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Single-atom catalysis enabled by high-energy metastable structures†

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Owing to limited degrees of freedom, the active sites of stable single-atom catalyst (SAC) often have one structure that is energetically much lower than other local-minimum structures. Thus, the SAC adopts one lowest-energy structure (LES) with an overwhelmingly larger proportion than any other high-energy metastable structure (HEMS), and the LES is commonly assumed to be solely responsible for the catalytic performance of an SAC. Herein, we demonstrate with SACs anchored on CeO_2 that the HEMS of an SAC, even though its proportion remains several orders of magnitude lower than the LES throughout the catalytic reaction, can dictate catalysis with extraordinary activity arising from its unique coordination environment and oxidation state. Thus, we unravel the key role of HEMS-enabled catalysis in single-atom catalysis, which shakes the common assumption in the studies of SACs and urges new developments in both experiment and theory to identify and exploit catalysis via HEMSs.

Introduction

Dynamic processes in heterogeneous catalysis have attracted great attention in recent years, owing to the rapid development of *operando* characterization techniques, which provide molecular-level insights into the catalytic process and thus promote the understanding of active sites under reaction conditions.^{1–6} However, it remains a grand challenge for experiments to elucidate the atomistic mechanisms at relevant microscopic timescales for the dynamic processes in heterogeneous catalysis. First-principles modeling presents a theoretical probe to unveil more fundamental and essential aspects, thus shedding light on the structure–performance relationship and catalyst design.^{7,8}

An intricate yet fundamental aspect is the dynamic structural evolution of active sites coupled with catalytic mechanisms,⁹ and this has been well exemplified by theoretical studies of catalysis on supported clusters and nanoparticles.^{7,8,10,11} The active sites of these catalysts are composed of multiple atoms and thus possess large degrees of freedom, which result in ensembles of local-minimum structures (LMSs) that are energetically close¹² and thus accessible to catalysis, based on the Boltzmann distribution.⁸ In addition, the LMSs in the accessible ensembles can vary with the reaction atmosphere, which is induced by adsorptions.^{13,14} These impose challenging complications on deciphering the structure–performance relationships of these catalysts.

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Nevertheless, as the number of LMSs exponentially decreases with the system size,¹² the scenario becomes intrinsically different when the size of the active site is pushed to the limit of a single atom, *i.e.*, the concept of a single-atom catalyst (SAC). Since it was first proposed in 2011,¹⁵ the SAC has developed into a promising design concept for highly efficient heterogeneous catalysts,^{16–19} and it also serves as an ideal model for the study of the structure–performance relationship of catalytic active sites, owing to its well-defined local structure with precise tunability.^{16,20} This exactly arises from the fact that because of the limited degrees of freedom, the active sites of stable SACs often present one lowest-energy structure (LES) dominant in quantity, and the other local minima are high-energy metastable structures (HEMSs) in negligibly low concentrations, as illustrated in Fig. 1.

Thus, it is a sensible and common practice for both experiment and theory to assume that the LES of an SAC is solely responsible for its catalytic performance, and a clear structure–performance relationship can be established. Yet, it has been reported that SACs can reversibly switch between different structures, including cluster forms and varying coordinations,^{9,21,22} in which the different structures are energetically close and thus are accessible with detectable concentrations, while the HEMSs remain reasonably ignored.

Herein, we found that the HEMSs of SACs can significantly contribute to catalysis, even though they remain at negligibly low concentrations throughout the catalytic cycle, which is thus often overlooked in both experiment and theory. By investigating the local minimum structures and phase diagrams of transition metal M (M = Fe, Co, Ni, Cu, Ru, Rh, Pd, Ag, Os, Ir, Pt, Au) SACs (M_1) anchored on the CeO_2 (110) surface (M_1/CeO_2) with density functional theory (DFT) calculations, we identified



