

**Solute diffusion and partitioning in multi-arm poly(ethylene glycol) hydrogels**

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1 Solute diffusion and partitioning in multi-arm poly(ethylene glycol) hydrogels

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10 Abstract

11 Controlling solute transport in hydrogels is critical for numerous chemical separation applications,
12 tissue engineering, and drug delivery systems. In previous review work, we have pointed out that
13 proposed theoretical models and associated experiments tend to oversimplify the influence of
14 hydrogel structure on solute transport by addressing only the effects of the polymer volume
15 fraction and mesh size of the networks on solute transport. Here, we reexamine these models by
16 experimenting with a library of multi-arm poly(ethylene glycol) (PEG) hydrogels with simultaneous
17 variations in four independent structural parameters. Standardized, high-throughput fluorescence
18 recovery after photobleaching (FRAP) experiments in hydrogels characterize size-dependent
19 solute diffusion and partitioning in each hydrogel formulation. Solute diffusivity dependence on
20 junction functionality shows an influence from network geometry that is not addressed by mesh
21 size-based models, experimentally validating the use of the geometry-responsive mesh radius in
22 solute diffusivity modeling. Furthermore, the Richbourg-Peppas swollen polymer network (SPN)
23 model accurately predicts how three of the four structural parameters affect solute diffusivity in
24 hydrogels. Comparison with the large pore effective medium (LPEM) model showed that the SPN
25 model better predicts solute size and hydrogel structure effects on diffusivity. This study provides
26 a framework for investigating solute transport in hydrogels that will continue to improve hydrogel
27 design for tissue engineering and drug delivery.

28 Keywords:

29 Solute transport; hydrogel; mesh size; mesh radius; swollen polymer network model

30 Introduction

31 Understanding solute transport in hydrogels is important for molecular separation processes using
32 hydrogel membranes,¹ for controlling drug delivery from hydrogel reservoirs,² and for managing
33 cellular communication in hydrogel-based tissue engineering scaffolds.³ Fluorescence recovery
34 after photobleaching (FRAP) experiments in hydrogels are an exceptionally accurate and fast,
35 high-throughput method for characterizing solute self-diffusion within hydrogels.⁴ Additionally, the
36 confocal microscope used for FRAP can quantify the partitioning of the solutes into the hydrogel
37 by comparing the concentrations of solutes within the hydrogel and in the source solution.

38 Solute diffusion and partitioning in hydrogels are generally understood to be affected by both the
39 properties of the solute and properties of the hydrogel, but current models generalize the solute

40 contributions to their hydrodynamic radii and the hydrogel contributions to their swollen polymer
41 volume fraction, mesh size, and fiber radius.⁵⁻¹⁰ Our previous work investigating the diffusion of
42 fluorescently tagged dextrans and linear poly(ethylene glycol) (PEG) in poly(vinyl alcohol) (PVA)
43 hydrogels demonstrated that solute diffusivities in hydrogels do not scale consistently with
44 hydrodynamic radius.⁴ Dextran diffusivity in hydrogels decreased with increasing solute size, but
45 PEG diffusivity increased with increasing solute size, indicating that solute interactions with the
46 hydrogel based on shape or chemistry may disrupt the size-dependence of their diffusion within
47 hydrogels.

48 In a theoretical analysis,¹¹ we argued that mesh size is a poor descriptor for solute diffusivity since
49 it does not account for how the geometry of the swollen polymer network influences solute
50 diffusivity. The proposed mesh radius correction for hydrogels with four, six, or eight chains
51 converging at a junction aims to account for the limitations of using mesh size (Fig. 1). The
52 accuracy of the mesh radius correction has not yet been experimentally tested, so we do so here.
53 In addition to comparing our swollen polymer network (SPN) model predictions to measurements,
54 we consider an alternative model, the large pore effective medium model (LPEM), which was
55 derived by Liu et al. to account for hydrodynamic drag and network obstruction of solute diffusion
56 only within accessible liquid-filled voids.⁶ Liu et al. provide the complete algorithm for calculating
57 solute diffusivities in hydrogels using the LPEM model in their work and demonstrate that it is
58 more effective for representing the diffusivity of FITC-dextrans in hydroxyethyl methacrylate
59 (HEMA)/methacrylic acid (MAA) hydrogels than Ogston model,¹² Phillips model,¹³ and
60 effective medium model.^{14, 15} The LPEM model notably uses obstruction/steric and hydrodynamic
61 theories of solute diffusion in hydrogels^{5, 6} and summarizes solute influence as the solute radius
62 and hydrogel influences as the polymer volume fraction, network tortuosity, and the fiber radius
63 (effectively ignoring the influences of the hydrogel structural parameters emphasized in the SPN
64 model). Direct comparison between the predictions of the SPN and LPEM models is possible
65 since both models use specific, quantitative parameters of the solute and network to predict the
66 diffusion coefficient of the solute within the hydrogel, despite fundamental differences in how
67 those values are calculated. Comparing theoretical models with robust experimental datasets is
68 critical for evaluating the advantages and limitations of each model.

69 Additional design-relevant information about solute-hydrogel interactions can be gained by
70 varying hydrogel structure using the independent, synthesis-controlled parameters considered in
71 the SPN model.^{7, 11} In our previous work, we investigated the diffusion of fluorescein, dextrans,
72 and PEGs in eighteen PVA hydrogel formulations with varying initial polymer volume fraction (ϕ_0)
73 and degree of polymerization between junctions (N_j). Here, we expand our focus on how hydrogel
74 structure affects solute diffusivity and investigate solute partitioning with fluorescein and two sizes
75 of dextrans in 73 formulations of multi-arm PEG hydrogels via simultaneous variation of four
76 independent, synthesis-controlled structural parameters: initial polymer volume fraction, degree
77 of polymerization between junctions, junction functionality (f), and frequency of chain-end defects
78 (γ). Full-factorial analysis of how these structural parameters affect solute diffusion and
79 partitioning in hydrogels provides unprecedented insight into how the hydrogel structure affects
80 solute transport, including confirming possible interactions between structural parameters that
81 might be obscured by a lower factorial matrix of formulations. Furthermore, the full factorial
82 approach provides context on hydrogel structural design options by showing how the limitations
83 of gelation depend on the intersection of multiple structural parameters.

84 In this study, we investigate the influences of hydrogel structure on solute diffusion and
85 partitioning in hydrogels and evaluate correlations between hydrogel swelling, solute diffusion in
86 hydrogels, and solute partitioning in hydrogels. We show that mesh size is an incomplete
87 descriptor of solute transport in hydrogels, especially when considering junction functionality as a
88 controllable parameter. Finally, we compare predictions of solute diffusion in hydrogels using the
89 SPN model and the LPEM model. Coordinating fundamentally derived hydrogel modeling with
90 robust experimental analysis clarifies the nuanced relationships between structure and function
91 necessary for biomedically relevant hydrogel design.¹⁶

92 **Methods**

93 **Norbornene-functionalization of hydroxyl-terminated multi-arm poly(ethylene glycol)**

94 To create norbornene-functionalized multi-arm PEG precursors, hydroxyl-terminated multi-arm
95 PEGs were functionalized based on adaptations of previously described protocols.^{17, 18} Nine
96 precursor polymers were used, all purchased from JenKem Technology USA (Plano, TX): (1) 4-
97 arm, 10 kDa PEG, (2) 4-arm, 15 kDa, (3) 4-arm, 20 kDa, (4) 6-arm, 15 kDa, (5) 6-arm, 21 kDa,
98 (6) 6-arm, 30 kDa, (7) 8-arm, 20 kDa, (8), 8-arm, 30 kDa, and (9) 8-arm, 40 kDa. The nine
99 polymers were chosen to explore three junction functionalities (4, 6, and 8) and three sets of
100 chain-arm lengths (approx. 2.5 kDa per arm, 3.75 kDa, and 5 kDa), which correspond to the
101 degree of polymerization between junctions ($N_j = 115, 165, 215$). For all precursor macromers,
102 polydispersity was confirmed by the manufacturer to be less than 1.05 and independently
103 confirmed upon receipt by gel permeation chromatography (data available upon request). All other
104 reagents and solvents were purchased from Sigma-Aldrich (St. Louis, MO) unless otherwise
105 noted.

