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Complete List of Authors:	Mehdipour, Iman; University of California Los Angeles Henry Samueli School of Engineering, Department of Civil and Environmental Engineering Falzone, Gabriel; University of California Los Angeles, Civil and Environmental Engineering Prentice, Dale; University of California Los Angeles, Civil and Environmental Engineering Neithalath, Narayanan; Arizona State University, School of Sustainable Engineering and the Built Environment Simonetti, Dante; University of California at Los Angeles, Department of Chemical and Biomolecular Engineering Sant, Gaurav; University of California, Los Angeles, Department of Civil and Environmental Engineering



The role of gas flow distributions on CO₂ mineralization within monolithic cemented composites: Coupled CFD factorial design approach

Iman Mehdipour (*,†), Gabriel Falzone (*,†), Dale Prentice (*,†), Narayanan Neithalath (‡), Dante Simonetti (†,§), Gaurav Sant (*,†,**,††,&)

8 ABSTRACT

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10 The carbonation kinetics of monolithic cementing composites are strongly affected by gas transport which is, in turn, influenced by microstructural resistances and the presence of liquid 11 water within pore networks. The non-uniform gas flow distribution within the CO_2 12 mineralization reactor can impart mass transfer resistance in the monolith microstructure, 13 14 which affects the uptake of CO₂ ("carbonation") of the cementing composites. This paper demonstrates how the gas spatial distribution (velocity and flow rate; quantified by CFD 15 16 analysis) and processing conditions (temperature, relative humidity, and flow rate; quantified by factorial design) affect drying and carbonation, and in turn, the engineering properties of a 17 representative 'monolithic' carbonate-cemented concrete component (i.e., herein concrete 18 19 masonry unit: CMUs, also known as concrete block). It is shown that the gas flow distribution 20 affects drying front penetration and results in moisture and carbonation gradients within the monolith. Particularly, variations in drying kinetics caused by non-uniformity of the contacting 21 gas velocity impose gradients in moisture saturation, which results in increasing microstructural 22 resistance to CO₂ transport. The resultant non-uniform carbonate-mineral formation (i.e., 23 24 carbonate cementation), if not controlled, can produce gradients in mechanical properties and may alter failure patterns upon loading. These insights inform the optimal design of gas flow 25 26 distribution systems and processing conditions within CO₂ mineralization reactors for the 27 manufacturing of low-CO₂ concrete components using CO₂-dilute industrial flue gas streams. 28 29 **Keywords:** CO₂ mineralization; flow distribution; kinetics; CFD; strength; process design. 30 31 32 33 34

* Laboratory for the Chemistry of Construction Materials (LC²), Department of Civil and Environmental Engineering, University of California, Los Angeles, CA 90095, USA

⁺ Institute for Carbon Management (ICM), University of California, Los Angeles, CA 90095, USA

⁺ School of Sustainable Engineering and the Built Environment, Arizona State University, Tempe, AZ 85287, USA

[§] Department of Chemical and Biomolecular Engineering, University of California, Los Angeles, CA 90095, USA

** Department of Materials Science and Engineering, University of California, Los Angeles, CA 90095, USA ⁺⁺ California Nanosystems Institute (CNSI), University of California, Los Angeles, CA 90095, USA

[&] Corresponding author: G. Sant, Phone: (310) 206-3084, Email: gsant@ucla.edu

35 INTRODUCTION AND BACKGROUND

- 36 Low-carbon cementation agents produced by *in situ* CO₂ mineralization ("mineral carbonation
- 37 reactions") offer a promising alternative to ordinary portland cement (OPC).^{1–3} CO₂
- 38 mineralization relies upon the reaction of dissolved CO₂ with inorganic alkaline reactants to
- 39 precipitate mineral carbonate (e.g., CaCO₃), which binds proximate particles and results in
- 40 cementation.^{2,4,5} Herein, a shape-stabilized concrete *green body*, that is composed of a mixture
- of reactants, water, and mineral aggregates, is exposed to CO₂ borne in industrial flue gas
- 42 streams or concentrated CO₂. Such CO₂ mineralization and utilization are foundational to
- decarbonize cement production by creating a waste-to-value or carbon-to-value economy (e.g.,
- 44 by valorizing waste CO₂ borne in flue gases and alkaline solid wastes such as fly ashes), reducing
- the costs and liabilities associated with waste management, and promoting the principles of
- 46 circular economy.^{1,6,7} Generally speaking, CO_2 mineralization allows the production of
- 47 construction components that feature equivalent engineering attributes to their ordinary
- 48 portland cement (OPC) based counterparts while featuring a much smaller embodied carbon
- 49 intensity (eCl). The reduction in eCl of such carbonated concrete products is attributable to: (i)
- the utilization of CO_2 from a waste emissions stream during production and (ii) the avoidance of
- 51 CO₂ emissions by the partial substitution of OPC by industrial solid wastes (e.g., fly ash) and
- 52 alkaline solids. Portlandite $(Ca(OH)_2)$ is a particularly attractive alkaline solid for use in such
- 53 applications because it can be produced at a substantively lower temperature than OPC,⁸ while
- 54 offering a remarkable CO₂ uptake capacity for a non-porous inorganic reactant (59 mass %).²
- 55

