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Modeling Henry's Law and Phase Separations of Water-NaCl-Organic Mixtures with Solvation and Ion-Pairing

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1 **Modeling Henry's Law and Phase**
2 **Separations of Water-NaCl-Organic Mixtures**
3 **with Solvation and Ion-Pairing**

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16

17 Abstract

18 Empirical measurements of solution vapor pressure of ternary acetonitrile (MeCN) H₂O-NaCl-
19 MeCN mixtures were recorded, with NaCl concentrations ranging from zero to the saturation limit,
20 and MeCN concentrations ranging from zero to an absolute mole fraction of 0.64. After
21 accounting for speciation, the variability of the Henry's law coefficient at vapor-liquid equilibrium
22 (VLE) of MeCN ternary mixtures decreased from 107% to 5.1%. Solute speciation was modeled
23 using a mass action solution model that incorporates solute solvation and ion-pairing
24 phenomena. Two empirically determined equilibrium constants corresponding to solute
25 dissociation and ion pairing were utilized for each solute. When speciation effects were
26 considered, the solid-liquid equilibrium of H₂O-NaCl-MeCN mixtures appear to be governed by a
27 simple saturation equilibrium constant that is consistent with the binary H₂O-NaCl saturation
28 coefficient. Further, our results indicate that the precipitation of NaCl in the MeCN ternary
29 mixtures was not governed by changes in the dielectric constant. Our model indicates that the
30 compositions of the salt-induced liquid-liquid equilibrium (LLE) boundary of the H₂O-NaCl-MeCN
31 mixture correspond to the binary plateau activity of MeCN, a range of concentrations over which
32 the activity remains largely invariant in the binary water-MeCN system. Broader comparisons with
33 other ternary miscible organic solvent (MOS) mixtures suggest that salt-induced liquid-liquid
34 equilibrium exists if: 1) the solution displays a positive deviation from the ideal limits governed by
35 Raoult's law; and 2) the minimum of the mixing free energy profile for the binary water-MOS
36 system is organic-rich. This work is one of the first applications of speciation-based solution
37 models to a ternary system, and the first that includes an organic solute.

38

39 1. Introduction

40 Solvent-driven fractional crystallization (SDFC) enables the efficient isolation and recovery of
41 high-value metals and critical materials from brines and wastes.¹⁻⁴ In SDFC, a partially miscible
42 organic solvent (MOS) induces fractional crystallization of dissolved inorganic ions at solid-liquid
43 equilibrium.⁵ However, unravelling the driving mechanism of solute-induced separations, is
44 particularly challenging given the divergence of solution theory for electrolyte and non-electrolyte
45 species.⁶⁻⁹

46 Contemporary approaches to model the interactions between water, salt, and organics
47 include: 1) semi-empirical models based on the McMillan-Mayer (e.g., NRTL¹⁰, UNIQUAC¹¹⁻¹³) and
48 Lewis-Randall (e.g., Pitzer-Debye-Hückel¹⁴⁻¹⁶) theories; and 2) fully empirical/Edisonian models
49 based on Setschenow constants¹⁷ or the Hofmeister series.¹⁸ These models are efficacious in
50 regressing and interpolating empirical data; however, they do not establish an underlying
51 mechanism in which the regressed parameters directly correspond to a phenomenon, thereby
52 lacking a correlative relationship.¹⁹ Molecular dynamics (MDs) is a powerful means to understand
53 complex mixtures involving water, salt, and organics systems on the intermolecular scale.²⁰
54 However, MD is challenged when predicting phase boundaries due to the length and time scales
55 available for simulations as well as the interplay between “a mixture of strong (e.g., ion-ion) and
56 weak (e.g., van der Waals) interactions” in complex mixtures.²⁰

57 To bridge existing knowledge gaps, Zivitsas^{6,7,21,22}, Heyrokska²³⁻²⁷, Reynolds^{8,28-30}, Wexler³¹⁻
58 ³⁵ and Wilson^{5,9,36,37} have recently explored mechanistic mass action models that incorporate
59 solvation and ion-pairing phenomena. Each of these models is distinct, with some approaches

60 retaining electrostatic terms. The implementation of ion pairing can occur before, after, or
61 concurrently with hydration and may impact the hydration model (e.g., decline in solvation upon
62 ion-pair formation). Ion pairing can be modeled with 1) conventional equilibria such as second-
63 order equilibrium for 1-1 and 2-2 salt, 2) unusual implementations such as concentration-
64 independent first-order dissociation (i.e., equilibrium coefficient corresponds to van 't Hoff
65 indices) or 3) the use of Debye-Hückel terms in lieu of ion-pairing.

66 Hydration has been modeled with three distinct approaches. First, through the application of
67 a concentration-independent hydration parameter. These fixed hydration values allow various
68 experimental data to be modeled across large concentration ranges. However, the model tends
69 to yield non-physical results at very high concentrations. Second, via equivalent-energy stepwise
70 hydration models, each hydration step of the solute can be treated as equal-energy reactions (e.g.,
71 identical equilibrium constants for each hydration step). This approach is premised on the
72 Brunauer–Emmett–Teller (BET) theory of vapor interacting with surfaces. The resulting models
73 predict statistical distributions of different degrees of solute hydration with the populations
74 varying with concentration.^{38–41} Third, hydration can be modeled through the application of
75 stepwise hydration in which the energy of hydration changes with each hydration step of the
76 solute. Effectively, each successive removal of a hydrating water molecule from a solute requires
77 more energy than the previous step, analogous to the removal of protons from a polyacid with
78 multiple pK_a equilibrium values.^{24,42} Based on this approach, the apparent degree of hydration
79 declines with solute concentration, a result which is attributed to a combination of changes in the
80 solute coordination environment and the joint solvation of solutes.⁹ The degree of ion pairing and
81 hydration can be derived based on the geometry (e.g., coordination sphere) or the energy of an

82 interaction with the individual solute coordination environment while maintaining an average
83 energy of interaction.

84 Together with an expanded experimental dataset, we employ a mass action speciation
85 framework that incorporates second-order ion pairing and variable-energy stepwise solute
86 hydration⁹ to correlate the solid-liquid and vapor-liquid equilibrium compositions of H₂O-NaCl-
87 MOS ternary mixtures. The model parameters are based on chemical equilibria that correlate
88 directly with physical phenomena. When NaCl and MOS are modeled as hydrates, we observe a
89 constant speciated NaCl mole fraction at solid liquid equilibrium (SLE) for MOS ternary mixtures.
90 Furthermore, our experiments suggest that the degree of NaCl crystallization is not driven directly
91 by MOS specific properties, such as dielectric constant³ or surface tension.⁴³ At vapor-liquid
92 equilibrium (VLE), we found that the variability of the Henry's law coefficient for MeCN ternary
93 mixtures fell from 107% to 5.1% for NaCl concentrations ranging from 0 to saturation once solute
94 speciation is considered. Lastly, we discuss speciation implications for the composition of salt-
95 induced liquid-liquid equilibrium (LLE) and for the Gibbs free energy of mixing in ternary organic-
96 salt-water mixtures.