106 Briefly, all reagent concentrations were scaled to the expected concentration of hydroxyl end-
107 groups for 5 g of the batch's PEG precursor. Initially, 5 molar equivalents (to PEG -OH groups) of
108 N,N'-dicyclohexylcarbodiimide and 10 molar equivalents of 5-norbornene-2-carboxylic acid were
109 mixed in 20 mL of dichloromethane under a nitrogen atmosphere and reacted at room
110 temperature for 30 minutes. The product solution was then centrifuged at 3000 rpm for 10 minutes
111 at room temperature in a Sorvall ST-16R centrifuge (Thermo Scientific, Waltham, MA) to separate
112 the precipitated byproduct. The supernatant liquid was then added to a 40 mL dichloromethane
113 solution on ice that contained 5 g of multi-arm PEG precursor, 5 molar equivalents of pyridine,
114 and 0.5 molar equivalents of 4-(dimethylamino)pyridine (DMAP) under a nitrogen atmosphere.
115 The resulting solution was left to react overnight on ice, under nitrogen, and in darkness. The
116 reacted solution was precipitated and centrifuged twice in ice-cold diethyl ether, and the resulting
117 pellet was left overnight to dry. The dry pellet was then resuspended in deionized water and
118 dialyzed for 24 hours (2000 MWCO) before lyophilization and storage until use. Norbornene
119 functionalization was confirmed via ¹H NMR (Agilent MN400) in triplicate with 16 scans per sample
120 (other parameters set based on UT Austin NMR core facility standards).¹⁹ Functionalization and
121 NMR protocols are included in the supplementary materials.

122 **Synthesis of multi-arm poly(ethylene glycol) hydrogels**

123 Multi-arm PEG hydrogels were synthesized with simultaneous variation along four structural
124 parameters. The structure of the multi-arm precursors defined the degree of polymerization
125 between junctions ($N_j = 115, 165, 215$) and the junction functionality ($f = 4, 6, 8$). The
126 concentration of the polymer in water defined the initial polymer volume fraction ($\varphi_0 =$

127 0.050, 0.075, 0.100), and the stoichiometric ratio of norbornene groups to crosslinking thiols
128 (dithiothreitol, DTT) defined the frequency of chain-end defects ($\gamma = 0, 0.2, 0.4$). The combination
129 of four structural parameters each with three values produced eighty-one unique hydrogel
130 formulations, but six hydrogel formulations were not able to form stable gels (A4-N115-V050-F04,
131 A4-N165-V050-F04, A4-N215-V050-F04, A4-N215-V075-F04, A4-N215-V100-F04, A8-N165-
132 V050-F04) and two formulations were not synthesized due to limited resources (A6-N165-V050-
133 F04, A6-N165-V075-F04), resulting in a total of 73 intact hydrogel formulations.

134 Briefly, multi-arm PEG solutions were made from 1X phosphate-buffered saline (PBS), one of the
135 nine norbornene-terminated PEG precursors, DTT, and the photoinitiator Lithium phenyl-2,4,6-
136 trimethylbenzoylphosphinate (LAP). Each solution was vortexed, then 3 mL of the solution was
137 placed between glass plates with a 1.5 mm spacer and placed on a UV transilluminator (365 nm,
138 3 mW/cm²; Analytik Jena, Germany) for 30 seconds on one side and 30 seconds on the other
139 side. For each hydrogel formulation, photo-crosslinking was repeated with three different 3-mL
140 solutions to account for variability. Immediately after photo-crosslinking, swelling was analyzed
141 for each hydrogel formulation. Hydrogel synthesis protocols are included in the supplementary
142 materials.

143 **Volumetric swelling characterization**

144 Volumetric swelling of the multi-arm PEG hydrogel formulations was characterized as previously
145 described.²⁰ Briefly, the volumes of 18-mm diameter hydrogel disc samples were measured
146 immediately following photo-crosslinking via a scale and density kit. Samples were then swollen
147 to equilibrium for 24 hours and their volumes were measured again. Finally, samples were dried
148 for 24 hours with heat (40 °C) and vacuum to measure the dry volumes. Swollen polymer volume
149 fractions (φ_s) were calculated by dividing the dry volume by the swollen volume for each sample.
150 Swollen polymer volume fractions were averaged for each hydrogel formulation ($n = 3$).
151 Remaining hydrogel samples used for solute diffusivity and partitioning measurements were kept
152 in the equilibrium-swollen state by storage in an excess of PBS.

153 **Solute diffusivity characterization**

154 The diffusivities of three solutes were determined in each of the 73 hydrogel formulations via
155 FRAP as previously described.⁴ In brief, fluorescein, fluorescein isothiocyanate-conjugated 4 kDa
156 dextran (4 kDa FITC-Dextran), and 20 kDa FITC-dextran were selected as fluorescent solutes
157 representing a range of solute sizes. Solute free diffusion coefficients (D_0) were determined via
158 FRAP in solution experiments, and hydrodynamic radii (r_s) were calculated using the Stokes-
159 Einstein equation, yielding 0.9 nm hydrodynamic radius for fluorescein, 1.7 nm for 4 kDa FITC-
160 dextran, and 2.9 nm for 20 kDa FITC-dextran. For each solute and hydrogel formulation pairing,
161 three hydrogel samples (2 mm diameter) were incubated for 24 hours in 3 mL of a 10 μ M solution
162 of the solute in PBS. 20 μ M was used for 4 kDa FITC-dextran due to low fluorescence intensities
163 at 10 μ M. FRAP experiments were performed with three runs per sample ($n = 9$ per solute-
164 formulation pairing) on a Zeiss LSM710 Confocal Microscope (Zeiss, Germany). FRAP analysis
165 was performed using our high-throughput FRAP analysis MATLAB program,⁴ yielding diffusion
166 coefficients for each solute-hydrogel pairing. Solute diffusivity data and the FRAP experiment
167 protocol are available online with links provided in the supplementary materials.

168 **Solute partitioning characterization**

169 For each solute-hydrogel pairing, solute partitioning into the hydrogel was measured by
 170 comparing fluorescence intensities. The pre-bleaching fluorescence intensity within each
 171 hydrogel and the fluorescence intensity of the source solution were measured under the same
 172 confocal imaging conditions (same experimental session, laser power, and intensity) using
 173 ImageJ analysis software. Measured intensities were compared to standard curves to confirm a
 174 linear relationship between intensity and concentrations, and then partitioning was calculated by
 175 the ratio C/C_0 , where C is the solute concentration within the hydrogel and C_0 is the concentration
 176 in the source solution. Partition coefficients were averaged across the three scans per each of
 177 three samples per solute-formulation pairing ($n = 9$). Solute partitioning data is available online
 178 with links provided in the supplementary materials.

179 Predictive swollen polymer network modeling of solute diffusion in hydrogels

180 Structure-based predictions of mesh size, mesh radius, and specific solute diffusivities in each
 181 hydrogel were made using the SPN model.^{7, 11} Swollen polymer volume fractions (φ_s) were
 182 calculated via Equation 1.

$$183 \quad \varphi_s^{-\frac{1}{3}} [\ln(1 - \varphi_s) + \varphi_s + \chi_1 \varphi_s^2] = -1 * \frac{\rho_d V_1}{M_r N_j} (1 - \gamma) \left(1 - \frac{2}{f}\right) \varphi_0^{\frac{2}{3}} \#(1)$$

184 In Equation 1, N_j , γ , f , and φ_0 are defined by the specific hydrogel formulation's network structure
 185 as explained above, and $\chi_1 = 0.426$ for PEG, $\rho_d = 1.12 \text{ g/mL}$ for PEG, $V_1 = 18 \text{ mL/mol}$ for water,
 186 and $M_r = 44 \text{ g/mol}$ for PEG.²⁰

187 Mesh size (ξ) was calculated from the swollen polymer volume fraction, structural parameters,
 188 and identity constants using Equation 2, a modification of the Canal-Peppas equation.^{7, 21}

$$189 \quad \xi = \varphi_s^{-\frac{1}{3}} \left(\left(1 - \frac{2}{f}\right) \bar{l}^2 C_\infty \lambda N_j \right)^{\frac{1}{2}} \#(2)$$

