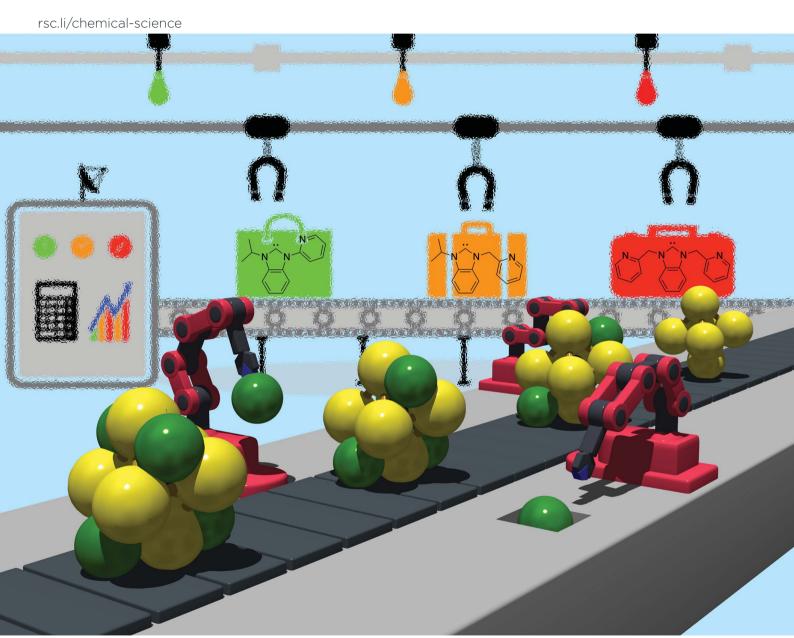
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Photoluminescence control by atomically precise surface metallization of C-centered hexagold(1) clusters using N-heterocyclic carbenes†

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The properties of metal clusters are highly dependent on their molecular surface structure. The aim of this study is to precisely metallize and rationally control the photoluminescence properties of a carbon(C)-centered hexagold(i) cluster (CAu $_0^1$) using N-heterocyclic carbene (NHC) ligands with one pyridyl, or one or two picolyl pendants and a specific number of silver(i) ions at the cluster surface. The results suggest that the photoluminescence of the clusters depends highly on both the rigidity and coverage of the surface structure. In other words, the loss of structural rigidity significantly reduces the quantum yield (QY). The QY in CH $_2$ Cl $_2$ is 0.04 for [(C)(Au 1 -BIPc) $_6$ Ag 1_3 (CH $_3$ CN) $_3$ I(BF $_4$) $_5$ (BIPc = N-isopropyl-N'-2-picolylbenzimidazolylidene), a significant decrease from 0.86 for [(C)(Au 1 -BIPy) $_6$ Ag 1_2 I(BF $_4$) $_4$ (BIPy = N-isopropyl-N'-2-pyridylbenzimidazolylidene). This is due to the lower structural rigidity of the ligand BIPc because it contains a methylene linker. Increasing the number of capping Ag 1 ions, i.e., the coverage of the surface structure, increases the phosphorescence efficiency. The QY for [(C)(Au 1 -BIPc 2) $_6$ Ag 1 4(CH $_3$ CN) $_2$ 1(BF $_4$) $_6$ (BIPc 2 = N,N'-di(2-pyridyl)benzimidazolylidene) recovers to 0.40, 10-times that of the cluster with BIPc. Further theoretical calculations confirm the roles of Ag 1 and NHC in the electronic structures. This study reveals the atomic-level surface structure-property relationships of heterometallic clusters

Introduction

Gold clusters have attracted a lot of attention in recent years due to their molecular structures based on aurophilicity between gold atoms and their optical properties such as structure-specific photoluminescence. ^{1,2} Gold clusters with such properties have been applied to a variety of applications such as OLEDs and bioimaging *etc.* ³ To realize on-demand synthesis of cluster-based phosphorescent materials, great efforts have been made over the past decades to correlate the structure of gold clusters with their photoluminescence. ⁴⁻⁶ In the meantime, several general strategies were developed to enhance or tune the photoluminescence. Examples include changes in electronic structure due to alloying of metal kernels, ⁷⁻¹⁰ surface hardening by additives to suppress non-radiative relaxation, ¹¹⁻¹⁴ supramolecular networks due to self-assembly of clusters, ¹⁵⁻¹⁸ and

chemical modification of supporting ligands by electronic donating/withdrawing groups and use of steric hindrance.¹⁹

