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$$\delta_1$$
$$\delta_2$$

Measured deformation

$$\delta_m = \delta_1 + \delta_2$$

$$\delta_1 = \delta \text{ elastic membrane}$$

$$\delta_2 = \delta \text{ cell wall compression}$$

$$\delta_m = \sum_{i=1}^{N} \Theta(F_m - F_0 - F_{lc,i})\Theta(F_{uc,i} - F_m + F_0)\left(\frac{F_m - F_0}{k_i}\right)^{\frac{1}{n_i}}$$

$$+ \sum_{i=1}^{N} \Theta(F_m - F_0 - F_{uc,i})\left(\frac{F_{uc,i}}{k_i}\right)^{\frac{1}{n_i}} + \delta_0$$

The graphic illustrates different types of deformation that occurring during indentation of a plant cell, including cell wall compression and membrane deflection. It also shows that the total measured deformation is a convoluted quantity, that we are seeking to find through the use of our new Multi-Regime Analysis method, the mathematical gist of which is illustrated by the formula at the bottom of the figure.
192x190mm (96 x 96 DPI)

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ARTICLE

Interpreting Atomic Force Microscopy Nanoindentation of Hierarchical Biological Materials using Multi-Regime Analysis

M.R. Bonilla,[a] J. R. Stokes,[ab] M.J. Gidley[c] and G. Y. Yakubov*[a]

We present a novel Multi-Regime Analysis (MRA) routine for interpreting force indentation measurements of soft materials using atomic force microscopy. The MRA approach combines both well established and semi-empirical theories of contact mechanics within a single framework to deconvolute highly complex and non-linear force-indentation curves. The fundamental assumption in the present form of the model is that each structural contribution to the mechanical response acts in series with other 'mechanical resistors'. This simplification enables interpretation of the micromechanical properties of materials with hierarchical structures and it allows automated processing of large data sets, which is particularly indispensable for biological systems. We validate the algorithm by demonstrating for the first time that the elastic modulus of polydimethylsiloxane (PDMS) films is accurately predicted from both approach and retraction branches of force-indentation curves. For biological systems with complex hierarchical structures, we show the unique capability of MRA to map the micromechanics of live plant cells, revealing an intricate sequence of mechanical deformations resolved with precision that is unattainable using conventional methods of analysis. We recommend the routine use of MRA to interpret AFM force-indentation measurements for other complex soft materials including mammalian cells, bacteria and nanomaterials.

1 Introduction

Atomic force microscopy (AFM) is widely used for nanoindentation to characterise the micromechanics of complex biological systems including cells.[1] The attraction of using AFM for nanoindentation is its ability to measure very low forces and its operational versatility, as well as the potential to include in-situ imaging. An appropriate contact mechanical model is needed to interpret force-indentation curves (FIC), the particular choice of which requires an expert knowledge of the system under scrutiny and awareness of the chosen model's limitations. This is challenging for systems that exhibit highly non-linear mechanical responses and for biological materials that are heterogeneous and comprise a number of morphological features, each having unique micro-mechanical properties. A further challenge in regards to using AFM for nano-indentation is the uncertainty of the true contact area and the absolute surface separation between probe and sample. Thus, the central displacement values during the

1 indentation are also uncertain, which inhibits quantitative
2 interpretation of experimental data. Here, we present a
3 simple algorithm that tackles these challenges and allows
4 analysis and interpretation of complex force-indentation
5 curves such as those collected on plant cells. [2, 3] The
6 algorithm is implemented into an automated routine, which
7 is essential for heterogeneous biological materials that
8 require an extensive number of measurements for
9 establishing statistical significance. The approach can be
10 equally applied to characterising the micromechanics of a
11 broad range of soft materials using the AFM, including
12 mammalian cells, bacteria and nanomaterials such as
13 polyelectrolyte multilayer capsules. [4]

14   In practice, the commonly used approaches for
15 analysing AFM nanoindentation data rely on choosing a
16 segment of the force-distance curve, in which reasonable
17 assumptions can be made with regards to compatibility with
18 a chosen mechanical model.[5] For example, it is typical to
19 analyse only those segments of a FIC where the force (F) is
20 a power law function of the indentation (δ), which is
21 consistent with the Hertzian small deformation
22 approximation: $F \propto \delta^{3/2}$ for a spherical probe or $F \propto \delta^2$
23 for a conical indenter such as an AFM tip. Variations from
24 a power-law response are usually accommodated by
25 refining the model to account for specific system properties
26 and measurement conditions. The Hertzian theory of
27 contact deformation is among the most widely used and has
28 received numerous modifications to account for:
29 anisotropic material properties [6] and multi-layered
30 structures; [7] finite thickness of tested films and the presence
31 of supporting substrate; [8, 9] large deformations; [10] adhesive
32 interactions; [11-15] and viscoelastic behaviour. [12, 16-18]

33   Despite the variety of contact mechanics models
34 available, a complication with interpreting AFM data stems
35 from the fact that indentation is convoluted with surface
36 forces, which renders determination of the position of zero-
37 indentation difficult unless surface forces are explicitly
38 included into the model. [19, 20] In biological systems, due to
39 the weakness of DLVO forces, the surface interactions are
40 typically dominated by steric forces associated with surface
41 bound polymers. In mammalian cells, these can be
42 glycocalyx mucins or polymeric species adsorbed from the
43 media, while for plant and bacterial cells, these are cell wall

44 polysaccharides and proteoglycans. Usually little is known
45 about the exact nature of such polymeric layers in
46 biological systems as their composition typically exhibits
47 microheterogeneity, [21] and hence it cannot be easily
48 accounted for using established theories like those used to
49 describe the micromechanical properties and surface forces
50 associated with well-defined polymer brushes. [22]
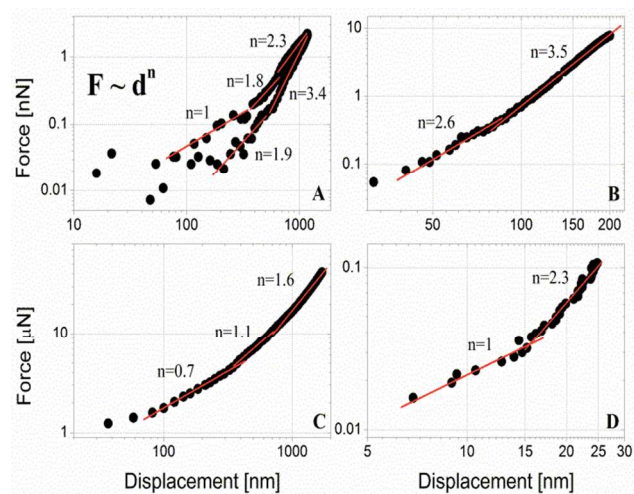
51

52 **Figure 1.** Characteristic indentation curves of (A) bovine
53 cartilage, [23] (B) bovine ovary, [24] (C) yeast, [25] and (D) cactus
54 spine [26] cells. FICs (A), (B) and (D) were obtained through
55 a conical AFM tip, while FIC (C) was obtained through a
56 50 µm diameter flat indenter. Despite the differences in the
57 magnitude of the forces and indenter geometry, all FICs
58 display a characteristic multi-linear shape in logarithmic
59 scale, suggesting that in different sections of the curve a
60 dominant power-law regime dictates the force (F) –
61 displacement (d) relationship. The value of the slope n
62 provides valuable information on the physical mechanisms
63 in action. Reproduced with permission.
64

65   The Oliver-Pharr (OP) model is used to avoid the
66 influence of the surface forces and to mitigate the
67 uncertainty of the true contact area when interpreting FICs.
68 [27] This model established an analytical relationship between
69 the Hertzian elastic modulus and the slope of the initial part
70 of the unloading curve, where it is assumed that the contact
71 area stays constant. The OP model gained significant
72 popularity due to its simplicity, analytical form, and ease of
73 implementation in the form of an automated routine for
74 processing large arrays of FICs. It has also been
75 implemented in the majority of commercial AFM software
76 packages. However, applicability of the OP model is
77 confined to contacts that behave within the Hertzian
78 approximation, and it cannot be used for any arbitrary curve
79 without adequate controls. There is thus a strong impetus to

1 develop a simple algorithm (as an opposite to a full
2 numerical simulation) that can be used to interpret FICs
3 where the choice of appropriate micromechanical model is
4 ambiguous.

