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nanoconfinement using lanthanides**

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## Defining silica-water interfacial chemistry under nanoconfinement using lanthanides

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### Environmental Significance Statement

The findings reported in this paper enable more accurate modeling for the fate and transport of contaminants, nutrients, and valuable chemical species, by taking into account nanoconfinement-driven changes to the energetics and products of interfacial reactions. Nanoconfined silica-water interfaces are pervasive in the environment, including nanopores in soils and in sedimentary silicate rocks. The reactivity of nanoconfined silica-water interfaces is hard to predict, compared to non-confined systems, due to the decrease in the dielectric constant and density of nanoconfined water across the pores. To quantify nanoconfinement-driven changes to silica-water interface reactivity we use lanthanide ions and their predictable variations in size, coordination environment, and hydration energies. We discovered that nanoconfinement promotes inner-sphere complexation and the formation of poly-nuclear surface species, and, as a result, changes the adsorption reaction from an endo- to an exothermic process. We report that ion's free energy of hydration is a descriptor that can be used in thermodynamic models to capture the nanoconfinement-driven changes in the equilibrium constant for inner-sphere adsorption reactions.

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17 **Defining silica-water interfacial chemistry under nanoconfinement using**  
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## Abstract

A quarter of Earth's land surface is covered by porous sedimentary silicate rocks, so silica-water interfaces are critical to the fate and transport of chemical species on a global-scale. However, while the physiochemical properties of unconfined silica-water interfaces are understood reasonably well, these properties have proven to be unpredictable when the interface is confined in nanometer-scale pores within sedimentary rocks. For example, the existing theories struggle to quantitatively predict how the energetics of adsorption reactions and the coordination environment of adsorbed species shift due to nanoconfinement of an interface. Here, we utilized gradual and known variations in the properties of trivalent lanthanide ions to decipher the chemical interactions that cause the nanoconfinement effects on chemistry at the silica-water interfaces. We discovered that the lanthanide's free energy of hydration ( $\Delta G_{\text{hydr}}$ ) is a descriptor that can be used to predict the extent to which nanoconfinement will change the thermodynamics and products of interfacial reactions. We show that nanoconfinement promotes inner-sphere complexation between lanthanides and silica surface, as well as the formation of polymeric surface species. In nanoconfined domains lanthanide's  $\Delta G_{\text{hydr}}$  becomes less negative, reducing the energy required to dehydrate the ion during the formation of an inner-sphere surface complex. These nanoconfinement effects on chemistry become more pronounced for ions with lower hydration free energies.

*Keywords: nanoconfinement, silica, lanthanides, hydration free energy, adsorption*

## Introduction

Molecular-scale chemical reactions at solid-water interfaces in near-surface environments define the macroscale fate, transport, and global cycling of all chemical species. The rates and products of these reactions are determined by the reactivity of solid interfaces but also by whether the interface is spatially confined.<sup>1,2</sup> While confinement at the nanoscale (nanoconfinement) can occur under a variety of conditions, H<sub>2</sub>O trapped in nanoscale silica (SiO<sub>2</sub>) pores are of particular interest to geochemists because they are the most pervasive interfaces on Earth.<sup>3</sup> Consequently, accurately predicting the behavior of these interfaces is crucial for a broad range of predictive models, from determining the potential pollution pathways for stored nuclear waste to the probable consequences of removing H<sub>2</sub>O or oil from underground reservoirs. The physiochemical properties of unconfined SiO<sub>2</sub>-H<sub>2</sub>O interfaces, whose surface chemistry is driven by silanol (Si-OH) functional groups, are reasonably well known, but the physiochemical properties of the nanoconfined interfaces are much less predictable.<sup>1,2,4-7</sup> The impact of nanoconfinement on adsorption reactions is not fully understood for SiO<sub>2</sub>-H<sub>2</sub>O interfaces.<sup>2,8-11</sup> Understanding these interactions is urgent because the fundamental nanoscale chemistry drives macroscopic chemical fluxes.<sup>1,2,8</sup> For example, in nanoporous channels, methane gas has anomalously high solubility.<sup>12</sup> Similarly, in nanotubes, bulk ion mobilities and diffusivities no longer apply,<sup>13</sup> and transport behavior is defined by ion size, ion solvated structure, and ion-nanostructure interactions.<sup>14</sup>

To date, research has focused on the fascinating changes in the properties of H<sub>2</sub>O confined in SiO<sub>2</sub> pores under idealized laboratory conditions and in molecular dynamic simulations.<sup>4,6,14-16</sup> For example, scientists previously observed that, as nanoscale pore size decreases, the ratio of

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3 structured H<sub>2</sub>O (molecules with lower rotational freedom) to unstructured H<sub>2</sub>O increases, due to  
4 increasing surface-to-volume ratio within the reactive domains.<sup>17, 18</sup> Therefore, nanoconfinement  
5 decreases the dielectric constant, density, surface tension, and freezing point of H<sub>2</sub>O,<sup>16, 19-22</sup>  
6 because of the overlap of electrical double-layers within the nanoscale pores and corresponding  
7 re-structuring of water's hydrogen bonding networks.<sup>20, 22</sup> However, the nanoconfinement effects  
8 are also impacted by the density of the Si–OH functional groups, and this phenomenon is not  
9 well studied, even though the variables are complex.<sup>9, 10, 23, 24</sup> Consequently, there is no fully  
10 reliable predictor for the thermodynamic and structural shifts in surface complexation  
11 (adsorption) reactions that occur between Si–OH and adsorbing ions when SiO<sub>2</sub>-H<sub>2</sub>O interfaces  
12 are confined. The changing chemical properties of H<sub>2</sub>O itself<sup>5-7, 17, 22, 25</sup> result in a decrease in the  
13 solvation energy of dissolved ions and an increase in the aqueous complexation,<sup>8, 26 27, 28</sup> affinity  
14 and surface speciation of ions adsorbed onto solid surfaces,<sup>8, 10, 23, 29, 30</sup> as well as changes to the  
15 diffusion properties, electron transfer,<sup>31-33</sup> and nucleation reactions.<sup>34-39</sup>

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35 One notable study on small molecule interactions with SiO<sub>2</sub> surfaces shows that the guest-host  
36 interactions become stronger with decreasing pore diameter and increasing density of Si–OH  
37 functional groups.<sup>24</sup> Another study examined surface speciation of zinc Zn<sup>2+</sup> adsorbed at  
38 nanoconfined SiO<sub>2</sub>-H<sub>2</sub>O interfaces, and found that the local coordination of Zn<sup>2+</sup> changes from  
39 primarily tetrahedral to a mixture of tetrahedral and octahedral inside progressively smaller SiO<sub>2</sub>  
40 pores.<sup>10</sup> In our previous studies, we used copper (Cu<sup>2+</sup>) to assess nanoconfinement effect on the  
41 energetics of adsorption and on coordination environment of adsorbed Cu<sup>2+</sup> because this ion is a  
42 contaminant of concern and has sufficient affinity for SiO<sub>2</sub> surface (suitable for investigation  
43 using X-ray absorption fine structure (XAFS) spectroscopy).<sup>9, 23</sup> We found that nanoconfinement  
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3 of the SiO<sub>2</sub>-H<sub>2</sub>O interface leads to dramatic changes in the energetics of Cu<sup>2+</sup> adsorption: the  
4 adsorption is *endothermic* for unconfined, and *exothermic* for confined SiO<sub>2</sub>. We also found that  
5 nanoconfinement promotes the formation of poly-nuclear Cu<sup>2+</sup> species on the SiO<sub>2</sub> surface.  
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7 However, this study was limited because only Cu<sup>2+</sup> ion was used to probe the reactivity of SiO<sub>2</sub>-  
8 H<sub>2</sub>O interfaces, and therefore a number of important variables, such as charge and size of the  
9 adsorbing ion and its hydration free energy ( $\Delta G_{\text{hydr}}$ ), were not investigated. Therefore, in this  
10 study we use Ln<sup>3+</sup> ions to further quantify how nanoconfinement affects the relative reactivity of  
11 nanoconfined (porous) and unconfined (non-porous) SiO<sub>2</sub>-H<sub>2</sub>O interfaces, in particular what role  
12 does the ion size and  $\Delta G_{\text{hydr}}$  play. Lanthanide (Ln<sup>3+</sup>) series, which includes elements with atomic  
13 numbers from 57 (lanthanum, La) to 71 (lutetium, Lu) all have the same charge (3+) and slight,  
14 gradual variations in their sizes (1.250 Å for La<sup>3+</sup> to 0.995 Å for Lu<sup>3+</sup>)<sup>40</sup>,  $\Delta G_{\text{hydr}}$  values, and  
15 hydration numbers (8 for La<sup>3+</sup> to 9 for Lu<sup>3+</sup>).<sup>41</sup> They also have reasonably high adsorption  
16 affinity for SiO<sub>2</sub> surface, making them a remarkable system to study the chemistry of  
17 nanoconfined SiO<sub>2</sub>-H<sub>2</sub>O interfaces.  
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38 We quantified the effects of nanoconfinement on the Ln<sup>3+</sup> adsorption reaction (both the  
39 energetics of adsorption and the coordination environment) by assessing the subtle and  
40 systematic differences in the ionic radii,  $\Delta G_{\text{hydr}}$  values, and hydration numbers. We then  
41 employed theoretical energetic calculations of the solvation and dimerization processes to  
42 further support our experimental conclusions. Batch adsorption, column flow calorimetry, XAFS  
43 spectroscopy and cluster-based density functional theory (DFT) calculations all show that the  
44 Ln<sup>3+</sup> ion's  $\Delta G_{\text{hydr}}$  determines the extent to which nanoconfinement changes the heat signature  
45 and the products of interfacial reactions at SiO<sub>2</sub>-H<sub>2</sub>O interfaces. This discovery can form the  
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3 basis for a predictive thermodynamic framework that explains the nanoconfinement-driven  
4 changes in interfacial chemistry at the abundant SiO<sub>2</sub>-H<sub>2</sub>O interfaces, at both the molecular and  
5 macroscales. Moreover, these chemical changes in the Ln<sup>3+</sup> binding at nanoconfined SiO<sub>2</sub>-H<sub>2</sub>O  
6 interfaces make it possible to improve the separation approaches for Ln<sup>3+</sup> series ions – a key  
7 technological hurdle of our time.<sup>42</sup>  
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## 18 Experimental

