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Complete List of Authors:	Langeslay, Blake; University of Illinois at Urbana-Champaign, Physics Juarez, Gabriel; University of Illinois at Urbana-Champaign,

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1 Microdomains and Stress Distributions in Bacterial Monolayers on 2 Curved Interfaces

3 Blake Langeslay¹ and Gabriel Juarez^{2*}

4 ¹*Department of Physics, University of Illinois at
5 Urbana-Champaign, Urbana, Illinois 61801, USA and*

6 ²*Department of Mechanical Science and Engineering,
7 University of Illinois at Urbana-Champaign, Urbana, Illinois 61801, USA*

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9 Abstract

10 Monolayers of growing non-motile rod-shaped bacteria act as active nematic materials composed
11 of hard particles rather than the flexible components of other commonly studied active nematics.
12 The organization of these granular monolayers has been studied on flat surfaces but not on curved
13 surfaces, which are known to change the behavior of other active nematics. We use molecular
14 dynamics simulations to track alignment and stress in growing monolayers fixed to curved surfaces,
15 and investigate how these vary with changing surface curvature and cell aspect ratio. We find that
16 the length scale of alignment (measured by average microdomain size) increases with cell aspect
17 ratio and decreases with curvature. Additionally, we find that alignment controls the distribution of
18 extensile stresses in the monolayer by concentrating stress in negative-order regions. These results
19 connect active nematic physics to bacterial monolayers and can be applied to model bacteria growing
20 on droplets, such as oil-degrading marine bacteria.

* Email address.; gjuarez@illinois.edu

21 I. INTRODUCTION

22 The role of mechanical forces in bacterial growth is of increasing interest to both biologists
23 and physicists [1–6]. Bacteria colonize a wide variety of interfaces (liquid-solid, liquid-
24 air, liquid-liquid) with vastly different properties [7–10]. To thrive under these diverse
25 conditions, cells must contend with physical forces such as surface tension and hydrodynamic
26 interactions to stably adhere to the interface over many generations. Bacteria growing on
27 a flat interface as a monolayer of cells have been successfully modeled as an active nematic
28 material. This is a widely studied class of active liquid crystal whose components align
29 parallel to one another and have end-to-end symmetry [2, 11]. Rod-shaped bacteria cells
30 have the required symmetry and, when in a dense monolayer, align due to steric interactions
31 between cells. Extensile activity can be produced by motility [12] or by the growth and
32 division of the cells [11]. In either case, forces in the monolayer are strongly coupled to
33 alignment, as both motility and growth exert forces along the axis of orientation.

34 The active nematic model of bacterial monolayers has proven powerful in predicting
35 the internal forces and behavior of real systems such as monolayers of gliding *Myxococcus*
36 *xanthus* and chaining *Bacillus subtilis* biofilms [12, 13]. In particular, the behavior of cells
37 near topological defects has been successfully tied to the behavior of other well-studied active
38 nematic systems. Topological defects are singularities in the director field of liquid crystal
39 alignment. At these locations, there is a net rotation of the director field, which is used to
40 define the defect’s charge. In active nematic materials, defects are almost always limited
41 to charges of $\pm 1/2$ [14]. These singularities drive much of the unique behavior of active
42 nematics. Comet-shaped $+1/2$ defects move as motile particles that generate complex flows
43 [14, 15]. In other systems, material is accumulated at positively charged defects while it
44 is depleted at negatively charged defects, allowing 2D materials to escape into the third
45 dimension by multilayering or buckling [16–20]. This last effect has been observed to drive
46 transitions from monolayers to multilayered 3D structures [12, 13].

47 Previous work on monolayers of rod-shaped bacteria has indicated that their alignment
48 behavior is dependent on whether the cells are hard rods (such as *E. coli*) or whether
49 they are flexible rods (such as *M. xanthus*) [2, 12, 21]. In this case of hard rods, cells
50 have been observed to segregate into microdomains, regions of near-parallel local alignment
51 analogous to grains in crystalline or granular materials [2]. Rather than having a continuous,

52 gradually changing alignment field, these systems exhibit sharp changes in alignment across
53 the boundaries between microdomains. This represents a fundamentally different type of
54 liquid crystal behavior from that observed in active nematics composed of microtubules or
55 flexible cells. In these systems, microdomains and their boundaries can replace topological
56 defects as a way of mapping alignment [2].

57 The alignment behavior of simulated and microtubule-based active nematic materials is
58 well known to change based on the curvature of their substrate. Topological defects respond
59 to curvature, with $+1/2$ ($-1/2$) defects accumulating at regions of positive (negative) Gaus-
60 sian curvature [22–24]. However, it is currently unknown what effect curvature might have
61 on the alignment of a more granular hard-cell system. One such system is a monolayer of the
62 oil-degrading bacterium *Alcanivorax borkumensis* growing on the surface of an oil droplet
63 in water. These cells have been observed to lie tangent to the oil-water interface and grow
64 to form a single monolayer. After completely covering the available surface area of the oil
65 droplet, the continued growth of cells within the monolayer generates interfacial stresses that
66 lead to the deformation of the oil-water interface [25, 26]. To understand how interfacial
67 growth stresses behave in a curved growing monolayer, it is crucial to first understand the
68 alignment behavior of cells within the layer.

69 To investigate this issue, we simulated the growth of rod-shaped cells adsorbed tangent to
70 the surface of spherical droplets. This enabled analysis of how substrate curvature influences
71 cell alignment and, therefore, stress within the monolayer. We find that both cell aspect
72 ratio and surface curvature play a role in controlling the length scale of alignment, with
73 higher curvature substrates limiting alignment. Additionally, we find that regions of high
74 stress are predicted by negative orientational order. These results enable predictions of how
75 granular monolayer behavior might vary on differently curved surfaces.

