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## Superior effect of edge relative to basal plane functionalization of graphene in enhancing polymer-graphene nanocomposite thermal conductivity – A combined molecular dynamics and Green's functions study

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## **ABSTRACT:**

To achieve high thermal conductivity (k) polymer graphene nanocomposites, it is critically important to achieve efficient thermal coupling between graphene and surrounding polymer matrix through effective functionalization schemes. In this work, we demonstrate that edgefunctionalization of graphene nanoplatelets (GnPs) can enable a larger enhancement of effective thermal conductivity in polymer-graphene nanocomposites, relative to basal plane functionalization. Effective thermal conductivity for edge case is predicted, through molecular dynamics simulations, to be up to 48% higher relative to basal plane bonding for 35 weight% graphene loading with 10 layers thick nanoplatelets. The beneficial effect of edge bonding is related to the anisotropy of thermal transport in graphene, involving very high in-plane thermal conductivity (~2000 W/mK) compared to the low out-of-plane thermal conductivity (~10 W/mK). Likewise, in multilayer graphene nanoplatelet (GnP), the thermal conductivity across the layers is even lower due to the weak van der Waals bonding between each pair of layers. Edge functionalization couples the polymer chains to the high in-plane thermal conduction pathway of graphene, thus leading to high overall high composite thermal conductivity. Basal-plane functionalization, however, lowers the thermal resistance between the polymer and the surface graphene sheets of the nanoplatelet only, causing the heat conduction through inner layers to be less efficient, thus resulting in basal plane scheme to be outperformed by edge scheme. The present study enables fundamentally novel pathways for achieving high thermal-conductivity polymer composites.

**KEYWORDS:** graphene, functionalization, polymer nanocomposites, thermal conductivity, interface

## **1. INTRODUCTION**

High thermal conductivity (k) polymer materials can improve thermal management in a wide range of applications such as automotive control units<sup>1</sup>, batteries<sup>2-4</sup>, solar panels<sup>5</sup>, electronic packaging<sup>6</sup> and electronic cooling<sup>7</sup> etc... A promising approach to enhance thermal conductivity of polymers is molecular orientation<sup>8-10</sup>, addition of high k fillers<sup>11-17</sup> to improve its overall thermal conductivity of polymer nanocomposites. However, benefits of adding high k fillers is limited due to the large interface thermal resistance between polymer and fillers in the range of  $10^{-8}$  to  $10^{-7}$ m<sup>2</sup> KW<sup>-1</sup> <sup>18,19</sup> due to phonon mismatch between these two. To improve interface thermal conductance, graphene is chemically functionalized by groups that are compatible with the surrounding polymer<sup>21</sup>. To achieve highest thermal conductivities possible, it is critically important to understand the optimal functionalization schemes. In particular, the difference in location of functional groups (such as edge versus basal plane) can lead to significant differences in thermal conductivity enhancement. Recent work demonstrated that multilayer graphene is more efficient at enhancing thermal conductivity than single layer graphene<sup>20</sup>. For such multilayer graphene, the anisotropy in thermal conductivity can be even larger, due to weak van der Walls coupling of graphene sheets in the through-plane direction, further modifying the difference between edge basal plane functionalization. In this work we demonstrate that functionalization on the edges can lead to significantly higher effective polymer nanocomposite thermal conductivity compared to functionalization on the basal plane. Detailed understanding of the effect is achieved through molecular dynamics as well as first-principles simulations based on density-functional theory. Presented results unravel promising new avenues for achieving high thermal conductivity polymer-graphene nanocomposites.

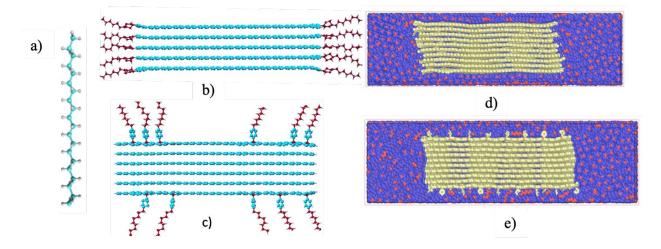
The benefit of edge-bonding is found to be related to enabling all graphene sheets to be covalently bonded to surrounding polymer chains, as the edges of all sheets are exposed to surrounding polymer (Fig. 1a) High in-plane thermal conductivity of individual sheets (~2000 W/mK)<sup>11,12</sup> combined with their efficient coupling with the surrounding polymer through edge functionalization leads to efficient thermal conduction pathway across the GnPs (Fig. 1a). Since all sheets are efficiently coupled with polymer through edge bonding, the entire nanoplatelet is

efficient in conducting heat through edge functionalization (Fig. 1a). For basal plane bonding, however, a higher density of functional groups can be expected to attach to the basal planes of the outermost layers of the nanoplatelet (Fig. 1b). The weak van der Waals coupling of outer layers with inner layers, then renders the inner layers to be less efficient in heat transfer due to poor through-thickness thermal conductivity of graphene ( $\sim 10 \text{ W/mK}$ )<sup>19,21</sup> (Fig. 1b). The lower heat transfer capability of inner layers for basal plane bonding, can cause the overall nanoplatelet heat conduction to be lower for basal plane bonding, relative to edge bonding.

