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Reactive Crystallization: A Review

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Abstract

Reactive crystallization is not new, but there has been recent growth in its use as a means of improving performance and sustainability of industrial processes. This review examines phenomena and processes in which reaction and crystallization are coupled in the production of a desired chemical species. Coverage includes fundamental phenomena, such as solubility, supersaturation, crystal nucleation and growth, and chemical kinetics. Systems examined are divided into two groups, those best described as undergoing ionic reactions (including neutralizations), which have near instantaneous rates and result in the formation of ionic bonds, and those undergoing covalent reactions in which the key step occurs at measurable rates and results in the formation of covalent bonds. Discussion of the latter category also includes the impact of catalysis. Examples of a variety of reactions and applications are enumerated, and special attention is given to the utility of reactive crystallization in chiral resolution. Integration of reactive crystallization into process design, including both batch and continuous operations, and the development and efficacy of modeling, monitoring and control are reviewed. Finally, a perspective addressing needs to advance the usefulness and applications of reactive crystallization is included.

Introduction

Crystallization is used in the production of a wide variety and quantity of products and intermediates, perhaps more than any other separation technique. In different applications,

30 crystallization can separate, concentrate, or purify a specific species or it may be part of
31 diagnostic or analytical procedures. In most applications the most important function of
32 crystallization is to generate a product in a specific solid form. Many medicines, synthetic
33 materials, food ingredients, and specialty and commodity chemicals require crystallization
34 during the transformation from raw materials to product. The process by which chemical species
35 are crystallized often impacts their properties, such as purity, morphology, mean size, and size
36 distribution. Such properties can affect therapeutic capabilities and dissolution profiles of
37 pharmaceuticals, the efficacy of agricultural chemicals, and a variety of material properties.

38 While the use of crystallization is older than the chemical industry, there are aspects of
39 the process that remain poorly understood. Furthermore, the diversity of processes utilizing
40 crystallization and the chemical and physical variations of species crystallized has led to many
41 different methodologies for conducting this operation. The present review focuses on **reactive**
42 **crystallization from solution: that is, those processes in which a chemical reaction produces**
43 **a specific crystallizable species in solution and, thereby, generates a driving force for the**
44 **formation of a crystalline product.** Clearly, the chemical reaction must produce sufficient
45 amounts of the crystallizing species to exceed solubility. While reactive crystallization may
46 fulfill the same functions of crystallization cited earlier, there also are two other important roles
47 that can be played by reactive crystallization: (1) If a reaction is controlled by equilibrium,
48 removal of the reaction product from solution by crystallization pulls the reaction towards the
49 product as dictated by Le Chatelier's principle. (2) Suppose the desired product is an
50 intermediate in a larger reaction network and the yield of that product is reduced by its
51 subsequent reaction. Then the yield can be increased by operating under conditions causing
52 crystallization of the product. As solids, species are stabilized and less likely to undergo
53 subsequent solution-phase reactions.

54 Besides being generated by reaction, the driving force for crystallization can be created or
55 enhanced by solvent removal (for example, by evaporation or transport through a membrane),
56 adjustment of pH, change in temperature, or addition of a nonsolvent. The presence of multiple
57 species in solution complicates the system but is frequently encountered in industrial processes.
58 In a reactive crystallization process, there are necessarily multiple species present—that is, the
59 reactants and products of the reaction—that may impact the solubility of each species, the pH
60 and temperature of the solution, and the kinetics of the reactions and the crystallization.

61 As the chemical industry continues to strive towards ambitious goals of process
62 intensification, efficiency enhancements and sustainability, reactive crystallization can be a
63 helpful tool in achieving such goals. Thermal separations dominate the chemical industry and
64 have a huge energy cost; on the other hand, reactive crystallizations can be operated without
65 expenditure of the thermal energy that is required for cooling crystallization, evaporative
66 crystallization, or many other separation processes.¹ The combination of reaction and
67 crystallization can also reduce production time and hold-up of intermediates, thereby reducing
68 the number of operations and eliminating the need to transfer materials between vessels. Use of
69 the same solvent for reaction and crystallization can additionally reduce waste production and
70 the need for wastewater treatment, and it may even eliminate the need to use additional solvents.

71 Reactive crystallization encompasses several fundamental phenomena. Reactant mixing
72 is limited by convection and diffusion, as are the reaction products as they are transported
73 through the bulk liquid to the surface of a growing crystal. New crystals are formed by either
74 primary or secondary nucleation, thereby generating fresh surfaces for growth. The rates at
75 which these kinetic phenomena occur are influenced by mixing, catalyst design, and other
76 engineering decisions, and they determine the size distribution, yield, and other aspects of crystal
77 quality. Moreover, such fundamental considerations work their way into the design,
78 implementation, and control of processes in which reactive crystallization plays the key role.

79 The aims of this review are to (1) describe fundamental thermodynamic and kinetic
80 phenomena important in reactive crystallization, (2) examine reaction types and provide
81 tabulations of references for specific reaction systems, (3) examine the design and control of
82 systems using reactive crystallization, and (4) identify areas for future research. Only
83 crystallization from solution is considered and there is an emphasis on processes involving high-
84 value products such as pharmaceuticals and specialty chemicals. A condensed summary of
85 fundamentals of crystallization and reactive processes is followed by a compilation, with
86 commentary, of recent studies of processes utilizing reactive crystallization. Processes are
87 categorized based on reaction type and relative rates of reaction and crystallization. Finally, the
88 future of reactive crystallization processes is discussed, including what needs to be accomplished
89 for more widespread adoption of this intensified process.

90

91 **Fundamentals**

92 **Solubility.** Solid-liquid equilibrium thermodynamics determine solute solubility: that is,
93 the maximum mole fraction (or other measure) of the solute in a solution at a specific set of
94 conditions, including temperature, pressure, pH, and solution composition. The governing
95 requirement for solid-liquid equilibrium is that the chemical potential of each component
96 distributed between the two phases is the same in the solid and liquid phases; that is $\mu_i^S = \mu_i^L$.
97 Proceeding from this fundamental expression, a thermodynamic framework for cases involving
98 complex liquid mixtures, multi-component solids, and polymorphs can be developed.²
99 Thermodynamics also may determine the state of the solid, which may be anhydrous, a hydrate
100 or solvate, a salt, or one of a family of polymorphs.* When the system involves a chemical
101 reaction, the thermodynamics must include interactions of reactants, products, and by-products,
102 all of which greatly complicate the system behavior and make it difficult to formulate working
103 expressions for solute solubility.

104 In reactive crystallization, system conditions usually are selected so that reactants and
105 byproducts[‡] remain in solution, and the driving force for crystallization of the reaction product is
106 created by its synthesis. This was the goal outlined by Encarnacion-Gomez *et al.*³ and McDonald
107 *et al.*⁴ who compared the effect of pH value on solubilities of a product, ampicillin, to those of
108 the reactant, 6-aminopenicillanic acid, and byproduct, phenylglycine, to guide selection of the
109 pH value at which to run the reaction and crystallization. The approach was extended to include
110 systems in which primary products included amoxicillin and cephalexin and corresponding
111 reactants and byproducts.⁵

112 In many instances, empirical relationships, which often are based on simplifying
113 assumptions regarding the fundamental thermodynamics, are used to relate solubility as a
114 function of temperature and composition. Such approaches require experimental measurements
115 of solubilities, and the resulting correlations provide a means of interpreting and interpolating the

* Hydrates and solvates are sometimes referred to a pseudopolymorphs, but strictly speaking they are distinct chemical entities. Polymorphs, on the other hand, are all the same species, but have different packing structures.

‡ Reactants are chemical species that are consumed by a reaction; byproducts are produced by a reaction but are not the desired species. Products are generated by a chemical reaction, but the term may also be used to indicate the output from the overall process.

116 data. As an illustration, consider the findings of Hu *et al.*⁶ on the solubility of an important
117 intermediate compound, methyl D-(–)-4-hydroxy-phenyl glycinate, C₉H₁₁NO₃, in the production
118 of certain β-lactam antibiotics. Over a pH range of 1-13 they showed that the solubility was
119 lowest at the isoelectric point,* which is discussed below. Solubilities increased with solvent
120 polarity, except when water was the solvent, and it was asserted that water was an outlier
121 because of the dominance of the hydrophobic groups in the solute molecule. Temperature had
122 the most significant effect on solubility in both pure and mixed solvents, which was correlated by
123 the Apelblat equation

$$124 \quad \ln x_1 = A + \frac{B}{T} + C \ln T \quad (1)$$

125 where x_1 is the mole fraction of solute 1 and A , B and C are constants fit to data for each solvent
126 or solvent mixture (T in Kelvin).

127 The rationale for the Apelblat equation was developed by Cuevas-Valenzuela *et al.*⁷ and
128 it has since been cited in over 400 publications, with each describing its use for a variety of
129 solutes and solvents. In some instances, the third term in the equation can be omitted to obtain
130 the classic van't Hoff relationship

$$131 \quad \ln x_1 = A' + \frac{B'}{T} \quad (2)$$

132 where A' and B' are fitted parameters, and B' is often referred to as the apparent heat of solution
133 (T in Kelvin).

* The isoelectric point (pK_i) is the pH at which the species carries no net charge. For a molecule with two proton-labile moieties, like many amino acids, the isoelectric point commonly is taken to be the average of the acid dissociation constant (pK_A) of each moiety.

134 Solubilities of amphoteric species,
 135 such as amino acids, are lowest at their
 136 isoelectric point. At this condition, the solid
 137 in equilibrium with the solution is a neutral
 138 zwitterion. Addition of acid or base to move
 139 the pH value away from the isoelectric point
 140 initially causes modest increases in solubility,
 141 but then much greater increases occur as pH
 142 moves further from the isoelectric point. The
 143 distribution of acidic, neutral, and basic forms
 144 of serine are shown in Figure 1 and illustrate the general behavior of amino acids.⁸

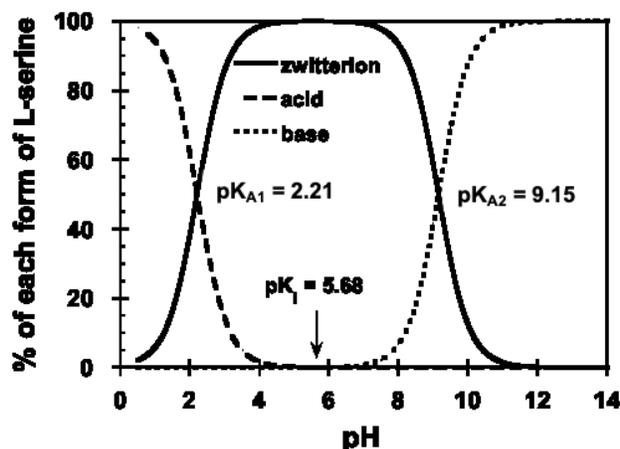


Figure 1. Distribution of acidic, neutral, and basic forms of L-serine as a function of pH value.

145 The composition of the solid in equilibrium with a coexisting solution of an amphoteric
 146 species can vary with pH. Over the pH range that includes the isoelectric point (see Figure 1), the
 147 coexisting crystal is the zwitterion (neutral species), but as pH moves towards the lower pK_{A1} the
 148 solid species may change from the zwitterion to an acid salt (for example, leucine hydrochloride
 149 when HCl is used to reduce pH). Kempkes and van Enkevort⁹ presented *in situ* micrographs
 150 showing both glutamic acid hydrochloride and glutamic acid crystals coexisting in a 1:1 solution
 151 of glutamic acid and HCl in water. Alternatively, addition of a base to a solution near the
 152 isoelectric point moves pH towards the higher pK_{A2} and the coexisting solid formed may be a
 153 basic salt: for example, sodium leucinate (or leucine sodium) when sodium hydroxide is added to
 154 a leucine solution near its upper pK_A. At pH extremes, solubilities of acid or basic salts may be
 155 lower than those of the zwitterion and used to enhance recovery of the species of interest. For
 156 example, Sano¹⁰ describes the early production of L-glutamic acid hydrochloride by contacting
 157 vegetable proteins with HCl, and then processing the recovered acid salt to become monosodium
 158 glutamate.

159 Tseng *et al.*¹¹ measured solubilities of five amino acids over a pH range from 2 to 10 and
160 used an NRTL model* to describe activity coefficients of the non-ideal solutions. Figueiredo *et*
161 *al.*¹² developed a methodology for estimating activity coefficients using UNIFAC methods and
162 the Debye-Hückel equation that they tested successfully against literature data. Additional data
163 on the effect of pH on the aqueous solubility of a number of amino acids can be found in various
164 sources.¹³⁻¹⁶

165 The presence of co-solutes and/or impurities can impact the solubility of a species of
166 interest. McDonald *et al.*¹⁷ showed that during crystallization of cephalexin, the reactants used
167 to make cephalexin inhibited complete consumption of supersaturation relative to the pure
168 cephalexin system, by effectively increasing the drug solubility. Hu *et al.*⁶ showed that
169 increasing concentrations of ammonium chloride or D-4-hydroxyphenylglycine methyl ester
170 hydrochloride increased the solubility of methyl D-(-)-4-hydroxy-phenyl glycinate. This is
171 particularly important because the ester is a reactant in the synthesis of the glycinate product. Co-
172 solutes can also decrease solubility; Isakov *et al.*²² showed that a compound with a valine-to-
173 isoleucine ratio of 2:1 was formed from solutions containing the two amino acids and the
174 compound formed a third separate solid phase with lower solubility that contaminated the pure-
175 component solid phases. The presence of electrolytes in solutions of amphoteric species such as
176 amino acids also affect the species' solubility. For example, the addition of sodium chloride to
177 neutral solutions decreased glycine solubility at low sodium chloride concentrations, but then
178 increased solubility as concentration was increased.²³ The researchers hypothesized that such
179 behavior is based on ions of the electrolyte shielding the hydrophobic characteristics of the
180 amino acid. Steendam *et al.*²⁴ examined how the difference in solubilities of two structurally
181 similar impurities in solutions of paracetamol (acetaminophen) impacted the properties of
182 paracetamol crystallized from those solutions. Further work with these species demonstrated that
183 despite their significant impact on paracetamol crystal properties, the impurities had little
184 influence on paracetamol solubility at the prescribed impurity concentrations.²⁵

* The NRTL model (non-random two-liquid model) is an expression used to correlate activity coefficients of species in solution with the composition (expressed as mole fractions) of the solution. Activity coefficients are used to account for solution nonidealities, which usually represent deviations from Raoult's law. UNIQUAC and UNIFAC are group-contribution techniques for predicting activity coefficients.

185 Solubility is a function of solvent composition. For example, Granberg and Rasmuson²⁶
186 measured solubilities of paracetamol in 26 solvents and determined ideal solubilities and activity
187 coefficients in the saturated solutions. Also, Jiang and Ni²⁷ considered how compositions of
188 water-acetic acid mixtures influenced paracetamol solubilities and crystal morphology. Solvent
189 effects on the solubilities of amino acids also have been investigated; the effects of ethanol on
190 aqueous solubilities of twenty amino acids were determined and found to be related to the side
191 chain on the amino acid.²⁸

192 The relationship of solubility to the form of a co-existing solid at equilibrium has been
193 observed in the work of Zhang *et al.*²⁹ who found that hydrogen-bonding ability was a key factor
194 in determining solubility and polymorph formation of clopidogrel hydrogen sulfate (CHS). They
195 used two different experimental procedures to determine solubilities of CHS Forms I and II in
196 five alcohols, two ketones and two acetates. The van't Hoff relationship was used to correlate
197 solubilities in the nine solvents for the two different polymorphic forms. Solubilities in ethyl
198 acetate of Forms I and II, along with that of an amorphous form, were also determined by Lu *et*
199 *al.*³⁰ Additionally, temperature may determine which of two polymorphs is more soluble in a
200 given solvent, with the one having lower solubility being more stable. In enantiotropic systems
201 the form that has the lowest solubility changes with temperature. While there do not appear to be
202 any studies on reactive crystallization of enantiotropic species, several well-known enantiotropes
203 can be crystallized by reactive crystallization (e.g. *p*-aminobenzoic acid^{31, 32}).

204 **Supersaturation.** The difference between a system at a given state and at equilibrium
205 represents a driving force for change, which in crystallization is referred to as supersaturation.
206 The formal definition of supersaturation is the difference in chemical potential of a solute at the
207 existing conditions (μ_i) and at equilibrium (μ_i^*): that is, $\mu_i - \mu_i^* = RT \ln(a_i/a_i^*)$, where a_i and a_i^*
208 are activities of solute i in the solution at the existing state and at equilibrium, T is absolute
209 temperature and R is the gas constant. Activity can be expressed as the product of an activity
210 coefficient (γ_i), mole fraction* and reference-state fugacity; choosing the same reference state for
211 the existing and saturated solutions (for example, pure supercooled liquid at the system
212 conditions) gives

* Activities based on other expressions of composition such as concentration (mol/L) can be used.

$$\Delta\mu_i = RT \ln \frac{\gamma_i x_i}{\gamma_i^* x_i^*} \quad (3)$$

Unless system conditions produce a significant difference between γ_i and γ_i^* , this equation reduces to the simple dimensionless expression

$$\frac{\Delta\mu_i}{RT} = \ln \frac{x_i}{x_i^*} \quad (4)$$

If the ratio of mole fractions is less than about 1.2, there is less than 10% error in substituting $\left[\left(x_i/x_i^*\right)-1\right]$ for $\ln\left(x_i/x_i^*\right)$. The dimensionless relative supersaturation σ_i then becomes

$$\sigma_i = \frac{x_i - x_i^*}{x_i^*} = S_i - 1 \quad (5)$$

where S_i is the ratio of mole fractions and is referred to as the supersaturation ratio. Expressions for systems involving hydrates, partially dissociated electrolytes and mixtures of electrolytes have been developed by Sohnle and Mullin.³³

Mass balances and other operations in crystallization are often more convenient when compositions are expressed in terms of ratios of mass of solute (w_i) per unit mass of solvent (w_s): $X_i = w_i/w_s$. The relative supersaturation and supersaturation ratio can be expressed as

$$\sigma_i = \frac{X_i - X_i^*}{X_i^*} = S_i - 1 \quad (6)$$

provided $\sum(w_i/M_i) \ll 1$ where w_i is the mass of solute i in solution and M_i is the molecular weight of i ; w_s and M_s are, respectively, the mass of solvent and the solvent molecular weight.

Another important way of expressing supersaturation is in terms of concentrations, c_i (mol/L):

$$\sigma_i = \frac{c_i - c_i^*}{c_i^*} \quad (7)$$

which is valid if the solution molar densities at system conditions and at saturation are approximately the same. Mullin³⁴ provides an example illustrating a violation of this assumption with mixtures of sucrose, where differences between system conditions and saturation are substantial.

237 It may be useful at this point to contrast how supersaturation is generated in reactive
238 crystallization with how it is developed in other settings: here a chemical reaction creates the
239 desired solute. If the system is isothermal and solvent has constant composition and is not being
240 removed, σ can be created only as a species is formed by a chemical reaction. If the system is
241 operating as a batch unit, with reactants added at the start of the process, the concentration of the
242 product, c_i would typically increase from an initial value of zero. Upon exceeding the solubility,
243 c_i^* , the supersaturation ratio, S_i , becomes greater than one, and crystallization can begin to occur
244 and proceed as long as the reaction maintains supersaturation in the system ($S_i > 1$).

245 Reactive crystallization necessarily occurs in the presence of multiple components, in
246 addition to the product. Accordingly, while the product solubility in pure solvent may provide a
247 first approximation to behavior in the reaction solution, such an assumption may be incorrect in
248 describing complicated interactions in the system with multiple species. As described earlier, the
249 effects of other solutes may alter (increase or decrease) product solubility, c_i^* , and therefore
250 supersaturation, and if solubility is increased, there may no longer be a driving force for
251 crystallization. As the objective is to recover pure product, the supersaturation ratio of other
252 species formed in the reaction system must remain below their metastable limits (described in the
253 next section). Otherwise, subsequent separation of species simultaneously crystallized will be
254 required and detract from the efficiency of the process.

255 ***Nucleation and Growth Kinetics.*** The kinetics of crystallization are defined by
256 nucleation and growth phenomena and play a central role in determining the characteristics of a
257 crystalline product, such as crystal size distribution.* In this section, nucleation is discussed from
258 the perspective of mechanisms leading to formation of crystals, and growth is recognized as how
259 crystals increase in mass (and size). Kinetics of nucleation and growth are given for several
260 crystallization systems to give context for crystallization kinetics in reactive systems.