76 II. METHODS

77 A. Experiments of bacterial growth at flat liquid interfaces

78 Cell cultures of *A. borkumensis* were grown for 24 hours in ATCC medium 2698 at 30
79 °C in an orbital shaker at 180 RPM. Cells were non-motile and rod-shaped with an average
80 length of 2.7 μm and width of 0.7 μm . To observe bacterial growth at oil-water interfaces, a

81 custom microfluidic device was used. A flat oil-water interface was pinned to a microscope
 82 slide by a thin copper TEM grid (18 μm , SPI Supplies, 2010C-XA) with square apertures 205
 83 μm wide. The cell culture was injected above this, allowing cells to adsorb on the interface.
 84 Then, a microfluidic chamber was constructed around the grid to house the interface and
 85 allow for the constant flow of growth media (diluted 10:1 with artificial seawater) at 2 μL
 86 min^{-1} . This flow prevented additional cells from settling on the grid during the experiment.

87 Time-lapse phase contrast microscopy was used to image the growing cell colony for
 88 8 hours using a 60 \times objective (NA = 0.6 and a depth of field of 2 μm). A single square
 89 aperture in the TEM grid was imaged in an experiment, selected for clarity and lack of visible
 90 contaminants. Images were recorded with a 50 ms exposure time at 2-minute intervals for
 91 24 hours (see supplementary video SV1).

92 B. Simulations of bacterial growth on flat and curved surfaces

93 Molecular dynamics simulations were conducted to obtain precise quantitative data on
 94 the physical characteristics of growing bacterial monolayers on flat and curved liquid-liquid
 95 interfaces. Each cell was modeled as a spherocylinder with a diameter d_0 and length l
 96 between the endcaps. To simulate cell growth, the length of the cylinder l increased linearly
 97 with time up to a maximum length l_0 while the diameter remained fixed at d_0 .

98 To model cells adsorbed on 2D surfaces, the center of volume of cells was constrained to
 99 coincide with the surface and the cell orientation was constrained parallel to the surface (or
 100 to the tangent plane at the point of contact, for spherical surfaces). Therefore, no out-of-
 101 plane motion was allowed. Out-of-plane forces and torques were assumed to be balanced by
 102 the surface tension of the interface. The changes in position \vec{x} and orientation θ of each cell
 103 were modeled by the overdamped Newton's equations as follows:

$$\frac{d\vec{x}}{dt} = \frac{1}{l\zeta} \vec{F}_{\parallel} \quad (1)$$

104

$$\frac{d\theta}{dt} = \frac{12}{l^3\zeta} \tau_N \quad (2)$$

105 where \vec{F}_{\parallel} is the total force on the cell due to cell-cell interactions after projection onto
 106 the plane tangent to the sphere at the cell's center. Similarly, τ_N is the torque on the
 107 cell projected to be normal to the same plane. Here ζ is a drag per unit length. This

108 term originates from Stokes drag on the adsorbed cells, thereby justifying the choice of
 109 overdamped motion [27].

110 The interactions between cells were modeled as Hertzian forces, with the force on cell i
 111 due to cell j acting at the point of contact and calculated as follows:

$$\vec{F}_{ij} = Y d_0^{1/2} h_{ij}^{3/2} \vec{N}_{ij} \quad (3)$$

112 where Y is proportional to the Young's modulus of a cell, h_{ij} is the overlap distance between
 113 the two cell bodies, and \vec{N}_{ij} is the vector normal to cell j at the point of contact [2, 28, 29].
 114 Additionally, to prevent perfect alignment of cells, each cell was subject to a "noise" force $\vec{\eta}$
 115 at each time step with random components η_x, η_y, η_z each in the range $[-\eta_0, \eta_0]$.

116 Cell growth was modeled using a time-independent rate g_0 . To prevent the synchronized
 117 division of cells, each cell was assigned random a value between $g_0/2$ and $3g_0/2$ for the
 118 growth rate. Whenever a cell length l exceeded the maximum length l_0 , cell division would
 119 occur where the cell would split into two identical cells, each with a length $(l_0 - d_0)/2$. The
 120 new cell would be initialized with the same orientation θ as the original cell, however, the
 121 new cell would be assigned a different randomized growth rate. At each time step, cells
 122 with lengths greater than l_0 were divided, then forces and torques on cells were calculated.
 123 Finally, cell positions were updated using the explicit Euler method to numerically integrate
 124 the equations of motion.

125 Simulations of growth on flat surfaces were conducted in a square periodic boundary
 126 of 40 μm per side. To correspond to experiments, simulations were initialized $22 \leq N \leq$
 127 26 randomly placed and oriented cells. Simulations of growth on spherical surfaces were
 128 initialized with two parent cells, one located at the north pole and the other at the south
 129 pole of the sphere. This resulted in two hemispherical colonies growing until contact was
 130 made at the equator, after which, the distribution of cells rapidly became homogeneous
 131 across the entire surface. Data was collected on fully-covered spheres once they had reached
 132 a packing fraction of $\phi = 1.05$; where ϕ was defined as the area fraction of the surface
 133 covered by cells, $\frac{1}{A_{\text{sphere}}} \sum_i a_i$, where a_i is the area of the i th cell projected onto the tangent
 134 plane to the sphere's surface at the cell's center.

