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Sulfamides direct radical-mediated chlorination of aliphatic C–H bonds†

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Given the prevalence of aliphatic amines in bioactive small molecules, amine derivatives are opportune as directing groups. Herein, sulfamides serve as amine surrogates to guide intermolecular chlorine-transfer at γ -C(sp³) centers. This unusual position-selectivity arises because accessed sulfamidyl radical intermediates engage preferentially in otherwise rare 1,6-hydrogen-atom transfer (HAT) processes through seven-membered transition states. The site-selectivity of C–H abstraction can be modulated by adjusting the steric and electronic properties of the sulfamide nitrogen substituents, an ability that has not been demonstrated with other substrate classes. The disclosed reaction relies on a light-initiated radical chain-propagation mechanism to oxidize C(sp³)–H bonds efficiently.

Introduction

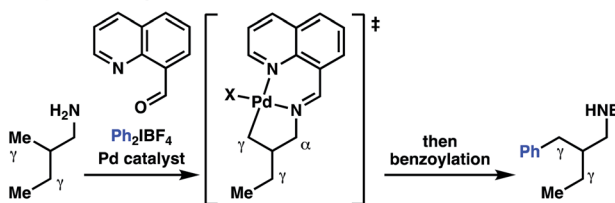
Aliphatic amines are important structural motifs within organic molecules, making alkyl amine derivatives readily available. These derivatives can be used to guide position-selective C–H functionalization reactions¹ to α -,² β -, γ -, and δ -positions.³ Nevertheless, few strategies result in γ -C(sp³)–H functionalization. Amine derivatives template γ -selective cyclometallation processes^{4–6} (Scheme 1A), and can stabilize metallonitrenoid or metalloradical intermediates to facilitate C–H amination reactions (Scheme 1B).^{7–9} As a mechanistic complement to these approaches, herein disclosed is the first reaction in which an amine surrogate guides γ -C(sp³)–H functionalization by way of free radical intermediates,¹⁰ enabling a sulfamide-guided chlorine-transfer process (Scheme 1C).

In these reactions, intermediate sulfamidyl radicals **2** engage in otherwise rare 1,6-HAT processes. With the exception of the recent discovery of sulfamate ester-templated reactions,^{11–13} transformations that employ cleavable linkers in 1,6-HAT processes lack generality. Fortunately, sulfamides appear to direct reactions based on 1,6-HAT processes,¹⁰ consistent with the geometrically originated prediction that elongated S–N bonds (~1.58–1.69 Å)¹⁴ kinetically favor a seven-membered transition state¹⁵ for C–H abstraction.

This concept is developed to enable position-selective chlorine-transfer reactions (Scheme 1C). Alkyl chlorides are durable, yet versatile synthetic intermediates,¹⁶ and can be found in bioactive small molecules.¹⁷ Yet, directed C(sp³)–H

chlorination reactions¹⁸ can be plagued by competitive off-site chlorine-installation arising from unguided C–H abstraction. The developed sulfamide-directed reactions offer high levels of position-selectivity with the unusual ability to predictably modulate site-selectivity based on variations in the steric and electronic properties of the substituents on the sulfamide nitrogen atoms. With appropriate substituents, the site of chlorine-transfer is complementary to that available based on other techniques,¹⁹ including sulfamate ester-guided

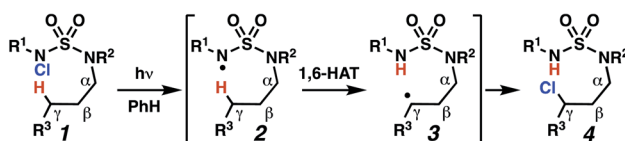
A. Cyclometallation enables γ -functionalization processes Depicted: Dong and co-workers



B. Metallonitrenoids mediate γ -selective amination reactions Depicted: Du Bois and co-workers



C. Free radical intermediates guide chlorine-transfer processes These investigations



Scheme 1 γ -C(sp³)–H reactions of amine derivatives.

