

Cite this: *Mater. Adv.*, 2023,  
4, 150Received 28th September 2022,  
Accepted 7th November 2022

DOI: 10.1039/d2ma00935h

rsc.li/materials-advances

# Elucidating the role of disorder introduced by nitrogen in the superconducting properties of tungsten thin films

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Tungsten thin films are successfully prepared by reactive sputtering at room temperature using different Ar/N<sub>2</sub> gas mixtures. The role of disorder and chemical composition in the presence of superconductivity is analyzed. The results show that the crystalline structure of the samples changes drastically due to nitrogen in the mixture increases. A small addition of nitrogen stabilizes the metastable β-W phase, which successively increases its disorder as more nitrogen is added. These changes in the microstructure manifest as an increment in the lattice parameter followed by an amorphization. The electrical transport shows that the β-W stabilized at low N<sub>2</sub> concentrations does not display superconductivity above 2.5 K. Superconductivity with  $T_c$  between 4 K and 4.7 K emerges for disordered β-W and remains in amorphous films. A detailed study of the chemical state and composition indicates that superconductivity may be related more to amorphous structures (nitrides + W) and strained β-W than to β-W as it is stabilized with low nitrogen impurities.

## Introduction

Tungsten is characterized by two different phases: alpha (α)-W (body-centered cubic structure) and beta (β)-W (A15 structure).<sup>1</sup> The latter is metastable,<sup>2</sup> and it is usually stabilized in sputtered films by modifying the deposition parameters<sup>3</sup> or adding nitrogen<sup>4,5</sup> or oxygen impurities in a reactive atmosphere.<sup>6–9</sup> The electrical resistivity of β-W is much higher than that of α-W.<sup>1</sup> Moreover, it displays high spin-orbit coupling (SOC) and type II superconductivity has been observed in disordered thin films.<sup>3,5,10</sup> The SOC converts the material into an exciting candidate for applications in spintronics.<sup>5,6,11</sup> On the other hand, superconductivity with a critical temperature ( $T_c$ ) ranging from 3 to 5 K may be relevant for fabricating devices such as superconducting nanowire single-photon detectors (SNSPDs).<sup>12</sup> However, the origin of superconductivity in disordered W films is unclear. When nitrogen impurities stabilize the β-phase, the films display  $T_c$  up to 4.7 K.<sup>5</sup> The figure agrees with reports for amorphous structures obtained by focused ion beam (FIB) assisted deposition,<sup>13–16</sup> suggesting that disorder at the nano-scale plays a role in the superconducting properties of W

nanostructures. Indeed, nanowires with  $T_c \approx 4.8$  K were obtained by FIB using tungsten hexacarbonyl and a gallium beam where the impurities were mainly C, Ga and O.<sup>13–15</sup> Consequently, one would expect that the origin of superconductivity reported in β-W may be strongly affected by the coexistence of amorphous structures induced by the presence of impurities and disorder.<sup>5,17,18</sup> Regarding nitrides WN<sub>x</sub> (W/N ≥ 1), the system displays two main stable phases: low-temperature hexagonal h-WN and high-temperature cubic c-WN and tungsten subnitride W<sub>2</sub>N.<sup>19</sup> Superconductivity has only been reported for disordered (β-W + WN<sub>x</sub>) thin film growth by reactive sputtering.<sup>17</sup>

Here, we performed a detailed study of the effect of nitrogen addition on the superconducting properties of W thin films grown by reactive sputtering on silicon substrates. We modified the N<sub>2</sub>/Ar ratio in the reactive atmosphere within a range where the film's structure evolved from nanocrystalline (α + β-W) to W amorphous (with high nitrogen content). The crystalline structure was studied by X-ray diffraction (XRD), and its chemical composition was determined using high-resolution X-ray photoelectron spectroscopy (XPS). The structural information was compared with electrical transport measurements to elucidate the origin of the superconducting behavior in nanocrystalline and amorphous W-based thin films.