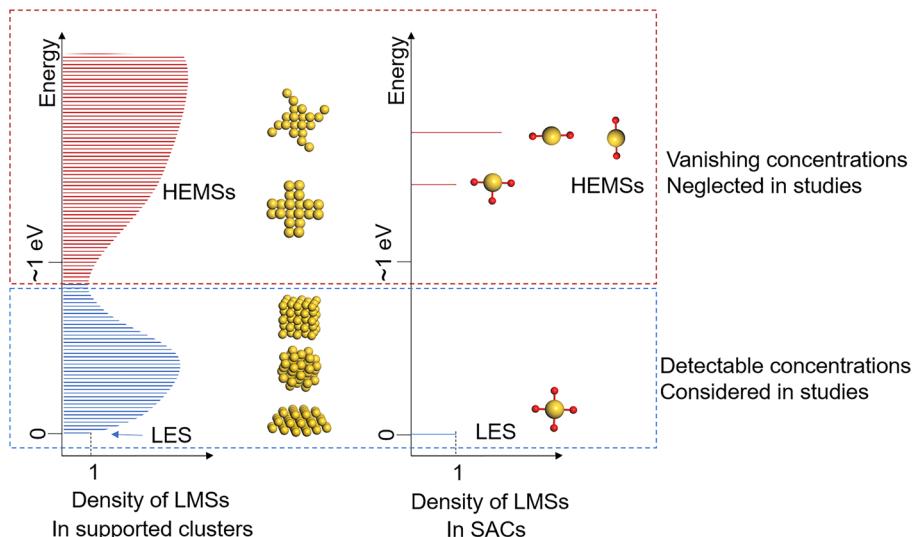


Fig. 1 Schematic illustration of densities of LMSs in supported clusters and SACs. Similar to the electronic density of states for the electronic structure, each LMS is a state of the atomic structure of the system, and the density of LMSs presents the number of all possible LMSs, i.e., the degeneracy, at each energy level for the atomic structure of the system. Arising from large degrees of freedom, supported clusters possess many LMSs that are energetically close to the LES, but the LMSs in SACs other than the LES usually are HEMSS with extremely low concentrations. Because of this intrinsic difference, it is necessary to consider the ensemble catalysis on supported clusters, while a clear structure–performance relationship is commonly assumed for the SAC, based on its LES.

that under a reductive environment, both Au_1/CeO_2 and Pt_1/CeO_2 possess a HEMS of the same type that is energetically higher than the LES by over 0.7 eV and is thus with a negligibly low concentration less than 10^{-5} . However, we demonstrated that this HEMS of Au_1/CeO_2 and Pt_1/CeO_2 SACs plays a key role in delivering the catalysis of reduction reactions by its much higher activity arising from the unique oxidation state of M_1 , and it is thus the HEMS that enables the catalytic performance of SACs for these reactions.

Computational methodology

All periodic DFT calculations were performed with the Vienna *ab initio* simulation package (VASP).^{23–25} The projector augmented wave (PAW)²⁶ method was used for the interactions between the core and valence electrons. The valence electron densities were described by plane-wave basis sets with an energy cutoff of 400 eV.²⁵ The exchange-correlation energies were calculated using the generalized gradient approximation (GGA) with the Perdew–Burke–Ernzerhof (PBE) functional,²⁷ and the spin-unrestricted Kohn–Sham scheme²⁸ was adopted. To partially account for the strong correlation of Ce 4f electrons, a Hubbard U correction was applied, with $U - J = 4.5$ eV.^{29,30} The D3 correction was included to describe the van der Waals interactions.³¹

The thresholds for converging the electronic wavefunctions and atomic structures are 10^{-6} eV for the energy and $0.02 \text{ eV} \text{ \AA}^{-1}$ for the maximal force, respectively. The calculated lattice constant (5.418 Å) and Ce–O bond (2.360 Å) length of the CeO_2 bulk are consistent with experimental results.³² The CeO_2 (110) surface was then modeled by a $p(3 \times 2)$ 5-layer supercell with the bottom 3 layers fixed, and a 15 Å vacuum gap was included

to separate the periodic images along the z -axis. A $2 \times 2 \times 1$ Monkhorst–Pack grid was used to sample the Brillouin zone. Dipole correction along the z -axis was applied.

The Gibbs free energy corrections (including enthalpic and entropic terms) of gas-phase molecules and surface-adsorbed species were calculated with the ideal gas approximation and the harmonic approximation for the vibrational degrees of freedom using the thermochemistry modules of the Atomic Simulation Environment (ASE).³³

Comparisons between electronic affinities with and without relativistic effects were obtained using the ADF program,³⁴ which uses all-electron Slater-type orbitals as basis sets. The relativistic effects are included in the Hamiltonian *via* the zero-order regular approximation (ZORA).³⁵

Microkinetic modeling was conducted using CatMAP³⁶ to explicitly investigate the catalytic kinetics under varying conditions. The partial pressures of all the gas phase reactants were set to 1 bar, while the partial pressures of the gas phase products were set to 0.1 bar for C_2H_2 and 10^{-15} bar for HCOOH to ensure overall exothermic reactions with positive net forward reaction rates. Note that the extremely low partial pressure of HCOOH is in accordance with the experimental conditions (see the note in the ESI†).

Results and discussion

Local-minimum structures and phase diagrams of M_1/CeO_2 SACs

The M_1/CeO_2 SACs present an important family and have been widely studied because of their promising applications^{37–41} and theoretical values.^{42–44} We first investigated all possible LMSs for the twelve groups 8–11 transition metal M_1/CeO_2 SACs ($\text{M} = \text{Fe}$ –



Cu, Ru–Ag, Os–Au), and calculated their phase diagrams under different redox atmospheres (additional details can be found in the ESI discussion and Fig. S1–S12†).

