

Environmental Science Water Research & Technology

Impacts of Antiscalants on the Formation of Calcium Solids: Implication on Scaling Potential of Desalination Concentrate

Journal:	Environmental Science: Water Research & Technology
Manuscript ID	EW-ART-04-2019-000351
Article Type:	Paper
Date Submitted by the Author:	29-Apr-2019
Complete List of Authors:	Jain, Tushar; University of California, Riverside, Chemical and Environmental Engineering Sanchez, Edgar; University of California Riverside Owens-Bennett, Emily ; Trussell Technologies Inc Trussell, R.; Trussell Technologies, Walker, Sharon; University of California, Riverside, Chemical and Environmental Engineering Liu, Haizhou; University of California, Riverside, Chemical and Environmental Engineering



Water Impact Statement

The management of desalination brine has become increasingly important and a costly issue, especially in inland areas. In particular, the presence of oversaturated calcium as scale-forming compounds in the brine is challenging to dispose. I nthis study, we established a quantitative relationship to predict the nucleation rate of three commonly observed scale-forming calcium minerals in desalination brine and three widely used antiscalants. The modeling of precipitation rate from this study provided crucial information on the relationship among the rate of precipitation, antiscalant dosage and critical saturation index in desalination concentrate.

1	Impacts of Antiscalants on the Formation of Calcium Solids:
2	Implication on Scaling Potential of Desalination Concentrate
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4	Tushar Jain [†] , Edgar Sanchez [†] , Emily Owens-Bennett [‡] ,
5	Rhodes Trussell [‡] , Sharon Walker [†] and Haizhou Liu ^{*†}
6	† Department of Chemical and Environmental Engineering, University of California at
7	Riverside, Riverside, CA, 92521 USA
8	[‡] Trussell Technologies, Inc. Pasadena, CA, 91101 USA
9	* Corresponding author, e-mail: haizhou@engr.ucr.edu, phone (951) 827-2076, fax
10	(951) 827-5696.
11	
12	Submitted to Environmental Science: Water Research & Technology

14 Abstract

15 Brackish water desalination has become increasingly important in arid inland regions for 16 reliable water supplies, but the management of desalination brine waste is costly. In 17 particular, the presence of oversaturated calcium as scale-forming compounds in the brine 18 is challenging to disposal. This study investigated the effects of three widely used 19 antiscalants, i.e., nitrilotri-methylenephosphonic acid (NTMP), ethylenediaminetetra-20 methylenephosphonic acid (EDTMP) and diethylenetriaminepentakis-methylphosphonic 21 acid (DTPMP) on the precipitation of calcium from solutions under chemical conditions 22 relevant to brackish desalination brine, with an emphasis on the nucleation and 23 precipitation of three calcium-containing solids including hydroxyapatite $Ca_5(PO_4)_3OH_{(s)}$, 24 gypsum $CaSO_{4(s)}$, and vaterite $CaCO_{3(s)}$. The nucleation rates and activation energy of 25 nucleation were investigated for the first time for hydroxyapatite relevant to a desalination 26 concentrate. Results showed that all three antiscalants exhibited uniquely time-dependent 27 effects on the inhibition of calcium solid formation. The precipitation kinetics exhibited a 28 three-phase behavior, with an induction phase, a rapid reaction phase, and a final 29 equilibrium phase. The effectiveness of antiscalant in delaying calcium precipitation and 30 slowing down the rate of precipitation followed the order of DTPMP > EDTMP > NTMP. 31 Antiscalants adsorb on the nuclei of calcium solids and inhibit the crystal growth process. 32 Activation energy of nucleation increased linearly with antiscalant dosage, but it decreased 33 as the regime changed from homogeneous to heterogeneous nucleation. This study 34 generated vital information on the precipitation kinetics of calcium solids in the presence 35 of phosphonate-containing antiscalants and advances the development of desalination 36 brine management strategies.

38 Introduction

39 As freshwater scarcity becomes more severe with increasing population and climate 40 change impacts, alternative water sources - in particular, brackish groundwater - have become increasingly important for arid inland regions.^{1,2} Brackish groundwater is usually 41 formed as a result of geological salt deposition or long-term agricultural activities.³⁻⁵ It 42 typically contains total dissolved solids (TDS) levels between 1 and 10 g/L.⁶⁻⁸ In recent 43 44 years, membrane-based brackish water desalination has been increasingly implemented to 45 supply drinking water in inland areas worldwide, including Australia, the Middle East and the United States.⁹⁻¹³ For example, the operational and planned brackish groundwater 46 desalination plants in California have a combined annual capacity of 260 million gallons 47 per day as of 2013.¹⁴ 48

