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## **The CH(X2Π) + H2O Reaction: Two Transition State Kinetics**



SCHOLARONE<sup>"</sup><br>Manuscripts

#### **The CH(X<sup>2</sup>) + H2O Reaction: Two Transition State Kinetics**

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#### **Abstract**

The reaction of ground state methylidyne (CH) with water vapor  $(H_2O)$  is theoretically reinvestigated using high-level coupled cluster computations in combination with semi-classical transition state theory (SCTST) and two-dimensional master equation simulations. Insertion of CH into a H-O bond of H<sub>2</sub>O over a submerged barrier via a well-skipping mechanism yielding solely H and CH<sub>2</sub>O is characterized. The reaction kinetics is effectively determined by the formation of a pre-reaction van der Waals complex (PRC,  $HC$ — $OH<sub>2</sub>$ ) and its subsequent isomerization to activated  $CH<sub>2</sub>OH$  in competition with PRC re-dissociation. The tunneling effects are found to be minor, while variational effects in the PRC  $\rightarrow$  CH<sub>2</sub>OH step are negligible. The calculated rate coefficient  $k(T)$  is nearly pressure-independent, but strongly depends on temperature with pronounced down-up behavior: a high value of  $2 \times 10^{-10}$  cm<sup>3</sup>  $s^{-1}$  at 50 K, followed by a fairly steep decrease down to  $8\times10^{-12}$  cm<sup>3</sup> s<sup>-1</sup> at 900 K, but increasing again to  $5 \times 10^{-11}$  cm<sup>3</sup> s<sup>-1</sup> at 3500 K. Over the *T*-range of this work,  $k(T)$  can be expressed as:

$$
k(T, P=0) = 2.31 \times 10^{-11} (T/300 \text{ K})^{-1.615} \exp(-38.45/T). \text{ cm}^3 \text{ s}^{-1} \text{ for } T = 50 - 400 \text{ K}
$$
  

$$
k(T, P=0) = 1.15 \times 10^{-12} (T/300 \text{ K})^{0.8637} \exp(892.6/T). \text{ cm}^3 \text{ s}^{-1} \text{ for } T = 400 - 1000 \text{ K}
$$
  

$$
k(T, P=0) = 4.57 \times 10^{-15} (T/300 \text{ K})^{3.375} \exp(3477.4/T). \text{ cm}^3 \text{ s}^{-1} \text{ for } T = 1000 - 3500 \text{ K}.
$$

## **I. INTRODUCTION**

Methylidyne (CH) is a highly reactive intermediate in the combustion of methane (CH<sub>4</sub>) and other hydrocarbons.<sup>1-4</sup> Its high reactivity towards closed-shell molecules is owed in part to the vacant p-orbital on the C atom. CH in hydrocarbon flames has been shown to be responsible for the formation of chemiions by its reaction with O atoms<sup>4</sup> – the basis of the Flame Ionization Detector – and to be the source of prompt NO by its reaction with  $N_2$ ,<sup>5</sup> while it was also identified as the source of chemi-luminescent OH by its reaction with  $O_2^6$  – an important diagnostic tool in combustion studies. As water vapor (H<sub>2</sub>O) is a principal product from combustion processes, CH can in principle react fairly fast with H2O in a combustion environment, a reaction that could be a major loss process of CH in flames, in particular in fuel-rich conditions. Surprisingly, this reaction has not gained much attention; to the best of our knowledge, there are no reported experimental kinetics results at combustion temperatures. Both CH and H<sub>2</sub>O have been detected in the interstellar medium,<sup>7, 8</sup> where the reaction between CH and H<sub>2</sub>O can be expected to yield formaldehyde  $(CH<sub>2</sub>O)<sub>9</sub>$ 

$$
CH(X2II) + H2O = CH2O + H
$$
\n(1)