261 *Nucleation*, in the context of this manuscript, is formation of a solid crystalline phase
262 from a liquid solution, which often sets the character of the process and is a critical factor in
263 determining product crystal size distributions. Classical nucleation theory (CNT) is based on

* Agglomeration and breakage, two additional kinetic phenomena that can affect crystal size distribution, are covered by Randolph and Larson,³⁵ Lewis *et al.*,³⁶ Ochsenein *et al.*,³⁷ and Salvatori and Mazzotti.³⁸

264 homogeneous and heterogeneous mechanisms, both of which describe formation of crystals
 265 through a process of sequentially combining constituent units to form larger and larger entities
 266 until a stable nucleus is produced.^{39, 40} Both heterogeneous and homogeneous mechanisms are
 267 referred to as primary nucleation because existing crystals play no direct role in the nucleation
 268 mechanism. Supersaturation has a highly nonlinear relationship to primary nucleation rate as
 269 illustrated by the following equation from classical nucleation theory:³⁶

$$270 \quad J = AS \exp \left(- \frac{\phi 16 \pi \gamma_{sl}^3 v^2}{3 (kT)^3 (\ln S)^2} \right) \quad (8)$$

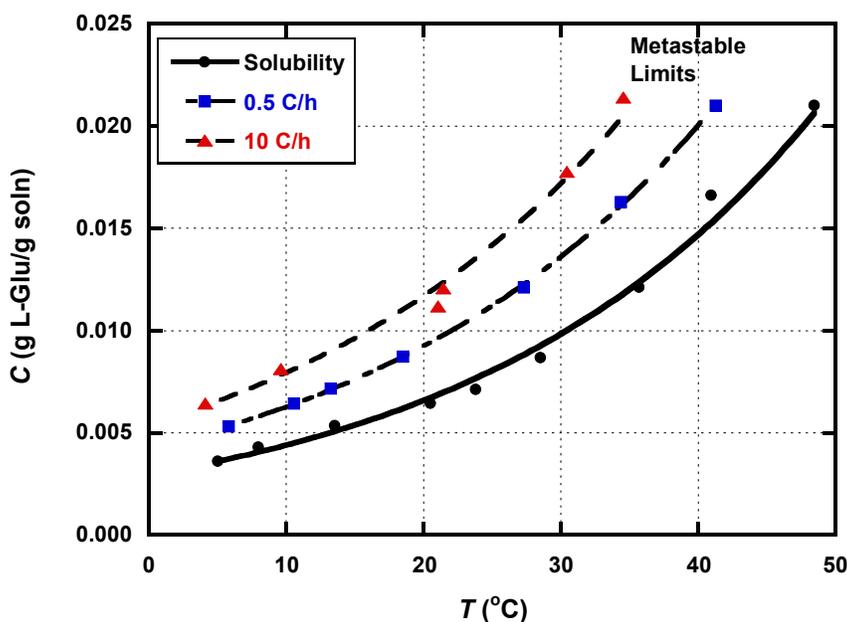
271 where J is the primary nucleation rate, A is a preexponential term, γ_{sl} is interfacial energy
 272 between solid and liquid, v is molecular volume, k is the Boltzmann constant, T is absolute
 273 temperature, and S is the supersaturation ratio as defined earlier. The term ϕ is an empirical
 274 parameter whose value is 1 for homogeneous nucleation (heterogeneous surfaces play no role in
 275 the nucleation event) and between 0 and 1 for heterogeneous nucleation (the presence of
 276 heterogeneous surfaces lowers the energy barrier to nucleation). Paxton *et al.*⁴¹ showed the effect
 277 of ϕ in distinguishing between homogeneous and heterogeneous nucleation of chicken egg-white
 278 lysozyme. Because the effect of supersaturation in the exponential term is much greater than in
 279 the preexponential, the equation is often written as:³⁴

$$280 \quad J = A' \exp \left(- \frac{\phi 16 \pi \gamma_{sl}^3 v^2}{3 (kT)^3 (\ln S)^2} \right) \quad (9)$$

281 Alternative mechanisms for primary nucleation have been proposed, including a two-step
 282 process in which a metastable liquid phase is formed prior to formation of solid. These are
 283 reviewed in various sources but are beyond the scope of this review.^{36, 42}

284 It is generally recognized that solutions can maintain supersaturation without primary
 285 nucleation taking place over modest observation timescales. Classical nucleation theory shows
 286 that formation of a stable nucleus at low supersaturations is rare, but then substantial nucleation
 287 occurs beyond a threshold referred to as a metastable limit. The region of a phase diagram
 288 between solubility and nucleation is referred to as a metastable zone; at a given solute
 289 concentration, the difference between the saturation temperature and the temperature at which
 290 nucleation occurs is known as the metastable zone width (MSZW). Figure 2 illustrates behavior

291 of mixtures of DL-glutamic acid in water by showing solubility and metastable limits obtained
 292 when initially undersaturated solutions were cooled at different rates. Clearly, metastable limits
 293 are not thermodynamic quantities.
 294



295
 296 *Figure 2. Solubility and metastable limits for glutamic acid. Adapted from the work of Svang-Ariyaskul.⁴³*

297 Primary nucleation in the metastable zone is unlikely but not impossible. More than 550
 298 references emerged from a recent search using key words nucleation and metastable zone,
 299 demonstrating the effort that has gone into measuring how the metastable limit varies according
 300 to the system in which it is measured. The width of the metastable zone has been measured to be
 301 as wide as 55 °C for citric acid ($\sigma \approx 1.4$) with a cooling rate of 0.05 K/min.⁴⁴ Kashchiev *et al.*⁴⁵
 302 and Kashchiev and van Rosmalen⁴⁶ provide a formula for estimating the width of metastable
 303 zones. In cooling crystallization, the MSZW increases with increased cooling rate (see Figure 2).
 304 Ma *et al.* found the same result for reactant addition rate; they showed that in the reactive
 305 crystallization of lithium carbonate, increasing the addition rate led to a larger MSZW.⁴⁷
 306 Generally, the MSZW increases as the rate of supersaturation generation increases. Boukerche *et*
 307 *al.*⁴⁸ found that adding heterogenous solids reduced metastable zone widths and facilitated
 308 primary nucleation of different polymorphs. Sparging of inert gases was found to shrink the
 309 MSZW for several systems⁴⁹ and lessen the induction time.⁵⁰

310 Primary nucleation rates are often linked to induction time, which is defined as the
311 elapsed time between a solution becoming supersaturated and observation of nuclei formation.
312 An estimate of this quantity frequently assumes that the time to form a nucleus is much greater
313 than the time required for that nucleus to grow to observable size. The stochastic nature of
314 primary nucleation contributes to variability in induction-time measurements, which have been
315 correlated to probability distribution functions.⁵¹⁻⁵⁵ Interestingly, most, if not all, of the studies
316 observing stochastic outcomes are in small volumes (frequently 1 mL). Noting this, other
317 researchers have pointed out that as system volume increases, the observed stochasticity in both
318 induction time and MSZW is diminished.^{56, 57} Kadam *et al.*⁵⁶ described experiments on
319 paracetamol nucleated from clear 1-mL and 1-L solutions. In the former, MSZWs in many
320 experiments ranged from 7.2 °C to 33.8 °C. Variations in the 1-L experiments were low, having
321 MSZWs between 7.0 °C and 7.5 °C: in other words, near the lower end of the range for 1-mL
322 measurements. Evolving from such observations, Kadam *et al.*⁵⁶ proposed what they called the
323 Single Nucleus Mechanism, which postulates that at a given supersaturation a single nucleus
324 forms and ultimately leads to secondary nucleation. Kadam *et al.*⁵² extended this analysis by
325 suggesting that MSZW is a volume-dependent stochastic property in which the stochastic nature
326 of primary nucleation is dominant in systems of small volume; however, increasing system
327 volume enhances the probability of primary nucleation, making it deterministic at sufficiently
328 large volumes.

329 Uncertainties associated with primary nucleation lead to the common practice of seeding,
330 which is intentionally adding pre-existing crystals of the desired species into the system expected
331 to produce product crystals. This shift in the controlling phenomenon from primary to secondary
332 nucleation is especially useful in industrial settings where reproducibility of outcomes is a
333 paramount consideration. Moreover, after startup, continuous crystallizers maintain a slurry of
334 crystals which serves to repopulate itself through secondary nucleation. By this mechanism, a
335 metastable polymorph may be produced continuously. Kollges and Vetter predicted by modeling
336 and demonstrated with metastable β -L-glutamic acid that by tuning the residence time of the
337 reactor to the secondary nucleation kinetics (or adjusting the secondary nucleation kinetics by
338 milling) a population of the metastable form could be sustained indefinitely.^{58, 59} Similar results
339 were found by Agnew *et al.*⁶⁰ for Form II of paracetamol.

340 Any mechanism involving existing crystals in the formation of new crystals is referred to
 341 as secondary nucleation. In the late 1960s and early 1970s, considerable research identified this
 342 form of nucleation as an important aspect of crystal formation, especially in industrial settings.
 343 This early work was summarized in a foundational review by Garside and Davey⁶¹ and a later
 344 review provided by Agrawal and Paterson.⁶² Among several mechanisms of secondary
 345 nucleation, contacts or collisions of existing crystals with other crystals, crystallizer internals,
 346 circulation pumps and impellers, which is known as contact nucleation or collision breeding, is
 347 considered most important. Contact nucleation is characterized by a low-order dependence on
 348 supersaturation (compared to primary nucleation) and absence of a metastable region. The latter
 349 factor means that substantial secondary nucleation can occur at low supersaturation. Although
 350 secondary nucleation is often considered to be a form of attrition,* it need not produce
 351 macroscopic damage to parent crystals (those from which secondary nuclei are produced).⁶³⁻⁷⁰

352 Secondary nucleation kinetics have been examined extensively for stirred-tank
 353 crystallizers, with some of the early proposed correlations provided by Grootsholten *et al.*,⁷¹
 354 Ploss and Mersmann,⁷² and others. Lewis *et al.*³⁶ summarize such relationships in two related
 355 power-law equations that link nucleation rate to variables such as impeller speed, power input,
 356 and mass of crystals per unit volume:

$$\begin{aligned}
 B_{\text{sec}} &= k_{\text{N}} G^i N^k M_{\text{T}}^j \\
 B_{\text{sec}} &= k'_{\text{N}} S^a P^b M_{\text{T}}^j
 \end{aligned}
 \tag{10}$$

358 where B_{sec} is the secondary nucleation rate [number/volume·time], G is crystal growth rate, N is
 359 rotational speed, M_{T} is a measure of the crystal concentration in the stirred-tank system (usually
 360 mass of crystals/volume of either slurry or solvent), S is supersaturation ratio, P is specific power
 361 input, and the other quantities are fitted parameters. Such correlations overlook some important
 362 process variables, such as type of impeller and existence of baffles or a draft tube and are likely
 363 to be most useful in scaling up between similar crystallizer geometries.

364 The roles of primary and secondary nucleation in a batch operation depend on whether
 365 seeding is used. Beginning with a clear solution (unseeded) means primary nucleation is an

* In this context, attrition is taken to mean removal of small parts of a crystal by abrasion, collision, or friction.

366 essential step in crystal formation. Even so, it is likely that crystals resulting from primary
 367 nucleation grow and then serve as stimuli for secondary nucleation, analogous to the Single
 368 Nucleus Mechanism.⁵² Li *et al.*⁷³ used experiments in which paracetamol was crystallized from
 369 clear solutions in ethanol to evaluate models, and then used these models to demonstrate that
 370 only a small fraction of the final crystals per batch originated from primary nucleation. The
 371 modeling results indicate that the foremost role of primary nucleation is to produce a small
 372 number of crystals, which then serve to stimulate secondary nucleation. The overall rate of
 373 crystallization in seeded batch and continuous operations is generally dominated by secondary
 374 nucleation.

375 *Crystal growth* rates depend on how they are measured, and they may be expressed in
 376 terms of those measurements. For example, both the linear advance rate of a specific crystal face
 377 and the rate of change in a characteristic dimension (which, again, can be determined in a variety
 378 of ways) are measures of growth kinetics. The rates of change in the mass of a crystal or a
 379 population of crystals also provide growth rates. These seemingly different measures are related
 380 through crystal shape and density:

$$381 \quad \frac{dm_{\text{crys}}}{dt} = 3\rho \frac{k_v}{k_a} a_{\text{crys}} G \quad (11)$$

382 where m_{crys} and a_{crys} are the mass and interfacial area of a crystal, ρ is its density, k_a and k_v are
 383 area and volume shape factors (quantities that relate crystal surface area and volume to a selected
 384 characteristic dimension), and G is rate of change in the characteristic crystal dimension.

385 At least two resistances in series must be overcome for growth to occur: (1) transport (by
 386 diffusion or convection) of a solute species through solution to the crystal face and (2)
 387 incorporation of solute into a crystal lattice. The rates at which the two processes occur must be
 388 equal at steady state, and the growth rate may be expressed in terms of transport coefficients and
 389 driving forces associated with each:

$$390 \quad G = k_d (c - c_{\text{int}}) \quad (12)$$

$$391 \quad G = k_r (c_{\text{int}} - c)^r \quad (13)$$

392 where r , k_d , and k_r are fitted parameters, c is solute concentration and c_{int} is solute concentration
 393 at the crystal-solution interface. Should the dominant resistance to growth lie in surface

394 incorporation, $c \rightarrow c_{\text{int}}$ and $G = k_r (c - c^*)^r$; alternatively, if the dominant resistance is transport
395 to the crystal surface, $c_{\text{int}} \rightarrow c^*$ and $G = k_d (c - c^*)$.

396 Concepts of how molecules or ions incorporate into a growth face generally are based on
397 either birth-and-spread or screw-dislocation theories. Mechanistic descriptions of these
398 approaches, along with primary sources, are provided in several references.^{34, 36} An empirical
399 power-law expression can be used to relate growth kinetics to supersaturation by fitting growth-
400 rate data:

$$401 \quad G = k_G A_G \sigma^g \quad (14)$$

402 where k_G is a rate coefficient and A_G is the surface area of the crystals. The exponent g is a fitted
403 parameter with typical values between 1 and 2. This range of values for g encompasses those
404 resulting from the cited theories, but, as demonstrated by Soto and Rasmuson,⁷⁴ distinguishing
405 among the birth-and-spread and spiral growth theories is difficult; the empirical power-law is
406 often sufficient.

407 Empirical expressions used to correlate nucleation and growth kinetics should be
408 developed in systems similar to those for which the expressions are to be used. Reactive
409 crystallizations present challenges in that regard because of the inherent presence of species
410 other than a primary crystalline product; in other words, reactants, byproducts, and other species
411 can impact crystallization kinetics of product crystals. The effect can result from changing either
412 the solubility (as discussed previously) or nucleation and/or growth kinetics. Illustrations of the
413 effect on growth kinetics are provided by Capellades *et al.*⁷⁵ who found that impurities from
414 upstream operations impacted the growth rate of the antibiotic ciprofloxacin in a continuous
415 crystallizer, while having little effect on nucleation kinetics. McDonald *et al.*¹⁷ found that during
416 the reactive crystallization of cephalixin (which is from an antibiotic family that is different from
417 ciprofloxacin) the presence of reactants inhibited crystal growth in a mechanism dependent on
418 both the reactant concentration and cephalixin supersaturation. Neither of these two studies
419 found an effect of co-solutes on nucleation kinetics. Kubota⁷⁶ presents a broad review of the
420 impact of co-solute species on crystal growth.

421 **Chemical Reactions.** Two broad categories of reactions are considered in this review:
422 ionic reactions and covalent reactions. Both will be covered in sections that provide specific
423 examples of such systems.

424 Ionic reactions are defined by bonds formed from electrostatic attractions between
425 oppositely charged ions; for example, a positive sodium ion and negative chloride ion in sodium
426 chloride (NaCl). Ionic reactions tend to be very fast; formation of the bond requires only
427 displacement of solvent molecules from the solvation shell and the interaction is governed
428 principally by coulombic forces. Computational work on aqueous NaCl crystallization suggests
429 that the rate limiting step in this reaction between Na^+ and Cl^- is the removal of water from the
430 chloride attachment site on the NaCl crystals.⁷⁷ One caveat to these results is the low
431 supersaturations studied. The ability of water to transport protons at a rate faster than expected
432 by diffusion suggests that in neutralizations (see below) the solvent may not pose the same
433 barrier as in inorganic ionic systems like the NaCl system.⁷⁸

434 Neutralizations are a subset of ionic reactions that involve the addition or removal of a
435 proton from a proton-labile functional group such as an acid, amine, or alcohol. Neutralization
436 reaction rates are often considered instantaneous in the reactive crystallization literature.^{3, 79-81}
437 The rates are governed by the collision frequency of the reactants; every collision between
438 reactants results in the product being formed, regardless of collision energy or orientation.
439 Therefore, these reactions are often treated as mixing-limited or diffusion-limited. Many studies
440 investigate means of mixing reactants to ensure a uniform reaction,⁸¹⁻⁸⁵ with a minireview by
441 Teychene *et al.*⁸⁶ The equilibrium composition of these reactions is highly pH-dependent in
442 aqueous systems; in organic solvents equilibrium composition depends on the species as well as
443 the proton capacity of the solvent.

444 Covalent reactions involve forming bonds requiring the sharing of electrons between
445 atoms. These reactions range from very slow to fast and often require a catalyst; both the flow
446 timescale of the reactor and diffusion in and out of the catalyst (if a heterogeneous catalyst is
447 used) may impact the effective reaction rates and overall conversion. While many covalent
448 reactions require a catalyst to proceed at appreciable rates, the presence of the catalyst does not
449 change the reaction equilibrium, which may favor reactants or products, depending on the
450 specific system. Many covalent reactions involve networks or series of reactions, which further
451 complicate reaction equilibria since the products of one reaction are reactants in another.
452 Covalent reactions may also be most amenable to reactive crystallization, as they may benefit
453 from shifts in equilibrium, enhancements in rate and selectivity, isolation of intermediates, and
454 many of the other motivators for implementing a reactive crystallization process.

455 The rate of reaction is described by an equation that expresses the rate of reactant
456 consumption as a function of reactant concentration and reaction conditions (such as
457 temperature, pressure, etc.). The function can be derived empirically, from insight into the
458 reaction mechanism, or through first-principle approaches in computational chemistry. For the
459 simple reaction $A \rightarrow B$, the elementary rate equation could be $r = -dc_A/dt = k_1 c_A^n$ where the rate
460 constant k_1 is typically a function of reactor conditions (e.g. temperature), c_A is the concentration
461 of A (mol/L), and the exponent n is the reaction order. If the reverse reaction $B \rightarrow A$ also occurs
462 then the overall rate equation for A (assuming a first order reaction so that $n = 1$) would be
463 $r = k_1 c_A - k_{-1} c_B$ where the subscript -1 indicates the reverse of the forward reaction.⁸⁷

464 Reaction equilibrium occurs when the rates of the forward and reverse reactions are equal
465 and therefore the overall rate is zero; that is, $dc_A/dt = 0$.^{*} Such conditions are reached when
466 sufficient product has accumulated for the forward (desired) and reverse reactions to have equal
467 rates. The ratio of the forward and reverse rate constants, k_1 and k_{-1} , is the equilibrium constant,
468 $K_{eq} = c_B/c_A$. Equilibrium for a reaction system involving multiple reactions (for example,
469 $A \rightleftharpoons B \rightleftharpoons C$) means that the concentrations of all species are constant and the reaction
470 equilibrium constant for the overall system is the product of the individual equilibrium constants:
471 $K_{overall} = K_1 K_2$. If the concentration of a compound, such as species B in the above system, is
472 elevated above its solubility, then crystallization removes the species from solution and pulls the
473 reaction further towards its production. Overall equilibrium of the system is reached when there
474 is no driving force for reactions, crystal nucleation, growth, or dissolution (i.e. the chemical
475 potential of each species is the same in all phases, and temperature and pressure are uniform).

476 In reactive crystallization, elementary kinetic expressions may be unknown, in which
477 case empirical relations can be derived. Take for example the reactive crystallization of a crop-
478 protection agent, Z, considered by Bhamidi *et al.*⁸⁸ The agent is synthesized in the reaction $2A +$
479 $M \rightarrow Z$ with Z crystallizing from the water/methanol reaction solvent. It was empirically
480 determined that consumption of M followed the rate equation $-dc_M/dt = k_1 c_A c_M$ where k_1 is the
481 rate constant, and c_A and c_M are the concentrations of A and M respectively. An Arrhenius

* This situation is analogous to solid-liquid equilibrium where the rates of crystallization and dissolution are equal.

482 relationship accounted for the dependence of k_1 on temperature, $k_1 = k_0 \exp(-E_A/RT)$ where k_0
 483 is the frequency factor, E_A is the activation energy, R is the universal gas constant, and T is the
 484 temperature. They were able to determine the heat of reaction as well as the activation energy
 485 and frequency factor using calorimetry. The relatively simple expression used here was sufficient
 486 for an economic analysis of the homogeneous uncatalyzed reaction to produce Z.