97 **1.1. Experimental Materials and Chemicals**

98 Nuclear magnetic resonance (NMR) spectra were acquired on a Bruker Avance III 600 MHz
99 spectrometer with a magnetic field strength of 14.093 T, corresponding to operating frequencies
100 of 600.13 MHz (¹H). All NMR experiments (except dimethyl ether) were captured with a co-axial
101 insert containing D₂O (Cambridge Isotopes Laboratories). The T₁ of each integrated shift was
102 verified as generally below 2 s, with no shifts above 4 s observed. Na concentrations were

103 measured with inductively coupled plasma-optical emission spectroscopy (ICP-OES) at a detection
104 limit of 0.011 $\mu\text{g/mL}$ Ca.

105 ACS-grade NaCl, free of anticaking agent, was used after being maintained for at least 48
106 hours in a vacuum oven at 150 °C. Solvents were obtained as anhydrous when possible. The MOS
107 used in these studies were dimethyl ether (DME), acetonitrile (MeCN), and 1,4-dioxane. From NMR
108 experiments, the H₂O to MOS mole ratio was less than 0.001 for all the MOS used in this study.

109 **1.2. Aqueous Phase Composition of Water-NaCl-MOS**

110 Stock solutions with known masses of NaCl and distilled H₂O were prepared. The MOS was
111 added to 1-3 g of a stock NaCl solution. When the solution became cloudy, additions were slowed
112 until a thin organic layer was clearly visible upon settling. After settling, 0.4 mL of the heavier
113 aqueous phase was transferred to an NMR tube fitted with a coaxial insert containing D₂O. T1
114 experiments were conducted to establish the relaxation time of water and the MOS. Quantitative
115 NMR was conducted on the sample using 90-degree pulses, with delays (30-60 s) at least five
116 times longer than the longest T1 and temperature regulated at 298 K throughout. The mole ratio
117 of H₂O to MOS was established with NMR, while the mole ratio of water to NaCl was calculated
118 through species conservation.

119 **1.3. Temperature Dependent Vapor Pressure Measurements**

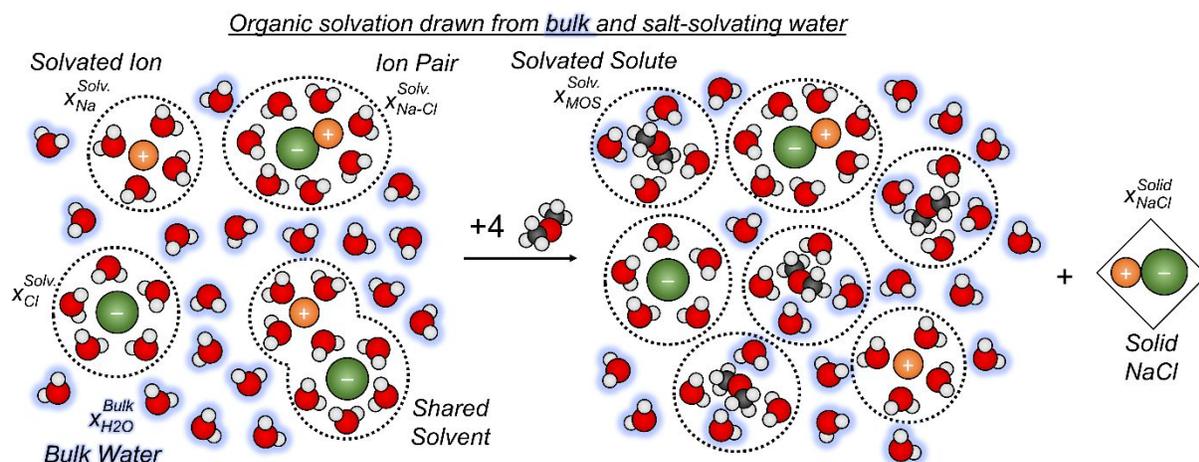
120 Vapor pressures of H₂O-NaCl-MeCN mixtures were determined using a Grabner Instruments
121 MINIVAP VPXpert vapor pressure analyzer using a triple expansion method at set temperatures
122 of 20.0, 25.0, and 30.0 °C with a 180 s equilibration time.

123 **2. Theory**

124 2.1. Modeling Solute Speciation

125 A mass action-based model premised on solvation and ion pairing was employed to model
 126 the VLE behavior of the ternary mixtures.^{9,36} The proposed framework correlates chemical
 127 equilibrium compositions to the degree of solvation and ion pairing for organic and inorganic
 128 solutes. Using two thermodynamic parameters for each inorganic salt, namely the equilibrium
 129 constants for solute hydration and ion dissociation, the speciation-based model was successful in
 130 regressing the VLE composition for 24 common 1-1 and 2-2 salts, with concentrations ranging
 131 from infinite dilution to saturation.⁹

132 As a consequence of solute solvation and ion pairing, the effective solute mole fractions
 133 depart from their corresponding absolute/anhydrous mole fractions. In the speciation model, as
 134 depicted in Figure 1, the solvent energetically partitions into two distinct phases; the solvent exists
 135 1) as part of the bulk phase ($x_{H_2O}^{Bulk}$) or 2) as solvating molecules that are a part of the speciated
 136 solutes ($x_B^{Solv.}$). This approach is consistent with the spatial response of solvents even in the
 137 presence of a small amount of charged solute.⁴⁴



139 **Figure 1:** (Left) Saturated aqueous binary NaCl solution speciated based on $K_{NaCl}^{Hyd.} = 3.67$ and $K_{NaCl}^{Dis.} = 0.033$.
 140 (Right) The addition of a miscible organic solvent, namely DME in this illustration, ($K_{DME}^{Hyd.} = 3.55$) results in
 141 precipitation of the NaCl. Here, the addition of DME induces a molar displacement of the solvated NaCl,
 142 precipitating it from the aqueous phase to maintain a constant speciated solute concentration at solid-
 143 liquid equilibrium. The solvation environment of DME is shaded in color to indicate the origins of its
 144 solvating water molecules relative to the saturated binary NaCl solution.