The most stable phase, *i.e.*, the LES of the active site, on each M_1/CeO_2 SAC widely changes with varying atmosphere. In particular, the coordination number of M to O (CN_O) varies among different LESs. In the reductive condition represented by the pressure of H_2 (p_{H_2}), the phase diagrams (Fig. S11 and S12†) indicate that all the M_1/CeO_2 SACs retain a particular type of LES with a CN_O of 2 (labeled as the $M_{\text{subO}-2}$ type) in a wide temperature range at p_{H_2} of 1 bar.

In the LES of the $M_{\text{subO}-2}$ type, the single-atom M is anchored at the O vacancy site and bonds to the two nearest O atoms to form an O–M–O configuration (Fig. 2a). The M atom can lose one of the M–O bonds to form an M–O configuration, and this is labeled as the $M_{\text{subO}-1}$ type (Fig. 2a). Only with M = Cu, Pd, Pt, and Au, can the M_1/CeO_2 SAC adopt $M_{\text{subO}-1}$ as a LMS.

Under the reducing environment with the standard p_{H_2} , $M_{\text{subO}-2}$ is the LES, and $M_{\text{subO}-1}$ is the HEMS that is over 0.7 eV higher in energy (Fig. 2a and Table S1†). Therefore, the concentrations of HEMS ($M_{\text{subO}-1}$) are less than 10^{-5} in the phase diagrams of the active sites of M_1/CeO_2 SACs (Fig. 2b and c), and the active sites dominantly adopt the LES ($M_{\text{subO}-2}$) (Fig. 2d and e). Conventionally, the catalytic performance by such a HEMS has often been overlooked for further investigation. However, this HEMS ($M_{\text{subO}-1}$) has an unusually low CN_O of only 1 (Fig. 2a), and such a highly unsaturated coordination mode of the single-atom M may spark extraordinarily high catalytic activity. Therefore, we further scrutinized the role of this HEMS of the $M_{\text{subO}-1}$ type in catalysis, in comparison with that of the LES of the $M_{\text{subO}-2}$ type.

Catalytic performance by the LES and HEMS

To obtain a panoramic understanding of the contribution of HEMS to catalysis, we investigated the CO_2 hydrogenation reaction (CO_2HR) on the Au_1/CeO_2 SAC and the semi-hydrogenation of acetylene (SHA) on the Pt_1/CeO_2 SAC, which are typical slow and fast catalytic reactions, respectively.^{45,46} Both reactions introduce a reducing environment, and thus, the two M_1/CeO_2 SACs adopt the $M_{\text{subO}-2}$ type as the LES under the standard conditions, with the $M_{\text{subO}-1}$ type as the HEMS (Fig. 2).

Fig. 3a shows the free energy profiles of the reaction pathways for CO_2HR catalyzed by the LES (L-pathway) and the HEMS (H-pathway) of the Au_1/CeO_2 SAC under standard conditions, with structures of all states illustrated in Fig. 3b. In the L-pathway, starting from the LES of the $M_{\text{subO}-2}$ type (L0), the CO_2 molecule prefers to bind with the surface O atom to form a carbonate group (L1, Fig. 3c) instead of weak physisorption on the positively charged Au_1 site of L0 (Fig. S13†). H_2 then easily dissociates into H^+ and H^- on the Lewis pair composed of the carbonate group and Au_1 site (L2) with a small barrier of 0.58 eV (L-TS1). Subsequently, H^- attacks the carbonate group to produce HCOOH (L3), which, however, poses a formidable barrier of 3.31 eV (L-TS2).

In contrast to the L-pathway, CO_2 in the H-pathway can spontaneously and directly bind to the Au_1 site in the HEMS of the $M_{\text{subO}-1}$ type (H1, Fig. 3d) with a bent configuration, indicating a chemisorbed CO_2 . It is subsequently hydrogenated by H_2 *via* an Eley–Rideal (ER) mechanism with a barrier of 1.38 eV (H-TS1) to form the co-adsorbed COOH and H on Au_1 (H2), which combine to produce HCOOH (H3) by overcoming a small barrier of 0.31 eV (H-TS2). Upon releasing HCOOH , the Au_1 site