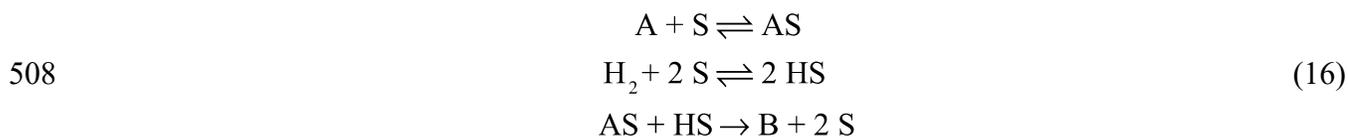
487 Complicated expressions are often required to describe complex reactions, especially
 488 those requiring catalysts. Uncatalyzed reactions may only have one or two local energy minima
 489 along their reaction pathway; catalyzed reactions, on the other hand, often have a more
 490 complicated energy pathway with several transition states and energy minima corresponding to
 491 different interactions between the catalyst and reacting species. Each of these steps has the
 492 potential to be a rate-limiting transition state, leading to complex rate equations.

493 For example, enzymes, which represent an important class of catalysts, were used in a
 494 reactive crystallization leading to deracemization of amino acids.⁸⁹ The authors of that study
 495 confirmed that in the reactive crystallization the enzyme D-amino acid oxidase followed
 496 Michaelis-Menten kinetics:

$$497 \quad r = c_{\text{enz}} \frac{k_{\text{cat}} c_A}{K_M + c_A} \quad (15)$$

498 where c_{enz} is the concentration of the enzyme, c_A is the concentration of the reactant, k_{cat} is the
 499 catalytic rate constant, and K_M is the Michaelis constant. When the reactant concentration is large
 500 ($c_A \gg K_M$), as is often the case, the reaction rate varies only with the enzyme concentration,
 501 rendering catalyst concentration an important design variable.⁸⁷ When $c_A \ll K_M$ the rate is
 502 sensitive only to the reactant concentration.

503 Catalyzed reactions involving two reactants require rate equations of even greater
 504 complexity; at different concentration regimes the order of the reaction may appear to change as
 505 the rate-limiting step shifts from one state to another. An example is palladium-catalyzed
 506 hydrogenolysis, involving hydrogen and a second reactant, which is found in several reactive
 507 crystallization systems.⁹⁰⁻⁹³ Yap *et al.*⁹⁴ found that these reactions follow the mechanism



509 where A is the species undergoing hydrogenolysis, B is the product, and S denotes a catalytic
 510 surface adsorption site; AS and HS indicate adsorbed reactant and hydrogen, respectively. They
 511 formulated the rate equation using Langmuir-Hinshelwood kinetics as

$$512 \quad r = kc_s^2 \frac{K_A c_A (K_H c_{H_2})^{1/2}}{\left[1 + K_A c_A + (K_H c_{H_2})^{1/2}\right]^2} \quad (17)$$

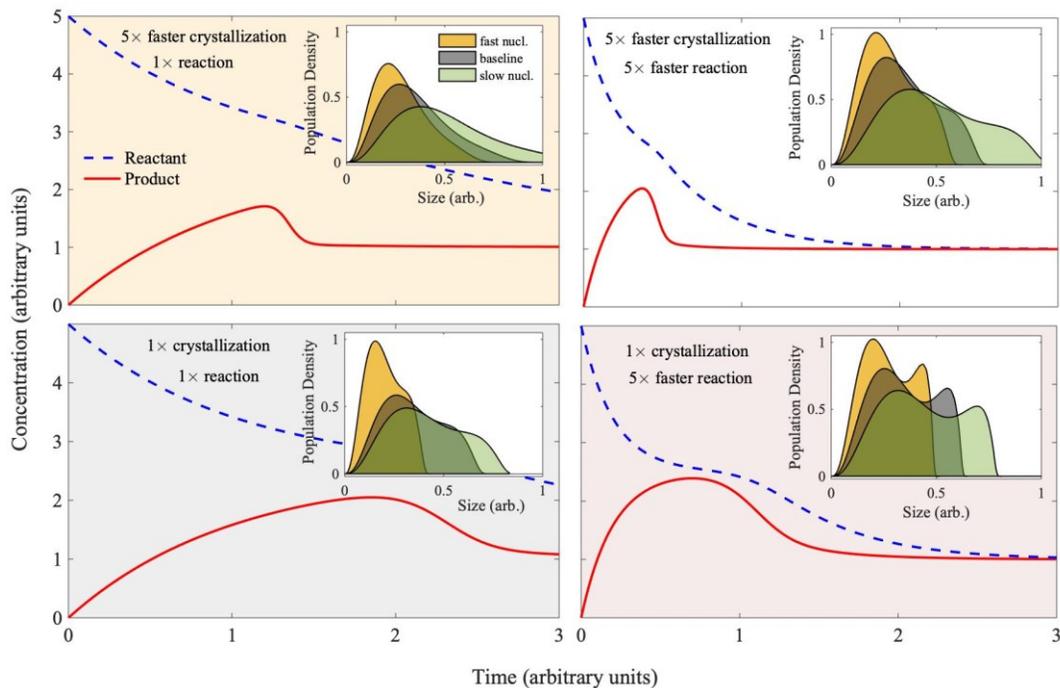
513 where c_A and c_{H_2} represent concentrations of reactants A and H_2 , c_s is the surface concentration
 514 of active sites S, and K_A , K_H , and k represent the surface adsorption equilibrium constants for the
 515 first reaction, the second reaction, and the rate constant of the third reaction, respectively. The
 516 number of reactants is not limited to one (as in the above enzyme example) or two (as in the
 517 above palladium example) reactants; in general, increasing the number of species increases the
 518 complexity of the overall rate equation unless simplifying assumptions can be made.

519 Catalysts may be homogeneous (dissolved in solution) or they may be heterogeneous; in
 520 the latter case, the active material often is bound to a porous, inert support. When a catalyst is a
 521 solid, for example platinum supported on ceramic or an enzyme immobilized on a polymer, both
 522 the rate of reactant consumption at the catalyst surface and the rate of reactant replenishment by
 523 diffusion or convection (from the bulk fluid to the surface) may affect the overall reaction
 524 kinetics. Solid catalysts are evaluated by their effectiveness factor η , which is defined as the ratio
 525 of the observed reaction rate r_{obs} to the reaction rate with rapid mass transfer r .⁹⁵ An
 526 effectiveness factor close to unity indicates good utilization of the active catalytic material (i.e.
 527 the palladium or enzyme on the solid support). An effectiveness factor $\ll 1$ indicates inefficient
 528 use of the catalytic material; a re-engineering of the catalyst may increase the effectiveness
 529 factor, possibly by changing the size or morphology of the catalyst surface, the catalyst loading,
 530 the pore size of the inert support, or other aspects of the catalyst. A similar concept for crystal
 531 growth involving resistances in series was described in the previous section, although usefulness
 532 of the effectiveness factor for crystal growth is limited.⁹⁶

533 **Combined Crystallization and Reaction Kinetics.** Taken together, the kinetics of
 534 nucleation, growth, and reaction, along with process configuration, determine the quality of the
 535 crystal product. For illustrative purposes, four different kinetic scenarios are examined for the
 536 first-order reversible reactive crystallization $A \rightleftharpoons B \rightarrow B_{(s)}$ (with $K_{eq} = 1$) taking place in a batch,
 537 isothermal, unseeded system: scenario (1) slow reaction and slow crystallization kinetics ($1\times$),

538 (2) fast reaction and fast crystallization kinetics ($5\times$), (3) slow reaction and fast crystallization
 539 kinetics, and (4) fast reaction and slow crystallization kinetics. For each of the four cases, three
 540 different relative rates of nucleation and growth were examined, where the primary and
 541 secondary nucleation rates (A' and k_N from Equations 9 and 10, respectively) were increased or
 542 decreased by a factor of five. The growth rate was varied to match the concentration profile
 543 while compensating for the change in nucleation rate, as is observed experimentally in many
 544 well-mixed crystallizers.⁹⁷ Details of the simulation are available in the supplementary material.

545 For each case, the concentrations of reactant A and product $B_{(s)}$ over time and endpoint
 546 normalized population densities (a representation of the more general crystal size distribution)
 547 are shown in Figure 3. Experimental observations of the concentration profile and end-point
 548 population density can be used to fit nucleation and growth kinetics.¹⁷ As can be seen, depending
 549 on the relative rates of reaction, nucleation, and growth, a batch reactive crystallization can yield
 550 a variety of population densities, some of which may not meet product specifications. Bimodal or
 551 skewed population densities may be particularly problematic.



552
 553 *Figure 3. Quadrant plot showing solution concentrations (normalized by the saturation concentration) of*
 554 *reactants (dashed blue curves) and products (solid red curves) during the first order reaction $A \rightleftharpoons B \rightarrow B_{(s)}$ for*
 555 *baseline reaction and crystallization kinetics (gray, lower left), fast reaction baseline crystallization kinetics (pink,*
 556 *lower right), fast crystallization baseline reaction kinetics (orange, upper left) and fast reaction and crystallization*
 557 *kinetics (white, upper right). The insets depict the population density calculated at baseline nucleation rate (gray),*
 558 *fast nucleation (yellow), and slow nucleation (green); for the different nucleation rates the growth rate was varied*

559 *to match the concentration profile. In real systems the growth rate typically varies to match the rate of*
560 *supersaturation generation. The size units and population density have been normalized such that the scale is the*
561 *same in each inset.*

562 The concentrations in Figure 3 have been normalized by the solubility of the product,
563 rendering the solid curve the product supersaturation. As expected, with slower crystallization
564 kinetics a larger supersaturation accumulates before crystal growth can match the rate of the
565 reaction. Crystallization is helping to pull the reaction towards the product, as illustrated by the
566 faster consumption of reactant in cases with faster crystallization kinetics. Sustained higher
567 supersaturations lead to large amounts of primary nucleation and bimodal crystal population
568 densities. If the product B were consumed by a second reaction the sustained higher
569 supersaturation would be expected to further decrease yield and productivity. When the rates of
570 reaction and crystallization are scaled together, comparable population density functions are
571 obtained, as can be seen in the similarity between the bottom left and top right insets in Figure 3.

572 In generalizing Figure 3 one realizes that in reactive crystallization systems the rate of
573 crystallization will always lag the reaction, a consequence of the sequential nature of the process.
574 Enhancing the rate of crystallization (and the benefits of reactive crystallization) can be
575 accomplished by increasing the rate of the reaction, as can be seen comparing the bottom two
576 panes of Figure 3; the faster reacting system spends less time at an elevated supersaturation and
577 reaches a higher peak supersaturation. Alternatively, the kinetics of crystallization can be sped
578 up by techniques such as milling, which is discussed in a later section, to improve overall yield
579 and size distribution. A detailed understanding of the process kinetics is indispensable for
580 producing material with the desired properties in a process with the desired performance.

581 **Types of Reactions**

582 ***Crystallization and Ionic Reactions.*** Ionic compounds utilized in applications ranging
583 from pharmaceutical additives^{98,99} to polymer fillers,^{100,101} can be produced via reactive
584 crystallization. Processes involving reactive crystallization can be used for removing
585 contaminants, such as heavy metals, from water,¹⁰²⁻¹⁰⁴ or for separating a product, such as
586 lithium carbonate, from solution.^{105,106} Ionic reactions include synthesis of inorganic
587 compounds, formation of salts, and neutralization of organic ions.

588 Reactive crystallization of ionic compounds is based on the reaction between an anion
589 and a cation in solution. The solutions are typically aqueous, but other solvents, such as
590 supercritical CO₂, have been used.¹⁰⁷ The solubility of the target compound is often substantially

591 lower than that of precursors supplying the reacting ions. For sparingly soluble ionic species,
 592 solubility is usefully defined in terms of a solubility product. For example, for the species A_aC_c
 593 having an anion A with a negative charge c^- and a cation C with a positive charge a^+ , the
 594 solubility product K_{sp} is given by

$$595 \quad K_{sp} = [A^{c-}]_{eq}^a [C^{a+}]_{eq}^c \quad (18)$$

596 where the bracketed terms represent the concentrations of ions at equilibrium in mol/L. The
 597 relative supersaturation σ for the compound A_aC_c may be defined as:

$$598 \quad \sigma = \frac{[A^{c-}]^a [C^{a+}]^c - K_{sp}}{K_{sp}} \quad (19)$$

599 $[A^{c-}]$ and $[C^{a+}]$ are the anion and cation concentrations at system conditions in the same units
 600 used for K_{sp} . The time course of ion concentrations during a process can be measured using an
 601 ion-selective electrode,¹⁰⁸ a conductivity sensor,⁹⁹ or a spectrophotometric probe, such as a UV-
 602 vis probe,¹⁰⁹ an IR probe,¹¹⁰ or a Raman probe.¹¹¹ In systems with high ionic strength, Equations
 603 18 and 19 should be modified by replacing each concentration with an activity, which is defined
 604 as the product of a concentration and an activity coefficient. In systems at low concentration,
 605 ions do not interact with each other and the activity coefficient can be assumed to be unity,
 606 otherwise, the activity coefficient for each species can be estimated using the Debye-Hückel
 607 theory.¹¹² Note that in some cases (for example, the production of calcium phosphate), the
 608 compounds may have several dissociation states, depending on pH value, and the solubility
 609 product should be corrected to take that feature into account.¹⁰⁵

610 A common theme in many ionic reactive crystallization studies is that the reaction between
 611 the anion and cation is considered instantaneous. The dynamic behavior of the system is governed
 612 by crystal nucleation, growth, and mixing. Fast reaction kinetics contrast with those undergoing
 613 covalent reactions such as enzymatic synthesis and crystallization of ampicillin, where the reaction
 614 step limits the overall timescale of the process.¹¹³ Rapid reaction kinetics, in addition to the
 615 formation of a practically insoluble compound, may lead to very high levels of supersaturation. In
 616 such cases, the mixing strategy, especially in fed-batch systems, can have a significant impact on
 617 process attributes such as crystal size distribution and shape.¹¹⁴ Mixing will be discussed further
 618 in the process design sections.

619 Examples of inorganic compounds produced by reactive crystallization are hydroxides
620 such as nickel⁸⁵ and aluminum hydroxide,¹¹⁵ carbonates such as lithium^{98, 106} and calcium
621 carbonate,¹¹⁶ phosphates such as calcium phosphate,¹⁰⁵ and sulfates such as barium sulfate.⁷⁹
622 Table 1 summarizes some of the representative inorganic ionic reactive crystallization studies
623 and precursor materials used in each. These systems have been examined from different
624 viewpoints, including developing kinetic models for crystal nucleation and growth,⁹⁸ prediction
625 and control of particle size distribution,¹⁰⁸ the effect of process parameters such as stirring rate
626 on product size and morphology,^{116, 117} and the effect of different additives on polymorph
627 formation.¹¹⁸

628 Gas-liquid reactive crystallizations result from contacting liquid and gas phases
629 containing reactants whose combination produces a crystalline product. Many of these systems
630 involve synthesis of carbonates through direct injection of CO₂ gas into the crystallizer.^{117, 119, 120}
631 The gaseous CO₂ gets absorbed by the liquid phase to form the carbonate ion:¹²⁰



633 The carbonate ions then react with cations to produce solid species. Several groups have studied
634 the effect of different gas-injection variables such as bubble size and CO₂ mole fraction on the
635 structural and chemical properties of the crystal product. For instance, Matsumoto *et al.*¹¹⁷
636 controlled the polymorphic form of calcium carbonate crystals by manipulating the CO₂-to-N₂
637 ratio of the inlet gas. Varma *et al.*¹²⁰ used the same method with different dispersion agents,
638 including citrate ions and polyacrylic acid, for producing calcium carbonate nanocrystals. These
639 systems can be used both for the recovery of metals from solutions and potential removal of CO₂
640 from industrial gas streams.^{120, 121}

641 A similar approach was proposed and illustrated for production of hydroxides by
642 injecting ammonia gas into the crystallization solution to produce hydroxide ions:¹⁰¹



644 In these gas-liquid-solid cases, the absorption of gaseous reactant into the liquid phase can affect
645 the supersaturation and kinetics of the process. Attempts have been made to model this transport
646 limitation, such as proposing a double-film theory-based mass-transfer model.¹²²⁻¹²⁴

647 Table 1 highlights some of the studies of reactive crystallization in the types of inorganic
648 systems discussed above. The studies include continuous and batch processes with various

649 reactor configurations. In inorganic systems the focus tends to be crystallization-centric, as seen
 650 from the last column in the table. The listed works either give insight into a specific
 651 crystallization phenomenon, such as growth mechanism, size control, or polymorph control, or
 652 are case studies on process designs for recovery of a certain species, such as nickel from
 653 wastewater or CO₂ from flue gas. In the coming sections it will be shown that many desirable
 654 features of reactive crystallization, such as equilibrium modification and intermediate isolation,
 655 are more common in organic systems.

656 *Table 1. A list of representative studies on the reactive crystallization of ionic compounds with the*
 657 *precursors used and the focus of the work. MgDS₂ stands for dodecyl sulfate, FB for fluidized bed, and CSD for*
 658 *crystal size distribution.*

Product	Reference No.	Reactant 1	Reactant 2	Focus
Carbonate				
Li ₂ CO ₃	106	LiOH	CO ₂	Li and CO ₂ recovery
Li ₂ CO ₃	98	Li ₂ SO ₄	Na ₂ CO ₃	Crystallization kinetics
Li ₂ CO ₃	125	LiCl	Na ₂ CO ₃	Growth morphology
Li ₂ CO ₃	121	LiCl	CO ₂	Growth mech./product characterization
Li ₂ CO ₃	126	LiCl	Na ₂ CO ₃	Effect of additives on shape/size
CaCO ₃	116	Ca(OH) ₂	Na ₂ CO ₃	Crystal polymorph control
CaCO ₃	117	CaNO ₃	CO ₂	Crystal polymorph control
CaCO ₃	120	Ca(OH) ₂	CO ₂	Nanocrystal formation
CaCO ₃	127	CaCl ₂	Na ₂ CO ₃	Crystal polymorph control
CaCO ₃	128	CaCl ₂	Na ₂ CO ₃	Crystal polymorph control
CaCO ₃	118	CaCl ₂	NaHCO ₃	Effect of additives on size/morphology
CaCO ₃	129	Ca(OH) ₂	CO ₂	Effect of additives on size/morphology
CaCO ₃	119	Ca(OH) ₂	CO ₂	Crystallization kinetics
MgCO ₃	130	Mg(OH) ₂	CO ₂	Effect of gas flow/stirring on process
NiCO ₃	102	NiSO ₄	Na ₂ CO ₃	Fluidized bed reactor design
NiCO ₃	131	NiSO ₄	Na ₂ CO ₃	Metal recovery and effect of seeding
BaCO ₃	108	BaS	Na ₂ CO ₃	Crystallization kinetics and CSD
BaCO ₃	132	BaCl ₂	Na ₂ CO ₃	Crystallization kinetics
BaCO ₃	133	BaCl ₂	(NH ₄) ₂ CO ₃	Crystallization kinetics and morphology
Hydroxide				
Ni(OH) ₂	85	NiSO ₄	NaOH	Study of airlift-loop reactor
Ni(OH) ₂	134	NiSO ₄	NaOH	Ni recovery from wastewater
Al(OH) ₃	115	NaAl(OH) ₄	NaHCO ₃	Crystallization kinetics and morphology
Mg(OH) ₂	99	Mg(NO ₃) ₂	NaOH	Crystallization kinetics
Mg(OH) ₂	101	MgCl/DS ₂	NH ₃	Impact of metal source on shape
Ca(OH) ₂	135, 136	CaCl ₂	NaOH	Crystallization kinetics
Phosphate				
CaClH ₂ PO ₄	105	CaCl ₂	H ₃ PO ₄	Process design for PO ₄ recovery
CaHPO ₄	137	Ca(NO ₃) ₂	K ₃ PO ₄	Effect of additives on size/shape
MgHPO ₄	138, 139	MgCl ₂	NaH ₂ PO ₄	FB reactor for phosphate removal
MgHPO ₄	140	MgSO ₄	NH ₄ H ₂ PO ₄	Effect of pH on product solid phase
Sulfate				
BaSO ₄	79	BaCl ₂	Na ₂ SO ₄	Process optimization
BaSO ₄	114	BaCl ₂	Na ₂ SO ₄	Effect of mixing on CSD
BaSO ₄	83	BaCl ₂	Na ₂ SO ₄	Effect of ultrasound on nucleation

659
 660 Examples of organic ionic products from reactive crystallizations include calcium¹⁴¹ and
 661 magnesium¹⁴² carboxylates, amines with carboxylic acid anions,⁸⁰ and amphoteric molecules

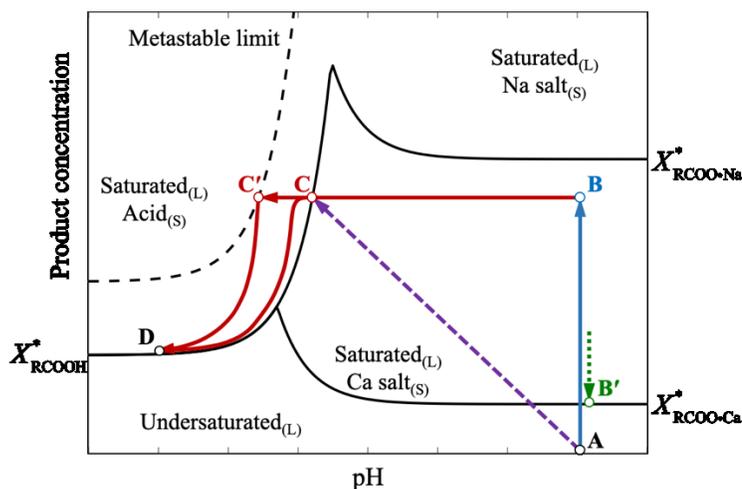
662 such as amino acids.¹⁴³ Together these reactions are termed neutralizations because they remove
663 acids or bases from solution. They are highly pH-dependent as many species only possess the
664 required charge in a specific pH range. Some neutralizations are fermentation-based where the
665 primary reactant is glucose, although many other nutrients are needed by the fermenting
666 microbes. The motivation for each of the cited works on organic ionic reactions is different, and
667 ranges from demonstration of continuous reactive crystallization in a chemical plant¹⁴⁴ to yield
668 enhancement by product sequestration¹⁴⁵ to crystal size optimization.¹⁴⁶ Applications of organic
669 ionic reactive crystallizations include pharmaceutical development, carbon capture, and
670 production of chemicals from renewable platforms.

