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# Types of Noncovalent Bonds within Complexes of Thiazole with CF4 and SiF4

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#### Abstract

The five-membered heteroaromatic thiazole molecule contains a number of electron-rich regions that could attract an electrophile, namely the N and S lone pairs that lie in the molecular plane, and  $\pi$ -system areas above the plane. The possibility of each of these sites engaging in a tetrel bond (TB) with CF<sub>4</sub> and SiF<sub>4</sub>, as well as geometries that encompass a CH<sup>..</sup>F H-bond, was explored via DFT calculations. There are a number of minima that occur in the pairing of thiazole with CF<sub>4</sub> that are very close in energy, but these complexes are weakly bound by less than 2 kcal/mol and the presence of a true TB is questionable. The inclusion of zero-point vibrational energies alters the energetic ordering, which is further modified when entropic effects are added. The preferred geometry would thus be sensitive to the temperature of an experiment. Replacement of CF<sub>4</sub> by SiF<sub>4</sub> leaves intact most of the configurations, and their tight energetic clustering, the ordering of which is again altered as the temperature rises. But there is one exception in that by far the most tightly bound complex involves a strong Si<sup>..</sup>N TB between SiF<sub>4</sub> and the lone pair of the thiazole N, with an interaction energy of 30 kcal/mol. Even accounting for its high deformation energy and entropic considerations, this structure remains as clearly the most stable at any temperature.

Keywords: tetrel bond; H-bond; chalcogen bond; electrostatic potential; SAPT; AIM; NBO

#### Introduction

There are numerous Lewis acid-base interactions within the full constellation of noncovalent bonds. Probably the most well studied and understood of this class is the H-bond (HB) AH<sup>..</sup>B where the AH acid molecule accepts a certain amount of charge from the base B. In the most common such bond, it is a lone pair of B which transfers charge into the  $\sigma^*(AH)$  antibonding orbital of the acid <sup>1-5</sup>. The HB is the prototype for a collection of similar bonds in which the bridging proton is replaced by other atoms, most of which are more electronegative than H. Many of these interactions are considered as closely related variants of the general  $\sigma$ -hole bond since they share a common feature consisting of a depletion of electron density along the extension of the R-A covalent bond, where A refers to the atom replacing H. Both this depletion and the resulting positive charge in the molecular electrostatic potential have been termed a  $\sigma$ -hole. Each such  $\sigma$ -hole bond is commonly categorized by the family of the A atom which contains this hole. The halogen atom X contains one such hole <sup>6-14</sup>, while a chalcogen Y atom would typically have two  $\sigma$ -holes <sup>15-27</sup>, one for each of its two R<sub>2</sub>Y covalent bonds. This pattern continues with three  $\sigma$ -holes on the pnicogen Z atom of R<sub>3</sub>Z <sup>28-35</sup>, and four for a tetrel atom T in a R<sub>4</sub>T molecule <sup>21, 36-43</sup>.

The growing accumulation of recent study has collectively developed a set of rules that govern the depth of the  $\sigma$ -hole and its resulting bond. This depth is heavily influenced by both the nature of the bridging A atom and any substituents R to which it is bonded. As one moves down a column of the periodic table, one typically sees a drop in the atom's electronegativity and a rise in polarizability. Both of these trends induce a deepening in the  $\sigma$ -hole and thereby a stronger bond with a base. Likewise, more powerful electron-withdrawing R substituents draw density away from A, aiding in the growth of this hole.

Of course, regions of positive potential are not necessarily limited to  $\sigma$ -holes that lie along these bond axes. It is not uncommon for positive potentials to occur directly above planar molecules <sup>44-58</sup>. For example, the F substituents on hexafluorobenzene extract density from the carbon ring which leaves the area above this ring with a positive potential. Likewise for a simpler molecule such as F<sub>2</sub>CO where the positive region is situated above the C. These positive areas above planar molecules are commonly designated as  $\pi$ -holes, and like their  $\sigma$ -hole cousins, can engage in strong noncovalent bonding with a nucleophile.

The thiazole molecule presents a fascinating assortment of possibilities. Its five-membered heterocyclic ring contains both a N and S atom. A  $\pi$ -orbital of the N atom coalesces with the entire aromatic  $\pi$ -system that also contains two of the S atom's electrons. In addition, the N and S atoms each contain a lone pair that lies in the plane of the ring. In combination with the region lying directly above the aromatic ring, there are thus a myriad of electron-rich regions in thiazole that could attract an electrophile. The four electron-withdrawing F substituents of CF<sub>4</sub> provide the C atom with four  $\sigma$ -holes, each of which have the capability to engage in a tetrel bond (TB) with a nucleophile, as has been demonstrated in the literature <sup>42, 59, 60</sup>. With its higher electropositivity and polarizability, the Si atom of the analogous SiF<sub>4</sub> ought to have deeper  $\sigma$ -holes on the central atom, and serve as a stronger partner in any such TB. Added to these

options, each of the CH groups of thiazole can engage in a H-bond with any of the F atoms of the  $CF_4$  or  $SiF_4$ .

