ref. 84 with permission from Elsevier, copyright 2020.



the binding affinity between ions and sulfonic groups follow the sequence $\text{Mg}^{2+} > \text{K}^+ > \text{Na}^+ > \text{Li}^+$, the selectivity of Li^+/Na^+ , Li^+/K^+ , and $\text{Li}^+/\text{Mg}^{2+}$ can reach 35, 67, and 1815, respectively. Here, the HKUST-1 MOF not only acts as a carrier for sulfonate groups but also provides an appropriate channel to sieve ions. Zhang *et al.* studied the separation performance of six PVC-based hybrid membranes containing metal organic frameworks for Li^+ ions and Mg^{2+} ions (Fig. 6(f)).⁸⁴ Compared to other membranes, the $\text{HSO}_3\text{-UiO-66-0.6@PVC}$ membrane with rich -SO_3^- groups on the channel wall exhibits the highest separation ratio of $\text{Li}^+/\text{Mg}^{2+}$ due to the strong affinity between Mg^{2+} and -SO_3^- , which decreases the diffusion rate of Mg^{2+} ions in the membrane.

2.2.3. The length and size of the channel. The channel geometry, including the length and size of the channel, will also significantly affect the diffusion behavior of ions. Generally, the longer the channel, the better the partitioning of different ions, which results in superior selectivity of the membrane. Wang *et al.* investigated the effect of channel length on ion permeation rate and ion selectivity in COF membranes.⁸⁵ As shown in Fig. 7(a), as the length of the channel increases, the permeation rates of both K^+ ions and Li^+ ions decrease, while the selectivity increases from 13.5 to 16.8.

For the channel size, it affects not only the entering process of ions in the channel opening but also their transportation inside the channels. When the channel wall is charged with a

