

Role of Solvation Site Segmental Dynamics on Ion Transport in Ethylene-Oxide based Side-Chain Polymer Electrolytes

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17	Abstract
18	Ion conducting capability is often imparted to polymeric materials through short polyether side-
19	chains, and yet the impact of this graft polymer architecture on ion solvation and conduction has
20	not been fully explored. Here we use a combination of impedance spectroscopy, vibrational
21	spectroscopy, and atomistic molecular dynamics (MD) to compare the conductivity, ionic
22	interactions, and polymer dynamics in a series of graft polyether electrolytes. We find that in
23	poly[(oligo ethylene oxide) methyl ether methacrylate] (POEM), a widely used graft polymer

electrolyte, the ionic conductivity drops more than an order of magnitude as the side-chain length 24 is decreased from nine ethylene oxide (EO) units to three. This difference in conductivity is 25 unexplained by differences in the calorimetric glass transition temperature (T_{σ}) , which varies only 26 slightly with side-chain length. Through vibrational spectroscopy and MD simulations we 27 demonstrate that both linear and graft polyethers solvate Li⁺ ions effectively and dissociate them 28 29 from large counterions, irrespective of side-chain length. Li⁺ ions do, however, show preferential solvation by EO units far from the methacrylate backbone. Similarly, EO units far from the 30 backbone show enhanced segmental dynamics, while those near the immobile methacrylate group 31 32 move substantially more slowly, as quantified by bond vector autocorrelation relaxation times. This heterogeneity in both ion solvation and local segmental relaxation explains variation in ion 33 conductivity where material-averaged properties such as $T_{\rm g}$ and number of free ions fail to do so. 34 Importantly, the ionic conductivity is dictated primarily by the segmental mobility of the EO units 35 which form effective solvation sites, rather than system-wide dynamics. 36

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38 MAIN TEXT

39 Introduction

Solid polymer electrolytes (SPEs) play a critical role in the development of high energy density electrochemical energy storage and conversion devices. In the field of lithium ion batteries, poly(ethylene oxide) (PEO) has long been the most promising candidate for use as a separator and electrolyte due to its ability to readily solvate and conduct alkali metal cations.¹ Many other materials chemistries have been considered for their potential as dry SPEs, such as polycarbonates^{2–4} and polyesters,^{5–7} but polyethers continue to outperform these other systems in terms of ionic conductivity and remain the most widely studied class of polymer electrolytes. However, the semi-crystalline nature of PEO at ambient temperatures and resultingly low room temperature conductivity, as well as a low lithium cation transference number, and an inverse relationship between ion transport and mechanical properties have prevented homopolymer PEO from satisfying the full set of requirements to enable safe cycling of high energy density lithium metal batteries.

New directions in the field of ion conducting polymers focus on incorporating additional 52 functionalities to the well-known ether-based electrolytes to improve on these mechanical and 53 electrochemical shortcomings of PEO. Such materials include microphase-separating block 54 55 copolymers, graft and bottlebrush polymers, and random copolymers or blends where secondary functional groups affect the phase behavior and electrochemical properties of the material.^{8–14} The 56 introduction of ethylene oxide (EO) segments as grafted side-chains on polymerizable 57 macromonomers is a particularly attractive as this approach is accessible through a number of 58 well-established synthetic techniques, including anionic polymerization,¹⁵ atom-transfer radical 59 polymerization (ATRP).¹⁶ and reversible-addition-fragmentation chain transfer polymerization 60 (RAFT).¹⁷ This method has the added benefit of reducing or eliminating room temperature 61 crystallization of the short polyether chains. These controlled living polymerization techniques are 62 also amenable to random or block copolymerization, which have been used successfully to 63 incorporate additional functionalities alongside the ion conducting EO groups, such as a 64 mechanically stabilizing group or single-ion conducting component.^{18–20} The ether oxygen motif 65 66 has also been incorporated into materials that are tailored for electrode binder applications due to their dynamic self-healing capability^{21,22} or coupled with polythiophene groups to create dual ion-67 electron conducting materials.^{23,24} Further improvement upon the design of these multi-functional 68

materials, however, requires a clearer understanding of how the polymer chain architecture andcomposition affects the solvation and transport of ions.

Ion transport in rubbery polymer electrolytes is generally understood to require a high 71 degree of salt dissociation, connectivity between polymer solvation sites, and fast segmental 72 dynamics to facilitate ion transport between solvation sites. PEO forms stable complexes with 73 74 alkali metal ions such as lithium through interactions with the lone pairs on the ether oxygens. This enables high degree of ionic dissociation from large, stable anions, such as the common 75 bis(trifluoromethanesulfonyl)imide (TFSI). The low glass transition temperature (T_{g}) of PEO 76 77 gives rise to fast segmental dynamics when completely amorphous (above ca. 50°C), which has been shown to facilitate rapid ionic transport.^{25,26} Low T_g alone, however, is not necessarily a 78 good predictor of ionic conductivity. This fact was exemplified by a recent study of 79 poly(trimethylene carbonate)-based polymer electrolytes, where it was demonstrated that the 80 introduction of long alkyl side-chains lowered the glass transition temperature, but a concomitant 81 increase in ionic conductivity was not observed.²⁷ Molecular dynamics (MD) simulations 82 indicated that, although the material overall exhibited faster dynamics when alkyl plasticizers were 83 present, the time between ion hopping events was significantly longer. Similarly, solvation site 84 connectivity has been explored in various systems as an additional metric to accounts for the 85 discrepancy between trends in T_g and ionic conductivity.^{28–30} Previous studies have found that in 86 branched polyethers, the length of polymer side-chains and the spacing between them are key 87 parameters in determining the conductivity of the system.^{31,32} MD studies have sought to provide 88 mechanistic insight into the effects of branched architecture and side-chain structure on ion 89 transport, though a clear connection between microscopic transport phenomena and macroscopic 90 material performance was not established.³³ Recent work by our group has demonstrated that 91

92 heterogenous ion solvation and local polymer relaxation rates in graft polymers result in 93 qualitatively different trends in ion conductivity than in linear polymer electrolytes.³⁴ Greater 94 understanding of how molecular-level transport processes are affected by the graft chain 95 architecture, chemical composition, and side-chain length are required to optimize the design and 96 development of these systems.

97 In this study, we synthesize, characterize, and computationally model a series of graft polyethers to examine the effects of polymer composition, chain architecture, and side-chain 98 length on the ion solvation, average and local segmental dynamics, and transport properties of 99 100 these electrolytes. We observe that the experimental ion conductivity varies by as much as an order of magnitude in poly[(oligo(ethylene oxide))methyl ether methacrylate] (POEM) materials of 101 different side-chain lengths, and this effect is not well explained by differences in $T_{\rm g}$ or ionic 102 dissociation. The same trend is observed in the simulated Li-ion diffusivity. Comparing solvation 103 site edge density from MD simulations and T_{g} -corrected experimental conductivity, we see that 104 solvation site connectivity, as defined in previous studies, only accurately predicts conductivity or 105 MSD at intermediate temperatures (T). We find significant deviations above and below the 106 solvation site predicted performance at high and low values of T- T_{g} , respectively. We demonstrate 107 that although ions are fully dissociated in all systems, Li⁺ ions show a strong preference for ether 108 oxygens over carbonyl groups. Constraints on the available conformations of those ether oxygens 109 giving rise to certain monomers having a much more significant role in solvation than others. We 110 111 further see that individual EO segments relax at substantially different rates as a function of position along the side-chain. Those EO units furthest from the relatively immobile methacrylate 112 113 backbone exhibit significantly faster relaxation rates than those near the backbone. This spatial variation in the segmental mobility is not captured by the $T_{\rm g}$ differences, but local EO segmental 114

dynamics seems to be critical in producing the observed trends in ionic conductivity. Specifically, 115 the dynamics of those EO segments which most frequently participate in the formation of solvation 116 sites have far greater impact on the ionic conductivity than the overall segmental dynamics. 117 Moreover, we find that making the backbone more flexible or increasing the fraction of high-118 mobility (far from the backbone) EO units at the same overall ether oxygen fraction both increase 119 the ionic conductivity. These findings have broad implications for developing graft and 120 multifunctional polymer electrolytes and provide clear design criteria for optimizing polymer 121 architecture and chemistry for high ionic conductivity. 122