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processes,¹¹ traditional Hoffman–Löffler–Freitag protocols,²⁰ templated methods,²¹ and unguided processes that rely on innate selectivity.^{1a,b,22,23}

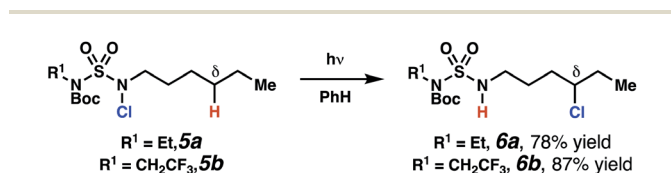
Results and discussion

Sulfamide substrates present two chemically distinct nitrogen atoms that can support nitrogen-centered radicals as reaction

intermediates. To simplify mechanistic investigations, we chose to access sulfamidyl radicals from *N*-chlorosulfamides **1** and **5** via light-initiated nitrogen–chlorine bond homolysis. The requisite sulfamides are prepared from alcohols through Mitsunobu reactions,²⁴ or from amines using a recently disclosed sulfamoylation strategy.²⁵ The generated sulfamides react with an electrophilic chlorinating reagent to provide structurally diverse *N*-chlorosulfamides.

As anticipated, *N*-chlorosulfamides prepared such that the chlorine atom initially resides on the “internal” sulfamide nitrogen (*i.e.*, **5**), engage in selective 1,5-HAT processes upon photoirradiation. These substrates provide δ -chlorinated alkanes **6** in good yield with exquisite selectivity (Scheme 2). As this selectivity mimics that observed in related HLF-type processes, our investigations primarily focus on reactions that target transformation of γ -C(sp³)-H bonds of amine derivatives, as technologies for γ -C(sp³)-H functionalization are limited (Scheme 1).

Building upon our laboratory's interest in transformations governed by 1,6-HAT processes,^{11,13a,d} we sought to exploit *N*-



Scheme 2 Chlorine-transfer from “internal” sulfamide nitrogen occurs through a 1,5-HAT process to provide δ -chlorinated alkanes.

Table 1 Sulfamides guide γ -selective chlorine-transfer reactions

Entry ^a	Product	Yield ^b
1		94
2		93
3		98
4		94
5		94 ^c
6		95
7		81
8		85
9		92
10		95 ^c

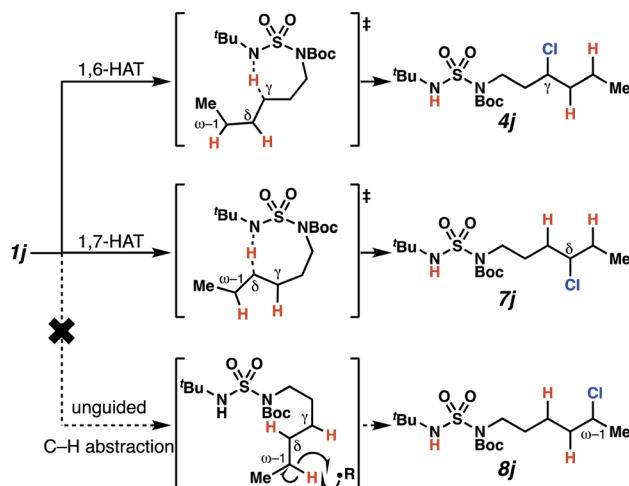
^a Conditions A: 1.0 equiv. *N*-chlorosulfamide **1**, PhH (0.04 M), UV light.

^b Isolated yield. ^c 1.0 equiv. *N*-chlorosulfamide **1**, *i*PrOAc (0.1 M), two 26 W CFL bulbs (1600 lumens).

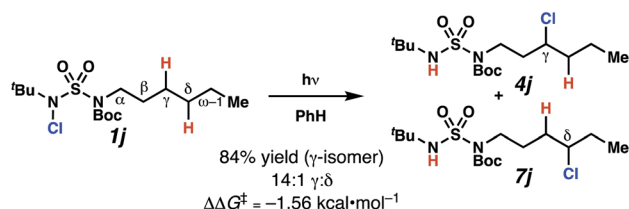
A. Pentyl amine-derived sulfamide generates mixture of γ - and δ -chlorinated isomers



B. With *N*-hexyl sulfamide **1j**, distinct chlorinated isomers would arise via potentially competitive C–H abstraction processes



C. Reaction outcome suggests that 1,6- and 1,7-HAT processes are competitive



Scheme 3 1,6- and 1,7-HAT processes appear competitive.