There are a number of experimental studies that have reported reaction rate constants over a temperature range between 50 K and  $725$ ;<sup>9-12</sup> all of these investigations found that the rate coefficient exhibits a negative temperature-dependence. The experimental results in the 300-725 K range can be divided in a set of lower rate constants and a set of higher rate constants, <sup>9-12</sup> the two sets differing by a factor of about 2.5.9-12 The reason for this discrepancy is unclear, although the notorious difficulty to accurately establish or measure gas-phase  $H_2O$  concentrations could be a cause. Given that this reaction plays an important role in areas as diverse as combustion- and astrochemistry, further experimental studies as well as high-level theoretical calculations are warranted to resolve the above disagreement and to extend the temperature range for  $k(T)$ . There are several early quantum chemical and theoretical kinetics studies or interpretations, 9, 11, 13-15 which characterized a barrier-less insertion mechanism through a fairly stable pre-reactive complex (PRC), consistent with the experimental negative temperaturedependence of the  $k(T)$  rate coefficient.<sup>9-12</sup> Blitz et al.<sup>10</sup>, relying in part on the quantum chemical result of Wang et al.<sup>15</sup> that the transition state for the actual insertion (TS1) is submerged for 6 kcal/mol, proposed that the reaction is controlled solely by the formation of the PRC; in their reasoning, the variational transition state (TS0) for formation of the PRC is very loose at low temperatures resulting in a high rate, whereas TS0 becomes gradually tighter at higher temperatures such that the rate decreases. Bergeat et al.<sup>11</sup> considered a two-transition state model, with TS0 and TS1 controlling the rate, and calculated the rate coefficient  $k(T)$  using a master-equation technique.<sup>11</sup> They concluded that to fit the 'lower' experimental  $k(T)$  set<sup>10, 11</sup> required a TS1 energy of  $-1.7$  kcal/mol relative to the reactants, whereas the 'higher'  $k(T)$  set required TS1 submerged for  $-3.9$  kcal/mol, showing in any case that the energy of TS1 is an important quantity in co-determining the rate of the title reaction, even at moderately high  $temperatures.<sup>11</sup>$ 

The first aim of this work is to use high-level coupled cluster calculations to construct the potential energy surface, focusing in particular on accurate energetics as well as vibration-rotation characteristics of TS1 which co-controls the rate already at moderate temperatures as shown by Bergeat et al.; <sup>11</sup> this will be combined with a proper variational treatment of TS0 for the barrier-less association entrance channel. Our second objective is to solve an *E,J*-resolved (two-dimensional) master equation in the frame of the two-TS model, in order to obtain rate constants as a function of both temperature and pressure. In this way we aim to provide highly accurate rate constants from first principles which can be compared with the experimental data and to extend the temperature range where *k*(*T*) data are available to 3500 K for high-temperature combustion modeling involving the CH radical.

### **II. THEORETICAL METHODOLOGY**

#### **II.1. Coupled Cluster Quantum Chemical Calculations**

All key stationary points on the lowest-lying doublet electronic potential energy surface for the reaction of CH and H<sub>2</sub>O were fully optimized using a frozen core  $CCSD(T)/aug-cc-pVTZ$  level of theory.16-18 Vibrational analyses were then done to confirm if the stationary points characterized are either a minimum (with all positive frequencies) or a transition state (with only one imaginary frequency that corresponds to the reaction coordinate). Anharmonic calculations were performed using the same level of theory to obtain anharmonic zero-point vibrational energy (ZPE), anharmonic constants, and rovibrational parameters for the following kinetics simulations. To obtain highly accurate relative energies, series of single-point energies with coupled cluster methods were then performed using a modification of the mHEAT-345(Q)<sup>19</sup> method reported recently (defined hereafter as amHEAT-345(Q)). Specifically, we have replaced cc-pVXZ basis sets<sup>20</sup> in the original mHEAT method by aug-cc-pVXZ basis sets<sup>20</sup> (where  $X = T$ , O, and 5). Such a modification may be essential for chemical species having an unpaired electron and for long range interactions. The amHEAT-345(Q) is a composite method in which the energy is given as a sum of separately evaluated contributions:<sup>19</sup>

$$
E_{mHEAT} = E_{SCF}^{\infty} + \Delta E_{CCSD(T)}^{\infty} + \Delta E_{T-(T)} + \Delta E_{(Q)-T} + \Delta E_{core} + \Delta E_{ZPE} + \Delta E_{DBOC} + \Delta E_{Scalar} + \Delta E_{SO}
$$
 (2)