### 21 SiO<sub>2</sub> substrates and adsorption experiments

23 A series of experiments were performed to measure the uptake of the lanthanide (Ln<sup>3+</sup>) ions  
24 neodymium (Nd<sup>3+</sup>), europium (Eu<sup>3+</sup>), terbium (Tb<sup>3+</sup>), thulium (Tm<sup>3+</sup>) and lutetium (Lu<sup>3+</sup>) onto  
25 porous and non-porous SiO<sub>2</sub>. All Ln<sup>3+</sup> ions were in trivalent oxidation state. All experiments were  
26 conducted using: (1) commercially available SBA-15 series mesoporous SiO<sub>2</sub> (Sigma Aldrich)  
27 with a mean pore diameter of 7.0±0.3 nm and 4.4±0.1 nm, and surface areas of 661±5 m<sup>2</sup> g<sup>-1</sup> and  
28 580±13 m<sup>2</sup> g<sup>-1</sup>, respectively<sup>23</sup> (referred to as “porous SiO<sub>2</sub>” throughout); and (2) non-porous  
29 fumed silica SiO<sub>2</sub> (Sigma Aldrich) with a surface area of 192 m<sup>2</sup> g<sup>-1</sup>.<sup>9</sup> Two types of adsorption  
30 experiments were performed: single adsorbate and competitive adsorbate (for which all five  
31 lanthanides were present simultaneously). The background electrolyte in all cases was 0.01M  
32 sodium chloride (NaCl). Milli-Q H<sub>2</sub>O with a resistivity of 18 MΩ·cm was used for all stock  
33 solutions and experiments. Lanthanide ion (Ln<sup>3+</sup>) stock solutions were prepared by diluting their  
34 nitrate salts Ln(NO<sub>3</sub>)<sub>3</sub> in Milli-Q H<sub>2</sub>O. Aqueous concentration was verified by inductively  
35 coupled plasma mass spectrometry (ICP-MS) analysis as described below.  
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3 For the single adsorbate experiments,  $20\pm 3$  mg of  $\text{SiO}_2$  was weighted into centrifuge vials, then  
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5 Milli-Q  $\text{H}_2\text{O}$  and 1M NaCl were added, and samples were hydrated for a minimum of 48 hours.  
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7 At the beginning of the adsorption experiment,  $\text{Ln}^{3+}$  stock solution was added, and the total  
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9 volume of each sample was brought to 20 mL. The pH was immediately adjusted to  $\text{pH } 6.0\pm 0.1$   
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11 using dilute sodium hydroxide (NaOH) or hydrochloric acid (HCl), and samples were reacted for  
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13 48 hours, at which point equilibrium was reached. For the competitive adsorption experiment,  
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15  $50\pm 3$  mg of  $\text{SiO}_2$  was weighted into centrifuge vials, and milli-Q  $\text{H}_2\text{O}$  and NaCl were added to  
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17 hydrate the substrate for a minimum of 48 hours. Stock solution containing  $19 \mu\text{M L}^{-1}$  of  $\text{Nd}^{3+}$ ,  
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19  $\text{Eu}^{3+}$ ,  $\text{Tb}^{3+}$ ,  $\text{Tm}^{3+}$  or  $\text{Lu}^{3+}$  were used, and the final concentrations for each  $\text{Ln}^{3+}$  in the reactors  
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21 were set at 0.2, 1, 5, and  $10 \mu\text{M L}^{-1}$ . The total volume of each reactor was 20 mL. Immediately  
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23 thereafter, dilute NaOH or HCl was used to adjust the pH of each reactor to  $\text{pH } 6.0\pm 0.1$ , and  
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25 samples were equilibrated for 48 hours on a shaker table. All experiments were performed at  
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27 ambient temperature ( $22 \text{ }^\circ\text{C}$ ).  
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35 At the completion of the adsorption experiments, samples were centrifuged to separate solid and  
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37 aqueous phases. The aqueous portion was filtered using a  $0.2 \mu\text{m}$  nylon membrane filter and  
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39 acidified using 6N ultrapure nitric acid ( $\text{HNO}_3$ ). Aqueous samples were analyzed using ICP-MS  
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41 to quantify the concentrations of each  $\text{Ln}^{3+}$  remaining in the aqueous phase after adsorption took  
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43 place. ICP-MS data was acquired using a NexION 350D mass spectrometer (Perkin Elmer)  
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45 equipped with a collision-reaction cell. The quantification of all  $\text{Ln}^{3+}$  concentrations was done in  
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47 normal mode. Calibration curves for each analyte were obtained by running certified standard  
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49 solutions prior to each analytical run, with a resulting  $R^2$  value of 0.9999 or better.  
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53 From aqueous concentrations, surface coverage (uptake) in  $\mu\text{moles m}^{-2}$  was calculated using:  
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$$\text{Surface coverage} = \frac{C_{\text{initial}} - C_{\text{final}}}{m_{\text{SiO}_2} \times SA_{\text{SiO}_2}}$$

Where  $C_{\text{initial}}$  and  $C_{\text{final}}$  are  $\text{Ln}^{3+}$  concentrations in  $\mu\text{moles L}^{-1}$  at the onset and at the completion of the adsorption experiment, respectively;  $m_{\text{SiO}_2}$  is mass in grams and  $SA_{\text{SiO}_2}$  is surface area in  $\text{m}^2 \text{g}^{-1}$  for  $\text{SiO}_2$  solids.

### X-ray absorption fine structure spectroscopy (XAFS) data collection and analysis

Samples for XAFS analysis were prepared by equilibrating aqueous suspensions of porous  $\text{SiO}_2$  with 4.4 nm and 7.0 nm pores and non-porous fumed  $\text{SiO}_2$  with the  $\text{Nd}^{3+}$ ,  $\text{Tb}^{3+}$ , and  $\text{Lu}^{3+}$  stock solutions described above. The pH was adjusted to  $5.8 \pm 0.1$ , and samples were suspended in 0.01 M NaCl background electrolyte.

XAFS data at the  $\text{Nd}^{3+}$ ,  $\text{Tb}^{3+}$ , and  $\text{Lu}^{3+}\text{L}_{\text{III}}$ -edges was collected using beamline 10-BM at the Advanced Photon Source (APS), Argonne National Laboratory. The beamline is equipped with a water-cooled Si(111) monochromator, which was calibrated using metal reference foils and detuned by 50% to reject higher harmonics. The monochromator step size was 10 eV in the pre-edge, 0.5 eV in the XANES region, and  $0.05 \text{ \AA}^{-1}$  in the XAFS region. Fluorescent counts were collected using a Vortex Si Drift solid-state 4-element detector. Standard compounds analyzed included  $\text{Nd}_2\text{O}_3$ ,  $\text{Tb}_2\text{O}_3$ , and  $\text{Lu}_2\text{O}_3$ .

The XAFS data processing was done using the Athena interface and XAFS data fitting was done using the Artemis interface<sup>43</sup> to the IFEFFIT<sup>44</sup> program. The background subtraction

(AUTOBK algorithm<sup>45</sup>), normalization, and conversion into k-space were conducted as described elsewhere.<sup>46</sup> The Fourier-transformed Nd, Tb, and Lu L<sub>III</sub>-edge XAFS spectra were analyzed using the Artemis interface to IFEFFIT by fitting theoretical paths,<sup>47</sup> which were based on the structures of lanthanide-containing apatite.<sup>48</sup> The structure files were edited to remove partial occupancies, so that FEFF calculations could be performed. The fitting was done in R-space using a Hanning window and k-weights of 1, 2, and 3. The amplitude reduction factor ( $S_0$ ) was determined by fitting XAFS spectra collected on Nd<sub>2</sub>O<sub>3</sub>, Tb<sub>2</sub>O<sub>3</sub>, and Lu<sub>2</sub>O<sub>3</sub> standards. Due to higher noise associated with the Nd adsorption samples, only the 1<sup>st</sup> shell was fitted. The amplitude reduction factor  $S_0$  was set at 0.88 for Nd, 0.67 for Tb, and 0.71 for Lu, based on fitting data collected on model compounds Nd<sub>2</sub>O<sub>3</sub>, Tb<sub>2</sub>O<sub>3</sub>, and Lu<sub>2</sub>O<sub>3</sub>. Errors at a 95% confidence level (2 sigma) are shown in parenthesis in SI Table S2.