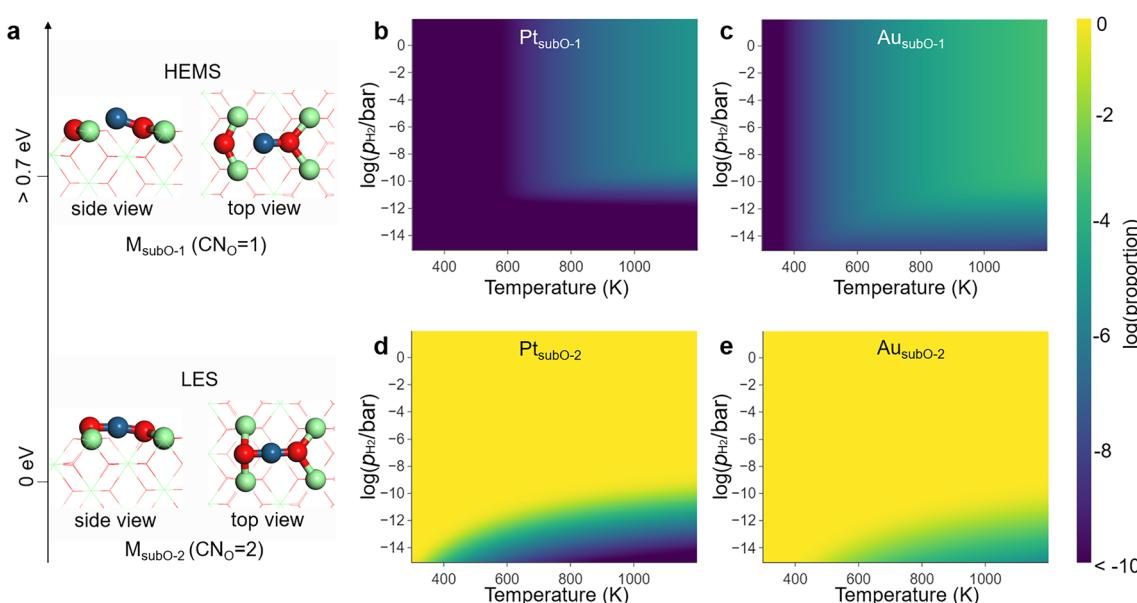


Fig. 2 (a) The $M_{\text{subO}-1}$ and $M_{\text{subO}-2}$ types of structures for active sites in the M_1/CeO_2 SACs. The two are well separated in energy by more than 0.7 eV, with the $M_{\text{subO}-2}$ type being the LES and the $M_{\text{subO}-1}$ type being the HEMS under reductive conditions. The energy gap results in the extremely low concentrations of (b) $\text{Pt}_{\text{subO}-1}$ and (c) $\text{Au}_{\text{subO}-1}$ in the phase diagrams, while the concentrations of (d) $\text{Pt}_{\text{subO}-2}$ and (e) $\text{Au}_{\text{subO}-2}$ dominate the phase diagrams of active sites in the corresponding M_1/CeO_2 SACs under varying temperatures and p_{H_2} (in logarithmic scale). Note that the number of atoms for $M_{\text{subO}-1}$ and $M_{\text{subO}-2}$ are the same, while the dependence of the phase diagram on p_{H_2} arises from the competition among all 8 types of SAC structures considered in Fig. S2–S8,† for which the numbers of O atoms are different.