## Results and discussion

Fig. 1a shows a typical AFM image for a 19.5 nm thick W15 film. The surface is highly flat and free of defects,<sup>20</sup> as evidenced in

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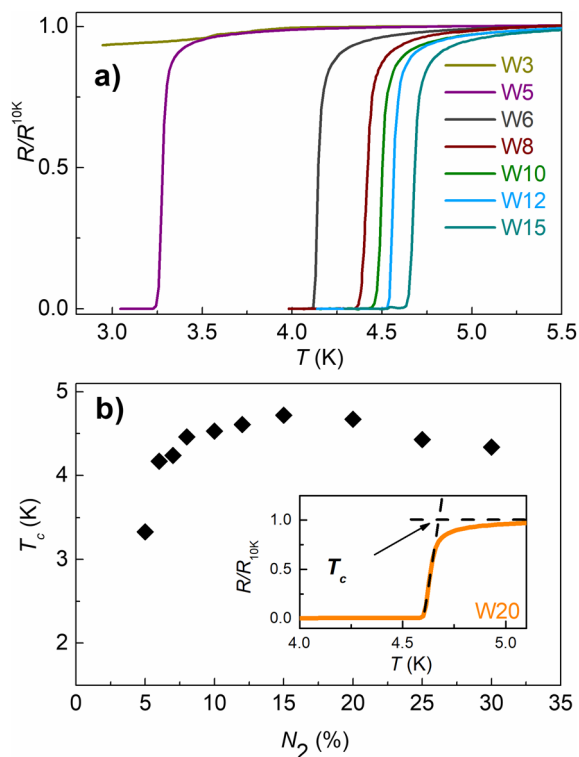


Fig. 3 (a) Temperature dependence of the normalized resistivity for films grown for 1 minute using different reactive Ar/ $N_2$  atmospheres (thickness between 18 and 20 nm). (b) Summary of the superconducting critical temperature as a function of the  $N_2$  concentration in the reactive gas mixture.

resistivity values at 10 K increase faster, adding a small amount of nitrogen from 0.2 to 1.5 to 2  $\mu\Omega$  m for  $\beta$ -phase films and increasing to 3  $\mu\Omega$  m for amorphous samples rich in nitrogen (see Table 1). The results show that superconductivity with percolation and  $T_c = 3.3$  K appears for W5. As nitrogen in the gas mixture increases to 30%,  $T_c$  remains between 4 and 4.7 K reaching a maximum for W15 (see Fig. 3b). This dependence implies that the superconducting behavior does not come from the initially stabilized  $\beta$ -W but rather from the addition of disorder produced by interstitial nitrogen (evidenced in the lattice parameter) or coexistence with amorphous structures. The latter may be a consequence of disordered W or nitrides.<sup>15,17</sup>

To compare the samples beyond  $T_c$ , we measured the upper critical fields ( $H_{c2}$ ) as a function of temperature for the different films. Magnetic field ( $H$ ) was applied perpendicular to the surface ( $S$ ). Fig. 4 summarizes the results using  $T/T_c$  at the  $x$ -axis. The inset corresponds to the curves using the absolute temperature. The dashed lines correspond to the fits using the Werthamer–Helfand–Hohenberg (WHH) model developed for dirty one-band superconductors.<sup>22</sup> The data were fitted considering a Maki parameter  $\alpha = 0$  and spin-orbit scattering constant  $\lambda_{so} = 0$ . For  $\alpha = 0$ ,  $H_{c2}(T)$  is given as the pure “orbital field limit”, corresponding to supercurrents circulating around the vortex cores. The analysis is supported in which the films are highly disordered with a very short mean free path.  $H_{c2}(T)$

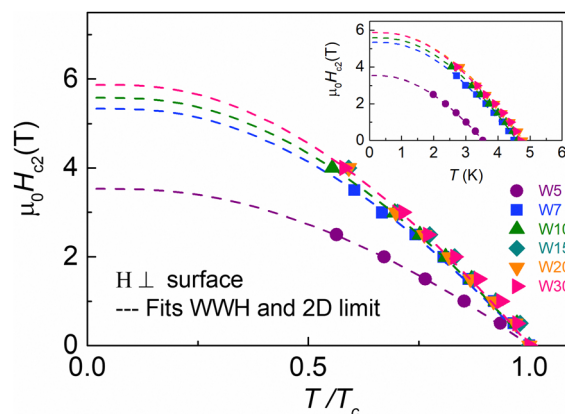


Fig. 4 Upper critical field as a function of the reduced temperature ( $T/T_c$ ) for 20 nm thick W thin film growth using different concentrations of  $N_2$  in the gas mixture. Inset: Similar to the main panel but with absolute temperature in the  $x$ -axis. Dashed lines correspond to the fit using the WHH model for dirty superconductors.