The work described below is designed to explore the entire range of possibilities of bonding arrangements between thiazole and both  $CF_4$  and  $SiF_4$ . The work thus addresses the competition between N and S, and between localized regions of charge buildup on a particular atom versus a more disperse area that lies over a larger aromatic ring. The thiazole unit can serve as electron donor or as acceptor, either within the context of a  $CH \cdot F$  H-bond or in a chalcogen bond involving the S. The comparison between  $CF_4$  and  $SiF_4$  opens a window into the changes effected by moving down just one row in the periodic table with regard to tetrel bond strength with each of the aforementioned electron-rich regions. This inquiry is further motivated by a recent rotational spectroscopic analysis <sup>61</sup> that identified the most stable structure of the thiazole- $CF_4$  pair. However, the computational results suggested a number of alternative geometries, with very similar energetics, but failed to address the nature of the bonding within any of these structures despite their competitive nature.

#### METHODS

Quantum chemical calculations were performed via the density functional approach (DFT), within the context of the M06-2X functional <sup>62</sup>, which has been shown to be an accurate means of treating noncovalent bonds of the sort of interest here <sup>63-73</sup>. An ultrafine grid was used for the M06-2X calculations, and a polarized triple- $\zeta$  def2-TZVP basis set <sup>74</sup> was chosen so as to afford a large and flexible set. Geometries were fully optimized and verified as true minima by the absence of imaginary vibrational frequencies. So as to ensure that all valid minima were identified, geometry optimizations were begun from forty different starting points with various attributes.

The Gaussian 16<sup>75</sup> program was chosen as the specific means to conduct these computations. The interaction energy E<sub>int</sub> of each dyad was calculated as the difference between the energy of the complex and the sum of the energies of the two constituent subunits, each in the geometry they adopt within the dimer. The counterpoise procedure <sup>76</sup> was applied to correct basis set superposition error of E<sub>int</sub>. Interaction energies were decomposed into individual components by the Symmetry Adapted Perturbation Theory (SAPT) approach <sup>77</sup> using the PSI4 program <sup>78</sup>. SAPT0 calculations employed the def2-TZVP basis set. The Multiwfn program <sup>79</sup> was applied to locate and quantify the extrema on the Molecular Electrostatic Potential (MEP) of each monomer. Reduced Density Gradient diagrams were generated via the VMD program <sup>80</sup>. Atoms in Molecules (AIM) bond paths and their associated critical points <sup>81</sup> were located and their properties evaluated with the aid of the AIMAII program <sup>82</sup>. Interorbital charge transfers were monitored via the Natural Bond Orbital (NBO) protocol <sup>83</sup> using the subroutines incorporated within Gaussian 16.

#### RESULTS

The ELF diagram of thiazole in Fig 1a clearly illustrates the lone pairs on both N and S that lie in the plane of the molecule. The molecular electrostatic potential (MEP) surrounding thiazole in Fig 1b presents a roadmap of sorts as to where an electrophile might be attracted. The most negative region, as an extensive red area, lies near the N atom, both in the molecular plane and above it. The minimum in the MEP on a 0.001 au isodensity surface is equal to -34.6 kcal/mol. There is a second, albeit not as strongly negative region, that lies directly above the C-C bond. This minimum is only -8.9 kcal/mol, but still negative enough to attract an electrophile. The area located above the S atom is slightly negative, as denoted by the yellow color, but not enough to actually contain a minimum. Both the CF<sub>4</sub> an SiF<sub>4</sub> molecules contain a classical  $\sigma$ -hole positive region directly along the extension of each F-T bond as witness the blue area in Figs 1c and 1d. Due to its more electropositive character, the Si  $\sigma$ -hole is considerably deeper, with a maximum of 39.4 kcal/mol, as compared to only 19.4 kcal/mol for C. Judging only by the shapes of these MEPs, one might expect the blue  $\sigma$ -hole of TF<sub>4</sub> to be most strongly attracted to the N atom of thiazole, but also to the  $\pi$ -region above the C-C bond albeit less so. The S atom is a possibility as well, but perhaps a dubious one due to the lack of a very negative MEP.



Fig 1. a) ELF diagram showing lone pairs on N and S of thiazole, contour shown is 0.8.
Molecular electrostatic potential (MEP) surrounding b) thiazole, c) CF<sub>4</sub>, d) SiF<sub>4</sub> on surface corresponding to 1.5 x vdW radii. Blue and red colors respectively indicate positive and negative regions, with extrema of a) +20, -10, b) +10, 0, and c) +13, -6 kcal/mol. Maximum (in blue) and minimum (in red) values displayed in kcal/mol.