5 The new Multi-Regime Analysis (MRA) developed
6 here is based on the fact that the FICs of many soft
7 materials display a characteristic multi-linear shape when
8 graphed in logarithmic scale, as depicted in Figure 1 for
9 bacterial, mammalian and plant cells. Every linear section
10 of the curve is associated with a dominant power-law
11 relationship between force F and indentation depth d, the
12 exponent of which can be identified with a particular
13 regime through a preliminary histogram analysis followed
14 by an optimization procedure. The new algorithm
15 maximizes the extraction of quantifiable information
16 convoluted within force indentation measurements, whilst
17 ensuring that force analysis complies with assumptions and
18 applicability limits of mechanical models. The adequacy of
19 the automated routine is demonstrated by characterizing the
20 complex micromechanical properties of heterogeneous
21 plant cells from *Lolium multiflorum* cell culture. We show
22 also that this new approach enhances the accuracy of
23 nanoindentation measurements on model elastomer
24 surfaces. Moreover, the qualitative similarity between the
25 FICs in Figure 1 arising from their multi-regime nature
26 allows us to suggest that MRA can be employed to interpret
27 indentation data on other complex systems.

28

29 **2 Materials and methods**

30 **2.1 Colloidal probe preparation**
31 Colloidal probes were fabricated in house using glass beads
32 (30-50 μm diameter) and Polybead™ polystyrene
33 microspheres (diameter 10.52 μm) both from Polysciences
34 (Polysciences Inc., PA). Spheres were attached on the top
35 of the AFM cantilever using epoxy glue (UHU GmbH &
36 Co. KG, Germany) and cured at room temperature (24°C)
37 for at least 72 hours. Before use, probes were cleaned in
38 oxygen plasma for 5 min, and immediately after cleaning
39 they were mounted in the holder and immersed in the
40 experimental cuvette with buffer. In addition to colloidal
41 probes, the following pre-manufactured AFM tips were
42 used; PNP-TR Si_3N_4 (R<10 nm) from NanoWorld

43 (NanoWorld AG, Germany), DNP Si_3N_4 (R~20 nm) from
44 Bruker (Bruker AFM Probes, CA), and NSC/CSC Si tips
45 (R<10 nm) from Mikromasch (NanoWorld AG, Germany).
46 For colloidal probes, several tipless cantilevers were used
47 including: CSG 11 (gold coated) from NT-MDT (NT-
48 MDT, Russia), and CSC 37/NSC 36 (Al coated) from
49 MikroMasch (NanoWorld AG, Germany). The spring
50 constant (k) of the sensors ranged from 0.05 up to 1 N/m,
51 and was determined using the Asylum Research GetReal™
52 routine that utilises a combination of the thermal noise and
53 the Sader methods [28, 29]. The geometric parameters of the
54 probes were obtained from analysis of scanning electron
55 microscope (SEM) microphotographs.
56

57 **2.2 *Lolium multiflorum* Suspension Culture Cells**
58 *L.multiflorum* suspended culture cells were used as a
59 model biological system with complex mechanical
60 properties. The culture was derived from the endosperm of
61 *Lolium multiflorum* grown in 250 ml Erlenmeyer flasks
62 containing 150 ml of modified White's medium [30] (ionic
63 strength 0.435 mol/l, osmotic pressure 1.17 MPa). The
64 cultures were maintained in the dark at 27°C with constant
65 shaking at 130 rpm. Sub-cultures were conducted every 10
66 days by weighing 30 g (fresh weight) of cells and
67 transferring the cells to 150 ml of fresh medium.

68 Prior to conducting AFM measurements, the
69 suspensions were sieved to isolate small cell clusters and
70 individuals cells. Sieving was performed using steel mesh
71 sieves (ISO 3310 Test Sieves, Essa, Australia). Firstly, a
72 sieve with 300 μm mesh was used; the filtrate was then
73 passed through the sieve with 90 μm mesh. An additional
74 volume of media was used to facilitate the penetration of
75 the cell slurry through the mesh. Two volumes of media
76 was used for sieving cell suspensions. After sieving, the
77 suspensions were transferred to the measuring apparatus
78 within 2 hours.
79

80 **2.3 PDMS preparation and bulk mechanical tests**
81 Two component polydymethilsiloxane (PDMS)
82 (SYLGARD® 184 Silicon Elastomer Kit, Dow Corning,
83 MI) substrates were prepared by casting. The Young's
84 modulus of the PDMS was measured through uniaxial
85 extension using the Instron MicroTester (MicroTester

1 model 5848, Instron, MA) as well as using a Texture
2 analyser (TA.XTplus, Stable Micro Systems, United
3 Kingdom) and was found to be 1.45±0.5MPa [31]. To
4 minimise adhesion, PDMS sheets were treated using
5 oxygen plasma (Expanded Plasma Cleaner PDC 001/002,
6 Harrick Plasma, NY) to render them hydrophilic. The
7 samples were held in a vacuum at a vapour pressure of
8 0.2mbar, and a current of 15mA was applied for 30
9 seconds; after treatment the samples were immediately
10 immersed in water and used at once.
11
12 **2.4 AFM measurements**
13 AFM measurements were conducted using a JPK
14 Nanowizard II AFM mounted on an inverted optical
15 microscope (JPK Instruments, Germany) for measurements
16 of cells using a CellHesion controller with a Z-piezoelectric
17 translator range of 100 μm. A MFP-3D-BIO AFM mounted
18 on an inverted optical microscope (Asylum Research, CA)
19 was used to conduct measurements on PDMS substrates.
20 All measurements were performed in the closed loop mode.
21 Indentation curves were recorded using driving speeds
22 ranging from 200 nm/s up to 1 μm/s; the value depended on
23 the radius of the probe so as to minimise the impact of
24 hydrodynamic drag that at all times was less than 5Å in the
25 deflection equivalent[32, 33]. The total Z-piezo travel distance
26 was typically from 1.5 to 3 μm, and zero dwell time was
27 selected between approach and retraction branches. This
28 allowed the contact time between tip and substrate to be
29 less than 2 seconds. To convert the output voltage of the
30 position sensitive device to a deflection in nanometers, we
31 calculated the slope of the constant compliance line
32 measured prior to and after the measurements in the same
33 buffer/solvent by recording the force curves against a
34 glass/Si wafer substrate. The force was calculated by
35 multiplying deflection by the cantilever spring constant.
36 The zero position was determined as the cross-section point
37 of the baseline and the tangent line corresponding to the
38 onset of the indentation curve, where cantilever deflection
39 started to deviate from the baseline. Positive values were
40 attributed to the indentation section of the curve. The
41 apparent separation was calculated by subtracting cantilever
42 deflection from the *z*-position of the piezotranslator. Such
43 processed indentation/surface force curves were used for