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Fig. 1. (a) Chemical structure of polymers studied and LiTFSI salt; (b) Representative snapshots
of united atom MD simulations showing common 1 and 2 chain solvation motifs in each system.
Ether oxygen units are in red, Li⁺ ions are cyan, aliphatic carbons are gray, backbone carbons are
black, and methacrylate group oxygens are purple.

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130 **Results and Discussion**

To explore the effects of polymer chain architecture and composition on ion conduction 131 and solvation in EO-based polymer electrolytes, we employ a combined experimental and 132 computational platform involving thin film electrochemical impedance spectroscopy (EIS), 133 Raman and Fourier Transform Infrared (FTIR) spectroscopy, and molecular dynamics (MD) 134 simulations. We investigate two classes of polyethers in this study: linear poly(ethylene oxide) 135 (PEO), and a series of graft polymers based on short polyether side-chains grafted to an acrylate 136 or methacrylate backbone. Side-chain polymers poly[(oligo (ethylene oxide)) methyl ether 137 methacrylate] (POEM_x), poly[(oligo (ethylene oxide)) methyl ether acrylate] (POEA_x), and a 138 139 random copolymer of POEM and poly(methyl methacrylate) (PMMA) were prepared by reversible addition fragmentation chain transfer polymerization (RAFT). The subscript x here refers to the 140 number of EO repeat units in the grafted side-chain, which in this study is either 3, 5, or 9. The 141 chemical structures of these materials are shown in Fig. 1a. The polymerization reactions were 142 performed at 70 °C in dimethylformamide (DMF) using azobisisobutyronitrile (AIBN) as a radical 143 initiator and 2-cyano-2-propyl dodecyltrithiocarbonate (CPDTC) as a chain transfer agent. The 144 reaction scheme is shown in scheme S1 and S2. The number average molecular weight (M_n) and 145 dispersity (D), as determined by gel permeation chromatography (GPC, Fig. S1), are given in 146 Table 1. The polymer electrolyte systems are modeled by MD simulations using a united atom 147 representation to characterize the equilibrium ion solvation structures and ion transport rates. 148 Representative snapshots of the MD simulations are shown in Fig. 1b. Throughout the study, 149 150 results from the simulations clarify and expand upon the experimental data and are used to help build a molecular level understanding of the effect of chain architecture and composition on 151 polymer electrolyte ion conduction. 152

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Material	$M_{ m n}~(m g~mol^{-1})$	Ð	$x_{\rm EO}$	$T_{\rm g}$ at $r = 0.05 ~(^{\circ}{\rm C})$
PEO	120,000	¹ 1.10	0.333	-50
POEM ₉	² 17,700	² 1.13	0.265	-57
POEM ₅	² 33,400	² 1.29	0.227	-41
POEM ₃	² 21,200	² 1.21	0.188	-31
POEA ₉	² 11,800	² 1.08	0.273	-50
POEM9-r-PMMA	² 13,500	² 1.17	0.172	-37

Table 1. Physical properties of materials studied

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¹ As reported by the supplier

² As determined from GPC-MALS in THF at 50 °C using dn/dc = 0.073 mL g⁻¹

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159 Side-chain length—not T_g—determines ionic conductivity in graft polyethers

All of the studied polymers are rendered ionically conductive by addition of lithium 160 bis(trifluoromethanesulfonyl)imide (LiTFSI) blended at a ratio of r = [Li]/[EO] = 0.05. Note that 161 the salt concentration is held constant with respect to the ether oxygen mole fraction of the polymer 162 (x_{EO}) , and so the mass fraction of salt in the system is not the same across different polymers. We 163 follow the approach taken by Pesko *et al.* in defining this mole fraction.²⁸ Briefly, this x_{EO} quantity 164 is the ratio of ether oxygens to the total number of atoms in the repeat unit, not including hydrogen 165 atoms. Implicit in this choice of salt loading is the assumption that only the ether oxygen units 166 contribute to solvation and conduction, and that the methacrylate groups constitute inactive 167 material. The choice to hold r constant, rather than total weight fraction of salt, is common in 168 studies of nonhomogeneous polyether electrolytes,^{16,21,30} and the validity of this assumption will 169

be discussed in greater detail in the text. After blending with LiTFSI, polymer electrolyte solutions are spin cast from either acetonitrile or a mixture of acetonitrile and toluene onto interdigitated electrodes (IDEs) that are surface-passivated with 0.8 nm SiO₂ by atomic layer deposition. These IDEs are used to perform EIS measurements on polymer films of 70 – 100 nm thickness. The resulting data is fit to an equivalent circuit model and converted to conductivity by an appropriate cell constant, as described in our previous work.³⁵

The temperature-dependent ionic conductivity of linear PEO and the graft polymers 176 POEM₉, POEM₅, and POEM₃, all at a salt ratio of r = 0.05, is shown in Fig. 2a. The ionic 177 conductivity in POEM₉ is lower than that of PEO by around a factor of two at all temperatures 178 above the PEO crystalline melting point (ca. 50 °C). POEM₉ conductivity it is still reasonably 179 high, however, above the commonly cited benchmark of 10⁻⁴ S cm⁻¹ at 50 °C.³⁶ More interestingly 180 181 though, the conductivity of $POEM_x$ decreases by an order of magnitude or more as x decreases from 9 to 3. This trend in ionic conductivity as a function of side-chain length is evident from Li⁺ 182 ion mean squared displacement (MSD) observed in the simulations (see Fig. S2). At the end of the 183 simulation time, Li⁺ MSD is highest for PEO at all temperatures, and it decreases with decreasing 184 side-chain length. Although differences in conductivity as a function of side-chain length have 185 been observed previously in POEM and other graft polyether systems, clear mechanistic reasons 186 for this effect have not been assigned.^{31,33} Understanding why this effect arises is critical to future 187 development of optimized polymer electrolytes based on side-chain architectures. 188



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Fig. 2. (a) Experimentally determined temperature dependent ionic conductivity for r = 0.05polymer electrolytes with solid lines representing the fits to the Vogel-Tamman-Fulcher (VTF) equation (*eq.* 1) and (b) experimental conductivity corrected by T_{g} .

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194 Ionic conductivity is commonly understood to be tied to the segmental dynamics of the 195 polymer host.³⁷ Vogel-Tammann-Fulcher (VTF) behavior of ionically conductive polymers is 196 often cited as evidence of this connection between ionic mobility and polymer relaxation times.^{25,38}

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The conductivity of all four materials follow VTF behavior as a function of temperature, with fits
to the VTF equation (*eq.* 1) drawn as solid lines in Fig. 2a.