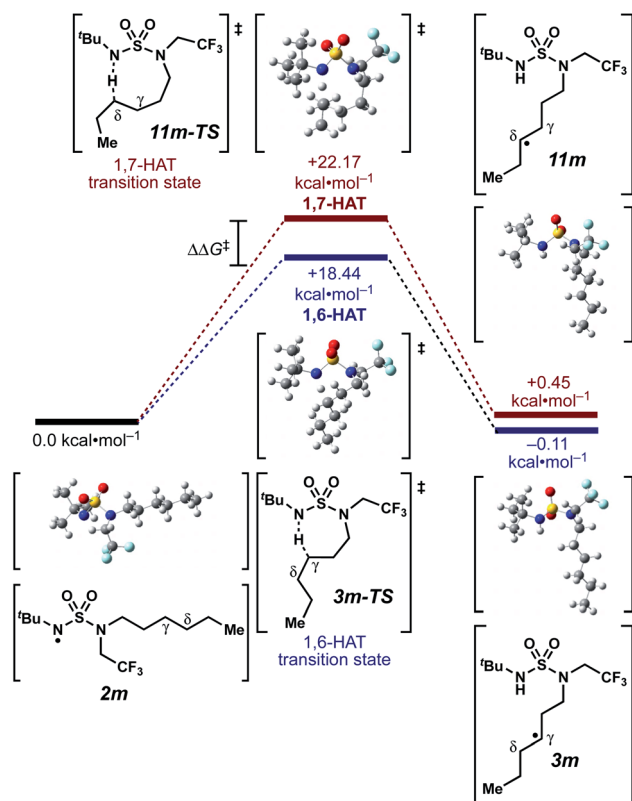


Fig. 1 Representative example of calculated energies and structures for competing 1,6- and 1,7-HAT pathways. Density functional calculations were performed using Gaussian 09 (revision D.01) using the μ B3LYP functional and the 6-31+G(d,p) basis set. See ESI† for further computational details.

This guided chlorine-transfer process overcomes site-selectivity arising from inductive deactivation. Electron-withdrawing groups, such as sulfamides, inductively deactivate proximate C–H bonds to abstraction by electrophilic radicals. Consequently, unguided C–H functionalization reactions engage more distal C–H bonds preferentially. This effect is particularly evident when employing unguided, radical-mediated reaction protocols with 3,7-dimethyloctyl derivatives where the C(7)–H bond serves as the predominant site of oxidation in azidation,²⁷ amination,²⁸ fluorination,²⁹ trifluoromethylthiolation,³⁰ and hydroxylation³¹ processes. By contrast, sulfamide **1h** undergoes templated chlorination at C(3)–H with exquisite site-selectivity (entries 9 and 10).

While the most consistently efficient protocol for chlorine-transfer relies on irradiation with UV light in benzene, some substrates react efficiently in *t*PrOAc upon photolysis with compact fluorescent lights (CFLs, entries 5 and 10).

Surprisingly, sulfamide substrates undergo competitive γ - and δ -chlorination when they incorporate γ -C(sp³)-H bonds in proximity to weaker δ -C(sp³)-H bonds, a phenomenon not generally observed in related sulfamate ester-guided reactions.^{11–13} For example, *N*-pentyl sulfamide **1i** yields a crude 8.8 : 1 mixture of γ - and δ -chlorinated **4i** and **7i** from which γ -chlorinated **4i** can be isolated in 75% yield (Scheme 3A). In

principle, δ -chlorinated minor product **7i** could form *via* either a substrate-guided 1,7-HAT process that relies on an eight-membered transition state, or an intermolecular C–H abstraction process.

To discriminate between these pathways, *N*-hexyl sulfamide **1j** was employed (Scheme 3B). With this substrate, a 1,7-HAT process would generate a δ -chlorinated product, whereas, a reaction reliant on innate selectivity would engage the most distal, secondary C–H bond to form (ω –1)-chlorinated **8j**. This reaction provides a crude 14 : 1 mixture of γ -chlorinated **4j** and δ -chlorinated **7j** (Scheme 3C). Fortuitously, (ω –1)-chlorinated **8j** is not detected, suggesting that δ -chlorinated **7j** may form through a guided 1,7-HAT process.