44 further analysis. No further assumption has been made with
45 regards to whether the low deflection sections of the FIC
46 correspond to surface forces or actual indentation.
47 Measurements on cells were carried out in the same
48 buffer used for cell culture after filtering it twice through a
49 0.2 μm pore size membrane filter (MillexGS MCE,
50 Millipore, Ireland). Upon immersion into buffer solution
51 the system was thermostated for typically 20-40 minutes to
52 ensure minimal cantilever drift. All probe surfaces were
53 considered to be hydrophilic (after plasma treatment) and
54 microparticles were found to have a RMS surface
55 roughness below 0.3nm over an area of 1 μm^2.
56 Figure 2 shows a *L. multiflorum* cell confined within a
57 PDMS microwell [34] that is indented using an AFM tip. To
58 avoid cell damage and minimize plastic deformation due to
59 prolonged contact, the maximum indentations were limited
60 to 500 nm, and maximal forces to 150 -200 nN, which is
61 adequate for plant cells which are much stiffer and larger
62 than mammalian cells. [35]
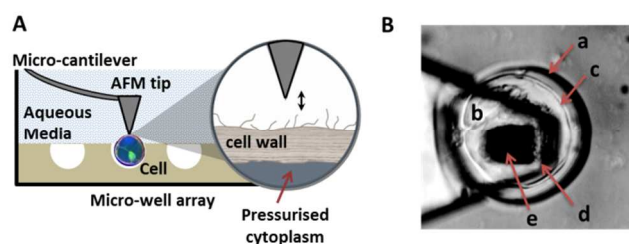
Figure 2. (**A**) Schematic diagram of indentation experiments using *Lolium multiflorum* cells confined within PDMS microwells. The zoomed-in sketch represents the complex layered structure of the cell surface, where the multi-regime nature of the elastic response originates. (**B**) A dual illumination (Bright-Field and Reflected Light) optical micrograph of a *L. multiflorum* cell (b) confined within a PDMS micro-well (a). An AFM cantilever (d) is positioned above the cell so that the tip (e) is positioned approximately above the apex of the cell. The cell wall (c) can be clearly visualised as a shell surrounding the cell.

63

64 ## 3 Results and discussion

65 ### 3.1 Theoretical framework for a Multi-Regime
66 Analysis (MRA)

67 Figure 3 presents typical FICs for a *L.multiflorum* cell
68 (A) and PDMS elastomer (B) recorded using a conical tip
69 and a colloidal probe respectively. Most contact mechanics
70 models predict that the force is a power-law function of the
71 central displacement, i.e. $F \propto \delta^n$, therefore it is more

convenient to display data in logarithmic coordinates. On a logarithmic scale (Figure 3, bottom panels), the experimental FICs frequently show two or more distinct power law regimes, with power law exponents for these regimes deviating from the expected Hertzian values of n=3/2 for a sphere and n=2 for a cone/pyramid.
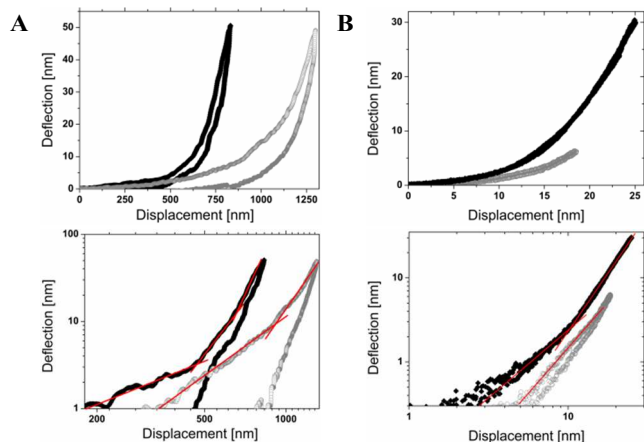


Figure 3. (A) Typical force versus indentation curves for a *L. multiflorum* suspension cell recorded using AFM tip ($R \sim$ 20 nm) and soft cantilever (~30 pN/nm). (B) Typical force versus indentation curves for PDMS elastomer recorded using a colloidal probe (R = 5.16±0.13μm) and moderately stiff cantilever (0.825±0.005 nN/nm). The logarithmic plots show empirical power law fits of different sections of the curve and illustrate the empirical basis of the Multi-Regime Analysis.

We note that each power law regime spans across a considerable range of indentation values, and therefore should be attributed to a consolidated set of deformations that dominate mechanical behaviour. To confirm this observation, i.e. that significant sections of FICs are characterized by the same slope; we have performed linear fitting (in log-log coordinates) of short segments of FICs, with gradients used to construct a frequency histogram. The individual histograms are then averaged to yield a spectrum of power law exponents.

To illustrate the method we will use results obtained for the *L.multiflorum* cells, the wall of which displays a clear hierarchical structure. In contrast to mammalian cells, the phospholipid plasma membrane in plant cells is surrounded by a stiff wall containing cellulose fibres (Figure 2A). The cell wall restricts the expansion of turgid cells, in a similar fashion to how the tough rubber of a bicycle tire provides a limit to the pumping of air into an elastic inner tube. During an indentation cycle, both the cell wall and the cell wall shell (shown as a spherical membrane in Figure 4A) deform. In Figure S3 of the Supplementary Information, a typical spectrum of power law exponents obtained for *L.multiflorum* cells is presented that suggests the presence of five dominant regimes. The position of the main maximum deviates from the value of 2 expected for a Hertzian contact exerted by an AFM tip. This deviation does not necessarily mean that the Hertzian model is not appropriate, since neither the contact area nor absolute deformation is known. [36] Deviation from the Hertzian model may also arise because deformations of different structures within the cell are convoluted within a single FIC; as illustrated in Figure 4A for plant cells. The total indentation in this example comprises two contributions; one is from the compression of the cell wall, and another from the deflection of a spherical shell. If we assume both structures deform elastically, a constitutive model can be defined by considering the system to be a set of springs connected in series (Figure 4B). [37]
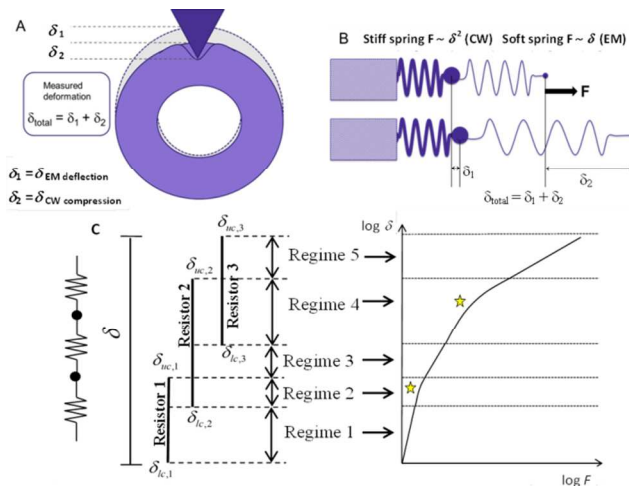
Figure 4. (**A**) The schematics of plant cell wall deformation during indentation with an AFM tip, and(**B**) the corresponding spring model, illustrating a scenario where cell wall (CW) compression and elastic membrane (EM) deflection are convoluted. (**C**) Generalization of a multi-resistors system: a sketch of three resistors in series with their ranges of action overlapping to produce five different elastic regimes. The FIC on the right has the combination of resistors shown on the left side. The regimes labelled with a star are the product of the simultaneous action of two resistors and cannot be represented by a single slope in the log-log plot. Instead, the slope evolves continuously from the characteristic power law exponent of one resistor to the

other.