where  $E_{SCF}^{\infty}$  is the Hartree-Fock energy extrapolated to a complete basis set (CBS) limit using aug-ccpVXZ<sup>20</sup> (with X = T, Q, and 5) basis sets;  $\Delta E_{CCSD(T)}^{\infty}$  is the electron correlation energy calculated in the frozen-core approximation with the CCSD(T) method<sup>16-18</sup> and extrapolated to a CBS limit using aug-ccpVXZ (with X = Q and 5);  $\Delta E_{T-(T)}$  is the energy difference of CCSDT and CCSD(T) calculations based on the cc-pVTZ basis set;  $\Delta E_{(Q)-T}$  is the energy difference of CCSDT(Q)<sup>21</sup> and CCSDT calculations

using the cc-pVDZ basis set;  $\Delta E_{core}$  is the core correlation correction;  $\Delta E_{ZPE}$  is the anharmonic zero-point vibrational energy obtained in the framework of second-order vibration perturbation theory (VPT2);<sup>22</sup>  $\Delta E_{DBOC}$  is the diagonal Born-Oppenheimer correction;  $\Delta E_{Scalar}$  is the scalar relativistic effect; and  $\Delta E_{SO}$  is the spin-orbit correction.

Further details of amHEAT have been documented elsewhere.<sup>19</sup> As seen in Figure 1, amHEAT calculations yield accuracies better than 0.2 kcal/mol as compared to benchmark ATcT values<sup>23</sup> for the reaction enthalpies; comparable accuracy can be expected for other species. Unless mentioned otherwise, all calculations were done using the CFOUR quantum chemistry package.<sup>24, 25</sup>

#### **II.2. E,J-Resolved Master Equation Analysis**

To be shown in next section, the chemical kinetics of the title reaction is effectively controlled by the formation step of pre-reactive complex (PRC),  $HC^{8+}$ — $^{8}OH_2$ , and its isomerization into CH<sub>2</sub>OH. The most important portion of the potential energy surface (PES) that kinetically controls the reaction is given in Scheme 1.

$$
\rm CH + H_2O\frac{{\rm k_{CH\rightarrow PRC}(E,J)}}}{{\rm k_{PRC\rightarrow CH}(E,J)}} \xrightarrow{\rm k_{PRC\rightarrow CH2OH}(E,J)} \rm CH_2OH^* \xrightarrow{\rm Very\,fast} CH_2O + H
$$

#### **Scheme 1:** Effective chemical kinetics scheme for the title reaction.

An *E,J*-resolved two-dimensional master equation that describes the time evolution for the competition of decompositions of PRC and energy transfer processes through collisions of PRC with buffer gas is given by:26-34

$$
\frac{\partial C_{PRC}(E_m J_m)}{\partial t} = \sum_{J_n=0}^{J_{max}} \sum_{E_{m=0}}^{E_{max}} P_{PRC}(E_m J_m | E_n J_n) \cdot \omega \cdot C_{PRC}(E_n J_n) \cdot dE_n - \omega \cdot C_{PRC}(E_m J_m) -\{k_{PRC \to CH}(E_m J_m) + k_{PRC \to H_2\text{COH}}(E_m J_m)\} \cdot C_{PRC}(E_m J_m) + OST(E_m J_m)
$$

$$
(3)
$$

In Eq. 3,  $J_{max}$  is the maximum angular momentum;  $E_{max}$  is the maximum internal energy;  $C_{PRC}(E_mJ_m,t)$ represents the (time-dependent) mole fractions of PRC in state  $(E_m J_m)$  and time t;  $\omega_{LI}$  (in s<sup>-1</sup>) is the Lennard-Jones collisional frequency;<sup>35-37</sup> and  $k_{PRC \to H_2COH}(E_m J_m)$  (in  $s^{-1}$ ) is the  $(E_m J_m)$ -resolved microcanonical rate coefficient for the isomerization step of PRC to CH<sub>2</sub>OH.  $P_{PRC}(E_mJ_m|E_nJ_n)$  is the *E,J*-resolved collisional transfer probability distribution function of PRC from state  $(E_n, J_n)$  to state  $(E_m,$  $J_m$ ). OST stands for the original source term, and is given by:<sup>38-41</sup>

$$
OST(E_mJ_m) = F_{PRC}(E_mJ_m) \cdot k_\infty(T) \cdot [CH] \cdot [H_2O],\tag{4}
$$