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$$\sigma = AT^{-0.5} \exp\left[\frac{-E_a}{R(T-T_0)}\right]$$
(1)

 T_0 is the Vogel temperature, E_a is the pseudo-activation energy, and A is a constant prefactor.³⁹ As 200 the length of grafted side-chains is known to increase the available free volume and increase 201 segmental mobility, it is plausible that decreased segmental dynamics in POEM₃ chains is 202 responsible for the low ionic conductivity.⁴⁰ T_g, as determined by differential scanning calorimetry 203 204 (DSC), is a common proxy for describing the effects of segmental dynamics on conductivity. DSC thermograms for each polymer at r = 0.05 are shown in Fig. S3, and the values for T_g are shown 205 in Table 1. T_g generally increases as side-chain length decreases in POEM_x, which would suggest 206 207 generally slower segmental dynamics and therefore lower ionic conductivity in materials with short side-chains. However, by plotting conductivity as a function of $1000/(T-T_g)$ (Fig. 2b), it is 208 clear that this difference in $T_{\rm g}$ is insufficient to explain the observed trends in conductivity. This 209 210 common approach to correcting for differences in $T_{\rm g}$ suggests that if all corrected conductivity falls along the same line, differences in segmental dynamics explain all differences in conductivity, 211 and $T_{\rm g}$ fully captures those differences in segmental dynamics.⁴¹ Although linear PEO and graft 212 POEM_x seem to follow VTF behavior, side-chain length appears to have an additional impact on 213 ionic mobility or that there are segmental dynamics influencing ionic mobility that are not captured 214 by traditional $T_{\rm g}$ measurements. 215

As side-chain length effects on T_g do not provide a clear evidence that average segmental dynamics—as described by T_g — dictate the differences in ionic conductivity in graft polyethers, differences in the polymer compositions and chain architectures may instead influence the density and connectivity of solvation sites available for ion hopping. Webb and coworkers have developed 220 a framework for quantifying the degree of solvation site connectivity based on the results of MD simulations like the ones performed here.^{28–30} Briefly, a solvation site is defined at the centroid of 221 a set of five or more ether oxygen atoms each within 3.7 Å of the centroid. These sites are shown 222 as filled circles in Fig. 3a. Solvation sites are connected by edges if the sites are within a cutoff 223 radius of 3 Å of each other. These edges are shown as colored lines in Fig. 3a. Note that 224 connections between solvation sites that are farther apart than 3 Å are not shown. A more thorough 225 explanation of the relationship between solvation site connectivity and ion transport as a function 226 of nearest-neighbor distance can be found in previous work by Pesko et al.²⁸ Importantly, this 227 228 analysis considers only ether oxygens as contributing to the formation of solvation sites. This results in an overall lower density of solvation sites and edges in POEM with lower ether oxygen 229 mole fraction, x_{EO} , as can be seen visually in Fig. 3a. The solvation site edge density, κ , normalized 230 by the solvation site edge density of PEO, κ_{PEO} , is shown in Fig. 3b for different POEM_x materials. 231 The value of $\kappa/\kappa_{\text{PEO}}$ varies linearly with x_{EO} , as seen by the linear fit dashed line in Fig. S4. In the 232 study of a series of linear polyethers by Pesko *et al.*, κ/κ_{PEO} was also found to vary linearly with 233 $x_{\rm EO}$ within a given family of materials.²⁸ The graft architecture of the polymers, moreover, does 234 not seem to negatively influence the density of solvation sites. Nevertheless, this monotonic 235 decrease in solvation site connectivity as a function of decreasing side-chain length does, at least 236 qualitatively, explain the observed trend in conductivity. Solvation site density and connectivity 237 are also found to be independent of temperature, depending solely on the ether oxygen content and 238 239 polymer chain architecture, suggesting that κ/κ_{PEO} represents an intrinsic material property.



Fig. 3. (a) Visualization of solvation site network in PEO and POEM_x from MD simulations; (b) Temperature averaged solvation site density ratio (gray) and normalized reduced conductivity (σ_{nr} , colors) at different fixed *T*-*T*_g for the three POEM_x materials. Solvation site density and experimental conductivity are normalized to the value for PEO. Ratio of solvation site edge density (dashed lines) and Li⁺ ion mean squared displacement (MSD, solid lines) in (c) POEM₉, (d) POEM₅, and (e) POEM₃ to PEO at different values of *T*-*T*_g.

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To quantitatively compare the calculated solvation site edge density to the experimentally determined conductivity, we introduce a normalized, temperature-reduced conductivity, σ_{nr} , similar to the scheme used by Pesko, *et al.*²⁸ σ_{nr} is calculated by first determining POEM conductivity at fixed values of reduced temperature, T- T_g , using the VTF fits to the data described previously and then normalizing this value by differences in x_{EO} and conductivity of PEO, as shown in *eq. 2*.

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$$\sigma_{\rm nr} = \left(\frac{\sigma(T - T_{\rm g})}{\sigma_{\rm PEO}(T - T_{\rm g})}\right) \left(\frac{x_{\rm EO, PEO}}{x_{\rm EO}}\right) \tag{2}$$

Implicit in the use of this normalized conductivity are the assumptions that ionic solvation is 255 256 similar in all materials being compared and that the effects of polymer segmental dynamics on 257 ionic mobility are well captured by T_g and fits to eq. 1. If these assumptions are valid for a given set of materials and no other factors are expected to limit conductivity, σ_{nr} would represent an 258 experimental solvation site connectivity, and it should vary with x_{EO} similarly to the solvation site 259 connectivity calculated from MD simulations and be independent of temperature. As can be seen 260 in Fig. 3b, σ_{nr} increases monotonically with increasing x_{EO} , suggesting that solvation site 261 connectivity does play a critical role in determining conductivity in graft polyethers. At 262 intermediate temperatures (T-T_g = 150 K) σ_{nr} is in excellent quantitative agreement with the 263 simulated κ/κ_{PEO} , suggesting that this theory fully captures the important physical properties 264 265 dictating ionic conductivity. σ_{nr} exhibits a strong temperature dependence for all three POEM 266 systems, however, suggesting that this parameter is not an intrinsic to the material, as was found in previous studies.⁴² At temperatures above and below $T-T_g = 150$ K, we see that experimental 267 268 σ_{nr} deviates significantly from the simulated κ/κ_{PEO} , by as much as a factor of 5. Specifically, at low values of T- T_g , σ_{nr} is substantially lower than κ/κ_{PEO} , indicating that other factors reduce ionic 269 conductivity that are not accounted for in this normalization scheme. Conversely, at high values 270 of T- T_g , κ/κ_{PEO} underpredicts σ_{nr} , suggesting that there are factors increasing the conductivity of 271 POEM relative to PEO. This difference is in contrast to the previous reports regarding linear 272

polyethers where σ_{nr} was found to be relatively constant with temperature.⁴² Note that the 273 experimental σ_{nr} values presented here at high and low temperatures are extrapolated from fits to 274 eq. 1, rather than experimentally measured, and they span a wider temperature range than was 275 reported by Pesko et al. The low temperature values $(T-T_g = 50K)$ would be below the 276 crystallization point of PEO, making experimental measurement of the ion conductivity of 277 amorphous PEO untenable. Nevertheless, analysis of this broad temperature range provides 278 important insight into the temperature dependent material behavior that may be missed if only a 279 narrow range is considered. 280

