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## Stood-up drop to determine receding contact angles

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The wetting behavior of drops on natural and industrial surfaces is determined by the advancing and receding contact angles. They are commonly measured by the sessile drop technique, also called goniometry, which doses liquid through a solid needle. Consequently, this method requires substantial drop volumes, long contact times, tends to be user-dependent, and is difficult to automate. Here, we propose the stood-up drop (SUD) technique as an alternative to measure receding contact angles. The method consists of depositing a liquid drop on a surface by a short liquid jet, at which it spreads radially forming a pancake-shaped film. Then the liquid retracts, forming a spherical cap drop shape (stood-up drop). At this quasi-equilibrium state, the contact angle ( $\theta_{\text{SUD}}$ ) closely resembles the receding contact angle measured by goniometry. Our method is suitable for a wide variety of surfaces from hydrophilic to hydrophobic, overcoming typical complications of goniometry such as needle-induced distortion of the drop shape, and it reduces user dependence. We delineate when the receding contact angle can be obtained by the stood-up method using volume-of-fluid (VoF) simulations that systematically vary viscosity, contact angle, and deposited drop volume. Finally, we provide simple scaling criteria to predict when the stood-up drop technique works.

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## 1 Introduction

Wetting<sup>1</sup> is ubiquitous in nature and technology, shaping phenomena such as drops rolling off plant leaves, animal skin, and insect wings, as well as applications including inkjet printing,<sup>2</sup> coatings,<sup>3</sup> forensics,<sup>4</sup> disease detection,<sup>5</sup> and DNA analysis.<sup>6</sup> Surface wettability is characterized by measuring contact angles. Primarily, three types of contact angles exist: Young–Dupré’s (equilibrium) contact angle,  $\theta_Y$ , advancing contact angle,  $\theta_a$ , and receding contact angle,  $\theta_r$ . Despite their relevance, measuring the different contact angles still remains

challenging, in particular measuring  $\theta_r$  due to distortions of the drop shape by the needle. Therefore, a needle-free method to measure the receding contact angle would be desired.

At thermodynamic equilibrium, a stationary drop on a solid adopts  $\theta_Y$  owing to the interfacial tension balance at the three phase contact line and follows Young–Dupré’s equation:<sup>7</sup>

$$\cos \theta_Y = \frac{\gamma_{\text{SG}} - \gamma_{\text{SL}}}{\gamma_{\text{LG}}} \quad (1)$$

where  $\gamma_{\text{SG}}$ ,  $\gamma_{\text{SL}}$  and  $\gamma_{\text{LG}}$  are the solid–gas, solid–liquid and liquid–gas interfacial tensions, respectively. It is important to point out that the Young–Dupré’s contact angle is a theoretical concept, often attributed to the static contact angle of sessile drops.<sup>8–12</sup> Although the static contact angle can classify surfaces as hydrophilic, hydrophobic and superhydrophobic, it provides little information on how drops adhere to, or roll or slide over a surface.

When the three-phase contact line moves, advancing of the liquid front yields  $\theta_a$ , whereas retraction over an already wetted region yields  $\theta_r$ . Both angles are affected by surface properties such as roughness and chemical heterogeneity,<sup>13</sup> surface adaptation,<sup>14</sup> and slide electrification.<sup>15</sup> In practice, contact angles of resting drops lie within  $[\theta_r, \theta_a]$ ; these bounds characterize wetting ( $\theta_a$ ) and de-wetting ( $\theta_r$ ) behavior on a given surface. The receding angle is indispensable for modeling drop

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removal. For example, the pull-off force per unit length is  $\gamma_{LG}(1 + \cos \theta_r)$ .<sup>16,17</sup> Lower  $\theta_r$  promotes residual drops during withdrawal ( $\theta_r < 90^\circ$ ), and  $\theta_r$  correlates with practical adhesion in anti-icing<sup>18,19</sup> and anti-biofouling<sup>20,21</sup> applications. Moreover,  $\theta_r$  predicts instabilities of receding lines, the occurrence and duration of rebound,<sup>22</sup> and drop-surface friction,<sup>23</sup> making it central to drop dynamics on solids.<sup>23–26</sup>

Standard measurements of  $\theta_a$  and  $\theta_r$  use sessile-drop goniometry: a needle injects liquid into a sessile drop to increase volume (advancing), then withdraws to decrease volume (receding). Despite algorithmic advances,<sup>27–32</sup> this protocol has drawbacks. The needle perturbs the free surface (capillary rise) and especially biases  $\theta_r$  at small volumes; needle position can alter the contact-line speed. Typical devices require samples of a few cm<sup>2</sup> and volumes of  $\sim 30$ – $50$   $\mu\text{L}$  to reach  $\theta_r$ , limiting heterogeneous or small specimens. The inflow/outflow cycle and setup time render the method time-consuming and user-dependent.<sup>33</sup> An alternative approach has also been proposed, in which a droplet is deposited through a pre-drilled hole in the substrate.<sup>34</sup> Although this method can prevent needle induced effects, it represents an idealized configuration,<sup>35</sup> which is time consuming and can induce surface damage in fragile samples. This can alter the local topography, compromising the integrity of heterogeneous or patterned surfaces.