dependences are similar in all the films except for W5 with lower  $T_c$ . All  $\mu_0 H_{c2}(0)$  ( $< 5.8$  T) are lower than those expected from the Pauli limit  $H_p \approx 1.84T_c$  (maximal possible magnetic field strength for a BCS superconductor). The coherence length estimated as  $\xi_{GL}(0) = \sqrt{\Phi_0/(2\pi H_{c2}^{lc}(0))}$  gives  $\xi(0) \approx 7.5$ –7.8 nm for all the films with  $T_c$  higher than 4 K. The results also allow the estimation of the electron diffusion constant  $D = 4k_B/(\pi e d H_{c2}/dT)$  (where  $k_B$  is the Boltzmann constant and  $e$  is the electron charge).<sup>23</sup> The latter is a parameter essential to determine the recombination quasiparticle time (normal electron in Cooper pairs) from the flux-flow instability in micro- and nano-bridges of dirty superconductors.<sup>24</sup>  $D$  is around 0.45  $\text{cm}^2 \text{s}^{-1}$  for all films with  $T_c > 4$  K. This value is similar to the reported for other dirty superconductors used in SNSPD.<sup>25</sup>

Considering the similitude in the superconducting properties and the differences in the X-ray data, we performed XPS measurements to determine the chemical state of the W in the films. For completeness, a W thin film growth in a reactive gas mixture with 50%  $N_2$  was included.<sup>5</sup> XPS measurements were performed to determine the surface chemical composition and chemical state of W films on a sequence of W-based surfaces prepared with increasing the  $N_2$  content in the Ar/ $N_2$  atmosphere during the synthesis, specifically with 0%, 1%, 5%, 10%, 15%, 25% and 50% of  $N_2$  content. The W4f and N1s spectra were analyzed for this sequence. Surface cleaning was performed with  $\text{Ar}^+$  sputtering (2 kV) for 15 min, after which the native oxide  $\text{WO}_3$  disappeared. Fig. 5 shows the W4f spectra as a function of increasing  $N_2$  content during the synthesis. The W4f spectrum consists of  $4f_{7/2}$  and  $4f_{5/2}$  spin-orbit doublet for each oxidation state. The spectra were fitted using Doniach–Sunjic profiles convoluted with Gaussian distributions plus a Shirley-type background. The total fitted intensities along with the experimental ones are shown in each spectrum. For W0, we observe a single component at BE  $\sim 31.47$  eV ascribed to the pure bulk W, in agreement with the reported values of BE  $\sim 31.42$  eV for W (111) and W (001).<sup>26</sup> For W1 and W5, we



Fig. 5 W4f spectra for W thin film growth in reactive gas mixtures with N<sub>2</sub> (%): 0, 1, 5, 10, 15, 25, and 50. With the progressive enhancement of N<sub>2</sub>, we identified different W-based phases:  $\alpha$ -W,  $\beta$ -W, amorphous W, WN<sub>0.2</sub>, and WN<sub>0.6</sub>.

observe the appearance of a new component at lower BE, specifically at BE  $\sim$  31.22 eV, which can be assigned to the  $\beta$ -W phase reported at BE  $\sim$  31.08 eV,<sup>9</sup> or amorphous W reported at BE  $\sim$  31.26 eV,<sup>9</sup> or to a mixture of both. For W10, W15, and W25, a new prominent component shows up at BE  $\sim$  31.4 eV and a minor component at BE  $\sim$  32 eV. The latter can be related to WN<sub>0.2</sub> and WN<sub>0.6</sub>, respectively.<sup>27,28</sup> They appear simultaneously with an increment in the nitrogen content of the films, evidenced by the N1s peak, as discussed below.

Fig. 6 displays the mentioned core-level spectra for W15, W25, and W50, with the same intensity axes at each stage. The N1s peak at BE  $\sim$  397.8 eV, compatible with nitrides,<sup>29</sup> was identified in all cases. The nitrogen signals at W15 could be associated with the W4f component at BE  $\sim$  31.4 eV, from which we can estimate the relative concentration of W/N and associate it with the compound WN<sub>0.2</sub> as obtained by I. Takano *et al.* using ion implantation.<sup>27</sup> In W25 and W50, the N1s peak increases its intensity with the appearance of the W4f component at BE  $\sim$  32 eV, in agreement with the nitride phase reported by M. Wen *et al.*<sup>28</sup> and D. Alegre *et al.*<sup>29</sup> by plasma nitriding. From the relative concentration of W/N, we could associate it with the formation of  $\sim$ WN<sub>0.6</sub>.