On the other hand, surface molecular design of metal clusters is a promising strategy for developing chemical and physical properties specific to metal arrays. Compared to the widely used phosphine ligands, NHC ligands are similarly stable monodentate ligands with flexible electronic properties such as electron-donating properties and high designability of chemical structures.20-27 Therefore, we have been working on photoluminescence control of C-centered Au^I and Au^I-Ag^I clusters by chemical modification with N-heterocyclic carbene (NHC) ligands.28-32 We found that the introduction of different types of ligands on the surface of Au^I and Au^I-Ag^I clusters dramatically changed their photoluminescence behavior, including excitation and emission energies, quantum yields (QYs, φ) and phosphorescence lifetimes (τ) . For example, the homometallic $[(C)(Au^{I}-BIiPr)_{6}](BF_{4})_{2}$ (1, BIiPr = N,N'-diisopropylbenzimidazolylidene) and the classic [(C)(Au^I-PPh₃)₆](BF₄)₂ (ref. 33–36) are structurally similar but exhibit very different emission properties in the solid state.30 More surprisingly, the heterometallic $[(C)(Au^{I}-BIPv)_{6}Ag_{2}^{I}](BF_{4})_{4}$ (2, BIPv = N-isopropyl-N'-2-pyridylbenzimidazolylidene) shows blue-shifted emission and 3 times higher QY in solution than [(C)(Au^I-dppy)₆Ag₂^I](BF₄)₄ (dppy = 2-pyridyldiphenylphosphine). 32,37

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Previously, Wang and co-workers reported a series of carbon-centered, phosphine-protected Au^I–Ag^I clusters.^{37–44} The second layer of Ag^I ions on the cluster surface fully protects the core portion, resulting in long life and highly efficient emission.^{43,44}

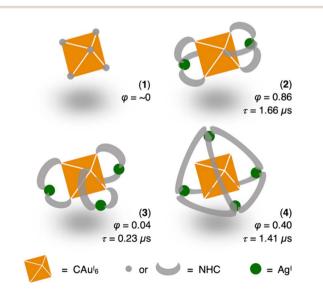
Chemical Science

ometallic clusters.

layer of Ag¹ ions on the cluster surface fully protects the core portion, resulting in long life and highly efficient emission. ^{43,44} In our recent work, we found that NHC ligands may further enhance the emission of heterometallic clusters. ³² These results suggest that, the silver(1) adatoms and NHC ligands synergistically contribute to the photoluminescence properties of heter-

In this study, we aimed to investigate this synergistic effects of NHC ligands and the silver(i) adatoms on the surface of heterometallic clusters. By taking advantage of pre-designed benzimidazolylidene-type NHC ligands with one or two picolyl pendant(s), we have achieved atomically precise metallization to the CAu $_6^I$ cluster site, and established correlations among the ligand structure, metal adatom number, and photoluminescence behavior (Scheme 1). We emphasize that the results of this work are not a mirror universe of phosphine-protected clusters, since (a) ligand design here is more elaborate; (b) the heterometallic clusters obtained show distinctly different molecular geometries; and (c) the photoluminescence of the clusters does not simply follow the "full protection" rule.

We first added a methylene linker between the benzimidazole and pyridyl groups of **BIPy** (Fig. 1). When acting as a bidentate ligand as in the case of **BIPy**, the methylene group seemed to give some structural flexibility to the resulting ligand N-isopropyl-N'-2-picolylbenzimidazolylidene (**BIPc**). Furthermore, since the pyridyl groups of **BIPy** mainly affect the electronic structure of the hexagold(i) cluster (Scheme S1†),³² the fundamental motivation for this design was the thought that the introduced methylene linker could separate the two heterocyclic moieties, thereby breaking the electronic perturbation from the directly connected imidazole and benzimidazole groups. By using this **BIPc**, a moderately phosphorescent cluster $[(C)(Au^{I}-BIPc)_{6}Ag_{3}^{I}(CH_{3}CN)_{3}](BF_{4})_{5}$ (3) was constructed,



Scheme 1 Phosphorescence properties of CAu_6^l clusters surrounded by different NHC or NHC-Ag^l shells in CH_2Cl_2 at room temperature (φ represents QY, τ represents lifetime).

Fig. 1 (a) Structure of ligand BIPr. (b) Structure of ligand BIPy. (c) Structure 2 of ligand BIPc. (d) Molecular structure of BIPc·HCl. (e) Structure of ligand BIPc. (f) Molecular structure of BIPc²·HCl.

in which the octahedral CAu_6^I core was capped by three $(\mathbf{BIPc})_2Ag$ moieties in a triangular arrangement (Scheme 1). Note that the tricapped octahedral structure has not been achieved yet in neither the NHC- nor the phosphine-protected CAu_6^I cluster family (Scheme S2†). The newly synthesized $CAu_6^IAg_3^I$ -type cluster 3 showed a red-shifted emission, but the QY was significantly lower ($\varphi=0.04$) and the lifetime was shorter (0.23 μ s) compared to the excellent photophysical properties of bicapped octahedral, $CAu_6^IAg_2^I$ -type cluster 2. The use of the picolyl group resulted in the coordination of another silver ion around the octahedral CAu_6^I structure, causing a redshift in the emission. On the other hand, the introduction of a methylene linker to the picolyl group resulted in a much looser structure of the coordination sphere, which was found to be responsible for the low QY and short lifetime.