1

2 To generalize this approach, the cantilever deflection is
3 assumed to be the result of N elastic resistors in a series at
4 any given point on an indentation curve, as illustrated in
5 Figure 4C. The restoring force for the i th resistor, F_i,
6 relates to its corresponding deformation, δ_i, by a law of the
7 form of equation (1). For a quasi-static system in series, the
8 restoring force is the same for all resistors, i.e. $F_i = F_j = F$
9 for all i, j; moreover, the total deformation δ is the
10 summation of the individual deformations (equation (2)),
11 which means that the FIC can be found as the solution to
12 the system of N equations with N unknowns (equation (3))

13

14 $$F_i = f_i(\delta_i^{n_i}, \delta_i^{n_i - 1}, ..., \delta_i) = f_i(\delta_i, n_i) \qquad (1)$$

15 $$\delta = \sum_{i=1}^{n} \delta_i \qquad (2)$$

16 $$f_i(\delta_i, n_i) = f_{i+1}(\delta_{i+1}, n_{i+1}); \quad i = 1, ..., N-1 \qquad (3)$$

17

18 Let us define δ_m and F_m as the experimentally measured
19 values of deformation and force, respectively, and δ_0 and F_0
20 as the corresponding measurements at zero deformation
21 (i.e. $\delta_0 = \delta_m - \delta_0$ and $F = F_m - F_0$). For a simple power law of
22 the form $f_i(\delta_i, n_i) = k_i \delta_i^{n_i}$, the above system of equations
23 can be rearranged into a linear form as a superposition of
24 individual deformations with $2N$ system parameters,

25 $\delta = \sum_{i=1}^{N} (F_i / k_i)^{1/n_i}$. Due to the intrinsic uncertainty in
26 determining the zero indentation and zero force using the
27 AFM, we – following existing approaches [38, 39] - include
28 the offsets in this expression to obtain

29

30 $$\delta_m = \sum_{i=1}^{N} \left(\frac{F_m - F_0}{k_i} \right)^{\frac{1}{n_i}} + \delta_0 \qquad (4)$$

31

32 If the force-deformation relationship for resistor i has a
33 more general power law form, say
34 $f_i(\delta_i, n_i) = \sum_{j=1}^{n_i} k_{j,i} \delta_i^{n_i - j + 1}$ (which applies to the deformation
35 of a thin film [8, 9]), it is possible to determine $\delta_i(F)$ by simple
36 interpolation (see Section S3 of Supplementary Information
37 for details).
38 In general, not all elastic resistors deform over the whole
39 range of measured deformations, but it is possible that an
40 upper critical deformation $\delta = \delta_{uc,i}$ exists for resistor i such
41 that, for $\delta > \delta_{uc,i}$ resistor i ceases to deform and does not
42 further contribute to change of the total elastic force. A
43 lower critical deformation $\delta = \delta_{lc,i}$ may also exist for
44 resistor i such that, for $\delta < \delta_{lc,i}$, resistor i displays infinite
45 stiffness and cannot be deformed. Fig. 4C depicts a
46 schematic arrangement of three resistors in series and a
47 diagram showing how overlap of their ranges of action
48 creates five different elastic regimes. The use of critical
49 deformations is an approximation that can be
50 computationally solved using a system of recurrent
51 equations. For example, if resistors 2 and 3 are acting in
52 regime 4, then for this regime $(\delta_{lc,3} \leq \delta \leq \delta_{uc,3})$ the
53 following relation is obtained for the experimentally
54 measured indentation:

55

56 $$\delta_m = \delta_{lc,3} + \Delta\delta = \delta_{lc,3} + \Delta\delta_2 + \Delta\delta_3 \qquad (5)$$

57

58 Where $\Delta\delta$ and $\Delta\delta_i$ are the total deformation and that
59 corresponding to resistor i only from the onset of regime 4.
60 Hence for this regime one can show that:

61

62 $$\begin{aligned} f_3\left(\delta_m - \left(\delta_{lc,3} + \Delta\delta_2\right)\right) \\ = F^{(3)} + f_2\left(\delta_{lc,3} + \Delta\delta_2\right) - f_2\left(\delta_{lc,3}\right) \end{aligned} \qquad (6)$$

63

64 Where $F^{(3)}$ is the maximum force experienced in the
65 preceding regime (regime 3 in this example). If resistors 2
66 and 3 can be described using a simple power law model (
67 $f_i(\delta_i, n_i) = k_i \delta_i^{n_i}$), then the system of equations (5) and (6)
68 can be solved analytically, yielding

69

1 $$\delta_m = \left(\frac{F_m}{k_3}\right)^{1/n_3} + \left(\frac{F_m - F^{(3)}}{k_2} + \delta_{lc,3}^{n_2}\right)^{\left(1/n_2\right)} \qquad (7)$$

2

3 Since all parameters in equation (7) except k_3 and n_3 are

4 already determined in the previous regime, the new regime

5 has only 2 unique fitting parameters. The algorithm

6 therefore limits the number of fitting parameters for each

7 segment of the curve. At the same time it enables modelling

8 of complex curves with multiple regimes to be described by

9 different physical models. In addition, this approach

10 enables capture of the transitional regions, and therefore

11 can simulate deformations with a wide range of power law

12 exponents.

13 Critical limits can also be defined in terms of forces ($F_{lc,i}$

14 and $F_{uc,i}$) instead of deformations as long as a one-to-one

15 relationship between $F_{lc,i}$ - $\delta_{lc,i}$ and $F_{uc,i}$ - $\delta_{uc,i}$ holds. In such

16 case, for N power law resistors the measured indentation

17 will be given by:

18

19 $$\delta_m = \sum_{i=1}^{N} \Theta(F_m - F_0 - F_{lc,i})\Theta(F_{uc,i} - F_m + F_0)\left(\frac{F_m - F_0}{k_i}\right)^{\frac{1}{n_i}}$$
$$+ \sum_{i=1}^{N} \Theta(F_m - F_0 - F_{uc,i})\left(\frac{F_{uc,i}}{k_i}\right)^{\frac{1}{n_i}} + \delta_0 \qquad (8)$$

20

21 where $\Theta(x)$ is the Heaviside function, taking the value zero

22 for $x < 0$ and unity otherwise. The last term on the right

23 hand side of equation (8) stems from the fact that resistors

24 above their critical limit at the given force contribute to the

25 total deformation with their maximum deformation.

26 Interpolation extracts $\delta_i(F)$ for resistors following more

27 complex functional forms, switching the regimes on or off

28 appropriately through the use of Heaviside functions (See

29 section S3 of Supplementary information).

30

31 **3.2 Implementation of automated routine**

32 The modelling procedure was implemented in MATLAB.

33 In order to enable the fitting of experimental data with

34 deformations spanning over several decades, an appropriate

35 re-scaling was introduced. Since our analysis is based on

36 observation of the multi-regime nature of the log-log

37 curves, it is more appropriate in this case to re-state the

38 objective function J for the fitting procedure in terms of the

39 logarithm of the displacements, as:

40

41 $$J = \sum_j \left(\log \delta_{m,j}^{\text{pred}} - \log \delta_{m,j}^{\text{exp}}\right)^2 + \alpha N_r + \beta N_p \qquad (9)$$

42

43 The superscripts "*pred*" and "*exp*" stand for predicted and

44 experimental values, respectively. Large deformations will

45 have a higher weight during the fitting process than small

46 ones, which is desirable as large deformation are associated

47 with smaller relative measurement errors; however, the

48 difference in the weight between large and small

49 deformations is considerably smaller than it would be if the

50 sum was taken over $\left(\delta_{m,j}^{\text{pred}} - \delta_{m,j}^{\text{exp}}\right)^2$. Penalties for

51 combinations of resistors generating a large number of

52 regimes or large sets of fitting parameters are added

53 through the last two terms on the right hand side, where N_r

54 and N_p are number of regimes and fitting parameters,

55 respectively, and α and β appropriate weights.