56 The carbonation kinetics of alkaline solid reactants and cementing composites are affected by

- 57 the gas processing conditions including: temperature *T*, relative humidity *RH*, CO₂ concentration
- [CO₂], and gas flow rate (Q).^{9,10} For monoliths, the carbonation kinetics increase with decreasing
- 59 *RH* and elevated *T*; so long as a critical *RH* is exceeded.³ Reducing *RH* decreases the quantity of
- 60 water within the pore spaces (i.e., which affects the so-called moisture saturation, S_w), thereby
- easing CO₂ transport into and within the microstructure. This is because, in a porous body, the
- 62 gas diffusivity through the microstructure is inversely proportional to the microstructural
- resistance factor (i.e., as described by the porosity and S_w).¹¹ Achieving the optimal carbonation
- 64 conditions within plug-flow style reactors requires precise control of the gas processing
- conditions, flow rates, and flow distributions because the non-uniform gas flow and velocity can
- 66 detrimentally impact moisture removal and drying and carbonation kinetics by imparting mass
- 67 transfer resistance, which leads to S_w gradients within monolithic components. Such S_w
- 68 gradients result in non-uniform CO₂ uptake across the monolith's volume and gradients in
- 69 properties (e.g., porosity).
- 70

71 Computational fluid dynamics (CFD) has been widely used for evaluating fluid flow patterns,¹²

- and mixing processes¹³ to understand gas flow distributions and heat- and mass-transfer¹⁴ to
- ⁷³ inform the design of chemical reactors.^{15,16} Although the importance of the gas velocity on gas-
- ⁷⁴ solid reactions has been extensively studied, developing reactor designs and process models for
- 75 systems that promote the carbonation reactions of cementitious composites is difficult because
- of the non-uniform boundary conditions at the gas-solid interface and unsteady state (dynamic)
- 77 nature of the process. Therefore, this study uncovers the role of gas flow distribution and
- 78 processing conditions on CO₂ mineralization reaction for a representative monolith (i.e., herein

- 79 concrete masonry unit: CMUs, also known as concrete block) that is carbonated within a plug-
- 80 flow style reactor at ambient pressure. As such, first, CFD simulations are used to link the
- velocity and spatial distributions of gas flowing across the monolith's surfaces within a CO₂
- 82 mineralization reactor to drying front penetration and CO_2 diffusion and their effects on the
- 83 measured bulk CO₂ uptake across monolith's volume. Second, the impact of stiffness/strength
- 84 gradients resulting from the non-uniform carbonate-mineral formation on the overall
- 85 mechanical performance of the concrete block is discussed and analyzed via finite element
- 86 modeling (FEM). Finally, for the optimal gas flow configuration, a factorial design approach is
- used to identify optimal gas processing conditions (*RH*, *T*, and *Q*) that best facilitates gas
- 88 diffusion within microstructure and enhance bulk CO₂ uptake across the monolith's volume.
- 89 Taken together, the outcomes offer new understanding to design optimal CO₂ mineralization
- 90 reactors and to identify the optimal gas processing routes to enable the scalable production of
- 91 low-eCl concrete components using waste-CO₂ borne flue gas streams.
- 92

93 MATERIALS AND METHODS

- 94 Materials and specimen preparation: A mixture of inorganic reactants (e.g., the *binder*), inert
- 95 fine aggregates (sand), and water was used to make "dry-cast" formulations suitable for the
- 96 fabrication of concrete blocks; the monolith geometry considered herein. The reactants used
- 97 consisted of commercially available portlandite (Ca(OH)₂) powder (Standard Hydrated Lime,
- 98 Mississippi Lime Co.), ASTM C150-compliant ordinary portland cement (Type I/II OPC),¹⁷ and
- ASTM C618-compliant fly ash (Class F, m_{CaO} = 2.18 mass % as determined via X-ray
- 100 fluorescence).¹⁸ The Ca(OH)₂ had a purity of 94 $\% \pm 2 \%$ (by mass) with the remainder being
- 101 composed of CaCO₃ as determined by thermogravimetric analysis (TGA).
- 102
- 103 A concrete block making machine (Stonemaker DM100) was used to produce structural "loadbearing" concrete blocks.¹⁹ The overall dimensions of the blocks were 200 mm x 200 mm x 400 104 mm ($w \times h \times L$) with face-shell and web thicknesses of 32 mm and 25 mm, respectively (see SI: 105 Figure S1) yielding a surface-to-volume ratio of 0.081 mm⁻¹. The concrete block mixture was 106 formulated with 10 mass % dry binder, 4.5 mass % water with the remainder consisting of 107 108 mineral aggregates. The mixing and forming process of the fresh concrete blocks are described in the SI. After forming, the fresh concrete blocks were pre-cured at $T = 21 \pm 1$ °C for 12 h to 109 110 gain green strength (compressive strength σ_c = 1.5 ± 0.5 MPa) to enable handling and loading
- 111 into the carbonation reactor. Based on the water content and the forming method, the pore
- water saturation S_w of the concrete blocks prior to carbonation was on the order of 0.62 ± 0.02
- 113 (unitless) determined as per ASTM C140.²⁰
- 114
- **Carbonation processing**: A bench-scale CO₂ mineralization system was fabricated consisting of
- 116 gas mixing equipment, a humidification chamber, and a carbonation reactor (see Figure 1a).
- 117 The gas processing parameters were examined over a range of temperatures (20 °C $\leq T \leq$ 80 °C),
- relative humidities (10 % \leq *RH* \leq 60 %), and gas flow rates (0.10 slpm \leq *Q* \leq 4.92 slpm). In all
- 119 cases, the CO₂ concentration $[CO_2]$ of the gas stream was fixed at 12.5 ± 0.2 % [v/v], as
- 120 confirmed using gas chromatography (GC; F0818, Inficon) to simulate the CO_2 -dilute flue gas
- stream of a coal-fired power plant.²¹ The gas mixture was prepared by mixing air and CO₂
- 122 streams at prescribed flow rates using calibrated mass flow controllers (MFC; Alicat). The mixed