ligand carbene N,N'-di(2-picolyl) benzimidazolylidene (BIPc²), which has a higher symmetry with two picolyl groups, was used to make the structure of the coordination sphere more rigid (Fig. 1).45-47 As a result, a tetrahedral form of $[(C)(Au^{I}-BIPc^{2})_{6}Ag_{4}^{I}(CH_{3}CN)_{2}](BF_{4})_{6}$ (4), a CAu₆^IAg₄-type cluster, was obtained in which the outer shell part composed of (BIPc²)₆Ag₄^I covered the octahedral CAu₆ cluster (Scheme 1). By introducing an additional ligand in the wingtip group of the carbene ligand and increasing the number of Ag^I ions bound to CAu^I₆, strong red phosphorescence with a QY of 0.40 and a lifetime of 1.41 μs was observed in CH₂Cl₂, both of which were significantly improved compared to cluster 3. The $CAu_6^IAg_4^I$ tetrahedron has edges of 5.544–5.947 Å, which is comparable to the Au₁₀ nanocluster, 48,49 one of the long pursued tetrahedral gold nanoclusters. This result indicates

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that not only the coverage of the cluster surface by additional metal ions but also the rigidity of the coordination structure is important for the strong and long-lived phosphorescent properties of metal clusters. The structure will also provide a useful new idea for rational synthesis of tetrahedral Au₁₀ and Au₂₀. 48-54

Results and discussion

Synthesis

Structures of BliPr, BIPy, BIPc and BIPc² are shown in Fig. 1. The ligands BIPc and BIPc² were synthesized as hydrochloride salts by a modified procedure of the literature (Fig. 1 and S1†). The CAu_6^I clusters $[(C)(Au^I-BIPc)_6](BF_4)_2$ (5) and $[(C)(Au^I-BIPc^2)_6](-BIPc^2)_6$ BF₄)₂ (6) as precursors were prepared in 46% and 43% overall yields based on the amount of gold, respectively (Fig. 2a, S2-S22 and Tables S1-S3†).§ CAu₆Ag₂-type cluster 2 was synthesized according to our previously reported literature.32

Next, heterometallic clusters were synthesized from clusters 5 and 6. The CAu₆^I cluster of 5 or 6 was mixed with AgBF₄ in CH_2Cl_2/CH_3CN (v:v = 9:1) and the reaction was monitored by ESI-MS spectrometry. When AgBF₄ was added to cluster 5, signals indicating the formation of heterometallic species of $[(C)(Au^{I}-BIPc)_{6}Ag^{I}](BF_{4})^{2+},$ $[(C)(Au^{I}-BIPc)_{6}Ag_{2}^{I}](BF_{4})_{2}^{2+},$ $Au_5^IAg_2^I(BIPc)_4](BF_4)^+$, and $[(C)Au_5^IAg_2^I(BIPc)_4](BF_4)_2^+$ appeared (Fig. S23†), which were found to be similar to the pattern of peaks seen in the BIPy-protected cluster.32 This complexation process in solution was also monitored by UV-vis absorption, fluorescence and ¹H NMR spectroscopies (Fig. S24-S26†). In the UV-vis spectra, the intensity of the peak around 340 nm decreased significantly with the addition of silver ions, and a new series of peaks and shoulders appeared. The emission spectra showed an increase in the intensity of the broad peak in the lower energy region. In fact, when the reaction mixture was irradiated with a UV lamp, a bright orange-yellow emission was observed. The decrease and increase in absorbance at 343 and 440 nm, respectively, and the increase in emission intensity at 609 nm were all strongly suggestive of the incorporation of three Ag^I ions into cluster 5. The ¹H NMR spectra showed that the sharp signals became unstructured with the addition of Ag^I ions, suggesting a flexible coordination structure of the product.

The complexation between cluster 6 and AgBF₄ in CH₂Cl₂/ CH₃CN was first monitored by ¹H NMR spectroscopy. The heterometallic species formed in situ exhibited a single set of relatively sharp signals, distinct from the complexation of cluster 5 and AgBF4 (Fig. S26 and 27†). ESI-MS spectroscopic analysis revealed the gradual formation of heterometallic species $([(C)(Au^{I}-BIPc^{2})_{6}Ag_{n}^{I}](BF_{4})_{n}^{2+} (n=1-4))$ containing one to four Ag^{I} ions (Fig. S28†). In the UV-vis absorption and emission spectra, a plot of absorbance/emission intensity against the amount of Ag^I added to cluster 6 indicates that three to four AgI ions were incorporated into cluster 6 (Fig. S29 and 30†). These data strongly suggest that a tetra-capped heterometallic structure was formed.