145 The absolute mole fraction of the inorganic ions was calculated with Equation 1, assuming
 146 full electrolyte dissociation of the salt.⁹ By rearranging the equilibrium relationships, the solute's
 147 concentration-dependent degree of hydration can be calculated with Equation 2. Here, a
 148 hydration equilibrium constant ($K_B^{Hyd.}$) that is solute specific was employed.⁹

$$[x_B^{Abs.}] = \frac{[x_{B+}^{Abs.}] + [x_{B-}^{Abs.}]}{[x_{B+}^{Abs.}] + [x_{B-}^{Abs.}] + [x_{H_2O}^{Abs.}] + [x_{MOS}^{Abs.}]} \quad (1)$$

$$n(H_2O)_B^{Hyd.} = K_B^{Hyd.} [x_{H_2O}^{Abs.}]^m \quad (2)$$

150 For the H₂O-NaCl-MOS ternary mixtures investigated in this paper, the solvated mole
 151 fractions of NaCl ($\bar{x}_B^{Solv.}$) and the miscible organic solvent (MOS) ($\bar{x}_{MOS}^{Solv.}$) were calculated with
 152 Equation 3. This formulation incorporates the solvating water molecules as part of the speciated
 153 solute mole fractions, by removing its contribution to the bulk solvent, as represented in the
 154 denominator of Equation 3:

$$\bar{x}_B^{Solv.} = \frac{[x_B^{Abs.}]}{[x_{H_2O}^{Abs.}] + [x_{MOS}^{Abs.}] + [x_B^{Abs.}] - K_{MOS}^{Hyd.} [x_{H_2O}^{Abs.}]^m [x_{MOS}^{Abs.}] - K_B^{Hyd.} [x_{H_2O}^{Abs.}]^m [x_B^{Abs.}]} \quad (3)$$

155 For water molecules that are not involved in solvation, an equivalent expression was used
 156 to calculate the speciated bulk water mole fraction ($x_{H_2O}^{Bulk}$), as shown in Equation 4:

$$\bar{x}_{H_2O}^{Bulk} = \frac{[x_{H_2O}^{Abs.}] - K_{MOS}^{Hyd.} [x_{H_2O}^{Abs.}]^m [x_{MOS}^{Abs.}] - K_B^{Hyd.} [x_{H_2O}^{Abs.}]^m [x_B^{Abs.}]}{[x_{H_2O}^{Abs.}] + [x_{MOS}^{Abs.}] + [x_B^{Abs.}] - K_{MOS}^{Hyd.} [x_{H_2O}^{Abs.}]^m [x_{MOS}^{Abs.}] - K_B^{Hyd.} [x_{H_2O}^{Abs.}]^m [x_B^{Abs.}]} \quad (4)$$

157

158 **2.2. Incorporating Ion-Pairing Phenomena**

159 The assumption of complete ionic dissociation is invoked by a majority of activity coefficient-
 160 based models. Although these models successfully regress equilibrium data for inorganic
 161 mixtures, poor model fidelity is often observed with mixtures of high ionic strength and valency,
 162 or with mixed-solvent solutions.⁴⁵ In fact, Pitzer noted that the complete ion dissociation
 163 conjecture was based on modeling convenience rather than on a mechanistic representation.¹⁴

164 Here, the ion-pairing phenomenon that dominates ion speciation was accounted for with the
 165 appropriate equilibrium constants. For 1-1 electrolytes, which includes NaCl as used in this study,
 166 the ionic equilibria between dissociated and associated ions can be represented by Equation 5,
 167 where $K_B^{Dis.}$ denotes the ion dissociation equilibrium constant, and $\bar{x}_{B+}^{Solv.}$, $\bar{x}_{B-}^{Solv.}$ and $\bar{x}_{B\pm}^{Solv.}$ represent
 168 the solvated mole fractions of Na⁺ and Cl⁻ ions, and Na-Cl ion pairs at equilibrium, respectively.
 169 The effective mole fraction of the inorganic species ($\bar{x}_B^{Solv.}$), which includes Na⁺ and Cl⁻ ions, and
 170 Na-Cl ion pairs was computed with Equation 6.

$$K_B^{Dis.} = \frac{[\bar{x}_{B+}^{Solv.}][\bar{x}_{B-}^{Solv.}]}{[\bar{x}_{B\pm}^{Solv.}]} \quad (5)$$

$$[\bar{x}_B^{Solv.}] = [\bar{x}_{B\pm}^{Solv.}] + [\bar{x}_{B+}^{Solv.}] + [\bar{x}_{B-}^{Solv.}] \quad (6)$$

171 Finally, the derived solvated mole fractions for H₂O, NaCl and MOS of the ternary mixtures
 172 were renormalized to enable comparisons between the absolute and solvated mole fraction
 173 frameworks, based on Equations 7 to 9.

$$[x_B^{Solv.}] = \frac{[\bar{x}_B^{Solv.}]}{[\bar{x}_B^{Solv.}] + [\bar{x}_{MOS}^{Solv.}] + [\bar{x}_{H2O}^{Bulk}]} \quad (7)$$

$$[x_{MOS}^{Solv.}] = \frac{[\bar{x}_{MOS}^{Solv.}]}{[\bar{x}_B^{Solv.}] + [\bar{x}_{MOS}^{Solv.}] + [\bar{x}_{H2O}^{Bulk}]} \quad (8)$$

$$[x_{H2O}^{Bulk}] = \frac{[\bar{x}_{H2O}^{Bulk}]}{[\bar{x}_B^{Solv.}] + [\bar{x}_{MOS}^{Solv.}] + [\bar{x}_{H2O}^{Bulk}]} \quad (9)$$

174

175 **2.3. Gibbs Free Energy Calculations**

176 Gibbs free energy calculation were based on Equation 10 with activities dependent on the
177 phase boundary domain, with a_n defined by Table 1.

$$g = x_x^{abs} \cdot RT(a_n) \quad (10)$$

178 Over the SLE domain, the speciated concentrations were used to calculate the water and
179 electrolyte activity; the MOS activity was further modified with an average Henry's law coefficient.
180 Henry's law representatively connects infinite dilution activity with experimentally determined
181 saturation activity. Over the LLE domain, the activities of the MOS and electrolyte were estimated
182 with fixed saturation values; the water activity was the residual of MOS saturation and speciated
183 electrolyte fractions. The established MOS saturation activity is described in the Results and
184 Discussion section.