Fig. 3c-e shows the ratio of Li⁺ ion mean squared displacement (MSD) from simulation in 281 POEM₉, POEM₅, and POEM₃ to Li⁺ MSD in PEO at different reduced temperatures. κ/κ_{PEO} is 282 shown as dashed lines in each system. This value is nearly invariant with temperature, showing 283 only slight fluctuations around an average value (the temperature averaged value is shown in Fig. 284 3b). Although the time scales of these simulations does not capture truly diffusive behavior, the 285 effective diffusivity (i.e. the MSD rate at the end of the simulation) exhibits the same qualitative 286 trends as was observed in the experimental system. At intermediate temperatures, the ratio of Li⁺ 287 ion MSD is close to the ratio of solvation site connectivity, whereas at high and low temperatures 288 289 the MSD ratios are well above or below κ/κ_{PEO} , respectively. It is clear that this temperature dependent behavior is inherent to graft polyethers, and one or more of the critical assumptions 290 made in using this model must be reconsidered or refined. 291

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293 Chain architecture influences structure of solvation environment

Our analysis of ionic conductivity behavior thus far has relied on three critical assumptions
about the solvation structure within POEM. First, we have assumed that only EO units participate

in creating Li⁺ ion solvation sites and facilitating ion transport, an assumption that is well supported by previous experimental and computational work involving similar systems.^{30,43} Second, we have assumed a similar degree of ionic dissociation in all systems. Third, we have neglected any effect that the polymer chain architecture (*i.e.* linear *vs.* graft) may have on the solvation environment, using ether oxygen content as the only metric for comparing between materials. To validate these assumptions, we use MD simulations, Raman, and FTIR spectroscopy to fully characterize the solvation environment and ionic interactions in PEO and POEM.

We begin by confirming the assumption that ether oxygens are the only polymer functional 303 304 groups interacting with Li⁺ ions, and solvation sites are formed exclusively from these ether oxygen atoms. From MD simulations, we can quantify the percentage of the total oxygens within 305 the first solvation shell of a lithium ion, here defined to be within 3.25 Å radius of the central ion, 306 307 belonging to a given class of oxygen atom. Fig. 4a shows the percentage of oxygens involved in solvation that come from ether (OET), carbonyl (OKT), ester (OKE), or TFSI anion (OTFSI) 308 groups in PEO and POEM salt blended systems. We find clear evidence that ether oxygens are 309 the only groups involved in polymer-ion solvation for all four systems, with a very small (< 1%) 310 prevalence of ester oxygen solvation counted in the $POEM_3$ and $POEM_5$ systems. This is visually 311 312 evident from the Li⁺-O radial distribution function (RDF) plots shown in Fig. S5. From the RDFs it is clear that EO oxygens form nearly the entirety of the first solvation shell. These findings are 313 consistent with previous reports of polymer electrolyte systems with multiple potential solvating 314 315 groups, where lithium ions have been observed to be highly selective towards coordination by ether oxygens over ester or carbonate moieties.^{30,43} We confirm this observation experimentally 316 using FTIR. Fig. 4b shows FTIR spectra for neat and r = 0.05 POEM systems in the wavenumber 317 range 1780 - 1680 cm⁻¹ (full spectra are shown in Fig. S6). The peak at 1737 cm⁻¹ in the neat 318

samples arises from the carbonyl stretch (C=O bond), and lithium ion coordination with the 319 methacrylate group should result in red-shifting of this peak.^{44,45} The salt blended samples (blue 320 curves in Fig. 4b) for POEM₉ and POEM₅ show no change whatsoever from the neat samples. The 321 r = 0.05 POEM₃ samples does exhibit a small secondary peak near 1710 cm⁻¹, suggesting that 322 some carbonyl oxygens do interact with lithium ions. The size of the low wavenumber peak is 323 much smaller than that of the free C=O peak at 1731 cm⁻¹, however, so the total fraction of lithium-324 carbonyl complexes in the systems is likely quite low.^{46,47} Shifts in several of the characteristic 325 ether side-chain peaks (C-O-C symmetric stretch at 1101 cm⁻¹, CH₂ wagging at 1352 cm⁻¹) indicate 326 327 that Li⁺ ions instead coordinate with ether oxygens, though the overlap of these peaks with those of the TFSI anion make direct comparison of the neat and r = 0.05 systems difficult.⁴⁸ This is 328 consistent with previous reports where it has been shown that in materials with both carbonate and 329 330 ether functionalities, Li⁺ ions may be preferentially coordinated with the C=O group if the ether chains contain only one or two oxygens.^{49,50} Once there are at least three EO units in a chain 331 however, the polyether chain can form a chelating structure around the Li⁺ ion, and this solvation 332 is favored over the C=O group association. These FTIR data are entirely consistent with the MD 333 results, and we can confidently conclude that the vast majority of ion solvation sites are comprised 334 of ether oxygens in all linear and graft polymers studied here. These results validate our use of 335 constant r ([Li]/[EO]) for this study, though this strong preference for ether oxygen association 336 may impose limitations on Li⁺ ion conduction pathways throughout the system. 337

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Fig. 4. Ionic association and solvation. (a) Relative percentage of solvating oxygen of each type 340 from MD simulations (ether oxygen - OET, carbonyl oxygen - OKT, ester oxygen - OKE, TFSI-341 ion – OTFSI); (b) experimental FTIR spectra of the carbonyl (C=O) stretch for neat and r = 0.05; 342 (c) percentage of free ions in r = 0.05 electrolyte systems as determined from Raman spectroscopy; 343 (d) percent occurrence of most common solvation motifs (XY-Z refers to solvation by X ether 344 oxygens, Y TFSI⁻ oxygens, involving Z polymer chains plus TFSI⁻ anions) from simulation; and 345 (e) percent occurrence of solvation by a given ether oxygen along the POEM side-chain from 346 simulation. 347

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The MD results also suggest that the prevalence of Li-TFSI complexation is low, with fewer than 10% of all solvating oxygen atoms coming from TFSI⁻ in any given system. To

experimentally confirm the absence of a large number of associated species which may reduce 351 ionic conductivity, we use Raman spectroscopy to probe molecular vibrations of the TFSI 352 molecule. Raman spectra for PEO and POEM r = 0.05 systems in the range of 720 - 760 cm⁻¹ are 353 shown in Fig. S7. The peak in this range can be fit to a free TFSI anion peak at 741 cm⁻¹ and an 354 associated anion peak at 744 cm⁻¹ to estimate a fraction of free ions in the system.^{51,52} The 355 percentage of free ions in the system is taken from the area fraction of the fitted Voigt peaks and 356 plotted in Fig. 4c. For all four polymer systems, the free ion content is nearly 100%, within error 357 of the peak fitting. Although the simulations suggest that there may be a greater fraction of TFSI 358 359 in the Li⁺ solvation shells, the Raman data suggest that these interactions are extremely weak and do not constitute ion pairs or higher order aggregates. We can assume that the ions are fully 360 dissociated, and lithium only briefly interacts with counterions that make up a small fraction of 361 any given solvation site. Differences in the degree of ionic dissociation is therefore not expected 362 to be a significant contributor to the decrease in conductivity observed in short side-chain POEM. 363

Although the degree of solvation is quantitatively similar for all four materials, the 364 solvation environment may be qualitatively different for each, based on the amount and 365 configuration of ether oxygens in the system. Atomistic MD simulations allow us to further 366 characterize these polymer electrolyte systems by the structure of individual solvation sites at the 367 molecular level. Fig. 4d shows the relative propensity for the four most common solvation motifs 368 in each polymer system. Several of these most common solvation motifs are shown as simulation 369 370 snapshots in Fig. 1b. Coordination motifs are denoted by "XY-Z", where X refers to the number of ether oxygens in the first solvation shell, Y refers to the number of TFSI molecules in the first 371 shell, and Z is the number of polymer chains plus TFSI anions present in the solvation shell. For 372 373 example, the 51-2 motif refers to coordination by five ether oxygens from a single chain and one