where  $k_{\infty}(T)$  is the *capture rate constant* – that can be calculated using micro-variational transition state theory ( $\mu$ vTST)<sup>42-45</sup> (see Eq. 6 below) – for the barrier-less association step of CH and H<sub>2</sub>O leading to PRC.  $F_{PRC}(E_mJ_m)$  is the *E,J*-resolved initial distribution function for the nascent energized PRC and given by: $38, 41$ 

$$
F_{PRC}(E_m J_m) = \frac{(2J_m + 1) \cdot k_{PRC \to CH}(E_m J_m) \cdot \rho_{PRC}(E_m J_m) \cdot \exp(-E_m / RT)}{\sum_{J_m=0}^{J_{max}} (2J_m + 1) \int_{E_i=0}^{E_{max}} k_{PRC \to CH}(E_m J_m) \cdot \rho_{PRC}(E_m J_m) \cdot \exp(-E_m / RT) \cdot dE_m},
$$
\n(5)

In Eq. 5,  $\rho_{PRC}(E_mJ_m)$  is the density of ro-vibrational states for PRC, and  $k_{PRC\rightarrow CH}(E_mJ_m)$  is the microcanonical rate constant for the PRC  $\rightarrow$  CH + H<sub>2</sub>O step, which is calculated using micro-variational TST.45, 46

$$
k_{\infty}(T) = \frac{\sigma}{h} \times \frac{Q_{tr}^{*} Q_{e}^{*}}{Q_{CH}^{re} Q_{H_{2}O}^{re}} \times \sum_{J=0}^{\infty} (2J+1) \int_{0}^{\infty} Min[G_{rv}^{*}(E,J)] \times \exp\left(-\frac{E}{k_{B}T}\right) dE
$$
 (6)

where h is Planck's constant,  $k_B$  is Boltzmann's constant, and  $\sigma=2$  is the reaction path degeneracy. T is the reaction temperature and E is the total internal energy.  $Min(G(E, J))$  stands for minimizing the chemical reaction flux at each pair of *E* and *J*.  $Q_{CH}^{re}$  and  $Q_{H_2O}^{re}$  are the complete partition functions for CH and H<sub>2</sub>O, respectively, but without the symmetry number in the rotational partition function of H<sub>2</sub>O. Q<sub>tr</sub> is the translational partition function, and  $Q_e$  is the electronic partition function of the TS (the superscripts "re" and "≠" designate reactants and transition state (TS), respectively). Electronic partition functions for all stationary points are equal to 2 for a doublet electronic state.  $G_{rv}^{\neq}$  is the sum of ro-vibrational quantum states of the TS for the given *E* and *J*, which can be obtained from its vibrational counterpart using the *J*shifting approximation, <sup>47-49</sup> Eq. 7:

$$
G_{rv}^{\neq}(E,J) = \sum_{K=-J}^{K=-J} G_{v}^{\neq}(E - E_{r}(J,K))
$$
\n(7a)

$$
\rho_{rv}(E,J) = \sum_{K=-J}^{K=+J} \rho_v(E - E_r(J,K))
$$
\n(7b)

In Eq. 7,  $G_v^{\neq}$  is the anharmonic (coupled) vibrational sum of states of TS that is calculated using Miller's semiclassical TST (SCTST) theory<sup>50-54</sup> on the basis of the Wang-Landau algorithm.<sup>55-58</sup> The SCTST theory50-54 automatically includes coupled anharmonic vibrations and multi-dimensional quantum mechanical tunneling.  $E_r$  is the (external) rotational energy level of TS, which is approximated by a symmetric top,  $59$  Eq. 8:

$$
E_r(J,K) = J(J+1)\overline{B} + (A-\overline{B})K^2
$$
, with  $\overline{B} = \sqrt{B \cdot C}$  and  $-J \le K \le +J$  (8)

It is worthy to emphasize that for  $CH(X<sup>2</sup>II)$  when  $T < 100$  K in astronomical environments, there is a strong coupling of the 2D rotation and the electronic motion. Thus, the rotational energy values of the components of doublet states of CH were computed using Hill and Van Vleck's formalism.60-62 The coupled rotational-electronic partition function of CH was then obtained through the direct state count, Eq. 9.

$$
Q_{elec\_rot}^{CH}(T) = \sum_{i} n_i e^{-E_i/RT}
$$
\n(9)

where  $n_i$  is the degeneracy number and  $E_i$  is the  $i^{th}$  eigenvalue.