Molecular structures and characterizations

Single crystals of heterometallic clusters were obtained by layering dry Et₂O on a CH₂Cl₂/CH₃CN solution of products in

tubes. Single-crystal X-ray diffraction (ScXRD) analysis determined the structures of the tricapped CAu₆^IAg₃^I-type 3 and the tetrahedral CAu₆Ag₄-type 4.§ The molecular structure and simplified scheme of the cationic part of cluster 3 are shown in Fig. 2b and c, respectively. The structure of 3 is clearly different from that of CAu₆Ag₂-type cluster 2, as the three Ag^I atoms, supported by the ligand BIPc, cap the three octahedral faces of the CAu₆ cluster, forming a triangulated monorectified tetrahedron (triangular frustum) structure. Specifically, two BIPc ligands adjacent via pyridyl groups and one additional acetonitrile ligand are coordinated to each AgI ion in cluster 3, so the overall structure can be viewed as a CAu₆ center supported by three (BIPc)₂Ag motifs. The reason why the synthesis in CH₂Cl₂/ CH₃OH did not work (Fig. S31 and S32, see ESI† for details) can be explained by the co-stabilization with acetonitrile. The Au^I-Ag^I distances in cluster 3 (2.8268(14)–2.9754(14) Å, Table S4†) were found slightly longer than that in cluster 2 (2.8467(17) Å). The ligand BIPc has one more methylene group than BIPy, making it relatively flexible. Notably, when cluster 3 was formed, the ¹H NMR spectra showed that the singlet signal of the methylene group of CAu_6^I -type cluster 5 ($\delta = 5.77$ ppm in CD_2Cl_2) was split into two doublet signals ($\delta = 6.10, 6.66$ ppm in CD₂Cl₂) (Fig. S4 and S33†). This is because, when the pyridyl group coordinates to AgI, the two hydrogen atoms of the methylene group become chemically inequivalent. One hydrogen atom is oriented toward the metal kernel to form a hydrogen-gold bond, while the other is oriented away from it. Indeed, in the structure of cluster 3, the estimated intramolecular C(sp³)-H···Au bond between the hydrogen atom and the gold atom was very short $^{55\text{--}60}$ (Fig. S37,† 2.677 Å). The results of the ¹H NMR measurements of cluster 3 were found to be affected from the deuterated solvent in the solvent used. In fact, very broadened signals were observed when measured in CD_2Cl_2/CD_3CN (v:v = 9:1, Fig. S38†), reproducing the results of the complexation between cluster 5 and AgBF₄ (Fig. S26†). This result suggests that the presence of coordinating acetonitrile molecules makes the coordination of ligand BIPc in cluster 3 slightly more fluxional. UV-vis absorption spectroscopy and ESI-MS were also employed to characterize cluster 3 (Fig. S39 and S40†). The results were similar to the spectra of heterometallic species formed in situ (Fig. S23 and S24†).

More interestingly, CAu₆^IAg₄^I-type cluster 4 has a tetrahedral structure (Fig. 2d and e). Tetrahedral gold clusters (e.g. Au₄, Au₁₀, Au₂₀) have long been explored because they can be regarded as fragments of bulk gold and have been found or predicted to exhibit unique structural properties such as wide energy gap and spherical aromaticity. 48-54,61-63 Despite the fact that Au₄ has actually been reported, structure information on the latter two clusters is not yet available. As shown in the simplified CAu₆Ag₄ structure in Fig. 2e, four Ag¹ atoms cap the four faces of the octahedral CAu_6^I in the central of cluster 4. The Au^I-Ag^I distances for cluster 4 are in the range of 2.7425(7) to 3.0507(7) Å, slightly off distances in 2 and 3. Another way to look at it is that the central CAu₆ is encapsulated in a tetrahedral (BIPc²)₆Ag₄ cage. Three of the twelve pyridyl groups were found not to be involved in metal coordination in the crystalline state, as indicated by the blue dashed circles. The coordinating

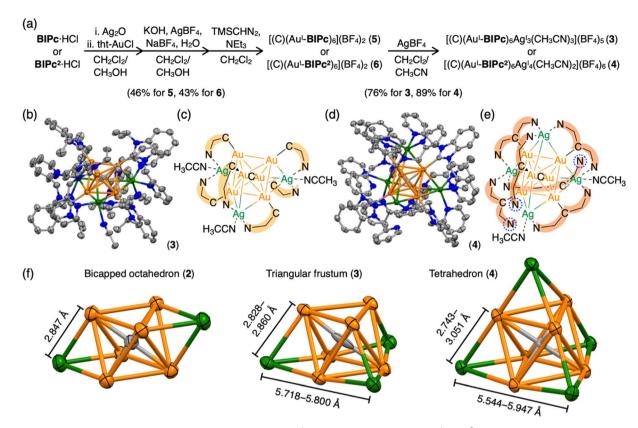


Fig. 2 (a) Synthetic schemes of the homometallic clusters $[(C)(Au^{1}-BIPc)_{6}](BF_{4})_{2}$ (5) and $[(C)(Au^{1}-BIPc^{2})_{6}](BF_{4})_{2}$ (6), and heterometallic clusters $[(C)(Au^{1}-BIPc)_{6}Ag_{3}^{1}(CH_{3}CN)_{3}](BF_{4})_{5}$ (3) and $[(C)(Au^{1}-BIPc^{2})_{6}Ag_{4}(CH_{3}CN)_{2}](BF_{4})_{6}$ (4). (b) Molecular structure of cluster 3. (c) A simplified scheme showing the structure of cluster 4. (e) A simplified scheme showing the structure of cluster 4. N^C^N represents ligand $BIPc^{2}$. Uncoordinated pyridyl groups are highlighted by dashed blue cycles. (f) Comparison of structures of bicapped octahedral $CAu_{6}^{1}Ag_{2}^{1}$ in cluster 2, triangular frustum-shaped $CAu_{6}^{1}Ag_{3}^{1}$ in cluster 3, and tetrahedral $CAu_{6}^{1}Ag_{4}^{1}$ in cluster 4. The length of the edge of each structure is shown.