Several studies have reported enhancement of thermal conductivity through functionalization schemes. Two orders of magnitude increase in interface thermal conductance<sup>22</sup> and 156% enhancement<sup>23</sup> in composite thermal conductivity were achieved through grafting of polymer chains on to graphene. Theoretical studies on polymer grafted graphene showed two-fold higher interfacial thermal conductance through functional groups<sup>22</sup>. Similarly pyrene-end poly(glycidyl methacrylate) functionalized graphene/epoxy composite achieved ~184% enhancement in k due to noncovalent functionalization<sup>23</sup>. Konatham et al.<sup>24</sup> demonstrated ~50% reduction in the interfacial thermal resistance between octane and functionalized graphene using molecular dynamics (MD) simulations study. Lin *et al.*<sup>25</sup> explored the enhancement of out-of plane thermal conductance of graphene facilitated by functional group of alkyl-pyrene on graphene via MD simulations. According to Ganguli et al.<sup>26</sup> silane-functionalized graphene improved the thermal conductivity by 50% compared to pristine graphene composite for 8% filler content. Xiang *et al.*<sup>27</sup> also compared edge versus basal plane functionalization of graphene for energy conversion and energy storage applications. However, there is a lack of detailed understanding of the relative effectiveness of edge versus basal plane functionalization in enhancing thermal conductivity of polymer-graphene nanocomposites. In particular, the role of different parameters such as nanoplatelet thickness, functional group density and functional group length in modifying the relative effectiveness of edge and basal plane functionalization is not well understood.

This study addresses the relative role of edge and basal plane functionalization in enhancing thermal conductivity through molecular dynamics simulations and first principles driven atomistic Green's function methods. Computational studies are also performed to understand the beneficial effects of edge bonding on - (a) thermal conductivity of individual graphene sheets (using MD simulations); (b) interface thermal conductance at individual junctions between graphene and polymer (performed using first principles driven atomistic Green's function method); and (c) damping of vibrations in the outer layers of a graphene nanoplatelet.

## **2. METHODS**



## 2.1 Molecular Dynamics Simulations

Fig. 1a) Polyethylene chain, b) and c) Edge and basal-plane functionalized graphene nanoplatelet, d) and e) Edge and basal plane functionalized graphene nanoplate embedded in polyethylene.

Molecular dynamics simulations were performed using LAMMPS package<sup>28</sup>. Interatomic force interactions between various atomic species were modeled using COMPASS force-field<sup>29</sup>. This force field has been widely used in the past to simulate polymer systems<sup>29</sup>. Polymer used for computational studies is polyethylene (PE). To compare edge and basal plane case computationally, we first functionalized the graphene nanoplatelet separately on its edges and basal plane to achieve edge (Fig. 1b) and basal plane functionalized (Fig. 1c) nanoplatelet. These functionalized nanoplatelets were then embedded into the polyethylene matrix (using PACKMOL package<sup>30</sup>) to yield edge functionalized (Fig. 1d) and basal plane functionalized (Fig. 1e) polyethylene-graphene nanocomposites. The lateral dimension of the GnP used for simulations was 10 nm x 10 nm while its thickness was varied from 4 to 10 layers. The polymer-graphene composite was prepared with a graphene nanoplatelet concentration of 35 weight%. The chain length of polyethylene used was 120 Carbon atoms. The system was relaxed using NPT ensemble (constant number of particles, pressure and temperature) to achieve an equilibrium configuration.

Simulations were performed at 300 K. A temperature difference of 50 K was imposed across the composite (using Langevin thermostats<sup>31</sup>) and simulations were performed until steady state was reached (typically after 5 ns). Upon reaching steady state the resulting heat flux was computed and compared for edge and basal plane functionalization cases. To validate our models, we simulated the thermal conductivity of pure polyethylene with a density of 0.898 gcm<sup>-3</sup> and obtained a value of 0.3 W/mK at 300 K which is in good agreement with simulations<sup>9,17,32,33</sup> and experimental results<sup>34,35</sup>.