- 123 gas was humidified by bubbling through gas washing bottles that were placed in an oven. The
- 124 humidified gas stream was then passed into the carbonation reactor, which was formed from a
- lidded stainless steel batch can (600 mm × 450 mm × 300 mm; $l \times w \times h$) and wrapped with
- heating-tape and insulated to regulate temperature. In longitudinal and transverse flow
- 127 configurations (Figure 1b), the gas inlet and outlet (6.35 mm diameter) were positioned in the
- middle of the reactor's sidewalls, while for top flow, the gas inlet was located in the middle of
- 129 the reactor's lid and the longitudinal outlet was used.
- 130



131

132 To assess the effect of gas flow distribution on carbonation, various gas flow configurations

- 133 (e.g., longitudinal, transverse, and top flow) were used as shown in Figure 1(b). Second, to
- 134 systematically evaluate the interactions between gas processing parameters (*T*, *RH*, and *Q*) for a
- 135 single flow configuration, a factorial Design-of-Experiments (DoE) approach was implemented.
- 136 The design variables and their corresponding lower and upper bounds are presented in Table S2
- in SI. The significance of variables and their interactions were determined by the analysis of
- 138 variance (ANOVA) approach using least-squares fitting. A non-linear regression analysis was
- used to derive statistical prediction models and develop response surfaces. The results of
- statistical models were then integrated into a multivariable optimization algorithm to
- 141 determine the optimal parameters that satisfy the performance targets.²² Here, for defined

- targets, the desirability functions d_i are obtained and simultaneously optimized to determine
- their best combination as quantified by the overall desirability D function²³:

$$D = (d_1^{r_1} \times d_2^{r_2} \times d_3^{r_3} \times ... \times d_n^{r_n})^{1/\sum r_i}$$
 [Eq. 1]

where n is the number of individual responses in the optimization, and r_i refers to the relative importance of each property, which varies from 1 to 5, reflecting the smallest to the highest

- degree of importance, respectively. And, d_i ranges between 0 (i.e., least desired response) and
- 147 1 (i.e., most desired response).²³ Hereafter, the concrete blocks were dried by exposure to
- flowing air to achieve different initial S_w prior to the carbonation process. The temperature,
- relative humidity, and flow rate during the drying step were equivalent to those applied during
- 150 carbonation, with the exception of using an air stream (i.e., $[CO_2] = 0.04$ %) during drying rather 151 than simulated flue gas ($[CO_2] = 12.5$ %) that was used during carbonation.
- 152
- 153 **Material characterization:** The concrete block was sampled across different sections including:
- each side (long dimension), each face (short dimension), and the web (i.e., the interior wall
- between the two hollows) to assess the variations in CO₂ uptake across different sections (see
- 156 SI: Figure S2). For sampling, a rotary hammer with a 6 mm drill-bit was used to extract powders
- through the entirety of the section's thickness. The total CO_2 uptake ($CO_{2,total}$) within a block
- 158 was estimated as a mass average of each section's CO₂ uptake as:

$$CO_{2,total} = \sum_{i=1}^{n=5} C(24h)_i (g_{CO_2}/g_{reactants}) \times m_i$$
 [Eq. 2]

- where, $C(24h)_i$ is the 24-h CO₂ uptake of the ith section (i.e., side, face, or web) and m_i refers to 159 160 the mass fraction of a section in relation to the entire block mass. Thermogravimetric analysis 161 (TGA: STA 6000, Perkin Elmer) was used to assess the extent of CO₂ uptake following ASTM C1872.²⁴ Around 50 mg of powder was heated from 35 °C to 975 °C at a rate of 15 °C/min in 162 aluminum oxide crucibles under ultra-high purity N₂ gas purge at a flow rate of 20 mL/min. The 163 carbonate content was quantified by assessing the mass loss associated with CaCO₃ 164 decomposition over the temperature range of 550 °C to 950 °C, normalized by the initial mass 165 of reactants (g_{CO2}/g_{reactants}; reactants: portlandite, fly ash, and OPC) within the solid. It should be 166 noted that the CO_2 uptake accounted for the initial quantity of carbonates that were present in 167 the precursor materials prior to the carbonation process. In addition to carbonate content, the 168 non-evaporable water content (w_n , mass %) was calculated as the mass loss over the 169 170 temperature range of 105 °C to 975 °C, excluding the mass loss from the decomposition of CaCO₃ and Ca(OH)₂ to estimate the extent of cement (OPC) hydration.^{35,36} 171 172 173 The net area compressive strengths of the concrete blocks were measured in accordance with 174 ASTM C140²⁰ under uniaxial monotonic displacement-controlled loading using a hydraulic jack with a capacity of 800 kN. The bearing plates used for compression testing were large enough 175
- to cover the contact surfaces of the block entirely to distribute the load evenly, and rigid
- enough (100 mm thick) to eliminate plate bending that can cause non-uniform stresses.²⁰ To
- 178 characterize the variations of carbonate mineral formation, the porosity and compressive
- strength of the different block's sections (i.e., sides, web, and faces) were determined.
- 180 Representative samples (50 mm \times 50 mm \times 25 mm; $l \times w \times t$) were cut from the middle of each

- 181 section of the concrete block using a low-speed saw. The total porosity and pore saturation
- 182 level of samples were quantified using a vacuum saturation method²⁷ and the compressive
- strengths of the samples were measured as per ASTM C39.²⁸ Finally, to assess the effects of gas
- 184 processing conditions on the transport properties (diffusion), the total moisture diffusion
- coefficient (i.e., the sum of liquid water and water vapor diffusion coefficients) during drying
 was estimated using Fick's 2nd law.²⁹ Herein, the sides of the sectioned samples (50 mm × 50
- 186 was estimated using Fick's 2^{nd} law.²⁹ Herein, the sides of the sectioned samples (50 mm × 50 187 mm × 25 mm; $l \times w \times t$) were double-sealed using adhesive-backed aluminum tape to ensure 1D
- 188 gas transport (exposed surfaces: 50 mm \times 50 mm; $l \times w$).
- 189