acetonitrile was thought to contribute to the stabilization. Similarly, in the case of cluster 3, two pyridyl groups and one acetonitrile are considered to be uniquely coordinated to the three Ag^I ions to stabilize the complex in solution. In the case of cluster 4, on the other hand, the ligand exchange reaction in solution is considered to be more complex because there can be multiple combinations of pyridyl groups and acetonitrile as ligands to the four Ag^I ions. The mismatched structure of the ligand $BIPc^2$ probably prevents the formation of a perfect tetrahedral structure.

An important structural point is that the composition of 4 is similar to previously reported $[(C)(Au^I-PPhPy_2)Ag_4^I](BF_4)_6$ (-PPhPy₂ = bis(2-pyridyl)phenylphosphine), but the arrangement of four Ag^I ions on the octahedral CAu_6^I surface is distinctly different from each other. The latter cluster has a butterfly-like molecular structure, that is, two opposite pairs of neighboring triangular faces are capped; whereas the four Ag^I ions in 4 are in a tetrahedral arrangement as far apart from each other as possible (Scheme S2†). This difference may be attributed to the different geometries of the NHC and phosphine ligands. In PPhPy₂, the two coordinative pyridyl groups are bonded directly connected to the same phosphorous atom, so the angle between these two pyridyl groups should be approximately 120°, and the

distance between the two N donors are relatively short. These two features are in geometrical contrast to $BIPc^2$, in which the two picolyl groups are on two sides of the benzimidazolylidene. The introduction of a methylene linker at the picolyl group further increased the distance between the two N donors in $BIPc^2$, making the coordination mode more flexible. These results demonstrate the designability of the NHC ligands and their superiority.

For heterometallic cluster **4**, we first performed a detailed evaluation of the solution structure by ¹H NMR spectroscopy (Fig. S41–S44†) and observed only one set of signals in the spectrum. Second, all peaks in the ¹H and ¹³C NMR spectra were sharp and showed no apparent fluxing, despite the use of a deuterated mixed solvent containing coordinating acetonitrile. This suggests that cluster **4** exists in a fairly symmetric structure in solution. A splitting of the methylene signal was also observed in the ¹H NMR spectrum of **4**, as in cluster **3**. The sharp singlet peak at 5.63 ppm in CAu₆^I cluster **6** split into two doublet peaks at 5.38 and 6.06 ppm when forming cluster **4** (Fig. S8 and S41†). This result suggests that the hydrogen atom on one side of the methylene chain of cluster **4** forms an intramolecular C(sp³)–H····Au bond and the pyridyl group is fixed in solution, as shown in Fig. S37.† Cluster **4** was further

characterized by ESI-MS and UV-vis spectroscopy (Fig. S45 and S46†). As a result, we were able to reproduce most of the data for the heterometallic products formed at the site (Fig. S28 and S29†). This indicates that cluster 4 is the main product of the complexation of CAU_6^1 cluster 6 with $AgBF_4$.

Correlation between phosphorescence and structure

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Clusters 2–4 have a common CAu₆^I octahedral core structure and exhibit properties characteristic of different external structures. In clusters 2–4, the two, three, and four faces of the central octahedral CAu₆^I were capped by Ag^I ions, forming bicapped octahedral, triangular frustum-shaped (monorectified tetrahedral), and tetrahedral metal kernels, respectively (Fig. 2f). In cluster 2, the Au^I–Ag^I distance is 2.847 Å. In cluster 3, the side edges of the frustum (Au^I–Ag^I) ranged from 2.828 to 2.860 Å and the lower bottom (Ag^I–Ag^I) side edges ranged from 5.718 to 5.800 Å. Tetrahedral cluster 4 was slightly distorted, with all edges in the 5.544–5.947 Å range. In the case of NHC ligands, on the other hand, the rigidity of the entire molecule depends on the presence or absence of a methylene linker in the ligand. As a result, it is inferred that clusters 2–4 exhibit structure-specific emission.

In the solid state, clusters 3 and 4 show orange and red emission with maxima at 640 and 661 nm, respectively, both significantly red-shifted compared to cluster 2 (573 nm; Fig. 3a, S47 and S48†). The emission maxima of clusters 2-4 also showed a similar red-shift in the CH₂Cl₂ solution (Fig. 3b, S49 and S50†). Both clusters 3 and 4 are very stable under ambient conditions. The absorption spectra of CH2Cl2 solutions of 3 and 4 ($c = 3.3 \times 10^{-5} \text{ mol L}^{-1}$) remain virtually unchanged after one week in sunlight at room temperature (Fig. S51†). Surprisingly, 4 remains robust in CH₂Cl₂/CH₃CN $(v:v = 9:1, c = 3.3 \times 10^{-5} \text{ mol L}^{-1})$ at 4 °C for about 18 months (Fig. S52†). The wingtip group of ligand BIPc in cluster 3 is one methylene chain longer than that of BIPy in cluster 2, so that one more AgI ion could be accommodated on the central hexagold(1) cluster. In the case of cluster 4, the number of pyridyl groups increased to twelve, creating new chances to bind further one more adatom. As a result, more red-shifted emission was observed from the clusters with more metal atoms, and the stability of cluster 4 was also improved by introducing a fourth silver atom.