#### **Dimer Geometries and Energetics**

The thiazole molecule was combined first with  $CF_4$  so as to ascertain all of the minima on the potential energy surface of this pair. Fig 2 illustrates the six different minima that resulted from

this extensive search. The N $\pi$  geometry in Fig 2a places the C atom of CF<sub>4</sub> above the N atom of thiazole, while the CF<sub>4</sub> lies in the molecular plane of N $\sigma$ , aligned with the N lone pair. There are two other geometries where the CF<sub>4</sub> is located above the plane of the ring. It lies nearly directly above the C-C bisector in the C $\pi$  structure, and over the S in S $\pi$ . In a fifth geometry type in Fig 2e, one of the F atoms of CF<sub>4</sub> is positioned nearly along the extension of the C-S bond axis of thiazole, suggestive of a CS<sup>..</sup>F sort of chalcogen bond. There are three CH groups on thiazole, any of which can form a H-bond to a F atom. The one pictured in Fig 2f utilizes the C<sub>1</sub>H atom that lies between the N and S, but the geometries and other features of the two other H-bonded configurations are very similar.



Fig 2. Geometries of complexes between thiazole and CF<sub>4</sub>. Distances in Å, angles in degs.

(Real/mol)										
	I	Ŧ	ZP	VE	E+Z	<b>PVE</b>	G(29	98 K)	-E	int
	C	Si	С	Si	С	Si	С	Si	С	Si
Νπ	0	-	46.66	-	0	-	0	-	1.78	-
Νσ	0.09	0	46.49	44.56	-0.09	0	-0.41	0	1.73	30.63
Сπ	0.19	6.71	46.66	43.83	0.19	5.97	0.10	4.42	1.62	3.11
Sπ	0.45	7.40	46.56	43.68	0.45	6.52	-0.46	4.25	1.35	2.42
CS…F	0.98	9.66	46.47	43.47	0.78	7.51	-1.20	4.62	0.90	1.32
$C_1H$ F	1.78	9.59	46.29	43.40	1.41	8.43	-0.77	2.33	0.24	0.49

Table 1. Energetic parameters of various arrangements and interaction energies within dimers (kcal/mol)

Various aspects of the energetics of these structures are contained in Table 1. The first column lists the relative electronic energies which place the N $\pi$  geometry as the most stable, followed closely by N $\sigma$  and C $\pi$ , both of which lie within 0.2 kcal/mol. Slightly higher are S $\pi$  and CS<sup>..</sup>F both still within 1 kcal/mol of N $\pi$ . The H-bonded structures are a little higher in

energy but still within 1.8 kcal/mol. The situation changes slightly when zero-point vibrational energies are added. As is evident in the next two columns of Table 1, the zero-point vibrational energies of the complexes are all in the range between 43.4 and 46.7 kcal/mol, with the CF<sub>4</sub> complexes a little higher in this regard. With either of the two TF<sub>4</sub> units, there are relatively small differences from one geometry to the next. The N $\pi$  and N $\sigma$  dimers switch places with the latter now slightly lower in energy after inclusion of ZPVE. There is also a relative destabilization of S $\pi$  up to 1.4 kcal/mol.

Adding in entropic factors and setting a temperature of 298 K leads to the relative free energies G in the succeeding column. This inclusion reorders the energetics significantly. The chalcogen-bonded CS<sup>..</sup>F dimer becomes favored over the others, followed by the H-bonded geometry, and then S $\pi$  and N $\sigma$ . Contrary to its favored status in terms of electronic energy, the N $\pi$  structure becomes disfavored, lower in energy than only C $\pi$ . The last energetic parameter listed in Table 1 is the interaction energy of each heterodimer. E<sub>int</sub> is evaluated as the difference in energy between the complex and the sum of energies of the two monomers, each taking the internal geometry they adopt within the complex. The N $\pi$  arrangement leads to the largest interaction energy of 1.78 kcal/mol. In fact the order of E<sub>int</sub> parallels the purely electronic energies of the configurations, with the H-bonded dimer the most weakly bound.

A very recent study <sup>61</sup> had found that it is the N $\sigma$  structure that appears in the microwave spectrum of the thiazole-CF<sub>4</sub> pair. The rotational frequencies of this structure were measured to be 3.13, 0.43, and 0.40 GHz, in nice coincidence with our computed values of 3.14, 0.45, and 0.42 GHz. In addition to this geometry, calculations by these authors identified three other minima that correspond to our N $\pi$ , C $\pi$ , and one that would appear to roughly approximate our S $\pi$  structure. The relative electronic energies of these three alternatives, including zero-point vibrational corrections, are 0.03, 0.10, and 0.20 kcal/mol, respectively, close to the values reported here in Table 1, with the exception of the S $\pi$  dimer which is a bit higher in our calculations. Unlike our study, the calculations reported earlier did not include a CS<sup>...</sup>F or any of the three H-bonded minima.

The replacement of the C of  $CF_4$  by Si is expected to very substantially enhance the ability of this central atom to act as electron donor within the context of a tetrel bond. Search of the potential energy surface of the possible complexes of SiF<sub>4</sub> with thiazole led to the five geometries illustrated in Fig 3. In keeping with the notion of a stronger tetrel bond, the R(Si··N) distance in the N $\sigma$  configuration of Fig 3a is only 2.105 Å, much shorter than the equivalent 3.274 Å in Fig 2b. This noncovalent bond strengthening is obvious also in its interaction energy of 30.6 kcal/mol, listed in the last column of Table 1, far larger than the 1.7 kcal/mol of the CF<sub>4</sub> N $\sigma$  complex.