135 Simulation model parameter values were chosen to be representative of a generic gram-
 136 negative, rod-shaped bacterium, including those for the *A. borkumensis* cells used in ex-
 137 periments at flat liquid interfaces [2]. Therefore, the values were set to the following: cell

138 diameter d_0 to $0.7 \mu\text{m}$, Young's modulus Y to 4 MPa , drag per unit length ζ to 200 Pa h ,
 139 and growth rate g_0 to $2 \mu\text{m h}^{-1}$. A simulation time step of 5×10^{-6} hours was used, with
 140 a maximum noise η_0 of $2 \times 10^{-9} \text{ N}$. To study the effect of different cell aspect ratios, the
 141 maximum growth length allowed was varied between $2 < l_0 < 5 \mu\text{m}$. Cell elongation was
 142 parametrized with the aspect ratio α , defined here as $\alpha = (l_0 + d_0)/d_0$, therefore, ranging
 143 from $3.9 < \alpha < 8.1$. To study the effect of varying substrate curvature κ , spherical substrates
 144 with radius $R = 10, 12, 15, 20,$ and $30 \mu\text{m}$ were used. Here, substrate curvature is defined
 145 as the Gaussian curvature, or $\kappa = R^{-2}$, for a spherical surface. The surface curvatures and
 146 cell lengths here were chosen such that cells following the surface constraint (tangent to the
 147 surface and attached at their center) did not extend more than $d_0/2$ above the interface,
 148 thus ensuring that they intersected the interface throughout their length.

149 III. RESULTS

150 In both experiments and simulations, bacteria grow and divide at the surface, forming
 151 a monolayer that eventually covers the entire available surface area, shown in Fig. 1. At
 152 early times, single cells grow and divide to form colonies, shown in Fig. 1 (top row). At
 153 later times, as the cells continue to grow and divide, their contact forces and torques cause
 154 them to align with their neighbors to form a liquid crystal with nematic symmetry, shown
 155 in Fig 1 (bottom row). As cells grow, the area covered by the colony increases exponentially
 156 with time until the available surface area is fully covered. These behaviors are consistently
 157 observed in experiments of growth on flat interfaces and in simulations of growth on flat
 158 and spherical substrates (Fig. 1). A side-by-side qualitative comparison of experimental
 159 and simulated results with similar color schemes and cell sizes is shown in supplementary
 160 information Fig. S1.

161 To establish correspondence between experiments on liquid-liquid interfaces and sim-
 162 ulations, the distribution of topological defects in cell monolayers on flat interfaces and
 163 substrates, respectively, are compared. First, to identify topological defects, a director field
 164 was established. In experiments, the director field was determined using a custom image-
 165 processing algorithm based on the brightness gradient of the phase contrast images (see
 166 supplementary information). In simulations, the director field was generated directly from
 167 the position and orientation of each cell. Then, to locate topological defects within the di-

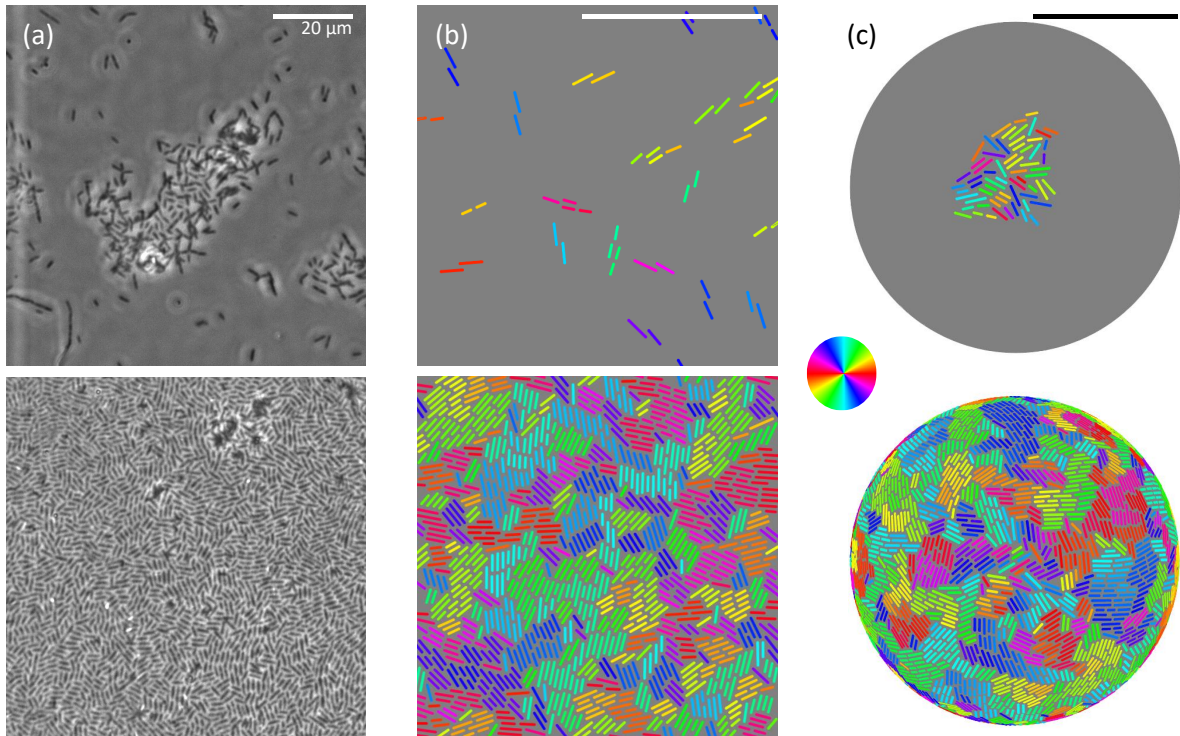


FIG. 1. Formation of a bacterial monolayer due to growth at flat and curved substrates. (a) Micrographs of *A. borkumensis* cells growing on a flat liquid interface at (top) early times and (bottom) up to full surface coverage. (b, c) Simulations of cell growth on (b) flat and (c) spherical substrates with $R = 20 \mu\text{m}$ at (top) early times and (bottom) up to full surface coverage. Colors correspond to the cell orientation angle. All scale bars shown represent $20 \mu\text{m}$. See supplementary videos SV1, SV2, and SV3.