TFSI anion. For POEM, each side-chain is considered separately, and in PEO, although it is a 374 single long chain, we consider noncontiguous segments of the backbone to be separate chains for 375 this purpose. We find that the most common motifs all involve either five or six ether oxygens, 376 consistent with previous findings that this represents the most stable configurations for cation 377 coordination.^{30,53,54} However, certain motifs are inaccessible to some polymer systems, such as the 378 379 60-1 motif (six ether oxygens from a single chain). This configuration is the most likely for PEO and is also readily adopted by POEM₉, though it cannot occur in POEM₅ or POEM₃. Instead, these 380 shorter side-chain systems exhibit a greater prevalence of the 60-2 configuration, creating the six-381 382 oxygen solvation shell from three oxygens each from two side-chains. Although Li⁺ ions are solvated in a qualitatively similar manner across all four polymer systems studied, the local 383 polymer conformations adopted to create those solvation shells is highly dependent on the chain 384 architecture and conformation. 385

The strong preference for specific solvation motifs gives rise to heterogeneity along the 386 387 side-chains of POEM, with some oxygens participating in solvation significantly more frequently than others. Fig. 4e shows the prevalence of ionic association with specific ether oxygens in POEM 388 as a function of distance along the side-chain. EO units are indexed from 1 being the unit closest 389 390 to the methacrylate group. In POEM₃, all oxygens participate at roughly the same frequency, as there are no ways to produce the 60-2 motif (>70% of the solvation structures) without involving 391 all three ether oxygens of a given side-chain. However, both POEM₅ and POEM₉ exhibit much 392 393 higher likelihood of coordination by EO units farther from the backbone, with units 3-5 and 4-9, respectively, being significantly overrepresented in solvation. This can be understood by two 394 combined effects. First, there are more permutations of three (or six) contiguous ether oxygens in 395 396 the middle of the side-chain, and so those EO units are statistically more likely to be involved in

397 solvation. Second, the EO units near the backbone are in very close proximity to the methacrylate 398 group which does not participate in solvation. This limits the ability of those EO units to come 399 close enough to EO units of another chain to form a full solvation shell. This heterogeneity in ether 400 oxygen involvement is a direct result of the graft chain architecture, and the relative contribution 401 of each ether oxygen to ion transport may not be equal.





Fig. 5. Inverse mean relaxation time $(1/\langle \tau \rangle)$ of different bonds along the polymer chains at (a) *T*-405 $T_g = 50$ K, (b) T- $T_g = 150$ K, and (c) T- $T_g = 250$ K derived from the bond vector autocorrelation 406 function. $1/\langle \tau \rangle$ serves here as an indicator of local segmental mobility. Index 0 is the C-C bond 407 along polymer backbone. The other indices refer to the C-O bonds in the ether side chain with 408 index 1 being the closest to the backbone. The solid colored lines are to guide the eye.

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410 Graft chain architecture results in heterogeneous polymer dynamics

The selective solvation by certain EO repeat units in the graft polyethers suggest that only part of the polymer chains meaningfully contribute to the measured ionic conductivity. This may explain why metrics such as T_g and solvation site density, which are system wide average values, do not fully capture the transport behavior. Instead, a more nuanced, local understanding of

segmental dynamics and solvation is warranted. Rather than using macroscopic averages of 415 segmental mobility by DSC, we can instead use the MD trajectories to determine the local mobility 416 of individual ether oxygen units. Fig. 5 shows the inverse mean relaxation time, $1/\langle \tau \rangle$, extracted 417 from the C-O bond vector autocorrelation function (BVAF) at different $T-T_g$ as a function of 418 position along the polymer side-chain. Detailed explanation of this calculation are provided in the 419 Supporting Information. Briefly, the BVAF describes how quickly neighboring bonds decorrelate 420 from an initial orientation. The mean relaxation time can be fit to a stretched exponential function, 421 and $1/\langle \tau \rangle$ serves as an indicator of local segmental mobility. This analysis was introduced in our 422 previous work, and the methodology is described in greater detail there.³⁴ 423

In the linear PEO system, $1/\langle \tau \rangle$ shows no dependence on ether oxygen position, as 150 kg 424 mol⁻¹ molecular weight used in the simulation is well above the chain length where chain ends 425 ought to impact local dynamics or conductivity for most ether units.⁵⁵ In all three POEM systems, 426 conversely, the local dynamics are strongly dependent on bond index. Those units closest to the 427 polymer backbone exhibit significantly suppressed dynamics relative to PEO, while EO monomers 428 near the side-chain end decorrelate at an equal or greater rate than PEO. This trend arises from 429 similar competing effects that were attributed to difference in ion complexation by different EO 430 431 positions. The C-C backbone carbon bond (bond index 0) exhibits between six and eight orders of magnitude slower relaxation rates than PEO, and the POEM ether units near this low mobility 432 backbone have similarly suppressed dynamics. The POEM ether units farthest from the backbone, 433 434 however, have greater free volume to sample, and exhibit faster dynamics as a result. Importantly, all of the $1/\langle \tau \rangle$ in Fig. 5 are determined at fixed temperature above the respective T_g of each 435 polymer. Any differences in the average mobility of ether oxygens between the different systems, 436

therefore, are not captured by T_{g} , and these differences may explain the observed ionic conductivity behavior.

In addition to the clear importance of ether oxygen placement along the side-chain, the 439 relaxation time of a given POEM EO unit relative to that of PEO is strongly dependent of 440 temperature. In Fig. 5a, at $T-T_g = 50$ K, the mobility of the backbone and EO units near it are 441 442 several orders of magnitude slower than PEO at the same relative temperature, and only EO units 7-9 in POEM₉ have $1/\langle \tau \rangle$ equal to or greater than PEO. At 250 K above T_g , on the other hand, 443 the backbone only has two orders of magnitude longer relaxation time than PEO, and essentially 444 all ether units in the POEM systems relax as fast or faster than the linear PEO. This temperature 445 dependence is likely due to rapidly increasing dynamics of the POEM backbone with temperature. 446 As a reference point, the T_g of poly(methyl methacrylate), which is chemically equivalent to the 447 POEM without the polyether side-chain, is around 100 °C compared to -50 °C for PEO. The 448 dynamics of polymers tends to increase most rapidly at temperatures at and just above the glass 449 transition, with relatively more modest increases in mobility with temperature at large values of 450 $T-T_{g}$.⁵⁶ This same effect is evident in these graft polymer systems where the lower mobility 451 backbone sees much greater increase in local segmental dynamics than the already high mobility 452 453 side-chains with the same increase in temperature.