Here we introduce the stood-up drop (SUD) method for receding-angle metrology. A short liquid jet (jetting time of a few ms) deposits a thin lamella that spreads radially and then retracts to a spherical-cap drop. After a quasi-equilibrium is reached, the apparent contact angle  $\theta_{\text{SUD}}$  closely approximates  $\theta_r$ . The measurement completes in  $\sim 10$  ms and requires no needle, mitigating deposition artefacts and facilitating automation. We validate SUD by directly comparing  $\theta_{\text{SUD}}$  with  $\theta_r$  across hydrophilic–hydrophobic substrates, and we delineate when  $\theta_{\text{SUD}}$  recovers  $\theta_r$  using direct numerical simulations based on a volume-of-fluid (VoF) technique that systematically varies viscosity, static contact angle, and deposited volume. Finally, we summarize simple scaling criteria that predict the SUD regime and practical volume limits, and we highlight conditions under which SUD can fail (*e.g.*, violent oscillations or detachment on highly hydrophobic surfaces). Together, these results position SUD as a fast, needle-free alternative for robust receding-angle characterization.

## 2 Materials and experimental methods

### 2.1 Experimental setup: stood-up drop (SUD) device

To form drops from a liquid jet, a device designed by KRÜSS company was used. The device generates a liquid jet by applying a constant pressure  $P_{\text{app}}$  to a liquid reservoir (Fig. 1a), which is connected to a valve and nozzle. The distance between sample and nozzle was kept at 4 mm. The applied pressure  $P_{\text{app}}$  was varied between 100 and 700 mbar. The time at which the valve is open (jetting time  $\tau$ ) can be controlled by software. It should not exceed a few milliseconds to ensure the formation of a thin lamella. If not stated otherwise,  $\tau = 1$  ms is used. A

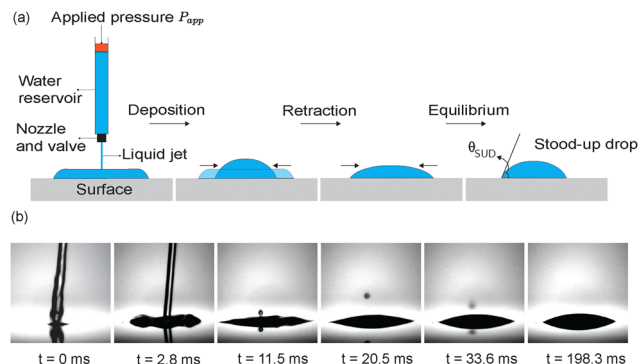


Fig. 1 (a) Experimental setup for SUD technique. A liquid jet is generated at certain applied pressure  $P_{\text{app}}$  for a very short jetting time  $\tau$ . Once the liquid impacts the sample surface, it spreads radially and then retracts. During the first retraction phase the drop can vibrate, before the contact line smoothly recedes. The liquid forms a drop with a spherical-cap shape, whose contact angle is ( $\theta_{\text{SUD}}$ ). The drop profile in the first column represents the initial configuration of the drop for the numerical simulations. The configuration resembles a pancake shape, similar to that observed in experiments post-impact. The second to fourth columns sketch the retraction of the drop from an initial (lighter shade) to the quasi-equilibrium state (darker shade) as time progresses. (b) Experimental snapshots of a liquid jet impacting on a Si wafer surface at  $P_{\text{app}} = 350$  mbar and jetting time  $\tau = 5$  ms. See also Video S1.

liquid jet is generated immediately after the valve opening. After spreading and retraction of the liquid, a stationary drop is formed (Fig. 1b). Here, the contact angle at this stage ( $\theta_{\text{SUD}}$ ) is measured and compared with  $\theta_r$  obtained by Goniometry technique. We determined  $\theta_{\text{SUD}}$  values by a polynomial fitting method, which was designed by a python code (SI). This code determines the average of  $\theta_{\text{SUD}}$  values from the average of contact angles at the left and right side of drops. Our results consider the  $\theta_{\text{SUD}}$  average of the last 50 frames of each video. For a subset of all investigated samples no high-speed recordings were performed. In such cases, the SUD contact angle was determined using the KRÜSS ADVANCE software after drop deposition using the KRÜSS DS3251 SUD dosing unit.