168 rector field, each point on the grid (or each cell in simulations) was tested for a net rotation
 169 of the surrounding director field (with net rotations of $\pm\pi$ corresponding to defect charges
 170 of $\pm 1/2$) [30]. Nearby points with similar net rotations were then grouped by a cluster-
 171 ing algorithm with the centroid of each cluster corresponding to a defect of the associated
 172 charge.

173 The distribution of topological defects in experiments at flat interfaces was compared to
 174 that in simulations of growing cells with the same dimensions as *A. borkumensis* on flat
 175 substrates, shown in Fig. 2 (top row, flat) and supplementary information Fig. S2. To find
 176 the length scale of alignment, the average defect separation $\langle \delta x \rangle$ was calculated as $\langle \delta x \rangle =$
 177 $\rho^{-1/2}$, where ρ is the defect density. In each experimental field of view, there were at least

178 ≥ 400 defects. In experiments, the mean defect separation over four experiments is 9.8 ± 0.8
 179 μm . In simulations, the mean defect separation over five simulations is $9.0 \pm 0.3 \mu\text{m}$. Here,
 180 the uncertainties represent the standard error. Based on this qualitative and quantitative
 181 agreement between experiments and simulations, the simulation model previously used for
 182 liquid-solid interfaces also captures the salient features at liquid-liquid interfaces in the
 183 packing fraction regime tested here.

184 Next, the effect of cell aspect ratio α and substrate curvature κ on orientational order, the
 185 degree of alignment, and stress within the cell monolayer was investigated using simulations.
 186 First, the orientational order S was evaluated to measure the degree of local alignment in
 187 the monolayer. This was calculated at each individual cell i using the following equation:

$$S_i = \frac{1}{N} \sum_j 2 \cos^2(\theta_i - \theta_j) - 1 \quad (4)$$

188 where θ_j is the orientation of each cell whose center lies within a search radius of cell i , N is
 189 the total number of cells within the search radius, and the difference in angles is calculated
 190 accounting for parallel transport on the curved surface. For the purpose of this analysis,
 191 the search radius was set equal to the division length l_0 of the cells. Here, $S \rightarrow 1$ represents
 192 ordered regions while $S \rightarrow 0$ represents disordered regions.

193 Simulations reveal regions of high order separated by regions of low order, shown in Fig.
 194 2 (top row). These regions of high cell alignment emerge for all combinations of substrate
 195 curvature and cell aspect ratio, including flat substrates. For a given curvature, increasing
 196 the cell aspect ratio from $\alpha = 4.9$ to $\alpha = 6.7$ increases the size of these regions, shown
 197 in Fig. 2 ($R = 20 \mu\text{m}$). Additionally, topological defects tend to coincide with areas of
 198 low order, shown in Fig. 2 (top row). This follows from the definition of defects, as the
 199 net rotation of the director field around the defect requires imperfect alignment. Therefore,
 200 increasing the cell aspect ratio also increases the distance between $\pm 1/2$ defects, as shown
 201 in supplementary information Fig. S3.

202 Next, the mean microdomain area $\langle A \rangle$ was calculated to characterize the degree of cell
 203 alignment in the monolayer. Boundaries between microdomains are one-dimensional discon-
 204 tinuities in the alignment field rather than point defects, separating regions of near-parallel
 205 alignment. Cells were sorted into microdomains using the following two criteria: two cells
 206 must be in the same domain if (i) they were in contact with one another and (ii) their orien-
 207 tation differed by less than 0.2 radians. Each pair of cells was checked to create an adjacency

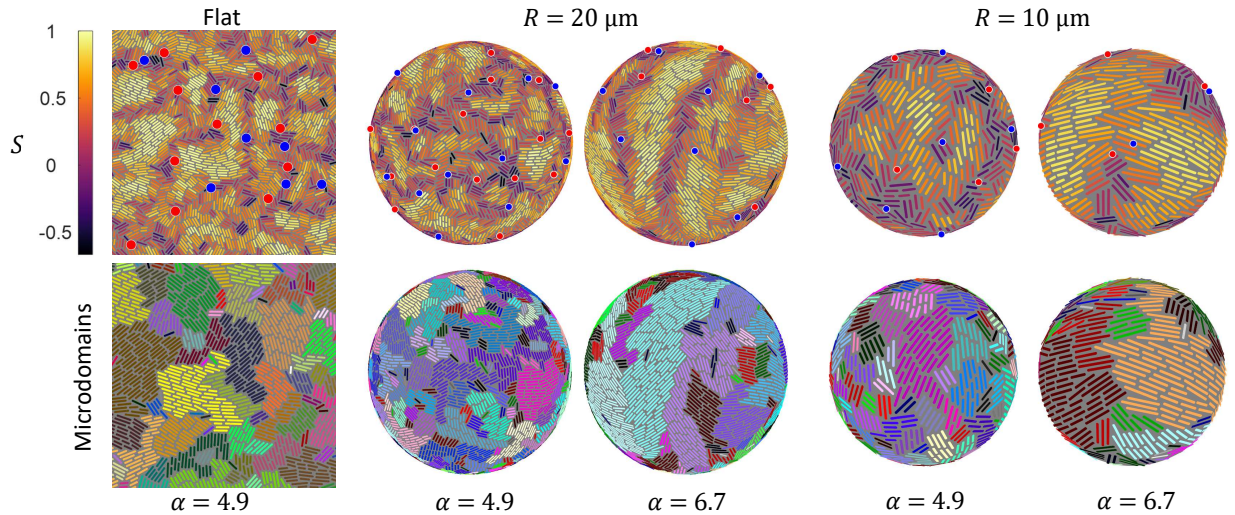


FIG. 2. Orientational order, topological defects, and microdomains in simulations of monolayers with varying cell aspect ratio α and substrate radii R . (Top row) Orientational order S and topological defects with charge $\pm 1/2$ shown in red/blue, respectively. Topological defects tend to occur in regions of low orientational order for all aspect ratios and substrate radii. (Bottom row) Microdomain representation of the cell monolayers shown in the top row. Microdomain boundaries tend to coincide with regions of low orientational order for all aspect ratios and substrate radii. For visualization purposes, spherical substrates ($R = 10 \mu\text{m}$ and $R = 20 \mu\text{m}$) are not shown to scale while the field of view for the flat simulations (leftmost column) is $50 \times 50 \mu\text{m}$.