If a guided 1,7-HAT process provides the δ -chlorinated product, the ratio of γ -chlorinated **4** to δ -chlorinated **7** will quantitatively reflect the energetic difference between transition state barriers for competing 1,6- and 1,7-HAT processes (Scheme 3, Table 2). To relate the measured product ratios to the difference in the transition state barrier heights (Gibbs free energies), we employed the equation

$$(\Delta\Delta G^\ddagger = -RT \ln(\gamma\text{-chlorinated } \mathbf{4}/\delta\text{-chlorinated } \mathbf{7})).$$

The ratio of γ - and δ -chlorinated **4** to **7** is sensitive to variations in substrate structure. Predictably, a C(6) ester inductively deactivates the δ -C-H bond to reaction, such that γ -chlorinated **4k** forms exclusively (entry 1). Unexpectedly, the ratio of γ - to δ -chlorinated **4** to **7** increases as substituents on the tertiary nitrogen of the sulfamide become more electron withdrawing, from *tert*-butoxycarbonyl-, to acetyl-, to trifluoroacetyl-, and 2,2,2-trifluoroethyl-groups (Scheme 3B; Table 2, entries 2–4). This is the opposite of the trend that would be predicted based on BDEs. By contrast, the ratio of γ - to δ -chlorinated products decreases as substituents on the secondary nitrogen of the sulfamide decrease in electron density from *tert*-butyl- to 2,2,2-trifluoroethyl-groups (Scheme 3B; Table 2, entries 5 and 8).

These trends are more evident with substrates bearing γ -secondary C-H bonds and weaker, δ -tertiary C-H bonds (entries 6-8). Moreover, the effects of these trends are synergistic. Indeed, the combination of these trends can be used to favor the formation of δ -chlorinated **7r** as the major product, possibly based on an eight-membered transition state (entry 8).

By contrast, with sulfamate esters **9**, substitution has a less pronounced effect on product ratios, with an influence over the ratio of γ - to δ -chlorinated product isomers that is not statistically significant (Table 2, entries 9–10). Apparently, sulfamate ester- and sulfamide-directed processes differ substantively owing to the marked influence of nitrogen substituents on the site of sulfamide-directed HAT processes. This pronounced effect distinguishes this method from comparable sulfamate ester-templated reactions.

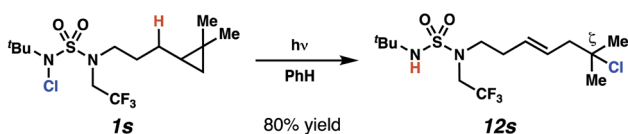
To the best of our knowledge, this is the first series of experimental data to provide evidence of the relative transition state barriers for competitive intramolecular radical-mediated processes. As such, we anticipate that the data published herein can serve as a benchmark that can be used to gauge the quality of computational transition state calculation methods.

^a $\Delta\Delta G^\ddagger = -RT \ln(\gamma\text{-chlorinated product}/\delta\text{-chlorinated product})$ as determined by ^1H or ^{19}F NMR of crude reaction mixture. ^b $\Delta\Delta G^\ddagger = (\Delta G(1,6\text{-HAT TS}) - \Delta G(1,7\text{-HAT TS}))$ as determined from the calculated Gibbs free energies using uB3LYP/6-31+G(d,p).

We set out to evaluate the ability of one of the more commonly recommended functional/basis set combinations to recapitulate qualitative trends in barrier heights associated with the disclosed radical-mediated transformations. To this end, we have modeled the product-determining intermediates (**2**, **3**, **11**) and transition states (**3-TS**, **11-TS**) for a subset of sulfamide and sulfamate ester chlorine-transfer processes using density functional theory (DFT, Fig. 1, Table 3). Using the uB3LYP functional and the 6-31+G(d,p) basis set, we observe that the DFT method over-predicts the stability of the 7-membered ring transition states adopted for 1,6-HAT processes with both sulfamate ester substrates (entries 1 and 2) as well as the hexyl-derived sulfamide substrates (entries 3–5). Within these classes of compounds, calculations qualitatively correlate well with experimental results.