### Microcalorimetry experiments

The flow microcalorimeter (FMC) used in this study was custom-designed and fabricated in the Kabengi Laboratory at Georgia State University. The details about this instrumentation and basic operational procedures can be found in previous publications.<sup>49</sup> To obtain the thermal signatures and subsequently the heats of Nd<sup>3+</sup>, Tb<sup>3+</sup>, and Lu<sup>3+</sup> adsorption, a  $20.0 \pm 0.5$  mg sample of porous SiO<sub>2</sub> or  $50.0 \pm 0.5$  mg of non-porous SiO<sub>2</sub> particles was homogeneously packed into the sample holder of the FMC's microcolumn. The packed column was equilibrated with a 0.01 M NaNO<sub>3</sub> solution at a flow rate of  $0.30 \pm 0.03$  mL min<sup>-1</sup> until thermal equilibrium was reached, as indicated by a steady baseline. A fixed mass of Ln<sup>3+</sup> was injected onto the column with a controlled volume of Ln(NO<sub>3</sub>)<sub>3</sub> stock solution. For porous SiO<sub>2</sub> experiments, the concentrations were 7.86 μM for Nd(NO<sub>3</sub>)<sub>3</sub>, 11.22 μM for Tb(NO<sub>3</sub>)<sub>3</sub> and 8.42 μM for Lu(NO<sub>3</sub>)<sub>3</sub>. Due to the low

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3 calorimetric signal obtained for non-porous SiO<sub>2</sub>, the concentrations of the stock solutions were  
4 increased to 157.2 μM for Nd(NO<sub>3</sub>)<sub>3</sub>, 224.4 μM for Tb(NO<sub>3</sub>)<sub>3</sub>, and 168.4 μM for Lu(NO<sub>3</sub>)<sub>3</sub>. To  
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6 keep the ionic strength (I) constant throughout the experiment, the NaNO<sub>3</sub> concentration was  
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8 kept at 0.01 M. The calorimetric signal corresponding to the interaction of Ln<sup>3+</sup> with the SiO<sub>2</sub>  
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10 sample was thus obtained. Once the thermal signal returned to the original baseline, the input  
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12 solution was switched back to 0.01 M NaNO<sub>3</sub>. Effluent samples were collected during the  
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14 experiment for quantifying aqueous concentrations of Ln<sup>3+</sup> using ICP-MS as described above.  
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16 Aqueous samples for ICP-MS analysis were collected during flow experiment and preserved  
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18 with 6N ultrapure HNO<sub>3</sub>. The mass of Ln<sup>3+</sup> retained at (and subsequently desorbed from) the  
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20 surface was determined by a mass balance calculation between the mass of the injected Ln<sup>3+</sup> and  
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22 the mass recovered in all effluents. The heats of reactions ( $Q_{\text{ads}}$  in mJ·m<sup>-2</sup>) and molar enthalpies  
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24 ( $\Delta H$  in kJ·mol<sup>-1</sup>) were calculated by integrating the calorimetric peaks and were converted to  
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26 energy units (Joules) by calibration with calorimetric peaks of known energy inputs generated  
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28 from a calibrating resistor. The solution pH was adjusted daily using dropwise addition of 0.1 M  
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30 HNO<sub>3</sub> and 0.1 M NaOH to achieve a final pH of 6.0 ± 0.1. Changes in total concentration and  
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32 ionic strength resulting from pH adjustments were determined to be negligible.  
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## 42 Density Functional Theory Calculations

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44 Cluster-based density functional theory (DFT) calculations with varying dielectric constants  
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46 were performed to estimate how  $\Delta G_{\text{hydr}}$  of Lu<sup>3+</sup> and Nd<sup>3+</sup> changes as a function of the dielectric  
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48 constant of H<sub>2</sub>O. The free energy of dimerization reactions for Nd<sup>3+</sup> and Lu<sup>3+</sup> were calculated in  
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50 pure H<sub>2</sub>O using Gaussian code g09,<sup>50</sup> with explicit H<sub>2</sub>O and the PCM dielectric solvation  
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52 method,<sup>51</sup> and the Stuttgart 1993 (“cep-121g”) effective core potential.<sup>52</sup> For Ln<sup>3+</sup> monomers in  
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3 H<sub>2</sub>O, 8- and 9-coordinated solvation shells were the most stable for Lu<sup>3+</sup> and Nd<sup>3+</sup> at both  $\epsilon=10$   
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5 and  $\epsilon=78$ . Two dimer clusters were considered, having overall nominal stoichiometries of  
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7 (Ln<sup>3+</sup>)<sub>2</sub>(OH<sup>-</sup>)<sub>2</sub>(H<sub>2</sub>O)<sub>n</sub>, with n=12 and 13, and the “OH<sup>-</sup>” groups bridging the cations. The latter  
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9 structure was found to be more stable, and therefore was used in all cases. Note that the  
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11 optimized dimer structures for Lu<sup>3+</sup> and Nd<sup>3+</sup> differ in their bridge structures. For Lu<sup>3+</sup>, the  
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13 bridging groups are in effect two H<sub>3</sub>O<sub>2</sub><sup>-</sup>, while for Nd<sup>3+</sup> they consist of one H<sub>3</sub>O<sub>2</sub><sup>-</sup> and an OH<sup>-</sup>.  
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## 21 Results and Discussion

### 22 Adsorption of lanthanides onto porous and non-porous SiO<sub>2</sub> surfaces

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24 Batch experiments were performed for single Ln<sup>3+</sup> ions (where only Nd<sup>3+</sup>, Eu<sup>3+</sup>, Tb<sup>3+</sup>, Tm<sup>3+</sup> or  
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26 Lu<sup>3+</sup> were present) and in competitive adsorption studies (with all five Ln<sup>3+</sup> ions present  
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28 simultaneously). Systematic variation in the adsorption affinity on the examined SiO<sub>2</sub> surfaces  
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30 was observed, specifically that the uptake of individual Ln<sup>3+</sup> ions increases at higher atomic  
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32 numbers (Figure 1a-b), in agreement with earlier investigations.<sup>53</sup> To assess how  
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34 nanoconfinement within SiO<sub>2</sub> affects adsorption trends, comparisons were made between the  
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36 surface-area-normalized Ln<sup>3+</sup> uptake on porous SiO<sub>2</sub>, with mean pore diameters of 4.4 nm and  
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38 7.0 nm, respectively. As in our previous study of Cu<sup>2+</sup>,<sup>9</sup> pore-diameter-dependent adsorption was  
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40 observed for the lighter (larger) Ln<sup>3+</sup> ions (Nd<sup>3+</sup>, Eu<sup>3+</sup>, and Tb<sup>3+</sup>); however, the heavier (smaller)  
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42 Ln<sup>3+</sup> ions (Tm<sup>3+</sup> and Lu<sup>3+</sup>) did not exhibit pore diameter dependence (Figure 1c-f).  
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49 Our previous research indicates that slight re-structuring of H-bonding networks in H<sub>2</sub>O confined  
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51 in SiO<sub>2</sub> pores results in a decrease in the freezing temperature and density of H<sub>2</sub>O,<sup>54</sup> and we  
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53 deduce that similar re-structuring of H<sub>2</sub>O inside the pores is likely to affect the local structure  
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3 around the adsorbing  $\text{Ln}^{3+}$  ions. Therefore, *here we hypothesize that nanoconfinement effects are*  
4 *more pronounced in weaker-hydrated ions than in ions with tighter hydration spheres and higher*  
5 *free energy of hydration ( $\Delta G_{\text{hydr}}$ ). The reported  $\Delta G_{\text{hydr}}$  values increase from -3280  $\text{kJ}\cdot\text{mol}^{-1}$  for*  
6  *$\text{Nd}^{3+}$  to -3515  $\text{kJ}\cdot\text{mol}^{-1}$  for  $\text{Lu}^{3+}$ ,<sup>40, 41</sup> and our calculated values listed in the SI file are -3454*  
7  *$\text{kJ}\cdot\text{mol}^{-1}$  for  $\text{Nd}^{3+}$  and -3629  $\text{kJ}\cdot\text{mol}^{-1}$  for  $\text{Lu}^{3+}$ . The batch adsorption results support our*  
8 *hypothesis since adsorption of strongly hydrated  $\text{Tm}^{3+}$  and  $\text{Lu}^{3+}$  is independent of pore diameter*  
9 *(Figure 1e,f). We therefore conclude that the main chemical descriptor determining whether*  
10 *nanoconfinement affects the adsorption behavior is the  $\Delta G_{\text{hydr}}$  of the adsorbing ion. As hydration*  
11 *numbers decrease and negative hydration free energy increases, dehydration reactions become*  
12 *more energetically costly, so the nanoconfinement effects on adsorption become less*  
13 *pronounced as the Ln series progresses from  $\text{Nd}^{3+}$  to  $\text{Lu}^{3+}$ . Our previous work on  $\text{Cu}^{2+}$  could also*  
14 *support this conclusion, since  $\text{Cu}^{2+}$  exhibits pore-diameter-dependent adsorption on the same*  
15  *$\text{SiO}_2$  materials and has the hydration energy lower than the examined  $\text{Ln}^{3+}$  ions (-506.75*  
16  *$\text{kcal}\cdot\text{mol}^{-1}$  or -2120  $\text{kJ}\cdot\text{mol}^{-1}$ ).<sup>23, 55</sup>*