The liquid impact process is recorded by a high-speed camera (Photron UX10) at up to 8000 fps. Simultaneous high speed-video experiments were performed from the top of the surface, to study the shape of the drop contact area and pinning of the three-phase contact line. Experiments were repeated at least three times for each surface (in some cases five times), with their wetting nature ranging from hydrophilic to hydrophobic. For each droplet, the contact angle was obtained by averaging the left and right contact angles, and then the mean and standard deviation were calculated across repeated experiments.

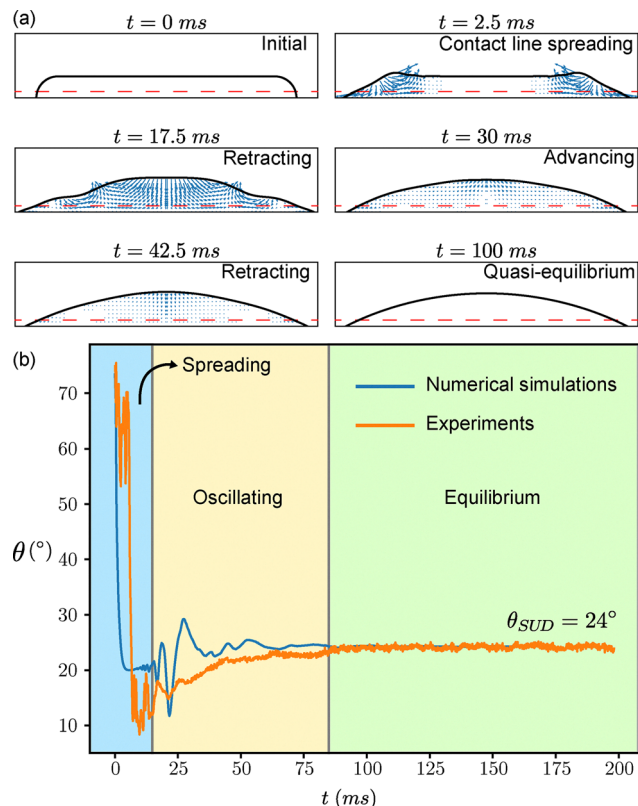
### 2.2 Receding contact angle measurements

Receding contact angles  $\theta_r$  were measured by the sessile drop method/Goniometer (KRÜSS, DSA100). First, a 0.5  $\mu\text{L}$  drop of Milli-Q water (18 megaohm) is deposited on the sample. Then, the baseline is positioned at the contact line between drop and surface, while the needle is adjusted to be in the middle of the drop. Afterwards, the volume is increased up to 50  $\mu\text{L}$  at a flow









**Fig. 3** (a) Snapshots of a simulated drop with static contact angle  $\theta_s = 27^\circ$  and volume of  $0.5 \mu\text{L}$ . The arrows represent the velocity profile inside the drop to visualize whether the drop is in the retracting or advancing phase. The dashed red line represents the height at which the contact angles are measured, in line with experimental conditions. (b) Comparison of measured contact angle from numerical simulations and experiments, as a function of time for the simulation shown in (a).  $\tau = 1 \text{ ms}$ .

(Fig. 3a) in our simulations. For hydrophilic substrates, the contact line initially spreads to achieve its maximum spreading state. Afterwards, the pancake-shaped drop recoils, converting surface energy back into kinetic energy and viscous dissipation (Fig. 3a), finally forming a static cap-spherical drop characterized by the stood-up contact angle  $\theta_{\text{SUD}}$  (Fig. 3,  $t \approx 100 \text{ ms}$ , Video S1).

In experiments, during spreading, the contact angle significantly decreases until reaching a minimum (Fig. 3b, blue region for both experiments and simulations). The minimum is caused by the large impact pressure, resulting in the formation of a very thin lamellae. As the contact line recedes, first the contact angle oscillates (yellow region). The release of the stored surface energy can cause the oscillations. Oscillations of the contact angle level off after approximately 80 ms at a larger angle.

The temporal development of the contact angle is well reproduced in numerical simulations (Fig. 3b). Oscillations are more pronounced on hydrophobic surfaces (Fig. S1) but they ultimately cease due to viscous dissipation, resulting in a plateau at  $\theta_{\text{SUD}}$  (Fig. 3b, blue line). Since no solid needle is required, effects on the drop shape due to the deposition protocol can be ruled out. This facilitates the fitting procedure to calculate contact angles.

To investigate possible pinning during retraction, we recorded the impacting jet from the top of the substrate using high-speed imaging. No pinning points or residual drops were observed (Fig. 4). The final SUD drop area was clearly circular, Video S2.