185 Table 1. Relationships used to calculate species activity, a_n .

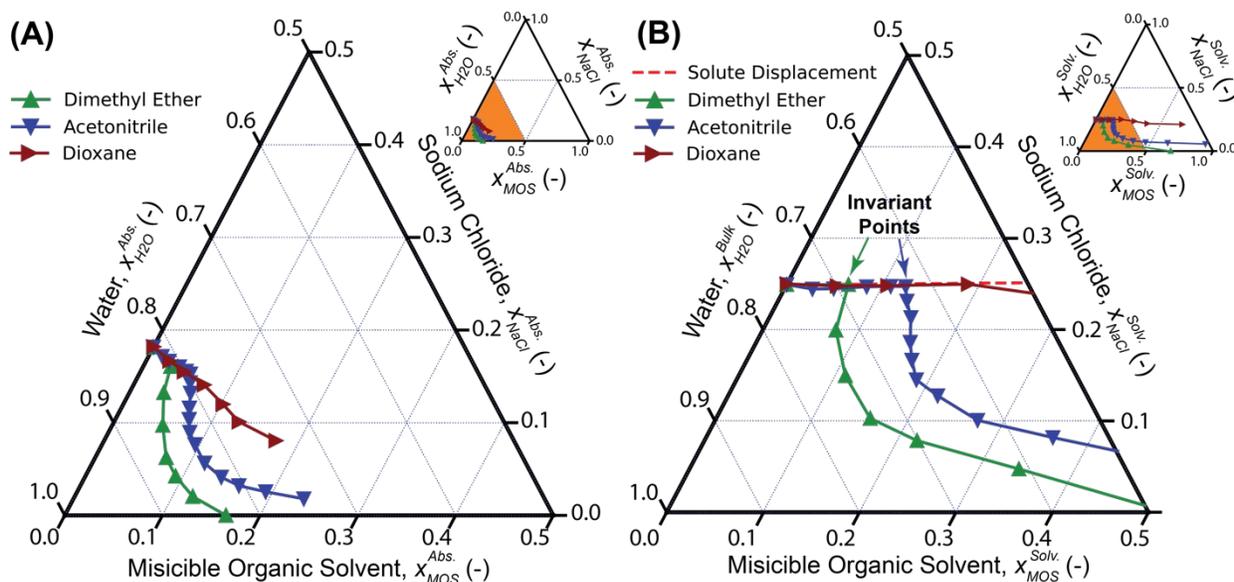
Governing Relationship	Domain and Concentration Range
$a_{H2O} = x_{H2O}^{Solv.}$	SLE, $x_{MeCN} = 0 - 0.057$

$a_{NaCl} = x_{NaCl}^{Solv}$	SLE, $x_{MeCN} = 0 - 0.057$
$a_{MOS} = x_{MeCN}^{Solv} \times k_{MeCN}^{Solv}$	SLE, $x_{MeCN} = 0 - 0.057$ $k_{MeCN}^{Solv} = 6.4$
$a_{H2O} = 1 - x_{NaCl}^{Solv} - x_{MeCN}^{Sat.}$	LLE, $x_{MeCN} = 0.057 - 0.800$ $x_{MeCN}^{Sat.} = 0.1$
$a_{NaCl} = a_{NaCl}^{Sat.} = 0.247$	LLE, $x_{MeCN} = 0.057 - 0.800$
$a_{MeCN} = a_{MeCN}^{Sat.} = 0.80$	LLE, $x_{MeCN} = 0.057 - 0.800$

186

187 **3. Results and Discussion**188 **3.1. Implications on Solvent-induced Solid-Liquid Equilibria Boundary**

189 The ion dissociation ($K_B^{Dis.}$) and hydration ($K_B^{Hyd.}$) equilibrium constants for NaCl were
190 regressed from the VLE data for binary H₂O-NaCl solutions, such that solvated mole fraction was
191 equal to the NaCl activity, as described in our prior work.⁹ The corresponding ion dissociation and
192 hydration equilibrium constants for DME, MeCN, and dioxane were derived from the aqueous
193 phase composition of ternary H₂O-NaCl-MOS mixtures obtained in this and prior work. MeCN
194 and dioxane were selected because they represent fully miscible solvents with and without salt-
195 induced LLE with significant differences in dielectric constant and molecular mass. DME was
196 selected because it is a partially miscible solvent with a salt-induced LLE and is a strong candidate
197 for SDFC water treatment and mineral recovery applications.^{1,2,5}



198

199 **Figure 2: (A)** Ternary phase diagram illustrating the aqueous-phase composition of the SLE boundary of
 200 H₂O-NaCl-MOS ternary mixtures for DME, MeCN, and 1,4-dioxane. The mole fractions correspond to the
 201 absolute scale, employing conventional full ion dissociation assumptions; **(B)** Ternary phase diagram
 202 illustrating the corresponding aqueous-phase composition of SLE boundaries of same H₂O-NaCl-MOS
 203 ternary mixtures, evaluated using the speciated mole fractions. The red line indicates the ideal molar
 204 displacement phenomenon observed with trace addition of MOS to a saturated binary NaCl solution. A
 205 constant speciated water mole fraction was observed with the addition of MOS, from the binary NaCl SLE
 206 to the respective invariant points. The model suggests that MOS addition draws solvating waters from the
 207 originally solvated NaCl ion pairs, causing solvent-induced SLE. The respective ion dissociation and
 208 hydration equilibrium constants used are: $K_{\text{NaCl}}^{\text{Hyd.}} = 3.67$, $K_{\text{NaCl}}^{\text{Dis.}} = 0.033$, $K_{\text{DME}}^{\text{Hyd.}} = 3.55$, $K_{\text{MeCN}}^{\text{Hyd.}} = 2.85$, $K_{\text{Dioxane}}^{\text{Hyd.}} = 3.00$.

209 The SLE composition for H₂O-NaCl-DME, H₂O-NaCl-MeCN and H₂O-NaCl-Dioxane ternary
 210 mixtures under the absolute mole fraction framework is depicted in Figure 2A. Using the
 211 speciation-based model incorporating hydration of the organic solute, the corresponding
 212 solvated mole fractions for the same ternary mixtures are presented in Figure 2B.

213 This speciation-based solution model treats both MOS and NaCl solutes as solvated in
 214 water. The dissolved solutes may interact with water through coordinating (e.g., hydrogen bonds)
 215 or non-coordinating mechanisms (i.e., when the water is not required to bond with the solute to
 216 solvate the solute, such as the formation of clathrate structures), or via a combination of
 217 processes.^{36,37} In the speciated description of a saturated NaCl system (Figure 1 Left), roughly half

218 the water molecules exist as in the bulk (~55%) while the other half (~45%) are involved in NaCl
219 solvation. In the same solution environment ion pairing between Na-Cl dominates, with over 66%
220 of the Na⁺ and Cl⁻ ions existing as ion pairs. At the molecular scale, when an MOS is added to a
221 saturated aqueous NaCl solution, the MOS is solvated by drawing water from the NaCl's solvation
222 environment.