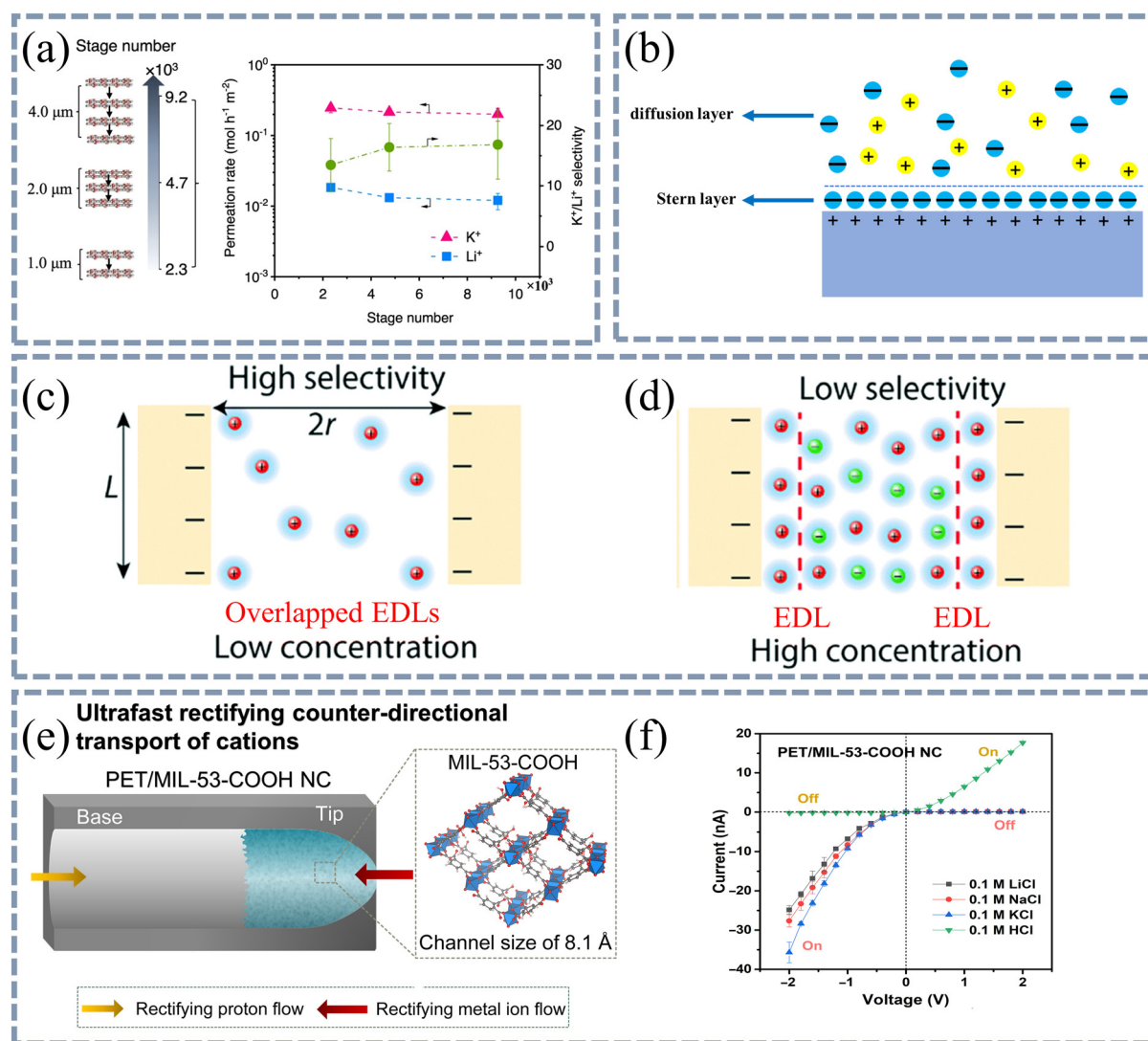


Fig. 7 The length and size of the channel affect the transport of ions in the membrane. (a) Transport performances of COF membranes under different stage numbers. As the stage number increases, the permeation rates of both K^+ and Li^+ ions decrease, while the selectivity increases from 13.5 to 16.8. (b) Schematic diagram of double layer model. The side near the interface is the Stern layer and that on the side away from the interface is the diffusion layer. (c) Double layer may not overlap when the ion concentration is low. (d) Double layer may overlap when the ion concentration is high. Reproduced from ref. 86 with permission from Royal Society of Chemistry, copyright 2022. (e) Schematic diagram of PET/MIL-53-COOH NC structure. (f) Asymmetrical *I-V* curves of 0.1 M LiCl, NaCl, KCl, and HCl in PET/MIL-53-COOH NC. The rectification effect occurs due to the overlap of the double layer.

certain amount of positive or negative charges, a double layer structure will form near the channel wall. According to the Stern model, the double layer is divided into the Stern layer and the diffusion layer (Fig. 7(b)). In the Stern layer, the surface charge of the channel wall would strongly attract the counter ions, forming a stable adsorption layer on the channel wall. However, beyond the Stern layer, the diffusion layer may consist of both cations and anions, which do not directly interact with the channel wall and are weakly affected by the electrostatic attraction or repulsion of the channel wall. As a result, the Stern layer of the channel usually exhibits much better selectivity than the diffusion layer. When the channel size reduces to a certain size where the Stern layers on both sides overlap each other, the selectivity towards counter ions could be significantly improved. Therefore, if the Stern layers on both sides of the channel overlap, there is selective passage of anions and cations through the channels (Fig. 7(c and d)).⁸⁶ The thickness of the Stern layer is very similar to the Debye shielding length (λ_D).⁸⁷ According to relevant literature reports, the thickness of the Stern layer is also sensitive to the ion concentration in the solution, where a high ion concentration should result in a thin Stern layer.^{88,89,86}

Lu *et al.* studied the rectification effect of alkali metal ions in PET/MIL-53-COOH nanochannels with a unique base–tip structure (Fig. 7(e and f)),⁹⁰ where the tip side is filled by the MIL-53 MOF with a channel size of 8.1 Å. For all the three salts (*i.e.* LiCl, NaCl and KCl), the diffusion current could be detected only when a reverse voltage is applied, suggesting that Li⁺, Na⁺ and K⁺ ions can migrate only from tip to base. In fact, when a reverse voltage is applied, the cation migration from tip to base is driven by both the potential gradient and the concentration gradient. Meanwhile, the anions may migrate from base to tip in the presence of an electric field. However, due to the overlap of the double layers at the tip, the anions cannot pass through the channels at the tip side, leading to the accumulation of anions at the base. Moreover, to balance the charge, more cations will enter the base side, and the cation diffusion from tip to base is further promoted. When a forward voltage is applied, the potential gradient of the cations is opposite to the concentration gradient, resulting in a much smaller number of migrated cations. For anions, the overlapped double electric layers at the tip would also prevent the anion diffusion from tip to base. Therefore, no diffusion current could be observed with a forward voltage.

Conclusions

The ion diffusion mechanism in the membrane separation process is summarized in this review. It should be noted that although the ion diffusion is divided into three stages, the influences of the above issues might be observed throughout the entire membrane separation process. Most studies that achieve ion selectivity through channels mainly focus on (i) the difference in dehydration process when ions enter the channels, where only the ions with small dehydration energies are allowed, and (ii) the difference in the interaction

between ions and channel wall groups. The reason why some ions can freely migrate within the channel, while others are anchored near the groups on the channel wall, could be attributed to the different bonding energies between different ions and groups on the channel wall.

At present, the main problems faced by using membrane technology to achieve ion selectivity through channels are (i) the inability to ensure good permeation flux while maintaining high ion selectivity, *i.e.* the trade-off between permeation and selectivity. The ideal membrane should have abundant channels with a narrow channel size distribution and the desired functional groups on the channel wall surface.⁹¹ The design and development of new membrane fabrication technologies should be a promising approach to tackle the above contradictions. (ii) The existing techniques cannot effectively measure the migration of ions in channels due to the limitations of temporal and spatial resolution.⁹² In order to further understand the ion transportation mechanism, researchers should first make good use of computational modelling, such as molecular dynamics simulation and density functional theory calculation. Secondly, relevant testing techniques should be further developed to meet the needs of *in situ* measurement during the membrane separation.⁶⁹ (iii) The stability of the membrane should be further improved. A series of materials, such as MOFs,²³ COFs,⁹³ MXene⁹⁴ and graphite oxides,⁹⁵ are employed to prepare membranes with superior structural and chemical stability. For MOFs and COFs, researchers should pay attention to the impact of defects on membrane performance. For MXene and graphite oxides, more attention should be paid to the influence of interlayer spacing expansion on membrane performance after immersion in the solution.

Author contributions

Jian Zhang: writing – original draft. Qiang Gao: conceptualization. Bo Han: writing – review & editing. Chenggang Zhou: funding acquisition.

Conflicts of interest

There are no conflicts to declare.

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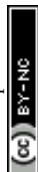
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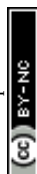
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