#### 2.2 Atomistic Green's Function (AGF) Method

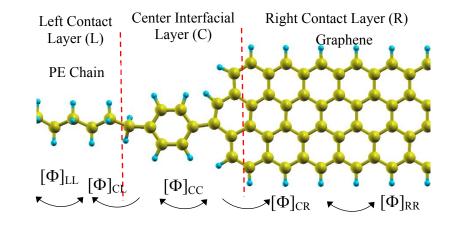
To compare interface thermal conductance for a junction (between functional group and graphene) located on edge versus basal plane, we used first-principles atomistic Green's function (AGF)<sup>36,37</sup>. The method offers several unique advantages for computation of interface conductance such as allowing use of accurate interatomic force interactions derived from density-functional theory as well as use of exact interfacial atomic arrangement. The method further enables detailed microscopic understanding of interfacial thermal transport in terms of transmission of individual phonon modes across the junction. For AGF calculations, system is divided into left contact lead, central interface region and right contact lead. In this work, left lead was comprised of polyethylene chain, right lead was graphene nanoribbon and central region was comprised of the junction between polymer and graphene (Fig. 2). Phonon interface thermal conductance is computed using Landauer formalism<sup>38</sup> from the estimate of phonon transmission rates. For this work, second-order interatomic force constants needed for the computation of phonon transmission were derived ab initio using open source DFT package QUANTUM-ESPRESSO<sup>39</sup>. Green's functions provide response of the system under a small perturbation and allow computation of phonon transmission across the interfacial region. Under harmonic approximation, the Green's function G—corresponding to the interfacial region—can be calculated as<sup>40</sup>,  $G_{d,d} =$  $[\omega^2 I - H_{d,d} - \Sigma_R - \Sigma_L]^{-1}$ , where  $\omega$  is the phonon frequency,  $H_{d,d}$  represents the dynamical matrix of the interfacial region, and  $\Sigma_L$  and  $\Sigma_R$  are the self-energies of the left and right reservoirs which represent the effect of contact reservoirs on the interfacial region. Total phonon transmission across the interfacial region can be calculated as  $\Xi(\omega) = Trace[\Gamma_L G_{d,d} \Gamma_R G_{d,d}^+]$  where  $\Gamma_R$  and  $\Gamma_L$ describe the rate at which phonons enter and exit the right and left contact leads respectively,  $\Gamma_L = i$ 

 $[\Sigma_L - \Sigma_L^+]$ ,  $\Gamma_R = i[\Sigma_R - \Sigma_R^+]$ , and '+' denotes the conjugate transpose of the matrix. The interface thermal conductance can then be calculated with Landauer formalism using the total phonon transmission,

$$J = \int \left(\frac{\hbar\omega}{2\pi}\right) \Xi(\omega) \frac{dN(\omega)}{dT} d\omega$$

where  $N(\omega)$  and T are the Bose-Einstein population and temperature respectively.

Harmonic interatomic force constant (IFC) matrices  $[\phi]$ (as shown in Fig. 2) and the masses of atoms in the various layers are the only inputs needed to compute the various quantities involved in calculation of thermal conductance. The harmonic force constant



**Fig. 2:** Atomic configuration for atomistic Green's function calculation of interfacial thermal conductance.

matrix  $[\Phi_{ij}]_{\alpha\beta}$ , between two regions  $\alpha$  and  $\beta$  ( $\alpha$ ,  $\beta$ = L, R or C) is comprised of the interatomic force interaction  $\Phi_{ij}$  between any atom *i* in region  $\alpha$  and another atom *j* in region  $\beta$ . These force constants  $\Phi_{ij}$  are the second derivatives of energy with respect to the displacements of atoms *i* and *j*. In this work these IFCs are derived accurately from density-functional theory (DFT) using perturbation theory<sup>39</sup>. Use of DFT has been shown to yield very accurate IFCs in prior works<sup>41</sup>. In our calculations, the right contact layer is the graphene nanoribbon and the left contact layer is a single chain of polyethylene while the center layer consists of the interfacial junction.

We first used DFT to optimize the structures of the polyethylene chain and graphene nanoribbon (ZGNR) as seen in Fig. 2. Electronic structure of PE is computed using a  $10 \times 1 \times 1$  Monkhorst-Pack k-grid and local density approximation is used for the exchange correlation. The width of the ZGNR is taken to be 4 zigzag chains across the nanoribbon (4-ZGNR). The edges of the ZGNR are passivated with hydrogen in this study. For computing the electronic structure of 4-

ZGNR, the unit cell of ZGNR was relaxed and 30 k points along the 1-D direction of the Brillouin zone were used for DFT calculations. Phonons of both PE and ZGNR are computed on a  $12 \times 1 \times 1$  q-grid, using the DFPT package; these are then used to obtain the interatomic force constants (IFCs) in real space. The IFCs derived for a single PE chain and 4-ZGNR are used for the left and right contacts, respectively. The IFCs within the interfacial region and between the interfacial region and the left and right contacts are derived by using a finite-difference approach. To compute the IFC between an interfacial atom and any other atom in the system through this approach, the interfacial atom is displaced by a small amount. The force on the other atom resulting from this displacement is computed. The IFC is taken to be the negative of the derivative of the force on the particular atom in the system with respect to the displacement of the interfacial atom. The calculation of IFCs related to the interfacial region is discussed next. Ultrasoft pseudopotentials were used for deriving the configurations. An energy cutoff of 60 Ry was used for wavefunctions and that of 480 Ry was used for charge density.