208 matrix, which then produced an unambiguous sorting into distinct microdomains.

209 Microdomains, represented as differently colored regions, correspond to regions of high-
 210 aligned cells, shown in Fig. 2 (bottom row). Borders between large microdomains correspond
 211 to regions of low order, reflecting the discontinuity in alignment between microdomains.
 212 Similarly, for a given curvature, increasing the cell aspect ratio increases the size of a single
 213 microdomain, shown in Fig. 2 ($R = 20 \mu\text{m}$). The area of a microdomain is given as
 214 $A = \phi^{-1} \sum a_i$, where a_i are the projected areas of each cell within the microdomain. The
 215 distributions of microdomain areas for each aspect ratio and surface curvature are shown in
 216 supplementary information Fig. S4. The mean microdomain area for a system is used to
 217 characterize the area scale of its cell alignment.

218 The mean microdomain area increased with increasing cell aspect ratio, shown in Fig.
 219 3(a). For the lowest curvature ($\kappa = 0.001 \mu\text{m}^{-2}$, $R = 30 \mu\text{m}$) the effect of cell aspect ratio

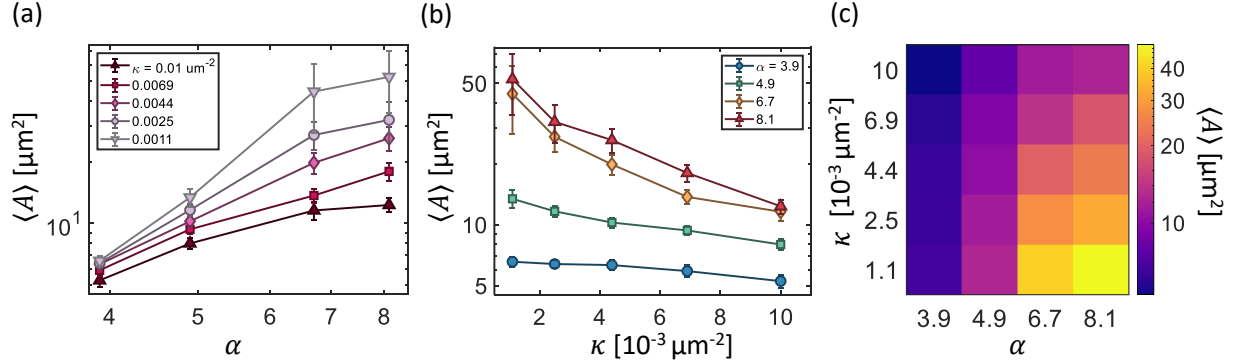


FIG. 3. The effect of cell aspect ratio and substrate curvature on microdomain area. (a) Log-log plot of mean microdomain area $\langle A \rangle$ for different cell aspect ratios α on five different substrate curvatures. Error bars represent standard error. Microdomain area increases with the aspect ratio for all curvatures. (b) Semilog plot of mean microdomain area $\langle A \rangle$ for different substrate curvatures κ and four different cell aspect ratios. Error bars represent standard error. Microdomain area decreases with substrate curvature for all aspect ratios. (c) Summary of the mean microdomain area $\langle A \rangle$ across the simulated parameter space of aspect ratio and substrate curvature.

220 was the most dramatic, with an increase in the mean domain area of seven-fold. For the
 221 highest curvature ($\kappa = 0.01 \mu\text{m}^{-2}$, $R = 10 \mu\text{m}$), however, the effect of cell aspect ratio was
 222 less prominent, producing an increase in the domain area of a factor of two. The increase
 223 in alignment at higher α is consistent with previous work on bacterial monolayers, which
 224 has shown that more elongated (higher aspect ratio) cells produce stronger alignment in flat
 225 monolayers [2]. To test that these results are not sensitive to the specific form of cell growth
 226 in our model, we conducted a limited set of extra simulations in which doubling time rather
 227 than growth rate was held constant. A comparison between results with the two types of
 228 growth is shown in supplementary information Fig. S5. The same relation between aspect
 229 ratio and microdomain area holds in both cases.

230 The mean microdomain area decreased with increasing substrate curvature, shown in
 231 Fig. 3(b). The effect was more pronounced for higher aspect ratio cells. Simulations with
 232 the highest aspect ratio ($\alpha = 8.1$) produced a 75% decrease in microdomain area over the
 233 range of curvatures investigated, while simulations with the lowest aspect ratio ($\alpha = 3.9$)
 234 exhibited a decrease of only 20%. In all cases, however, more curved substrates produced
 235 consistently lower microdomain areas.

236 Measurements of mean domain area across a range of aspect ratios and curvatures were
 237 combined to show the system's response over the $\alpha - \kappa$ parameter space, shown in Fig. 3(c).
 238 The combined effect of cell aspect ratio and substrate curvature on microdomain area is
 239 evident. The largest domain areas are observed at high cell aspect ratios and low substrate
 240 curvatures. The smallest domain areas, however, are observed at low cell aspect ratios and
 241 high substrate curvatures.