190 COMSOL[®] MULTIPHYSICS: CFD AND FEM SIMULATIONS

- 191 CFD simulations were used to assess the effects of gas flow configurations on the spatial
- distribution and velocity of contacting gas across the concrete block's surfaces within the
- 193 carbonation reactor. The gas flow analysis was carried out using the $k \omega$ turbulence model,³⁰
- which is suitable for gas velocity analysis near solid wall regions.^{31,32} The Reynolds number Re
- based on inlet diameter d_{inlet} and inlet velocity V_{inlet} was calculated to be greater than 2,300
- suggesting turbulent flow. In the $k \omega$ model, the turbulent kinetic energy k and specific
- 197 turbulent dissipation rate ω describe the turbulence of gas flow. The governing equations of
- 198 the $k \omega$ turbulence model are described in the SI. A representative CFD simulation of the gas 199 flow distributions across the concrete block's surfaces within the carbonation reactor for the
- 199 flow distributions across the concrete block's surfaces within the carbonation reactor for the 200 top flow direction is shown in Figure 2(a). The boundary conditions used in the simulations
- included the gas inlet velocity ($V_{inlet} = Q_{inlet}/A_{inlet}$) and outlet gas pressure ($P_{outlet} = 0$). The
- model's mesh consisted of 25,000 tetrahedral elements for the concrete blocks and 10,000
- triangular elements for the reactor walls. The size of elements ranged from 0.005 m to 0.01 m
- for concrete block and reactor domains, respectively. To quantify the average contacting gas
- velocity and velocity non-uniformity, the gas flow field for every surface of the concrete block
- 206 (see Figure 2b) was discretized into cells and their corresponding velocity magnitudes were
- extracted. The average contacting gas velocity across the ith surface of the concrete block $V_{ave,i}$ was then quantified as:

$$V_{ave,i} = \frac{\sum_{x=1}^{n} V_x}{n}$$
 [Eq. 3]

- where *n* is the number of cells (5 mm \times 5 mm) on the block surface and V_x corresponds to the velocity magnitude in each cell. To rationalize the data, in all cases, the average contacting gas
- velocity magnitude in each cell. To rationalize the data, in all cases, the average contacting gas velocity $V_{ave,i}$ was normalized by the gas inlet velocity V_{inlet} . The degree of non-uniformity (i.e.,
- variation) of the contacting gas velocity across the block surfaces was then quantified as:

Velocity Non-uniformity Index =
$$\frac{\sqrt{\sum_{x=1}^{n} (V_x - V_{ave,i})^2}}{V_{ave,i}}$$
 [Eq. 4]

213

- 214 Thereafter, FEM analysis of the linear elastic behavior of the concrete block was carried out
- 215 using COMSOL Multiphysics³³ to assess the effect of stiffness variations resulting from CO₂
- 216 uptake across the different block's sections on the overall mechanical response of the concrete
- 217 block. The measured strength data of the block's sections was used to estimate material
- 218 stiffness as an input in the FEM analysis as follows^{47,48}:

$$E_{c,i} = k\sigma_{c,i}$$
 [Eq. 5]

where $E_{c,i}$ (MPa) and $\sigma_{c,i}$ (MPa) are Young's modulus and compressive strength, respectively, of 219 the ith section of the concrete block and k is the coefficient relating elastic modulus to the 220 compressive strength that was taken as 900 herein.³⁴ For dry-cast composites such as concrete 221 blocks on account of their high aggregate contents, the elastic modulus is dictated by the 222 stiffness of aggregate inclusions and degree of compaction.³⁶ As such, no distinction in elastic 223 224 modulus is expected between traditional cement-based and carbonated concrete blocks. The 225 estimated Young's moduli of the sections were input in the FEM analysis to simulate the concrete block (see Figure 2c). The governing equations of FEM analysis are detailed in the SI. 226 To mimic compressive loading and minimize local stress concentrations, the steel bearing plates 227 were modeled as well. As the boundary conditions, the displacements of the bottom plate were 228 229 taken as zero in all directions (x, y, and z) and compressive stress was applied to the top surface 230 by systematically increasing the applied stress from 0 to 15 MPa in 1.5 MPa increments. Perfect 231 contact between the bearing steel plates and the surfaces of the concrete block was prescribed.

232



Figure 2: (a) CFD simulations of gas flow distributions across the concrete block's surfaces within the carbonation reactor for the top flow configuration. The velocity vectors within the reactor are shown as red arrows and the large arrows depict the gas inlet and outlet directions. (b) A contour plot of the gas velocity field across the surfaces of the concrete block (shown as dashed lines; outlet facing view). (c) FEM simulation of uniaxial compression of the carbonated block showing sections (i.e., sides, faces, and web) with different Young's moduli. The variations in Young's moduli of each section $E_{c,i}$ are shown in different colors.