More importantly, the photoluminescence QYs and lifetimes of clusters 2–4 were very different from each other. First, the QY and lifetime of cluster 3 were measured to be 0.04 and 0.23 μs , respectively, about an order of magnitude smaller than those of cluster 2 (0.86 and 1.66 μs , respectively). However, these values for cluster 4 were 0.40 and 1.41 μs , respectively, almost recovering to the level of the values for cluster 2. The high QY, microsecond-scale lifetime, and large Stokes shift indicate that the emissions of clusters 2–4 are phosphorescence.

The radiative and non-radiative rate constants ($k_{\rm r}$ and $k_{\rm nr}$, respectively) of each cluster were then calculated from the QY and lifetime values (Table 1). Because all of these clusters are protected by benzimidazolylidene-type ligands, we were able to

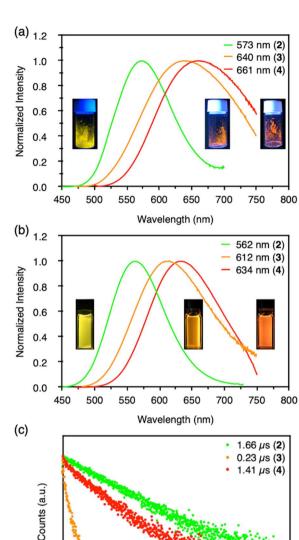


Fig. 3 (a) Emission spectra of $CAu_{6}^{l}Ag_{n}^{l}$ -type clusters 2–4 (n=2,3,4) in the solid state at room temperature and corresponding emission photographs of 365 nm excitation (from left to right). (b) Emission spectra of clusters 2–4 in $CH_{2}CI_{2}$ at 20 °C and corresponding emission photographs of 365 nm excitation (from left to right). (c) Emission decays of clusters 2–4 in $CH_{2}CI_{2}$ at room temperature.

Table 1 Emission QYs (φ) , lifetimes (τ) , radiative (k_r) and non-radiative (k_{nr}) rate constants of $CAu_6^lAg_n^l$ -type clusters **2–4** (n=2, 3, 4) in CH_2Cl_2

Cluster	φ	τ (μs)	$k_{\rm r}~(imes 10^5~{ m s}^{-1})$	$k_{\rm nr} (\times 10^5 \; {\rm s}^{-1})$
2	0.86	1.66	5.18	0.84
3	0.04	0.23	1.74	41.7
4	0.40	1.41	2.84	4.26

correlate two factors with respect to the emissions of clusters: the wingtip groups of the carbene ligand, and number of Ag^I atoms in the cluster.

First, the values of k_r and k_{nr} for CAu₆^IAg₃^I-type cluster 3 were changed by a factor of 1/3 and about 50 times, respectively, compared to those of cluster 2. These marked differences are likely due to a significant decrease in the stability of the bond between the methylene group of the BIPc ligand of cluster 3 and the Ag^I ion (Scheme S2†). This increase in the non-radiation deactivation process of 3 is due to the introduction of a flexible structure, which may have had a significant impact on the emission efficiency. Furthermore, the $k_{\rm nr}$ value of ${\rm CAu_6^IAg_4^I}$ type cluster 4 decreased by about a factor of 10, indicating that non-radiation deactivation process was significantly suppressed. In cluster 3, the six ligands have one picolyl ligand each, with two picolyl nitrogens and one acetonitrile coordinating to the three AgI ions. In cluster 4, six ligands have two picolyl groups each, and most or all of them can interact with the four AgI atoms, as shown by ScXRD and NMR data. Considering that the bond formation between the picolyl group and Ag^I has a small effect on the bond lengths and bond angles of the methylene-bridged N-C-C bonds in the ligand moiety of clusters 3 and 4, it is estimated that the incorporation of the fourth AgI atom into the CAuI core of cluster 4 serves to further enhance QY by efficiently suppressing the non-radiation process, and that the immobilizing effect of the picolyl groups, although not negligible, is not a decisive factor.

Theoretical calculations

Density functional theory (DFT) and time-dependent density functional theory (TD-DFT) calculations were carried out to disclose electronic structures of the clusters and the origin of the phosphorescence. First, the Bader and NPA (natural

population analysis) charges of the central C, Au and Ag atoms in CAu₆^IAg₃^I-type cluster 3 and CAu₆^IAg₄^I-type cluster 4 were analyzed (Table S5†). Compared to CAu₆-type clusters 5 and 6, the negative charges of the central C atoms in clusters 2, 3 and 4 are reduced and the positive charges of the Au atoms are reduced. These results indicate that Ag ions covering the CAu₆ kernel affect the charge distribution of the metal clusters. Furthermore, the larger the number of Ag ions, the greater the effect on the charge distribution.