## 4.2 Further experimental results

### 4.2.1 Influence of pressure on the observed SUD contact angle.

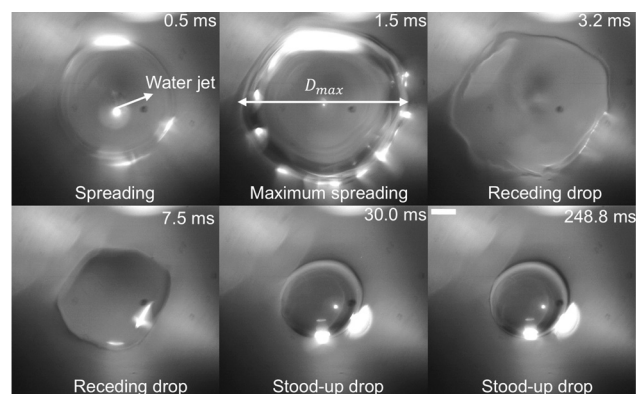
To analyze the influence of pressure on  $\theta_{\text{SUD}}$ , we generate SUD drops at three different applied pressures  $P_{\text{app}}$  (100, 350, and 700 mbar) on PMMA. Our experiments show that  $\theta_{\text{SUD}}$  remains largely unchanged across this pressure range (Fig. S2). As  $P_{\text{app}}$  increases, the liquid impacts the surface with higher speed and kinetic energy, causing the drop to spread further and reach larger maximum diameters  $D_{\text{max}}$ , thus increasing the aspect ratio  $\Gamma$  – an effect analogous to increasing the Weber number  $We$  for impacting drops.<sup>46</sup> Nonetheless, as the drop retracts, memory effects can be excluded. The impacting jet is always turned off before the retraction phase starts. As soon as the drop comes to rest the contact angle converges to a constant value of  $\theta_{\text{SUD}}$  and is independent of  $P_{\text{app}}$ .<sup>47</sup>

We stress that increasing  $P_{\text{app}}$  increases both the flow rate (volume of liquid ejected per unit time during valve opening) and the maximum attainable SUD drop volume. This volume depends on  $P_{\text{app}}$ , the jetting time  $\tau$ , and the nozzle diameter. At the end of the retraction phase, a SUD behaves like a spherical cap with volume (Fig. 4):

$$\Omega = \frac{\pi}{6} H_c (3r^2 + H_c^2), \quad (9)$$

where  $H_c$  and  $r$  are the height and footprint radius of the cap. However, the SUD volume variation is insignificant in our experiments due to the short  $\tau$  used. For instance, on a PMMA surface, the SUD volume increases by  $\sim 0.5 \mu\text{L}$  when  $P_{\text{app}}$  changes from 350 to 700 mbar. An ejected volume that is too large can prevent the SUD state (see Section 4.3.1).

In previous work,<sup>47</sup> we showed that the flow rate—defined by the combination of  $P_{\text{app}}$  and the jet diameter—is the key



**Fig. 4** Top view snapshots of the impacting liquid jet on a PMMA surface. Frame rate: 4000 fps. No pinning points are observed. Pressure: 350 mbar. Jetting time:  $\tau = 1 \text{ ms}$ . Scale bar represents 0.5 mm. White dots correspond to specular reflections.



factor determining the largest drop volume that still achieves the SUD state. If, for a given flow rate, the final drop volume is below a critical threshold, the contact line recedes after dosing, and the drop's rest angle is the receding contact angle  $\theta_r$ . From experiments on six substrates,<sup>47</sup> we identified a phenomenological correlation between the flow rate and the maximum drop volume ensuring SUD dosing.

**4.2.2 Comparison between  $\theta_{\text{SUD}}$  and  $\theta_r$ .** We measured the corresponding  $\theta_{\text{SUD}}$  for different surfaces, from hydrophilic to hydrophobic and compared the values with  $\theta_r$  obtained by the goniometer technique. Our results reveal a good agreement between  $\theta_r$  and  $\theta_{\text{SUD}}$  (Fig. 5). Agreement is slightly worse for a few samples showing particularly low contact angle hysteresis, such as polycarbonate.

Remarkably, SUD technique is suitable for a hydrophilic surface (bare glass slide), overcoming the difficulties of measuring contact angles for these surfaces by the sessile-drop method, caused by evaporation and drop pinning. As the SUD drop forms in a few milliseconds, evaporation does not affect  $\theta_{\text{SUD}}$  values. Moreover, the high-speed of the liquid jet for both spreading and the first period of the retraction phase, avoid efficiently the influence of pinning points on the drop dynamics. These pinning points can prevent the contact line motion during inflation/deflation of drops using goniometry. Determining  $\theta_r$  for a very hydrophilic glass slide using goniometry has proven challenging. However, a contact angle of  $\theta_r = 4.5^\circ$  has been determined previously by capillary bridges.<sup>48</sup> This is in good agreement with our  $\theta_{\text{SUD}}$  values of  $\sim 6^\circ$  (Fig. S3).