190 In Equation 2, $\bar{l} = 0.15 \text{ nm}$, $C_\infty = 4$, and $\lambda = 3$ for PEG.

191 Mesh radii (r_m) were calculated from mesh sizes and junction functionalities using Equation 3.¹¹

$$192 \quad r_m = \begin{cases} \frac{\sqrt{6}}{3} \xi & f = 4 \\ \frac{1}{2} \xi & f = 6 \#(3) \\ \frac{\sqrt{2}}{4} \xi & f = 8 \end{cases}$$

193 Solute diffusivities in hydrogels (D) were calculated according to Equation 4, a modified multiscale
 194 diffusion model based on hydrogel and solute properties.^{4, 7, 11, 22}

$$195 \quad \frac{D}{D_0} = \operatorname{erf} \left(\frac{r_{FVW}}{r_s} \right) \exp \left[-1 * \left(\frac{r_s}{r_{FVW}} \right)^3 \left(\frac{\varphi_s}{1 - \varphi_s} \right) \right] + \operatorname{erfc} \left(\frac{r_{FVW}}{r_s} \right) \exp \left[-\frac{\pi}{4} \left(\frac{r_s + r_f}{r_m} \right)^2 \right] \#(4)$$

196 In Equation 4, D_0 is the diffusivity of the solute in a free aqueous solution and r_s is the associated
197 hydrodynamic radius of the solute. As measured previously,⁴ for fluorescein, $D_0 = 278 \mu\text{m}^2/\text{s}$ and
198 $r_s = 0.88 \text{ nm}$. For 4 kDa FITC-dextran, $D_0 = 142 \mu\text{m}^2/\text{s}$ and $r_s = 1.73 \text{ nm}$. For 20 kDa FITC-
199 dextran, $D_0 = 85 \mu\text{m}^2/\text{s}$ and $r_s = 2.89 \text{ nm}$. The average radius of free volume voids in water is r_{FVW}
200 $= 0.269 \text{ nm}$,²² and the fiber radius of PEG with a monolayer of water is $r_f = 0.51 \text{ nm}$.

201 The primary method for predicting solute diffusivity in hydrogels used in this work is to calculate
202 Equations 1-4 in sequence with D as the output. To compare with prior models that ignored how
203 mesh radius differs from mesh size based on network geometry, diffusion coefficients for each
204 solute and hydrogel pairing were also calculated with Equation 3 omitted and with half the mesh
205 size ($\xi/2$) substituted for mesh radius in Equation 4 (reproducing the multiscale diffusion model
206 of Axpe et al.²² without the mesh radius correction).¹¹ SPN model predictions are available online
207 with links provided in the supplementary materials.

208 **Predictive large pore effective medium modeling of solute diffusion in hydrogels**

209 Solute diffusivities in hydrogels were calculated using the LPEM model⁶ as an external
210 comparison to the swollen polymer network model predictions. The full derivation of the LPEM
211 model is provided in the original work.⁶ Here, we repeat the LPEM predictive calculations for multi-
212 arm PEG hydrogels, using 0.51 nm as the fiber radius for PEG,²² a tortuosity of 1 for dilute PEG
213 hydrogels,²³ and the measured swollen polymer volume fractions as the relevant polymer volume
214 fractions. LPEM model predictions and the R script used to make them are available online with
215 links provided in the supplementary materials.

216 **Results**

217 **Experimental design and hydrogel synthesis**

218 This work aims to experimentally validate the fundamental model-predicted relationships between
219 hydrogel structure and solute transport in hydrogels, specifically focusing on the diffusion
220 coefficients and partitioning of solutes in the hydrogels. A library of 73 unique multi-arm PEG
221 hydrogel formulations was synthesized by systematic, simultaneous variation of four structural
222 parameters: the degree of polymerization between junctions (N_j), the junction functionality (f), the
223 initial polymer volume fraction (φ_0), and the frequency of chain-end defects (γ).¹¹ Six of the initially
224 planned 81 formulations did not form stable, intact hydrogels, and two were not synthesized due
225 to limited synthesis materials. Of the six incomplete formulations, all six had the highest frequency
226 of chain-end defects ($\gamma = 0.4$), five had four arms ($f = 4$), and four had the lowest initial polymer
227 volume fraction ($\varphi_0 = 0.050$). Since no one parameter value consistently failed to form intact
228 hydrogel formulations, this suggests that gelation is affected by the combination of all four
229 structural parameters. Notably, the lowest frequency of chain-end defects ($\gamma = 0.4$) was chosen
230 to be just above the required “real” junction functionality of >2 for the four-arm precursors. Two
231 connecting chains or less from each macromer would result in a linear polymer or no
232 polymerization, respectively. That four of the four-arm, $\gamma = 0.4$ formulations formed intact
233 hydrogels near this boundary of the gelation space indicates that the photoinitiated norbornene-
234 DTT crosslinking reaction is robust and efficient, despite the likelihood of other unmeasured
235 variations in the overall network structure of each hydrogel formulation. Comparison with other
236 methods of crosslinking multi-arm PEG hydrogels may help to clarify the role of crosslinking
237 reactions on overall network structure.^{18, 24-27}

238 Each hydrogel formulation was paired with three solutes of varying sizes for diffusion and
239 partitioning experiments. Fluorescein (0.9 nm hydrodynamic radius) represents a small, soluble
240 molecule, and 4 kDa and 20 kDa FITC-dextran (1.7 nm and 2.9 nm) are included to show how
241 increasing solute size affects their transport in hydrogels. Diffusivity and partitioning were
242 measured directly for each solute-hydrogel pairing and compared to fundamental predictions
243 made using the SPN and LPEM models.^{4, 6, 7, 11}

244 **Main solute size effects on partitioning and diffusion**

245 Generally, solute diffusivity within hydrogels and partitioning into hydrogels decreased with
246 increasing solute size (Fig. 2). The hydrogel formulation-dependent ranges for solute diffusivity
247 and partitioning per solute were broadest for the smallest solute, fluorescein, and narrowest for
248 the largest solute, 20 kDa FITC-dextran. Notably, some of the fluorescein-hydrogel pairings
249 exhibited diffusion coefficients higher than the measured diffusion coefficient of fluorescein in free
250 solution ($278 \mu\text{m}^2/\text{s}$). This is likely due to fluorescein forming dimers in free solution, whereas the
251 more constrained hydrogel environment would favor monomers that are smaller and diffuse more
252 quickly (estimated $D_0 = 489 \mu\text{m}^2/\text{s}$ and $r_s = 0.50 \text{ nm}$).⁴ 4 kDa and 20 kDa FITC-dextran in
253 hydrogels all have diffusivities lower than their diffusivities in free solution ($142 \mu\text{m}^2/\text{s}$ and 85
254 $\mu\text{m}^2/\text{s}$).

255 The partition coefficients much greater than one for the fluorescein-hydrogel pairings indicate that
256 fluorescein has an attractive chemical interaction with the PEG hydrogels, likely resulting from the
257 negative charge of fluorescein, which is not shared by the neutral FITC-dextran. The widely
258 spread, multimodal distribution of partition coefficients for fluorescein in the hydrogels, including
259 partition coefficients less than one, indicates that the network structure has a significant effect on
260 fluorescein partitioning. 4 kDa FITC-dextran have partition coefficients slightly greater than one
261 in three hydrogel formulations but are otherwise less than one, and all 20 kDa FITC-dextran
262 pairings have partition coefficients well below one.

263 Unlike diffusivity, which is measured by self-diffusion coefficients within hydrogels, partitioning is
264 affected by the surface accumulation of solutes. Surface accumulation is more likely for larger
265 solutes that can be excluded from the network, as shown by qualitative imaging at the edges of
266 hydrogel samples (Supp. Fig. S1). Negligible surface accumulation was observed for fluorescein
267 (Supp. Fig. S1A), and significant accumulation was observed for the larger 20 kDa FITC-dextran
268 (Supp. Fig. S1B), which may block solute transport into the network and contribute to the reduced
269 large-solute partitioning into hydrogels. Notably, none of the 73 hydrogel formulations completely
270 excluded any of the three solutes.