233

234 **RESULTS AND DISCUSSION**

Effects of gas flow distribution on carbonation reaction: The time-dependent CO₂ uptakes of 235 236 different sections of the concrete blocks for different gas flow configurations were evaluated 237 (see Figure 3). The CO_2 uptake was noted to vary significantly based on the gas flow 238 configuration. Although all inlet faces featured nearly similar CO₂ uptake-time profiles (Figure 3a), the CO₂ uptake profiles of the outlet faces were expectedly impacted by the gas flow 239 240 configuration (see Figure 3b). Unlike significant CO₂ uptake variations between different block's sections for both longitudinal and transverse flow configurations, the top flow featured the 241 most uniform CO₂ uptake and the highest CO₂ uptake (see SI: Figure S3a). The overall 24-h CO₂ 242 243 uptake was 0.089 g_{CO2}/g_{reactants}, 0.121 g_{CO2}/g_{reactants}, and 0.150 g_{CO2}/g_{reactants} for the longitudinal, transverse, and top flow configurations, respectively. To quantify the effect of the flow 244

- configuration on carbonation kinetics, the time-CO₂ uptake profiles were fitted to an equation 245
- of the form $C(t) = C(t_u)(1 \exp[(-k_{carb}t)/C(t_u)])$ [Eq. 6], where k_{carb} is the apparent 246
- carbonation rate constant and $C(t_u)$ is the ultimate CO₂ uptake that was taken as the 24-h CO₂ 247
- uptake. Similar to CO₂ uptake, the carbonation rate constant for the different sections indicated 248 a strong dependency on gas flow configuration. For instance, k_{carb} for block's section facing the
- 249
- gas outlet was 4x lower than that of the inlet for the longitudinal direction, while near 250
- 251 equivalent carbonation kinetics for both sections were observed for the top flow configuration. 252



Figure 3: The time-dependent traces of the CO₂ uptake of the concrete block sections for different gas flow configurations for: (a) inlet and (b) outlet positions. The data was fitted to an equation of the form $C(t) = C(t_u)(1 - \exp[(-k_{carb}t)/C(t_u)])$. The insets depict the flow direction and sampling location (denoted by a cross) of the concrete block. In all cases, the gas stream featured $[CO_2] = 12.5 \%$, $T = 70 \degree$ C, RH = 50 %, and 2.45 slpm flow rate. (c) The evolution of the moisture ratio for different sections of the concrete block for varying gas flow configurations. The drying rate constant k_{dry} was estimated by fitting the drying data to an equation of the form: $MR(t) = \exp[-k_{drv}t^n]$. During drying, the air stream featured [CO₂] = 0.04 %, T = 70 °C, RH = 50 %, and a flow rate of 2.45 slpm.

253

The suppression of carbonation kinetics across some of the block's sections is on account of 254 higher water content in the block's pores (i.e., higher S_w) that was imposed by insufficient 255 drying within sections whose surfaces are starved of gas flow. Our previous work has shown 256 that the presence of water within the pores of microstructure inhibits carbonation by imparting 257 CO₂ mass transfer resistance.³ To assess the drying kinetics as a function of different gas flow 258 259 configurations, the moisture ratio (MR) evolution was evaluated. To exclude the competing effects of carbonation and moisture transport, the concrete block was exposed to flowing air 260 that was conditioned similarly (T, RH, and Q) to the carbonation experiments. The drying rate 261 constant k_{drv} was estimated as $MR(t) = \exp[-k_{drv}t^n]$ [Eq. 7],³⁷ where n is the fitting 262 exponent and MR(t) is the dimensionless moisture ratio at time t, which is given as MR(t) =263 $(\omega_t - \omega_e)/(\omega_0 - \omega_e)$ [Eq. 8],^{38,39} where ω_t , ω_e , and ω_0 are moisture content at time t, the 264 equilibrium moisture content, and initial moisture content, respectively. Generally, the drying 265 rate dMR(t)/dt decreases with time due to the transition from connected-liquid bridge drying 266 to vapor diffusion as the drying front progressively penetrates deeper into the body.^{40,41} In 267

- agreement with the results of carbonation kinetics, the top flow configuration resulted in more
 uniform drying kinetics between inlet and outlet sections than that of the longitudinal flow (see
 Figure 3c). The similarity between carbonation and drying behavior of the concrete block's
- 271 sections shows that the carbonation rate constant k_{carb} is strongly correlated with and
- 272 controlled by the drying rate constant k_{dry} (see SI: Figure S3b), since enhanced drying facilitates
- CO_2 diffusion and thereby promotes the carbonation kinetics. This suggests that the variation of
- 274 CO₂ uptake is induced on account of the different distributions of water content and drying
- 275 front penetration across block's sections which affect gas diffusion (i.e., since gas diffusion in
- 276 water $\approx 10^4$ times slower than in air²⁹).
- 277



Figure 4: (a) CFD analysis of contacting gas velocity across different block's surfaces for varying gas flow configurations. **(b)** The evolution of the apparent carbonation rate constant k_{carb} as a function of contacting gas velocity. Here, k_{carb} was estimated using Eq. (6). The variation in pore saturation level S_w with contacting gas velocity for different block's sections is also shown in **(b)**. The concrete block featured $S_{w,initial} = 0.62$ prior to the carbonation process. In all cases, the gas stream featured $[CO_2] = 12.5 \%$, $T = 70 \degree$ C, RH = 50 %, and 2.45 slpm flow rate. **(c)** Representative drying rate dMR(t)/dt and carbonation rates dC(t)/dt traces at different contacting gas velocities.

278

The variations in drying kinetics across the different sections of the block are attributed to the 279 spatial variations of the contacting gas velocity. Indeed, our CFD analysis revealed that the top 280 flow configuration resulted in the most-spatially uniform and the highest average velocity 281 across block's surfaces (see Figure 4a). This explains the more uniform and higher CO₂ uptake 282 for the top flow configuration. The evolution of carbonation rate constant k_{carb} showed a 283 logarithmic scaling as a function of contacting gas velocity (Figure 4b). This suggests that the 284 overall carbonation reaction rate is controlled by the overall drying rate, since a higher drying 285 rate enhances the penetration of the drying front^{*}, as evidenced by the reduced S_w from 0.62 to 286 0.40. In turn, increasing the contacting gas velocity by 3 orders of magnitude resulted in a 287 proportionate 3.5x enhancement of carbonation rate (Figure 4b). Independent of the gas flow 288

^{*} The term "drying front" is generically defined as the interface between fully saturated and partially saturated regions.^{40–42} We use this term here to indicate the transition zone between regions that have a reduced pore saturation as compared to the initial pore saturation level of a concrete block ($S_{w,initial} = 0.62$).