223 In Figure 2B, once solute speciation has been incorporated, we observed an ideal molar
224 displacement relationship that is largely parallel to a solvated NaCl mole fraction of approximately
225 0.25, remaining constant between the saturated binary NaCl SLE and the respective MOS invariant
226 points. The degree of organic solute hydration was adjusted to match the idealized displacement
227 relationship between MOS and NaCl, as represented by the linear relationship (red line). This
228 suggests that once the solutes are fully speciated, the concentration of NaCl is constant in the
229 presence of varying organic solute concentrations. Therefore, it appears that when the MOS is
230 added to the saturated NaCl solution, the MOS draws water from the speciated NaCl ion pairs
231 and bulk water, increasing the speciated concentration of NaCl. According to the model, NaCl
232 precipitates upon MOS addition to maintain a constant speciated NaCl concentration (i.e.,
233 speciated solubility constant, K_{sp} , is independent of MOS concentration).

234 The displacement of NaCl by MOS was observed for all three ternary mixtures.⁵ A K_{sp}
235 defining the SLE boundary and the implication of ideal molar behavior is surprising, given that
236 concentrated salts and dilute MOS solutions are generally known to be thermodynamically non-
237 ideal. In this case, NaCl deviates modestly with rational activity coefficients of 1.25^{49,50} while MeCN
238 is far from ideal with a rational activity coefficient of 13.5.⁵¹

239 For the ternary mixtures containing MeCN or DME, we observed an invariant point in their
240 liquid phase boundary at the transition between SLE and LLE. The invariant point is the physical
241 condition where the further addition of MOS does not result in a decline of NaCl concentration
242 via solvent-induced crystallization of salt (SLE).^{52,53} Likewise, further addition of NaCl does not
243 result in MOS concentration decline via salt-induced displacement of MOS (LLE).^{52,53} In contrast,
244 the dioxane mixtures do not display a salt-induced LLE despite having a lower dielectric constant
245 than MeCN (i.e., ϵ of 2.1 vs. 36.6).⁵⁴ Further, dioxanes can fractionally crystallize ammonium sulfate
246 whereas nine out of thirteen polar solvents with a higher dielectric constant are incapable of
247 crystallizing ammonium sulfate under the same conditions.⁵⁵ Based on these observations, and
248 in contrast with common rationalizations in the literature,^{56–58} the NaCl precipitation in these
249 ternary mixtures appears to not be driven by solvent polarity as conceived by a primitive non-
250 explicit model of a solution. To better understand these systems an in-depth study of the H₂O-
251 NaCl-MeCN ternary mixture has been conducted. The MeCN system was selected for these studies
252 in part as a proxy for DME (which has potential in SDFC applications^{1,2,5}) because MeCN displays
253 a salt-induced LLE, like DME, but MeCN is a liquid at ambient conditions, in contrast to DME being
254 a gas. The concentrations and property measurements of H₂O-NaCl-MeCN systems can be more
255 accurately measured and controlled than H₂O-NaCl-DME systems because MeCN is a liquid.

256 **3.2. Invariability of Henry's Law Coefficients at Vapor-Liquid Equilibrium**

257 Figure 3A depicts the empirical vapor pressure of H₂O-NaCl-MeCN ternary mixtures, plotted
258 based on an absolute mole fraction basis. In the figure, MeCN was added to a binary H₂O-NaCl
259 mixture, for NaCl concentrations ranging from 0 (pure water) to its binary saturation value. At a
260 solution temperature of 298 K, the vapor pressure of pure MeCN is 12.2 kPa, as compared to the

261 vapor pressure of H₂O at 3.17 kPa. As expected from Henry's law, the addition of MOS induces a
262 linear increment in the solution vapor pressure. The gradient of the linear relationship between
263 the vapor pressure and the MeCN concentration (here evaluated on the absolute scale) is used to
264 calculate the Henry's law coefficient for the H₂O-NaCl-MeCN ternary mixture.

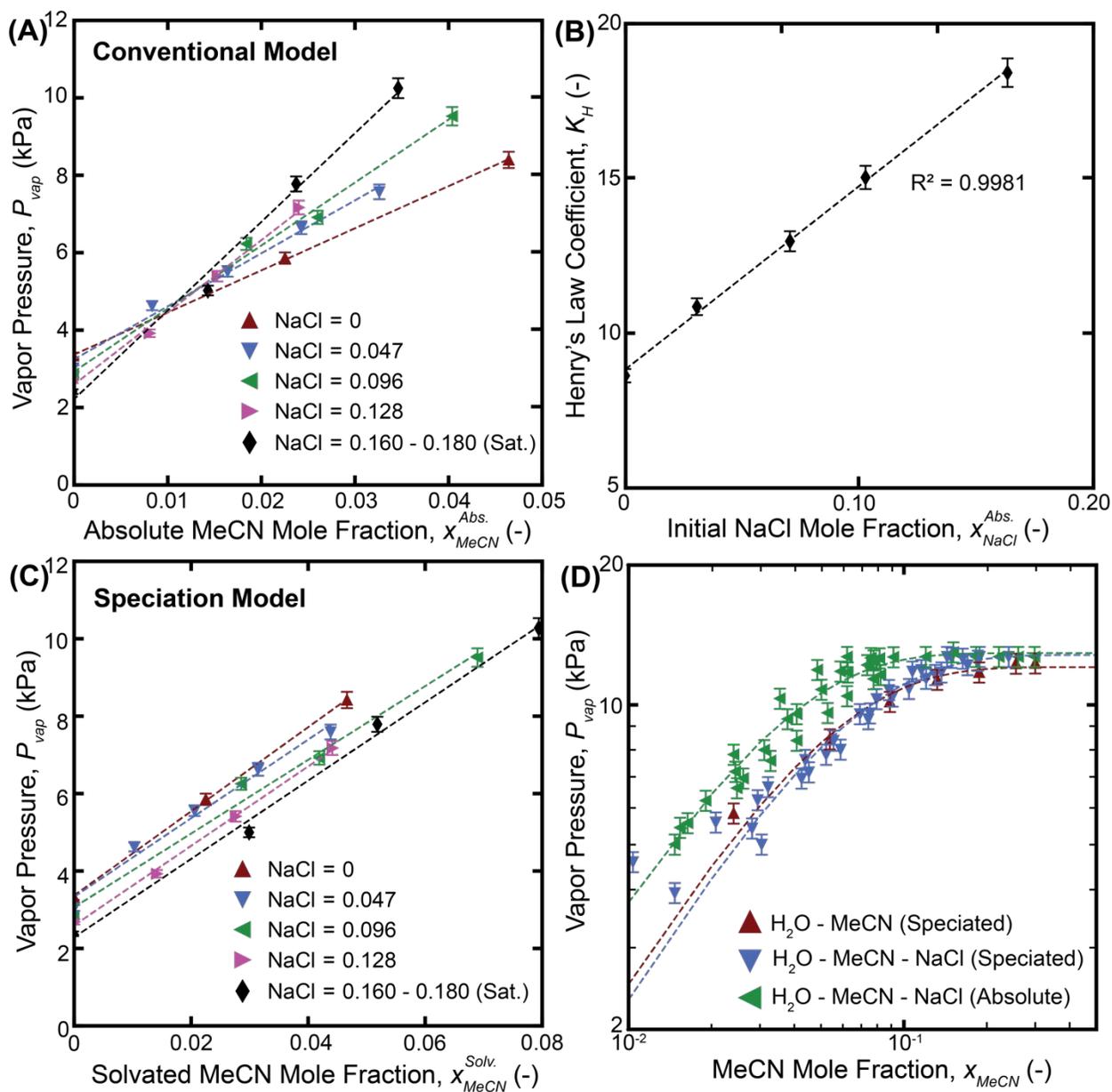
265 The apparent Henry's law coefficient is plotted against the initial NaCl concentrations in
266 Figure 3B, for NaCl concentrations ranging from zero to the binary saturation value. The derived
267 Henry's law coefficient appears to increase with NaCl concentrations, increasing from 816.0 kPa
268 with pure H₂O to 1,689 kPa with saturated NaCl solutions when visualized in absolute mole
269 fractions. A strong linear relationship between the Henry's law coefficient and the initial absolute
270 NaCl mole fraction is evident.