242 Lastly, the parallel component of the Virial stress σ_{\parallel} on each cell was measured to de-
 243 termine the force distributions in the monolayer. The Virial stress $\boldsymbol{\sigma}_i$ on a cell is given as
 244 follows [2, 6]:

$$\boldsymbol{\sigma}_i = \frac{\phi}{a_i} \sum_j \mathbf{r}_{ij} \mathbf{F}_{ij} \quad (5)$$

245 where a_i is the area of cell i 's projection onto the tangent plane, \mathbf{r}_{ij} is the vector from
 246 the center of cell i to the point of contact with cell j , and \mathbf{F}_{ij} is the force from cell j on
 247 cell i . When $\boldsymbol{\sigma}$ is calculated in the basis of vectors parallel and perpendicular to the cell's
 248 orientation in the plane tangent to the sphere at the cell's center, it can be decomposed into
 249 parallel (σ_{\parallel}), perpendicular (σ_{\perp}), and shear (τ) components:

$$\boldsymbol{\sigma} = \begin{bmatrix} \sigma_{\parallel} & \tau_{ij} \\ \tau_{ji} & \sigma_{\perp} \end{bmatrix}$$

250 The parallel stress σ_{\parallel} corresponds to the force in the direction of the cells' growth. Because
 251 of the extensile nature of the system, σ_{\parallel} and σ_{\perp} are always negative (corresponding to a
 252 compressive force), while the shear stresses are much lower on average because all forces
 253 between cells are normal to the cells' surfaces at the point of contact.

254 The parallel component of the Virial stress, normalized by the mean stress, for each cell
 255 in the monolayer on a curved substrate with $R = 15 \mu\text{m}$ is visualized and shown in Fig.
 256 4(a). At the cell level, the normalized stress varied over a wide range of values. For example,
 257 for $\alpha = 4.9$ and $R = 15$, the mean stress was $\langle \sigma_{\parallel} \rangle = -0.030 \text{ N/m}$, and the normalized stress
 258 varied from a minimum of zero up to a maximum of $\sim 3.1 \langle \sigma_{\parallel} \rangle$. For an aspect ratio of $\alpha = 6.7$
 259 and the same surface curvature, the mean stress was $\langle \sigma_{\parallel} \rangle = -0.025 \text{ N/m}$ and the normalized
 260 stress varied from a minimum of zero up to a maximum of $\sim 4.7 \langle \sigma_{\parallel} \rangle$. Stress visualization in
 261 growing monolayers with varying values of α and κ can be seen in supplementary videos SV4
 262 – SV7. The average parallel and perpendicular stress at each aspect ratio and curvature are
 263 shown in supplementary information Fig. S6(a,b,d,e).

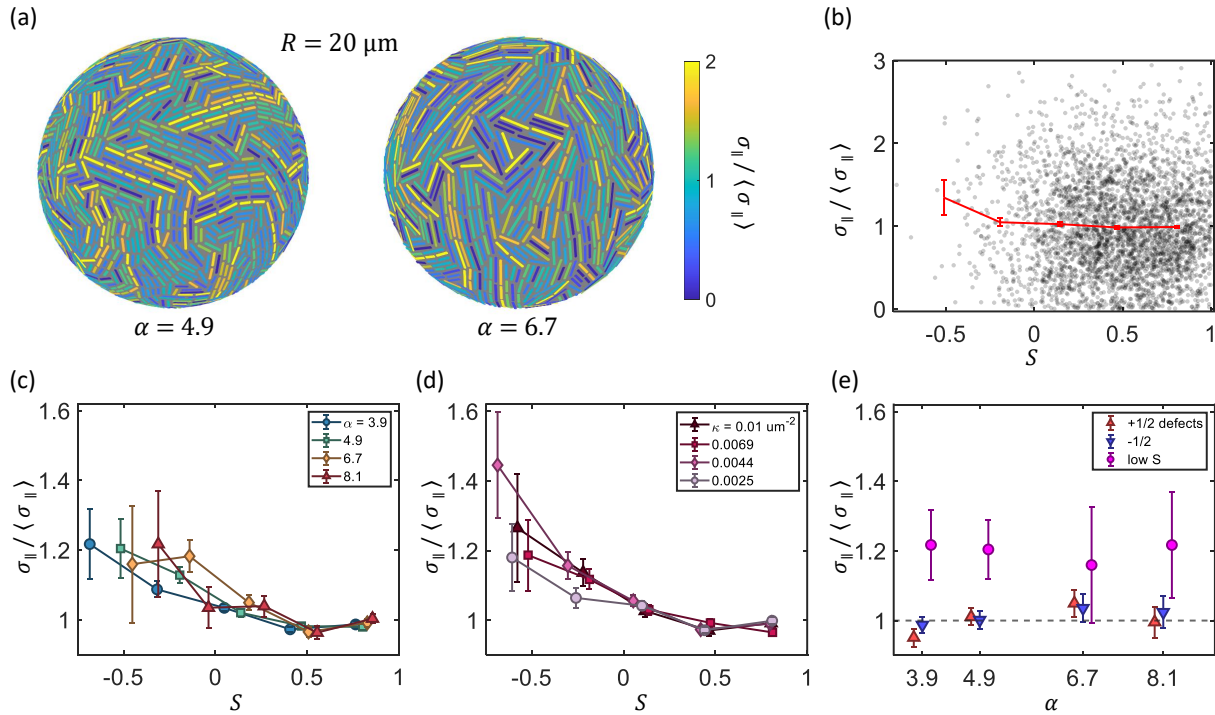


FIG. 4. Parallel component of the Virial stress σ_{\parallel} in growing cell monolayers on curved surfaces. (a) Visualization of the normalized parallel stress in cell monolayers on a curved surface with $R = 15 \mu\text{m}$ and for cell aspect ratios of $\alpha = 4.9$ and 6.7 . (b) Scatter plot of the normalized parallel stress of individual cells and their local orientational order for the case of $R = 20 \mu\text{m}$ and $\alpha = 4.9$. The trendline shows the data binned by orientation order. (c) Relation between the normalized parallel stress magnitude and the orientational order for differing aspect ratios. Average parallel stress magnitude increases by up to 20% in the most negative order bin. (d) Relation between the parallel stress magnitude and the orientational order for differing surface curvatures. (e) Deviation from mean parallel stress at topological defects ($+1/2$ in red, $-1/2$ in blue) and in the most negative order regions (in magenta). Negative-order regions have a greater deviation from the mean stress than topological defects for all curvatures and aspect ratios. All error bars show standard error.