- configuration, the contacting gas velocity diminished significantly within the web section. This resulted in the lowest carbonation level among all sections of the concrete block (see Figure 4a) in the occluded web. This is on account of the low length-to-depth ratio (L/D = 1) of the concrete block's hollows, as a result of which marginal flow occurs within the core-sections suggesting the formation of dead regions ($V \approx 0$).⁴³ A greater initial drying rate and faster drying resulted in a greater carbonation rate at early ages followed by a faster decrease in the carbonation rate as evidenced by the profiles in Figure 4(c).
- Although the rate of penetration of the drying front increases with gas velocity, the enhanced
- 298 formation of carbonate minerals (CaCO₃) in the direction of the drying front can produce
- blockages in the microstructure. This can impose an additional transport limitation that can
- 300 suppress the carbonation rate at later reaction times. It is important to note that the effect of 301 the contacting gas velocity on moisture transfer within the pore spaces is also affected by the
- 302 gas processing conditions (*T* and *RH*). For instance, for a given contacting gas velocity,
- increasing the *RH* of the gas stream slows moisture transport and penetration of drying front
- due to the competition between inward and outward transport of (condensed) moisture within
- 305 the pores, as discussed in the next section.
- 306

Effects of interactions between gas processing conditions on carbonation reaction: For a given
 gas flow configuration, the carbonation of concrete components is strongly influenced by the
 gas processing parameters (*T*, *RH*, and *Q*). To systematically assess such effects and their
 interactions, a factorial Design-of-Experiments (DoE) approach was used to generate response

- 311 surfaces and derive statistical prediction models. To vary the initial pore saturation level
- 312 $S_{w,initial}$, the blocks were initially dried by exposure to flowing air prior to the carbonation
- process. The ANOVA results are presented in Table S3 in SI, which indicates the significant
- parameters and interactions. As an example, the response surface of CO₂ uptake visualizes the
- 315 combined effect of *RH* and *Q* of gas (see Figure 5a). The statistical models for S_w after drying
- and 24-h CO_2 uptake of concrete blocks were derived as:

 $S_{w,idrying} = 0.62890 - 0.00397 \times T + 0.00198 \times RH - 0.07348 \times Q_i + 0.00111(RH \times Q_i)$ [Eq. 9] $C(24h)_i = -0.00592 + 0.00127 \times T - 0.00022 \times RH + 0.04373 \times Q_i - 0.00064(RH \times Q_i)$ [Eq. 9]

10]

317 The significant parameters and interactions were found to be identical between both

- 318 responses, although having opposite signs, demonstrating the significance of S_w as a dominant
- variable that affects the carbonation of concrete components. Hereafter, to predict the CO_2
- 320 uptake of the different block's sections, the variations in the contacting gas velocity as a
- 321 function of gas inlet flow rate were determined using CFD analysis. Increasing the flow rate at
- 322 the gas inlet enhanced the contacting gas velocity and improved the velocity uniformity across
- different block's surfaces (see Figure 5b). For a given block surface, the correlation between
- normalized contacting velocity and gas flow rate can be described by the power function of the
- form $V_{ave,i}/V_{inlet} = aQ_i^b$ [Eq. 11], where a and b are fitting parameters that depend on the
- 326 concrete block section (see Figure 5b). Knowledge of the normalized contacting gas velocity and

the corresponding gas flow rate Q_i (using Eq. 11), allows prediction of the average CO₂ uptake

328 for a given concrete block's section using Eq. 10; for this specific reactor configuration.

329



Figure 5: (a) Response surface of the 24-h CO₂ uptake of the concrete block under different *RH* and *Q* of gas at T = 35 °C. (b) The variations of contacting gas velocity (determined by CFD analysis) as a function of *Q* for different block's surfaces. (c) The variations in 24-h CO₂ uptake as a function of initial pore water saturation S_w after the drying step. The shaded regions in (c) represent different processing conditions. In all cases, the concrete blocks were initially dried by exposure to flowing air prior to the carbonation process. (d) Arrhenius plots of the activation energy of moisture diffusion (E_a) at different gas *RH* during drying. Herein, all the data corresponds to the "top flow" configuration.

330

Coming back to pore water saturation, the 24-h CO₂ uptake of the block sections was noted to 331 scale with $S_{w,drying}$ (see Figure 5c), as estimated by a linear function of the form $C(24h)_i =$ 332 $-0.46 \times S_{w,i} + 0.30$ for $S_w > 0.11$ [Eq. 12]. It should be noted that this equation is valid only for 333 the design space considered herein. For instance, it has been previously noted that critical $S_{w.c.}$ 334 ≈ 0.10 is required to sustain the dissolution-carbonation reaction of portlandite.^{3,9} To capture 335 this breakpoint, a separate dataset (outside the design space) was collected under aggressive 336 drying at T = 80 °C and RH = 20 % that revealed that CO₂ uptake was substantially suppressed 337 338 when S_w dropped below 0.11. This is significant since it indicates that (Eqs. 9, 10, and 12) are valid for $S_w > S_{w,c} \approx 0.10$. The CO₂ mineralization mechanism via portlandite carbonation 339 within concrete monoliths proceeds via a dissolution-precipitation pathways including⁴: (i) 340