271 **Hydrogel structure effects on partitioning and diffusion**

272 The 73 multi-arm PEG hydrogel formulations based on a matrix of four structural parameters
273 provide a robust dataset for evaluating how hydrogel structure affects the partitioning and diffusion
274 of solutes in hydrogels. Comparing swollen polymer volume fractions to solute diffusion and
275 partitioning, grouped by degree of polymerization between junctions (Fig. 3), shows that solute
276 diffusivity tends to decrease with increasing swollen polymer volume fraction (Fig. 3A-C), whereas
277 partitioning does not show a consistent overall trend (Fig. 3D-F). Curiously, for fluorescein and 20
278 kDa FITC-dextran, swelling-diffusivity trends are separated by degree of polymerization between
279 junctions, with increasing degrees shifting the trend down and to the left (Fig. 3A,C) but the
280 intermediate size solute, 4 kDa FITC-dextran does not show the same dependence on the degree

281 of polymerization between junctions (Fig. 3B). Though not further separated by color and shape,
282 initial polymer volume fraction, junction functionality, and frequency of chain-end defects have
283 redundant effects on the relationship between swelling and solute diffusivity (see Supp. Fig. S2).
284 Increasing initial polymer volume fraction and junction functionality decreases diffusivity and
285 increases swollen polymer volume fraction, and increasing the frequency of chain-end defects
286 increases diffusivity and decreases the swollen polymer volume fraction.

287 Contrasting the strongly correlated diffusivity trends, solute partitioning into the hydrogels
288 inconsistently correlates with swollen polymer volume fraction and the four controlled structural
289 parameters. For 20 kDa FITC-dextran, partitioning appears to decrease with increasing swollen
290 polymer volume fraction (Fig. 3F), which would seem reasonable on the assumption that having
291 more polymer would reduce the solute-accessible volume within the hydrogel, but fluorescein and
292 4 kDa FITC-dextran do not match this trend (Fig. 3D-E). Furthermore, the grouping effect of the
293 degree of polymerization between junctions is not consistent across the three solutes, and the
294 degree of polymerization between junctions does not have a consistent influence on partitioning.

295 Summarizing the main effects of structural parameters on diffusion and partitioning is informative
296 to hydrogel design (Table 1). Generally, initial polymer volume fraction and junction functionality
297 have simple interactions with solute diffusivity and partitioning. Increasing either structural
298 parameter consistently decreases both diffusivity and partitioning.

299 Increasing the frequency of chain-end defects increases diffusivity across all three solutes but
300 has a size-dependent effect on partitioning. Increasing the frequency of chain-end defects
301 decreases partitioning for the small solute, fluorescein, has little effect on the mid-sized solute, 4
302 kDa FITC-dextran, and increases partitioning for the largest solute, 20 kDa FITC-dextran. This
303 size-dependent shift in partitioning, especially in the context of a consistent diffusivity effect,
304 establishes the frequency of chain-end defects as a potential high-contrast parameter for
305 hydrogel-based separations applications.

306 As indicated in Fig. 3, the degree of polymerization between junctions has an inconsistent effect
307 on solute diffusivity and partitioning. No trends were conserved across the three solutes for either
308 diffusivity or partitioning. These results starkly contrast both modeling predictions and prior data
309 with similar structural manipulations on comparable hydrogel systems,^{4, 7, 11, 20} as will be further
310 discussed in the following sections.

311 **Relationship between solute partitioning and diffusion in hydrogels**

312 Solute diffusivity and partitioning are both key properties of solute transport in hydrogels, but they
313 are not correlated across variations in multiple structural parameters and varying solute sizes
314 (Fig. 4). However, according to the relationships in Table 1, if initial polymer volume fraction and
315 junction functionality were the only two structural parameters varied, they would be positively
316 correlated. This difference demonstrates how limited experimental spaces can lead to
317 oversimplified conclusions about structure and property interactions.

318 **Mesh size, mesh radius, and network geometry**

319 Mesh size is often used as an intermediate structural parameter to summarize solute transport in
320 hydrogels.²⁸⁻³⁵ Unlike the four structural parameters used to define hydrogel formulations
321 throughout this work, mesh size is an intermediate descriptor because it is a composite result of
322 several network interactions and therefore not independently tunable. It has not been measured

323 directly because it is a nanoscale, average property that must be measured in a hydrated state.
324 Moreover, the novel ability to explicitly control junction functionality with multi-arm PEG hydrogels
325 requires that we consider network geometry in addition to mesh size when evaluating solute
326 transport in hydrogels.¹¹ We previously suggested that mesh radius should replace mesh size in
327 the multiscale diffusivity model (as shown in Eq. 4), but we did not have experimental data on
328 hydrogels with varying junction functionality to prove our theoretical argument at the time.

329 Selecting a subset of hydrogel formulations that only varies junction functionality ($f = 4,6,8$) while
330 keeping the other structural parameters consistent ($\phi_0 = 0.075, N_j = 165, \gamma = 0.2$), we observe
331 that diffusivity predictions based on mesh radius better correlate with measured values than
332 predictions based solely on mesh size (Fig. 5). For fluorescein, both mesh size- and mesh radius-
333 based predictions positively correlated with measured diffusivities (Fig. 5A), but for the larger 4
334 kDa FITC-dextran and 20 kDa FITC-dextran, mesh-size based predictions negatively correlated
335 with measured diffusivities (Fig. 5B-C). With larger solutes that are closer in size to the mesh
336 radius and mesh size of the network, the effect of network geometry on solute diffusivity is more
337 substantial. The junction functionality-dependent shift from negative prediction-measurement
338 correlation using the mesh size equation to positive prediction-measurement correlation using the
339 mesh radius equation is consistent across the full library of hydrogel formulations (Supp. Fig. S4).
340 These results indicate that mesh size is insufficient for predicting the diffusivity of larger solutes
341 in hydrogels without addressing network geometry via the mesh radius correction.¹¹

342 **Comparison with the Large Pore Effective Medium Model**

343 The SPN model is one of several models under active investigation for solute transport in
344 hydrogels.⁵ Many of these models, including the SPN model, have not been experimentally cross-
345 evaluated by research groups other than the ones who proposed them, meaning that they are
346 often tested on limited datasets. One of the main restrictions to these cross-evaluating studies is
347 that researchers do not provide enough information about the models or the raw experimental
348 datasets they are interpreting with the models to facilitate comparisons. Serious, unbiased cross-
349 evaluation efforts would help to identify the advantages and limitations of different models. Here,
350 we consider the LPEM model proposed by Liu et al.⁶ because 1) it derives from obstruction and
351 hydrodynamic theories, complementing the obstruction and free volume theory sources for the
352 SPN model, 2) Liu et al. demonstrated that it describes the diffusion of 4 kDa FITC-dextran and
353 20 kDa FITC-dextran in HEMA/MAA hydrogels better than three related models, 3) it is presented
354 with fully defined equations so the calculations can be applied to a different dataset, and 4) it is a
355 fundamental model with no phenomenological fitting parameters. However, like other existing
356 models, it neglects the influence of network geometry on solute transport within hydrogels, instead
357 assuming a random distribution of network chains, extending from obstruction theory and the
358 Ogston model.

359 For the multi-arm PEG hydrogels, the LPEM model predictions became less accurate than the
360 SPN model for larger solutes (Fig. 6). For fluorescein, the LPEM-predicted diffusivity increased
361 with the increasing degree of polymerization between junctions like the SPN model's predictions
362 despite the measured diffusivity decreasing (Fig. 6A,D). The consistent false correlation for both
363 the LPEM model and SPN model supports our hypothesis that the measured relationship between
364 the degree of polymerization between junctions and solute diffusivity in multi-arm PEG hydrogels
365 indicates a novel mechanism of structure-property interactions in hydrogels. For 4 kDa and 20
366 kDa FITC-dextran, the LPEM model predictions deviate from measurements at low diffusion
367 coefficient values whereas the SPN model predictions maintain a positive correlation for all

368 structural parameters other than the degree of polymerization between junctions. For larger
369 solutes, the SPN model better accounts for the influences of hydrogel structure on solute transport
370 than the LPEM model does.