Next, we simulated the UV-vis absorption spectra of 3 and 4. As shown in Fig. 4a and b, the appearance of shoulder bands in the lower energy region (~410 nm for cluster 3, 405 nm for cluster 4) was well reproduced. The first peak at 403 nm of cluster 3 is mainly due to the transition from HOMO-2 (highest occupied molecular orbital) to LUMO (lowest unoccupied molecular orbital), as shown in Fig. 4c, S54 and Table S6.† The strongest peak at 377 nm is mostly derived from transitions between three occupied molecular orbitals (HOMO, HOMO-1, and HOMO-2) and two unoccupied molecular orbitals (LUMO and LUMO+1). The occupied MOs are localized in the Au kernel, and a large contribution from Ag atoms is observed in the unoccupied MOs. In the case of 4 with four Ag atoms, an onset peak appears around 416 nm, with the strongest peak located around 359 nm. As summarized in Table S7 and Fig. S55,† these absorption peaks originate from transitions among MOs of Au and Ag, and the distribution of orbitals involved is similar to that of 3. Orbital composition analysis by Mulliken partition was then performed for 2-6 (Table S8†). In all clusters, the central C and Au atoms show large contributions (~70%) to the occupied molecular orbitals (HOMO, HOMO-1, and HOMO-2). For the virtual molecular orbitals (LUMO+2, LUMO+1, and LUMO), the ligands

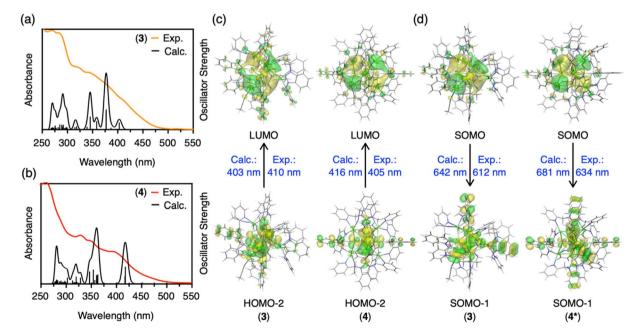


Fig. 4 (a) Calculated and experimental UV-vis absorption spectra of cluster 3. (b) Calculated and experimental UV-vis absorption spectra of cluster 4. (c) Calculated HOMO and LUMO, and comparison of calculated and experimental excitation energies of clusters 3 and 4. (d) Calculated SOMOs (singly occupied molecular orbitals, in the triplet state), and comparisons of calculated and experimental emission energies of clusters 3 and 4*

contribute significantly (\sim 60%) in homometallic clusters 5 and $^{-}$

contribute significantly (\sim 60%) in homometallic clusters 5 and 6, while the silver atoms contribute mainly in LUMO (\sim 30–40%) in heterometallic clusters 2–4.

Finally, we calculated the lowest triplet excited state to estimate the phosphorescence energies of CAu₆Ag₃-type cluster 3 and CAu₆Ag₄-type cluster 4, which were determined as 1.94 (642) nm) and 1.97 eV (629 nm), respectively (Fig. 4d, S56 and Table S9†). However, these results were in conflict with the experimental results, in which clusters 2-4 clearly showed a trend of red-shift. Considering that cluster 4 maintains a fairly symmetric structure in solution, as indicated by the NMR results, we removed the two acetonitrile molecules from cluster 4 and constructed a highly symmetric structure with a T point group, namely $[(C)(Au^{I}-BIPc^{2})_{6}Ag_{4}^{I}](BF_{4})_{6}$ (4*, Table S10 and Fig. S57, S58†). The phosphorescence energy of 4* was calculated to be 1.82 eV (681 nm), supporting a red-shift compared to cluster 3. As shown in Fig. 4d, the SOMOs of clusters 3 and 4* were mainly located in the silver atoms of the clusters, similar to the LUMOs of clusters 3 and 4. On the other hand, a large contribution from the benzimidazolylidene motif of the ligand was observed in the SOMO-1 orbitals of clusters 3 and 4*. These are very different from the occupied MOs of clusters 3 and 4, because the central CAu₆ cores are more involved in HOMO-2 etc. Thus, the calculations indicate that the contribution of the outer shells (ligands and silver atoms) in the phosphorescent relaxation process is significant. Theoretical evaluation of the phosphorescence lifetimes and radiative rate constants of 3 and 4* lead to similar conclusions that the outer shells are significantly involved in each state, which changed the coupling of the spin-orbit states of each cluster (Tables S11 and S12, for the details see ESI†).