271 Based on classical solution thermodynamics at VLE, the fugacity of H₂O and MeCN are equal
272 between the vapor and the liquid phases.⁵¹ When a small amount of MeCN is added to a NaCl
273 solution, the change in the liquid-phase fugacity of H₂O and MeCN results in a corresponding
274 change to the vapor-phase fugacity. The observed difference in the fugacity shift with varying
275 NaCl concentrations is conventionally rationalized with concentration-dependent fugacity
276 coefficients, which are dimensionless parameters describing the deviations of the vapor pressure
277 from the expected values of an ideal mixture.

278 The vapor pressure of the ternary mixture can be reevaluated against the speciated MeCN
279 mole fractions, as depicted in Figure 3C. The vertical intercepts in the figure correspond to the
280 vapor pressure of the respective binary NaCl solutions. Once speciation effects are incorporated,
281 we observed that the apparent Henry's law coefficients become largely consistent and invariant

282 to the initial NaCl concentrations, averaging 766.5 ± 38.9 kPa, as evident by the parallel linear
283 relationships. This observation is in agreement with recent reports demonstrating alignment with
284 ideal mixing laws even at high solute concentrations, after incorporating speciation effects.^{31,32}

285 The concentration-dependent vapor pressures of H₂O–NaCl and H₂O–NaCl–MeCN are
286 plotted in Figure 3D. Between the two mixtures under the absolute scale, we observed a rise in
287 the apparent vapor pressure for a given MeCN mole fraction, as indicated by the first (H₂O–MeCN
288 Speciated) and third (H₂O–MeCN–NaCl Absolute) series plotted in the figure panel. Of note, when
289 the vapor pressures are reassessed with the speciated mole fractions, the apparent vapor pressure
290 of the ternary mixtures deviates less than 4% from the binary values. In sum, the result suggests
291 that a speciation-based solution theory successfully predicts the vapor pressure of
292 thermodynamically non-ideal mixtures and can potentially be applied to model VLE without
293 fugacity coefficients.



294

295 **Figure 3 (A)** Measured vapor pressures for ternary compositions of H₂O-NaCl-MeCN mixtures plotted
 296 against the absolute mole fraction concentration of MeCN for a series of initial NaCl to H₂O ratios. The slope
 297 is the Henry's Law volatility constant, K_H ; **(B)** K_H plotted against the residual of the initial water activity of
 298 the binary water-NaCl fraction; **(C)** Measured vapor pressures for ternary H₂O-NaCl-MeCN mixtures plotted
 299 against the speciated concentration mole fraction concentration of MeCN. The derived Henry's law
 300 coefficient appears to be invariant with initial NaCl concentration and is consistent across a concentration
 301 range from pure water to binary saturation; **(D)** Plot of the measured vapor pressure versus the mole
 302 fraction of binary H₂O-MeCN and ternary H₂O-NaCl-MeCN mixtures. Once speciation effects are
 303 incorporated, the apparent vapor pressure of the binary and ternary mixtures deviate less than 4% from the
 304 speciated mole fraction of MeCN.

305 Given the proposed interaction mechanism of the speciation-based solution theory the effect
306 of NaCl on the Henry's law constant of MeCN is suspected to affect 1,4-dioxane, DME, and other
307 organic solvents in similar manner. The Henry's law constant of an organic solute expresses the
308 relationship between concentration and activity which directly relates to partial liquid-liquid
309 miscibility and salt-induced LLE. Salt-induced LLE appears to prevent DME from crystallizing salts
310 out of solutions containing a threshold concentration of high-activity salt (salts that reduce the
311 activity of water below ~ 0.9). This threshold is defined by the influence of high-activity salts on
312 the activity/Henry's law constant of DME. Further studies are underway into the threshold for salt-
313 induced LLE in H₂O-salt-DME for various salts. The physical properties that make certain MOS
314 prone to NaCl-induced LLE and other salts are resistant to this LLE can be evaluated with
315 previously published data.