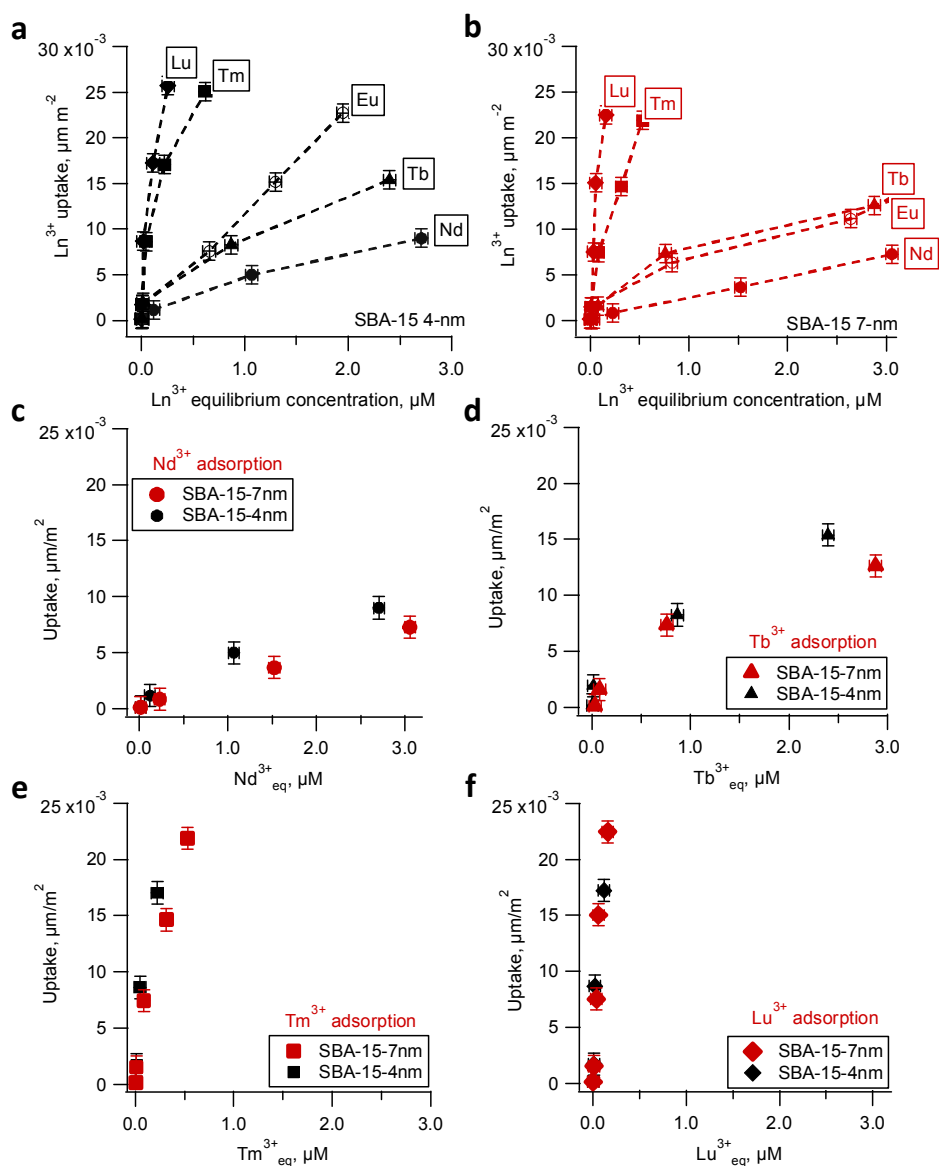
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38 The competitive adsorption results agree with the single-element tests, showing that heavier  
39 (smaller)  $\text{Ln}^{3+}$  ions have higher affinity for  $\text{SiO}_2$  surfaces (Figure 2a-c). Interestingly, the slope in  
40 the uptake vs. ionic radius plot of the  $\text{Ln}^{3+}$  ions becomes steeper with increasing surface  
41 coverage, indicating that the difference in affinities between lighter and heavier  $\text{Ln}^{3+}$  ions  
42 depends primarily on the surface coverage (uptake) (Figure 2a-c). Consequently, the surfaces of  
43 both non-porous and porous  $\text{SiO}_2$  solids become progressively more selective towards heavier  
44  $\text{Ln}^{3+}$  ions, as increasing coverage results in increasing competition for the adsorption sites.  
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54 Consequently, as more porous  $\text{SiO}_2$  surface sites are occupied, the task of separating individual  
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Ln<sup>3+</sup> ions from each other using column or batch separation becomes increasingly efficient. The overall Ln<sup>3+</sup> uptake was higher for non-porous SiO<sub>2</sub>, likely because adsorption of Ln<sup>3+</sup> onto porous SiO<sub>2</sub> is hindered by slow diffusion into the long channels in porous SiO<sub>2</sub> (Supporting Information, Figure S1). In the competitive adsorption study, the pH values for porous SiO<sub>2</sub> samples with the highest concentrations of Ln<sup>3+</sup> ions decreased from an initial pH of 6.0 to a pH of 5.6 or 5.7. However, under the same Ln<sup>3+</sup> adsorption conditions, the pH in non-porous SiO<sub>2</sub> samples remained constant at a pH of 6.0. These pH trends may indicate that, during Ln<sup>3+</sup> adsorption onto porous SiO<sub>2</sub>, inner-sphere complexation reactions cause the SiO<sub>2</sub> surface to deprotonate. In contrast, the predominant mode of adsorption for non-porous SiO<sub>2</sub> is outer-sphere complexation, where Ln<sup>3+</sup> ions do not displace protons from the surface, as indicated by the lack of change in pH.

To further elucidate the mechanism of surface complexation reactions, the equilibrium constants of the reactions for porous and non-porous SiO<sub>2</sub> solids were assessed. The reactive sites on the SiO<sub>2</sub> surfaces are the silanol functional groups Si–OH. The surface-site density of silanol groups is 2.3 ± 0.2 OH nm<sup>-2</sup> for the porous SiO<sub>2</sub> with 4.4 nm pores, 1.8 ± 0.2 OH nm<sup>-2</sup> for the porous SiO<sub>2</sub> with 7.0 nm pores,<sup>54</sup> and 2.15 ± 0.2 OH nm<sup>-2</sup> for non-porous SiO<sub>2</sub>.<sup>9</sup> The hydroxyl site densities are similar for the porous and non-porous SiO<sub>2</sub> solids; however, a different concentration of surface Si–OH groups was available in each reactor, since the constant was the mass of the solid (50 mg) rather than the surface area (661 ± 5 m<sup>2</sup> g<sup>-1</sup> for 7.0 nm, 580 ± 13 m<sup>2</sup> g<sup>-1</sup> for 4.0 nm, and 192 m<sup>2</sup> g<sup>-1</sup> for non-porous SiO<sub>2</sub><sup>54,9</sup>). The equilibrium constant for the surface complexation reaction was calculated using:

$$K_{ads} = \frac{[Ln_{ads}^{3+}] \times [H^+]}{[Si-OH_{surf}]}$$

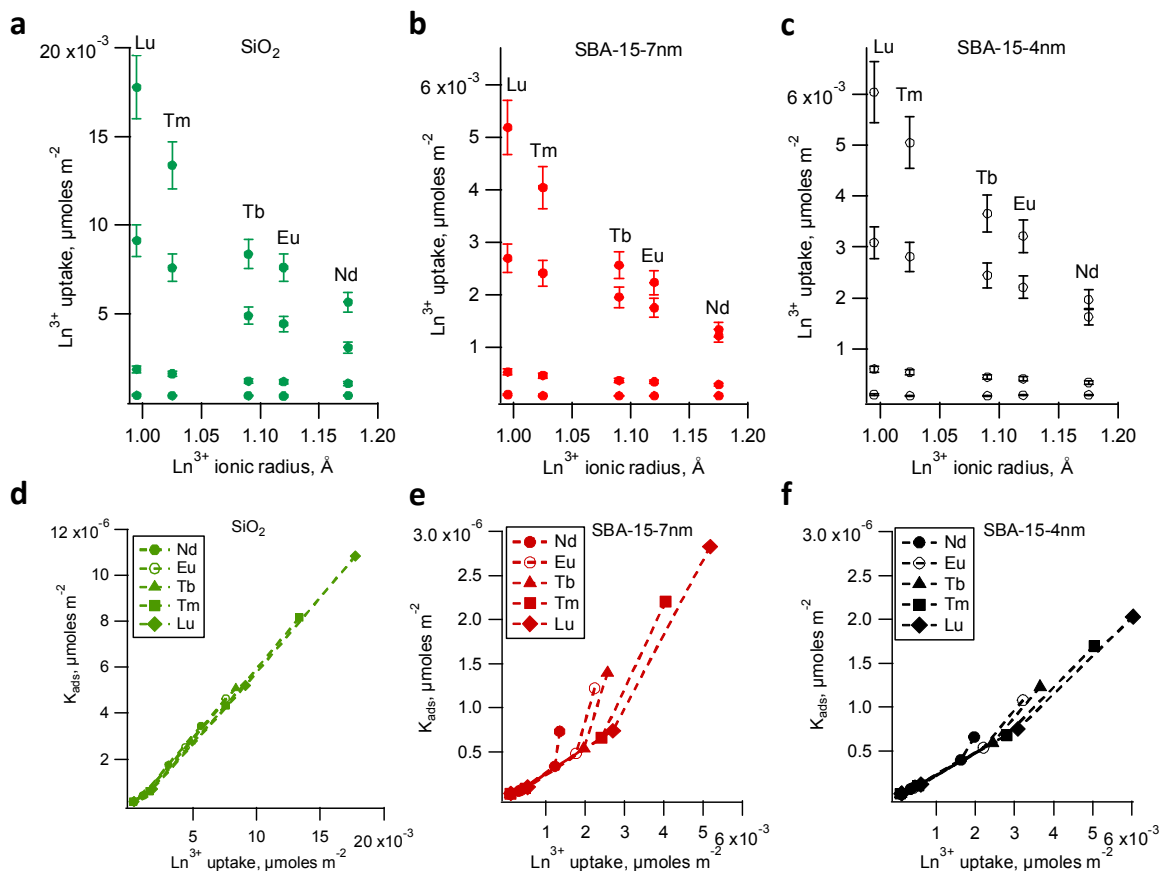
where  $[Ln_{ads}^{3+}]$  in moles $\cdot$ m $^{-2}$  is the concentration of adsorbed  $Ln^{3+}$ ,  $[H^+]$  in moles $\cdot$ L $^{-1}$  is the proton concentration at the completion of the experiment, and  $[Si - OH_{surf}]$  in moles $\cdot$ L $^{-1}$  is the concentration of available hydroxyl surface sites available in the reactor. The calculated  $K_{ads}$  values are shown in Figure 2d-f, and the summary table with these values is included in the SI file (Table S2). Plotted against the surface coverage by  $Ln^{3+}$  ions, these  $K_{ads}$  values elucidate the differences between the chemical adsorption mechanisms for porous and non-porous SiO $_2$ . For



**Figure 1.** Mass-dependent uptake of individual  $Ln^{3+}$  ions onto porous SiO $_2$  with (a) 4.4 nm pores, and (b) 7.0 nm pores. Comparison of the uptake on 4.4 nm pores and 7.0 nm pores is shown for (c) Nd $^{3+}$ , (d) Tb $^{3+}$ , (e) Tm $^{3+}$ , and (f) Lu $^{3+}$ . For the lighter  $Ln^{3+}$  ions (Nd $^{3+}$ , Tb $^{3+}$ , and Eu $^{3+}$ ) the uptakes are higher on SiO $_2$  surfaces with 4.4 nm pores than on surfaces with 7.0 nm pores. For the heavier Tm $^{3+}$  and Lu $^{3+}$  ions, the uptakes are independent of the pore diameter.



non-porous SiO<sub>2</sub>, the plot gradually collapses into a single line; however, for porous SiO<sub>2</sub>, the relationship is non-linear (Figure 2d-f).



**Figure 2.** Competitive adsorption of lanthanides onto (a) non-porous SiO<sub>2</sub> and porous SiO<sub>2</sub> solids with (b) 4.4 nm and (c) 7.0 nm pores. The slope of uptake vs. ionic radius becomes steeper for the higher surface loadings, indicating increasing competition for surface adsorption sites. Equilibrium constant for adsorption reaction  $K_{ads}$  plotted vs. Ln<sup>3+</sup> uptake for (d) non-porous SiO<sub>2</sub> and porous SiO<sub>2</sub> solids with (e) 4.4 nm and (f) 7.0 nm pores.

Bulk adsorption experiments (pH shifts and  $K_{ads}$  values) indicate that adsorption mechanism differs when porous and non-porous SiO<sub>2</sub> are compared. This conclusion was further validated by the XAFS and microcalorimetry measurements, and DFT calculations discussed below.

### Local coordination environment of adsorbed lanthanides

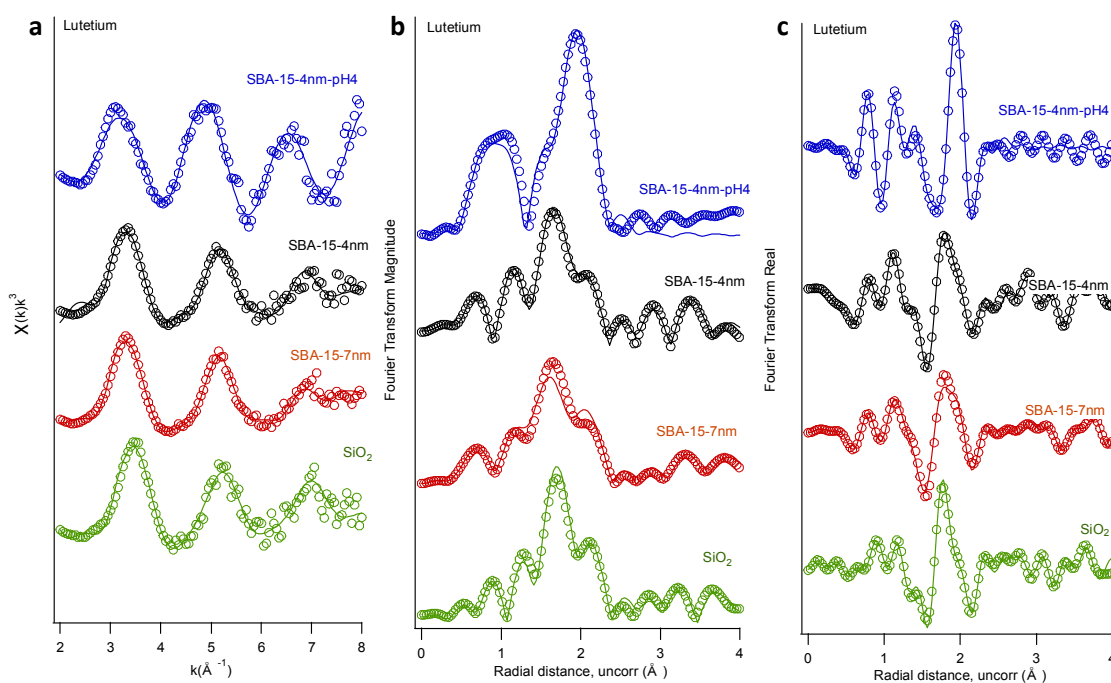
The local coordination environment around  $\text{Nd}^{3+}$ ,  $\text{Tb}^{3+}$ , and  $\text{Lu}^{3+}$  adsorbed onto non-porous and porous  $\text{SiO}_2$  solids was characterized using XAFS. As anticipated, the XAFS data shows that the nanoconfinement affects the local coordination environment of adsorbed species. However, surprisingly, the nanoconfinement effects proved to be similar for all examined  $\text{Ln}^{3+}$  ions, regardless of mass (XAFS fitting parameters are shown in SI Table S2).

The XAFS analysis was performed on both the 1<sup>st</sup> and 2<sup>nd</sup> shell nearest-neighbors to assess the nanoconfinement effects. However, only the 1<sup>st</sup> shell Nd–O spectral feature was fit for  $\text{Nd}^{3+}$ , due to poor signal-to-noise ratio. The 1<sup>st</sup> shell Nd–O spectral feature was fit with one Nd–O backscattering path at 2.50 Å for non-porous  $\text{SiO}_2$ , and at 2.54-2.56 Å for  $\text{Nd}^{3+}$  adsorbed onto porous  $\text{SiO}_2$  with 7.0 nm and 4.4 nm pores (Table S2). The Nd–O distances become slightly longer (by 0.04-0.06 Å) under nanoconfinement, which shows that first shell hydration sphere around adsorbed  $\text{Ln}^{3+}$  may be “relaxing” under nanoconfinement.