671 Specially tailored amines are used to remove carboxylates or other anions selectively
672 from solution. Custelcean *et al.*¹⁴⁷ engineered a *m*-benzene-(bis-iminoguanidine) (*m*-BBIG)
673 anion for crystallization of an amino-carbonate salt for direct air capture and sequestration of
674 carbon dioxide. A much different application was described by Sturm *et al.*¹⁴⁸ who used
675 diphenylamine to crystallize the pharmaceutical compound cefdinir from a solution of impurities.
676 In addition to carboxylates, specialty amines can be used in reactively crystallizing other highly
677 soluble anions. Custelcean *et al.*¹⁴⁹ synthesized urea functionalized amines to remove sulfate
678 from a nuclear-waste simulant and examined the competition between accelerated reaction
679 kinetics and increased solubility as the system temperature is increased. In these cases,
680 engineered amines were used to remove specific anions by reactive crystallization,

681 Amines can also be removed from solution through reactive crystallization. However,
682 unlike the cases for carboxylic acids, simple ammonium salts tend to have high solubility,¹⁵⁰
683 which means complex anions are needed to form salts with low solubility. Aakeroy *et al.*¹⁵¹
684 screened 105 potential reactive crystallizations of amines with carboxylates and found 30
685 combinations in which crystal products resulted, although the kinetics of these reactions and the
686 possible role of solvent evaporation are unclear. Quon *et al.*⁸⁰ developed a continuous approach
687 to crystallize the amine drug aliskiren as the hemifumarate salt. Cole *et al.*¹⁵² produced the amine
688 drug prexasertib as the lactate salt. While many amines are crystallizable as carboxylate salts, the
689 applications are mostly limited to specialty and pharmaceutical chemicals produced in low
690 volumes. General guidance for producing solid amines takes advantage of the reduced solubility
691 of the free amine compared to their salts,¹⁵⁰ reacting the amine salt with a hydroxide to
692 crystallize the free amine.

693 Reactive crystallization may be used to control the pH in a fermenter, as in the synthesis
 694 of carboxylic acids such as citric, lactic, gluconic, and itaconic acids. Synthesis of the acids
 695 decreases the pH in the fermenter, and at high concentration can halt the fermentation. Addition
 696 of a neutralizing base such as one of the calcium compounds $\text{Ca}(\text{OH})_2$, CaO , or CaCO_3 stabilizes
 697 pH and causes many carboxylic acids to crystallize as calcium salts,¹⁵³ which may further benefit
 698 the fermentation by sequestering inhibitory products.¹⁵⁴ Magnesium compounds are also used,
 699 but to a lesser extent.¹⁵⁵ Reactive crystallization with a calcium neutralizing agent is not always
 700 the most economical approach to separating carboxylic acids^{153, 156}.

701 Figure 4 illustrates several alternative operating procedures for reactive crystallization in
 702 the production of carboxylic acids. Line AB' represents neutralization with a calcium compound
 703 that produces a saturated solution at B' while Line AB represents neutralization with a soluble
 704 base such as sodium hydroxide. The need for neutralization can be avoided by engineering acid-
 705 tolerant strains of the fermenting microorganism, in which case the operating line of the
 706 fermentations may be represented by Line AC .¹⁵⁷



707
 708 *Figure 4. Concentration of product species in the fermentation broth as a function of broth pH for*
 709 *metastability, saturation, and process operating lines for the reactive crystallization of an organic acid produced by*
 710 *fermentation. Black solid curves are solubilities; the black dashed curve is a metastable limit. Line AB represents*
 711 *fermentation at constant pH with neutralization by NaOH . Line AB' represents fermentation with neutralization by*
 712 *$\text{Ca}(\text{OH})_2$. Line BC represents acidification of solution with mineral acid. Curve CD follows the product solubility as*
 713 *it is crystallized. Line AC follows fermentation using an acid-tolerant microorganism. Point C' represents conditions*
 714 *at which unseeded crystallization is initiated.*

715 Changes in solubility with pH often are exploited to isolate carboxylic acids. For
 716 example, after microbial production by fermentation, cinnamic acid,¹⁵⁸ furan dicarboxylic
 717 acid,¹⁵⁹ and fumaric acid¹⁶⁰ is recovered by lowering the pH of the fermentation broth. Paths of

718 acidification are illustrated in Figure 4, which represent a case in which either seed crystals are
719 added to initiate nucleation (curve BCD) or primary nucleation at the metastable limit is
720 followed (curve BC'D). Acidification after fermentation and continuous neutralization with Ca^{2+}
721 are two competing methods to isolate the product acid from a fermentation broth. The same
722 process is used to isolate amino acids, although amino acids with multiple acid and base moieties
723 have more complex solubility curves than shown for the monoprotic acid in Figure 4.¹⁶¹

724 The inverse of acidification, deprotonation of an amine by a strong base, is also feasible.
725 However, there are fewer studies of these systems as solid amines are typically limited to
726 specialty chemicals and pharmaceuticals. For example, Diab *et al.*¹⁶² optimized the continuous
727 production of nevirapine with a final reactive crystallization step between sodium hydroxide and
728 nevirapine hydrochloride.

729 Acidification of an organic acid by a strong mineral acid is at the boundary between ionic
730 and covalent reactions; the product itself is covalent (e.g. RCOOH), but the reactants are ionic
731 (e.g. $\text{RCOO}^- + \text{H}^+$), and the reaction kinetics are fast ($\sim 10^{10}$ mol/sec), which is why acidification
732 is discussed in this section. The organic acid, after receiving a proton from the dissociated strong
733 acid, crystallizes from solution, as exemplified by the chemical equation



735 Typically, though not always, the neutral form of organic acids (or bases) tends to be less
736 soluble than the negatively (or positively) charged deprotonated (or protonated) form in aqueous
737 solution. Ferreira *et al.*¹⁶³ exploit this feature to produce the beta-lactam antibiotic precursor 6-
738 aminopenicillanic acid (6-APA). 6-APA is produced enzymatically from penicillin G at neutral
739 pH where it exists primarily in a soluble, dissociated state. After complete conversion of
740 penicillin G to 6-APA the solution is acidified to the isoelectric point, pH 3, and the zwitterionic
741 6-APA crystallizes.

742 McDonald *et al.*¹⁷ used the extremely fast kinetics of acid/base reactions to study
743 crystallization kinetics in the reactive crystallization of cephalexin. Cephalexin, which can be
744 produced by a slow enzymatic reactive crystallization,¹⁶⁴ was instead crystallized by reacting
745 HCl with a solution of cephalexin sodium. The reaction is mass-transfer controlled and, with
746 sufficient agitation, can be considered instantaneous. By adding the reactants of the enzymatic
747 system to the cephalexin sodium solution, cephalexin nucleation and growth could be studied in

748 a manner representative of the enzymatic process without needing to deconvolute the enzyme
749 reaction kinetics and crystallization kinetics.

750 Table 2 lists reactive crystallizations involving organic acids and bases and their salts.
751 The diversity of listed compounds is much greater than was the case for inorganic reactive
752 crystallizations. The cited studies are also more wide ranging as these species tend not to be the
753 model compounds used to study phenomena but are industrial products or intermediates with
754 economic motivators for an intensified process.

755 *Table 2. A list of representative studies on the reactive crystallization of acids and bases in which a species*
756 *is crystallized as a salt or is crystallized as an acid (or base) by acidification with a stronger acid (or base).*

Product	Reference No.	Reactant 1	Reactant 2	Focus
Organic Salts				
Aliskiren hemifumarate	80	Aliskiren free base	Fumaric acid	Optimization of purity and yield
Aliskiren hemifumarate	144	Aliskiren free base	Fumaric acid	Control of crystallization in an integrated continuous plant
Amino acid bicarbonates	143	K and Na salts of amino acids	CO ₂	Found enhanced carbon capture using precipitating CO ₂ absorbing solvents
<i>m</i> -BBIG carbonate	147	<i>m</i> -BBIG (see text for abbr.)	CO ₂	Improved ligand for reversible crystallization for CO ₂ direct air capture
Sodium cefuroxime	146, 165	Cefuroxime	Sodium acetate	Control of mixing and particle size distribution, stability of product
Ca citrate	166	Citric acid	CaO	Large amount of gypsum byproduct, from <i>A. niger</i> fermentation
Ca gluconate	167	Glucose	Ca(OH) ₂ , CaCO ₃	Crystallization during fermentation in <i>A. niger</i> inhibits oxygen transfer
Mg 6-hydroxynicotinate	168	Nicotinic acid	MgO	Hydroxylated by <i>A. xylosoxidans</i> . Improved yield
Ca lactate	145	Glucose	Ca(OH) ₂	<i>B. coagulans</i> fermentation. 75% yield increase, 1.7x productivity increase
Mg lactate	142	Glucose	MgO	Reduction in water use by 40% and nutrient use by 43%
Ca malate	169	Ca fumarate		Used overexpressed fumarase, better kinetics with solubilized Ca fumarate
Ca malonate	141	Glucose	Ca(OH) ₂	Fermentation with <i>P. kudriavzevii</i>
1-PEA DPPA salt	170	<i>i</i> PA-DPPA	Acetophenone	Conversion increase from 19% to 91% by shifting equilibrium (see text for abbreviations)
Pyridinium salts	151	2-aminopyridine derivative	Carboxylic acids	Screening for new salts and cocrystals. 105 pyridine/carboxylate pairs tested
Ca succinate	171	Glucose	Ca(OH) ₂	Review of several fermentation technologies
NH ₄ succinate	155	Glucose	Ammonia	Future directions discussed, enhanced regeneration (succinate back to succinic acid) with ammonium salt.
TREN-tris-urea sulfate	149	1,1',1''-(nitriлотris(ethane-2,1-diyl))tris(3-(pyridin-3-yl)urea	Na ₂ SO ₄	Sulfate recovery from nuclear waste by crystallization with engineered ligands, kinetic and equilibrium study
Acids/Bases				
6-amino-penicillanic acid	163	6-APA NH ₄ salt	HCl	Growth and solubility in presence of precursor and byproduct

Amoxicillin trihydrate	172	Amoxicillin hydrochloride	NaOH	Nucleation and growth in the presence of impurities
Ampicillin trihydrate	173	Ampicillin sodium	HCl	Monitoring with online PAT
BACE inhibitor	92	BACE inhibitor hydrochloride	NaOH	Purification, control of particle size, control of fouling
Cefixime trihydrate	174	Cefixime disodium	HCl	Control of crystal morphology in a mixing limited reaction
Cephalexin monohydrate	17	Cephalexin sodium	HCl	Nucleation and growth in the presence of precursor molecules
Cinnamic acid	175	Sodium cinnamate	HCl	Templating agents reduce induction time
Ciprofloxacin	176	Ciprofloxacin sodium	HCl	Continuous process in flow
Fumaric acid	160	Glucose	Na ₂ CO ₃ , H ₂ SO ₄	Optimize of fermenter neutralization to compete with benzene route
Fumaric acid	157	Glucose Starch	KOH	Review with optimization of feedstocks and organism engineering
Furan dicarboxylic acid	159	Hydroxymethyl furancarboxylate	O ₂ , H ₂ SO ₄	Recovery of terephthalic acid alternative from <i>P. putida</i> fermenter
Glutamic acid	79	Monosodium glutamate	HCl	Continuous manufacturing, control of size and productivity
Glutamic acid	177, 178	Monosodium glutamate	H ₂ SO ₄	Modeling, control, and parameter estimation
Glutamic acid	179, 180	Monosodium glutamate	H ₂ SO ₄	Control of reactive crystallization
<i>p</i> -Hydroxybenzoic acid	158	<i>p</i> -Hydroxybenzoate	HCl	Electrochemically induced crystallization by manipulation of local pH
Itaconic acid	181	Glucose	NaOH, HCl	Fermentation by <i>A. terreus</i> . Inhibition overcome by product removal
Malic acid	182	Fumaric acid	H ₂ SO ₄	Fumarase in <i>S. cerevisiae</i> as catalyst. Continuous process with electro-dialysis. Yield up from 78% to 91%
Nevirapine	162	Nevirapine hydrochloride	NaOH	Continuous manufacturing, including reactive crystallization, of API
Riboflavin	183	Glucose	NaOH	Review of riboflavin fermentation processes

757

758 **Crystallization and Covalent Reactions.** Covalent reactions are inherently more complex

759 than ionic reactions; the bonding moieties tend to be bulky with a variety of characteristics

760 (polarity, hydrophobicity, size, etc.) playing a role in the nature and strength of bonds formed.

761 This section addresses that complexity by dividing covalent systems into three broad categories:

762 non-catalytic, catalytic, and biocatalytic reactions. Lastly, reactive crystallization for chiral

763 resolution, an application with enormous industrial importance and unique operating

764 considerations, is discussed.

765 Dividing covalent reactive crystallization according to the use and nature of catalysts

766 assists in comparing the different process conditions each reaction type requires. Uncatalyzed

767 reactive crystallization is accomplished by controlling only the reactant concentrations and

768 crystallizer conditions (e.g. solvent composition, temperature, etc.). However, catalyzed

769 processes can be adjusted with variation of catalyst properties and loading. Reactive
770 crystallization utilizing traditional metal catalysts may have wider operating ranges than
771 uncatalyzed processes as the catalyst helps decouple reaction rates from important crystallization
772 conditions, such as temperature and solvent composition. Biocatalytic processes are constrained
773 by limited biocatalyst stability, but reactive crystallization is often applied to biocatalytic
774 processes as a means of overcoming other catalyst deficiencies, for example poor selectivity.¹⁸⁴
775 Chiral resolution by reactive crystallization may be accomplished with any of the listed catalytic
776 strategies provided the reaction, which racemizes the enantiomers, is much faster than the
777 crystallization and prevents nucleation of the undesired form. Chiral resolution is given its own
778 section because of this unusual (in the context of the other examples) operating requirement and
779 industrial importance. Reactive crystallization enables chiral resolution by diastereomeric
780 resolution,¹⁸⁵ preferential crystallization,¹⁸⁶ enantiomeric enrichment,⁸⁹ and attrition enhanced
781 deracemization.¹⁸⁷

782 *Uncatalyzed covalent reactive crystallization.* The literature has relatively few examples
783 of covalent reactive crystallizations that do not use a catalyst. However, one prominent class
784 involves synthesis of amides by coupling amines with acid chlorides.^{84, 122, 188} The amines and
785 acid chlorides often have higher solubility than the resulting amides, making these products good
786 candidates for reactive crystallization. Liu *et al.*¹²² used a fed-batch system as the rate of reactant
787 addition provided adequate control over the rate of reaction and rate of generation of
788 supersaturation. As is typical of most crystallization processes, decreased supersaturation
789 suppressed nucleation and increased mean crystal size. Covalent reactions typically cannot be
790 considered instantaneous, and their rate is a strong function of temperature. In the system studied
791 by Liu *et al.*,¹²² raising the temperature was shown to have a stronger effect on increasing
792 product solubility compared to the impact on reaction rate; the outcome was an overall lower
793 supersaturation at higher process temperatures and, concomitantly, larger mean crystal size.
794 While this result is important to note, the competition between increasing reaction rate and
795 solubility with temperature is system-specific and results from a single system cannot be used to
796 predict the outcome for other chemistries.

797 As another example of uncatalyzed covalent reactive crystallization, Jiang and Ni¹⁸⁹
798 studied the synthesis of paracetamol from 4-aminophenol and acetic anhydride. The same
799 authors investigated several different types of reactors, including batch and continuous

800 oscillating-baffle reactors and concluded that combining reaction and crystallization improved
801 yield by limiting the extent of further paracetamol reactions.¹⁹⁰ It was also found that the growth
802 mechanism for paracetamol was different in an aqueous solvent from that in a predominately
803 acetic acid solvent. Crystal shape also depended on the solvent composition, in qualitative
804 agreement with the observed change in growth kinetics.

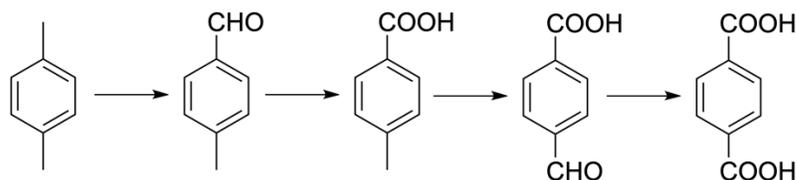
805 Reactive crystallization can provide a framework to understand biological assembly,
806 supporting a means for chemical selection and evolution. For example, the assembly of peptide-
807 like polymers into paracrystalline assemblies is driven by uncatalyzed polycondensation
808 reactions. Thioesters of racemic amino acids undergo polymerization and then beta-sheet
809 assembly, providing a selection for isotactic peptides.¹⁹¹ In a more recent study, peptide aldehyde
810 monomers first polymerize, driving a liquid-liquid phase separation from which beta-sheet
811 crystals nucleate and grow. The resulting peptides are highly monodisperse, supporting a
812 secondary nucleation mechanism for templated polymerization.¹⁹²

813 It is difficult to adjust the rate of reaction independent of the rate of crystal growth in
814 uncatalyzed reactive crystallizations; both are sensitive to temperature, composition, and
815 concentration. While the lack of a catalyst makes the process simpler, it may complicate
816 production of a specified size, shape, and form of crystal if the reaction rate cannot be adequately
817 controlled.

818 *Inorganic catalyzed covalent reactive crystallization.* Combining catalysis with reactive
819 crystallization results in complex but useful processes. For example, hydrogenolysis is a
820 commonly encountered reaction that takes place on metal catalysts. Hansen *et al.*⁹² published a
821 workup of a BACE (beta-site amyloid precursor protein cleaving enzyme) inhibitor, with
822 potential as an anti-Alzheimer's drug, involving hydrogenolysis of a precursor by hydrogen gas
823 in an aqueous environment with a palladium-on-carbon catalyst. The API (active pharmaceutical
824 ingredient) crystallized in the reaction environment, which made reclaiming the solid catalyst
825 difficult. Rather than pursue a solid-solid separation, acid was added to the reaction solvent to
826 increase the API solubility and allow the catalyst to be filtered off. After catalyst recovery the
827 API was deprotonated by reaction with sodium hydroxide and crystallized based on the
828 acidification mechanism described in the ionic reaction section.

829 Reactive crystallization to produce terephthalic acid (TPA), a precursor to the ubiquitous
830 polymer polyethylene terephthalate, by oxidizing *p*-xylene can improve the impurity profile of

831 the resulting product.¹⁹³ Species formed during the oxidation, which is catalyzed by soluble
 832 cobalt/manganese catalysts with bromine promoter, are shown in Figure 5. Incomplete oxidation
 833 leads to the formation of 4-carboxybenzaldehyde (4-CBA), which can incorporate into the
 834 terephthalic acid crystals. Rejection of 4-CBA during crystallization of terephthalic acid is
 835 paramount as 4-CBA terminates polymerization. Wang *et al.*¹⁹³ found that 4-CBA was
 836 incorporated to a greater extent when the TPA growth rate was faster and seed crystals were not
 837 used. They developed a process with slow feed rate and higher temperature to minimize impurity
 838 incorporation, while maintaining the same mean crystal size.