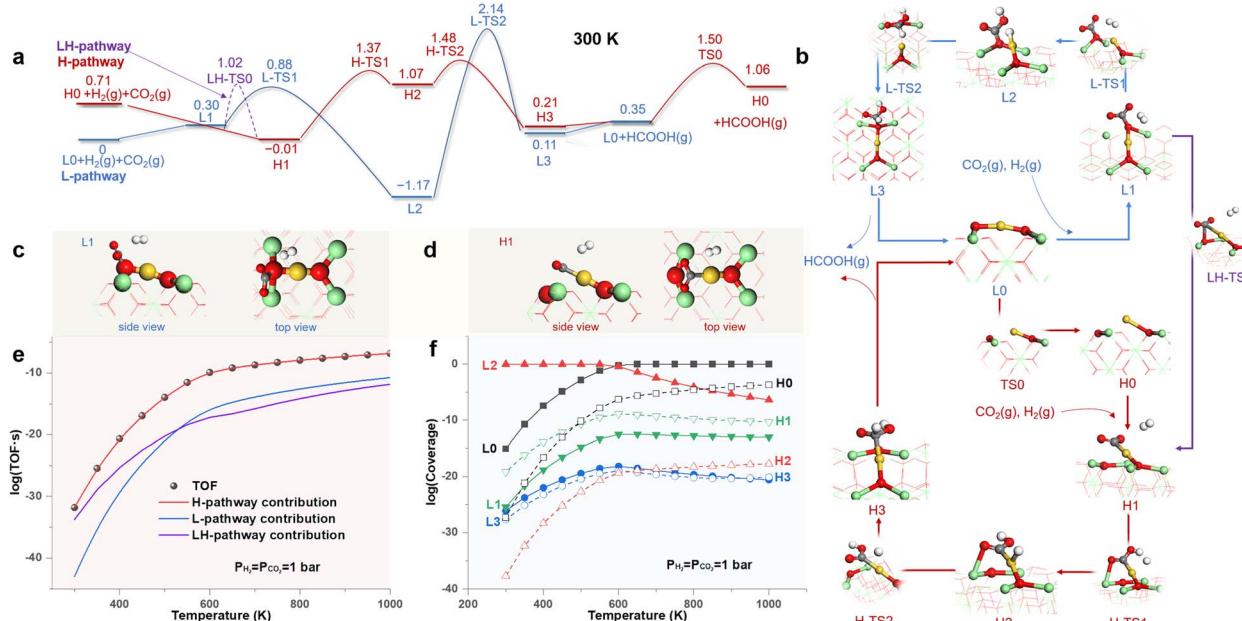


Fig. 3 (a) Free energy profiles (in eV) of CO_2HR on the Au_1/CeO_2 SAC following pathways enabled by the LES (L-pathway) and HEMS (H-pathway). (b) Structures of all states. Configurations of CO_2 activation on (c) the LES and (d) the HEMS. Calculated (e) turnover frequency (TOF) and (f) coverages of states as functions of temperature.

transforms to $\text{L}0$, which recovers $\text{H}0$ by overcoming a barrier of 1.15 eV.

Fig. 3c and d highlights the key difference between the CO_2 activation modes driven by the two types of active sites, *i.e.*, the LES of the $\text{M}_{\text{sub}\text{O}_2}$ type activates CO_2 on its O site to form a carbonate group, while the HEMS of the $\text{M}_{\text{sub}\text{O}_1}$ type chemisorbs CO_2 directly on its Au_1 site to form a bent CO_2 .

In addition, we investigated the direct transformation of $\text{L}0$ to $\text{H}1$ upon the adsorption of CO_2 on Au . This, however, requires the C atom of CO_2 to approach the positively charged Au_1 site of $\text{L}0$, which leads to a large repulsion, and it is more favored for the C atom of CO_2 to bind to the surface O to form $\text{L}1$. Thus, the transformation from $\text{L}0$ to $\text{H}1$ follows a detour through $\text{L}1$ with a barrier of 1.02 eV (LH-TS0 in Fig. 3a) referenced to $\text{L}0$, and this forks to a new pathway labelled as the LH-pathway.

The three pathways, in fact, compose a complex reaction network *via* common states, and thus, they all contribute to the kinetics of catalysis. Therefore, we performed microkinetic modeling³⁶ of this complex reaction network. The results (Fig. 3e) show that the H-pathway dominates the contribution to the TOF, and is larger than those of the L- and LH-pathways by several orders of magnitude. Nevertheless, Fig. 3f shows that the coverages of states in the H-pathway ($\text{H}0\text{--H}3$) are extremely small ($<10^{-19}$ at 300 K and $<10^{-4}$ even at 1000 K), and thus, they remain marginal and barely detectable. In contrast, the state ($\text{L}2$ or $\text{L}0$) in the L-pathway dominates the Au_1/CeO_2 SAC surface at all temperatures considered. Therefore, it is in fact the HEMS with a minuscule concentration, instead of the LES, that drives the CO_2HR on the Au_1/CeO_2 SAC, and the extraordinary catalytic ability of the HEMS arises from the unique oxidation state of its Au_1 site to activate CO_2 , as discussed later.

Fig. 4a shows the free energy profiles of the reaction pathways for SHA catalyzed by the LES (L-pathway) and the HEMS (H-pathway) of the Pt_1/CeO_2 SAC under standard conditions, with the structures of all states illustrated in Fig. 4b. In the L-pathway, the LES of the $\text{M}_{\text{sub}\text{O}_2}$ type ($\text{L}0$) prefers the physisorption of H_2 ($\text{L}1$) to that of C_2H_2 and delivers the dissociative chemisorption of H_2 ($\text{L}2$) by overcoming a barrier of 0.90 eV (L-TS1). Subsequently, C_2H_2 consumes the adsorbed H atoms ($\text{L}3$, Fig. 4c) through an ER mechanism with a small barrier of 0.28 eV (L-TS2) and produces C_2H_4 .