The analysis of N1s and W4f peaks also allows a quantitative estimation of the N content. There is no direct relationship



Fig. 6 W4f and N1s spectra for W thin film growth in reactive gas mixtures with N<sub>2</sub> (%): 15, 25, and 50. With the progressive incorporation of nitrogen, we identified different tungsten nitride phases:  $\sim$ WN<sub>0.2</sub> and  $\sim$ WN<sub>0.6</sub>.

between N<sub>2</sub> content in the atmosphere and the resultant stoichiometry. As mentioned above, nitrogen does not incorporate homogeneously in the films due to the coexistence of phases with different W/N ratios. The nitrogen in W5 is negligible but increases to WN<sub>0.2</sub> for W15. On the other hand, the amount of nitrogen in W50 is close to twice the presence in W25. The latter is evidenced by a marked increase in the WN<sub>0.6</sub> component (see Fig. 6).

The summary of results indicates a further correlation between superconductivity and disorder. The  $\beta$ -W stabilizes with a minor amount of nitrogen. However, superconductivity appears for reactive gas mixtures with 5% N<sub>2</sub>, where the lattice parameter of  $\beta$ -W increases due to interstitial disorder and possibly coexist with amorphous structures. For gas mixtures between 7% and 30%,  $T_c$  remains above 4 K, reaching a maximum of 4.7 K at 15%. These samples that initially display XRD peaks corresponding to  $\beta$ -W become amorphous as nitrogen increases in the gas mixture. The XPS data indicate the coexistence of  $\beta$ -W together with chemical bonding corresponding to nitrides. The different WN<sub>x</sub> are evident mainly as changes in the BE of the W component but have imperceptible changes in the BE of the N1s. A similar behavior was observed by Alegre *et al.* in thin films with different amounts of disorder.<sup>29</sup> As we mentioned above, there is a slow diminution of  $T_c$  as the gas mixture increases above 15% and the amorphous phases are enriched in nitrogen. The latter indicates that, as in amorphous WSi<sub>x</sub> and MoSi<sub>x</sub>,<sup>30,31</sup> the maximum  $T_c$  can be associated with specific stoichiometry and disorder. In our results, the temperature dependence and absolute values of the upper critical fields are similar in all the films, which shows that the nature of the superconductivity is the same.

A particular highlight of these samples is that they display  $T_c$  comparable to nanowires obtained by FIB.<sup>13–16</sup> Moreover, the superconducting properties are similar to those observed in amorphous superconductors such as MoSi<sub>3</sub><sup>32</sup> and WSi.<sup>33</sup> The





Fig. 7 Magnetic field dependence of the critical current density,  $J_c$ , for films grown for 1 minute (thickness between 18 and 20 nm). The measurements were performed with the magnetic field perpendicular to the surface of the films. Inset: Typical IV curves in log-log scales and the criterion for the determination of  $J_c$ .

latter are materials typically used for designing SNSPD, characterized by fast response time. The devices require electrical and geometrical homogeneity to guarantee equal response through the wire.<sup>12</sup> Considering that requirement, we test the magnetic field dependence of the critical current density of the samples performing IV curves at 3.5 K. The absolute values of  $J_c$  and its magnetic field dependence usually relate to a balance between intrinsic properties and vortex pinning produced by crystalline defects. Therefore, any severe change in the superconducting volume with chemical composition should be evident. For thin films with thickness lower than the penetration depth ( $\lambda$ ), in addition to crystalline imperfections, the thickness fluctuations and edge quality impact  $J_c$ .<sup>23,34</sup> Fig. 7 shows  $J_c(H)$  for several representative samples. The measurements were performed with the magnetic field applied perpendicular to the surface. The inset to Fig. 7 shows typical IV curves in log-log scales and the criterion for  $J_c$ . The absolute values of  $J_c$  in all the samples are similar with a value of  $\approx 2 \times 10^8$  ( $\text{A m}^{-2}$ ) at  $\mu_0 H = 0.012$  T and these values drop fast as the magnetic field increases. Representing  $J_c(H)$  as a power-law with  $J_c \propto B^{-\alpha}$ ,  $\alpha$  takes values  $\approx 1.3$ . This magnitude in the  $\alpha$  exponent is characteristic of films with negligible bulk vortex pinning, as expected for films with flat surfaces and defects smaller than  $2\xi$ .<sup>35</sup> The similitude in  $J_c(H)$  for samples suggests that inhomogeneities at the nanoscale produced by variations in the chemical environment of the W do not play a role in the vortex pinning. As mentioned above,  $J_c$  for all the films may be determined by edge barriers and possible variations of the strip profile.<sup>34</sup> Indeed, increments of  $J_c$  up to 3 times have been reported for MoSi bridges *via* edge-quality improvement using milling by a focused ion beam.<sup>36</sup>