To understand differences in phonon transmission for edge and basal plane case, we used polarization dependent AGF method. Through this approach, the contributions of individual polarizations of graphene and polyethylene to overall transmission can be analyzed<sup>42</sup>. To achieve such decomposition, it should be noted that matrices  $\Gamma_L$  and  $\Gamma_R$  can be written as  $\Gamma_L = \phi_{LC}A_L\phi_{CL}$ and  $\Gamma_R = \phi_{RC}A_R\phi_{CR}$ , where  $\phi$  are the force interaction matrices as discussed earlier. In these expressions matrix A is proportional to phonon density of states and can be written in terms of its eigenvectors and eigenvalues as<sup>42</sup>  $A = \sum_i \lambda_i e_i e_i^+$ , where  $\lambda_i$  and  $e_i$  are the eignevalues and eignevectors of matrix A respectively<sup>42</sup>. Above decomposition of matrix A allows  $\Gamma_L$  and  $\Gamma_R$  to be replaced with polarization dependent phonon escape rates defined as  $\gamma_L = \phi_{LC}\lambda_{L,i}e_{L,i}e_{L,i}^+\phi_{CL}$ ,  $\gamma_R$  $= \phi_{RC}\lambda_{R,i}e_{R,i}e_{R,i}e_{R,i}\phi_{CR}$ . This allows phonon transmission from left into specific phonon polarizations on the right to be written as  $\xi(\omega) = Trace[\Gamma_L G_{d,d}\gamma_R G_{d,d}^+]$ . In this work, we take the phonon escape rates for out-of-plane and in-plane vibration modes in the right contact to be

$$\gamma_{R}^{out \ (in)} = \phi_{RC} \bigg[ \sum_{i,i \in out \ (in)} \lambda_{R,i} e_{R,i} e_{R,i}^{+} \bigg] \phi_{CR}$$

The transmission from polymer in to the out-of-plane and in-plane vibration modes in graphene can then be computed as  $\xi^{out}(\omega) = Trace[\Gamma_L G_{d,d} \gamma_R^{out} G_{d,d}^+]$  and  $\xi^{in}(\omega) = Trace[\Gamma_L G_{d,d} \gamma_R^{in} G_{d,d}^+]$ .

## **3. RESULTS AND DISCUSSION**

# 3.1 Molecular Dynamics Simulations

The heat flux through the composite (for both edge and basal plane cases) was calculated from the

slope of the "energy exchange versus time" graph using the equation,  $J=\Delta E/(A.\Delta t)$ , where  $\Delta E$  is

the change in energy, A is the cross-sectional area and  $\Delta t$  is the time over which  $\Delta E$  is computed.

These calculations were performed using the linear portion of the graph (which corresponds to

steady state). Energy exchange ( $\Delta E$ ) with time is shown in Fig 3a for composites prepared with

edge functionalized (EFGNP) and basal-plane functionalized (BFGNP) graphene nanoplatelet.

Results of heat flux computation show a significant increase of nearly 48% for heat flux for the

EFGNP/PE nanocomposite case over the BFGNP/PE nanocomposite case for the 10 layers thick

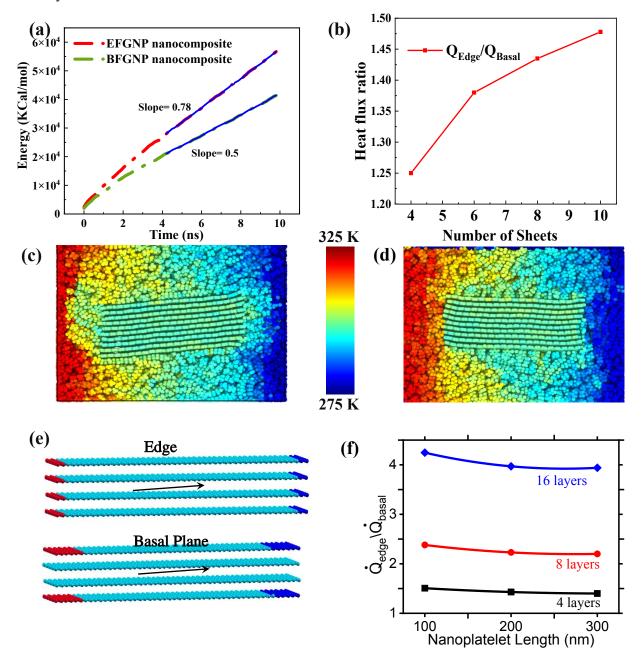
nanoplatelet (Fig. 3b). The enhancement in heat flux is found to be thickness dependent (Fig. 3b),