All parameters (including collisional energy transfer, maximum energy, energy grain, and total angular momentum) used in the master-equation simulation are provided in Table S1 in the Supplementary Material. Given that the title reaction is only slightly pressure-dependent as shown in Fig. 3, the calculated rate coefficients in the pressure range of interest are only marginally influenced by the collisional parameters selected.

#### **II.3. Variational Treatment for TS1**

TS1 is a tight, well-defined transition state. As already mentioned above, Miller's SCTST theory is used to compute rate constants passing through TS1. However, it is well known that Miller's SCTST theory does not explicitly take variational effects into account. The variational effects are expected to reduce the chemical reaction flux via TS1, thus decreasing the overall rate constants. In this work, the variational effects are estimated by computing a ratio of rate constants with and without variational treatments, Eq. 10.

$$
f_{ve}(T) = \frac{k_{with}(T)}{k_{without}(T)}\tag{10}
$$

The variational treatment requires a minimum energy path along the reaction coordinate (RC) as well as ro-vibrational parameters of grid points on the RC.<sup>63</sup> In this work, the intrinsic reaction coordinate (IRC) was first computed using the UB97-1/6-311G $(d,p)^{64}$  level of theory. Harmonic vibrational frequency calculations with projecting out the  $RC^{65}$  were then performed using the same UB97-1 level of theory to obtain ZPEs and ro-vibrational parameters for grid points on the RC. Relative energies were next refined using CCSD(T)/aug-cc-pVTZ single-point energy calculations based on the UB97-1 geometries (see Fig. S1 in the Supplementary Material).

From these data, both  $k_{with}(T)$  and  $k_{without}(T)$  can be computed at the low-pressure limit (LPL) using Eq. 11 (see below). Ratios  $(f_{ve}(T))$  as a function of temperature (displayed in Fig. S2 in the Supplementary Material) show that the variational effects are found to be negligibly small, less than -2% for the entire temperature range considered in this work. The rationalization is that TS1 presents a sharp potential energy maximum (see Fig. S1), the imaginary frequency being  $i \times 1503$  cm<sup>-1</sup>. So, in the results discussed below these variational effects are neglected.

#### **III. RESULTS AND DISCUSSION**

#### **III.1. Potential Energy Surface (PES)**

Figure 1 displays the important reaction pathways for the reaction between CH and  $H_2O$ . The first step is the barrier-less association leading to a pre-reactive complex (PRC), which has a binding energy of  $-8.93$  kcal/mol. This PRC (HC<sup> $\delta$ +</sup>—<sup>- $\delta$ </sup>OH<sub>2</sub>) is formed by a polar interaction of a lone pair orbital of the O atom and an empty p-orbital of the C atom. Subsequently, the PRC can isomerize to CH<sub>2</sub>OH by insertion of CH into an O-H bond of  $H_2O$  through transition state TS1, in competition with re-dissociation of the PRC into the reactants. TS1 lies 1.43 kcal/mol below the initial reactants, such that the insertion of CH into H2O is overall a barrier-less process. Important to note is the 1D hindered internal rotation (1DHR) of the  $H_a$  atom of the  $H_aOH_b$  moiety about the O-H<sub>b</sub> axis, with  $H_b$  the shared atom (see Fig. 1); this results in a second, non-equivalent minimum at  $-1.16$  kcal/mol, as shown in the hindered rotation PES as function of the rotation angle in Fig. S3. The quantum states of the 1DHR mode were found by solving the Schrödinger equation using the Multiwell program suite,<sup>62</sup> and its integrated sum of states  $G_v(E)$  was convoluted with the anharmonic (coupled) vibrational sum of accessible states of the other modes. The CH2OH\* produced has a high vibrational excitation energy of about 87 kcal/mol, thus quickly decaying to  $H + CH<sub>2</sub>O$  via H-loss. The H-elimination to yield  $H + CH<sub>2</sub>O$  can occur directly via TS4 or indirectly after conversion to CH3O. All three barriers of TS2, TS3, and TS4 lie very low in energy as compared to the