264 A scatter plot of the normalized parallel component of Virial stress and the orientational
 265 order for a representative simulation ($R = 20$, $\alpha = 4.9$) is shown in Fig. 4(b), grey points.
 266 It is evident that, at the individual cell level, stress values can vary over a wide range with
 267 respect to the average value of stress. No trend is immediately visible in the scattered data,
 268 however, binning the data by the orientational order S reveals a relationship between the

269 normalized stress $\sigma_{\parallel}/\langle\sigma_{\parallel}\rangle$ and orientational order S . First, five evenly spaced bins were
 270 determined by identifying the minimum S_{min} and maximum S_{max} values of the orientational
 271 order for each simulation. Then, the mean orientational order and mean parallel stress were
 272 computed for each bin. The result is shown in Fig. 4(b), red line. For this example ($R = 20$,
 273 $\alpha = 4.9$), the binned data shows that cells in regions of most negative order experience
 274 a slightly higher magnitude of parallel stress compared to cells in high-order regions. The
 275 average order at each aspect ratio and curvature is shown in supplementary information Fig.
 276 S6(c,f).

277 This trend appears much more robustly in data aggregated across multiple simulations
 278 with the same cell aspect ratio or surface curvature. Plots of normalized parallel stress
 279 binned by order and averaged across all simulations with the same aspect ratio or curvature
 280 are shown in Fig. 4(c) and 4(d), respectively. For all cases, the average normalized stress
 281 decreases with increasing orientational order. Specifically, in regions of high orientational
 282 order ($S > 0.5$), the local average of normalized stress approaches unity, or $\sigma_{\parallel} \approx \langle\sigma_{\parallel}\rangle$. In
 283 regions of negative orientational order, however, the local average of normalized stress is
 284 15% to 22% larger than the global average stress, or $\sigma_{\parallel} \geq 1.15\langle\sigma_{\parallel}\rangle$. The same analysis was
 285 also performed for the perpendicular component of stress and no consistent relation was
 286 observed in this case, shown in supplementary information Fig. S7.

287 The stress in other active nematics, such as those composed of epithelial cells, is higher
 288 near $+1/2$ topological defects, which themselves are low-order regions by definition [16].
 289 To investigate whether this effect was responsible for the correlation of high stress and low
 290 order in bacterial monolayers, stress near topological defects was compared to the previously
 291 calculated stress in the most negative order regions ($S < 0.1$). The mean value of the
 292 parallel component of the Virial stress (σ_{\parallel}) was computed for all cells within close proximity
 293 ($r = l_0/2$) of a $\pm 1/2$ topological defect within the monolayer. Then, this value was compared
 294 to the average normalized parallel stress of the bin with the lowest orientational order and
 295 is shown in Fig. 4(e). For all cases, the average deviation from the mean stress near $\pm 1/2$
 296 defects is less than 5%, or $\sigma_{\parallel} \leq 1.05\langle\sigma_{\parallel}\rangle$. The average order in the same regions near these
 297 defects is between $0.2 < S < 0.5$, shown in the supplementary information Fig. S8. In
 298 contrast, the average deviation from the mean stress in regions of negative orientational
 299 order is always greater than 15%, or $\sigma_{\parallel} \geq 1.15\langle\sigma_{\parallel}\rangle$, for all cell aspect ratios and substrate
 300 curvatures. This shows that the observed high stress-low order correlation in this system is

301 not caused by stress concentration near topological defects, and is instead a distinct effect.

302 IV. DISCUSSION

303 Previous work on monolayers of growing hard-rod cells has shown that, in the case of
304 a solid-liquid growth substrate, the overdamped Hertzian model described here accurately
305 models the system [2]. We have shown through comparisons of simulations and experiments
306 that this model can be extended to a liquid-liquid interface. To do this, we modeled the
307 surface tension forces fixing cells to the interface with the constraint that cells lie with
308 their center on the interface and their orientation parallel to the local tangent plane. This
309 constraint matches behavior seen in experiments on cells adsorbed at liquid-liquid interfaces,
310 both in this work (i.e. shown in Fig. 1(a)) and elsewhere [26]. The liquid-liquid extension
311 holds as long as the curvature is small compared to the cell length, so the interface is locally
312 flat, and the packing fraction is small enough to prevent inter-cell forces from affecting the
313 interface shape. Deformations of the interface occur after the point of complete interface
314 coverage [25, 26]. The equations of motion in the liquid-liquid version remain overdamped
315 because of the hydrodynamic drag on the nonmotile cells.

316 Application of this model to flat monolayers has shown that microdomain size increases
317 with increasing cell aspect ratio [2]. Our work is consistent with this result, and further con-
318 firms that the trend holds for monolayers growing on curved surfaces as well. Additionally,
319 while previous work demonstrated the relation between microdomain size and aspect ratio
320 for an unconfined growing colony [2], our results show that the same relation is true for a
321 growing colony confined to a finite substrate area, such as the surface of a sphere. Together,
322 these show that microdomain formation and its dependence on cell aspect ratio are robust
323 collective behaviors in growing hard-rod monolayers under a variety of conditions.