316 **3.3. Implications on Binary and Salt-induced Liquid-Liquid Equilibrium Composition**

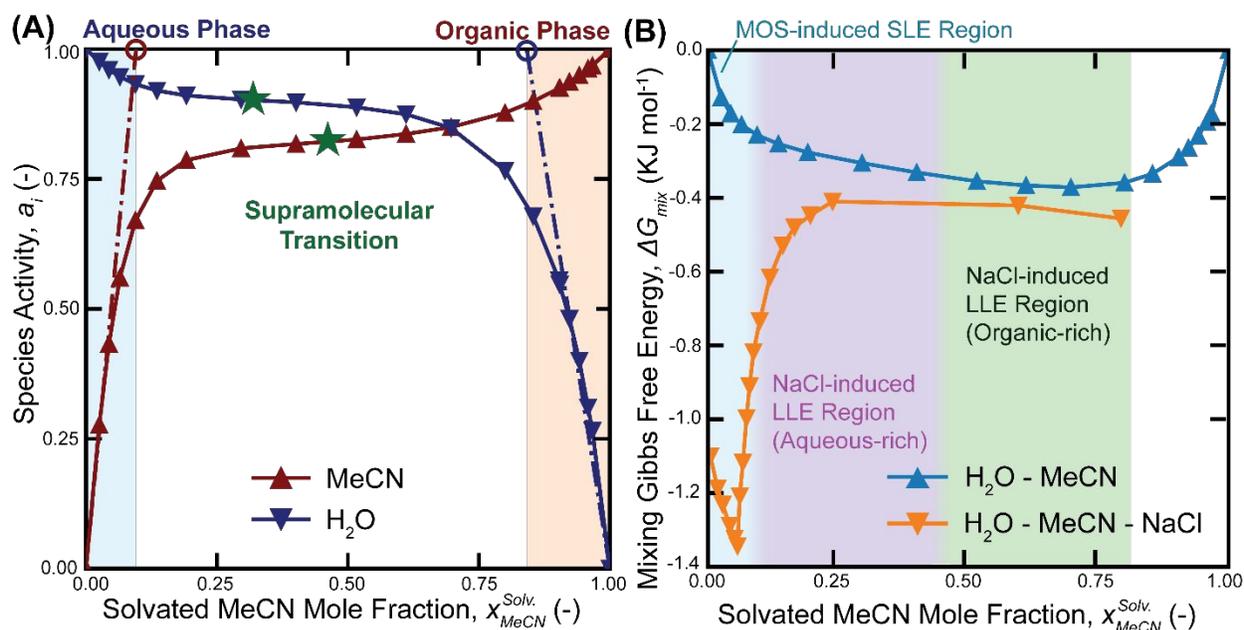
317 In binary H₂O–MOS mixtures at liquid-liquid equilibrium (LLE), complementary saturated
318 compositions exist in both liquid phases, where chemical potentials of water and MOS are equal,
319 producing a condition of isoactivity. A binary mixture with an effective composition in between
320 the two saturation compositions at LLE will disproportionate into the two distinct liquid phases
321 because the intermediate concentration achieves a lower free energy of mixing than the resulting
322 two-phase system. Binary H₂O–MOS mixtures that form positive azeotropes are also likely to
323 exhibit salt-induced LLE in the presence of NaCl, including MOS like tetrahydrofuran,⁵⁹
324 isopropanol,⁶⁰ and 2,2,2-trifluoroethanol⁶¹.

325 Positive azeotropes form due to positive deviations from an ideal linear Raoult's law behavior,
326 arising from hetero interactions (between H₂O and MOS) that are weaker than homo interactions
327 (between H₂O and H₂O, or MOS and MOS). This results in the activities of the components (a_{H_2O}
328 and a_{MOS}) summing to a value greater than unity; any system in which the total activity is greater
329 than unity suggests the existence of two possible distinct phases on a supramolecular scale larger
330 than the solvation environment, even when the mixture appears to be fully miscible.⁶² A growing
331 body of experimental evidence supports the existence of distinct supramolecular or micro-
332 heterogeneous solution states in conventional fully miscible solvent systems, such as the H₂O-
333 MeCN mixture.⁶²⁻⁶⁴

334 The transition from a partially to fully miscible binary mixture can be conceptualized as the
335 process of reducing the compositional difference between the minimum mixing energy states for
336 each of the two separate phases. However, a transition from a two-phase system to a fully mixed
337 single-phase solution requires a dramatic change on a molecular scale. It is likely that
338 supramolecular mixing with micro-heterogeneities would exist at an intermediate state between
339 a partially miscible and a fully mixed binary system. In the binary water-MeCN system, the
340 unambiguous aqueous phase is defined by a linear decline in the water activity at low MeCN
341 concentrations (1:1 correlation between activity and mole fraction based on Raoult's law).
342 Following this linear decline, the mixture enters a region in which the water and MeCN activities
343 plateau, with modest change in the activities with respect to the mole fractions, as depicted in
344 Figure 4A. Based on the conjecture of supramolecular phase segregation, there are likely two
345 micro-phases in this region, a water-rich and an organic-rich phase, which are distinct on length
346 scales of nanometers to micrometers. The changes in water and MeCN activity over the

347 supramolecular mixing region can be attributed to the changes in the relative ratio of the two
348 phases. This interpretation is also supported by a range of spectroscopic, diffraction,
349 computational, and theoretical evidence.⁶⁵

350 In the binary H₂O-MeCN system, the MeCN concentration in the water-rich sub-micron phase
351 at LLE can be estimated from the inflection point of the H₂O activity, as denoted by the solid stars
352 in Figure 4A. For the aqueous-rich phase of the H₂O-MeCN system, this inflection point occurs for
353 water activities between 0.89 and 0.91, suggesting that the H₂O-rich phase is saturated with mole
354 fractions of MeCN ranging from 0.09 to 0.11. The derived molecular solubility values coincide with
355 predictions from Henry's law for MeCN with a solubility of 0.5 mol/(m³·Pa), corresponding to a
356 0.099 mole fraction for MeCN 298 K, as denoted by the red marker at an activity of 1.0.⁶⁶ Similarly,
357 the MeCN molecular phase is saturated with a H₂O mole fraction between 0.17 and 0.19, aligning
358 with the projections from Henry's law for water, as depicted in Figure 4. The aqueous, organic,
359 and supramolecular transitions are also supported by Soft X-ray Absorption Spectroscopy.⁶⁷ These
360 micro-phase compositions also correlate to the MOS activity at the salt-induced LLE, which
361 corresponds to the pressure limit of the H₂O-NaCl-MeCN system in Figure 3D.



362

363 **Figure 4 (A)** Activity isotherm of binary H_2O -MeCN mixtures in VLE at 298.15 K.⁶⁸ The dashed traces relate to Henry's law and their pure component saturation points. Based on the division, the corresponding aqueous, organic, and supramolecular/microheterogeneity phases can be identified; **(B)** Plot of Gibbs free energy of mixing for binary H_2O -MeCN and ternary H_2O -MeCN-NaCl mixtures. The ternary data was calculated with Equation 10 and Table 1 with ternary data between 0.5 and 0.85 MeCN drawn from literature.⁶⁹ The free energy of mixing for the ternary mixtures displays a minimum around MeCN mole fractions of 0.05 and 0.7, corresponding to the NaCl- and MeCN-rich phases, respectively.