In contrast to $\text{L}0$, $\text{H}0$ in the H-pathway favors strong bonding to C_2H_2 ($\text{H}1$, Fig. 4d), which is exothermic by 2.01 eV. Such strong adsorption of C_2H_2 can couple with the transformation of active sites and leads to a low barrier of 0.59 eV at 300 K (LH-TS1 in Fig. 4a). This forks to a new pathway labeled as the LH-pathway (Fig. 4a) that involves the coupling of C_2H_2 adsorption and $\text{L}0\text{--H}1$ site transformation. However, this low barrier rapidly increases with temperature due to the entropic contribution of gas phase C_2H_2 , and it reaches 1.32 eV at 800 K (LH-TS1 in Fig. S15†). Thus, the transformation of the active site is decoupled from the chemisorption of C_2H_2 , favoring the direct transformation from $\text{H}0$ to $\text{H}1$ at temperatures higher than 710 K (Fig. S15† shows the scenario at 800 K), and this recovers the H-pathway with the initial state of $\text{H}0$.

In the H- and LH-pathways, upon the chemisorption of C_2H_2 ($\text{H}1$), H_2 then hydrogenates the adsorbed C_2H_2 *via* an ER mechanism to produce C_2H_4 by sequentially overcoming two barriers of 0.93 eV (H-TS1) and 0.27 eV (H-TS2). Upon releasing C_2H_4 , the H-pathway reaches $\text{L}0$, which recovers $\text{H}0$ *via* a barrier of 1.23 eV (TS0).

Fig. 4c and d highlights the key difference between the C_2H_2 activation modes driven by the two types of active sites. The LES

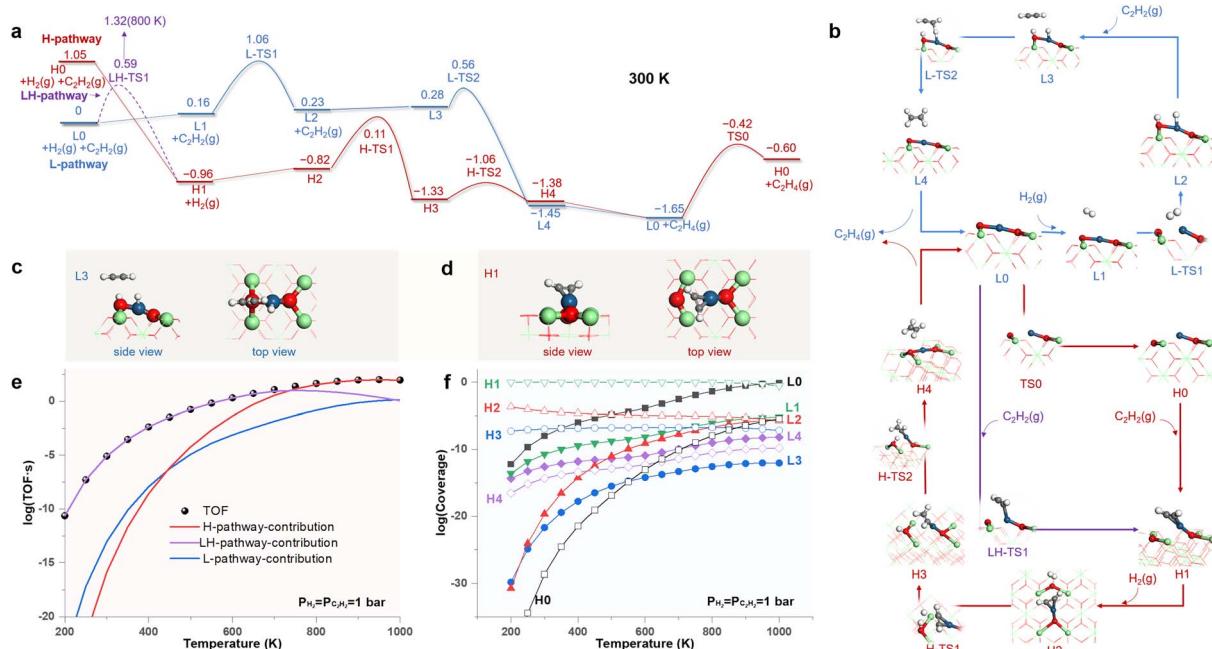


Fig. 4 (a) Free energy profiles (in eV) of SHA on the Pt₁/CeO₂ SAC following pathways enabled by the LES (L-pathway) and the HEMS (H-pathway). (b) Structures of all states. Configurations of C₂H₂ activation on (c) the LES and (d) the HEMS. Calculated (e) turnover frequency (TOF) and (f) coverages of states as functions of temperature.

of the M_{subo-2} type cannot adsorb C₂H₂, and instead, it activates H₂ to the adsorbed H atoms on its Pt and O sites, which then activate C₂H₂. In contrast, the HEMS of the M_{subo-1} type can directly chemisorb C₂H₂ on its Pt₁ site.