Therefore, SUD method arises as a reliable alternative to determine  $\theta_r$  for surfaces with low wettability.

For the case of hydrophobic surfaces like PFOTS and PDMS surfaces, the equilibrium state at which the SUD is formed takes longer time. This occurs due to the capillary oscillations generated during the retraction phase, when the surface energy is converted back to kinetic energy and viscous dissipation.

Drop oscillations can lead to asymmetric contact line motion and the drops can even slide owing to this asymmetry or that of the surface orientation. The effect is more pronounced when the hydrophobicity increases, as shown for the case of Teflon AF on ITO (Fig. S1). The SUD method fails when: (1) insufficient viscous dissipation allows drops to oscillate violently and settle in an advancing phase or (2) rapid receding motion generates enough upward momentum for the drop to detach from the surface. Both situations are common on highly hydrophobic surfaces, where bubble entrainment during rapid retraction can further complicate the dynamics.<sup>49–52</sup> Under these conditions, the SUD state is not the result of a final receding of the contact line, and thus the measured contact angles no longer correspond to  $\theta_r$ . Therefore, the SUD technique requires that the final motion of the contact line is a clear, dominant receding event, which is essential for reliably resembling the receding contact angle.

A particular case arises on highly hydrophobic pillared surfaces. At sufficiently high impact pressures, the liquid jet may impale the surface, leading to a localized Wenzel state at the impact spot. If a clean receding phase is achieved at a given pressure without liquid detachment, the SUD state can still be

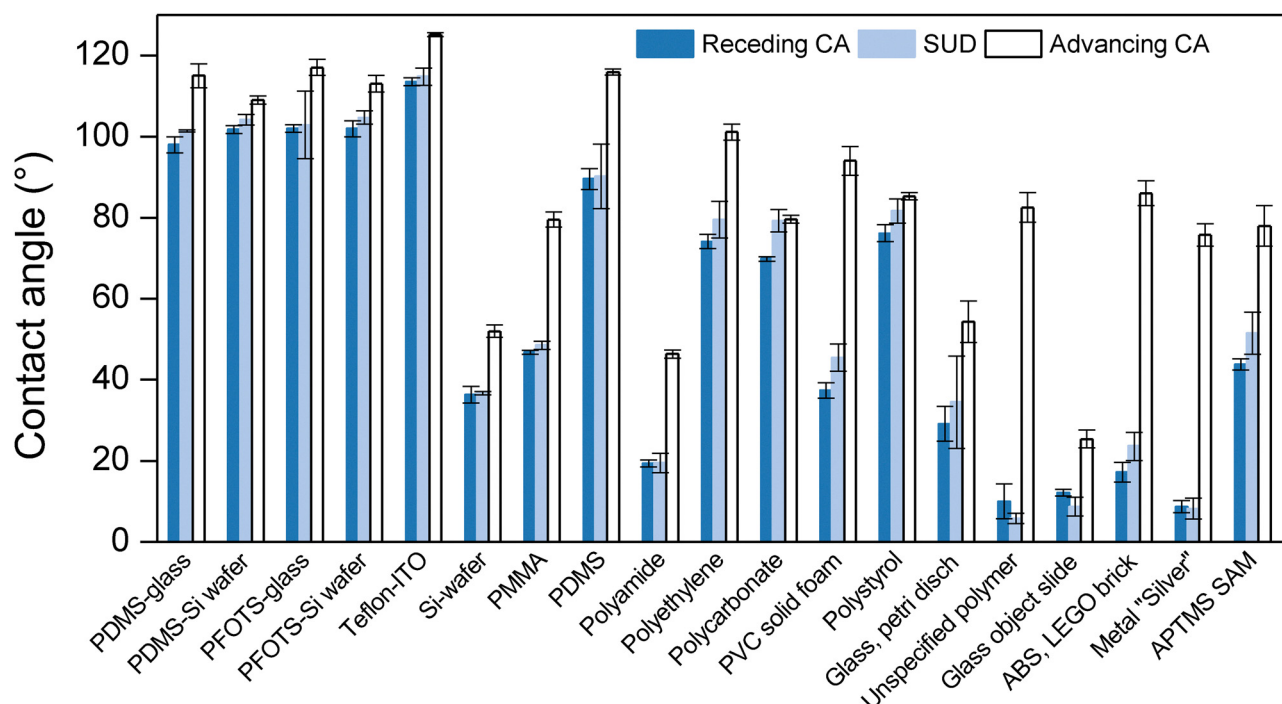


Fig. 5 Comparison between the receding ( $\theta_r$ ) and advancing ( $\theta_a$ ) contact angles measured by goniometry technique (dark blue and white rectangles) and the stood-up contact angles (light blue rectangles) ( $\theta_{\text{SUD}}$ ). Values of ( $\theta_r$ ) and ( $\theta_{\text{SUD}}$ ) are very close, apart from a few samples. For the following samples: PDMS/PFOTS on Si wafer and glass, Teflon on ITO, and Si wafer,  $\theta_{\text{SUD}}$  was measured by the tangent fitting method described in Section 2.3, while the rest of the surfaces by the Young–Laplace fit provided by the goniometer software.