available internal energy of  $CH_2OH^*$ , so  $CH_2OH^*$  and  $CH_3O^*$  are highly unlikely to be thermalized by collisions unless at very high pressures of >100 atm. As a result, the roles of the intermediates  $CH_2OH/CH_3O$  are kinetically unimportant; such a mechanism is known as well-skipping.  $CH_2OH^*$  might decompose via TS5 for H<sub>2</sub>-loss leading to H<sub>2</sub> + HOC, but this pathway must overcome a high barrier of 83.5 kcal/mol and is therefore negligible and irrelevant.

#### **III.2. Reaction Rate Coefficients**

 As explained above, the mechanism and kinetics of the title reaction are effectively governed by the initial step of CH + H<sub>2</sub>O  $\rightarrow$  PRC (HC<sup> $\delta$ +</sup>—<sup>- $\delta$ </sup>OH<sub>2</sub>) through the variational entrance TS0 and PRC isomerization through TS1 to yield  $CH<sub>2</sub>OH<sup>*</sup>$  (see Figure 1) in competition with PRC re-dissociation through TS0, a prototype of the 2-TS kinetics model.<sup>66-68</sup> It is fairly well established<sup>10</sup> that formation of the PRC through the loose, variational TS0, governed by the long-range interaction between CH and  $H_2O$ , limits the reaction kinetics at low to moderate temperatures, while the isomerization of PRC over the submerged TS1 — with its higher total number of accessible ro-vibration states — far outruns redissociation of the PRC through TS0. So, a proper variational treatment of the bottleneck TS0 is desired to obtain highly accurate rate constants. For the tight inner TS1, Miller's SCTST theory is used to compute  $k_{\text{PRC}\rightarrow\text{CH2OH}}(E,J)$ , while microvariational TST theory is used to locate the kinetic bottleneck TS0 and to obtain  $k_{\text{CH}\leftrightarrow\text{PRC}}(E,J)$  by minimizing the chemical reaction flux. Figure 2 presents the minimumenergy path for the barrier-less association of CH and  $H_2O$  yielding the PRC, constructed using CCSD(T)/aug-cc-pV5Z calculations based on the CCSD(T)/aug-cc-pVTZ geometry. In addition, the electron correlation corrections from fully triple electron excitations (with CCSDT/cc-pVTZ) and noniterative quadruple electron excitations (with CCSDT(Q)/cc-pVDZ) were also included. A temperature of 50 K was chosen as lower limit for the microvariational treatment of TS0, because at even lower temperatures the interaction between CH and  $H<sub>2</sub>O$  is very long-range, such that TS0 becomes too loose to be described by a rigid-rotor, harmonic oscillator model. Calculation of the tunneling factor, which is

always small,  $\leq 1.5$ , is incorporated in the SCTST implementation. The  $k(T,P)$  results described below were not corrected for the very small variational effect (see Methodologies section), which is always less than  $2\%$  (see Fig. S2).

Figure 3 shows fall-off curves for  $k(T, P)$  for T = 50 to 1000 K and P = 1 to 10<sup>6</sup> Torr, obtained by solving the *E,J*-resolved master equation (3). As seen, the reaction is marginally pressure-dependent up to about 1 atm, on account of the short lifetime of the PRC complex, about 0.1 ns, due to the fast PRC  $\rightarrow$  $CH<sub>2</sub>OH*$  step. The difference between 1 Torr to 1000 Torr is found to be less than 5%. It is therefore concluded that the reaction is practically in the low-pressure limit where an *exact* solution of the twodimensional master equation can be obtained, as given by: $69, 70$ 

$$
k_{LPL}(T, P = 0) = \frac{\sigma}{h} \times \frac{Q_{tr}^{\neq} Q_e^{\neq}}{Q_{CH}^{re} \cdot Q_{H_2O}^{re}} \times \sum_{J=0}^{\infty} (2J+1) \int_0^{\infty} \frac{Min(G_0^{\neq}(E,J)) \times G_1^{\neq}(E,J)}{Min(G_0^{\neq}(E,J)) + G_1^{\neq}(E,J)} \times \exp\left(-\frac{E}{k_B T}\right) dE
$$
\n(11)

where  $Min(G_0^{\neq}(E,J))$  stands for the minimum value of the sum of ro-vibration states  $G_0^{\neq}(E,J)$  for the variational TS0 along the reaction path for given E,J, and  $G_1^{\neq}(E,J)$  is the sum of ro-vibrational states of TS1 for given *E,J*.e