We further performed microkinetic modeling³⁶ of the complex reaction network composed of all three pathways in Fig. 4a. The results in Fig. 4e show that the LH-pathway dominates the contribution to the TOF at low temperatures, and the H-pathway dominates the contribution to the TOF at high temperatures. Fig. 4f shows that the Pt₁/CeO₂ SAC surface is dominated by H1 at most of the temperatures because of the strong adsorption of C₂H₂ on the HEMS. Thus, the adsorption state derived from the HEMS is detectable in this scenario, but the HEMS itself (H0) retains a negligibly small coverage (<10⁻³⁰ to 10⁻⁸). Nevertheless, the coverage of LES (L0) increases with temperature and then dominates the Pt₁/CeO₂ SAC surface at 1000 K. Therefore, the HEMS drives the SHA on the Pt₁/CeO₂ SAC at high temperatures, and LES drives the SHA at low temperatures. The extraordinary catalytic ability of the HEMS arises from the unique oxidation state of its Pt₁ site to activate C₂H₂, as discussed below.

Negatively charged M₁ in the HEMS

The oxidation state (OS) of the single-atom metal (M₁) in the SAC is a key characteristic denoting its catalytic capability.^{47,48} The M₁'s in most SACs supported on metal oxides are positively charged,⁴⁹ but their OSs may substantially change as the catalytic reaction proceeds.^{21,22,50} Such evolution of the OS in the SAC may stem from the emergence of metastable states and play a key role in catalysis.⁵¹

We investigated the OSs of M₁'s in the M₁/CeO₂ SACs. Fig. 5a shows the results of the Bader charge analysis,^{52,53} which indicates that the M₁'s in the LES (M_{subo-2} type) of all M₁/CeO₂ SACs are positively charged, but the Pt₁ and Au₁ in the HEMS (M_{subo-1} type) are negatively charged. The Hartree potential difference (ΔV_H)^{54,55} in Fig. S17† also implies similar conclusions. Together with the spin population analysis (Fig. S18†), our results suggest that the OSs of Pt₁ and Au₁ in the HEMS are both -1.

We further calculated the 1s core level shifts of Pt₁ and Au₁ (Table S2†), and the results also indicated that the OSs of Pt₁ and Au₁ in the HEMS are -1. Although there are no clear-cut methods to determine the OS, various analyses provided strong evidence indicating that Pt₁ and Au₁ in the HEMS are negatively charged. This may be similar to the case of negatively charged Au SAC on CuO, which was experimentally observed by *in situ* scanning tunneling microscopy (STM) imaging and X-ray photoelectron spectroscopy (XPS) in a reducing environment.⁵⁶

To understand why Pt and Au can reach negatively charged states, we calculated the electron affinities (EAs) of gas phase metal atoms with and without the relativistic effects (Fig. 5b). If no relativistic effects were taken into account, Pt and Au would have similar EAs to those of Pd and Ag, which were much less likely to take electrons from the support. With including the relativistic effects, Pt and Au possess the largest EAs among all metals. This arises from the contraction and thus stabilization of the 6s orbitals introduced by relativistic effects,⁵⁷⁻⁶⁰ which enables Pt and Au to hold extra electrons.

The negatively charged Au₁ and Pt₁ in the HEMSs serve as strong electron donors that can deliver facile activation of CO₂ and C₂H₂. The differential electron density contour in Fig. 5c illustrates significant electron transfer from Au₁ to CO₂ that