With regard to secondary minima, they are all much less stable than N $\sigma$ . The C $\pi$  and S $\pi$  geometries are about 7 kcal/mol higher in energy, and more than 4 kcal/mol higher than N $\sigma$  in terms of free energies. The H-bonded C<sub>1</sub>H··F and CS··F configurations are higher still, by nearly 10 kcal/mol, even though this difference is reduced to 2.3 kcal/mol when entropic considerations are added to the H-bonded structure. The N $\pi$  geometry of CF<sub>4</sub> decays to N $\sigma$  during optimization.



Fig 3. Geometries of complexes between thiazole and SiF<sub>4</sub>. Distances in Å, angles in degs.

The total entropy of each dimer is listed in Table 2, along with their rotational and vibrational components. The H-bonded structures in the last row have the largest entropy which leads to their stabilization relative to the others in terms of  $\Delta G$ . Most of this enhanced entropy can be traced to their higher vibrational contributions. The entropy increases in an inverse relationship to the overall stability, i.e.  $N\sigma < C\pi < S\pi < CS^{..}F < C_1H^{..}F$ , principally attributable to the vibrational entropy. It is for this reason that the stability ordering of  $\Delta G$  is quite different than that of the energy.

	total		rotat	ional	vibrational		
	C	Si	С	Si	С	Si	
Νπ	105.10	-	30.22	-	33.53	-	
Νσ	104.75	100.72	30.65	30.39	32.75	28.71	
Сπ	105.41	107.68	30.20	30.53	33.86	35.53	
Sπ	108.10	110.45	30.22	30.53	36.53	38.30	
CS…F	112.36	111.20	30.52	30.99	40.49	38.59	
$C_1H$ ··F	122.50	124.30	31.81	32.16	49.34	50.52	

Table 2. Total and contributions to entropy of complexes (cal/mol K)

# **Energy Decomposition**

The underlying nature of the bonding in these dimers can be assessed by partitioning each interaction energy into its components. SAPT decomposition yields first an electrostatic element (ES) resulting from the attraction between the nuclei and electron clouds of the two units, prior to any polarization caused by their mutual interaction. The stabilizing effects of this polarization and charge transfer fall under the heading of the induction (IND) component, complemented by

dispersion energy (DISP). Pauli exchange (EX) resulting from the steric repulsions of the two molecular electron clouds prevent the two units from collapsing into one another.

The results of the SAPT partitioning listed in Table 3 indicate that the largest contributor to most of the interactions between thiazole and  $CF_4$  originates in the dispersion energy. While ES is slightly larger than DISP for N $\sigma$ , it is the latter that is more important for the other structures, particularly for S $\pi$  and CS<sup>..</sup>F. Induction plays only a minor role in any of these dimers. The situation changes somewhat for the SiF<sub>4</sub> complexes. For the more loosely bound complexes in the last five rows of Table 4, ES is competitive with DISP, and even larger in several cases. But the most dramatic distinction is connected with the tightly bound N $\sigma$  structure, wherein all of the attractive components are magnified. Most notable, ES plays by far the largest role, followed by IND and then DISP.

Table 3. SAPT components of interaction energies (kcal/mol) in complexes pairing thiazole with CF<sub>4</sub>.

	ES	EX	IND	DISP	total
Νσ	-2.95	3.65	-0.35	-2.29	-1.94
Νπ	-2.13	4.44	-0.25	-3.54	-1.48
Сπ	-2.19	4.79	-0.24	-3.55	-1.19
Sπ	-1.64	4.17	-0.21	-3.31	-0.99
CS…F	-1.19	2.68	-0.18	-2.11	-0.80
$C_1H$ ··F	-0.13	0.13	-0.02	-0.32	-0.34

Table 4. SAPT components of interaction energies (kcal/mol) in complexes pairing thiazole with SiF<sub>4</sub>.

	ES	EX	IND	DISP	total
Νσ	-67.30	77.12	-21.20	-12.78	-24.16
Sπ	-3.22	6.57	-0.66	-4.08	-1.39
Сπ	-4.33	7.56	-0.73	-4.45	-1.96
CS…F	-1.72	3.29	-0.37	-2.19	-0.99
C <sub>1</sub> H	-0.60	0.36	-0.07	-0.46	-0.78
C <sub>2</sub> H	-0.56	0.39	-0.07	-0.50	-0.74

It might be noted that SAPT predicts that the N $\sigma$  dyad of thiazole with CF<sub>4</sub> if a bit more stable than is N $\pi$ , which reverses the supermolecule order in Table 1. This reversal is not attributable to the SAPT0 data in Table 3, since raising the level to SAPT2 maintains the same order, changing the total energies in the last column of Table 3 by less than 0.02 kcal/mol.