release of Ca²⁺ species into the pore liquid due to dissolution of alkaline reactants, (ii) transport 341 and dissolution of CO₂ though and within the monolith's pore network, and (iii) precipitation of 342 343 carbonate minerals via combination of dissolved species (Ca^{2+} , CO_3^{2-} , and HCO_3^{-}). It should be 344 noted, however, that a critical moisture saturation level ($S_{w,c} \approx 0.10$) is required to sustain the carbonation reaction.^{3,9} So long as $S_{w,c}$ is exceeded, Ca²⁺ species liberated following the 345 346 dissolution of portlandite react with dissolved CO_2 species (i.e., CO_3^{2-} and HCO_3^{-}) to precipitate 347 calcium carbonate.44,45 348 Further, limited CO₂ uptake was noted when gas RH was similar to the initial $S_w = 0.62$ of the 349 350 concrete block (see the shaded blue region in Figure 5c). This is attributed to a small driving force for evaporation, and a balance between moisture transport into and out of the pore 351 structure, such that drying is hindered. This was evidenced by quantifying the apparent 352 activation energy of moisture diffusion (see Figure 5d). Indeed, Arrhenius analysis of moisture 353 diffusivity at RH = 60 % shows a small dependence on temperature as compared to moisture 354 diffusion at RH = 20 %. In general, the small apparent activation energy (<20 kJ/mol) is reflective 355 356 of limited temperature sensitivity for drying of the monoliths; and indicates a transport-357 controlled, i.e., rather than surface reaction-controlled process. Accordingly, at RH = 60 % ($E_a \approx$ 5.5 kJ/mol), wherein the contacting gas's relative humidity is similar to the pore water 358 359 saturation of the concrete block ($S_w = 0.62$), drying is hindered due to the similar rates of 360 moisture transfer inward from the ambient environment and outward from pore network. As 361 the RH of the contacting gas stream is reduced, moisture removal becomes somewhat more 362 sensitive to temperature (e.g., a 3x reduction in the RH translates to only a doubling of the activation energy). Unsurprisingly, the activation energies of moisture diffusion noted herein 363 are considerably lower than that reported for mature, hardened cement paste (e.g., \approx 32-45 364 kJ/mol for water-to-cement ratio = 0.40-0.60^{46,47}); under conditions where no air-flow occurred. 365 The smaller temperature dependence (E_a) of moisture diffusivity in the presence of air flow is 366 367 likely because air flow facilitates moisture transport due to a sharper, and sustained RH 368 gradient between the ambient vapor and the monolith's surface from where evaporation 369 occurs. These findings reinforce the premise that both optimal reactor (gas) flow distribution 370 and gas processing conditions are critical to enhancing carbonation kinetics and carbonation 371 uniformity within concrete components. 372

373 **Effects of gas flow distribution on carbonation strengthening:** The strengthening of concrete components during CO₂ exposure is affected by cement hydration, pozzolanic, and carbonation 374 reactions.³ As the extent of CO₂ uptake determines carbonate cementation, 1,3 variations in CO₂ 375 uptake can induce non-uniformity in carbonation strengthening, which can impact the overall 376 377 mechanical response of carbonate-cemented components. Herein, it was noted that the 378 porosity of carbonated samples, that were extracted from different sections of the concrete 379 block, demonstrated a sigmoidal/tri-linear refinement with CO₂ uptake (see Figure 6a). On account of more uniform CO₂ uptake, the top flow configuration resulted in a lower porosity 380 381 and smaller variations in porosity across different block's sections as compared to the 382 longitudinal and transverse flow directions. The tri-linear trend indicated a secondary slope m_2 383 = 76.6 (i.e., between 0.05 $g_{CO2}/g_{reactants}$ and 0.15 $g_{CO2}/g_{reactants}$) that was substantially steeper

- than the first and third slopes ($m_1 = 6.7$ and $m_3 = 3.5$) on account of the enhanced formation 384 of space-filling carbonate products. The smaller slope m_1 is attributed to the small extent of 385 cement hydration (W_n/m_{OPC}) and minimal carbonation. The smallest slope m_3 results from a 386 near-complete conversion (i.e., carbonation) of portlandite (~85 % based on TGA analysis) 387 388 which is the primary reactant used for CO₂ mineralization in the concrete monolith. As a result, the contribution of carbonation to porosity refinement saturates as portlandite carbonation 389 reaches the final conversion extent. To exclude the effect of cement hydration, the compressive 390 strength results were normalized by W_n/m_{OPC} and plotted as a function of CO₂ uptake (see 391 Figure 6b). Interestingly, $\sigma_c/({}^{W}n/m_{OPC})$ enhanced exponentially with an exponent of 8.72 per 392 unit mass of CO₂ uptake, confirming that strengthening offered by carbonation is foundational 393 in ensuring the strength gain of the structural component. Additionally, the extrapolation of the 394 curve to determine the y-intercept (see solid line in Figure 6b) yielded nearly an equivalent 395 value to that of uncarbonated concrete block suggesting that carbonation does not 396 397 detrimentally affect the strength gain resulting from cement hydration.
- 398



function of CO₂ uptake under different gas flow configurations. (b) The normalized strength evolution as a function of the CO₂ uptake for different sections of concrete blocks. (c) The FEM analysis of the uniaxial compressive stress-displacement response of carbonated concrete blocks. The Young's modulus of every section was estimated using [Eq. 5]. The reference concrete block was modeled using a homogenous Young's modulus of 14 GPa.³⁴

Strain distributions across top surfaces of concrete blocks at $\sigma_c = 15$ MPa are shown. (d) The variations in the measured compressive strengths of concrete blocks as a function of overall CO₂ uptake for different gas flow configurations. During carbonation, the gas stream featured $[CO_2] = 12.5 \%$, $T = 70 \degree$ C, RH = 50 %, and 2.45 slpm flow rate.