This local heterogeneity in segmental mobility may reconcile the discrepancy between κ/κ_{PEO} and σ_{nr} discussed earlier (Fig. 3). At intermediate $T-T_g$ the average mobility of the EO units in POEM is quite similar to that of PEO, and differences in T_g accurately capture the important dynamics in the system. As a result, after normalization by $T-T_g$, solvation site connectivity accurately captures the differences in conductivity as a function of POEM side-chain length. At high temperatures, many of the ether oxygens most often involved in ion complexation are more

mobile than the linear PEO, and the $T_{\rm g}$ of the graft system does not adequately describe the 460 important segmental dynamics. σ_{nr} therefore overpredicts the solvation site connectivity because 461 normalization by $T_{\rm g}$ fails to account for the fast ether oxygens at the side-chain ends. This effect 462 is more pronounced in the longer side chain materials, as there are more of these fast ether units 463 present. In POEM₃ even the furthest EO unit from the backbone is still affected by the main-chain 464 465 dynamics and is only marginally more mobile than PEO. In POEM₉, on the other hand, six of the nine side-chain oxygens exhibit faster local segmental mobility than PEO. Conversely, the 466 dynamics of many of the most commonly solvating ether units in POEM are considerably slower 467 than PEO at low temperatures. Here the ionic conductivity is limited by the slow dynamics of the 468 methacrylate backbone. In this case σ_{nr} falls short of the solvation site connectivity prediction 469 because the important dynamics in the system are slower than what is captured by the overall 470 material conductivity. Again, the POEM₃ is the system most negatively impacted by the low 471 mobility of the methacrylate backbone, whereas the highest index EO units of POEM₉ reach or 472 473 exceed the relaxation rate of PEO. These results suggest that local segmental dynamics of the polymer side-chain are at least as important as $T_{\rm g}$, ionic dissociation, and solvation site 474 connectivity in determining ionic conductivity in graft polyethers. Both backbone flexibility and 475 side-chain length are critical parameters in designing materials with rapid ionic transport. 476



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- Fig. 6. (a) Temperature dependent conductivity (experiment), (b) Ratio of Li⁺ ion MSD, and (c)
 inverse mean relaxation time in POEA₉ compared to POEM₉ (simulation).
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To validate this model for ion transport in graft polyethers, two more materials were 481 synthesized and characterized. POEA₉, the polyacrylate analogue to POEM₉, and a random 482 483 copolymer, POEM₉-*r*-PMMA, with the same x_{EO} as POEM₃ were synthesized by the same RAFT polymerization as described previously. The experimental conductivity, Li⁺ ion MSD vs time, and 484 local BVAF decorrelation times for POEA₉ and POEM₉-*r*-PMMA at r = 0.05 are shown in Fig. 6. 485 From Fig. 6a, we can see that the POEA₉ conductivity exceeds that of POEM₉ at low temperatures 486 by a factor of more than three, but the conductivity of the two systems converge above ca. 100 °C. 487 Although we measure the T_g of the two systems to be relatively similar (see Table 1), the 488 polyacrylate backbone should be more flexible than the polymethacrylate one, as T_{g} of poly(methyl 489 acrylate) is ca. 5 °C, well below that of polymethyl methacrylate. Previous bottle-brush copolymer 490 systems based on POEA have been shown to exhibit higher ionic conductivity than similar systems 491 incorporating POEM.⁵⁷ That the conductivity of these two systems converges at high temperature, 492 however, is consistent with the hypothesis that backbone dynamics become less significant to ion 493 494 transport at higher temperatures. At these elevated temperatures the difference between the relaxation times in the polyacrylate and polymethacrylate backbones is small, and the identical 495 nature of the two side chains results in similar ionic conductivity values. These experimental 496 497 observations are confirmed by MD simulations, where we find a similar temperature dependence in the ratio of Li⁺ ion MSD in POEA₉ to that in POEM₉ (Fig. 6b). At $T-T_g = 200$ K, the ratio of Li⁺ 498 ion MSD in POEM₉ to that of POEA₉ is 0.9 or greater, while at $T-T_g = 50$ K the ratio is ca. 0.7. 499 500 Additionally, as seen in Fig. 6c, the POEM₉ backbone relaxes significantly more slowly than the POEA₉ backbone at low temperatures, with $1/\langle \tau \rangle$ several orders of magnitude higher in the methacrylate polymer. This difference in backbone relaxation rate results in a persistently faster local relaxation rate in POEM compared to POEA at $T-T_g = 50$ K for all ether oxygens. At $T-T_g =$ 200 K, conversely, the backbone relaxation rates are identical in both systems, as are the dynamics of all ether oxygens in the two materials. Clearly, at these elevated temperatures the acrylate and methacrylate backbones both relax relatively quickly compared to the ether side-chain, and the effect of the backbone is minor in determining the material conductivity.



Fig. 7. (a) Temperature dependent conductivity (experiment), (b) Ratio of Li⁺ ion MSD, and (c)
inverse mean relaxation time in POEM₉-*r*-PMMA compared to POEM₃ and POEM₉ (simulation).

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A POEM₉-*r*-PMMA copolymer was synthesized with an ether oxygen fraction similar to that of POEM₃ to validate the importance of side-chain length—and not just x_{EO} —in determining conductivity. Fig. 7a shows the experimental conductivity for these two systems. The random copolymer exhibits consistently higher ionic conductivity, by approximately three-fold, irrespective of temperature. This behavior is not explained by the modest differences in measured T_g of the two systems, nor is it captured by differences in solvation site density and connectivity, which depends primarily on x_{EO} . Instead, this behavior can be explained only by the outsized

importance of EO units far from the backbone can have on ion transport within graft polymers. 519 Whereas the POEM₃ consists of densely packed but extremely short side-chains, the POEM₉-r-520 PMMA system contains a lower density of side-chains with mobile ether oxygens far from the 521 backbone. Although the presence of randomly distributed, nonconducting PMMA units clearly 522 disrupts the solvation network and negatively effects the material conductivity, this dilution effect 523 is significantly less severe than the absence of any long side-chains capable of rapid segmental 524 mobility. These findings are again confirmed by MD simulations. The ratio of Li⁺ ion MSD of 525 POEM₉-r-PMMA to POEM₃ (Fig. 7b) closely matches the ratio of experimentally determined 526 527 conductivity (ca. 2.6-3.2 from experiment, and 2.8 at 50 ns from simulation). The local segmental mobility analysis (Fig. 7c) similar validates this understanding of the differences between these 528 two materials. Although the connectivity between the solvation sites should be similar between 529 530 the two systems based on their similar ether oxygen content, the mobility of the POEM₉ is unperturbed by the presence of PMMA. The local mobility of the EO units furthest from the 531 backbone remain much more flexible than those in POEM₃, and as a result are capable of 532 facilitating more rapid ionic transport. 533

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535 Implications for the design of polyether-based polymer electrolytes

These results underscore the critical relationship between polymer dynamics and ion transport that must be understood when measuring and analyzing new ion conducting materials, particularly those based on short side-chain ether units. We have clearly demonstrated that a single value for T_g does not account for the local heterogeneity in oxygen mobility in these side-chain systems, and it does not fully capture the relevant dynamics for producing fast ionic transport. While there are differences in the T_g of the graft polyethers examined in this study, these

differences were negligible relative to the orders of magnitude different measured ionic 542 conductivities. The observed difference in ionic conductivity was largely related to segmental 543 dynamics, but DSC measurements failed to capture the local nature of these dynamics. The 544 discrepancy between segmental dynamics measured by DSC and simulations highlight the 545 importance of other experimental techniques, such as quasi-elastic neutron scattering, to probe the 546 relevant local dynamics of these systems.⁵⁸⁻⁶⁰ Moreover, the oxygens most likely to be involved 547 in solvation (*i.e.* those towards the side-chain ends) were more mobile than the polymer average, 548 giving rise to fast conduction without exhibiting a low T_{g} . On the other hand, materials that lack 549 550 those mobile oxygens due to having only short ether side-chains were limited by the relatively low mobility backbone. Though all materials studied here exhibit a glass transition well below room 551 temperature, it is not until around 150 K above T_g that the backbone begins to relax at a rate 552 comparable to the ether side-chains. As a result, many of the EO units close to the backbone are 553 prevented from effectively participating in the conduction mechanism. While side-chain mobility 554 555 directly controls the conductivity, the side-chain mobility itself is largely dependent on the backbone mobility. Tailoring the connection between the side-chain and backbone to maximize 556 flexibility offers a potential materials design opportunity to optimize the conductivity of these 557 558 systems.