However, the reaction strongly depends on temperature; and is found to exhibit negative temperature-dependence up to about 900 K, thus being consistent with the experimental data.<sup>9-12</sup> Figure 4 shows the calculated rate coefficient, using eq. (11), not corrected for the negligible variational effect of TS1, for a wide temperature range between 50 K and 3500 K, which covers most practical applications from chemistry in interstellar clouds to combustion. Figure 4 shows that the negative temperature dependence of the rate coefficient holds up only to about 900 K, where *k*(*T, P=0*) reaches a minimum, above which it increases markedly with temperature. This new finding has important implications for the combustion chemistry of the CH radical. This behavior is explained as follows — referring also to Fig. S4 which shows additionally the hypothetical  $k(T, P=0)$  if solely TS1 were to limit the reaction rate at all  $T$ ,

i.e. if TS0 were to possess an infinite number of ro-vibration states. In the low-to-moderate temperature regime, the forward chemical reactive flux to the PRC via the loose, variational, outer TS0 is the ratedetermining step, such that the rate coefficient decreases with temperature as TS0 becomes more rigid at higher temperature. Starting from about 300 K, TS1 begins to take some control of the reaction together with TS0, i.e. part of the PRC re-dissociates, further depressing the reaction rate; the reason for this is the higher rigidity of TS1 compared to TS0. At about 900 K,  $k(T)$  bottoms out and above 1000 K, the more rigid TS1 becomes the sole rate-limiting transition state, while at the same time *k*(*T*) increases again with temperature, because once  $T > 1000$  K, the 1DHR mode with its closely spaced lower eigenvalues (see Fig. S3), the bending vibration modes and the  $C-O$  stretch of TS1 are or become activated, increasing the partition function *Q* of TS1 faster than that of the reactants with only one bending mode and 5 relative rotation and translation modes for which *Q* increases only as *T* 5/2 .

Figure 4 shows that the calculated rate constants support the high experimental values of  $k(T)$  of  $(2-0.3) \times 10^{-10}$  cm<sup>3</sup> s<sup>-1</sup> in the 50 – 300 K range observed by Hickson et al.<sup>9</sup>, although our values are on average 2 times lower. In addition, the values from first principles are a constant factor of *ca.* 1.5 higher that the experimental results of Blitz et al.<sup>10</sup> and that of Bergeat et al.<sup>11</sup>:  $k_{exp}(T) = 2 \times 10^{-11} - 5 \times 10^{-12}$  cm<sup>3</sup>  $s^{-1}$  in the 300–725 K range, but are about 2 times lower than the data of Zabarnick et al.<sup>12</sup> in the same range. As noted by Bergeat et al.,<sup>11</sup> the  $k(T)$  values in this range depend markedly on the precise energy of the submerged TS1; our accurate high-level *ab initio* results put this energy at a high  $-1.43$  kcal/mol and therefore favor the lower *k* values. Also, the present theoretical data show a smoother transition from the low-*T* to the moderate-*T* regimes than the experimental results. The sets of experimental data on the whole suggest that further experimental studies are warranted. Further theoretical work that focuses on the kinetics at very low temperatures could examine the merits of variable reaction coordinate TST<sup>71</sup> for an alternative description of the loose TS0.

For the purpose of modelling, the first-principles  $k(T)$  of this work over the 50 – 3500 K range can be expressed as:

$$
k(T, P=0) = 2.31 \times 10^{-11} (T/300 \text{ K})^{-1.615} \exp(-38.45/T)
$$
. cm<sup>3</sup> s<sup>-1</sup> for  $T = 50 - 400 \text{ K}$ 

$$
k(T, P=0) = 1.15 \times 10^{-12} (T/300 \text{ K})^{0.8637} \exp(892.6/T)
$$
. cm<sup>3</sup> s<sup>-1</sup> for  $T = 400$  --1000 K

$$
k(T, P=0) = 4.57 \times 10^{-15} (T/300 \text{ K})^{3.375} \exp(3477.4/T)
$$
. cm<sup>3</sup> s<sup>-1</sup> for  $T = 1000 - 3500 \text{ K}$ 

In addition, the calculated rate constants from first-principles are also provided in Table S2 in the Supplementary Material.