The two feasible reaction paths differ in terms of the carbon-chlorine bond forming events. In a radical-chain propagation process, carbon-centered radical **3h** engages another equivalent of *N*-chlorosulfamide substrate **1h** in chlorine-atom abstraction (Scheme 4). This sequence would produce desired chlorinated

In spite of the rapid speed of radical chain propagation, the generated radical has a long enough lifetime to promote ring-opening of an appropriately positioned cyclopropane (Scheme 5). Upon photoirradiation, *N*-chlorosulfamide **1s** reacts to furnish ring-opened isomer **12s** in 80% yield, with exclusive detection of ring-opened products. This cascade sequence provides position-selective access to a more distally ζ -



Scheme 5 Cyclopropyl-containing substrate provides evidence for radical reaction pathway.

chlorinated product with an intervening olefin. The presence of an intact olefins is interesting, as alkenes are not tolerated under typical *N*-chlorination conditions.

Conclusions

These investigations demonstrate that sulfamides guide 1,6-HAT processes. This mechanistic manifold has been employed to access alkyl chlorides, which are high-value synthetic intermediates. Consequently, this sulfamide-directed process establishes the premise for a broadly translatable γ -C(sp³)-H functionalization approach that complements known alkane functionalization technologies.

Furthermore, these investigations establish that sulfamide substitution can be used to predictably vary the site-selectivity of C–H abstraction processes. Initial calculations have not qualitatively recapitulated experimental trends. Fortunately, the mere ability to experimentally quantify the relative transition state barriers for two competing radical-mediated reaction steps is of benefit as a benchmark for computational methods, where quantitative data relating to barrier heights is scarce.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

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Notes and references

- 1 (a) H. M. L. Davies and J. R. Manning, *Nature*, 2008, **451**, 417;
 (b) T. W. Lyons and M. S. Sanford, *Chem. Rev.*, 2010, **110**,
 1147; (c) J. He, M. Wasa, K. S. L. Chan, Q. Shao and
 J.-Q. Yu, *Chem. Rev.*, 2017, **117**, 8754.
 2 K. Nakajima, Y. Miyake and Y. Nishibayashi, *Acc. Chem. Res.*,
 2016, **49**, 1946.