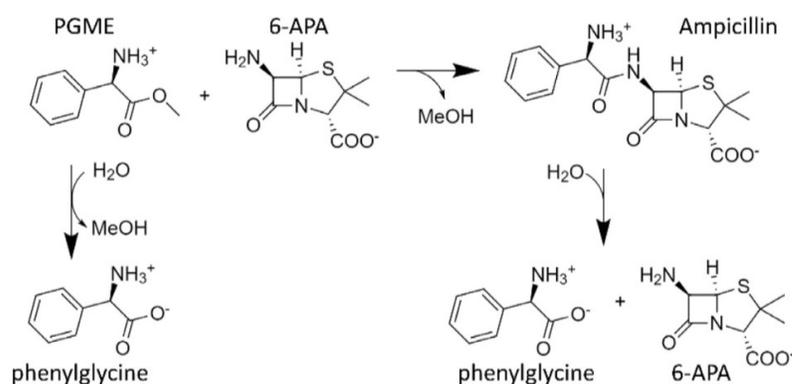
839
 840 *Figure 5. Successive oxidation in the conversion of p-xylene (left) to TPA (right). CBA (second from right)*
 841 *can incorporate into TPA crystals at high concentration, requiring tuning reaction conditions to prevent buildup of*
 842 *CBA while maintaining slow formation of TPA for crystal size control.*

843 *Biocatalytic covalent reactive crystallization.* In this section, biocatalytic reactions are
 844 described that crystallize products formed from specific reactants. There has already been some
 845 discussion on reactive crystallization as it pertains to fermentation, which can be considered a
 846 highly non-selective form of biocatalysis (glucose is converted into a myriad of products). In the
 847 biocatalysis community reactive crystallization is sometimes referred to as *in situ* product
 848 crystallization, ISPC (a subset of *in situ* product removal, ISPR). Hulsewede *et al.*¹⁹⁴ provide a
 849 minireview on ISPC; here ISPC is discussed in the general framework of reactive crystallization.

850 Biocatalytic processes are well-positioned to benefit from reactive crystallization. Many
 851 biocatalysts, such as whole live cells, are poisoned by high concentrations of products, which can
 852 be reduced by reactive crystallization.¹⁹⁵ Other biocatalysts, such as resting or whole dead cells,
 853 may catalyze undesired reactions with the desired product as reactant, but utilization of reactive
 854 crystallization can insulate that product from further reaction.¹⁹⁶ Purified enzymes, while highly
 855 specific and more resistant to poisoning, often catalyze reactions with equilibrium coefficients on
 856 the order of unity leading to low yields; reactive crystallization can shift equilibrium towards
 857 products.¹⁹⁷

858 Synthesis of beta-lactam antibiotics is a well-studied example of a biocatalytic reactive
 859 crystallization. Ferreira *et al.*¹⁹⁸ have demonstrated good recyclability of an immobilized

860 penicillin G acylase (PGA) for production of ampicillin in saturating conditions. The three main
 861 reactions catalyzed by PGA are shown in Figure 6 for ampicillin; they are synthesis (desired,
 862 top), reactant hydrolysis (undesired, left), and product hydrolysis (undesired, right). Using PGA
 863 entrapped in agarose gel particles afforded only slight mass transfer resistance in the catalyst
 864 particle.¹⁹⁸ After some time, the solution saturated and ampicillin crystallized because the
 865 reactants, phenylglycine methyl ester (PGME) and 6-APA, are both more soluble than ampicillin
 866 on a molar basis. Once again, the crystallization made reclaiming the catalyst difficult and so the
 867 product was dissolved after filtration, leaving behind the immobilized enzyme for recycling.
 868 Another study used a soluble version of the same enzyme to increase the selectivity towards
 869 ampicillin by >50% by sequestering the product from enzymatic hydrolysis by crystallization.⁴

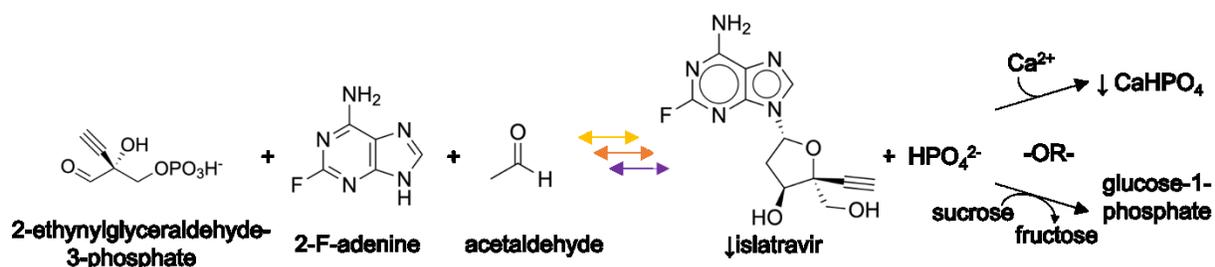


870
 871 *Figure 6. PGA-catalyzed synthesis of ampicillin (desired, top), hydrolysis of phenylglycine methyl ester,*
 872 *PGME (undesired, left), and hydrolysis of ampicillin (undesired, right).*

873 The value of the biocatalyst (relative to the value of the product) often dictates whether
 874 the catalyst is immobilized on a solid, which enables catalyst recovery and reuse, or is soluble,
 875 enabling product recovery by filtration. In the case of ampicillin, the product is less valuable than
 876 the enzyme, which must be recycled repeatedly for economic sustainability; since solid-solid
 877 separations are difficult, the product crystals may be re-dissolved to enable recovery of the
 878 enzyme in solid form.¹⁹⁸ With the simplified recovery of a solid biocatalyst comes the challenge
 879 of catalyst engineering: choosing a particle size and material to avoid mass-transfer limitations
 880 and efficiently utilize the active material, for example PGA in Figure 6.¹⁸⁴ When catalyst
 881 recovery is a nonissue, and trace catalyst does not impact downstream quality, e.g. heavy metal
 882 toxicity, a reactive crystallization with a dissolved catalyst may be preferable.

883 Recently, a biocatalytic process with reactive crystallization to produce the HIV drug
 884 islatravir has been described.¹⁹⁹ The reactive crystallization involves four dissolved enzymes.

885 The three final reactions to islatravir are reversible, so crystallization helps shift the equilibrium
 886 towards the product, and the fourth enzyme catalyzes a reaction to consume a byproduct and
 887 further improve the yield of islatravir (see Figure 7). The high value of the product favors its
 888 recovery by filtration and use of fresh enzyme for each batch. Upstream of the reactions shown
 889 in Figure 7 product recovery by filtration is not favorable, and five immobilized enzymes are
 890 used. The starting solution for the reactive crystallization is the filtrate from the reactions
 891 catalyzed with immobilized enzyme. The relative harmlessness of enzymes (compared to heavy
 892 metals) and the value of the reaction products favor reactive crystallization processes.
 893 Furthermore, the strong specificity of enzymes enables coupling many reactions to transform
 894 soluble reactants to the desired insoluble product. A more recent study of the same system used
 895 crystallization of the byproduct (previously consumed by the fourth enzyme) as a calcium salt to
 896 drive the reaction further; the improvement in reaction yield (82% versus 76%) outweighed the
 897 difficulty of recrystallization.²⁰⁰



898
 899 *Figure 7. Enzymatic synthesis of islatravir by three enzymes in a single vessel from an alkyne precursor*
 900 *(also produced enzymatically). Islatravir crystallization helps drive the reaction to the right; consumption of the*
 901 *phosphate byproduct by (top) reaction with calcium and crystallization of calcium phosphate or (bottom) enzymatic*
 902 *reaction with sucrose pulls the reaction further towards the product. Adapted from Huffman et al.¹⁹⁹*

903 Many chemistries that do not seem plausible with biocatalytic processes could be
 904 implemented with biocatalytic reactive crystallization. For example, equilibrium favors removal
 905 of CO₂ from carboxylic acids, not carboxylation by addition of CO₂. However, Ren *et al.*²⁰¹
 906 overcame the unfavorable reaction equilibrium when they carboxylated phenols with a
 907 decarboxylase enzyme (which, as the name suggests, typically catalyzes removal of CO₂) by
 908 crystallizing the products as quaternary ammonium salts, improving the yield from 40% to 97%.

909 Table 3 lists several examples of the three types of covalent reactive crystallizations
 910 discussed, non-catalytic, catalytic, and biocatalytic. The product, reactants, and focus of the
 911 study are listed for each entry in Table 3. The focuses are varied, reflecting the wide-ranging
 912 applications of covalent reactive crystallization.

913
914

Table 3. A list of representative studies on covalent reactive crystallization processes, divided based on catalyst usage and type.

Product	Reference No.	Reactant 1	Reactant 2	Focus
Uncatalyzed				
Paracetamol	189	4-aminophenol	Acetic anhydride	Impurity content, crystal shape, growth and nucleation kinetics
Paracetamol	190	4-aminophenol	Acetic anhydride	Continuous oscillating baffled reactor
2,4,6-triamino-1,3,5-trinitrobenzene	122	2,4,6-trichloro-1,3,5-trinitrobenzene	Ammonia	Gas, liquid, solid phase. Effect of feed rate and temperature on particle size in bubble column reactor
Dithiocarbamate (DTC)	88	DTC-precursor	Formaldehyde	Narrow CSD, avoid oiling out and spherulites, optimize productivity
Amides	84	Acid chlorides	Amines	Plug flow reactor crystallizer, examined fouling
Inorganic catalyst				
Terephthalic acid (TPA)	193	<i>p</i> -xylene	Oxygen	Intermediate impurity incorporation, Co/Mn catalyst, Br promoter
TPA	202	<i>p</i> -xylene	Oxygen	Evaporative cooling of exothermic reaction to avoid fouling
TPA	203	<i>p</i> -xylene	Oxygen	Two reactive crystallizers in series to eliminate intermediate impurity
BACE inhibitor	92	Isoxazolidine derivative	Hydrogen	Difficulty separating Pd/C catalyst from solid product, redissolved
Relebactam	204	Carboxybenzyl relebactam	Hydrogen, silylating agent	Pd/C, DABCO then HOAc. <i>In situ</i> protect/deprotect with crystallization
Akt kinase inhibitor	91	Amine precursor	Methyl phenylacetate	Cs ₂ CO ₃ catalyst, impurity rejection
		Boronate precursor	Chloropyridine derivative	Pd catalyzed Suzuki coupling, enhance yield and selectivity
Hedgehog pathway inhibitor	93	Carboxybenzyl protected API	Hydrogen	Solids formed on Pd/C catalyst, form HCl salt instead
Biocatalytic				
Ampicillin	4	6-amino penicillanic acid (6-APA)	Phenylglycine methyl ester (PGME)	Improved enzymatic yield with crystallization
Ampicillin	173	6-APA	PGME	Reactive crystallization of product and byproduct, phenylglycine
Ampicillin	198	6-APA	PGME	Taylor-Couette flow reactor to suspend slurry with low shear
Ampicillin, Amoxicillin, Cephalexin	205	6-APA, 7-amino-desacetoxy-cephalosporanic acid (7-ADCA)	Phenylglycine amide, 4-hydroxy-phenylglycine amide	Used supersaturated reactants for three different pen G acylase catalyzed reactions
Ampicillin	206	6-APA	Phenylglycine amide	Fed batch, solid reactants dissolving, solids purity versus conversion
Amoxicillin, Cephalexin	5, 113	6-APA, 7-ADCA	PGME	Continuous reactive crystallization modeling, size, purity, yield
Cephalexin	207	6-APA	Phenylglycine nitrile	Complex product with 1,5-dihydroxynaphthalene (reduced sol.)
Islatravir	199	2-Ethynyl-glyceraldehyde-3-phosphate	2-F-adenine	Three reactions in series, crystallization pulls equilibrium right
Methyl trans-3-(4-methoxy-phenyl) glycidate	208	Racemate		Lipase immobilized on membrane to facilitate enzyme recovery from crystals. Deracemization
Levodione	154, 195	4-oxoisophorone		Reduction by live <i>S. cerevisiae</i> , crystallization reduce over-reduction

Nicotinamide	²⁰⁹	3-cyano pyridine	water	Avoid overhydration to nicotinic acid by crystallization
Methionine, phenylalanine	²¹⁰	Racemate	Ammonia borane, oxygen	Deracemization
Alanine	¹⁹⁶	Aspartic acid		Deracemization, whole cell (dead) <i>Pseudomonas dacunhae</i> catalyst
2,3- and 2,6-dihydroxybenzoate	²⁰¹	Resorcinol	KHCO ₃	Use of quaternary ammonium salts to increase yield from 40% to 97%
Allo-threonine	²¹¹	Catechol		Isomerase reaction, solid reactant and product, constant liquid composition
Z-aspartame	²¹²	threonine		
		Carboxybenzyl aspartate	Phenylalanine methyl ester	Two enzymes tested, reaction kinetics
L-Homo-phenylalanine	²¹³	2-oxo-4-phenylbutyric acid	L-aspartate	Fed batch to overcome substrate inhibition
L-phenylglycine	²¹⁴	Phenylglyoxylate	L-glutamate	Thermophilic enzyme, crystallization shifted equilibrium to products
Peptides	²¹⁵⁻²¹⁹	Amino acid with protected amine	Unprotected amino acid	Improving yield, conversion

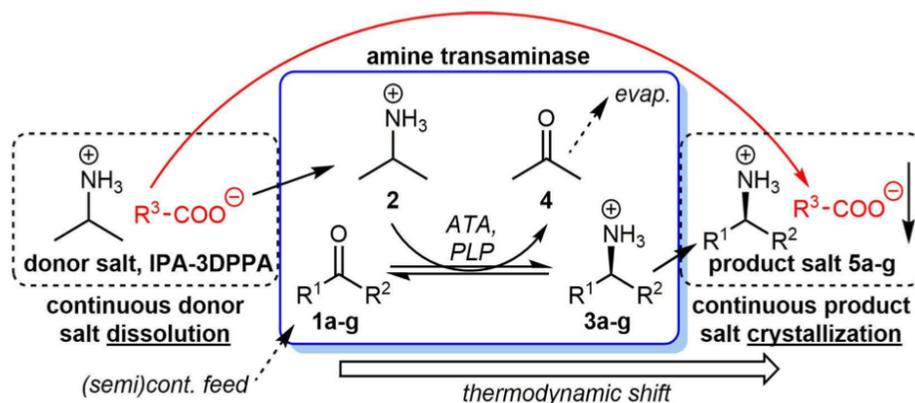
915

916 In the carboxylation example by Ren *et al.*²⁰¹ the product formed is an organic salt, but it
 917 is discussed in the covalent section of this review because the rate-limiting step is the formation
 918 of covalent bonds (carboxylation). The kinetics of this process are more representative of those
 919 found for other covalent and biocatalytic reactive crystallizations. The same behavior is observed
 920 in fermentation with continuous neutralization by calcium hydroxide; the rate-limiting step is not
 921 the reaction between carboxylate and neutralizing base, but rather production of the acid by the
 922 microorganism. The product, a dissociated acid, is ionic, but the rate-limiting reaction that
 923 produced the acid forms covalent bonds. Neutralization in batch at the end of the fermentation
 924 may also be practiced, in which case the ionic reaction between Ca²⁺ and the carboxylate is rate-
 925 limiting. The use of a second species, such as Ca²⁺ for carboxylates, to form a less-soluble
 926 complex with the product is a common application of reactive crystallization.

927 Enzymatic peptide synthesis is thermodynamically unfavorable in aqueous solutions, but
 928 reactive crystallization enables even thermodynamically-controlled reactions to achieve high
 929 yields, especially when using a second species to promote crystallization. For example, the
 930 thermolysin-catalyzed synthesis of the artificial sweetener aspartame (L-asp-L-phe-OMe) is used
 931 in a 10,000 ton/year-scale process with 96% yield in the enzymatic step.^{220, 221} Carboxybenzyl L-
 932 aspartate (Z-asp) is coupled with equimolar L-phenylalanine methyl ester (L-phe-OMe) at
 933 neutral pH in purely aqueous solution. The anion generated at neutral pH values, Z-aspartame
 934 (Z-asp-L-phe-OMe), forms an insoluble salt with cationic D-phe-OMe, Z-asp-L-phe-OMe·D-
 935 phe-OMe. Racemic DL-phe-OMe is employed in 2:1 molar ratio with Z-aspartate such that the
 936 L-enantiomer is consumed in the reaction and the D-enantiomer promotes crystallization.

937 Eichhorn *et al.*²¹⁷ demonstrated that reactive crystallization of thermolysin-catalyzed dipeptide
 938 couplings leads to high yields with a wide range of amino acids and their derivatives. In a high-
 939 solids medium (only about 10% aqueous solution), at the kilogram scale, mixing limits the
 940 reaction rate. In theoretical work on peptide synthesis, Erbeldinger *et al.*²¹⁶ and Ulijn *et al.*²¹⁵
 941 showed that high yield is the consequence of reactive crystallization and that above a threshold
 942 of product solubility, yield switches from low values to values of almost 100%.

943 The work of Hulsewede *et al.*¹⁷⁰ described a nearly 5-fold increase in the yield of 1-
 944 phenylethylamine (1-PEA), synthesized by a transaminase enzyme, by reactively crystallizing
 945 the 1-PEA. Starting with acetophenone and isopropylammonium-3,3-diphenylpropionate (*i*PA-
 946 DPPA), the enzyme transfers the amine group from *i*PA to acetophenone and the resulting 1-
 947 PEA crystallized as a salt with DPPA. The crystal product was a salt, but the rate-limiting step is
 948 the enzyme-catalyzed covalent reaction. The DPPA was present in stoichiometric quantity
 949 throughout the reaction since the *i*PA was fed as the DPPA salt. It was found that low reaction
 950 equilibrium (19%) could be overcome by coupling to the favorable crystallization of 1-PEA-
 951 DPPA and 92% conversion could be reached. The general process, illustrated in Figure 8, is also
 952 applicable to similar chemistries.²²²



953
 954 *Figure 8. Reaction scheme of the amine transaminase (ATA, cofactor pyridoxal phosphate, PLP) catalyzed*
 955 *stereoselective amination of a ketone with iPA donor amine. The amine product forms a salt with the anion from the*
 956 *amine donor. In the main text, $R_1 = C_6H_5$, $R_2 = CH_3$, and $R_3 = DPPA$. Reprinted with permission from Hulsewede *et*
 957 *al.*¹⁷⁰ copyright 2019, John Wiley and Sons.*

958 Depending on the nature of the interactions between the product and the second species,
 959 the resulting crystals may be called salts (coulombic interactions) or cocrystals.²²³⁻²²⁵ In the
 960 previous example, 1-PEA is crystallized as a salt of DPPA, but numerous examples can be found
 961 where the final solid is a cocrystal. As an illustration, the yield of cephalosporin antibiotics can

962 be increased by reactive crystallization with an aromatic species to isolate the antibiotic product,
963 which is an intermediate in an enzymatic cascade. The process has been demonstrated for
964 cefaclor (yield increased from 57% to 80%),²²⁶ cephalexin (42% to 67%),²²⁷ and cephadrine
965 (yield not evaluated).²²⁸ Recent published work on cocrystallization has focused on discovery
966 and/or prediction of cocrystal-forming systems,^{229, 230} which could make reactive crystallization
967 practical for a wider range of products if co-formers* promoting crystallization can be identified
968 for more products. Other applications of cocrystallization include: improved solids handling,²³¹
969 solubility,²³² stability,²³³ and pharmaceutical activity,²³⁴ Karimi-Jafari *et al.* reviewed the entire
970 topic.²³⁵

971 Carbamazepine has been a favorite model compound for cocrystal research and is the
972 only compound for which cocrystallization kinetics have been published. Gagniere *et al.*²³⁶
973 qualitatively examined the rates of cocrystallization in the carbamazepine-nicotinamide system
974 while Rodriguez-Hornedo *et al.*²³⁷ used Raman spectroscopy to monitor the nucleation and
975 growth of carbamazepine-nicotinamide from a slurry of the individual solids. Kudo and
976 Takiyama²³⁸ have worked out much of the thermodynamics of reactive cocrystallization in the
977 carbamazepine-saccharin system. Each of these studies highlights the difficulties designing
978 reactive crystallizations with multiple small molecules, namely complex phase diagrams with at
979 least three solids (more with chiral compounds and if cocrystals with several stoichiometries
980 exist) and uncertain driving forces for complexation.

981 *Chiral Resolution.* Enantiomers are prevalent in pharmaceutically active compounds,
982 with one enantiomer typically being responsible for clinical activity and, in some cases, the
983 mirror compound having deleterious effects. Both left and right enantiomers have the same
984 solubility, vapor pressure, partition coefficients, etc. (in achiral solvents), making their separation
985 by traditional methods very difficult. Many non-biological reactions are agnostic of chirality, the
986 products are racemic mixtures that, by definition, contain equal amounts of the two enantiomers.
987 Producing a compound with a single chirality often involves a deracemization step. Provided a
988 racemizing reaction (a reversible reaction interconverting the two enantiomers) occurs with

* The FDA defines a co-former (or cofomer) as one of the two different molecules in the same crystal lattice, forming a co-crystal. More information can be found at <https://www.fda.gov/media/81824/download>

989 appreciable speed, the left- and right-hand enantiomers (*S* and *R*) will exist in a 1:1 ratio in
990 solution, irrespective of removal of one of the enantiomers from solution by crystallization.