For  $\text{Tb}^{3+}$  and  $\text{Lu}^{3+}$ , the improved signal-to-noise ratios allowed for the examination of 2<sup>nd</sup> shell features. The 1<sup>st</sup> Tb–O shell was fit with two Tb–O backscattering paths at 2.22-2.28 Å and at 2.42 Å (Table S2). The presence of the Tb–Si backscattering feature indicates that  $\text{Tb}^{3+}$  forms inner-sphere adsorption complexes (consistent with our batch adsorption pH trends) on the examined porous  $\text{SiO}_2$  solids, where the Tb–Si distance is consistent with a bi-dentate bi-nuclear complex geometry (Tb–Si is 3.41-3.66 Å). With decreasing pore diameter, the Tb–O increases slightly, from 2.22 Å for  $\text{SiO}_2$  with 7.0 nm pores to 2.28 Å for  $\text{SiO}_2$  with 4.4 nm pores. For both pore diameters, the presence of Tb–Tb backscattering suggests that some of the adsorbed  $\text{Tb}^{3+}$

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3 forms dimers or other type of polymer species on the SiO<sub>2</sub> surface, and the Tb–Tb distance of  
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5 3.64–3.75 Å further suggests that the terbium dimers exist as edge-sharing moieties (*e.g.*, as in  
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7 the structure of xenotime<sup>56</sup>). This indicates that nanoconfinement may promote the formation of  
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9 poly-nuclear (*e.g.*, dimer) Ln<sup>3+</sup> species on SiO<sub>2</sub> surface.  
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For  $\text{Lu}^{3+}$  adsorption samples prepared at pH 6.0, the optimum fit for the Lu–O 1<sup>st</sup> shell was achieved by using two Lu–O backscattering paths at 2.13–2.17 Å and at 2.31–2.35 Å. Again, decreasing pore diameter results in a subtle elongation of the mean Lu–O distance. The 2<sup>nd</sup> shell was fit with Ln–Si backscattering path at 3.33–3.63 Å and (like  $\text{Tb}^{3+}$ ), reflects a bi-dentate bi-nuclear adsorption complex with backscattering features that indicate that some of the adsorbed  $\text{Lu}^{3+}$  formed dimer or other type of polymer surface species. The resulting Lu–Lu distances were 3.81–3.93 Å, indicating a single link between  $\text{Lu}^{3+}$  polyhedra (an edge sharing, or 2 links would



**Figure 3.** X-ray absorption fine structure (XAFS) spectroscopy data and shell-by-shell fitting results for  $\text{Lu}^{3+}$  adsorbed onto non-porous silica ( $\text{SiO}_2$ ) and porous  $\text{SiO}_2$  with 4.4 nm pores (SBA-15-4nm) and with 7.0 nm pores (SBA-15-7nm). (a) XAFS data and fits shown in k-space, (b) magnitude of the Fourier transform, and (c) the real part of Fourier transform. The markers denote the experimental data and the lines are the fits.

occur around 3.55 Å, as reported for keiviite in Yakubovich, *et al.*<sup>57</sup>). The XAFS data and fits for  $\text{Lu}^{3+}$  are shown in Figure 3.

The pH effects were also tested on  $\text{Lu}^{3+}$ , which was chosen due to its high affinity for the  $\text{SiO}_2$  surface (the uptake of all  $\text{Ln}^{3+}$  is lower at pH 4.0 than pH 6.0), consistent with adsorption edge

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3 data for cations).<sup>58</sup> Importantly, the coordination environment of adsorbed Lu<sup>3+</sup> proved to be  
4 quite different between samples prepared at pH 6.0 and at pH 4.0 (Table S2). The porous SiO<sub>2</sub>  
5 sample prepared with 4.4 nm pores at pH 4.0 showed lower surface loading and a worse signal-  
6 to-noise ratio than the sample prepared at pH 6.0. Consequently, only the 1<sup>st</sup> shell Lu–O distance  
7 in this sample was fit, and the fit required two Lu–O backscattering paths. The results confirmed  
8 significantly longer Lu–O distances for the pH 4.0 sample (2.27 and 2.39 Å) than for the pH 6.0  
9 sample (2.17 and 2.35 Å), presumably due to changes in the deprotonation state of H<sub>2</sub>O/OH<sup>-</sup> in  
10 the 1<sup>st</sup> shell of Lu<sup>3+</sup>. At pH 4.0, more H<sub>2</sub>O molecules around the Lu<sup>3+</sup> are in the fully protonated  
11 state (H<sub>2</sub>O), while at pH 6.0 some of these molecules de-protonate to OH<sup>-</sup>. Given their respective  
12 electrostatic considerations, the Lu–OH<sup>-</sup> distance should be shorter than the Lu–H<sub>2</sub>O distance.  
13 For example, in the Lu<sup>3+</sup> dimer calculation, the two Lu<sup>3+</sup> are linked by two H<sub>5</sub>O<sub>2</sub><sup>+</sup> “bridges,”  
14 which can be regarded as a mix of OH<sup>-</sup> and H<sub>2</sub>O. The distance between Lu<sup>3+</sup> and the O atoms in  
15 these OH<sup>-</sup>-containing bridges are 2.19, 2.26, 2.33, and 2.38 Å (average 2.29 Å), while the Lu<sup>3+</sup>–  
16 O<sub>water</sub> distances are more uniform and range from 2.30 to 2.38 Å (averaging 2.35 Å).  
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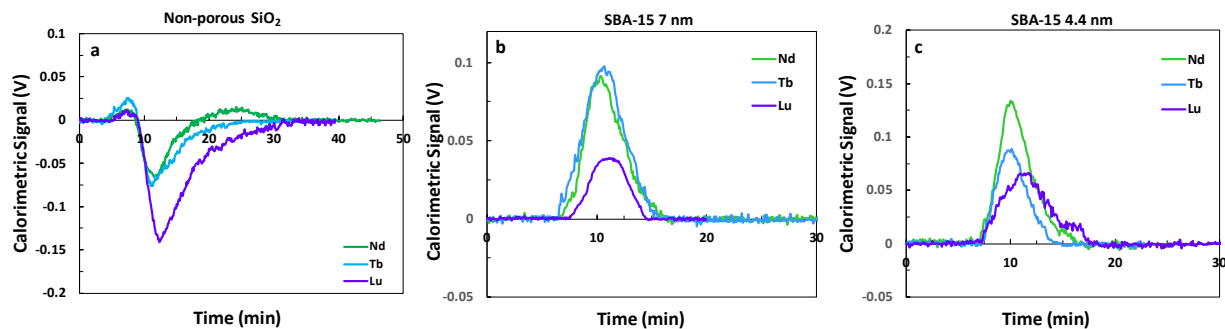
### 38 Heats of adsorption measured with flow microcalorimetry