with thicker nanoplatelets demonstrating larger advantage of edge relative to basal plane

functionalized cases. While for 4 sheets thick nanoplatelet, EFGNP/PE composite has 25% higher

heat flux compared to BFGNP/PE composite, increasing the sheet thickness to 10 layers, increases

the difference in heat flux to 48%. These data provide first computational understanding of the superior effect of edge-bonding in enhancing polymer-graphene nanocomposite thermal conductivity.



**Figure 3.** (a) Energy transfer vs time for edge and basal plane functionalized nanocomposites and (b) heat flux ratio for edge vs basal functionalized nanocomposite as function of nanoplatelet thickness, (c) EFGNP/PE and (d) BFGNP/PE nanocomposites. (e) Temperature boundary conditions to simulate heat flux through single nanoplatelet for edge and basal plane functionalization (arrows show direction of heat flow) (f) Heat flux ratio of different length of nanoplatelet shows higher heat flux for edge bonding.

This higher heat flux is mainly due to all layers of graphene nanoplatelet being efficiently coupled to polymer matrix leading to lower interfacial thermal resistance for edge bonding case (Fig. 1b). For basal plane case, however, only the outermost layers are the dominant heat conductors, as they are covalently bonded with the surrounding polymer (Fig. 1c). For this case, inner layers interact with the outer layers through weak van der Waals forces, diminishing heat transfer from outer to inner layers, thus diminishing the contribution of inner layers to overall heat transfer for basal plane case. This degrades the heat transfer performance for basal plane functionalized graphene nanoplatelet. These differences in heat transfer reflect in the temperature profiles across the nanocomposite for the two cases; for the edge case, temperature profile is significantly smoother at the interface (at the edge) between graphene and polymer (Fig. 3c), relative to basal plane case (Fig. 3d), where a sudden temperature jump is seen across the nanoplatelet edge. This indicates a smaller interface thermal resistance for edge functionalization case, resulting in higher effective thermal conductivity.

While above simulations study the entire nanocomposite, we also performed simulations for single nanoplatelet (Figs. 3e and 3f) to demonstrate the effect more clearly. Fig. 3e shows single graphene nanoplatelet with the thermostats applied across either the edges of the entire nanoplatelet (to simulate edge bonding) or across only the outermost layers (to simulate basal plane bonding). These thermostats establish a temperature gradient of 50 K. Fig. 3f shows comparison

of heat transfer rate between edge and basal plane case. Edge case is seen to outperform basal plane case as seen by the ratio (  $\dot{Q}_{edge}/\dot{Q}_{basal}$ ) being greater than 1. It is further seen that the advantage of edge bonding (indicated by the heat transfer rate ratio) increases with increasing number of layers (*n*) within the nanoplatelet. While for a 4-layer thick nanoplatelet, the heat transfer rate ratio is ~1.5, this ratio increases sharply to more than 4 for

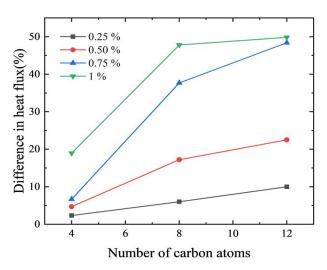


Figure 4: Effect of grafting density and number of backbone carbon atoms in the functionalized chain, on difference in heat flux between edge and basal plane functionalized composites.