991 Conglomerate-forming systems are ones in which each of the two enantiomers form
992 enantiomerically pure crystals that may be produced as a physical mixture if crystallized
993 together. Racemate-forming systems produce crystals in a single lattice structure with a 1:1 ratio
994 of the two enantiomers. Conglomerate-forming systems are more amenable to resolution by
995 reactive crystallization, and are estimated to comprise 5-20% of all enantiomeric systems with
996 racemates making up the remainder.^{239, 240} Reviews of several techniques for enhancing
997 enantiomeric purity, some involving reactive crystallization, are provided by Lorenz and Seidel-
998 Morgenstern,²⁴¹ Palmans,²⁴² and Brands and Davies.¹⁸⁵ In the following discussion, special
999 emphasis is given to a class of covalent reactive crystallizations used to recover enantiomerically
1000 pure products.

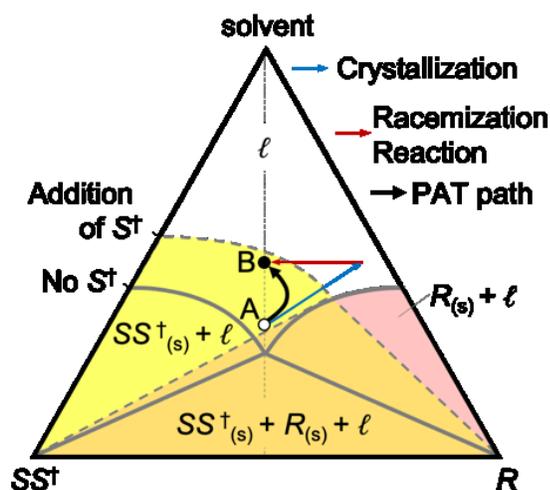
1001 Crystallization can result in deracemization in four ways: (1) by formation of a
1002 diastereomeric salt with a chiral resolving agent, (2) by preferential crystallization, (3) by
1003 selectively subjecting the undesired enantiomer to racemization with an asymmetric reaction,
1004 thereby enriching the solution in the preferred enantiomer and facilitating its crystallization, and
1005 (4) by attrition-enhanced deracemization of conglomerate-forming enantiomers.

1006 Diastereomeric resolution, or crystallization with a resolving agent, sometimes referred to
1007 as “classical resolution,” takes advantage of differences in interactions between two chiral
1008 molecules. In this process, two enantiomers of a single species are reacted with a single
1009 enantiomer of another compound (resolving agent) to form two diastereomers that have different
1010 properties, including solubilities. The two diastereomers may then be separated by crystallizing
1011 the less soluble of the two. The desired free enantiomer is then recovered by reversing the
1012 reaction that formed the diastereomer.

1013 An illustration of diastereomeric resolution is the production of the unnatural amino acid
1014 *R*-(-)-2-phenylglycine, *R*-PG, mentioned previously in reference to certain beta-lactam
1015 antibiotics. In the commercial process, a racemic mixture of phenylglycine (*RS*-PG) is reacted
1016 with (1*S*)-(+)-camphor-10-sulfonic acid, *S*-CS, to produce two diastereomeric salts, *RS*-PG-CS
1017 and *SS*-PG-CS. The former has a lower aqueous solubility (5.75 g/100 g at 25 °C) than the latter
1018 (>150 g/100g, 25 °C), which facilitates separation.²⁴³ Racemization of *RS*-PG in the presence of

1019 one equivalent of *S*-CS and half an equivalent of hydrochloric acid (to keep zwitterionic PG from
 1020 crystallizing) leads to greater than 90% yield of *R*-PG from *RS*-PG.

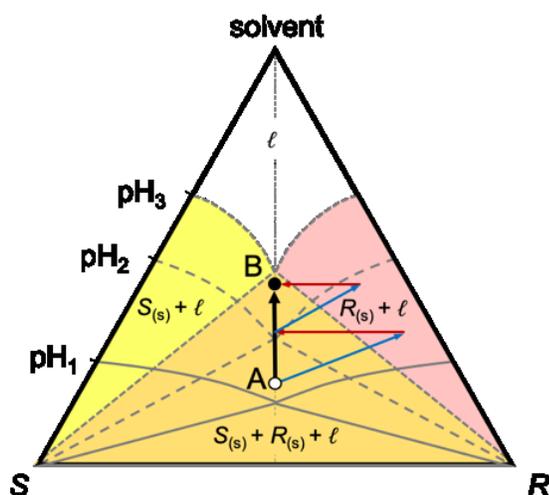
1021 The simultaneous use of multiple resolving agents has been shown to enhance resolution,
 1022 likely by inhibiting nucleation of the undesired diastereomeric salt.²⁴⁴ Brands and Davies¹⁸⁵ list
 1023 many systems for which diastereomeric salt resolution has proven successful. The utility of this
 1024 method is demonstrated by its use in the production of large quantities of (*S*)-naproxen, (*R*)-
 1025 phenylglycine, and (*R*)-4-hydroxyphenylglycine.²⁴¹ Diastereomeric resolution can be used to
 1026 resolve individual enantiomers of conglomerate-forming and racemate-forming compounds.
 1027 Figure 9 represents the resolution of the *S* enantiomer of a conglomerate forming compound by
 1028 addition of resolving agent S^\dagger . The apex represents pure solvent, while the lower left vertex is
 1029 pure *S* or SS^\dagger and the lower right vertex represents pure *R*. Using process analytical technology
 1030 (PAT, discussed further in the process design section) one would observe the solution
 1031 composition following the solid black curve from Point A to Point B, with movement up and to
 1032 the right due to crystallization and movement left due to racemization.



1033
 1034 *Figure 9. Isothermal ternary phase diagram for diastereomeric resolution. The phase equilibrium before*
 1035 *addition of the resolving agent is symmetrical, shown by bold gray curves, while after addition the resulting*
 1036 *diastereomer SS^\dagger phase equilibrium is asymmetric, shown by dashed gray curves, enabling crystallization of only*
 1037 *the desired enantiomer. During the process, the solution moves from Point A (undersaturated) to B upon addition of*
 1038 *S^\dagger with concurrent racemization in solution.*

1039 Preferential crystallization utilizes the addition of seed crystals to solutions of
 1040 enantiomers in the metastable zone to initiate nucleation and subsequent growth of a single
 1041 enantiomer from a racemic solution. The methodology is useful for conglomerate-forming
 1042 systems. Seed crystals of the desired enantiomer are added, and the supersaturation is held within

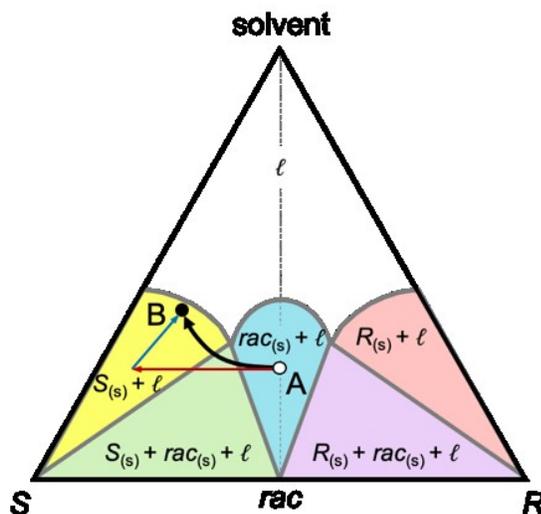
1043 the metastable zone. The seed crystals grow and breed new crystals of the desired chirality while
 1044 the undesired enantiomer remains in solution; primary nucleation must not occur as it would
 1045 initiate crystallization of the undesired enantiomer. Simultaneously subjecting the solution to a
 1046 racemization reaction enhances the yield of the seeded species. Yoshioka²⁴⁵ summarized several
 1047 examples of preferential crystallization of amino acids, both proteogenic and unnatural, with
 1048 racemization by catalytic salicylaldehyde. Petrussevska-Seeback *et al.* give an example of
 1049 combining preferential crystallization with enzymatic racemization.²⁴⁶ Supersaturation may be
 1050 generated by cooling, pH adjustment or other means. Figure 10 shows the preferential
 1051 crystallization of *S* by acidification reactive crystallization, where $\text{pH}_1 > \text{pH}_2 > \text{pH}_3$ and the
 1052 solubility decreases with decreasing pH value.



1053
 1054 *Figure 10. Ternary phase diagram for preferential crystallization of S by addition of S seed crystals.*
 1055 *Supersaturation is generated by decreasing the pH from pH_1 to pH_3 while a racemization reaction converts excess R*
 1056 *in solution to restore a 1:1 ratio of R:S in solution. Again, the bold black curve from Point A to Point B represents*
 1057 *the solution composition observed by PAT, while the blue arrows represent movement due to crystallization and the*
 1058 *red arrows movement due to racemization.*

1059 Enantiomeric enrichment followed by crystallization is especially valuable if an
 1060 enantiomerically pure product is to be recovered from a racemate-forming system. Enrichment in
 1061 the present context means that the relative proportion of the desired enantiomer in solution is
 1062 increased to an extent that crystallization of enriched pure enantiomer is feasible. Enrichment of
 1063 a specific enantiomer can be accomplished in several ways. For example, Johnson *et al.*²⁴⁷ used
 1064 an asymmetric palladium catalyst in route to an API, producing the desired enantiomer at a
 1065 solution enantiomeric excess of 95%; crystallization was used to upgrade the enantiomeric
 1066 excess of the solid to >99%. Encarnacion-Gomez *et al.*²¹⁰ used a chemo-enzymatic

1067 stereoinversion reaction system to enrich the concentration of a desired enantiomer to
 1068 appropriate concentrations for crystallization of the pure enantiomer. They demonstrated the
 1069 process using racemic mixtures of phenylalanine and of methionine and recovered crystals of the
 1070 desired pure enantiomer from each system. Harriehausen *et al.*²⁴⁸ suggested several process
 1071 configurations that combined enantioselective chromatography with enzymatic racemization to
 1072 recover pure enantiomer with nearly complete extinction of the undesired enantiomer. Figure 11
 1073 shows enantiomeric enrichment in a racemate forming system by reacting *R* to *S* followed by
 1074 crystallization in a racemate-forming system. The middle cone-shaped region identifies
 1075 conditions corresponding to equilibrium between crystals of the racemate and the solution. The
 1076 objective of enantiomeric enrichment is to move from the central region to the yellow region,
 1077 thereby facilitating crystallization of the desired enantiomer.



1078
 1079 *Figure 11. The ternary phase diagram for enantiomeric enrichment in a racemate-forming system. The*
 1080 *enantiomeric enriching reaction occurs under supersaturated conditions, but high conversion ensures only the*
 1081 *desired enantiomer is crystallized. Again, the bold black curve from Point A to Point B represents the solution*
 1082 *composition observed by PAT, while the blue arrow represents movement due to crystallization and the red arrow*
 1083 *movement due to an enantioselective isomerization reaction.*

1084 Attrition-enhanced deracemization, sometimes referred to as “Viedma ripening,” was
 1085 observed originally by Viedma²⁴⁹ and explored further by Viedma²⁵⁰ and Blackmond.^{251, 252} The
 1086 original observations were on aqueous solutions of sodium chlorate, a species that is achiral in
 1087 solution but which, on crystallization, produces chiral crystals. Experiments included seeding
 1088 with mixtures of *R* and *S* chiral crystals that had been subjected to attrition before being added to
 1089 the system and which were subject to continuous attrition by the presence of glass beads that
 1090 were added to the stirred system. After stirring for a sufficiently long period, the resulting

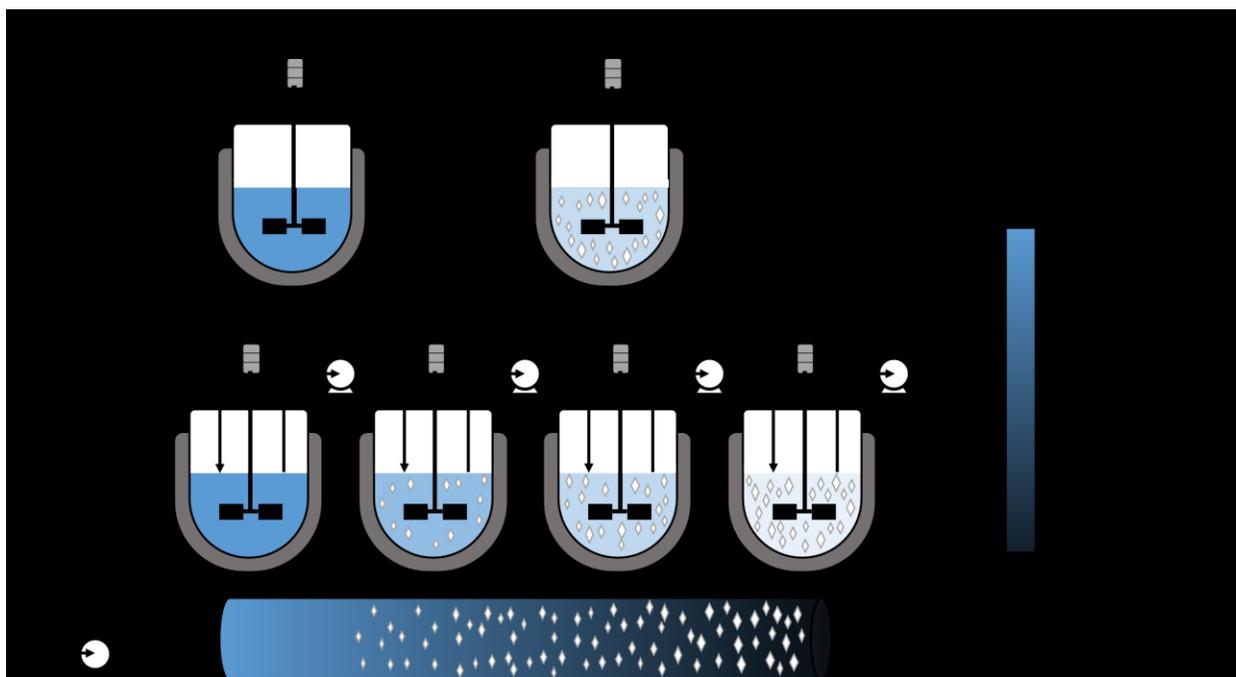
1091 crystals were found to be enantiomerically pure *R* or *S*. Later work found similar behavior for
1092 conglomerate-forming enantiomers that underwent rapid racemization reactions and, therefore,
1093 maintained the ratio of enantiomers in solution near 1:1. Examples of such systems include: an
1094 amino acid derivative N-(2-methylbenzylidene)-phenylglycine amide;²⁵³ aspartic acid, one of
1095 two conglomerate forming proteogenic amino acids;²⁵⁰ and an imine that is the key component in
1096 clopidogrel.²⁵⁴ Spix *et al.*²⁵⁵ converted the racemate-forming amino acids alanine and
1097 phenylalanine to conglomerate-forming salts alanine 4-chlorobenzene sulfonic acid and
1098 phenylalanine 2,5-xylenesulfonic acid. After deracemization of the salts, the free amino acids
1099 were recovered by neutralizing the salts with alkali.

1100 **Reactive Crystallization Process Design**

1101 Development of reactive crystallization processes for use at the industrial scale is a
1102 challenging multi-objective problem. The generation of a given product by reactive
1103 crystallization involves simultaneous fundamental thermodynamic and kinetic phenomena,
1104 including reaction, mass transfer, and crystal nucleation and growth, all coupled with the
1105 engineering aspects of reactor design, configuration, control, and product recovery. While each
1106 of these has been well-studied in the literature, decisions for process design, optimization, and
1107 control are often unique to the system of interest.

1108 Reactive crystallization processes generate supersaturation by synthesizing a product
1109 through a reaction, concomitantly increasing the concentration of the product and leading to
1110 crystallization. The rates of the reaction and crystallization steps guide strategies for reactor
1111 design and control. In cases where fixed operating conditions favor both reaction and
1112 crystallization, reactive crystallization can be performed in a single vessel. For example, many of
1113 the ionic reactions mentioned earlier produce a sparingly soluble compound in an instantaneous
1114 reaction and fall into this category. Other cases may require the steps to be temporally or
1115 spatially separated, several configurations of which are illustrated in Figure 12. Temporally
1116 separated processes include well-mixed batch or semi-batch designs in which synthesis reactions
1117 occur, followed by a shift in temperature or pH to promote subsequent crystallization of the
1118 product. Processes that are spatially separated utilize multiple vessels or different segments of a
1119 vessel—first performing the reaction to generate supersaturation and then feeding the mixture
1120 into a second vessel for crystallization. Process intensification in the form of combining both
1121 reaction and crystallization steps into a single vessel is likely to lead to savings in capital and

1122 operating costs as the technology matures,^{256, 257} but like many aspects of design problems, the
 1123 potential benefit is system-dependent.



1124
 1125 *Figure 12. (a) Temporal separation of reaction and crystallization favoring conditions in a well-mixed*
 1126 *batch reactor; (b) Spatial separation of reaction and crystallization favoring conditions in continuous well-mixed*
 1127 *reactors (above) and tubular reactors (below).*

1128 Key factors in process design for reactive crystallization include the presence of multiple
 1129 components (sometimes with more than one crystallizing), effects of mixing on crystallization
 1130 kinetics, the necessity of maintaining mutually beneficial operating conditions for reaction and
 1131 crystallization, and the need for producing crystals that can be readily separated from a reaction
 1132 slurry. In instances where a heterogeneous catalyst is used to facilitate a desired reaction,
 1133 separating the catalyst from product crystals represents an additional challenge. As crystal shape
 1134 and size distributions are strongly influenced by supersaturation, process control is also a unique
 1135 challenge due to the generation of supersaturation from a reaction rather than by temperature
 1136 manipulations, evaporation, or anti-solvent addition. In the following discussion, challenges
 1137 unique to reactive crystallization process design and control that focus on the aforementioned
 1138 issues are discussed in more detail.

1139 **Reactor Design.** Design and implementation of reactive crystallization systems rely
 1140 heavily on reaction and crystallization kinetics. A strong distinction between the operation of a
 1141 reactive crystallizer and a traditional crystallizer is that reactive crystallization conditions must

1142 satisfy *both* the reaction *and* the crystallization. For example, an enzymatic reaction usually
1143 requires benign temperatures (20 to 37 °C), aqueous conditions, and near-neutral pH values. If
1144 these conditions promote crystallization of the desired product, then reaction and crystallization
1145 may be conducted in the same vessel. If the conditions for reaction do not permit crystallization
1146 of the product, then using multiple vessels may need to be investigated. Alternatively, the
1147 conditions within the vessel may be varied over the time course of the reactive crystallization or
1148 across the volume of the reactor (specifically for tubular reactors). For example, Jiang *et al.*¹⁹⁰
1149 varied the temperature across a tubular reactor to allow for enhanced reaction kinetics in the
1150 upstream section and improved crystallization kinetics in the downstream section.

1151 Configurations of vessels in which reactive crystallizations are conducted usually are
1152 similar to those of non-reactive crystallizers. The perfectly mixed continuous crystallizer, which
1153 is often referred to as a mixed-suspension mixed-product removal (MSMPR) crystallizer,^{*} is an
1154 idealized version of a continuous stirred-tank crystallizer. A similar vessel may serve as a batch
1155 crystallizer with feed added at time zero and product removed at a designated endpoint. In a
1156 semi-batch (or fed-batch) unit, one or more feed streams is added during the course of a run and
1157 product removed at the designated endpoint. More details on these generic configurations, which
1158 often have to do with mixing, are available in general references on industrial crystallization.^{36,}
1159 ²⁵⁸

1160 Most applications of reactive crystallization described in the literature focus on batch or
1161 semi-batch systems. While these are often relatively simple to design and operate, continuous
1162 reactive crystallization processes offer several benefits. Advantages of continuous systems have
1163 been outlined specifically for pharmaceuticals manufacturing by Lee *et al.*²⁵⁹ and Acevedo *et*
1164 *al.*²⁶⁰ Some of these benefits include higher process capacity and productivity, more efficient use
1165 of raw materials and energy, production of fewer intermediate compounds, and more robust
1166 control. The design and use of various arrangements of reactive crystallization equipment for
1167 batch, semi-batch and continuous operation are covered in the following discussion.

* The MSMPR crystallizer is a useful model for continuous stirred-tank crystallizers. The assumptions of perfect mixing and uniformity of residence time distributions of solvent and crystals of all sizes are approximations often approached in actual systems.