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40 Flow microcalorimetry was performed to quantify heats of reaction on non-porous and porous  
41 SiO<sub>2</sub> solids during Ln<sup>3+</sup> adsorption. These heat measurements indicate mass-dependent and pore-  
42 size-dependent adsorption of Nd<sup>3+</sup>, Tb<sup>3+</sup>, and Lu<sup>3+</sup> onto non-porous and porous SiO<sub>2</sub> surfaces.  
43 For all three Ln<sup>3+</sup> ions, the flow microcalorimetry notably indicates a reverse in the sign of the  
44 calorimetric signal, showing an *exothermic* signal on SiO<sub>2</sub> with 4.4 nm and 7.0 nm pores and  
45 *endothermic* signal for non-porous SiO<sub>2</sub> (Figure 4). This finding is consistent with our earlier  
46 report for Cu<sup>2+</sup> adsorption onto the same SiO<sub>2</sub> substrates, evaluated using the same experimental  
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3 setup.<sup>9</sup> The summary of microcalorimetry measurement results and surface coverages is shown  
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5 in SI (Table S3). For Nd<sup>3+</sup>, Tb<sup>3+</sup> and Lu<sup>3+</sup>, the molar enthalpies of adsorption  $\Delta H_{\text{ads}}$  on porous  
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7 SiO<sub>2</sub> solids are significantly more energetic (*exothermic*, more negative) than on non-porous  
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9 SiO<sub>2</sub> (*endothermic*, less negative). Additionally, as the pore diameter decreases from 7.0 nm to  
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11 4.4 nm, Nd<sup>3+</sup> shows the largest change in the adsorption enthalpy (increase from -69.565 kJ·mol<sup>-1</sup>  
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13 to -87.270 kJ·mol<sup>-1</sup>), which indicates that the energetics of adsorption for the lighter lanthanides  
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15 are more strongly affected by nanoconfinement, further validating the batch adsorption results  
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17 (Figure 1c-f). In the microcalorimetry set of experiments, the Ln<sup>3+</sup> eluent concentrations were  
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19 chosen to correspond to the higher end of the surface coverages observed in the batch adsorption  
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21 experiments, although kinetic constraints in the flow systems prevent the achievement of full  
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23 adsorption equilibrium. The flow microcalorimetry experiments on non-porous SiO<sub>2</sub> had to be  
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25 conducted at a higher Ln<sup>3+</sup> eluent concentration to achieve a detectable calorimetric signal.  
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27 Because of this adjustment in the experimental design, higher Ln<sup>3+</sup> surface coverages were  
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29 achieved for non-porous SiO<sub>2</sub> than either of the porous SiO<sub>2</sub> solids (Table S3). Surface coverage  
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31 is an important variable in flow microcalorimetry measurements, since solid surfaces commonly  
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33 have more than one type of reactive site. Adsorption onto high-energy sites, which are occupied  
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35 first, will result in a more energetic calorimetric signal, compared to lower-energy surface sites.  
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37 Therefore,  $\Delta H_{\text{ads}}$  values can only be compared for similar surface coverages (Ln<sup>3+</sup> uptakes).  
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47 The reverse in the calorimetric signal from *endo-* to *exothermic* between non-porous and porous  
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49 SiO<sub>2</sub> solids could be explained by four possible mechanisms. First, the predominant adsorption  
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51 mechanism may be inner-sphere complexation for porous SiO<sub>2</sub> and outer-sphere complexation  
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53 for non-porous SiO<sub>2</sub>, as supported by the pH measurements in the bulk adsorption experiments  
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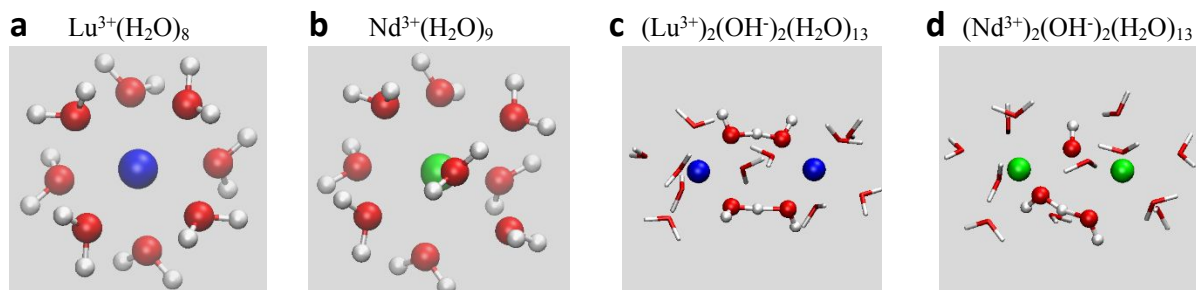
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3 (which offer evidence of surface de-protonation reactions only for porous SiO<sub>2</sub> solids) and the  
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5 XAFS data (which shows stronger Lu-Si backscattering for porous SiO<sub>2</sub>). Literature reports  
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7 similar effects for muscovite surfaces (for which the adsorption free energy  $\Delta G_{\text{ads}}$  is more  
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9 negative when the ion forms an inner-sphere complex<sup>59</sup>) and zeolites (which demonstrate  
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11 enhancement of inner-sphere complexation for major cations, specifically Na<sup>+</sup>, K<sup>+</sup>, and Ca<sup>2+</sup><sup>11</sup>).  
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14 Second, the formation of polymeric Ln<sup>3+</sup> species only on the surfaces of porous SiO<sub>2</sub> solids could  
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16 cause an *exothermic* reaction. For Ln<sup>3+</sup> to form a dimer, one or two H<sub>2</sub>O molecules must be  
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18 removed from the Ln<sup>3+</sup> hydration sphere; followed by the proton release and the formation of a  
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20 new Ln<sup>3+</sup>–(OH<sup>-</sup>)–Ln<sup>3+</sup> bond (Table 1), which are, cumulatively, an *exothermic* process. The Ln<sup>3+</sup>  
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22 dimerization on the SiO<sub>2</sub> surface may be more prevalent for porous SiO<sub>2</sub>, as indicated by the  
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24 slightly higher Lu–Lu backscattering amplitude in porous SiO<sub>2</sub> (CN column in Table S2). Third,  
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26 due to nanoconfinement, H<sub>2</sub>O inside SiO<sub>2</sub> pores has altered local structure, causing changes in  
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28 the local hydration structure around Ln<sup>3+</sup> ions approaching SiO<sub>2</sub> surface. This re-structuring of  
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30 H<sub>2</sub>O molecules is expected to change the  $\Delta G_{\text{hydr}}$ , and therefore the overall energetics of the  
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32 adsorption reaction. Based on the calculated and measured thermodynamic values, we anticipate  
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34 that these three mechanisms are acting simultaneously. Fourth, the surface coverages achieved  
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36 by Ln<sup>3+</sup> ions for porous SiO<sub>2</sub> solids are lower (Table S3), compared to non-porous SiO<sub>2</sub>, so high-  
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38 energy adsorption sites are occupied first, which likely leads to higher heat signature.<sup>60</sup> We  
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40 postulate, however, that this difference in surface coverages plays a secondary role, because Cu<sup>2+</sup>  
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42 surface coverages in our earlier work on porous and non-porous SiO<sub>2</sub> were similar, and yet we  
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44 saw the same switch from *endo-* to *exothermic* process when non-porous and porous SiO<sub>2</sub> were  
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46 compared.<sup>9</sup>  
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**Figure 4.** Total heats of adsorption for  $\text{Nd}^{3+}$ ,  $\text{Tb}^{3+}$  and  $\text{Lu}^{3+}$  (a) for non-porous  $\text{SiO}_2$ ; (b) for porous  $\text{SiO}_2$  with 4.4 nm pores; and (c) for porous  $\text{SiO}_2$  with 7.0 nm pores. For concentration-normalized data see Table S3.

### Energy considerations for lanthanide adsorption at nanoconfined $\text{SiO}_2$ surfaces

To further test the validity of the second and third proposed mechanisms ( $\text{Ln}^{3+}$  dimerization and  $\Delta G_{\text{hydr}}$  change under nanoconfinement), density functional theory calculations were performed for  $\text{Nd}^{3+}$  and  $\text{Lu}^{3+}$  in pure  $\text{H}_2\text{O}$  (Figure 5). An  $\text{H}_2\text{O}$  value for dielectric constant ( $\epsilon$ ) of  $\epsilon = 78$  was used for the unconfined (bulk) water calculations. To approximate the nanoconfinement effect, the  $\epsilon$  of  $\text{H}_2\text{O}$  was lowered to  $\epsilon = 10$  for the confined calculations.<sup>17</sup> The results are summarized in Table 1. Note that the “ $\text{H}^+$ ” free energies and enthalpies, only, relevant to dimerization due to proton release, are calculated using a B3LYP/6-311+G(d,p) level of theory<sup>61</sup> instead of the BP86 functional widely used to model  $\text{Ln}^{3+}$  hydration. The reason is that the B3LYP method yields proton hydration free energies in good agreement with measurements, while the BP86 functional significantly overestimate  $\text{H}^+$  stabilization in water.





**Figure 5.** Schematic of (a) Lu<sup>3+</sup> monomer with 8 neighboring H<sub>2</sub>O<sub>s</sub>; (b) Nd<sup>3+</sup> monomers with 9 neighboring H<sub>2</sub>O<sub>s</sub>; (c) Lu<sup>3+</sup> dimer; (d) Nd<sup>3+</sup> dimer. In (c) and (d), only the negatively charged bridging groups are shown as ball-and-stick models; the other H<sub>2</sub>O molecules are depicted as stick figures. These systems (c and d) were used to assess the free energy of the dimerization reaction.

Our calculations further support the postulated effect of dimerization reactions on the calorimetric data. The Gaussian calculations show that dimerization is favorable for Lu<sup>3+</sup> in bulk liquid H<sub>2</sub>O ( $\epsilon=78$ ), but not for Nd<sup>3+</sup>. As  $\epsilon$  decreases (due to nanoconfinement), the favorability of dimerization for Lu<sup>3+</sup> increases (Table 1). These results support the hypothesis that a reverse in the calorimetric signal could be caused by the increased formation of polymeric Lu<sup>3+</sup> species on the surfaces of porous SiO<sub>2</sub> solids. Nd<sup>3+</sup> dimerization favorability in bulk water is not predicted to be strongly affected by lowering the dielectric constant. However, the SiO<sub>2</sub> surface was not explicitly included in this analysis, and it is possible that other plausible H<sub>2</sub>O configurations would alter the calculations. Even so, the structural difference in the hydrated Lu<sup>3+</sup> and Nd<sup>3+</sup> dimer structures are readily reproducible (*e.g.* in the Fig. 5d structure, if Nd<sup>3+</sup> is replaced with Lu<sup>3+</sup>, and structure is re-optimized, then the configuration recovers, as in Fig. 5c).

**Table 1.** Calculated free energies of dimerization for Nd<sup>3+</sup> and Lu<sup>3+</sup> in pure H<sub>2</sub>O with a dielectric constant ( $\epsilon$ ) of 78, and in pure H<sub>2</sub>O with an  $\epsilon$  of 10 (nanoconfinement conditions). The stoichiometry of assumed reactions is shown.