As another issue, some of the small energy differences encountered here between various dyads suggests the possibility that some relative energies might be reversed by alterations in the DFT functional or the basis set. Table 5 reaffirms a very low sensitivity to these issues. For example, the addition of a Grimme <sup>84</sup> D3 dispersion term has little to no effect upon the relative energies. The same insensitivity occurs if the basis set is changed from an Ahlrichs Def2-TZVP to a Pople-type 6-311+G\*\*. Specifically, the latter set tends to enhance the stability of the

preferred conformation relative to the secondary minima, but leaves the energetic ordering unchanged.

Table 5. Relative energetic parameters of various arrangements (kcal/mol) with different basis sets and GD3 dispersion correction.

	M06	5-2X	M06-2X-GD3		M06-2X	
	Def2-	TZVP	Def2-	TZVP	6-31	1+G**
	C	Si	С	Si	C	Si
Νπ	0.00	-	0.00	-	0.00	-
Νσ	0.09	0	0.07	0.00	0.19	0.00
Сπ	0.19	6.71	0.19	6.70	0.23	10.21
Sπ	0.45	7.40	0.46	7.39	0.67	11.44
CS…F	0.98	9.66	0.99	8.60	1.50	13.12
$C_1H \cdot F$	1.78	9.59	1.86	9.64	2.52	14.04

## Electron Density Topology

Analysis of the electron density via AIM provides indications as to the specific bonding contacts between atoms. The AIM diagrams of the thiazole-CF<sub>4</sub> dimers in Fig 4 provide some intriguing findings. Most notable, in no case is the central C atom of CF<sub>4</sub> implicated in a bonding interaction with the thiazole. It is the set of three F atoms that are tied to the thiazole N by bond paths for both N $\pi$  and N $\sigma$ . The density of the bond critical point of these six bond paths in Figs 4a and 4b are between 0.0052 and 0.0071 au, as summarized in Table 6, characteristic of a weak noncovalent bond. There are four separate bond paths in the  $C\pi$  dimer, which connect either to the C atoms of thiazole or to the C-C and C-S bonds. The S atom of thiazole is involved in only one of the three bond paths in the  $S\pi$  dimer, the other two leading to the neighboring C atoms. One of the two bond paths in CS<sup>..</sup>F is a direct product of the chalcogen bond, with the other indicating a CH"F H-bond. The rather weak CH"F H-bond in Fig 4f is consistent with a low density of 0.0020 au. The AIM diagrams in Fig 5 echo the failure of the central Si atom to be connected via a bond path to thiazole with one notable exception. The unambiguous presence of a Si<sup>..</sup>N tetrel bond in the Nσ conformer of Fig 5a contains a large BCP density of 0.0573 au. The patterns within the other SiF<sub>4</sub> diagrams are similar to those of their CF<sub>4</sub> congeners, although the BCP densities are somewhat larger, mimicking the higher interaction energies of the former.

The BCP density of 0.0573 au within the N $\sigma$  geometry of the SiF<sub>4</sub> complex falls within the usual limits of a noncovalent tetrel bond. The same categorization would result from the 0.150 au density Laplacian at this point. One can ascribe a small amount of covalency to this bond, based on its total energy density of -0.022 au. The formation of this complex induces a certain amount of distortion into the geometries of the two subunits. That of thiazole is minimal, amounting to only 0.5 kcal. However, the transition of SiF<sub>4</sub> from a perfect tetrahedron to something more akin to a trigonal bipyramid, with  $\theta$ (FSiF) angles of 97°, causes an energy rise of 20.9 kcal/mol. It is for this reason that the energy difference between the N $\sigma$  configuration is only some 7-10 kcal/mol more stable than the other structures in Table 1, despite its very large interaction energy

of 30.6 kcal/mol. The full reaction energy  $^{38, 85-90}$ , transforming a pair of optimized monomers to the N $\sigma$  complex would thus be exothermic with  $\Delta E$  equal to -10 kcal/mol.



Fig 4. AIM diagrams of complexes between thiazole and  $CF_4$ . Bond paths are indicated by broken lines with bond critical point shown by small red ball. Density at each BCP in  $10^{-4}$  au.



Fig 5. AIM diagrams of complexes between thiazole and SiF<sub>4</sub>. Bond paths are indicated by broken lines with bond critical point shown by small red ball. Density at each BCP in 10<sup>-4</sup> au.

The reduced density gradient (RDG) offers a somewhat different graphical view of the bonding interactions. The intermolecular region in Fig 6 takes on a blue color for strongly attractive regions, green for mildly attractive, and turns red for repulsions. The colored area of Fig 6a for the N $\sigma$  conformer of CF<sub>4</sub> is rather diffuse, covering not only the central C but also the three neighboring F atoms. In addition, the green color is deeper in hue along the N $\cdot\cdot$ F lines, all conforming to the AIM diagram of Fig 3a. Replacing CF<sub>4</sub> by SiF<sub>4</sub> within this same N $\sigma$  geometry provides a very different picture in Fig 6b. The Si $\cdot\cdot$ N region is very blue, fading to repulsive red as one moves away from the central Si and toward the peripheral F centers. This pattern strongly supports the AIM Si $\cdot\cdot$ N bond path and a tetrel bond. The N $\pi$  configuration of CF<sub>4</sub> in Fig 6c is not unlike that for its N $\sigma$  geometry in Fig 6a, also in line with the AIM picture of three separate N $\cdot\cdot$ F bond paths in Fig 4b.