56 Nevertheless, performing curve fitting in linear scale is a

57 convenient cross-validation method that adequate regimes

58 and parameters are being produced, as discussed in Section

59 S4 of the Supplementary Information.

60 Given the large number of parameters resulting from fitting

61 of a single curve, the likelihood that a non-unique set of

62 parameters locally minimizes the objective function J is

63 high. In order to reduce the computational burden and

64 improve consistency, the pre-selection of at least one

65 resistor for which $\delta_{lc,i} = 0$ (or $F_{lc,i} = 0$) and one resistor for

66 which $\delta_{uc,i} = \delta_{max}$ (or $F_{uc,i} = F_{max}$) is convenient. For most

67 biological and soft materials, the regime with $\delta_{lc,i} = 0$

68 corresponds to surface roughness (partial contact) and/or

69 the presence of a loose layer of polymer chains protruding

70 from the core material. High values of the power law

71 exponent, n, are usually associated with large deformation

72 behavior (i.e. when approaching the linear limit of the AFM

73 cantilever spring) and, as a consequence, it is likely that the

74 elastic resistor with highest n has δ_{max} as its upper critical

75 limit. Again, this does not mean that another resistor cannot

76 have δ_{max} as its upper critical limit. Setting these two

77 "boundary" resistors in advance avoids fitting with an

78 otherwise difficult restriction.

3.3 Complete FI curve modelling of a model elastomer

In order to validate the methodology, we studied micromechanical properties of PDMS elastomer. PDMS has complex micromechanical properties due to partial penetration of water into the material[40], viscoelastic properties associated with uncrosslinked silicone polymer still present in the material,[18] as well as possible changes within the surface layer associated with plasma treatment. Nevertheless, in the applied load and speed range the response was essentially elastic, producing negligible hysteresis. We chose PDMS because it has been extensively studied before using nanoindentation[41, 42] and its bulk mechanical modulus is measurable using alternative methods. In addition, the expected values for the elastic modulus of PDMS elastomer are of the order of a few MPa, which matches juvenile plant cells that are of interest here. Thus Milani et al. [43] measured a modulus of ~5 MPa and ~1.5 MPa for respectively the tip and flank cells of the shoot apical meristems of *Arabidopsis thaliana*. The modulus may be higher (10-100 MPa)[44, 45] for other types of plant cells, while for mammalian cells it can be as low as a few kPa[46]. This, however, does not change the principle of the applied analysis, although the exact choice of deformation regimes should be tailored for each individual system.

In order to illustrate the use of MRA for the extraction of mechanical parameters the procedure described in the previous section is followed in detail for the analysis of indentation of PDMS with a 10 µm radius spherical probe. Figure 5 combines the approach histograms of 5 different indentations. Here, along with major peaks between the slopes 2 and 3 (indicative of an elastic thin film), minor peaks are noted between slopes 0-1 and 1-2, corresponding to surface interactions (including possible uncertainties in δ_0 and F_0) and Hertzian elastic response. The lack of major peaks above a slope of 4.5 makes it reasonable to discard contributions from non-linearity of cantilever deflection (i.e. hyperelastic regime).
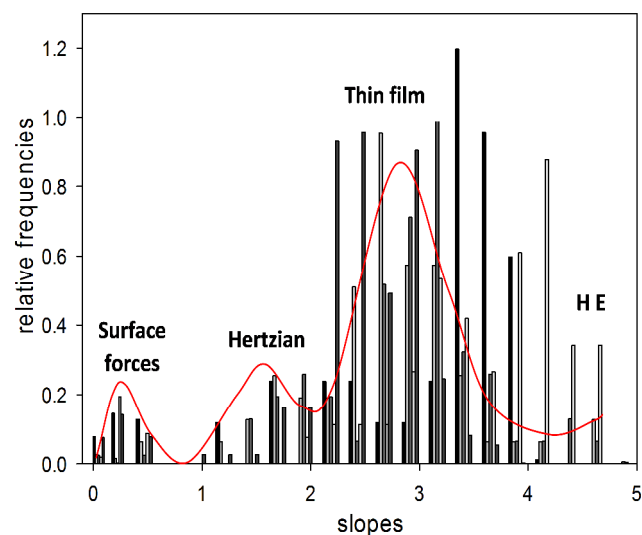
Figure 5. Selected histograms of the approach branch for five FICs (bars) of PDMS using a 10.5 µm diameter spherical indenter and the best fit using a combination of Gaussians (red line). The individual histograms display the concurrent contribution of several regimes. Hyperelasticity (HE) effects are relatively minor and will not be considered in the fitting process.

From the information provided by the histograms, three different resistors are considered:

1) Polymer steric repulsion model (equation (S.1)), $n < 1$;

2) Hertzian-Sneddon model (HS), (equations (S.3)-(S.4)), $n = 3/2$ for a sphere;

3) Thin film elastic model developed by Chadwick and co-workers (HC) as a series expansion with power law terms with exponents $n = [3/2, 2, 5/2, 3, 7/2]$ for a sphere (equation (S.5))

The lower critical limit for resistor 1 is $\delta_{lc,1} = 0$, while the upper critical limit for resistor 3 is set to $\delta_{uc,3} = \delta_{max}$. The fitting parameters arising from the resistor models are k_p, n_p, h, E_{eff}^{HS} and E_{eff}^{HC}, where superscripts HS and HC indicate Hertzian-Sneddon or Hertzian-Chadwick, respectively. One scenario in which resistors 2 and 3 coexist within the same regime is that in which thin film and substrate deform concomitantly to a sufficient degree that the substrate contribution is significant. Additional fitting parameters are the critical limits $\delta_{lc,2}$, $\delta_{lc,3}$, $\delta_{uc,1}$, $\delta_{uc,2}$ and the offsets in force and indenter displacement, δ_0 and F_0. It is entirely possible that regime i is not present, i.e. $\delta_{lc,i} = \delta_{uc,i}$. Given the structure of the objective function this scenario will be slightly favored, as it leads to a reduction in the number of regimes, N_r and parameters, N_p.