<b>Nd<sup>3+</sup>, <math>\epsilon = 78</math></b>			
H <sub>2</sub> O + Nd(III) (H <sub>2</sub> O) <sub>8</sub> → Nd(III) (H <sub>2</sub> O) <sub>9</sub>	$\Delta G = -0.03$ eV	$\Delta G = -2.99$ kJ/mol	
2Nd(III) (H <sub>2</sub> O) <sub>9</sub> → 3H <sub>2</sub> O + 2 “H <sup>+</sup> ” + Nd(III) <sub>2</sub> (OH <sup>-</sup> ) <sub>2</sub> (H <sub>2</sub> O) <sub>13</sub>	$\Delta G = 0.48$ eV at pH=6, [Nd]=10 <sup>-5</sup> M	$\Delta G = +46.08$ kJ/mol $\Delta E = +85.74$ kJ/mol	
<b>Nd<sup>3+</sup>, <math>\epsilon = 10</math></b>			
H <sub>2</sub> O + Nd(III) (H <sub>2</sub> O) <sub>8</sub> → Nd(III) (H <sub>2</sub> O) <sub>9</sub>	$\Delta G = -0.13$ eV	$\Delta G = -12.80$ kJ/mol	
2Nd(III) (H <sub>2</sub> O) <sub>9</sub> → 3H <sub>2</sub> O + 2 “H <sup>+</sup> ” + Nd(III) <sub>2</sub> (OH <sup>-</sup> ) <sub>2</sub> (H <sub>2</sub> O) <sub>13</sub>	$\Delta G = 0.48$ eV at pH=6, [Nd]=10 <sup>-5</sup> M	$\Delta G = +46.43$ kJ/mol $\Delta E = -1.46$ kJ/mol	
<b>Lu<sup>3+</sup>, <math>\epsilon = 78</math></b>			
H <sub>2</sub> O + Lu(III) (H <sub>2</sub> O) <sub>8</sub> → Lu(III) (H <sub>2</sub> O) <sub>9</sub>	$\Delta G = +0.03$ eV	$\Delta G = 2.89$ kJ/mol	
2Lu(III) (H <sub>2</sub> O) <sub>8</sub> → H <sub>2</sub> O + 2 “H <sup>+</sup> ” + Lu(III) <sub>2</sub> (OH <sup>-</sup> ) <sub>2</sub> (H <sub>2</sub> O) <sub>13</sub>	$\Delta G = -0.25$ eV at pH=6, [Lu]=10 <sup>-5</sup> M	$\Delta G = -23.87$ kJ/mol $\Delta E = +20.30$ kJ/mol	
<b>Lu<sup>3+</sup>, <math>\epsilon = 10</math></b>			
H <sub>2</sub> O + Lu(III) (H <sub>2</sub> O) <sub>8</sub> → Lu(III) (H <sub>2</sub> O) <sub>9</sub>	$\Delta G = +0.02$ eV	$\Delta G = 1.93$ kJ/mol	
2Lu(III) (H <sub>2</sub> O) <sub>8</sub> → H <sub>2</sub> O + 2 “H <sup>+</sup> ” + Lu(III) <sub>2</sub> (OH <sup>-</sup> ) <sub>2</sub> (H <sub>2</sub> O) <sub>13</sub>	$\Delta G = -0.39$ eV at pH=6, [Lu]=10 <sup>-5</sup> M	$\Delta G = -37.35$ kJ/mol $\Delta E = -47.48$ kJ/mol	

Notes:

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3 “H<sup>+</sup>” denotes H<sub>5</sub>O<sub>2</sub><sup>+</sup> as in Grabowski et al., 2002.<sup>48</sup>

4  $\Delta E$  denotes the net energy of reaction.

5  $\Delta G$  was calculated at pH=6 and Ln<sup>3+</sup> concentration of 10<sup>-5</sup> M to explore the same conditions as in the experiments.

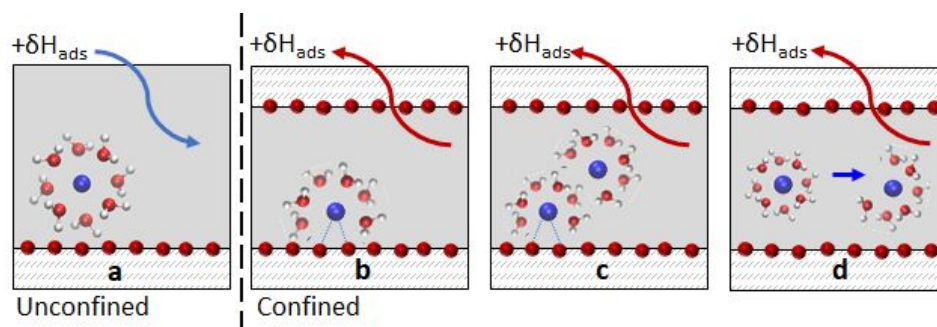
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8 In addition to the free energies shown in Table 1, the solvation energies of single Ln<sup>3+</sup> ions in  
9 H<sub>2</sub>O were calculated for different dielectric constants. In agreement with the literature, the Nd<sup>3+</sup>  
10 ions were coordinated to nine H<sub>2</sub>O molecules and the Lu<sup>3+</sup> ions were coordinated to eight <sup>41</sup>  
11 (Table S4). Due to the changes in the thermodynamic properties of H<sub>2</sub>O residing inside the  
12 pores,<sup>5, 54</sup> the thermodynamic properties of the confined Ln<sup>3+</sup> ions differ from the “standard”  
13 (unconfined) values. When Ln<sup>3+</sup> ion resides in a confined domain, its  $\Delta G_{\text{hydr}}$  becomes less  
14 negative (Table S4), which would make Ln<sup>3+</sup> dehydration less energetically costly and therefore  
15 favor inner-sphere adsorption, in agreement with the pH trends from the batch adsorption  
16 experiments.  
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## 32 Conclusion

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34 An ion’s  $\Delta G_{\text{hydr}}$  determines whether (and to what degree) nanoconfinement will change its  
35 adsorption energetics and coordination environment on a SiO<sub>2</sub> surface. Three chemical  
36 mechanisms could explain the observed shifts in the energetics and macroscopic adsorption  
37 trends due to nanoconfinement of the SiO<sub>2</sub>- H<sub>2</sub>O interface, either alone or in tandem: (1)  
38 nanoconfinement promotes inner-sphere complexation between Ln<sup>3+</sup> ions and the SiO<sub>2</sub> surface;  
39 (2) nanoconfinement promotes the formation of polymeric Ln<sup>3+</sup> species only on the surfaces of  
40 porous SiO<sub>2</sub> solids (not on non-porous SiO<sub>2</sub>); (3) nanoconfinement makes the Ln<sup>3+</sup>  $\Delta G_{\text{hydr}}$  less  
41 negative, reducing the energy required to achieve a dehydration reaction and the formation of an  
42 inner-sphere surface complex. These proposed mechanisms are illustrated in Figure 6.  
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54 Additionally, we observed that nanoconfinement causes a slight elongation of the Ln–O and  
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Ln–Si bond lengths for Ln<sup>3+</sup> adsorbed onto the SiO<sub>2</sub> surface as an inner-sphere complex. The combination of these nanoconfinement effects on the interfacial chemical processes cumulatively result in a dramatic shift in the energetics of Ln<sup>3+</sup> adsorption, causing the reaction to switch from an *endo-* to an *exothermic* process. In summary, nanoconfinement changes the energetics and products of interfacial reactions at the SiO<sub>2</sub>–H<sub>2</sub>O interface, and these effects are more pronounced for ions with lower hydration free energies.



**Figure 6.** Proposed Ln<sup>3+</sup> adsorption mechanisms which can result in an *endothermic* (+ $\delta H$ ) or an *exothermic* (- $\delta H$ ) signal. (a) Ln<sup>3+</sup> adsorption as an outer-sphere complex on unconfined SiO<sub>2</sub> surface; (b) Ln<sup>3+</sup> adsorption as an inner-sphere complex on confined SiO<sub>2</sub> surface; (c) Ln<sup>3+</sup> adsorption as an inner-sphere dimer complex on confined SiO<sub>2</sub> surface; (d) Decrease in  $\Delta G_{\text{hydr}}$  under nanoconfinement, making dehydration reaction less energetically costly.

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10 Laboratory. This paper describes objective technical results and analysis. Any subjective views  
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12 or opinions that might be expressed in the paper do not necessarily represent the views of the  
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14 U.S. Department of Energy or the United States Government.  
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## 20 Conflicts of interest

21  
22  
23 The authors declare no competing interests.  
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## 26 Author contributions

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29 AGI developed research hypothesis, performed batch adsorption and XAFS experiments and  
30 data analysis, and wrote the manuscript with input from the co-authors. PIK and NK performed  
31  
32 microcalorimetry experiments and interpreted the data. KL performed DFT calculations and data  
33  
34 analysis. AWK assisted with XAFS data collections, and LL assisted with bulk adsorption  
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36 experiments.  
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## 42 Supporting Information Available

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45 Supporting information includes transmission electron microscopy image of porous silica  
46  
47 channels; Summary Table containing  $K_{\text{ads}}$  values calculated for competitive adsorption  
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49 experiments; Summary Table of XAFS shell-by-shell fitting results; Summary Table of  
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51 measured heats of adsorption in flow microcalorimetry experiments; and Calculated  $\Delta G_{\text{hydr}}$  for  
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3 Nd<sup>3+</sup> and Lu<sup>3+</sup> as a function of dielectric constant of H<sub>2</sub>O. This material is available free of  
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