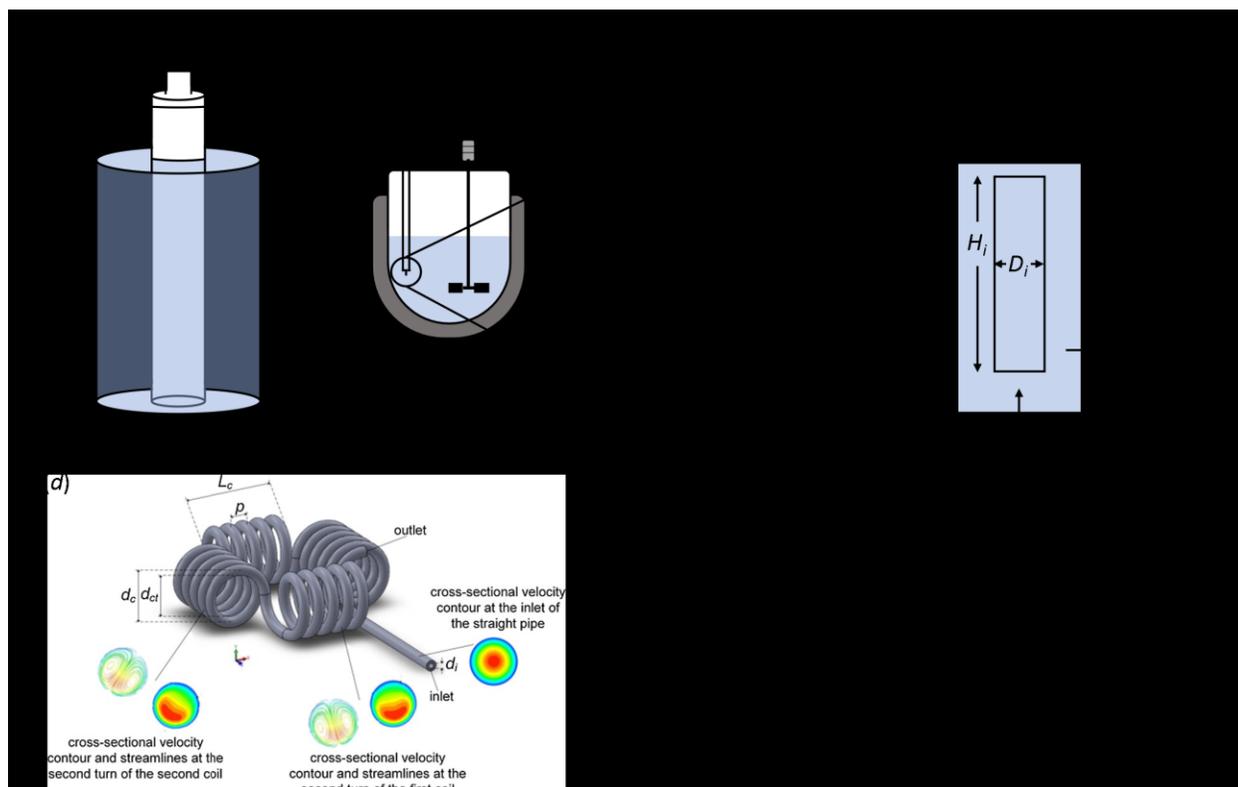
1168 *Batch and semi-batch systems.* The use of a batch reactor allows for adjustment of
1169 process parameters during the time course of the reactive crystallization, such as decreasing the
1170 temperature or adjusting the pH value towards the end of a batch so as to crystallize more
1171 product and increase the overall process yield. For example, in the enzymatic synthesis of beta-
1172 lactam antibiotics shown in Figure 6, the solution pH value typically decreases as the reaction
1173 progresses due to the formation of acidic products. The lower pH value further decreases the
1174 solubility of the product, improving product crystallization and yield.^{4, 261}

1175 Batch and semi-batch reactive crystallization processes are operated in well-mixed
1176 reactors that allow for implementation of on-line PATs, are robust, and are more resistant to
1177 clogging and encrustation issues than tubular reactors. Also, these well-mixed reactors are often
1178 highly modular, allowing for the inclusion of baffles, a draft tube,²⁶² or different impeller types
1179 to enhance mixing.²⁶³ Cao *et al.*⁸⁵ used an airloop-lift reactor (ALR) to improve mixing for the
1180 batch reactive crystallization of Ni(OH)₂ over traditional impeller stirring. Another alternative to
1181 traditional impeller-stirred reactors is the Taylor-Couette reactor used by Ferreira *et al.*,¹⁹⁸ which
1182 uses a combination of inner rotating and outer stationary cylinders to gently mix the slurry of
1183 crystals and catalyst particles in the region between the cylinders (Figure 13). The design is used
1184 to protect the catalyst particles, which are susceptible to the shear stress induced by an impeller
1185 in a conventionally mixed reactor. Often, traditional impeller stirring may be adequate for a
1186 system, but for very fast reactions, the various parameters involving mixing and reactant addition
1187 rate or novel techniques of mixing may need to be investigated to achieve a desirable crystal size
1188 distribution.

1189 In the case of fast reactions in semi-batch systems, mixing and the method and rate of
1190 reactant addition significantly impacts the product size distribution. Åslund and Rasmuson²⁶⁴
1191 studied the effect of stirring rate, impeller type, reactant concentration, reactant feed rate, and
1192 feed position (e.g. surface level, bulk liquid, next to impeller feeds) on the size distribution of
1193 benzoic acid crystals formed via reactive crystallization. The rate of addition of the reactant
1194 hydrochloric acid, reactant concentration, and stirring rate significantly influenced the product
1195 size distribution. As the stirring rate was increased, the size of resulting crystals increased up to a
1196 maximum where crystal size began to decrease; the type of impeller and feed position had a
1197 lesser effect on the product size distribution, especially at higher stirring rates. Chen *et al.*¹¹⁴
1198 investigated mixing during reactive crystallization of barium sulfate. Three separate scales of

1199 mixing, Kolmogorov, turbulent, and convective, were proposed in a new mixing model
 1200 composed of viscous deformation and molecular diffusion in a slab element. The model was
 1201 used to give accurate predictions of the effect of stirring speed, feed location, and viscosity on
 1202 particle sizes. Zauner and Jones^{265, 266} investigated the effect of feed rate, feed concentration,
 1203 feed tube diameter, impeller type and stirring rate on particle size for the reactive crystallization
 1204 of calcium oxalate and calcium carbonate. Overall, the results of the aforementioned mixing
 1205 studies suggest that poor mixing conditions promote a higher rate of primary nucleation, leading
 1206 to a larger number of nuclei and a size distribution of smaller final crystals.

1207 *Continuous systems.* As in batch systems, the stirred tank is the most commonly-used
 1208 vessel in continuous systems, but alternative geometries have also been proposed and
 1209 implemented. Several examples of alternatives to the stirred-tank crystallizer are shown in
 1210 Figure 13. These include Taylor-Couette, impinging jet, airlift loop, continuous flow inversion,
 1211 and oscillatory baffled crystallizers. Examples (a), (b), and (c) in Figure 13 approximate
 1212 MSMPRs, while (d) and (e) are used to provide near plug-flow behavior.



1213
 1214 *Figure 13. Summary of novel reactive crystallizers; (a) Taylor-Couette,^{198, 267} (b) Impinging jet mixer,¹⁶⁵ (c)*
 1215 *airlift loop,⁸⁵ (d) continuous flow inverter – Reprinted with permission from Kurt et al.²⁶⁸ copyright 2017, Elsevier,*
 1216 *(e) continuous oscillatory baffled.¹⁹⁰*

1217 For reactions of short timescales, often a reactor that is nearly perfectly mixed is used due
1218 to its robust operation and the ease of implementing process analytical technologies (which are
1219 discussed later and may include *in situ* microscopy, Raman and IR spectroscopy, and particle
1220 size analysis). Well-mixed reactors such as an MSMPR are also used when high supersaturation
1221 is not desired, such as when high supersaturation promotes the formation of an undesired
1222 polymorph or a finer crystal size distribution. For reactions in which high reactant concentrations
1223 are preferred, a single well-mixed reactor may not be the best design because it operates at outlet
1224 conditions; that is, conditions throughout the vessel correspond to those at the outlet. However,
1225 the use of a plug-flow reactor may introduce clogging concerns.²⁶⁹ To address this issue, Hu *et*
1226 *al.*²⁷⁰ utilized multiple MSMPR reactors in series to approach plug-flow behavior for a second-
1227 order reaction in which high reactant concentration was needed to achieve high conversions.

1228 When the reaction proceeds much faster than crystallization (both nucleation and
1229 growth), techniques such as wet-milling or sonocrystallization can promote nucleation and more
1230 rapid consumption of supersaturation. Yang *et al.*²⁷¹ and Acevedo *et al.*²⁷² showed that wet
1231 milling in a continuous crystallizer increased the yield, operating as a promoter of both primary
1232 and secondary nucleation for paracetamol in two different solvents. Use of wet-milling has also
1233 been shown to enable deracemization of conglomerates by combining the principles of
1234 preferential crystallization and Viedma ripening.²⁷³ Sonocrystallization, or the application of
1235 ultrasound to a crystallizer, has been shown to hasten crystallization in batch.²⁷⁴ Hatakka *et al.*¹⁸⁰
1236 used sonocrystallization to selectively produce a single polymorph during the batch reactive
1237 crystallization of L-glutamic acid while experiments without sonication resulted in a mixture of
1238 polymorphs. The authors concluded that the polymorphic purity results from reduced
1239 supersaturation due to enhanced nucleation by sonication. Wet-milling and sonocrystallization
1240 can both lead to narrower, finer size distributions as a result of increased nucleation.^{275, 276}

1241 Slower reactions may require the use of multiple vessels in series to achieve higher
1242 conversions. Mo and Jensen²⁷⁷ demonstrated the use of a micro-CSTR cascade for two separate
1243 solid-forming reactions: (1) the reaction of glyoxal and cyclohexylamine to form the practically
1244 insoluble N,N'-dicyclohexylethylenediimine and (2) the sulfonylation of 2-octanol which
1245 produced the sparingly soluble side product triethylamine hydrochloride. For the first reaction, a
1246 six-unit CSTR cascade (15-minute total residence time) was needed to reach nearly 100%
1247 conversion while the second reaction only required three CSTRs to achieve 100% conversion.

1248 Effective control of process parameters such as temperature and pH, often important variables in
1249 determining the reaction and crystallization rates, is typically achieved in well-mixed reactors
1250 with the inclusion of probes, a thermal jacket, and addition of acid or base. Process control will
1251 be discussed in more detail below.

1252 Mixing intensity may be an issue in continuous reactive crystallization. Like batch
1253 crystallizers, if the reaction utilizes a catalyst that is susceptible to high shear, a Taylor-Couette
1254 style reactor may be operated with a feed and continuous product removal. Aggregation of
1255 mixing-induced nuclei may also be a concern, leading to a wide crystal size distribution (CSD).
1256 Liu *et al.*¹⁶⁵ found that incorporation of an impinging jet mixer in the continuous reactive
1257 crystallization of the antibiotic sodium cefuroxime resulted in a narrower CSD and improved
1258 product stability compared to a traditional impeller-stirred reactor. Jung *et al.* found a similar
1259 decrease in the size distribution using a Taylor-Couette reactor for calcium hydroxide production
1260 because the more gentle mixing discouraged agglomeration.²⁷⁸

1261 Continuous tubular reactors such as plug flow reactors (PFRs) are frequently used in the
1262 chemical industry. Higher overall concentrations of reactants across the length of the reactor lead
1263 to higher conversions for positive-order reactions. For reactive crystallization, unlike in a well-
1264 mixed tank, temperature or pH value may be varied along the length of the reactor, allowing for
1265 the enhancement of reaction or crystallization kinetics in different sections. Jiang and Ni¹⁹⁰
1266 varied the temperature across a continuous oscillatory baffled crystallizer (COBC), a type of
1267 continuous tubular reactor designed to achieve plug flow at low fluid velocities, such that higher
1268 temperatures in the initial segments favored the reaction and lower temperatures towards the
1269 outlet improved the rate of crystallization. Kurt *et al.*²⁶⁸ achieved near plug-flow behavior of
1270 slurry by designing and operating a coiled flow inverter (CFI) crystallizer for the reactive
1271 crystallization of calcium carbonate. The inverting flow and helically coiled tubing enhanced
1272 mixing via formation of Dean and Taylor vortices, which increased secondary flow
1273 perpendicular to the primary flow direction. Others have physically segmented plugs of slurry by
1274 injecting inert gas spacers.²⁷⁹ All of these crystallizers enhance mixing and slurry suspension by
1275 achieving a more plug-flow-like flow profile than conventional PFRs. Increased turbulence using
1276 these novel designs permits the use of reactors with larger diameters and shorter lengths to
1277 achieve the same residence times. In general, using small-diameter tubing to achieve adequate
1278 turbulence and slurry suspension is a concern in PFRs because of clogging. Polster *et al.*⁸⁴

1279 attempted to design a continuous reactive crystallization process for a BACE inhibitor using a
 1280 PFR, but eventually settled on an MSMPR due to clogging inside the reactor tubing. Oroskar and
 1281 Turian²⁸⁰ developed the following correlation to estimate the critical slurry velocity, which is
 1282 defined as the velocity required to suspend particles and prevent their deposition in a tube or
 1283 pipe:

$$1284 \quad \frac{v_c}{\sqrt{gd(s-1)}} = 1.85C^{0.15}(1-C)^{0.36} \left(\frac{d}{D}\right)^{-0.38} \left(\frac{D\rho_l\sqrt{gd(s-1)}}{\mu}\right)^{0.090} x^{0.30} \quad (23)$$

1285 All dimensional variables are in SI units and v_c represents the critical velocity, d the equivalent
 1286 spherical particle size, C the fractional slurry density, D the pipe diameter, ρ_l the liquid density,
 1287 μ the liquid viscosity, and s the ratio of the liquid-to-solid density. Here, x is a correlation factor
 1288 estimated using the fraction of particles above the critical velocity generally approximated to be
 1289 unity. This correlation may be used to estimate the minimum diameter of a PFR to avoid
 1290 clogging keeping in mind that the minimum diameter, while providing the most turbulence, must
 1291 be large enough to accommodate the largest crystals.

1292 Another downside of using continuous tubular reactors is that the composition of the
 1293 suspension cannot be easily manipulated after the inlet. Thus, controlling the pH can be difficult
 1294 (especially for reactions involving acids and bases), which may lead to unintended changes in
 1295 reaction or crystallization kinetics across the reactor. Controlling pH is a special challenge in
 1296 working with enzymes as biocatalysts typically work in very narrow, well-regulated pH
 1297 environments. As a solution, Jiang and Ni¹⁹⁰ used multiple sampling ports across the length of a
 1298 tubular reactor to learn more about the slurry by off-line analysis. Another issue arises when a
 1299 continuous tubular reactor requires seed crystals to initiate crystallization; either the reactor must
 1300 be fed seed crystals or a recycle stream must be incorporated to introduce crystals at the inlet,
 1301 complicating the design and operation of the reactor. In contrast, a well-mixed reactor (for
 1302 example, an MSMPR unit) does not face this issue as it operates with a suspension of crystals
 1303 that participate in secondary nucleation and foster crystal breeding during continuous operation.

1304 ***Modelling, Monitoring, and Process Control.*** A control scheme for reactive
 1305 crystallization processes depends on the nature of the species being produced and its desired
 1306 characteristics. Various factors such as temperature,¹⁹³ pH,¹²⁷ and the presence of additives²⁸¹
 1307 can dictate the final crystal properties in specific processes. More generally, control of

1308 supersaturation and seeding have the greatest effect on crystal size distribution, crystal shape,
1309 and polymorphic form. Compared to crystallization alone, supersaturation may be more difficult
1310 to control in a reactive crystallization process because it can only be manipulated indirectly via
1311 adjusting the reaction rate. Extreme examples are near-instantaneous reaction rates, typical of
1312 ionic systems, where the only manipulation of the reaction rate is through the supply of reactants.
1313 Slow-reacting systems are also difficult to control as the solution stays near saturation ($S \approx 1.0$).
1314 Reactive crystallization models that couple the kinetics of the three governing phenomena of
1315 chemical reaction, nucleation, and crystal growth are constructed to narrow an operating window
1316 that will provide a desired CSD, crystal shape, and polymorph.^{5, 113} From models, the
1317 development of process control algorithms for reactant flow rate or seed-crystal addition can be
1318 tuned to optimize robust production of the desired crystal properties.

1319 One of the earliest and most general models for semi-batch reactive crystallization
1320 processes focused on developing reactive phase equilibrium equations and diagrams based on
1321 reaction equilibria where the products are non-soluble and instantly form a solid.²⁸² While useful
1322 for identifying reaction conditions and simulating reactor performances that generate only solid
1323 products, this model focused on hypothetical examples and did not include the kinetics of
1324 nucleation and growth that determine CSD and crystal shape. Kelkar and Ng²⁸³ expanded this
1325 model to include nucleation and growth kinetics for MSMPR crystallizers. Their model included
1326 the steps for reactions in solution generating supersaturation, nucleation, and linear growth rate
1327 of crystals from supersaturated product in solution. Applying their model for process design,
1328 they studied the reaction rate under different reactor throughput conditions, dissolution rates, and
1329 mass transfer rates. The effect of different reaction rates, nucleation rates, and growth rates on
1330 the product weight fraction distribution was also predicted.

1331 The previously discussed models primarily focus on using hypothetical kinetic
1332 parameters to simulate reactor performance, while only a few studies have been directed towards
1333 process optimization. Choong and Smith²⁸⁴ further expanded semi-batch reactive crystallization
1334 models by including a population balance to allow for the optimization of CSD. Assuming
1335 perfect mixing, the initial amount of reactants, feed addition time, and number of feeds were
1336 considered to be design variables for two optimization problems: (1) maximizing crystal size
1337 with a constraint of maximum coefficient of variation of the size distribution and (2) minimizing
1338 the coefficient of variation subject to a constraint of minimum average crystal size. A stochastic

1339 optimization framework was then used to circumvent traditional pitfalls such as nonconvergence
1340 or suboptimal solutions in highly nonlinear systems.²⁸⁴ The model neglected secondary
1341 nucleation with the rate of nuclei generation being defined by Equation (9). Within that
1342 limitation, their model allowed for devising nonlinear control policies that could be implemented
1343 in a semi-batch reactive crystallization process.

1344 While the studies discussed above are not exhaustive, they have developed models that
1345 present the primary features of reactive crystallization processes and strategies for their
1346 optimization. Other reactive crystallization models include more specific studies on modelling
1347 and control of enantiomer and polymorph crystallization,²⁸⁵ multi-objective optimization and
1348 generation of Pareto-optimal solutions for desired crystal properties,²⁸⁶ incorporation of seeding
1349 strategies,²⁸⁷ resistances in double-film mass transfer models for gas-liquid systems,¹²¹ and
1350 effects of macro- and micromixing regimes on crystal size distributions.¹¹⁴ System-specific
1351 models to predict control profiles for optimal mean crystal size and narrow CSD have also been
1352 developed for ampicillin,²⁸⁸ barium carbonate,¹⁰⁸ aluminum hydroxide,¹¹⁵ and 2,4,6 -triamino-
1353 1,3,5-trinitrobenzene.¹²² Similar models for continuous reactive crystallization have also been
1354 developed but focus primarily on instantaneous reaction kinetics²⁸⁷ or are specific to a given
1355 system^{5, 113} and examples in the literature are still quite limited in the literature.

1356 Reactive crystallization process modeling and process evaluation would not be robust
1357 without in-line monitoring using PAT and sensors to obtain qualitative and quantitative data on
1358 the evolution of the solution and crystal phases.²⁸⁹ The use of PAT is important for process
1359 monitoring, which in turn allows for analyses of reaction and crystallization mechanisms and
1360 process control. A summary of PATs common to reactive crystallization processes is shown in
1361 Figure 14. Attenuated total reflectance-Fourier transform infrared (ATR-FTIR) coupled with
1362 multivariate models is often used to analyze the liquid-phase composition during the process, as
1363 it has low solid-phase sensitivity.^{29, 290, 291} Raman spectroscopy can be used to quantify solution
1364 or crystal composition for molecules that can undergo large polarization changes and thus exhibit
1365 strong Raman scattering. Raman measurements are especially useful in systems with co-
1366 crystallization or multiple polymorphs to distinguish different solids.^{180, 237, 290, 291} Focused beam
1367 reflectance measurement (FBRM) estimates the evolution of chord-length distributions of
1368 crystals (a proxy for, but fundamentally different from, the crystal size distribution) in real
1369 time.^{84, 98, 146, 173, 270, 292} Coupled with system-dependent algorithms, chord-length distributions

1370 can be directly related to crystal size distributions; however, substantial work is required to
1371 transform chord-length distributions for comparison with size distributions obtained by laser
1372 diffraction or optical imaging.^{293, 294} Particle vision and measurement (PVM) can provide *in situ*
1373 estimates of crystal size and shape by observing crystals in a crystallizer or a reactor as
1374 transformations take place. PVM has been shown to be especially useful in observing polymorph
1375 shifts,²⁹⁵ agglomeration,^{88, 296} and crystal growth under different process conditions.²⁹² Other
1376 monitoring techniques include HPLC for offline solution composition measurements and laser
1377 diffraction particle size analyzers coupled with image analysis to collect information about
1378 particle size and shape. Crystal structure can be further characterized offline with x-ray
1379 diffraction (XRD) and x-ray powder diffraction (PXRD). For products that undergo color
1380 changes upon degradation, a stability chamber and transmittance measurements using UV to
1381 obtain color-grade data can be used to evaluate purity of the final product. These methods are
1382 performed offline after crystal isolation but they do provide metrics for confirmation and
1383 calibration of online measurements or process stability.²⁹⁷ PATs are often combined to give a
1384 more complete view of the reaction and crystallization phenomena.