**Table 1.** Model parameters obtained through MRA for the fitting of the FIC in Figure 6.

Parameter	value
δ_0	2.07 nm
F_0	0.53 nN
k_1	0.57 nN/nm$^{0.53}$
n	0.97
E_{eff}^{HS}	10^2 MPa
E_{eff}^{HC}	1.46 MPa
h	529 nm
$\delta_{lc,2}$	14.01 nm
$\delta_{lc,3}$	0 nm
$\delta_{uc,1}$	14.01 nm
$\delta_{uc,2}$	$\delta_{max} = 34.03$ nm

Figure 6 depicts an example FIC for PDMS. The MRA provides adequate fitting throughout the entire range of indenter displacement. From the location of the critical limits, two regimes are obtained; the first one consists of a serial arrangement of resistors 1 and 3 (surface forces and elastic thin film) and the second of a serial arrangement of resistors 2 and 3 (elastic solid and elastic thin film). The presence of two regimes in the FIC is in fact evident from direct inspection of the log-log curve, as illustrated by the piece-wise linear fit (blue line) although the MRA determines that these arise from 3 different resistors. From visual analysis, the line spanning from $\delta_m = 2$ nm to $\delta_m = 14$ nm has a slope of 1.61. The slight departure from 1.5 can be accounted for in the MRA by a *realistic* non-zero displacement offset, δ_0. If $F \propto (\delta_m + \delta_0)^{3/2}$, it is only for $\delta_m \gg \delta_0$ that the log-log curve asymptotically approaches a slope of 1.5. The appropriate combination of resistors using MRA predicts the measured slope. The full set of fitting parameters for this particular curve is summarized in Table 1. Notice that $E_{eff}^{HS} = 10^2$ MPa $\gg E_{eff}^{HC} = 1.46$ MPa, which means the Hertzian resistor essentially does not deform. This does not mean the substrate supporting the film is rigid; it simply means that a maximum indentation of 36.1 nm does not produce a significant deformation of the substrate, given a film thickness of 529 nm. On the other hand, while the maximum indentation is small compared to the thickness of the film, it is considerable enough to have the FIC modelled as a thin film rather than an elastic solid because of the large radius of the indenter ($\chi > 1$ at maximum depth).
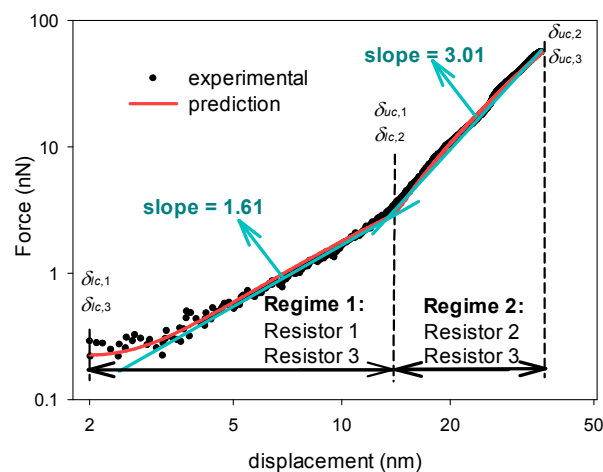
Figure 6. Example FIC of PDMS with a spherical indenter. The MRA provides adequate fitting throughout the entire range of indenter displacement. As a reference, the green line represents the best two-regime linear fit of the plot, with slopes 1.6 and 3.0 respectively. Comparing this Figure and Figure 4C, it is clear there is not necessarily a correlation between the number of mechanical resistors and regimes.

Figure 7 compares the values of the Young's modulus obtained through several methods by fitting experimental FIC data using:

- Oliver-Pharr (OP)[27] model using

$$dP/dh = 2\sqrt{R_{tip}}\, E_{eff}\, \delta_{max}^{1/2} \,;$$

- Hertz-Chadwick (HC) [8, 9] model for final portion of the FIC (asymptotic fit);
- HC model for the full FIC (full FIC fit).

In addition, it includes fitting of the linear region of the force-strain curve from uniaxial extension testing (UA), measured on a bulk elastomer.

Table 2. Average values of Young's modulus and standard deviations extracted using Hertz-Chadwick (HC) model [47],

Oliver-Pharr (OP) model [27], and the MRA method for PDMS indented with a 10.5 µm spherical probe.

Method	Mean (MPa)	Standard deviation (MPa)
MRA	1.52	0.50
HC - full FIC fit	0.74	0.22
OP (log-log slope < 3)	2.00	0.41
HC–asymptotic (log-log slope < 3)	2.10	0.43
UA	1.45	0.50

An increase in the predicted modulus with maximum indentation depth is observed in all indentation models, but particularly in those involving asymptotic fitting. However, if δ_{max} is taken as the point at which the log-log slope of the FIC reaches 3, a mean modulus of 2 MPa is obtained with a small standard deviation (0.41) using OP. The OP model yields results with the lowest standard deviation among the different methods (see Table 2) when a maximum slope of 3 is specified. However, if curves are analysed without checking for the slope at the position of the maximum, then the standard deviation exceeds that from MRA by a factor of 4; this is understandable since MRA performs an automatic check of regime applicability with respect to the range of power law exponents. The OP model results in a higher modulus compared to the MRA, while full fitting with the HC model gave lowest values of the elastic modulus, probably due to influence from the surface forces.

The MRA yielded values closest to the bulk values of elastic modulus, which can be considered as a successful criterion that validates the routine. We note that the good correlation between the bulk and MRA nanoindentation moduli is not due to a larger number of fitting parameters handled by the MRA model; on the contrary, the large number of parameters is usually less reliable since it increases the chance of non-unique combinations of parameters to satisfy the fit. The lower standard deviations and the corresponding consistency of the results do, however, benefit from multiple parameters that enable it to accommodate multiple scenarios of the indentation process. It should be noted that the modulus obtained using MRA is that from the thin film, which turned out to be the most adequate to describe the indentation of the elastomer's

surface. UA is, on the other hand, a bulk measurement performed over a 1 cm thick strip that is likely unaffected by the presence of a 0.5 µm surface layer. The surface layer is likely a swollen, hydrated layer of PDMS exhibiting viscoelastic behavior that is not intrinsic to the elastomer but a consequence of water diffusion (poroelasticity) [48]. If the time-dependent response vanishes quickly (which is reasonable for such small penetrations), the equilibrium modulus converges to the bulk modulus, explaining the excellent agreement between MRA and UA data over the indentation range 15 nm to 50 nm. For a maximum depth below ~15 nm, under-prediction is not surprising due to the dominance of the surface forces.

3.4 Analysis of FI curves for *Lolium multiflorum* cells

The choice of plant-based systems as a biological model was dictated by the innate features of plant cells that have multiple structural elements with distinct mechanical properties. [2, 3] Typically, the micromechanical properties are examined by collecting a 2D array of force curves over an area of interest. Such an array, also called a force volume plot, can be then used to present results in a graphical format as an image or a 3D contour plot. For the purposes of testing the MRA routine, however, we required high spatial density of force curves to ensure that any point-to-point variations are associated with the material properties and not with experimental or analysis artefacts. Thus, instead of a 2D array we have recorded numerous 1D tracks with 2-3 curves per point and with about 100-300 curves per track. By doing so, we ensured that the distance between points is less than ~2-4 times the radius of the tip. In Figure 8, typical FICs for *L. multiflorum* suspension-cultured cells are presented, together with fitting lines produced using the MRA routine. We generally observed little or no adhesion, although at certain locations on the cell surface we recorded multiple detachment peaks consistent with stretching of surface bound polymers, which we expect to be from the non-cellulosic polysaccharides (mostly hemicelluloses in this case). The analysis of these adhesive interactions has been already successfully realised within an automated routine [49], and hence was out of the scope of the current paper. Fig. 8

1 shows a hysteresis between the approach and retract curves,

2 which is significantly larger than that observed for PDMS.