371 Discussion

372 Network structure affects solute diffusivity in PEG and PVA hydrogels

373 With a robust library of multi-arm PEG hydrogels, we identified how four independent structural
374 parameters of hydrogel design ($N_j, f, \varphi_0, \gamma$) affect solute self-diffusion within hydrogels and
375 partitioning into hydrogels. Notably, junction functionality, initial polymer volume fraction, and
376 frequency of chain-end defects have consistent and model-predictable effects on solute
377 diffusivities, but the degree of polymerization between junctions has an inconsistent, unpredicted
378 effect. Not only was the influence of the degree of polymerization on solute diffusivities different
379 depending on the solute (Table 1), but the measured relationships differed from predictions (Fig.
380 6A-C). This result sharply contrasts our recent study of solute transport in PVA hydrogels using
381 the same FRAP experiments and analysis method.⁴ In the PVA hydrogels, initial polymer volume
382 fraction and degree of polymerization between junctions were independently manipulated and the
383 diffusivities of fluorescein, 4kDa FITC-dextran, and 20 kDa FITC-dextran as well as other solutes
384 were measured in each hydrogel formulation. With PVA hydrogels, increasing initial polymer
385 volume fraction decreased diffusivities for all solutes as predicted and as measured here, but
386 increasing the degree of polymerization between junctions consistently increased diffusivity as
387 predicted, unlike with the multi-arm PEG hydrogels in this study. Future work should investigate
388 whether the unexpected effects of the degree of polymerization between junctions on solute
389 transport for multi-arm PEG hydrogels reproducibly apply to a broader variety of solutes. Because
390 the effect was shown here for a large, redundant library of hydrogel formulations, we hypothesize
391 that there is a substantial, unanticipated mechanism relating the degree of polymerization
392 between junctions to solute diffusivities for multi-arm PEG hydrogels.

393 Mesh radius captures junction functionality effects on solute transport

394 This study of solute transport in hydrogels definitively demonstrates that including mesh radius in
395 the modeling of solute transport in hydrogels is an improvement over mesh size-based models.
396 The conversion from mesh size to mesh radius primarily addresses how changing junction
397 functionality affects the molecular geometry of a swollen polymer network.¹¹ This work extends
398 prior work by Lutolf and Hubbell³⁶ and Lee, Tong, and Yang^{28, 29} to understand how changing
399 junction functionality affects solute transport in hydrogels. However, Lutolf and Hubbell did not
400 directly measure solute transport in hydrogels,³⁶ and Lee, Tong, and Yang interpreted changes in
401 solute diffusivity as a function of junction functionality (with equivalent mesh sizes) to be the result
402 of changing network homogeneity.^{28, 29} The introduction of mesh radius and consideration of
403 network geometry provides a predictable fundamental mechanism for their experimental results.

404 Solute transport properties in hydrogels are not universally correlated

405 Lutolf and Hubbell created multi-arm PEG hydrogels with different junction functionalities but used
406 swelling ratios as a proxy for solute transport properties.³⁶ Similarly, Cha et al. effectively varied
407 the frequency of chain-end defects in PEG diacrylate hydrogels but similarly assumed that the
408 swelling ratio summarizes solute transport properties.³⁷ Here we show in Fig. 3 that swelling is
409 not universally correlated with solute diffusivity or partitioning in hydrogels (noting that the swelling
410 ratio is the inverse of the swollen polymer volume fraction). This work therefore demonstrates that

411 assuming swelling ratios can be used as proxies for other solute transport properties is overly
412 simplistic and inappropriate. Instead, relevant solute transport properties should be measured
413 directly where possible—for example, the FRAP-based self-diffusion of solutes within hydrogels
414 measured here is not guaranteed to correspond to the diffusion coefficients of solute release from
415 hydrogels.

416 Similarly, this work disproves the assumption that mesh size or even mesh radius can be used to
417 summarize a hydrogel's solute transport properties. Neither mesh size nor mesh radius
418 completely captured the differences in solute diffusivity or partitioning between different hydrogel
419 formulations. Even once used to predict solute diffusivities with the SPN model, which also scales
420 based on the swollen polymer volume fraction, there were systematic discrepancies between the
421 prediction and the measured diffusivities. Since different solute transport properties are shown
422 here to not be correlated, it may be impossible to identify a single hydrogel formulation-specific
423 parameter that summarizes how the hydrogel influences solute transport.

424 Browning et al.³⁰ and Munoz-Pinto et al.³⁸ both summarized what they described as diffusion
425 experiments using mesh size. However, they performed partition coefficient measurements,
426 where solutes diffused into the hydrogels over 24 hours and then were released into a second
427 solution for 24 hours. They compared the concentration of solutes in the initial and final solutions,
428 effectively yielding a partition coefficient instead of a diffusion coefficient, which was unclear in
429 their figures due to their use of mesh sizes. We showed in Fig. 4 that partition coefficients and
430 diffusion coefficients are not robustly correlated within hydrogels. The absence of correlations for
431 solute transport properties in hydrogels indicate the need for more extensive experimental study
432 and modeling of solute transport properties hydrogels with a focus on matching the measured
433 property to the target application.

434 **Solute size-based models oversimplify solute-hydrogel interactions**

435 The modified multiscale diffusion model used in this study maintains the assumption that solute
436 diffusion in hydrogels scales universally with solute size. We demonstrated the limitations of this
437 assumption in our previous study of FITC-dextran and FITC-PEGs diffusing in PVA hydrogels.⁴
438 Preliminary studies with the multi-arm PEG hydrogels showed that FITC-PEGs partitioned
439 homogeneously into the PEG-based hydrogels, but their self-diffusion was extremely slow
440 compared to the diffusion of FITC-dextran in the PEG hydrogels or either solute group in PVA
441 hydrogels (data not shown), so we concluded that there is a specific PEG-PEG interaction and
442 only used FITC-dextran for the full study. Furthermore, the 70 kDa FITC-dextran used in the
443 PVA study were partitioned into the multi-arm PEG hydrogels at such low concentrations that we
444 were unable to measure their diffusion coefficients. Successfully including the 70 kDa FITC-
445 dextran would have enabled a study of size effects in chemically similar molecules without the
446 confounding chemical differences between fluorescein and FITC-dextran, potentially clarifying
447 whether the 4 kDa FITC-dextran behavior was anomalous as suggested by the fluorescein and
448 20 kDa FITC-dextran data or part of a scaling relationship specific to FITC-dextran.

449 Identifying the conditions for size-based equivalency of solute diffusion in hydrogels is critical for
450 drug and protein delivery applications. Here, as in many comparable studies,³⁹⁻⁴¹ we use FITC-
451 dextran as readily available, globular, hydrophilic solutes that cover a range of sizes relevant to
452 bioactive soluble proteins (~1-10 nm hydrodynamic radius). However, shape, charge, and solute-
453 hydrogel interaction differences may mean that these solutes are poor substitutes for the proteins
454 they aim to model. A positive proof-of-concept study by Rehmann et al. indicated that two proteins

455 of near-equivalent hydrodynamic radii (Bovine serum albumin at 7.2 nm and platelet-derived
456 growth factor-BB at 7.0 nm) have similar release profiles from the same hydrogel formulation,
457 suggesting that some extent of size-diffusivity equivalence is viable.³² The confounding effects of
458 shape, charge, and other solute-hydrogel interactions are under-investigated, and the high-
459 throughput FRAP experiments and analysis here could help to clarify their nuanced effects.

460 **Surface accumulation of solutes may affect partitioning and diffusivity**

461 This study focuses on the self-diffusion of solutes within a hydrogel as measured by FRAP, and
462 the partitioning is likewise measured based on the solute concentration within the hydrogels as
463 measured by confocal microscopy. Alternatively, it is common to characterize solute diffusion
464 from hydrogels via release studies²⁸ and measure partitioning based solely on changes in
465 supernatant concentrations.³⁰ The greatest difference between these methods is the effect of
466 solute accumulation at the surface of the hydrogel. In release studies, surface accumulation
467 contributes to burst release, and measuring partition coefficients via supernatant concentrations
468 does not distinguish between surface accumulation and partitioning into the interior of the
469 hydrogel, reducing accuracy and reproducibility. In this work, the self-diffusion of solutes is
470 measured within hydrogels via FRAP, and partition coefficients are based on the interior
471 concentration of solutes, avoiding the experimental limitations of prior diffusion and partitioning
472 methods.

473 The confocal microscopy used for FRAP experiments facilitated qualitative imaging of solute
474 surface accumulation on the edges of hydrogel samples (Supp. Fig. S1). The surface
475 accumulation may also affect FRAP experiments by screening larger solutes but allowing smaller
476 solutes into the hydrogel. Since the FITC-dextrans have a distribution of solute sizes, the
477 distribution that made it into the hydrogel may be different from the distribution in the solution,
478 effectively distorting model predictions based on the average solute size in solution. Future
479 studies should measure whether the partitioning of polydisperse solutes into hydrogels favors the
480 smaller solutes, especially where there is significant surface accumulation. Such distribution shifts
481 could explain the discrepancies observed between 4 kDa and 20 kDa FITC-dextrans.