399

On account of the lowest CO_2 uptake, the smallest compressive strength was noted for the web 400 401 sections of carbonated concrete block. The variations in material strength and elastic properties 402 across the concrete block's sections can result in non-uniform stress and displacement 403 distributions under loading. This is confirmed by FEM simulations of the stress-displacement 404 response of concrete blocks (see Figure 6c). In contrast to top flow, concrete blocks carbonated under the longitudinal and transverse flow directions featured far more non-uniform strain 405 406 distributions, and as a result, the compressive strength reduced from 15 MPa to 6 MPa for a 407 given displacement of 0.4 mm. Based on the displacement analysis for the reference concrete block with uniform Young's modulus, the web section experienced the largest deformation as 408 compared to the other sections (see Figure 6c and Figure S7 in SI). This is in agreement with 409 410 other studies wherein the failure of CMUs usually occurs when the web section cracks.^{48,49} In analogous to traditional cement-based blocks, therefore, the web section which experiences 411 the lowest CO_2 uptake dictates the overall mechanical response in carbonated concrete blocks. 412 413 In agreement with the FEM simulations, the measured compressive strengths of the concrete 414 blocks were noted to be affected by gas flow distribution and correlated with overall CO₂ uptake (see Figure 6d). Importantly, the failure mode of concrete blocks was noted to vary from 415 "conical" failure for top flow to "conical/shear" failure for longitudinal and transverse flow 416 configurations in accordance with failure modes described in ASTM C1314.⁵⁰ Expectedly, more 417 cracking was observed in the less-carbonated sections (e.g., web) of the blocks. This is thought 418 to result from variations in material strength/stiffness properties that strongly dictate the 419 420 failure mode by inducing shear/tension cracks along with the weakest zones.^{62,63}Therefore, the 421 reduced compressive strength of less-carbonated blocks is linked to the combined effects of non-uniformity of material elastic properties and the reduced carbonation strengthening 422 423 contribution. 424

425 IMPLICATIONS FOR THE DESIGN OF CO₂ MINERALIZATION REACTORS AND PROCESSES

426 The CFD modeling carried out herein allows analysis of the spatial distribution and velocity of

- 427 contacting gas to inform the optimal: (a) design of gas flow distribution systems and (b)
- 428 geometrical arrangement of concrete components within a CO₂ mineralization reactor's volume
- so as to maximize and ensure the uniformity of CO₂ uptake of low-carbon concrete products.
- 430 These aspects are particularly related to how variations in the contacting gas velocity affect
- drying, drying gradients, and consequently CO₂ uptake gradients within a monolith's volume.
- The outcomes of this work, importantly, offer a basis of extension to other component
- geometries, e.g., other than the concrete block, which feature varying thicknesses and surface-
- to-volume ratios, i.e., to expand the palette of products that can be produced via CO₂
- 435 mineralization processes. In addition, the CFD simulations carried out herein, form the basis for
- the development of a fully coupled heat-mass-chemical reaction-transport model that is
- 437 required to comprehensively relate aspects of binder composition, gas processing conditions
- 438 (e.g., *T*, *RH*, $[CO_2]$, and *Q*), reactor geometry, component geometry, and CO_2 (mineralization)

- 439 uptake, to each other so as to maximize direct CO_2 utilization using industrial flue gas emission 440 streams, in a time-, cost- and energy-efficient manner.
- 441

442 SUMMARY AND CONCLUSIONS

- This study has elaborated on how gas flow distributions within a plug-flow style reactor affect
 CO₂ uptake and the resulting carbonate cementation of monolithic concrete components (i.e.,
 herein concrete masonry units: CMUs, also known as the concrete block). Special focus was
 paid to uncover how drying kinetics and liquid water distributions, resulting from varying gas
- flow distributions, impact the rate and extent of carbonation. The dependence of carbonation
- kinetics on the contacting gas velocity is attributed to the variation in drying kinetics and the
- 449 penetration rate of drying front (i.e., S_w gradients) which affect the microstructural resistance
- to gas diffusion. Such S_w gradients result in non-uniform CO_2 uptake across the monolith's
- volume, which imposes gradients in material properties (e.g., porosity and stiffness), and
- 452 thereby impacts the overall mechanical response of carbonate-cemented concrete
- 453 components. Both CFD and FEM simulations were used to assess the effects of the spatial
 454 distribution of contacting gas velocity across a concrete block's surfaces on variations in CO₂
- distribution of contacting gas velocity across a concrete block's surfaces on variations in CO₂
 uptake within concrete block's sections and resultant material properties (stiffness and
- 455 uptake within concrete block's sections and resultant material properties (stimless and
- 456 strength). Finally, for the optimal gas flow configuration, the effects of gas processing
- 457 conditions (*RH*, *T*, and *Q*) on CO_2 mineralization reactions of the concrete block were 458 highlighted. The understanding gained is critical to inform the optimal design of CO_2
- 458 highlighted. The understanding gained is critical to inform the optimal design of CO₂
- 459 mineralization systems and the selection of gas processing routes to enhance and to ensure
 460 uniformity of CO₂ uptake and material properties evolution within concrete components. The
- uniformity of CO₂ uptake and material properties evolution within concrete components. The
 outcomes are of relevance to design optimal carbonation systems, and to manufacture low-CO₂
- 462 concrete components that utilize waste CO₂ borne in flue gas streams and fulfill relevant
- 463 construction standards, without a need for a carbon capture step, and at ambient pressure.
- 464

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- 475

476 SUPPORTING INFORMATION

- 477 Oxide composition of binders, concrete block forming process, factorial Design-of-Experiment,
- sampling procedure for CO₂ uptake characterization, CFD and FEM governing equations, CO₂
- 479 uptake variations, CFD simulations of contacting gas velocity, derivation of statistical prediction
- 480 models, desirability response for multivariable optimization, and FEM analysis of the uniaxial
- 481 compressive response of concrete block.
- 482

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