3 The average energy dissipated during the indentation cycle,

4 $E_{Dissipated} = \int_0^{\delta_{max}} (F_{approach} - F_{retract}) d\delta$, is found to

5 be $69(\pm 6.7 s.e.) \cdot 10^{-18}$ J per indentation cycle. The degree of

6 hysteresis for the plant cells varied significantly, with the

7 minimum and maximum values of $1.59 \cdot 10^{-21}$ J and $0.7 \cdot 10^{-15}$

8 J respectively.
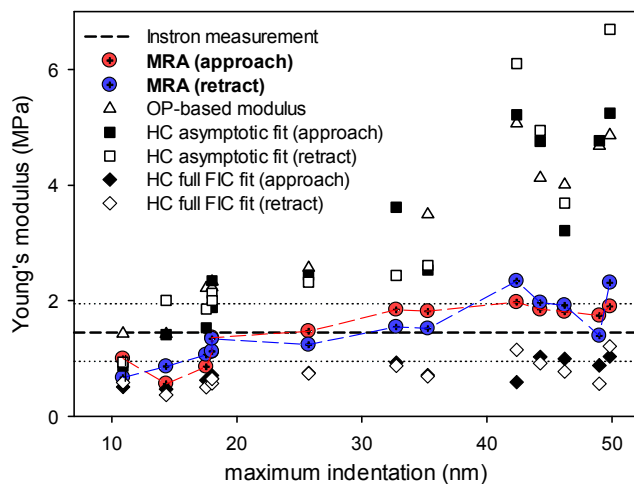
Figure 7. MRA was validated by comparing the Young's modulus of PDMS obtained through MRA interpretation of AFM nanoindentation and that from uniaxial stretching (UA) experiments. For indentations above 15 nm, the MRA predicts modulus values that are highly consistent with the bulk modulus from UA measurements (generally within one standard deviation shown by dashed-dot lines) and there is no apparent dependence on indentation depth. The OP and HC based moduli were also computed. The OP-based modulus is similar to that obtained from the asymptotic fit of the FIC using the HC model, with values increasing with indentation depth. Fitting the entire curve with HC produces consistent underprediction of the bulk modulus, as a consequence of the influence of surface interactions.

9 The values of fitting parameters for the entire dataset

10 are summarized in Table S1 (Supplementary Information).

11 The majority of datasets recorded for *L. multiflorum* cells

12 using an AFM tip displayed a behavior characterized by

13 three resistors: a surface force, linear deformation (a quasi-

14 'elastic shell') and a thin elastic film. The linear deformation

15 normally occurred concomitantly with the other resistors,

16 creating a two regime response. A significant number of

17 curves had some discontinuities that are likely to be

18 associated with the penetration of the tip into voids within

19 the polysaccharide mesh of the cell wall. Since large

20 discontinuities may cause considerable error in parameter

21 estimation if not taken into account, the algorithm is

22 allowed to produce as many discontinuities as there are

23 regime transitions, given that it is in these instances that the

24 largest discontinuities are found. Still, the presence of

25 discontinuities is the most challenging aspect to be handled

26 during curve fitting and more rigorous approaches to

27 incorporate them need to be developed.
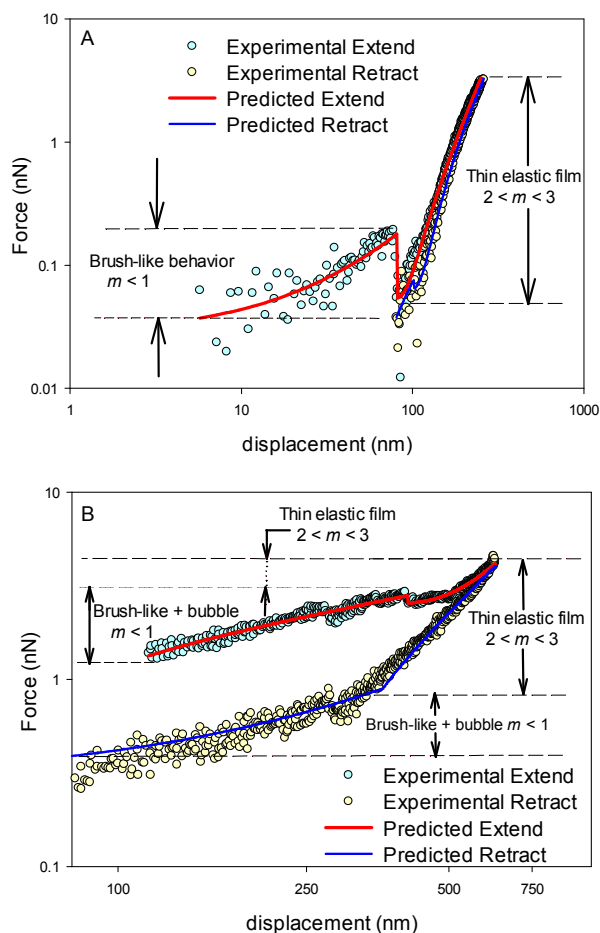
Figure 8. Typical FICs for *L. multiflorum* suspended culture cells. The majority of FICs were characterized by three resistors: a surface force (**A** and **B**), a quasi-'elastic shell' or 'bubble' (**B** only) and a thin elastic film (**A** and **B**). The 'bubble' in **B** occurred concomitantly with the other resistors, generating a two regime response. In both cases, discontinuities associated with penetration of the tip into the voids of the cell wall polysaccharide mesh are present.

28

29 To compare the performance of MRA, OP and HS

30 models, we used 1D datasets collected on *L.multiflorum*

31 cells. Figures 9A and B depict the parameters obtained

from interpretation of indentation data taken along an arc trajectory (3 μm long) on the surface of the cell. Firstly, we found that the average difference between the moduli calculated from the approach and retract branches is 1.1 MPa for the HS model, considerably higher than that found for the MRA method of 0.3 MPa. The good correlation between the moduli obtained from approach and retract curves using MRA is better appreciated in Figure 9C, where it is clear that superior consistency is achieved compared to HS. The large differences between approach and retract observed in HS are associated with the cross-talk between surface forces and the elastic part of the indentation curve. This may arise from the weak brush-like interactions that are evident on the approach branch before the tip makes full contact with the cell wall, which the HS model attributes entirely to a soft Hertzian film/solid, leading to an approach modulus considerably lower than obtained from the retract branch. Such an effect is not observed for PDMS because surface roughness is expected to be more pronounced for the locally disordered and highly heterogeneous surface of a plant cell. On the other hand, the high modulus from the retract curve using HS is a consequence of the presence of highly non-linear segments, with large values of the power law exponent. In MRA such segments are accounted for by using an empirical hyperelastic model. The OP fitting was performed by truncating the curve when its log-log slope was above 3, which means this method does not suffer from the presence of higher order regimes. Among all the methods compared in Figure 9, OP is the one with the lowest averaged-standard deviation (i.e. the average of the standard deviations at every point) and follows closely the trend obtained through MRA. However, since OP is entirely based on analysis of the retract curve, it is not possible to check its consistency.

We also note that the discrepancy in the values of the modulus obtained through MRA (~2MPa) and OP (~0.5MPa) is not due to a potential correlation between thickness and elastic modulus, which is a recognized issue in the thin film model by Chadwick and co-workers [8, 9]. Simultaneous determination of the modulus and wall thickness from AFM measurements is a challenging task, and similar issues are recognized for indentation of plant cells with a macroscopic flat punch [50]. Fortunately, the thin film deformation region is only ~100-300 nm in thickness, which is a fraction of the total indentation and much smaller than the thickness of L.multiflorum cell walls (ca. 1000-3000 nm according to microscopy measurements[51]). Therefore, a 10% error in wall thickness results in only a 1% error in elastic modulus, provided indentation-thickness ratio stays ≤0.1, i.e. $\frac{\Delta E}{E} \sim \frac{\delta_{Thin\,Film}}{h}\left(\frac{\Delta h}{h}\right) \sim 0.1\frac{\Delta h}{h}$.