482 **Study limitations**

483 Practical limitations of this study include the small number of solutes studied (3) compared to our
484 previous study with seven solutes,⁴ some technical limitations with the confocal microscope, and
485 the lack of a complete predictive model for solute partitioning in hydrogels. As discussed above,
486 FITC-PEG solutes diffused slowly in the multi-arm PEG hydrogels, likely due to specific PEG-
487 PEG interactions. With more time and experimental optimization, it would be informative to
488 measure the diffusion coefficients of those FITC-PEGs in the multi-arm PEG hydrogels, but the
489 slow diffusion means that those studies will take much longer than the FITC-dextran diffusion
490 studies. Additional studies with fluorescent probes other than fluorescein may reveal biases
491 associated with that probe, and protein transport in hydrogels should be studied for further
492 analysis of solute shape, chemical interactions with the network, and biological relevance.^{32, 42}
493 Also, the six degrees of polymerization between junctions studied in the PVA hydrogel study
494 generated a continuous response trend,⁴ whereas only three values for each structural parameter
495 were used in this study, meaning that little could be concluded from data that did not produce a
496 continuous trend over the three values (e.g., for the degree of polymerization between junctions).
497 Practically, the need for a higher, 20 μ M concentration of 4 kDa FITC-dextran introduced the
498 possibility of concentration-dependent behavior, which was not thoroughly studied here.

499 Additionally, midway through the FRAP experiments for this study, maintenance was performed
500 on the confocal microscope that greatly increased the laser power, possibly creating a
501 measurement artifact dividing data before and after the increase. To help mitigate this distortion,
502 laser powers and gains were selected that kept scans within the linear intensity-concentration
503 ranges, and standard curves were taken at each laser power and gain used.

504 A robust predictive model for solute partitioning in hydrogels would allow more hypothesis-driven
505 experimentation on solute partitioning in hydrogels and facilitate the sort of iterative model
506 refinement we demonstrated with solute diffusion modeling in Fig. 5 and Fig. 6. Kotsmar et al.
507 predicted partitioning of solutes into hydrogels based on the integration of the Ogston model,³⁹
508 but it is unclear if a similar model could be developed that is consistent with the current iteration
509 of the SPN model, which incorporates features of free volume theory as well as the Ogston-based
510 obstruction theory.⁷ It would also be worthwhile to investigate a greater variety of models for solute
511 transport in hydrogels, as was demonstrated here with the LPEM model.⁵ Ultimately,
512 fundamentally derived, experimentally validated models of solute transport in hydrogels should
513 be able to account for the nuances of solute release, partitioning, and self-diffusion within
514 hydrogels. Comprehensive models of solute transport in hydrogels will only be possible with
515 continuous, iterative modeling and experimentation using a broad variety of solutes and hydrogel
516 formulations.

517 **Conclusions**

518 In this contribution, we demonstrate that solute diffusion and partitioning in hydrogels are both
519 linked to the hydrogel's network structure, but they are not always correlated. Notably, the
520 frequency of chain-end defects has a discerning effect on diffusivity and solute partitioning. A
521 higher frequency of chain-end defects consistently increased diffusivity but shifted from
522 decreasing to increasing partitioning with increasing solute size.

523 Multi-arm PEG hydrogels have exceptional control of junction functionalities based on the number
524 of arms per precursor molecule, allowing precise investigation of how junction functionality affects
525 solute transport. The experimental results confirmed our theory that more geometrically restrictive
526 networks reduce solute diffusivity even with equivalent mesh sizes. We therefore recommend the
527 use of mesh radius over mesh size in models relating hydrogel structure to solute diffusivity.

528 FRAP and confocal-based partitioning methods overcome some of the problems associated with
529 surface accumulation during solute transport in hydrogel studies. However, large polydisperse
530 solutes may still create a screening effect in these studies where only the smaller solutes make it
531 into the hydrogels. This effect should be investigated in future studies.

532 Overall, complementary FRAP and partitioning experiments enable robust, high-throughput
533 studies of solute transport in hydrogels that can provide overwhelming evidence for questions
534 unanswered by smaller-scale or unidimensional studies (e.g., only varying solute size). Further
535 use of these methods, especially when used to test assumptions in fundamental hydrogel models,
536 will accelerate predictive hydrogel design for diverse biomedical applications. As shown by the
537 differences between predicted and measured diffusivities in this work, there is still much room for
538 improving hydrogel design models, even with the relatively simple multi-arm PEG hydrogels and
539 solute transport properties. Thoroughly validated, accurate models are required for the clinically
540 relevant scale-up of precise and highly tunable hydrogel scaffolds and drug delivery devices.

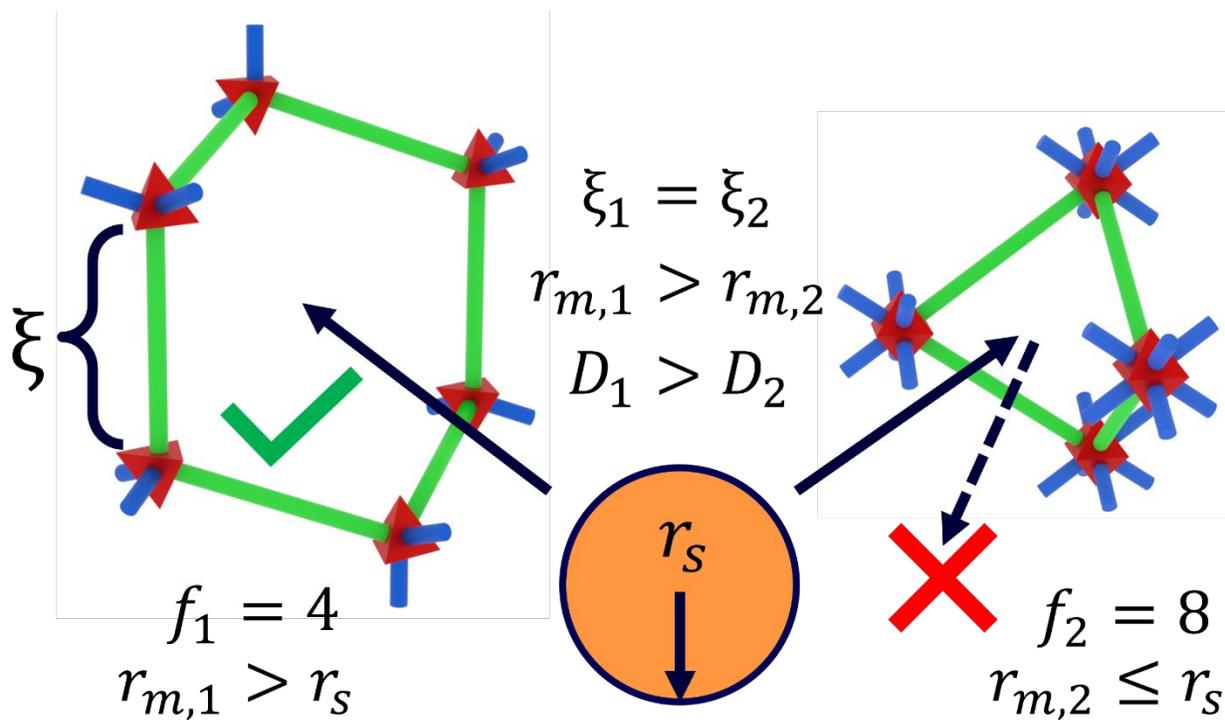
541 **Conflicts of Interest**

542 There are no conflicts of interest to declare.

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552 Figures



553

554 **Figure 1. Model predictions of how network geometry affects solute transport in hydrogels.**

555 For two network portals with equivalent mesh sizes (ξ) but different junction functionalities ($f = 4, 8$)

556) and therefore different mesh radii (r_m), a large solute (with radius r_s) may be able to pass more

557 easily through the portal with the lower junction functionality (higher mesh radius) than the portal