reached. However, at higher pressures the contact line dynamics may be influenced by local liquid penetration, as previously reported for droplets impacting superhydrophobic nanostructured surfaces.<sup>53</sup> This scenario would represent an additional limitation of the SUD method, with underlying physics that lies beyond the scope of the present study.

In the following section, we quantitatively analyze when the SUD method works by systematically exploring the parameter space defined by the Ohnesorge number  $Oh$  and the aspect ratio  $\Gamma$  at three representative static contact angles of  $\theta_s = 60^\circ$  (hydrophilic),  $\theta_s = 90^\circ$ , and  $\theta_s = 120^\circ$  (hydrophobic).

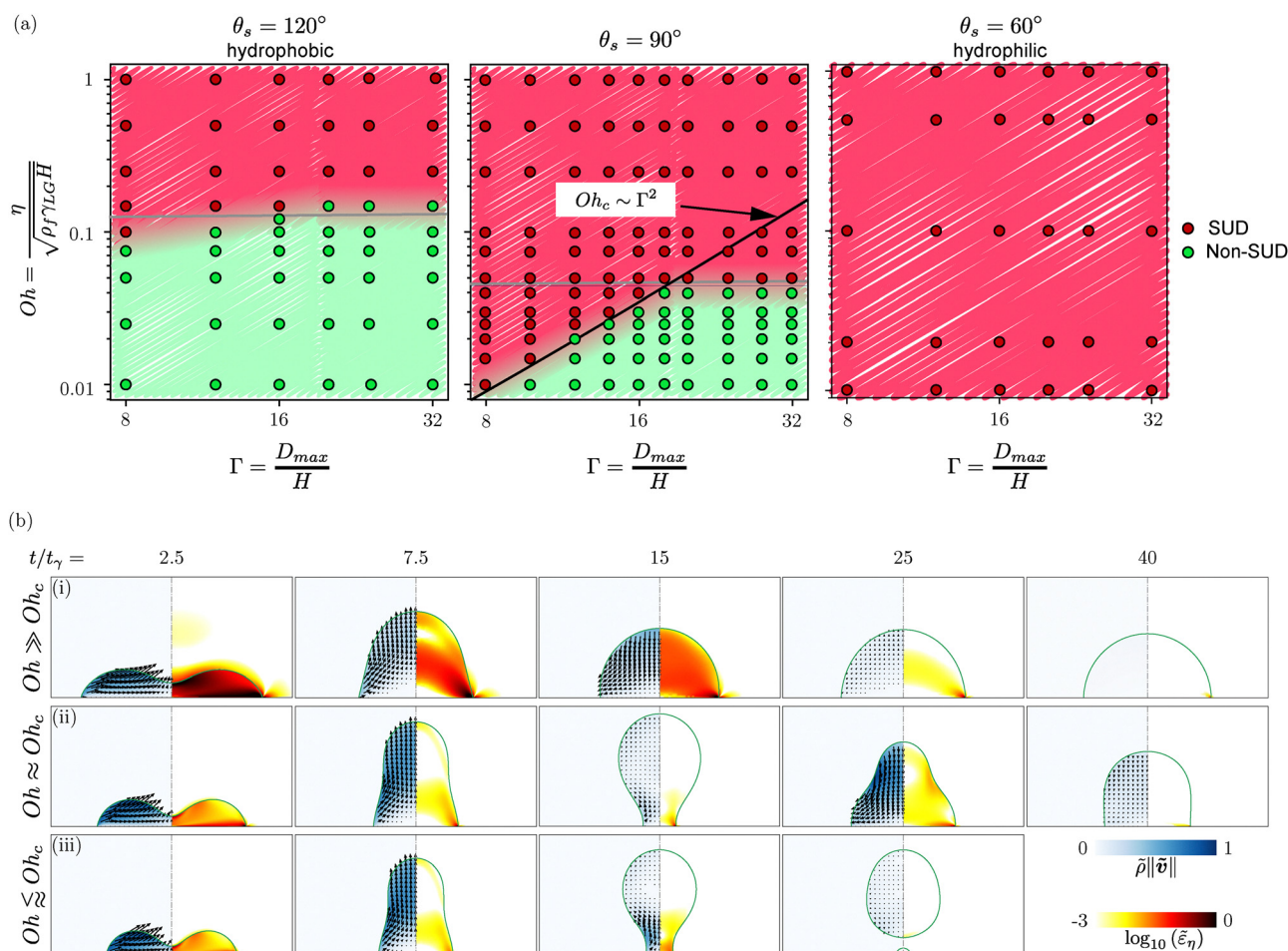
### 4.3 Simulation results for the full $Oh$ – $\Gamma$ parameter space