These results demonstrate the power of the MRA to reasonably interpret complex and non-linear FICs obtained during approach and retraction of an AFM cantilever. The method is particularly powerful for biological samples that display significant hysteresis between approach and retract, thereby providing superior quantification of micromechanical properties over the routinely used OP and HS models.

4 Conclusions

A Multi-Regime Analysis (MRA) has been developed as a new routine for analysing complex force indentation measurements from the AFM. This analysis provides, for the first time, a simple means in which to obtain relevant micromechanical properties of materials where there are multiple contributions to mechanical response in force-indention experiments. The advantage of the approach is that it enables non-linear FICs to be interpreted using several contact micromechanics models, and ensures that these models are used within their relevant ranges of applicability. Another major advantage of the MRA approach, particularly for naturally variable biological systems, is that the MRA can be routinely used to analyse large data sets of FICs, even when they contain several deformation regimes as is the case for complex soft materials such as cells. The key feature of the analysis, as applied here, is that it resolves convoluted force-indentation curves by assuming the force-indentation response is a result of the serial superposition of elastic resistors, each operating within a well-defined range of deformations.

The MRA algorithm is demonstrated to accurately interpret nano-indentation measurements performed on PDMS microspheres. We find this approach allows

1   identification of three major contributors to the
2   micromechanical response of the spheres; surface force, an
3   elastic thin film and elastic solid. It uniquely obtains an
4   elastic modulus that is similar to the bulk elastic modulus of
5   the PDMS. In comparison, the OP model results in
6   significantly higher modulus than the bulk value while the
7   HC model under predicted its value; these regularly used
8   models are unable to account for multiple contributions to
9   the measured mechanical response.

10   The MRA is used in an automated routine to analysis
11   plant cells to show that their micromechanical response
12   arises from a combination of surface forces, a stiff cell wall,
13   and a Hertzian thin film. We discover that the MRA
14   approach uniquely predicts the same modulus of the cell
15   wall from both approach and retraction curves, which
16   further validates the MRA model. Since plant cells, like
17   many other biological systems, are inherently
18   heterogeneous, the advantage of a MRA is that it is readily
19   automated to allow large sets of FIC curves at multiple
20   locations around a cell, and/or on multiple cells, to be
21   routinely analysed. We use this method to identify that
22   there are local variations in the mechanical parameters of
23   plant cell walls, which may be relevant to cell growth and
24   require further research; this new technique will allow such
25   research to be possible.
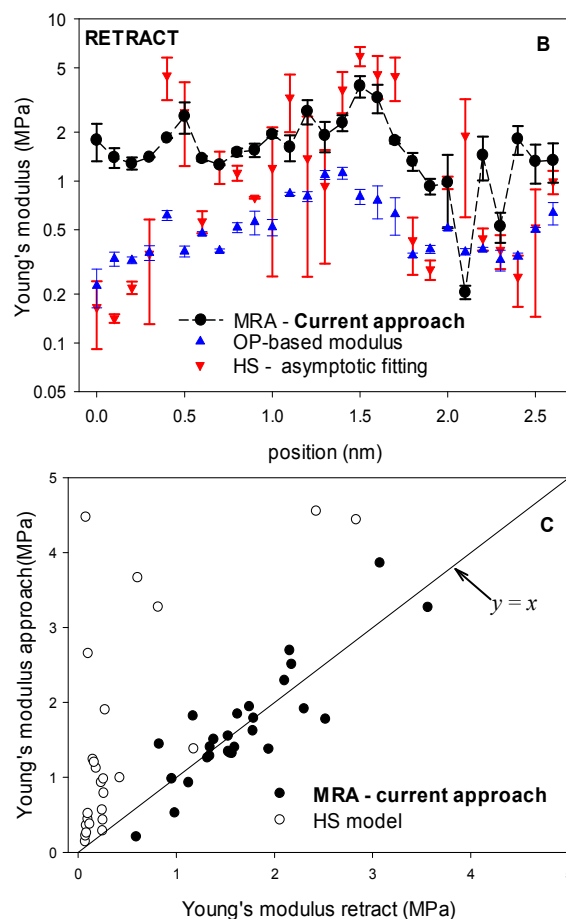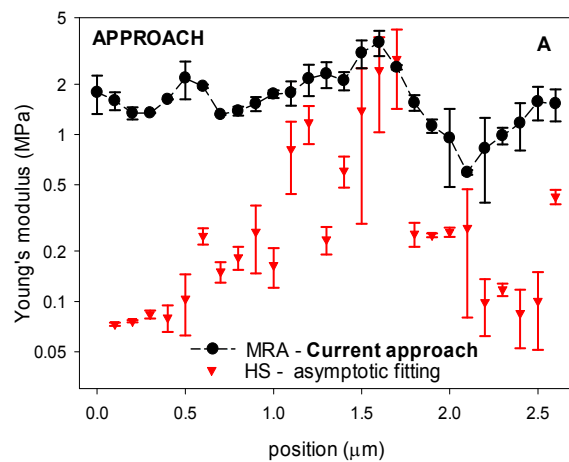
Figure 9. Validation of MRA through interpretation of AFM nanoindentation experiments on plant cells. The plots compare 1D track elastic moduli calculated from MRA, OP and HS. Two repetitions per point were performed; the symbols represent the average value and the bars standard deviation during (A) Approach and (B) Retract. The OP fitting was performed by truncating the curve when its log-log slope was above 3. (C) Correlation between elastic moduli extracted from Approach and Retract branches of the force curve through HS and MRA. The strong correlation displayed by the MRA-based moduli strongly supports the validity of the technique. On the other hand, HS produces approach and retract moduli that greatly deviates for the $y = x$ line.

26

27   We consider that the MRA approach will add
28   significant value to recent technique developments for the
29   AFM, including research that combines linear indentation
30   with oscillatory measurements, such as multi-harmonic
31   analysis [52], Amplitude-Modulated-Frequency-Modulated
32   AFM [53], or PeakForce tapping QNM® (Quantitative
33   Nanomechanical Property Mapping) [54]. The essential
34   principle of oscillatory methods is that they analyse
35   changes in the Fourier spectrum of the AFM cantilever
36   oscillations upon interaction with the cell surface. Further,

the spectrum parameters can be related to local mechanical properties of the surface [55, 56] and hence can probe high frequency viscoelastic response that is inaccessible in liner indentation measurements, and therefore provides important complimentary information.

In conclusion, Multi-Regime Analysis extracts new information from AFM indentation measurements by disentangling different mechanical contributions convoluted within a force-versus indentation curve. The extraction of conventional elastic parameters such as Young's modulus yielded high consistency, thus leading to a more accurate and precise nanomechanical mapping of biological materials using AFM. The method can be easily extended and adapted to include viscoelastic and plastic regimes. The method provides an important first approximation tool in discovering underlying mechanisms of mechanical behaviour in biological systems, and is essential for interpreting force-indentation measurements of such systems and other soft materials with hierarchical structures.

Acknowledgements

Notes and references

[a] ARC Centre of Excellence in Plant Cell Walls, School of Chemical Engineering, The University of Queensland, Brisbane, Australia.
[b] School of Chemical Engineering, The University of Queensland, Brisbane, Australia.
[c] ARC Centre of Excellence in Plant Cell Walls, Centre for Nutrition and Food Sciences, Queensland Alliance for Agriculture and Food Innovation, The University of Queensland, Brisbane, Australia.
* Corresponding author: g.yakubov@uq.edu.au

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