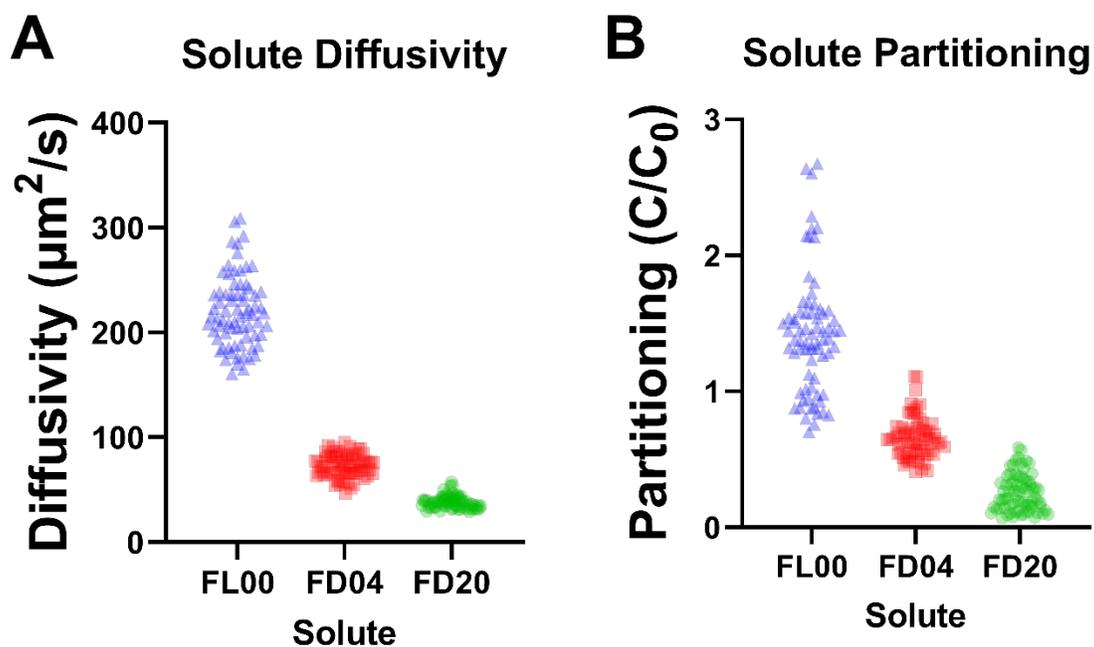
558 with the higher junction functionality (and lower mesh radius). Resultingly, diffusion coefficients (D)

559) are higher in the network with a higher mesh radius. Network chains are represented as straight

560 rods for clarity, and the smallest network portal for each junction functionality is highlighted in

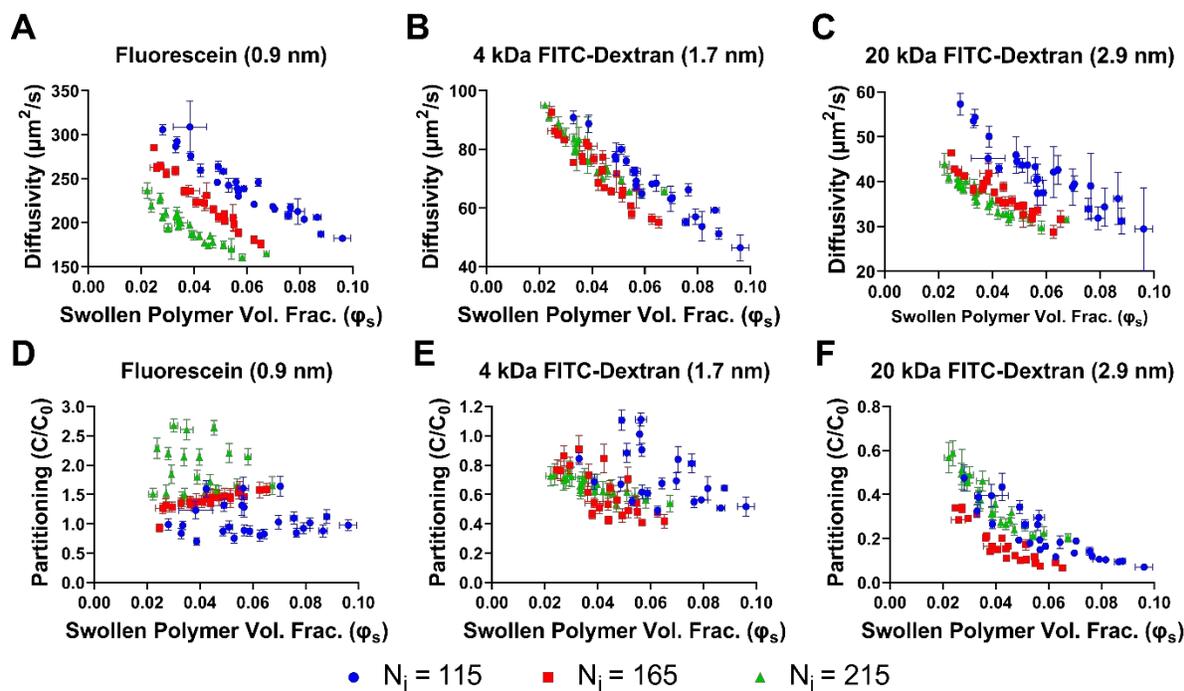
561 green.

562



563

564 **Figure 2. Solute diffusivity (A) and partitioning (B) in multi-arm PEG hydrogels.** FL00 is
565 fluorescein (0.9 nm hydrodynamic radius), FD04 is 4 kDa FITC-dextran (1.7 nm), and FD20 is
566 20 kDa FITC-dextran (2.9 nm). Each point represents a unique solute-hydrogel formulation
567 pairing. Error bars are not shown for visual clarity.



569

570 **Figure 3. The influence of the degree of polymerization between junctions (N_j) on (A-C)**
 571 **the relationship between swelling and diffusivity and (D-F) between swelling and**
 572 **partitioning in multi-arm PEG hydrogels.** Whereas the other three structural parameters
 573 studied have an overlapping effect on the relationship between swelling and diffusivity, N_j has
 574 the distinctive effect of higher values decreasing both swollen polymer volume fraction and
 575 diffusivity, at least for fluorescein (A) and 20 kDa FITC-dextran (C). However, swelling-
 576 partitioning trends are inconsistent across formulation and solute. Error bars represent standard
 577 deviations (for swelling, $n = 3$, for diffusivity and partitioning, $n = 9$).

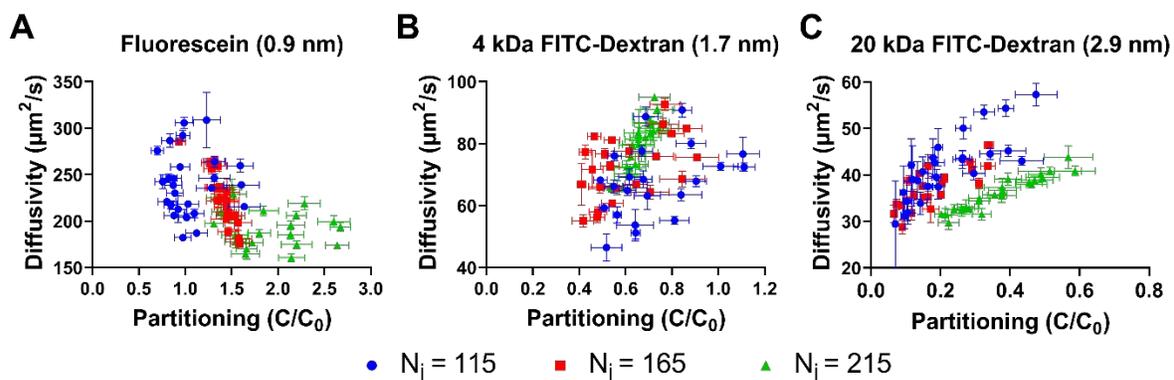
578

579 **Table 1. Hydrogel Structural Parameters Main Effects on Diffusivity and Partitioning**

Structural Parameters	Fluorescein (0.9 nm)	4 kDa FITC-Dextran (1.7 nm)	20 kDa FITC-Dextran (2.9 nm)
Initial Polymer Volume Fraction (ϕ_0)	D↓, P~	D↓, P↓	D↓, P↓
Degree of Polymerization Between Junctions (N_j)	D↓, P↑	D↑, P↓*	D↓, P↑*
Junction Functionality (f)	D↓, P↓*	D↓, P↓	D↓, P↓
Frequency of Chain-End Defects (γ)	D↑, P↓	D↑, P~	D↑, P↑

580 D for diffusivity, P for partitioning, ↑ indicates a property increase when the parameter increases,
 581 ↓ indicates the property decreases when the parameter increases. * indicates that the trend is
 582 not consistent across formulations, and ~ indicates that the parameter appears to not affect the
 583 property. An example of the figures used to evaluate these relationships is provided in Supp.
 584 Fig. S3.