Fig 6. RDG diagrams of N $\sigma$  complexes of thiazole with a) CF<sub>4</sub> and b) SiF<sub>4</sub>; c) N $\pi$  geometry of CF<sub>4</sub>. Contour shown has RDG=0.5 au, with blue and red color extremes representing (sign  $\lambda_2$ )· $\rho$ = -0.03 and +0.03 au, respectively.

# **Electronic Displacements**

NBO treatment is frequently very helpful in elucidating the particular atoms involved in molecular interactions as well as the relevant orbitals on each, offering an alternate view to AIM. However there are certain discrepancies between these two different views of bonding. Taking the N $\sigma$  interaction with CF<sub>4</sub> as an example, the NBO data in Table 6 suggest the presence of a C··N tetrel bond with a E2 perturbation energy of 0.12 kcal/mol for N<sub>lp</sub> $\rightarrow \sigma^*$ (CF), although no such bond was suggested by AIM. The three AIM F··N bond paths in Fig 4a, each to a different F atom, are reduced to the involvement of only one of these F centers, with charge transfers from the F lone pair to three different  $\pi$  MOs of the thiazole. A similar discrepancy arises in the N $\pi$  configuration. NBO again suggests the involvement of only one of the F atoms of CF<sub>4</sub>, where its lone pair transfers density to two different thiazole MOs. NBO is less ambiguous and consistent with AIM in its finding of a Si··N tetrel bond in the N $\sigma$  dimer with SiF<sub>4</sub>. The E2 perturbation for charge transfer from NC bonding orbitals of thiazole to the appropriate  $\sigma^*$ (SiF) antibonding orbital is 23.0 kcal/mol, supplemented by 13 kcal/mol transfers to each of the other three SiF  $\sigma^*$  orbitals.

The fundamental distinctions between the N $\sigma$  dimers involving C and Si are highlighted by electron density shift diagrams which are derived when the electron densities of the two

monomers are subtracted from that of the full complex. The purple and green regions of Fig 7 show respectively gain and loss of density as a result of the dimerization process. The pattern in Fig 7b for SiF<sub>4</sub> is characteristic of a tetrel bond, with a large purple density enhancement in the region between the Si and N nuclei, and a small depletion closer to the N. The pattern is quite different for the CF<sub>4</sub> analog in Fig 7a where the dominant feature between the C and N nuclei is a substantial green depletion. As an illustration of the density shifts in the  $\pi$ -type complexes, one sees a loss near the F nuclei of CF<sub>4</sub> in the N $\pi$  complex in Fig 7c, with an accretion in the region lying above the N. The EDS diagrams of the C $\pi$  arrangements of the CF<sub>4</sub> and SiF<sub>4</sub> complexes are exhibited in Fig 7d and 7e. These patterns are similar to that in Fig 7c which are characterized by a gain above the C atom of the thiazole, and depletions on the three F atoms of TF<sub>4</sub>.

Table 6. Bond critical point densities (10<sup>-4</sup> au), NBO E2 (kcal/mol), and total charge transferred CT to  $TF_4$  (me)

	$\rho_{BCP}$		E	2	СТ	
	С	Si	С	Si	C	Si
Νπ	3x55	-	0.17	-	0.4	-
Νσ	3x67	573	0.12	23.04	-0.7	138.5
Сπ	3x52	3x69	0.32ª	1.16 <sup>b</sup>	0.7	2.0
Sπ	3x51	4x63	0.22	0.32	0.9	4.4
CS…F	2x49	73	0.33	0.51	0.0	0.6
$C_1H$ ··F	20	37	-	0.15	0.2	0.3

 $a\pi(CC) \rightarrow \sigma^*(CF) + F_{lp} \rightarrow \pi$ 

<sup>b</sup>  $\pi(CC) \rightarrow \sigma^*(SiF) + F_{lp} \rightarrow \pi^*(CC)$ 





Fig 7. Electron density shifts accompanying formation of complexes of thiazole with a)  $CF_4$  in N $\sigma$  structure, b) SiF<sub>4</sub> in N $\sigma$  structure, c) CF<sub>4</sub> in N $\pi$  structure, d) CF<sub>4</sub> in C $\pi$  structure, e) SiF<sub>4</sub> in C $\pi$  structure. Purple and green colors respectively indicate gain and depletion of density, with contours shown a) ±0.0005, b) ±0.005, c) ±0.0004, d) ±0.0003, e) ±0.0005 au.