Conclusions

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By using pre-designed NHC ligands with one pyridyl, or one or two picolyl pendants, we have achieved atomically precise surface metallization of C-centered $\mathrm{Au_6^I}$ clusters with a specific number of silver(I) atoms. It was confirmed experimentally and theoretically that the NHC-AgI shells contribute significantly to the photoluminescence properties of the resulting heterometallic clusters. Specifically, reducing rigidity will favor non-radiative pathways more, while increasing coverage and protection will efficiently suppress those pathways. This study has precisely elucidated the relationship between heterometallic cluster structure and phosphorescent properties at the atomic level. Advancements in basic design methods for highly photoluminescent metal assemblies confined in organic and organometallic shells are expected.

Data availability

All the data are shown in the ESI.†

Author contributions

Z. L. performed the synthesis, characterizations and analysed the data. P. Z. performed the theoretical calculations. X.-L. P.

assisted in the synthesis and characterizations. H. U., M. E. and M. S. directed the study. All authors prepared the manuscript.

Conflicts of interest

There are no conflicts to declare.

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Notes and references

§ Crystallographic data for BIPc·HCl: $C_{16}H_{18}N_3Cl$, a = 9.26934(12), b =14.15286(15), c = 12.30478(15) Å, $\beta = 111.3536(14)^{\circ}$, $V = 1503.42(3) \text{ Å}^3$, monoclinic space group $P2_1/c$, Z = 4, T = 93(2) K, 9271 reflections measured, 2931 unique (R_{int} = 0.0357), final R_1 = 0.0366, wR_2 = 0.0974 for 2797 observed reflections $[I > 2\sigma(I)]$. For **BIPc**²·HCl: $C_{19}H_{17}N_4Cl·H_2O$, a = 13.3991(2), b = 9.82400(10), c = 13.8269(2) Å, $\beta = 105.9170(10)^{\circ}$, V = 1750.29(4) Å³, monoclinic space group $P2_1/n$, Z = 4, $T = 100.9170(10)^{\circ}$ 93(2) K, 8598 reflections measured, 3359 unique ($R_{\text{int}} = 0.0176$), final $R_1 = 0.0393$, $wR_2 = 0.1039$ for 3247 observed reflections $[I > 2\sigma(I)]$. For $[(C)(Au^I-BIPc)_6Ag_3(-I)]$ $CH_3CN)_3](BF_4)_5$ (3): $C_{103}H_{111}B_5N_{21}F_{20}Ag_3Au_6$, a = 28.2746(8), b = 33.2019(8), c = 28.2746(8)29.4805(10) Å, $\beta = 106.484(3)^{\circ}$, V = 26537.9(14) Å³, monoclinic space group I2/a, Z= 8, T = 93(2) K, 62 923 reflections measured, 25 505 unique ($R_{int} = 0.0481$), final $R_1 = 0.0970$, $wR_2 = 0.2906$ for 15 540 observed reflections $[I > 2\sigma(I)]$. For $[(C)(Au^I)]$ $BIPc^2$)₆ $Ag_4(CH_3CN)_2$](BF₄)₆ (4): $C_{119}H_{102}B_6N_{26}F_{24}Ag_4Au_6 \cdot 2CH_2Cl_2 \cdot CH_3CN$, a = 035.5410(3), b = 15.07664(17), c = 50.5683(5) Å, $\beta = 93.2056(9)^{\circ}$, V = 27.054.0(5) Å³, monoclinic space group I2/a, Z=8, T=93(2) K, 74 304 reflections measured, 26 513 unique ($R_{\text{int}} = 0.0522$), final $R_1 = 0.0605$, $wR_2 = 0.1686$ for 22 778 observed reflections $[I > 2\sigma(I)]$. For $[(C)(Au^{I}-BIPc)_{6}](BF_{4})_{2}$ (5): $C_{97}H_{102}B_{2}N_{18}F_{8}Au_{6}\cdot CH_{2}Cl_{2}$, $a = 13.57251(16), b = 22.5778(2), c = 17.07448(17) \text{ Å}, \beta = 99.9220(11)^\circ, V =$ 5153.99(10) Å³, monoclinic space group $P2_1/n$, Z = 2, T = 93(2) K, 31 050 reflections measured, 10 136 unique ($R_{\text{int}} = 0.0363$), final $R_1 = 0.0496$, $wR_2 = 0.1311$ for 8499 observed reflections $[I > 2\sigma(I)]$. For $[(C)(Au^I-BIPc^2)_6](BF_4)_2$ (6): $C_{115}H_{96}B_2N_{24}F_8$ $Au_6 \cdot CH_2Cl_2$, a = 14.44142(13), b = 43.0804(4), c = 17.47381(12) Å, $\beta = 92.7197(7)^\circ$, $V = 10.858.95(16) \text{ Å}^3$, monoclinic space group $P2_1/c$, Z = 4, T = 93(2) K, 59.653 reflections measured, 21 354 unique ($R_{\rm int}=0.0392$), final $R_1=0.0379,~wR_2=0.0379$ 0.0949 for 18 478 observed reflections $[I > 2\sigma(I)]$. All crystallographic data have been deposited at the CCDC under deposition numbers CCDC 2153516 (for BIPc·HCl), 2153517 (for BIPc²·HCl), 2153518 (for 3), 2153519 (for 4), 2153520 (for 5), and 2153521 (for 6).

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