More generally, although low T_g is conventionally used as a hallmark of a potential candidate for high ionic conductivity, this may not always be a good proxy, and more detailed descriptions of segmental dynamics are necessary. As demonstrated here, such descriptions can be best captured by a combined experimental and computational approach. Local relaxation times, in addition to conventional metrics, such as ether oxygen content, T_g , and ionic dissociation, as well more recently introduced quantifiers, such as solvation site connectivity, must be accurately modeled in order to fully capture the ionic transport behavior of graft polyether electrolytes. Most
importantly, it is the local mobility of the segments actively participating in the formation sites,
not the overall dynamics of the system, that appears to be critical in limiting the ion conductivity
of these materials.

Side-chain length has also been shown to be an important materials design criterion that 569 570 may apply to a broad range of polyether electrolytes. In linear polyether ion conducting polymers, ether oxygen content and T_{a} may be used to accurately predict the conductivity of a newly prepared 571 material. In systems where short PEO chains are connected to a polymer backbone, however, we 572 573 have demonstrated that the flexibility of the main chain and its effect on the mobility of side chain ether units, as well as the length of the PEO chains have an outsized effect on the overall ionic 574 conductivity. The role of backbone flexibility has significant implications for the development of 575 576 graft copolymers based on POEM or POEA repeat units that represent an important class of potential lithium battery electrolyte membranes with a wide potential design window.¹⁶ Even 577 broader polymer chemistry is available in the development of bottlebrush polymer electrolytes, 578 where the ion conducive side-chains can be incorporated by a graft-to or graft-through synthetic 579 approach.^{12,61,62} With this synthetic flexibility, the choice of backbone of chemistry and side-chain 580 581 linkages may be tailored to maximize ether side-chain dynamics, such as polysiloxane or polyphosphazene main chains.^{63,64} Another technologically relevant system that makes use of 582 short, periodically spaced PEO chains connected to less flexible moieties is crosslinked polyether 583 binder materials.⁶⁵ Further investigation is warranted to explore how these ideas of local ether 584 oxygen mobility affect conductivity in systems where ether chains are tethered at both ends, or in 585 the case of dynamic crosslinked networks, one or both chain ends is covalently linked to a 586 587 crosslinking site.²¹ Finally, dual ion-electron conducting polymers of interest for lithium ion

battery applications often make use of ether side-chains covalently bonded to an electronically conductive conjugated backbone.⁶⁶ In these systems, the ion conductivity will likely be significantly affected by the length of ether side chain and type of covalent linkage to the rigid thiophene backbone.²³ In these systems, and in all ion conducting polymers based on nonlinear polyethers, the interplay between polymer composition and architecture, backbone rigidity, and side-chain relaxation rates will play a critical role in determining the temperature dependent conductivity behavior.

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596 Conclusions

In this study we have clarified the relationship between side-chain length, ion solvation, 597 segmental dynamics, and ionic conductivity in graft polyether electrolytes. Ionic conductivity of 598 599 POEM₉ was found to be more than an order of magnitude higher than in POEM₃ even after correcting for differences in T_{g} . This behavior was partially explained by solvation site 600 connectivity, but a temperature dependence in the normalized conductivity could not be reconciled 601 by this approach. MD simulations and vibrational spectroscopy found that ions were fully 602 dissociated in all systems, but dissolved Li⁺ ions were found to preferentially reside in the ether 603 side chains, rather than associating with the carbonyl groups in the methacrylate backbone. 604 Moreover, ether units furthest from the backbone were most likely to coordinate with Li, 605 suggesting that these units have an outsized effect on the formation of solvation sites and in 606 607 facilitating ionic motion. Most importantly, these same ether oxygen atoms at side-chain ends exhibited much faster dynamics than those near the methacrylate backbone, and this effect 608 explained both the trend in conductivity as a function of side-chain length as well as the 609 610 temperature-dependent normalized conductivity behavior. These differences in C-O bond

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relaxation rates were not captured by differences in T_g , and therefore T_g alone may not be a good proxy for the relevant polymer dynamics resulting in high ionic conductivity in graft polymer electrolytes. Instead, the mobility of the EO segments that participate in solvation site formation is the most critical factor, and the dynamics of non-participating segments is secondary.

From the results presented here, several important design criteria can be proposed. First, 615 more mobile backbone moieties can be introduced to improve the low temperature conductivity of 616 graft polymer electrolytes. This was exemplified by comparing otherwise equivalent acrylate and 617 methacrylate graft polyethers, where the acrylate exhibited three-fold higher conductivity at room 618 619 temperature. This effect was minimal at higher temperatures, however, once the backbone dynamics approached those of the ether side-chains. Improvement to the conductivity at all 620 temperatures was shown in a random copolymer based on long side-chains compared to that of a 621 622 compositionally identical polymer with shorter side-chains. The important material parameter here was shown to be the presence of mobile oxygens at the side-chain ends, not the overall ether 623 oxygen content. Finally, the solvation properties and segmental dynamics should be considered 624 at a local, rather than global scale, when designing new ion conducting polymers based on short 625 Here, atomistic MD simulations, coupled with experimental characterizations, 626 EO chains. provided deeper insight into the important mechanisms of ion transport in these systems, and future 627 materials design may be accelerated by taking this combined approach. 628

629

630 Experimental Methods

631 Materials

PEO was purchased from Polymer Source, Inc. and dried in an argon glovebox antechamber at 50 632 °C overnight before use. All other chemicals-acetonitrile (99.8%, anhydrous), toluene, 633 dimethylformamide (DMF), tetrahydrofuran (THF), hexanes, diethyl ether, LiTFSI (battery grade, 634 >99.95% 2-cyano-2-propyl 635 trace metal basis), dodecyl trithiocarbonate (CPDTC), azobisisobutyronitrile (AIBN), and all monomers-were purchased from Sigma Aldrich. 636 Oligo(ethylene oxide) methyl ether methacrylate (OEM_x, where x = 3, 5, or 9; $M_n = 232$, 300, or 637 500 g mol⁻¹), methyl methacrylate (MMA), and oligo(ethylene oxide) methyl ether acrylate (OEA₉, 638 $M_{\rm n}$ = 475 g mol⁻¹) were purified of inhibitor before use by passing through a column of basic 639 alumina. LiTFSI was further under vacuum at 100 °C for 48 h. Polymers and LiTFSI were stored 640 in an argon glovebox after the drying processes. AIBN was recrystallized in ethanol before use. 641

Synthesis of POEM_x and POEA₉ homopolymers- POEM_x and POEA₉ homopolymers were 642 prepared by RAFT polymerization according to Scheme S1. For the synthesis of POEM₉, 5 g (10 643 mmol) of OEM₉ monomer was placed in a round bottom flask along with 0.17 g (0.5 mmol) 644 CPDTC, 8.2 mg (0.05 mmol) of AIBN, and 9.8 mL of DMF. The flask was sealed with a rubber 645 septum and the solution sparged with dry N₂ for 30 minutes. The flask was then placed in an oil 646 bath at 70 °C for 20 hours, after which it was quenched in an ice water bath. The crude reaction 647 mixture was concentrated under vacuum and then diluted with THF. This polymer was then 648 649 precipitated from cold diethyl ether or a mixture of diethyl ether and hexanes. This purification process was repeated three times, or until ¹H-NMR spectra showed no residual monomer in the 650 material. Purified polymer was then dried in a vacuum oven to a constant mass and then further 651

dried under high vacuum for 24 hours before storing in an argon glovebox. The otherhomopolymers were prepared in a similar manner.