## Experiment

Nitrogen-doped W thin films were grown by reactive sputtering at room temperature on (100) Si.<sup>5</sup> The base pressure in the

chamber was  $4 \times 10^{-5}$  Pa. The substrate was directly set over a W target (99.99% purity) during deposition. The reactive atmosphere was modified increasing the  $\text{N}_2$  partial pressure in a total ( $\text{Ar} + \text{N}_2$ ) pressure of 0.67 Pa. The study was performed by growing films with  $\text{N}_2$  concentrations (%) of 0, 0.5, 1, 2, 5, 6, 7, 8, 10, 12, 14, 15, 16, 20, 25 and 30. For each concentration, thin films were grown using deposition times of 1 and 3 minutes. To avoid target passivation, before each film, the targets were cleaned by performing sputtering for 3 minutes in pure argon followed by 3 minutes in the corresponding reactive atmosphere. The notation W% corresponds to a tungsten film growth with (%) the percentage of  $\text{N}_2$  in the reactive atmosphere.

X-ray diffraction (XRD) and low-angle X-ray reflectivity (XRR) data were obtained using a Panalytical Empyrean equipment operated at 40 kV and 30 mA with  $\text{CuK}\alpha$  radiation and an angular resolution of  $0.013^\circ$ . The thickness of the films was fitted XRR with the Parratt32 code.<sup>21</sup> XPS was performed in ultra high-vacuum conditions ( $2 \times 10^{-8}$  Pa) using a monochromatic  $\text{AlK}\alpha$  X-ray source (1486.71 eV) and a 150 mm hemispherical spectrometer (Phoibos150, SPECS). For the analysis, the samples were mounted with a adhesive graphitic carbon tape. The binding energy (BE) scale was determined by measuring the Fermi level cut-off. The electrical transport measurements were performed on  $80 \mu\text{m}$  (length,  $L$ )  $\times$   $5 \mu\text{m}$  (width,  $w$ ) using the standard four-terminal transport technique. The bridges were fabricated using optical lithography and argon ion milling. The characteristic current-voltage (IV) curves were obtained with a Keithley Nanovoltmeter Model 2128A and a Keithley Current source Model 6221 AC/DC operating in synchronized mode with a pulse duration of 0.2 ms.

## Conclusions

Tungsten thin films were successfully prepared by reactive sputtering at room temperature using different  $\text{Ar}/\text{N}_2$  gas mixtures. We analyzed the role of the disorder and chemical composition in the presence of superconductivity. The results show that the crystalline structure of the samples changes drastically as nitrogen in the mixture increases. A small addition of nitrogen stabilizes the metastable  $\beta$ -W phase, which successively increases its disorder as more nitrogen is added. These changes in the microstructure manifest as an increment in the lattice parameter followed by an amorphization. The electrical transport shows that  $\beta$ -W stabilized at low  $\text{N}_2$  concentrations does not display superconductivity above 2.5 K. Superconductivity with  $T_c$  between 4 and 4.7 K emerges for disordered  $\beta$ -W and remains in amorphous films. These values are similar to those reported in nanowires obtained by FIB, indicating the fundamental role of amorphous structures in the superconductivity of disordered W nanostructures (independently of the impurity). Our results have important implications for the optimization of superconducting W films and the development of SNSPD.



## Author contributions

J. A. H. and N. H. grew the samples and performed XRD and electrical transport measurements. S. B. and J. A. H. performed XPS measurements and analysis. All the authors contributed equally to the discussion and the writing of the manuscript.

## Conflicts of interest

There are no conflicts to declare.

## Acknowledgements

The authors acknowledge S. Anguiano and B. Pentke for their technical assistance. This work was partially supported by the ANPCYT (PICT 2018- 01597), U. N. de Cuyo 06/C576 and CONICET PIP 2015-0100575CO. SB and NH are members of the Instituto de Nanociencia y Nanotecnología INN (CNEA-CONICET).

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