## **IV. CONCLUSIONS**

In this work, high-level coupled cluster calculations were used to characterize the rate determining steps for the reaction of methylidyne and water vapor, of interest to combustion chemistry and chemistry in the interstellar medium. The barrier-less insertion of  $CH$  into  $H<sub>2</sub>O$  is confirmed to proceed via a well-skipping mechanism *directly* yielding H and CH2O exclusively. Of the two controlling transition states, the loose entrance bottleneck, TS0, is characterized by a proper variational treatment while the inner, tight, submerged TS1 is characterized at high levels of theory. TS0 is confirmed to uniquely determine the reaction rate at low temperatures, though only up to *ca.* 300 K. TS1 is found to lie at  $-1.43$  kcal/mol, substantially higher in energy that in previous theoretical studies, such that TS1 begins to influence the reaction rate already at T *ca*. 300 K, and takes full control of the reaction rate once  $T \geq$ 1000, The rate coefficient *k*(*T*), calculated using a two-dimensional master equation technique for extended temperature and pressure ranges  $(T=50-3500 \text{ K}$  and  $P=1-10^6 \text{ Torr}$ ) is found to be nearly pressure-independent, but strongly dependent on temperature, showing a down-up behavior with increasing *T*. At *T* = 50 K, as in interstellar clouds, the theoretical  $k(T)$  is *ca*.  $2 \times 10^{-10}$  cm<sup>3</sup> s<sup>-1</sup>, in agreement with a recent experimental value.<sup>9</sup> At increasing temperatures, the  $k(T)$  of this work first decreases markedly, favoring the lower available experimental values in the  $300 - 725$  K range. We provide the first kinetics data on this reaction for T> 725 K: the first-principles *k*(*T*) bottoms out at 900 K

with a value of  $8\times10^{-12}$  cm<sup>3</sup> s<sup>-1</sup> and further increases again to reach  $5\times10^{-11}$  cm<sup>3</sup> s<sup>-1</sup> at 3500 K. It is therefore concluded that the reaction is an important if not major CH removal process in hydrocarbon combustion.

#### **Supplementary Material**

See the [supplementary material](https://www.scitation.org/doi/suppl/10.1063/5.0043046) for optimized geometries, ro-vibrational parameters, anharmonic constants, the calculated rate coefficients, and additional figures.

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#### **DATA AVAILABILITY**

The data that support the findings of this study are available within the article and its [supplementary](https://www.scitation.org/doi/suppl/10.1063/5.0043046)  [material](https://www.scitation.org/doi/suppl/10.1063/5.0043046). The data that support the findings of this study are available from the corresponding author upon reasonable request.



Figure 1: Schematic reaction energy profile for the reaction of  $CH(X<sup>2</sup>II) + H<sub>2</sub>O$  constructed using the amHEAT-345(Q) method (see text). Benchmark ATcT<sup>23</sup> values are also given in parentheses for comparison.



**Figure 2:** Minimum energy path for the association of  $CH(X<sup>2</sup>II)$  and  $H<sub>2</sub>O$  leading to pre-reactive complex, PRC, calculated using the CCSD(T)/aug-cc-pV5Z + ZPE +  $\Delta E_{T-(T)}$  +  $\Delta E_{(Q)-T}$  level of theory (see text).



Figure 3: Fall-off curves for the  $CH(X<sup>2</sup>II) + H<sub>2</sub>O$  reaction calculated for an extensive range of temperature (T=50–1000 K) and pressure (P=1–10<sup>6</sup> Torr). Note that when  $T > 1000$  K, the reaction becomes effectively pressure-independent.



**Figure 4:** Rate coefficients for the CH( $X^2\Pi$ ) + H<sub>2</sub>O reaction calculated for an extensive temperature range between 50 K and 3500 K. Experimental data $9-12$  are included for comparison.

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