370

371 As illustrated in Figure 4B, the minimum mixing energy for binary H_2O -MeCN mixtures is located at a MeCN mole fraction of 0.7. For ternary H_2O -NaCl-MOS mixtures, in general, the Gibbs free energy of mixing profile can have two minimum points, one associated with a high NaCl mole fraction and another associated with a high MOS mole fraction. For MeCN ternary mixtures, the local minima are located at MeCN mole fractions of 0.05 and ~ 0.80 , creating two distinct free energy minima.

377 Water-MOS mixtures that exhibit positive azeotropic phenomena do not necessarily display a salt-induced LLE in a ternary water-NaCl-MOS mixture. For instance, the water-dioxane mixture displays a positive azeotrope but does not achieve the two minima, likely due to the position of

380 the binary free-energy minimum, which is reported at a dioxane mole fraction of ~ 0.5 .^{70,71} Shifting
381 the MOS's organic-water energy minimum from an organic mole fraction of 0.7 (MeCN-Water) to
382 0.5 (dioxanes-water) is towards the salt-defined energy minimum in the ternary mixture (H₂O-
383 NaCl-MOS). The two minima associated with binary mixtures of H₂O-NaCl and H₂O-MOS are likely
384 convoluted in the ternary system (H₂O-NaCl-dioxane). A salt-induced LLE is not observed in water-
385 dioxane mixtures even though dioxane is less polar than MeCN.

386 Acetone and water displays mixed phenomenon with MOS-induced SLE occurring
387 simultaneously with LLE.⁵ Similar to the mixtures with dioxane, the binary water-acetone energy
388 of mixing minimum exists at MOS mole fraction of ~ 0.5 .⁷² This suggests that the binary water-
389 MOS energy of mixing minimum must be at a MOS mole fraction of ~ 0.5 or less to avoid a salt-
390 induced LLE, and that salt-induced LLE is not a result of a low MOS affinity for water. Thus, a binary
391 water-MOS system whose energy of mixing minimum is: 1) shallow (positive deviation from the
392 Raoult's law ideal with a plateau suggesting microstructuring) and; 2) majority organic (i.e. MOS
393 mole fraction greater than ~ 0.5) should be able to produce a salt induced LLE, as is the case with
394 tetrahydrofuran,⁷³ isopropanol,⁷² and 2,2,2-trifluoroethanol.⁷⁴

395 Despite identifying a relationship for micro-phase saturation and interpreting a salt's influence
396 on the Henry's law constant for an MOS, it is unlikely that a speciation-based solution model
397 (based on chemical equilibria alone) can fully characterize salt-induced LLE in H₂O-NaCl-MeCN
398 mixtures, given the microstructural basis of LLE. The salt-induced LLE is quantitatively challenging
399 to model for the same reason it is difficult to model the transition from Henry's law behavior of
400 activity to non-Henry's law activity. The challenges arise because the activity is defined by
401 molecular environments while the supramolecular environments, which involve collections of

402 molecules to form a minimal structural unit, are defined by higher order equilibrium functions that
403 are not easily reduced to lower order equilibrium expressions. The potential of percolation^{19,75–77}
404 or Windsor Type III⁷⁸ phase theories to bridge the existing gaps for the microstructured mixtures
405 should be evaluated in future work.

406 **4. Conclusions**

407 This paper is the first application of a speciation-based model to correlate the vapor-liquid
408 and solid-liquid equilibria of ternary mixtures containing organic solutes. The model utilizes two
409 equilibrium constants for each solute, accounting for ion pairing and solute solvation phenomena.
410 Using speciated mole fractions, our results indicate that the solid-liquid equilibrium boundaries
411 of ternary H₂O-NaCl-MeCN mixtures are governed by a simple saturation equilibrium condition
412 that is consistent with the respective saturation coefficients of the binary mixtures. Furthermore,
413 the degree of NaCl precipitation appears to be uncorrelated with changes in the solution dielectric
414 behavior. Original measurements for the vapor pressure of ternary H₂O-NaCl-MeCN mixtures
415 were recorded, for NaCl mole fractions ranging from zero to saturation and MeCN mole fractions
416 ranging from 0 to 0.64 on an absolute mole fraction scale. At vapor-liquid equilibrium, the
417 variability of the Henry's law coefficient fell from 107% to 5.1% once speciation effects were taken
418 into account by the proposed model. Deeper analysis suggests that salt-induced liquid-liquid
419 equilibrium occurs in ternary mixtures where the MOS phase exhibits stronger interactions with
420 the water solute than the corresponding interactions between the water phase and the MOS
421 solute. The proposed speciation framework can be leveraged as a basis for future work to model
422 liquid-phase microheterogeneities for the prediction of salt-induced SLE, organic-induced LLE,
423 and VLE of ternary systems.

424 **Nomenclature**

Symbol	Description
a_n	Species activities defined by domains (Table 1)
a_x	Activity of solute NaCl or MOS
$K_x^{Hyd.}$	Hydration equilibrium constant of NaCl or MOS
$K_x^{Dis.}$	Ion-pair dissociation equilibrium constant of NaCl
k_{MOS}^{sol}	Average speciated Henry's Law constant
B	Sum electrolyte; meaning varies with superscript
$B +$	Cation
$B -$	Anion
$B \pm$	Modeled ion pair
g	Gibbs free energy
$n(H_2O)_B^{Hyd.}$	Concentration-dependent hydration variable
m	Hydration exponent
MOS	Miscible organic solvent
$x_x^{Abs.}$	Absolute concentration of NaCl or MOS
$x_{H_2O}^{Bulk}$	H ₂ O not energetically involved in solvation of solute
$x_x^{Sat.}$	Saturated concentration
$\bar{x}_x^{Solv.}$	Unnormalized speciated concentration of NaCl or MOS
$x_x^{Solv.}$	Speciated concentration of NaCl or MOS

425

426 **Author Contributions**

427 **A.D. Wilson:** Conceptualization, Computation, Formal Analysis, Writing – Original Draft; **Z.H. Foo:**
428 Visualization, Computation, Formal Analysis, Writing – Original Sections; **A.S. Jayasinghe, C.**
429 **Stetson, H. Lee, H.W. Rollins:** Experiment, Writing – Review and Editing; **A. Deshmukh, J.H.**
430 **Lienhard:** Formal Analysis, Writing – Review and Editing

431 **Conflicts of Interest**

432 The authors declare no conflicts of interest that may have appeared to influence the content of
433 this paper.

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