As a quantitative measure of overall density motions from one molecule to the other, the total charge transfer (CT) in the last columns of Table 6 was computed as the sum of the natural charges of all the atoms on each monomer. In line with the weak interactions within the CF<sub>4</sub> complexes, the total charge transferred from thiazole to CF<sub>4</sub> are all less than 1 me. These quantities are much larger for SiF<sub>4</sub>, with CT equal to 2 and 4 me, respectively, for the C $\pi$  and S $\pi$  geometries. But by far the largest transfer occurs within the N $\sigma$  structure, with 139 me moving from thiazole to SiF<sub>4</sub>, another indicator of a true tetrel bond.

## Internal Deformations

Since most of these interactions are fairly weak, one would not anticipate that the internal geometries of the two monomers would be much affected by the complexation. The bondlength changes within the two subunits are reported in Tables 7 and 8 for the dyads containing CF<sub>4</sub> and SiF<sub>4</sub>, respectively. As indicated by the first row of Table 7, the approach of the CF<sub>4</sub> unit above the thiazole N atom in the N $\pi$  structure induces a slight elongation of the two bonds to the N, with small contractions of the other bonds. In keeping with the charge transfer to the CF<sub>1</sub> antibonding orbital, this bond stretches a bit. Fairly similar changes are noted in the N $\sigma$  structure. As the CF<sub>4</sub> approaches the C<sub>2</sub>-C<sub>3</sub> midpoint in the C $\pi$  geometry, this bond lengthens, whereas the thiazole bondlengths are relatively unaffected by the S $\pi$  complexation. The largest change occurring within the CS<sup>...</sup>F structure is the lengthening of the C<sub>1</sub>-S bond, attributable to the transfer into the corresponding  $\sigma^*$  antibonding orbital.



Table 7.	Changes in	internal bond	llengths (Å	) caused by co	mplexation of	of thiazole with	ı CF <sub>4</sub> .
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	$N-C_1$	$C_1$ -S	$S-C_2$	$C_2-C_3$	C <sub>3</sub> -N	$C-F_1$	C-F <sub>2</sub>
Νπ	0.0007	-0.0014	-0.0004	0.0000	0.0002	0.0034	-0.0019
Νσ	0.0005	-0.0016	0.0000	-0.0001	0.0000	0.0060	0.0024
Сπ	0.0000	-0.0002	-0.0001	0.0005	-0.0001	0.0012	0.0019
Sπ	-0.0004	0.0000	-0.0002	0.0000	0.0005	0.0010	0.0015
CS…F	-0.0005	0.0010	0.0002	-0.0002	0.0004	-0.0008	-0.0014
$C_1H$ ··F	0.0001	-0.0007	-0.0006	0.0003	0.0001	0.0029	-0.0013

	N-C <sub>1</sub>	C <sub>1</sub> -S	S-C <sub>2</sub>	C <sub>2</sub> -C <sub>3</sub>	C <sub>3</sub> -N	Si-F <sub>1</sub>	Si-F <sub>2</sub>
Νσ	0.0085	-0.0214	0.0022	-0.0055	0.0021	0.0394	0.0342
Сπ	-0.0002	-0.0004	0.0008	0.0017	-0.0003	0.0022	0.0025
Sπ	-0.0016	0.0036	0.0016	-0.0009	0.0010	0.0017	0.0024
CS…F	-0.0008	-0.0005	-0.0008	0.0000	0.0008	-0.0001	0.0029
C <sub>1</sub> H··F	0.0002	0.0001	-0.0001	0.0000	0.0002	0.0025	-0.0015

Table 8.	Changes in	internal bondlength	s (Å) ca	used by c	complexation of	of thiazole with SiF <sub>4</sub> .
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For the most part, the bondlength changes when thiazole is complexed with SiF<sub>4</sub> in Table 8 mirror those in Table 7 with some exceptions. In the first place, given the somewhat stronger bonding with SiF<sub>4</sub> as compared to CF<sub>4</sub>, a number of changes are larger in Table 8. For example, the two bonds connecting to S barely change in the  $S\pi$  geometry with CF<sub>4</sub>, whereas elongations of 0.004 and 0.002 Å occur with SiF<sub>4</sub>. But the most dramatic distinction is associated with the N $\sigma$  configuration. The order of magnitude increase in the interaction energy for SiF4 is reflected in quite substantial bondlength changes. The two bonds to N are stretched by 0.002 and 0.009 Å, accompanied by a substantial contraction of the C<sub>1</sub>-S bond. Also all four of the Si-F bonds undergo a stretch of 0.034 to 0.039 Å, due in large measure to the additional density added to their  $\sigma^*$ (SiF) antibonding orbitals.

## CONCLUSIONS

There exists a delicate balance between the various geometries of the heterodimer involving thiazole and CF<sub>4</sub>. All of the structures are weakly bound with interaction energies less than 2 kcal/mol. The two most stable conformers orient the CF<sub>4</sub> near the thiazole N atom, either in the molecular plane or directly above the N. Two other configurations, only slightly less stable, place the CF<sub>4</sub> above either the thiazole C-C bond or its S atom. There is also a chalcogenbonded CS<sup>..</sup>F configuration, as well as H-bonded complexes to each of the CH groups of thiazole. The energetic ordering of these various structures is scrambled when entropic considerations are included in their free energies, making the chalcogen-bonded geometry most stable. The replacement of the C of CF<sub>4</sub> by Si leads to an unambiguous identification of a structure with SiF<sub>4</sub> located within the thiazole plane as by far the most stable. This Si<sup>..</sup>N tetrel-bonded heterodimer has an interaction energy of 30.6 kcal/mol. The C $\pi$ , S $\pi$ , and CS<sup>..</sup>F geometries remain as minima, more tightly bound than their analogues with CF<sub>4</sub>, but still far less stable than the global minimum. Despite the lone pair on S, this region is unable to attract either electrophile.