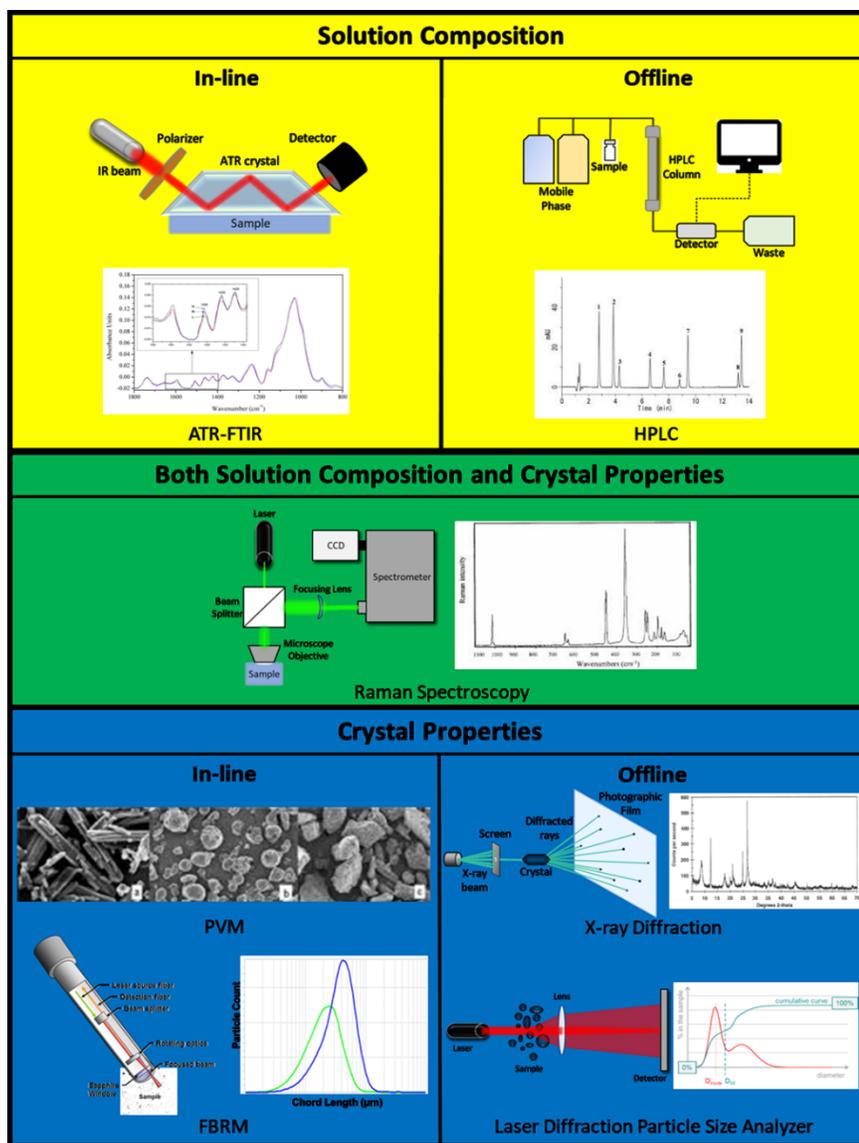


Figure 14. Common PAT used for characterizing composition and concentration of species in solution as well as crystal properties. Representative data outputs from each PAT are shown.

1385 Control of final product properties can be achieved without modelling the system of
 1386 interest but requires a detailed understanding of how different process parameters affect qualities
 1387 of the solution and crystal phases. Polster *et al.*⁸⁴ developed a continuous reactive crystallization
 1388 process for production of an API for clinical trials and studied experimentally how crystallizer
 1389 residence time, temperature, solvent composition, and recycle configuration impacted size
 1390 distribution, final blend flow function coefficients, yield, and tapped density. The control
 1391 strategy then focused on feedback control of reactant flow rates and pH adjustments.

1392 In any control application, model-free control is simpler and easier to implement
1393 compared to model-based optimal control, but the latter can provide superior performance if an
1394 accurate model is available. A representative example for how PAT can assist in modelling,
1395 monitoring, and optimal control during the development of a large-scale process is the reactive
1396 crystallization of glutamic acid from monosodium glutamate and sulfuric acid.²⁹⁸ A common
1397 control strategy in batch antisolvent or cooling crystallizations is to determine the optimal
1398 supersaturation trajectory for the process as a function of some manipulated variable such as
1399 temperature or anti-solvent flow rate and to design a feedback control system to maintain the
1400 optimal state using ATR-FTIR for direct measurement of solution concentrations.^{299, 300} Direct
1401 concentration control commonly used in antisolvent or cooling crystallizations is often difficult
1402 to employ in reactive crystallizations due to strong process nonlinearities that can arise from
1403 coupled reaction, dilution, and crystallization dynamics. For instance, the desired supersaturation
1404 trajectory in the reactive crystallization of glutamic acid is dome-shaped, and conventional
1405 concentration control cannot be used at many operating points because it would require a
1406 reduction in volume to hit the desired trajectory. However, volume is constantly increasing from
1407 the startup of the system due to the addition of reactants. A variation of direct concentration
1408 control known as Just-in-Time-Learning, JITL, can be employed to build a nonlinear model-
1409 predictive control strategy based on extended predictive self-adaptive control that accounts for
1410 nonlinearities.³⁰¹ This method is used to identify a set of empirical state-space models along the
1411 desired process trajectory.¹⁷⁷ JITL has also been coupled with system models to include batch-to-
1412 batch model predictive control strategies.³⁰²

1413 Glutamic acid crystallization is further complicated by the existence of two polymorphs;
1414 the desired α form is thermodynamically metastable and eventually transforms into the undesired
1415 but stable β form. Obtaining the metastable α form requires a detailed monitoring and control
1416 process. Alatalo *et al.*²⁹⁰ showed that ATR-FTIR measurements coupled with thermodynamic
1417 modeling in a multivariate partial least squares model were effective in accurately measuring
1418 glutamic acid concentrations in solution over the course of the reaction. By using coupled ATR-
1419 FTIR and Raman spectroscopy measurements, Qu *et al.*²⁹¹ determined that formation of the
1420 stable β polymorph was favored at high supersaturation. They speculated that this was due to the
1421 β form having a higher barrier to nucleation than the α form. The in-line monitoring techniques
1422 allowed discovery of the formation of the β polymorph at conditions of high global

1423 supersaturation and in regions of poor mixing, especially those where feed was introduced above
1424 the liquid surface in the crystallizer. Alatalo *et al.*^{298, 303} further extended this work to the design
1425 of a closed-loop feedback control algorithm based on the ATR-FTIR measured concentration of
1426 glutamic acid in solution and adjustment of the sulfuric acid feed rate with a PID controller. Such
1427 an arrangement allowed control of supersaturation and the formation of the α polymorph in a 50-
1428 L reactor.

1429 **Perspectives and Future Directions for Reactive Crystallization**

1430 Reactive crystallization provides opportunities for process intensification and product
1431 improvements, which could be favorable to product economics. In this section the necessary
1432 developments needed for reactive crystallization to advance to new applications are outlined,
1433 with emphasis on the need for more data, improved PAT, advanced crystallizer design, and
1434 better understanding of reaction and crystallization mechanisms. Brief guidance for adaptation of
1435 existing processes or creation of new processes for reactive crystallization is given. Finally,
1436 possible future enhancements centered on reactive crystallization, primarily continuous
1437 manufacturing and hybrid systems, are outlined.

1438 *Kinetics: distinguishing reactive crystallization from other separation techniques.*

1439 Utilizing crystallization, and therefore reactive crystallization, in industrial processes presents
1440 unique challenges with respect to product quality: namely those associated with meeting criteria
1441 on crystal size, size distribution, purity and form. Such challenges must be met while also
1442 satisfying the usual process requirements of yield and economics. Advancing reactive
1443 crystallization to where it can increase the yield of a product, while at the same time meeting
1444 quality criteria, is a great challenge. Environmental and economic sustainability add urgency that
1445 new manufacturing processes are implemented and matured.

1446 Some specific studies of how reactive crystallization can fit into a useful process have
1447 already been published.^{84, 113} However, relating reactive crystallization to meet final product
1448 specifications including purity, size distribution, morphology (including polymorphic form and
1449 crystal shape), and more, remains a difficult task. For example, a few authors have undertaken
1450 the task of optimizing simulated reactive crystallization processes,^{79, 282, 284} but bypassed the
1451 significant effort required to characterize the reaction kinetics and crystallization kinetics in the
1452 combined reactive crystallization environment.

1453 Several authors have shown that the kinetics of crystal growth and nucleation, which
1454 together with system configuration determine product crystal size distribution, can vary in the
1455 presence of other species such as reactants and byproducts.^{17, 75, 76} Elucidating reaction and
1456 crystallization kinetics in complex environments requires large volumes of data, which can come
1457 from either high-throughput or data-rich experiments. High-throughput experimentation involves
1458 measuring reaction and crystallization (that is, nucleation and growth) rates across a large
1459 sampling of process conditions and compositions to predict complex process features such as
1460 crystal size distribution. Data-rich experimentation, on the other hand, uses a smaller number of
1461 experiments, but with collection of high-dimensional data, such as crystal size distribution,
1462 which can be used to work backwards and determine reaction and crystallization kinetics. Both
1463 approaches enable the required level of description for designing new reactive crystallization
1464 processes, and substantial progress has been made towards both ends; however, each approach
1465 also comes with its own hurdles and challenges.³⁰⁴⁻³⁰⁶

1466 Reactive crystallizations typically take place in more complex solutions than cooling,
1467 antisolvent, or evaporative crystallization; PAT tools that are effective in such complex solutions
1468 would enable more accurate modeling and precise control of reactive crystallization processes.
1469 Taking ATR-FTIR as an example, each dissolved species contributes to the overall IR spectrum,
1470 and through careful construction of calibration models the concentration of each species can be
1471 extracted from the overall spectrum.^{110, 307, 308} However, the presence of uncharacterized species
1472 such as impurities, intermediates, byproducts, or catalysts, can break calibration models, and the
1473 work required to characterize all species and their combination may be too laborious or even
1474 impossible (e.g. non-isolatable intermediates). Improved baselining algorithms and regression
1475 techniques may make calibration model construction more manageable, such as recent work by
1476 Maggioni *et al.*¹¹¹ based on blind source separation and independent component analysis
1477 requiring only single point calibration with robustness against unknown species. The
1478 methodology was demonstrated on mixtures of simple oxyanions and did not perform as well
1479 when the anions' spectra overlapped. For many reactive crystallizations the reactants,
1480 intermediates, and products have similar functional groups and IR spectra; continued
1481 chemometric development is required for general solution phase monitoring by spectroscopic
1482 methods. Additionally, many species may only be present at low concentration compared to the
1483 reactants and products. In the production of terephthalic acid the intermediate 4-CBA has a

1484 maximum concentration of <10% of the total concentration of aromatics, leading to 1% 4-CBA
1485 in the final product. Using control to minimize the 4-CBA concentration is difficult as improved
1486 spectroscopic analysis would be needed to quantify the small amount of 4-CBA in such a
1487 complex solution (see Figure 5).^{193, 309} Likewise, in the enzymatic production of beta-lactam
1488 antibiotics the undesired byproduct phenylglycine (see Figure 6) may crystallize and contaminate
1489 the antibiotic slurry. Detecting the nucleation of phenylglycine amounts to detecting a change in
1490 phenylglycine concentration of <10 mmol/L in a solution with >100 mmol/L 6-APA and PGME,
1491 both of which have IR spectra with significant overlap with phenylglycine, and has proven to be
1492 very challenging with ATR-FTIR.³¹⁰

1493 Improvement in the characterization of solids will also benefit reactive crystallization
1494 process design and process control. In the case of beta-lactams the ability to distinguish between
1495 antibiotic crystals and byproduct crystals *in situ* could circumvent the challenges associated with
1496 solution-phase monitoring. FBRM has been used to indicate polymorph transformation in
1497 paracetamol³¹¹ and in-situ microscopy with machine learning has been demonstrated for
1498 classifying individual crystals versus agglomerates.³⁷ Both FBRM and *in situ* microscopy are
1499 restricted to use in slurries of low solids concentration.^{312, 313} Reactive crystallization would
1500 benefit considerably from the development of techniques that can identify new particle types
1501 with minimal training data and calibration effort, especially since many systems involve solid
1502 reactants dissolving, reacting, and crystallizing.^{196, 206, 314, 315} A promising development for these
1503 systems, where solution concentration cannot quantify reaction conversion, are composite PAT
1504 arrays and crystallization informatics.²⁸⁹ An array of complimentary sensors combined with
1505 process expertise has been shown to enable quantification of different solids concentrations in
1506 other solution-mediated solids transformations, such as polymorph transformations³¹⁶ and
1507 hydrate-to-anhydrate transformations;³¹⁷ application to a reactant-to-product transformation
1508 follows naturally.

1509 ***Determining the applicability and utility of reactive crystallization.*** Heuristics to
1510 identify when a reactive crystallization could enhance a process do not exist and should be
1511 created. It is often assumed that the product must be less soluble than the reactants, however fed-
1512 batch and continuous stirred-tank reactors (with independent solution and solids residence times)
1513 can enable reactive crystallization even when the product is more soluble. Use of co-formers can
1514 decrease the solubility of the product below that of the reactants, also enabling productive

1515 reactive crystallization. A brief guide to how reactive crystallization can improve a process is
 1516 presented in Table 4, below.

1517 *Table 4. A list of useful heuristics for recognizing when reactive crystallization is advantageous and/or*
 1518 *feasible.*

Product Type	
Inorganic	Reactive crystallization almost always possible, preferable with sparingly soluble compounds, mixing control key to supersaturation control and size control
Organic Ionizable	Usually possible with appropriate counter-ion. Preferable for temperature-sensitive compounds and hydrates. Ideal for isolating intermediates, overcoming reaction equilibrium. Requires modest aqueous solubility in charged state
Organic Nonionic	Should be evaluated on a case by case basis. Examples of successful processes include covalent reactions eliminating charged groups in aqueous solution (e.g. amide bond formation) or creating charged groups in nonpolar solvents (e.g. hydrogenolysis)
Critical Quality and Process Attributes	
Yield, Productivity, Selectivity, Sustainability	Reactive crystallization ideal for improving yields and selectivity by shifting equilibrium, isolating inhibitory products, protecting reactive intermediates
Purity, Form, Solvate	Complex composition in reaction mixture can increase number of possible impurities, may change form preference from pure solution, reaction solvents may limit solvate options
Crystal Size Distribution	Fast reactions, i.e. neutralizations and acidifications, will create a fines-dominated CSD. Slow reactions and seeding typically give large crystals. Reaction rate modification by catalyst engineering can enable fine-tuning of CSD
Methods of Reactive Crystallization	
Neutralization	Reactive crystallization by neutralization ideal for intermediate process steps, e.g. isolating an intermediate as a calcium salt before dissolving salt for further processing. Limited by neutralizing agents, usually calcium, magnesium, and ammonium
Acidification	Ionizable compounds typically least soluble in protonated (neutrally charged) form, ideal for removing acids/bases from complex mixtures of nonionic species
Covalent reaction	System specific, often catalyst dependent. Least generalizable but most opportunity for process improvement. Requires that the catalyst be in a form that can easily be separated from the crystal product

1519
 1520 ***Continuous manufacturing.*** The end-to-end integrated continuous manufacturing
 1521 paradigm is becoming increasingly important in the pharmaceutical industry, due in large part to
 1522 the potential benefits of lower costs, shorter supply chains, smaller footprints, and better quality

1523 monitoring and controls with PAT.^{259, 318, 319} In this relatively new paradigm in pharmaceutical
1524 manufacturing, reactive crystallization processes should be designed to be adapted to the whole
1525 process, rather than considered as an independent unit operation. For example, traditional batch
1526 operations may allow operational flexibility over a range of conditions, such that the reaction
1527 time can be shortened or extended based on the extent of reaction; such alterations are not easily
1528 made in continuous reactors.

1529 Control of raw materials to an integrated reactive crystallization is important, as: (1) raw
1530 materials often include insoluble particles requiring a clarification bypass system beforehand;³²⁰
1531 (2) variability in raw materials (like differences in purity or water content) could result in lower
1532 yield or higher impurity profile. Batch processes have more flexibility to handle raw material
1533 variability; different control strategies for continuous reactive crystallization may be more or less
1534 amenable to mitigating the risks of variability in raw material composition, based on the
1535 frequency and extent of the irregularity.

1536 ***Novel reactive crystallization process designs.*** Process intensification has been cited as
1537 one of the primary reasons for implementing a reactive crystallization process. Further
1538 intensification can be found with examples of evaporative reactive crystallization,²⁰² cooling
1539 reactive crystallization,³²¹ membrane-assisted reactive crystallization,^{322, 323} liquid-liquid
1540 extraction reactive crystallization,¹⁸¹ and chromatography-assisted reactive crystallization.^{241, 324}
1541 In each case multiple techniques may be applied simultaneously: for example, a reaction
1542 occurring in one liquid phase, crystallization occurring in a second liquid phase, and rapid mass
1543 transfer between phases;³²² or sequentially: for example, a reactive crystallization occurring at
1544 high temperature with fast reaction kinetics followed by cooling to reduce solubility and generate
1545 supersaturation while sacrificing reaction speed.⁸⁹

1546 Most complex chemical processes require catalysts to control reactions and produce
1547 desired products. Using stoichiometric amounts of catalysts is often undesirable from the
1548 standpoints of process economics as well as purification. Catalysts must be recovered for
1549 sustainability and product purity. Separating solid catalysts from a crystal slurry can be
1550 prohibitively difficult; several examples of reactive crystallization followed by dissolution for
1551 the purpose of catalyst recovery have already been discussed.^{92, 198} Alternatively a soluble
1552 catalyst can be used and retained/recovered via ultrafiltration, which may work well for
1553 dissolved biocatalysts as bio-macromolecules can be separated from small molecules with

1554 ease.^{182, 325} Nanofiltration, which has proven useful for removing impurities during
1555 crystallization,³²⁶ may be useful for recovery of non-biologic soluble catalysts. However,
1556 membranes are subject to fouling and are not compatible with all solvents, substrates, and
1557 catalysts, in which case the pursuit of solid-solid separations based on size, density, or other
1558 properties may be preferable. Examples of such solid-solid crystal-catalyst separators include
1559 hydrocyclones,¹⁴¹ elutriation,³²⁷ and sieves.¹⁹⁸

1560 Further research into the fundamentals of crystallization in complex environments, i.e.
1561 with multiple solutes, solvents, and surfaces, will enable future synthesis and separation
1562 processes with improved yield and sustainability.

1563 **Concluding remarks**

1564 As process designers continue to experiment with novel methods of increasing economic
1565 and environmental sustainability, reactive crystallization has become increasingly attractive as a
1566 means to those ends. Reactive crystallization is not particularly new, as ionic compounds have
1567 been synthesized by reactive crystallization since the beginning of the chemical industry.
1568 However, new applications of reactive crystallization promise to make possible new processes
1569 and improve existing ones. New applications of ionic reactive crystallization include capturing
1570 greenhouse gases as carbonates, recovering minerals from wastewater, and enabling fermentation
1571 routes to platform chemicals. Covalent reactive crystallization, while less developed, has more
1572 promise as a tool to enhance existing reactions or overcome the kinetic and equilibrium
1573 limitations of formerly untenable reactions. Biocatalytic processes could benefit the most, as
1574 those systems are most sensitive to accumulations of products and intermediates. Additionally,
1575 crystallization plays a dominant role in processes to separate enantiomers, where the
1576 combination of a racemization reaction and crystallization can lead to enantiomeric excess
1577 greater than 99%. The design of reactive crystallization systems follows closely the design of
1578 crystallizers in general. Crystallization is a highly nonlinear process; controlling crystallization
1579 coupled with a reaction is difficult but many control strategies and reactor designs have proven
1580 effective for specific cases. The future of reactive crystallization rests on collection of more data
1581 and generalization of findings from disparate case studies, which is the primary aim of this
1582 review. While this review may not be exhaustive, it should serve as a starting point for the design
1583 of reactive crystallization processes for any type of compound across many scales of industry.

1584 **Conflicts of Interest**

1585 The authors have no conflicts to declare.

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