This section delineates the regions in the  $Oh$ – $\Gamma$  parameter space, for hydrophobic ( $\theta_s > 90^\circ$ ),  $\theta_s = 90^\circ$ , and hydrophilic ( $\theta_s < 90^\circ$ ) surfaces, where SUD is a viable technique. In the SUD regime, the viscous dissipation is sufficient to ensure an overdamped retracting drop that stays on the surface. Additionally, the total volume of the drop (keeping all other material and

flow properties fixed) presents additional constraints on this technique, which is discussed at the end of this section.

**4.3.1 When does the SUD technique work?** For drops smaller than the gravito-capillary length ( $H \ll l_c \equiv \sqrt{\gamma_{LG}/\rho_L g}$ ), the amount of viscous dissipation during the retraction phase largely dictates whether a drop remains attached to the surface after contact line recoiling (SUD regime), with or without oscillations or detaches from the surface (non-SUD regime).<sup>45</sup>

Detached drops often fall back onto the surface. This leads to pronounced oscillations for drops already in a spherical cap shape, which opens the possibility of the final drop at rest to be the result of a wetting process and not of a de-wetting process. Consequently, the contact angle might not resemble the receding angle but rather a contact angle between advancing and receding angle. To systematically characterize the conditions classifying stable SUD formation *versus* detachment, we explored the parameter space spanned by the Ohnesorge number  $Oh$  and aspect ratio  $\Gamma$  across multiple static contact angles  $\theta_s$ , as illustrated in Fig. 6.



**Fig. 6** (a) The  $Oh$ – $\Gamma$  parameter space illustrating regions where SUD is a viable technique for  $\theta = 120^\circ$  (left, hydrophobic),  $\theta = 90^\circ$  (middle), and  $\theta = 60^\circ$  (right, hydrophilic). (b) Numerical simulations of drop evolution for  $\theta = 90^\circ$ ,  $\Gamma = 12$  at  $Oh =$  (i)  $0.75 \gg Oh_c$ , (ii)  $0.025 \approx Oh_c$  – a narrow neck forms at  $\tilde{t} \sim t/t_\gamma = 15$ , but the drop escapes pinch off and continues surface oscillations, and (iii)  $0.022 \ll Oh_c$  – a narrow neck develops which eventually pinches off. Here,  $Oh_c(\Gamma, \theta)$  represents the Ohnesorge number dictating the SUD to non-SUD transition. The left half of every simulation snapshots represents the dimensionless momentum and the right half shows the dimensionless rate of viscous dissipation per unit volume normalized using the inertio-capillary scales, represented on a  $\log_{10}$  scale to differentiate the regions of maximum dissipation. The black arrows depict the velocity vectors inside the drop.



We observe three distinct mechanisms governing the transition between SUD and non-SUD regimes, dependent on the static contact angle:

1. For highly hydrophobic surfaces (large  $\theta_s$ ), contact line dissipation is minimal, and the transition is primarily governed by bulk dissipation overcoming the excess surface energy—analogue to the bouncing-to-non-bouncing transition on superhydrophobic surfaces.<sup>45</sup> In this regime, the critical Ohnesorge number  $Oh_c$  remains approximately constant; drops with  $Oh > Oh_c$  dissipate sufficient energy to remain in the SUD regime, while those with  $Oh < Oh_c$  detach.

2. For intermediate wettability ( $\theta_s \approx 90^\circ$ ), there is a balance between dissipation and released energy as illustrated by the numerical snapshots in Fig. 6(b). For sufficiently large  $Oh$ , dissipation in both bulk and contact line produces SUD behavior, with the drop undergoing overdamped oscillations as it dissipates energy (Fig. 6(b-i)). Near the critical threshold  $Oh_c$ , drops may undergo several oscillation cycles before eventually stabilizing (Fig. 6(b-ii)). The SUD method fails when insufficient viscous dissipation allows drops to oscillate violently and drops settle in an advancing phase. Below  $Oh_c$ , insufficient viscous dissipation leads to detachment, with the liquid neck pinching off as shown in Fig. 6(b-iii).

3. For hydrophilic surfaces (small  $\theta_s$ ), contact line dissipation dominates and effectively suppresses detachment across the entire parameter range investigated – encompassing the parameter space relevant for experimental applications. Consequently, as shown in Fig. 6(a) – ( $\theta_s = 60^\circ$ ), all simulated conditions for hydrophilic surfaces result in stable SUD behavior, making the technique particularly robust for such surfaces.