585

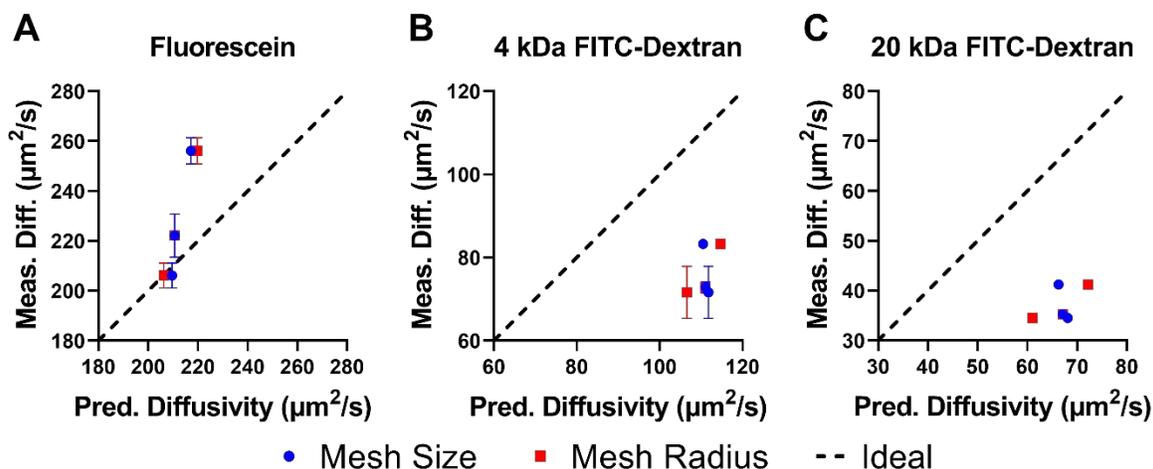


586

587 **Figure 4. Relationship between diffusivity and partitioning in multi-arm PEG hydrogels.**588 Trends were ambiguous across solutes and hydrogel structural parameters. Overall, there is not
589 a strong or structurally consistent correlation between solute diffusivity and partitioning. Error
590 bars represent standard deviations ($n = 9$).

591

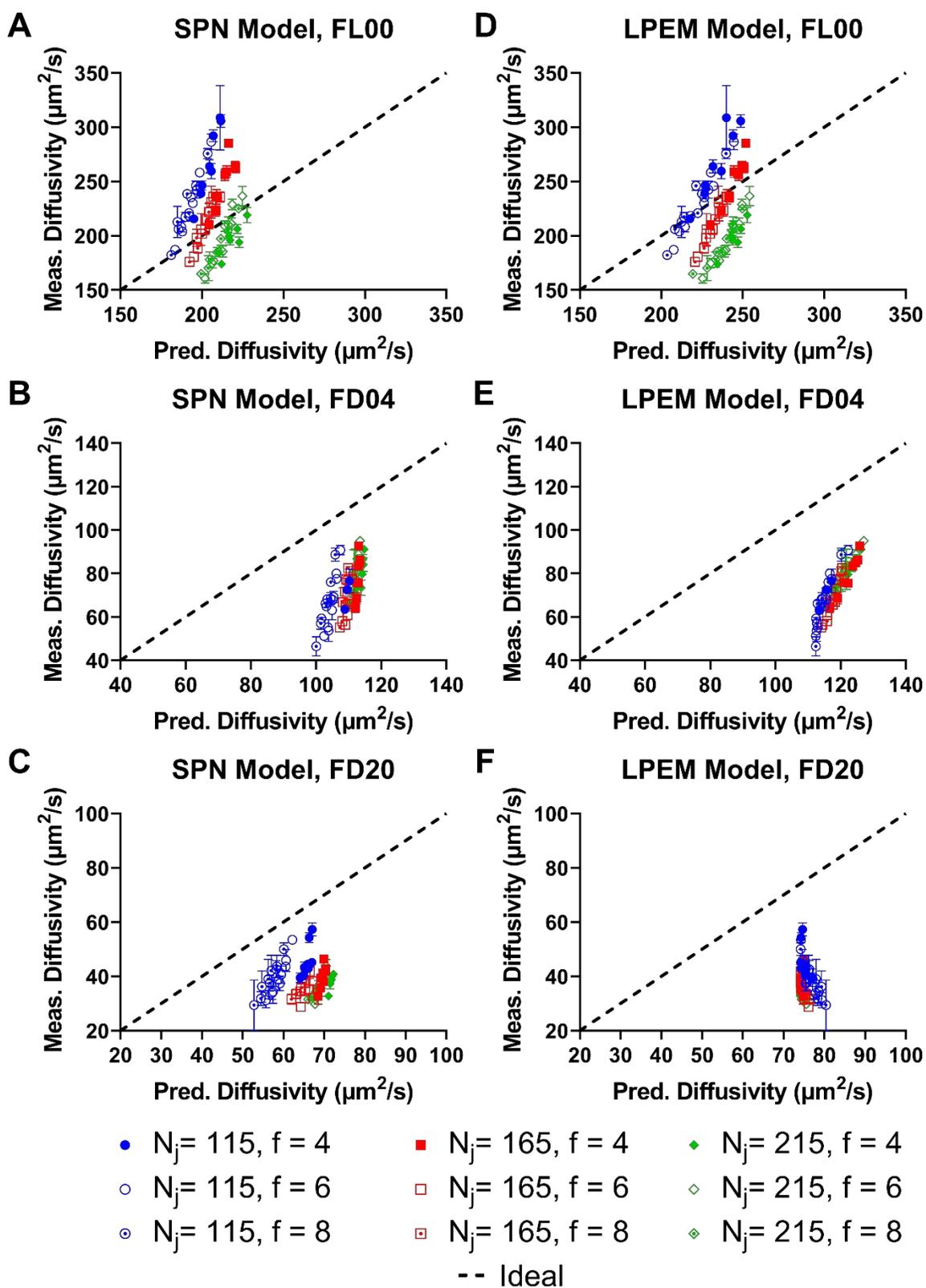
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593

594 **Figure 5. Comparing mesh size-based predictions and mesh radius-based predictions to**
 595 **measured diffusivities for a subset of hydrogel formulations with changing junction**
 596 **functionality.** Three hydrogel formulations with changing junction functionality ($f = 4,6,8$) and
 597 other structural parameters held constant ($\varphi_0 = 0.075$, $N_j = 165$, $\gamma = 0.2$) were used to summarize
 598 how junction functionality affects predictions of solute diffusivity in hydrogels. Mesh radius
 599 predictions positively correlate with measurements, whereas mesh size-based predictions
 600 negatively correlate with measurements for larger solutes (B,C). A comparison for all hydrogel
 601 formulations is provided in Supplementary Figure S3. Error bars represent standard deviations ($n = 9$).
 602 Ideal: 1:1 correlation between prediction and measurement.

603



605 **Figure 6. The swollen polymer network (SPN) model predictions vs. the large pore effective**
606 **medium (LPEM) model predictions compared to measured values.** (A-C) the swollen polymer
607 network model explicitly addresses the influence of hydrogel structural parameters and uses free
608 volume theory to account for large solutes, whereas (D-F) the large pore effective medium model
609 is based on obstruction and hydrodynamic theories and inaccurately predicts how hydrogel
610 structure affects solute diffusivity at high solute sizes. (A,D) Both models inaccurately predict the
611 influence of the degree of polymerization between junctions (N_j) on fluorescein diffusivity. Error
612 bars represent standard deviations ($n = 9$). FL00: fluorescein, 0.9 nm hydrodynamic radius. FD04:
613 4 kDa FITC-dextran, 1.7 nm. FD20: 20 kDa FITC-dextran, 2.9 nm. Ideal: 1:1 correlation between
614 prediction and measurement.

615

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