The global thiazole-SiF<sub>4</sub> minimum clearly involves a tetrel bond with a high proportion of electrostatic stabilization. However, the other minima identified on the two potential energy surfaces contain much higher proportions of dispersion, in most cases even larger than the electrostatic component; induction contributions are minimal. The tetrel-bonded thiazole-SiF<sub>4</sub> heterodimer is the only species for which there is an AIM bond path that involves the central tetrel atom. The bond paths of most of the other configurations connect the F atoms of TF<sub>4</sub> to the

thiazole. This lack of direct central T atom involvement in the bonding is largely verified by NBO and RDG analyses, as well as mappings of the electron density shift patterns. Overall, this work reinforces the reluctance of the C atom to engage in tetrel bonds, in strong contrast to its heavier congeners such as Si.

There are several lessons to be gleaned from the calculations presented here. Firstly, they demonstrate how a molecule like thiazole, with a few electrophilic sites, is able to bind to a simple molecule like CF<sub>4</sub> in a number of entirely different ways. A tetrel bond can be formed between the C of CF<sub>4</sub> to the N, both to its lone pair in the molecular plane, and directly above the N. With CF<sub>4</sub> hovering above the thiazole plane, the tetrel bond can also engage with the S atom and with a C=C  $\pi$ -bond. Some of these dyads occur despite the absence of a corresponding minimum in the MEP of the thiazole, so the presence of such a minimum is clearly not a prerequisite for the formation of a stable structure. There is also the possibility of an interaction that involves an entirely distinct CS<sup>..</sup>F chalcogen bond when one F of CF<sub>4</sub> lies in the thiazole plane; all of these various configurations are complemented by three different CH. F H-bonded structures. One of the remarkable features of this molecular pairing is the tight clustering of the energies of these eight different structures, all within 2 kcal/mol of one another. Despite their similar energies, these complexes are bound together by diverse interactions, viz. tetrel, chalcogen, and hydrogen bonds. Another important lesson is the way in which the energy ordering changes upon addition of zero-point vibrations, which is further remodified when entropic factors are included. The expectations as to the structure to be expected in an experiment are thus heavily dependent upon the particular temperature.

A second important conclusion is connected with the modification that arises when the C of  $CF_4$  is replaced by its Si congener. While most of the configurations observed for  $CF_4$  remain intact, there is a larger spread of their relative energies. Nonetheless, the energy ordering is again modified by the inclusion of entropic effects which make the H-bonded structures preferred at higher temperatures, despite their higher electronic energy. But the principal difference incurred by this C $\rightarrow$ Si substitution is the prominence of the planar Si $\cdot$ N tetrel-bonded structure which is some 30 times stronger than its C $\cdot$ N analogue, with an interaction energy of 30.6 kcal/mol. It is this structure which is inarguably the one that will be observed experimentally, regardless of temperature. The enormous enhancement in the interaction energy within this Si $\cdot$ N tetrel bond can be attributed in part to the deeper  $\sigma$ -hole on Si. But it should be noted that the amplifications of the several other interactions in the SiF<sub>4</sub> $\cdot$  triazole pair are much milder, despite their interaction with this same  $\sigma$ -hole.

With regard to the various computational tools applied to this series of complexes, the calculation of the electronic energy does not fully conform to the result obtained if corrected by zero-point vibrational energies; the energetic ordering is further adjusted when entropic effects are added. The SAPT formulation provides interaction energies in good accord with the supermolecule approach when corrected for basis set superposition error. It is also worth noting that the addition of a further dispersion term to the DFT functional has little effect upon relative energetics, nor does application of a different sort of triple-valence basis set. In terms of various

quantities that are derived from the wavefunctions, the AIM bond paths provide evidence as to the particular atoms of the two units that are bonded to one another, so help to distinguish between say, a tetrel bond and a set of F. N interactions. However, AIM tends toward atomatom bonding, even in  $\pi$ -systems where the interaction might be better described as connecting to a bond midpoint. Pictorial RDG patterns tend to favor a rather diffuse sort of bonding in many cases, clouding a more specific bonding picture; the same is true for some electron density shift maps. It is worth noting that NBO bonding pictures are not always consistent with AIM.

# **Contributor Roles**

Conceptualization SS; Data curation AA; Formal analysis SS; Funding acquisition SS; Writing SS and AA; Visualization AA; Supervision SS; Investigation AA

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# **Conflict of Interest**

The authors declare no conflict of interest.

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