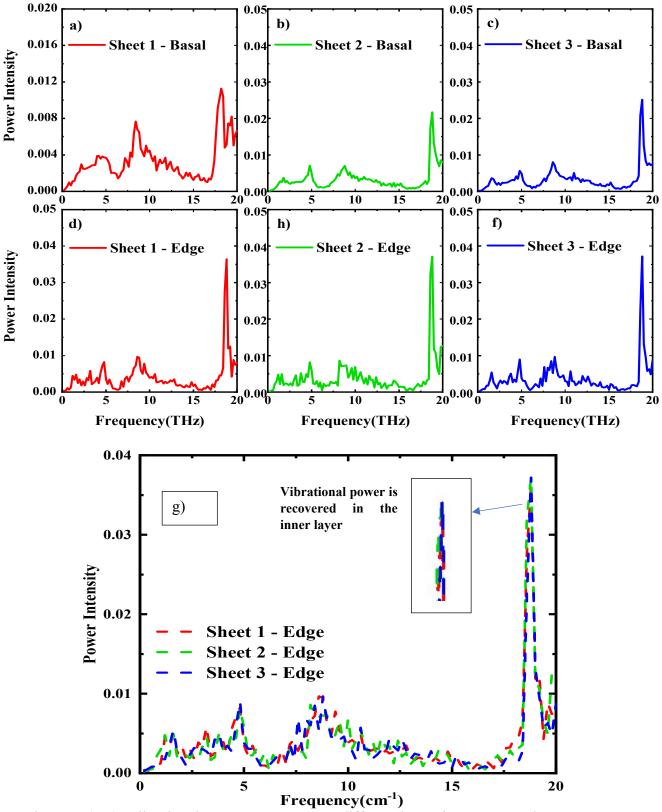


Figure 5. (a-g): Vibrational power spectra across different layers in EFGNP and BFGNP.

a 16-layer thick nanoplatelet. The increase in difference between edge and basal plane functionalized case with increase in n can be understood by realizing that for the basal plane functionalized nanoplatelet, increasing the number of inner layers does not result in significant increase in overall heat transfer rate, since inner layers do not conduct heat efficiently due to being poorly coupled with outermost layers (which receive heat through functionalization). For edge case, however, since all layers conduct heat efficiently, increase in n leads to a proportional increase in overall heat transfer. This causes the ratio of heat transfer for edge and basal plane functionalization to increase with number of graphene sheets. This also explains the increase in heat flux ratio for edge and basal plane cases with increase in thickness for the nanocomposite (Fig. 3b). Fig. 4 shows the effect of grafting density (0.25% - 1%) and number of backbone carbon atoms in the functionalized chain on thermal conductivity enhancement of the nanocomposite. It is observed that, the difference in heat flux increases with increase in both grafting density and number of carbon atoms and saturates at 1%, in good agreement with previous works<sup>43,44</sup>. At high higher number of backbone carbon atoms, functionalized molecules bend and fold, increasing the interface thermal resistance<sup>44</sup>. Hence, we observed a maximum difference in heat flux of 48% at 1% grafting density and with 12 backbone carbon atoms.

While above results demonstrate the advantage of edge bonding in enhancing thermal conductivity through the coupling effect of all graphene layers to polymer, we next present other advantages of edge bonding, namely, a) lower damping of vibrations in graphene layers by surrounding polymer for edge bonding case, b) higher thermal conductivity of individual edge-functionalized graphene sheets (studied using MD), c) higher interface thermal conductance at an individual junction between polymer and graphene on the edge compared to basal plane (studied using first-principles atomistic Green's function analysis).

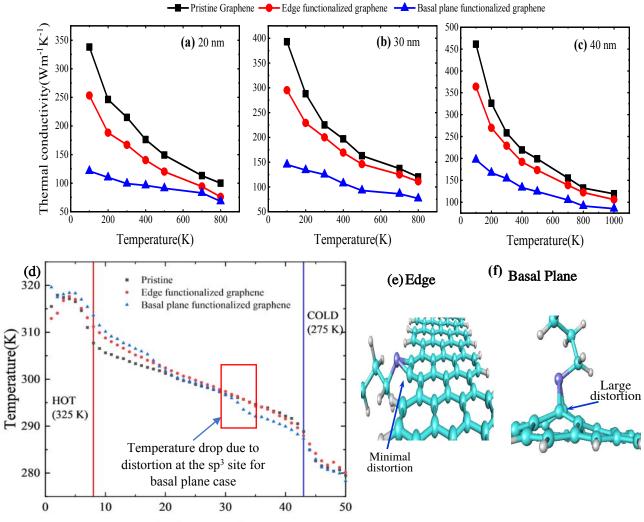
We first discuss effect of edge bonding on damping of vibrations within graphene sheets. Vibrational power density spectrum<sup>18</sup> is a powerful method to study damping of vibrations in graphene sheets and is computed from the discrete Fourier transform of the velocity autocorrelation function as shown below,

$$D(\omega) = \int_0^\tau \langle v(0).v(t) \rangle \exp((-i\omega t)dt \quad (1)$$

where  $\langle v(0).v(t) \rangle$  is the velocity autocorrelation obtained by correlating the velocity at every 2 fs time interval,  $\tau$  is the total correlation time = 5 ps and  $D(\omega)$  is the phonon vibrational power spectra at frequency  $\omega$ .