- 3 J. C. K. Chu and T. Rovis, *Angew. Chem., Int. Ed.*, 2018, **57**, 62; *Angew. Chem.*, 2018, **130**, 64.
- 4 Y. Xu and G. Dong, *Chem. Sci.*, 2018, **9**, 1424.
- 5 (a) V. G. Zaitsev, D. Shabashov and O. Daugulis, *J. Am. Chem. Soc.*, 2005, **127**, 13154; (b) Y. Xu, M. C. Young, C. Wang, D. M. Magness and G. Dong, *Angew. Chem., Int. Ed.*, 2016, **55**, 9084; *Angew. Chem.*, 2016, **128**, 9230; (c) Y. Liu and H. Ge, *Nat. Chem.*, 2017, **9**, 26; (d) Y. Wu, Y. Q. Chen, T. Liu, M. D. Eastgate and J. Q. Yu, *J. Am. Chem. Soc.*, 2016, **138**, 14554; (e) A. Yada, W. Liao, Y. Sato and M. Murakami, *Angew. Chem., Int. Ed.*, 2017, **56**, 1073; *Angew. Chem.*, 2017, **129**, 1093.
- 6 J. Calleja, D. Pla, T. W. Gorman, V. Domingo, B. Haffemayer and M. J. Gaunt, *Nat. Chem.*, 2015, **7**, 1009.
- 7 (a) C. G. Espino, K. W. Fiori, M. Kim and J. Du Bois, *J. Am. Chem. Soc.*, 2004, **126**, 15378; (b) T. Kurokawa, M. Kim and J. Du Bois, *Angew. Chem., Int. Ed.*, 2009, **48**, 2777; *Angew. Chem.*, 2009, **121**, 2815.
- 8 (a) H. Lu, H. Jiang, L. Wojtas and X. P. Zhang, *Angew. Chem., Int. Ed.*, 2010, **49**, 10192; *Angew. Chem.*, 2010, **122**, 10390; (b) H. Lu, Y. Hu, H. Jiang, L. Wojtas and X. P. Zhang, *Org. Lett.*, 2012, **14**, 5158; (c) H. Lu, K. Lang, H. Jiang, L. Wojtas and X. P. Zhang, *Chem. Sci.*, 2016, **7**, 6934.
- 9 X. Xiao, C. Hou, Z. Zhang, Z. Ke, J. Lan, H. Jiang and W. Zeng, *Angew. Chem., Int. Ed.*, 2016, **55**, 11897; *Angew. Chem.*, 2016, **128**, 12076.
- 10 Concurrently, another PI and co-workers have advanced a sulfamide-guided radical-mediated group-transfer process: T. Duhamel, M. D. Martínez, I. K. Sideri and K. Muñoz, *ACS Catal.*, 2019, **9**, 7741.
- 11 M. A. Short, J. M. Blackburn and J. L. Roizen, *Angew. Chem., Int. Ed.*, 2018, **57**, 296–299; *Angew. Chem.*, 2018, **130**, 302.
- 12 S. Sathyamoorthi, S. Banerjee, J. Du Bois, N. Z. Burns and R. N. Zare, *Chem. Sci.*, 2018, **9**, 100.
- 13 (a) K. Muñoz, E. Del Castillo, M. D. Martínez, A. E. Bosnidou, T. Duhamel, C. Q. O'Broin, H. Zhang, E. C. Escudero-Adán and M. Martínez-Belmonte, *Chem.–Eur. J.*, 2018, **24**, 17225; (b) S. K. Ayer and J. L. Roizen, *J. Org. Chem.*, 2019, **84**, 3508; (c) Z.-Y. Ma, L.-N. Guo, Y. You, F. Yang, M. Hu and X.-H. Duan, *Org. Lett.*, 2019, **21**, 5500; (d) A. L. G. Kanegusuku, T. Castanheiro, S. K. Ayer and J. L. Roizen, *Org. Lett.*, 2019, **21**, 6089; (e) W. Shu, H. Zhang and Y. Huang, *Org. Lett.*, 2019, **21**, 6107.
- 14 See ESI† for S–N bond lengths in related sulfamides.
- 15 M. Nechab, S. Mondal and M. P. Bertrand, *Chem.–Eur. J.*, 2014, **20**, 16034.
- 16 W. R. Gutekunst and P. S. Baran, *Chem. Soc. Rev.*, 2011, **40**, 1976.
- 17 G. W. Gribble, *Naturally Occurring Organohalogen Compounds: A Comprehensive Update*, Springer-Verlag, Weinheim, Germany, 2010.
- 18 P. S. Skell and H. N. Baxter, *J. Am. Chem. Soc.*, 1985, **107**, 2823.
- 19 J. Y. Su, D. C. Grünenfelder, K. Takeuchi and S. Reisman, *Org. Lett.*, 2018, **20**, 4912.