324 We find a new dependence of microdomain area on the curvature of the surface. Re-
325 gardless of cell aspect ratio, higher curvature substrates resulted in smaller microdomains.
326 This decrease in alignment is attributable to the structure of microdomains, which consist
327 primarily of near-parallel lines of cells spaced one cell width apart in both flat [2] and curved
328 systems. The “straightest” lines possible on the surface of a sphere are great circles, which
329 cannot lie parallel to each other. Thus, as domain size increases, the lines of cells must
330 either converge or bend, deviating from the great circle. In either case, this prevents the

331 microdomain from forming a fully parallel crystalline structure, decreasing its stability and
332 leading to fracture. On more curved surfaces these lines of cells diverge at shorter length
333 scales, leading to lower average microdomain sizes, while less curved surfaces will eventually
334 limit to the flat case in which microdomain size is limited only by growth-powered activity
335 [2]. With the growth rate and range of curvatures simulated here, both activity and curva-
336 ture play a role in inhibiting microdomain size with neither effect dominating, and therefore
337 microdomain size does not exhibit a straightforward dependence on curvature. Such depen-
338 dence could be investigated by simulating higher-curvature surfaces or much lower growth
339 rates.

340 We also find that the extensile (parallel) stress of the monolayer has the highest magnitude
341 in cells with negative local order. This is a contrast to previous simulations of bacteria
342 growing in a channel with outlets on the ends, where stress could be released as cells exited
343 the system [28]. In these systems, lower-order regions were found to have lower stress, the
344 opposite of our findings. The likely source of this difference is the fact that our system has
345 no way to reduce total stress other than the reorientation of cells to more efficient packing.

346 More recent simulations of a similar setup have produced a model for stress distribution in
347 highly-aligned columns of cells, where the parallel and perpendicular components of stress
348 decouple [31]. While our system is much more confined, the columnar model still sheds
349 light on the stress behavior of high-order cells in microdomains compared to that of low-
350 order cells. Columns of high-order cells compressed at both ends can distribute extensional
351 stress evenly throughout the column, while disordered cells have no way to distribute their
352 stress without reorganizing their local geometry. This could lead to greater stress buildup
353 in individual disordered cells.

354 Our results are robust for a range of packing fractions. While the results presented here
355 are specifically for $\phi = 1.05$, the same analysis addressing the curvature-microdomain area
356 and order-stress relationships for $\phi = 1.1$ can be found in the supplementary information
357 Fig. S9 and Fig. S10, respectively. This analysis shows that both relations persist in the
358 same form at the higher packing fraction. For packing fractions $\phi < 1.05$, the surface is not
359 homogeneously covered, and we would expect results to differ significantly.

360 In a continuous (non-granular) active nematic composed of flexible epithelial cells, exten-
361 sile stress is highest at positively charged topological defects [16]. These stress concentrations
362 cause the cell layer to deform at these points, producing mounds localized near the defects

363 [16]. Similar deformations are seen in other continuous active nematics at deformable 2D in-
364 terfaces, such as microtubules on the surface of a vesicle or actin fibers in the morphogenesis
365 of multicellular organisms [32, 33], and this behavior has been further confirmed and studied
366 in numerous simulations and theoretical works [34–39]. In a granular active nematic, our
367 simulations show that extensile stress concentrates at all negative-order cells rather than
368 at the locations of point $+1/2$ topological defects, likely because the non-continuous nature
369 of the director field decreases the robustness of defect definitions. This can be expected to
370 result in different forms of deformation under growth stress. In fact, comparable deforma-
371 tions have been imaged in systems of *A. borkumensis* growing on the surface of oil droplets
372 in water [25, 26]. As confocal images in these experiments show that cells maintain the
373 same surface attachment during deformations, a similar simulation setup to ours in which
374 the interface’s shape is allowed to change and respond to cell growth and forces could be an
375 effective way to model these deformations.

376 Our results are relevant for systems of bacteria growing at liquid-liquid interfaces, such
377 as at the oil-water interface of a droplet. For example, previous work has shown that cell
378 growth confined to the surface of a droplet produces tube-like protrusions similar to those
379 produced by continuous active nematics [25, 26]. However, a complete theoretical descrip-
380 tion of droplet deformation by cell growth is still lacking. Our results suggest that these
381 protrusions should nucleate at lower-order sites such as boundaries between microdomains,
382 rather than nucleating exclusively at $+1/2$ defects. By extension, this allows us to predict
383 how interfacial curvature influences deformations due to the underlying microstructure. For
384 example, higher curvature (small radii) droplets will produce more closely spaced protrusions
385 since the characteristic size of their microdomains decreases.

386 Our results also emphasize the importance of constituent particle properties on collective
387 behavior.

388 While a hard-rod monolayer exhibits many of the same properties as a nematic composed
389 of microtubules or other flexible components [11], it produces microdomains that are dis-
390 tinct from the continuous alignment fields of other active nematic systems. Furthermore,
391 its internal forces are not well predicted by topological defects, which are themselves less
392 robustly defined due to the non-continuous alignment field. Other fundamental differences
393 between granular and continuous nematics in more highly aligned systems have recently been
394 discovered as well [31]. The partially granular nature of a bacterial monolayer is clearly of

395 great importance to understanding its collective behavior.

396 In conclusion, we have shown that stress distributions in a hard-rod bacterial monolayer
397 vary predictably based on cell aspect ratio and substrate curvature. Specifically, our simu-
398 lations show that stress in a hard-rod monolayer concentrates in negative-order cells, which
399 occur at the boundaries of microdomains. The length scale of these microdomains increases
400 with cell aspect ratio and decreases with substrate curvature. These results demonstrate
401 that while a bacterial monolayer can be effectively modeled as a continuum active nematic,
402 in some cases when its cells act as hard rods, the alignment and stress distributions behave
403 in distinctly different ways.

404 V. AUTHOR CONTRIBUTIONS

405 **Blake Langeslay:** Conceptualization, Methodology, Software, Investigation, Formal
406 analysis, Visualization, Writing - original draft, Writing - review and editing. **Gabriel**
407 **Juarez:** Conceptualization, Methodology, Supervision, Writing - original draft, Writing -
408 review and editing.

409 VI. CONFLICTS OF INTEREST

410 There are no conflicts of interest to declare.

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