654 *Synthesis of POEM-r-PMMA random copolymer-* $POEM_9$ -*r*-PMMA was synthesized according 655 to Scheme S2 following the same general procedure as the homopolymer materials. 3.5 g (7 mmol) 656 of OEM₉, 1.5 g (15 mmol) of MMA, 0.17 g (0.5 mmol) CPDTC, 8.2 mg (0.05 mmol) of AIBN, 657 and 9.8 mL of DMF were combined in a round bottom flask, sealed with a rubber septum, sparged 658 with dry N₂, and placed in a 70 °C oil bath for 20 hours. The crude solution was purified by the 659 same process as the homopolymers. The ratio of OEM₉:MMA in the resulting polymer was 660 determined by ¹H-NMR. The NMR spectrum and peak comparison is Fig. S8.

661 *Polymer electrolyte solution preparation-* Polymer solutions were prepared inside of an argon 662 glovebox by dissolving polymer in either pure acetonitrile or a mixture of acetonitrile and toluene 663 (50/50 v/v). Solutions were heated to 50 °C to help facilitate dissolution of the polymer and then 664 were left stirring overnight. LiTFSI in acetonitrile solutions were prepared in the same manner. 665 Polymer electrolyte solutions were prepared by blending polymer and salt solutions at an 666 appropriate volumetric ratio to obtain a ratio of r = 0.05 = [LiTFSI]/[EO].

667

668 Materials Characterization

669 *Size exclusion chromatography (SEC)*- Size exclusion chromatography (SEC) measurements 670 were conducted on a Shimadzu Prominence High Performance Liquid Chromatograph system with 671 THF as eluent at a flow rate of 1 mL/min. Separation was achieved using two PLgel mixed-D 672 columns (Agilent) maintained at ambient temperature. The differential refractive index signal was 673 collected using a Wyatt Optilab T-rEX differential refractometer ($\lambda = 658$ nm). On-line multi-674 angle light scattering (MALS) measurement was performed using a Wyatt Dawn Heleos II light scattering detector. Weight-averaged molecular weight and dispersity were determined by MALS using the previously reported refractive index increment for POEM9 in THF (dn/dc = 0.073mL/g).⁶⁷

Determination of copolymer composition by ¹**H-NMR-** POEM₉-*r*-PMMA copolymer composition was determined by ¹H-NMR in CDCL₃. Data were acquired on a 500 MHz Bruker Avance-II+ spectrometer equipped with a ¹H QNP probe, using Topspin 2.1. Copolymer composition was determined by comparing the methacrylate backbone methyl group peaks ($\delta =$ 0.7 – 1.5 ppm) to the methyl ether peaks at the end of the POEM₉ side-chain ($\delta = 3.38$ ppm).⁶⁸ The copolymer was determined to have a POEM₉ mole fraction of 0.273.

Differential Scanning Calorimetry- Calorimetric glass transition temperatures (T_g) of neat 684 polymers and polymer electrolytes were determined by DSC using a TA Instruments Discovery 685 2500 DSC. Sample pans were prepared in the glovebox by drop casting solutions, heating at 65 $^{\circ}$ C 686 until dry, and then repeating until 5 - 10 mg of material was in the pan. The pans were then 687 hermetically sealed before removing from the glovebox to avoid any water adsorption before DSC 688 measurement. Samples were conditioned at 135 °C followed by three cycles of cooling to -85 °C 689 and heating to 135 °C at a scan rate of 10 °C/min. T_g is reported as the inflection point of the heat 690 flow thermograms taken from the third heating curve (shown in Fig. S3). 691

Vibrational Spectroscopy- Samples for Fourier Transform Infrared (FTIR) measurements were prepared on Au-coated Si substrates by spin coating. Samples were prepared inside of a glovebox, annealed at 135 °C for 15 minutes, and sealed then until immediately before measurement to minimize water absorption. Measurements were performed using a Shimadzu IRTracer-100 spectrometer using a diamond prism for attenuated total reflection (ATR) at ambient temperature from 400 – 4000 cm⁻¹ at a resolution of 4 cm⁻¹. Raman samples were prepared by drop casting films on Au-coated Si substrates inside of a glovebox. Films were dried and then annealed at 135
°C for 15 minutes inside of the glovebox and then sealed until measurement. Raman experiments
were performed using a Horiba LabRAM HR Evolution NIR confocal Raman microscope. Raman
spectra were collected with a 100x objective and a 633 nm wavelength laser.

Thin film conductivity measurements- Polymer electrolyte conductivity was determined by 702 electrochemical impedance spectroscopy (EIS) of thin films on interdigitated electrodes (IDEs) as 703 described previously.⁶⁹ Briefly, IDEs are microfabricated by photolithography on top of thermal 704 oxide Si wafers. 5 nm of Ti followed by 45 nm of Au are deposited in the lithographically defined 705 electrode area, and excess metal is removed by liftoff in warm *n*-methyl pyrrolidone. IDEs are 706 designed with N = 160 electrodes, l = 1 mm of electrode overlap, w = 2 µm electrode width, and d 707 = 8 μ m interelectrode distance. IDEs were then coated with 0.8 nm of SiO₂ by plasma-assisted 708 709 atomic layer deposition to inhibit dewetting of the polymer films. Polymer electrolyte thin films were cast onto the IDEs by spin coating at 4000 rpm inside of the glovebox, followed by drying 710 on a hot plate at 70 °C before EIS measurements. Polymer film height (h) was determined by 711 casting an identical film on a Si wafer and performing ellipsometry (J.A. Woollam alpha-SE 712 ellipsometer). IDEs were placed on a custom heating stage in the glovebox and connected to a 713 Gamry 600+ potentiostat by tungsten probe tips. Potentiostatic EIS was performed with an applied 714 amplitude of 100 mV over a frequency range of 1 MHz to 1 Hz. EIS data is fit to an appropriate 715 equivalent circuit that models the physical process of thin film-IDE systems using the Gamry E-716 717 chem Analyst software, and the resulting film resistance (R_f) is used to find the conductivity (σ) by eq. 3.⁷⁰ All conductivity data is reported as the average of three samples, with error bars 718 representing the standard deviation. 719

720
$$\sigma = \frac{d}{R_f (N-1) lh}$$
(2)

721

722 Molecular Dynamics Simulations

The polymers are represented by united atoms, using an adapted Trappe-UA force-field⁷¹⁻⁷³ that 723 has been previously validated to match the density of PEO⁷⁴. Li⁺ and TFSI⁻ ions are represented 724 by a compatible all-atom model⁷⁵. A cutoff radius of 12 Å is used for short range non-bonded 725 interactions. Long range non-bonded interactions use a cutoff radius of 12 Å and are handled using 726 the Particle-particle particle-mesh solver⁷⁶ with 10⁻⁴ accuracy. The simulation is conducted using 727 the LAMMPS package⁷⁷. The velocity-Verlet integrator with a 1 fs timestep is used. For NVT 728 729 simulations, the Nose-Hoover thermostat with a damping parameter of 100 fs is used. For NPT simulations, the Nose-Hoover barostat with a damping parameter of 1000 fs is used. Additional 730 details of the simulation procedures and force field parameters are included in the Supporting 731 732 Information.

733

734 Conflicts of Interest

735 There are no conflicts to declare.

736

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748				
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