Figs 5a-g shows the difference in vibrational power spectra for edge and basal plane functionalization cases for a 6 sheet nanoplatelet (embedded in the polymer matrix). The power spectra are presented for individual sheets within the nanoplatelet. Sheet 1 denotes the outermost layer from bottom. We have shown the vibrational power spectra of sheets 1-3. We focus on vibrational power density at a frequency of around 18 THz<sup>45</sup>. Comparing Fig. 5a and d, it is seen that vibrational power in Sheet 1 (outermost sheet) is lower in BFGNP than EFGNP by almost a factor of 3.5. This stronger damping of vibrations in outermost sheet for BFGNP case is caused by strong covalent-bond mediated interaction between outer sheet and polymer for BFGNP case, in contrast to the case of edge bonding where the interactions are much weaker caused by van der Walls forces.

Vibrational power for inner sheets is also higher for edge case compared to basal plane functionalization. The inner layers for edge case do not have a large contact area with the



Bins(Angstrom)

**Figure 6.** Temperature dependence of thermal conductivity for pristine, edge functionalized and basal plane functionalized graphene with lateral dimensions of (a) 20 nm, (b) 30 nm, and (c) 40 nm (d) Temperature distribution along the simulation box in pristine, edge, and basal plane functionalized graphene. Relaxed atomic configurations for (e) edge and (f) basal plane functionalization demonstrates larger distortion of graphene for basal plane functionalization.

surrounding polymers (only interact through edges) and therefore are less damped compared to outer sheet, causing a small increase in their power density (see inset in Fig. 5g) relative to outer sheet. The inner sheets for edge case at the same time receive heat from edges through strong covalent bonds. For basal plane case, however, vibrational power for inner sheets stays lower relative to edge case. This is simply due to the weak van der Waals interaction of inner layer with

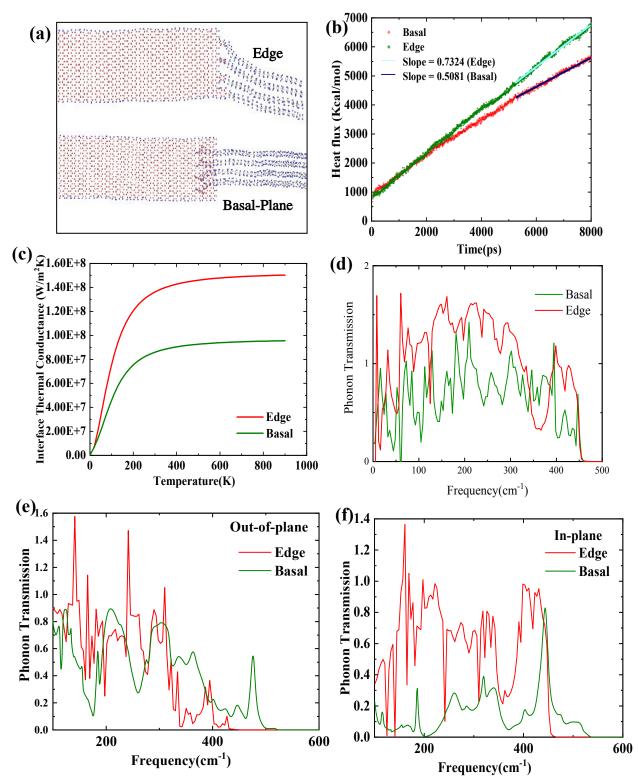
the outer layer for basal plane case which causes poor heat transfer to the inner layers for basal plane case. Above comparison of vibrational power density spectrum highlights the significant advantages of edge bonding for heat conduction.

We next compare the effect of edge and basal plane bonding on thermal conductivity of individual graphene sheets. Edge-bonding is found to enable remarkably superior thermal conductivity of individual graphene sheets relative to basal plane functionalization (Fig. 6). For pristine graphene case, k at nanometer length scales is found to be in good agreement with previous works<sup>46</sup>. At length scale of 20 nm and at room temperature (300 K), the thermal conductivity (k)of pristine, edge functionalized, and basal plane functionalized graphene are computed to be 215 W/mK, 167 W/mK, and 99 W/mK, respectively. The thermal conductivity predicted for edgefunctionalized case is 68.7% higher than the basal plane case and 28.7% lower than pristine graphene. This reduction in thermal conductivity upon functionalization (relative to pristine graphene) is due to the distortion of the graphene structure. Large reduction in thermal conductivity in basal plane functionalization is attributed to much larger distortion of graphene in its basal plane as shown in Fig 6f. Edge bonding distorts graphene to a much smaller degree compared to basal plane case, as seen in the relaxed DFT (density-functional theory) structures in Fig. 6e and f. Carbon atoms on the basal plane of graphene are sp<sup>2</sup> hybridized; in forming an extra bond to functionalize, they transform to sp<sup>3</sup> state, protruding outwards and distorting graphene in the process. Unlike inner carbon atoms, edge atoms can adopt tetrahedral geometries more freely without causing extra strain. Lower distortion through edge bonding results in significantly higher  $k_{graphene}$  relative to the basal plane case. To demonstrate this effect clearly, we present the temperature along the length of the graphene sheet for pristine, edge functionalized and basal plane functionalized graphene. We have divided the graphene (100 Å long) into 50 bins. For the basal plane case, a sudden temperature drop at the functionalized sites is observed, indicating a reduction in thermal conductivity due to phonon scattering at functionalization sites. However, temperature distribution within the edge functionalized graphene remains linear due to the minimal distortion and shows no such sudden temperature drops. These results clearly demonstrate that edge functionalized graphene has superior heat conduction ability compared to basal plane functionalized graphene.