- 20 (a) Q. Qin and S. Yu, *Org. Lett.*, 2015, **17**, 1894; (b) J. Ozawa and M. Kanai, *Org. Lett.*, 2017, **19**, 1430; (c) S. P. Morcillo, E. M. Dauncey, J. H. Kim, J. J. Douglas, N. S. Sheikh and D. Leonori, *Angew. Chem., Int. Ed.*, 2018, **57**, 12945; *Angew. Chem.*, 2018, **130**, 13127; (d) E. A. Wappes, A. Vanitcha and D. A. Nagib, *Chem. Sci.*, 2018, **9**, 4500.
- 21 (a) R. Breslow, R. J. Corcoran, B. B. Snider, R. J. Doll, P. L. Khanna and R. Kaleya, *J. Am. Chem. Soc.*, 1977, **99**, 905; (b) R. Breslow and D. Heyer, *J. Am. Chem. Soc.*, 1982, **104**, 2045; (c) H. Guan, S. Sun, Y. Mao, L. Chen, R. Lu, J. Huang and L. Liu, *Angew. Chem., Int. Ed.*, 2018, **57**, 11413.
- 22 (a) T. Brückl, R. D. Baxter, Y. Ishihara and P. S. Baran, *Acc. Chem. Res.*, 2012, **45**, 826; (b) T. Cernak, K. D. Dykstra, S. Tyagarajan, P. Vachal and S. W. Krska, *Chem. Soc. Rev.*, 2016, **45**, 546.
- 23 (a) R. A. Quinn, Z. A. Könst, S. E. Michalak, Y. Schmidt, A. R. Szklarski, A. R. Flores, S. Nam, D. A. Horne, C. D. Vanderwal and E. Alexanian, *J. Am. Chem. Soc.*, 2016, **138**, 696; (b) W. Liu and J. T. Groves, *J. Am. Chem. Soc.*, 2010, **132**, 12847; (c) W. Liu and J. T. Groves, *Acc. Chem. Res.*, 2015, **48**, 1727; (d) G. Li, A. K. Dilger, P. T. Cheng, W. R. Ewing and J. T. Groves, *Angew. Chem., Int. Ed.*, 2018, **57**, 1251; (e) S. Liu, Q. Zhang, X. Tian, S. Fan, J. Huang and A. Whiting, *Green Chem.*, 2018, **20**, 4729; (f) F. Minisci, R. Galli, A. Galli and R. Bernardi, *Tetrahedron Lett.*, 1967, **8**, 2207; (g) N. C. Deno, R. Fishbein and J. C. Wyckoff, *J. Am. Chem. Soc.*, 1971, **93**, 2065.
- 24 Y. Iso, T. Irie, T. Iwaki, M. Ku, Y. Sendo, K. Motokawa and Y. Nishitani, *J. Antibiot.*, 1996, **49**, 478.
- 25 (a) J. M. Blackburn, M. A. Short, T. Castanheiro, S. K. Ayer, T. D. Muellers and J. L. Roizen, *Org. Lett.*, 2017, **19**, 6012; (b) M. F. Shehata, M. A. Short, M. A. Sanders and J. L. Roizen, *Tetrahedron*, 2019, **75**, 3186.
- 26 *CRC Handbook of Chemistry and Physics*, ed. John R. Rumble, 98th edn, (Internet Version 2018), CRC Press/Taylor & Francis, Boca Raton, FL, 2018.
- 27 (a) A. Sharma and J. F. Hartwig, *Nature*, 2015, **517**, 600; (b) K. A. Margrey, W. L. Czaplyski, D. A. Nicewicz and E. J. Alexanian, *J. Am. Chem. Soc.*, 2018, **140**, 4213; (c) X. Li and Z.-J. Shi, *Org. Chem. Front.*, 2016, **3**, 1326.
- 28 F. Collet, C. Lescot, C. Liang and P. Dauban, *Dalton Trans.*, 2010, **39**, 10401.
- 29 (a) C. Gal, G. Ben-Shoshan and S. Rozen, *Tetrahedron Lett.*, 1980, **21**, 5067; (b) S. Rozen and C. Gal, *J. Org. Chem.*, 1987, **52**, 4928.
- 30 S. Mukherjee, B. Maji, A. Tlahuext-Aca and F. Glorius, *J. Am. Chem. Soc.*, 2016, **138**, 16200.
- 31 J. M. Howell, K. Feng, J. R. Clark, L. J. Trzepkowski and M. C. White, *J. Am. Chem. Soc.*, 2015, **137**, 14590.
- 32 (a) N. Mardirossian and M. Head-Gordon, *Mol. Phys.*, 2017, **115**, 2315; (b) A. J. Cohen, P. Mori-Sánchez and W. Yang, *Chem. Rev.*, 2012, **112**, 289; (c) X. Xu, I. M. Alecu and D. G. Truhlar, *J. Chem. Theory Comput.*, 2011, **7**, 1667.
- 33 M. A. Cismesia and T. P. Yoon, *Chem. Sci.*, 2015, **6**, 5426.
- 34 C. G. Hatchard and C. A. Parker, *Proc. R. Soc. London, Ser. A*, 1956, **235**, 518.