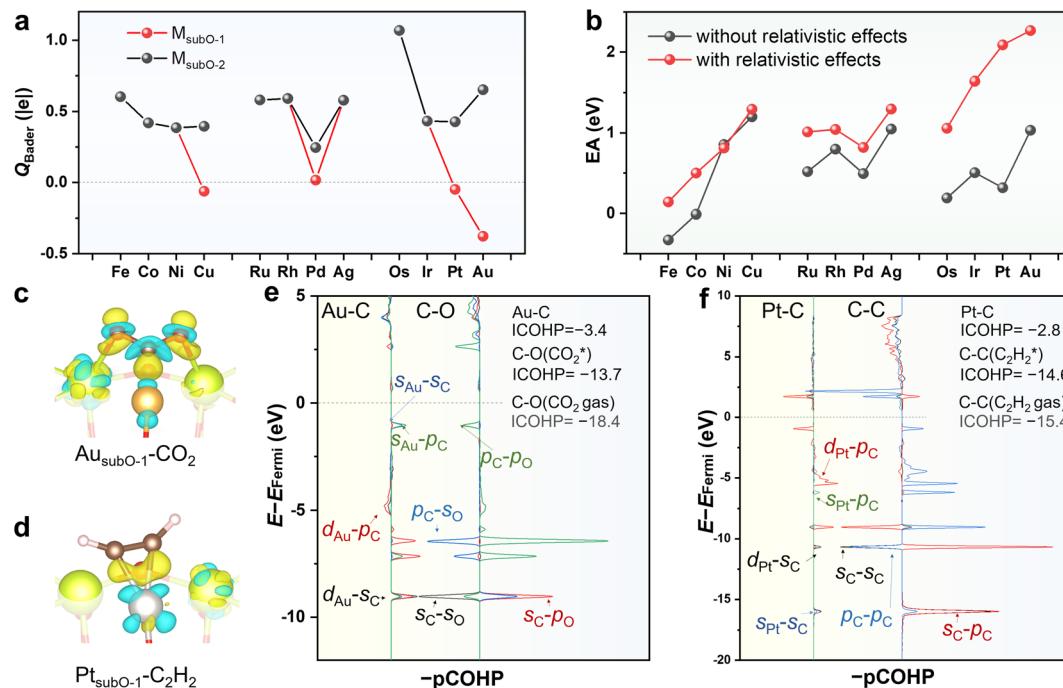


Fig. 5 (a) Bader charges (Q_{Bader}) of M_1 in the $M_{\text{subO-1}}$ and $M_{\text{subO-2}}$ types of M_1/CeO_2 SACs. (b) Calculated electronic affinity (EA) of gas-phase metal atoms with and without the relativistic effects. The differential electron density contours of (c) CO_2 adsorption on $\text{Au}_{\text{subO-1}}$ and (d) C_2H_2 adsorption on $\text{Pt}_{\text{subO-1}}$ (cyan indicates a decrease in electron density, and yellow indicates an increase in electron density upon adsorption). Projected crystal orbital Hamilton population (pCOHP) analyses of (e) CO_2 adsorption on the HEMS of Au_1/CeO_2 and (f) C_2H_2 adsorption on the HEMS of Pt_1/CeO_2 . $E - E_{\text{Fermi}}$ is the energy level referenced to the Fermi level.

subsequently results in a bent $\text{CO}_2^{\delta-}$. The bent $\text{CO}_2^{\delta-}$ forms strong bonding with Au s and d orbitals, as shown by the projected crystal orbital Hamilton population (pCOHP) analysis of Au-C in Fig. 5e, with an integrated COHP (ICOHP) of -3.4 eV. Consequently, the ICOHP of the C-O bond in CO_2 increases from -18.4 eV to -13.7 eV upon adsorption, indicating the presence of greatly weakened C-O bonds.

Similarly, the differential charge density contour in Fig. 5d shows significant electron transfer from Pt_1 to bonding with C_2H_2 that results in a bent C_2H_2 , implying a transition from the sp hybridization of C to sp^2 hybridization. The pCOHP analysis of Pt-C in Fig. 5d indicates strong bonding between C and the s and d orbitals of Pt, with an ICOHP of -2.8 eV. As a result, the C-C bond in C_2H_2 is weakened, as revealed by the increase in the ICOHP of C-C from -15.4 eV to -14.6 eV.

Conclusions

In summary, we demonstrated that the HEMS can play a key role in single-atom catalysis, as illustrated by the two case studies of CO_2HR catalyzed on Au_1/CeO_2 and SHA on Pt_1/CeO_2 , in which the HEMS is overwhelmingly outnumbered by the LES, yet dictates the catalytic performance due to the extraordinarily high activities that arise from the unique oxidation state of M_1 in the HEMS. However, there is difficulty in experimentally detecting these HEMSs with unique oxidation states because of their extremely low concentrations (H_0 in Fig. 3f and 4f) that barely reach the detection limits of operando characterization

techniques. Also, there is difficulty in discovering them with normal *ab initio* molecular dynamics simulations because the high formation energies of HEMSs render extremely low probabilities (as rare events) according to the Boltzmann distribution.

Our finding shakes the common assumption in the studies of SAC that the LES, which is much lower in energy by approximately 1 eV than any other HEMS, is responsible for the catalytic performance of the SAC. Therefore, this urges developments of new methodologies and techniques in experiment and theory to scrutinize the role of HEMS in the structure–performance relationship of SAC. Moreover, the HEMS in SACs may be further promoted and thus exploited with external fields, as in the scenarios of electrochemistry and photochemistry.

Data availability

The dataset of optimized SAC structures in this work is available at the following DOI: [10.5281/zenodo.7638276](https://doi.org/10.5281/zenodo.7638276). The rest of the datasets supporting this work's conclusions are available in the ESI.†

Author contributions

H. X. and Z. X. conceived and designed the study. Z. X. conducted all the theoretical modeling. Z. X. and H. X. wrote the initial manuscript. All authors contributed to the revisions of the manuscript and approved the final version.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

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