While above results demonstrate advantage of edge bonding in heat conduction in individual graphene sheets, we next demonstrate that interface thermal conductance is also higher at an individual junction (between polymer chain and graphene) located on edge of graphene as opposed to on the basal plane. This implies that heat conducts into graphene more efficiently through a junction located on edge compared to basal plane. Molecular dynamics simulations were used to compare interface thermal conductance for junction at an edge relative to on the basal plane. Atomic structures for the two cases are shown in Fig. 7a which shows polymer chains bonded on the edge as well as on the basal plane of graphene. Temperature difference of 20 K was applied across the location of bonding (junction) and resulting heat flux was computed. MD computations reveal almost 40% higher heat flux for edge case relative to basal plane case (Fig. 7b). Understanding of this higher interface thermal conductance is achieved using first-principles Green's function calculations, described next.

## 3.2 Atomistic Green's Function Computations

Fig. 7c shows that AGF method also predicts almost 60% higher interface thermal conductance for edge case relative to basal plane bonding at 300 K. This agrees qualitatively with MD simulation results.



**Figure 7.** a) Junction involving polymer chain bonded on edge and basal plane of graphene. Comparison between edge and basal plane functionalization in terms of (b) heat flux across junction c) interface thermal conductance and d) overall phonon transmission. Comparison between edge and basal plane in terms of transmission to e) in-plane phonons and f) out of-plane phonons of graphene.

Fig. 7d shows that this higher thermal conductance is due to the higher phonon transmission for a junction on edge of graphene relative to basal plane. To understand this higher phonon transmission for edge case, we split the total phonon transmission from polymer chain into inplane and out-of-plane vibration modes of graphene using polarization dependent atomistic Green's function method (details provided in Methods). Results show that transmission from polymer to in-plane vibration modes of graphene is much larger for edge case relative to basal plane bonding. The contribution of out-of-plane vibration modes to total transmission is found to be comparable for edge and basal plane bonding cases. This higher transmission for edge relative to basal plane cases, resulting in higher interfacial thermal conductance for edge case. Above computations provide a comprehensive understanding of the higher polymer-graphene nanocomposite thermal conductivity through edge relative to basal plane functionalization.

#### 2. CONCLUSION

In summary, this work provides a detailed comparison of edge and basal plane functionalization of graphene nanoplatelets in enhancing thermal conductivity of polymergraphene nanocomposite, through both molecular dynamics study and Green's function calculations. Edge bonding is shown to lead to superior enhancement in composite thermal conductivity relative to basal plane bonding. Molecular dynamics simulations reveal this advantage of edge bonding to be due to all sheets of graphene nanoplatelets interacting efficiently with surrounding polymer through edge bonding. Coupling of the high in-plane thermal conductivity of graphene (~2000 W/mK) with the surrounding polymer through edge bonding leads to an efficient thermal conduction pathway through the composite. For basal plane bonding, only the outermost layers (surface layers) of the nanoplatelet have significant thermal interaction with the polymer. Poor out-of-plane thermal conductivity of graphene (~ 10 W/mK) causes inefficient heat conduction from outer to inner layers, resulting in the overall nanoplatelet being less effective in heat conduction for basal plane bonding compared to edge bonding. Overall, simulations predict 48% higher k through edge relative to basal plane bonding, at 35 weight% composition and for 10 layer thick nanoplatelets. Simulations further reveal other advantages of edge bonding, such as lower damping of vibrations in all layers of the nanoplatelet through edge

bonding, high thermal conductivity of individual graphene layers through minimal distortion of graphene structure induced by edge functionalization, and higher thermal conductance of individual junction at edge relative to basal plane, mediated by higher phonon transmission to inplane phonons of graphene. This work opens up new avenues to achieve higher thermal conductivity of polymer-graphene nanocomposites, with important applications in a wide range of thermal management technologies.

## **Conflicts of Interest**

There are no conflicts of interest to declare.

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