We develop a theoretical model balancing surface energy and viscous dissipation to quantify these transitions. The initial surface energy of the pancake-shaped drop at  $t = 0$  is  $E_{\text{surf}} = \gamma_{\text{LG}} A_{\text{surf}}$ . To leading order in  $\Gamma$ , the surface area scales as

$$E_{\text{surf}} \sim \gamma_{\text{LG}} H^2 \Gamma^2. \quad (10)$$

During retraction, viscous dissipation<sup>41</sup>

$$E_{\text{diss}} = 2 \int_0^t \int_{\Omega} \eta(\mathcal{D}:\mathcal{D}) d\Omega dt \quad (11)$$

enervates energy from the system. With velocity gradients scaling as  $v_\gamma/\lambda$  (where  $\lambda$  is the characteristic length scale) and dissipation occurring over volume  $\Omega_{\text{diss}}$ , we obtain

$$E_{\text{diss}} \sim \eta \left(\frac{v_\gamma}{\lambda}\right)^2 \tau_\gamma \Omega_{\text{diss}} \sim \eta v_\gamma H \left(\frac{\Omega_{\text{diss}}}{\lambda^2}\right) \quad (12)$$

The dominant velocity gradient arises from shear flow with  $\lambda \sim H$ , giving  $v_\gamma/H$ .

The location of viscous dissipation depends critically on the Ohnesorge number. At high  $Oh$ , velocity gradients develop throughout the drop immediately—analogue to the high-viscosity limit in Taylor–Culick retraction.<sup>54,55</sup> Here, dissipation occurs over the entire bulk volume:

$$\Omega_{\text{diss}} \sim H^3 \Gamma^2 \quad (13)$$

Substituting into eqn (12) yields

$$\begin{aligned} E_{\text{diss,bulk}} &\sim \eta v_\gamma H \left(\frac{H^3 \Gamma^2}{H^2}\right) \\ &\sim \eta V_\gamma H^2 \Gamma^2 \\ &\sim \gamma_{\text{LG}} H^2 \Gamma^2 Oh \end{aligned} \quad (14)$$

When bulk dissipation dominates and balances the released surface energy, we get

$$Oh_c \sim 1, \quad (15)$$

where  $Oh_c$  is the critical Ohnesorge number for SUD behavior.<sup>45,56</sup>

At low  $Oh$ , viscous effects remain localized near the retracting contact line, with the central film region remaining nearly stationary initially. Dissipation concentrates in a boundary layer of volume:<sup>57,58</sup>

$$\Omega_{\text{diss}} \sim \lambda^3 \quad (16)$$

The boundary layer thickness  $\lambda$  is bounded by the drop thickness  $H$  (Fig. 6). With  $\lambda \sim H$ , eqn (12) gives

$$\begin{aligned} E_{\text{diss,CL}} &\sim \eta v_\gamma H \left(\frac{H^3}{H^2}\right) \\ &\sim \eta v_\gamma H^2 \sim \gamma_{\text{LG}} H^2 Oh \end{aligned} \quad (17)$$

When contact line dissipation dominates and balances the surface energy,

$$Oh_c \sim \Gamma^2 \quad (18)$$

These criteria accurately demarcate the SUD and non-SUD regimes in Fig. 6(a) – ( $\theta_s = 90^\circ$ ). At very large  $Oh$  values, the transition becomes controlled primarily by bulk dissipation, resulting in a constant  $Oh_c$  marked by the gray line for  $\theta_s = 120^\circ$  and  $90^\circ$ . Lastly, below a critical static contact angle (exemplified by  $\theta_s = 60^\circ$  in Fig. 6a), the system features only SUD behavior.

A drop detaching from the surface obviously poses serious challenges for measurements using the SUD technique. Such detachment can cause the drop to exit the camera frame, entrain bubbles during pinch-off and redeposition,<sup>52</sup> or significantly increase the time required to reach equilibrium. Furthermore, detached drops often fall back onto the surface, resulting in uncontrolled secondary deposition unlike the controlled jetting process discussed previously.

Indeed, a key takeaway from the numerical simulations is that SUD technique remains viable for hydrophilic surfaces across the entire parameter space, even at extreme combinations of small  $Oh$  and large  $\Gamma$ . For hydrophobic surfaces, however, the technique only works within the restricted range of large  $Oh$  and small  $\Gamma$ . Lastly, we stress that apart from the non-SUD cases discussed in this section, the technique can also fail when surfaces are superhydrophobic, causing the jet to bounce instead of depositing a drop, or when drop breakup occurs (Fig. S4). Analysis of lift-off during jet impingement lies beyond our current scope.





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## Notes and references

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