49 Another major challenge with desalination is scaling of the membranes themselves, a 50 phenomenon attributed to the inevitable precipitation of calcium-containing minerals 51 including calcium sulfate $CaSO_{4(s)}$, calcium carbonate $CaCO_{3(s)}$ and calcium phosphate Ca₅(PO₄)₃OH_(s) at the membrane surface.^{15,16} The efficiency of reverse osmosis based 52 53 brackish water desalination is inherently limited by membrane scaling. To control 54 membrane scaling, scale-inhibiting chemicals known as antiscalants are added to the feed water.¹⁷⁻¹⁹ These chemicals interfere with the nucleation process of calcium solids and 55 retard the crystal growth.²⁰ The continuous application of antiscalants in the feed water 56 57 results in an oversaturation of dissolved calcium that coexists with antiscalants in the brackish desalination concentrate (also known as brine).^{21,22} Meanwhile, the inhibiting 58 59 effects of antiscalants on the precipitation of calcium solids are time sensitive. For 60 example, in the Inland Empire of Southern California, a 70-mile brine pipeline system 61 carries inland brackish water desalination concentrate to a coastal disposal facility.²³ The 62 presence of antiscalants in the discharged brine prevents calcium precipitation at the entry 63 points along the brine line, but as the brine wastewater travels along the pipeline, a 64 substantial amount of additional solids are generated, creating problematic scaling issues in the pipeline.^{24,25} Other studies similarly reported the delayed precipitation of solids in 65 membrane concentrate.²⁶⁻²⁸ This inadvertent solid formation and associated challenge with 66 67 scale formation during brine disposal make it urgent to understand the effects of 68 antiscalants on solid formation.

69 Furthermore, recovery of water from desalination brine is important to minimize brine 70 disposal cost. However, the presence of oversaturated scale-forming calcium in the brine 71 is undesirable to additional water recovery. In contrast, a tunable control on antiscalants 72 can potentially accelerate the precipitation of calcium solids. This decrease in scale-73 forming constituents can help achieve higher recovery of water from brine using secondary 74 membrane units. Therefore, it is critical to understand the nature and effects of antiscalants 75 on the chemical stability of calcium solids in the brine, which can lead to the development 76 of sustainable concentrate management for inland desalination.

Most antiscalants are organic phosphorus chemicals known as phosphonic acids. They contain multiple phosphonate functional groups (-PO₃H₂) within a tertiary amine structure.^{29,30} The phosphorus-carbon bond in antiscalants exhibits a good thermal stability,³¹ and promotes their applications in desalination plants as well as cooling towers.^{32,33} The concentration of phosphonic acids in desalination processes depend on the composition of the feedwater. For brackish water desalination concentrate it is typically in the range of 2-10 μ M.^{34,35} In particular, nitrilotri-methylenephosphonic acid (NTMP), ethylenediaminetetra-methylenephosphonic acid (EDTMP) and
diethylenetriaminepentakis-methylphosphonic acid (DTPMP) are among the most widely
used antiscalants in water industry.³⁶⁻³⁹ Their molecular structures are shown in Figure S1
of the SI section.

88 Prior studies examined the impact of different antiscalants on the precipitation of calcite, 89 gypsum, silica, etc.^{29,40-42} Multiple studies have tried to quantify the dose response of antiscalants with respect to the extent of supersaturation.^{19,43,44} Recent studies investigated 90 91 the cost associated with maximizing the water recovery in membrane desalination process for brackish water with these scaling minerals.⁴⁵ Phosphonic antiscalants can also form 92 complexes with calcium and undergo multiple steps of deprotonation.⁴⁶⁻⁴⁸ However, the 93 94 effect of antiscalants on the nucleation and crystal growth process of calcium solids 95 remains unknown. Typically, the onset of solid precipitation is delayed in the presence of 96 antiscalants. This delayed period, known as induction time, is controlled by the activation energy of the nucleation process.^{49,50} A better and quantitative understanding on how 97 98 antiscalants impact the induction time is critical to predict the effectiveness of antiscalants. 99 Furthermore, although the presence of antiscalants delays nucleation reaction, the nuclei 100 formation eventually takes place. Therefore, it is important to quantify the kinetics of solid 101 precipitation in the presence of antiscalants.

In recent years, membrane-based advanced reuse of domestic wastewater in agricultural and industrial sectors have been increasingly implemented. Reclaimed wastewater is also increasingly used for industry and landscaping. Sparingly soluble hydroxyapatite $Ca_5(PO_4)_3OH_{(s)}$ in the brine becomes a major limiting factor in these scenarios where the reclaimed water is rich in phosphate.⁵¹⁻⁵⁴ While there are studies mainly focused on the 107 commonly observed scaling minerals such as $CaSO_{4(s)}$ and $CaCO_{3(s)}$,⁵⁵⁻⁵⁸ To the our best of 108 knowledge, no study has looked into the impact of antiscalants on the precipitation 109 mechanisms and kinetics of hydroxyapatite nucleation. However, the nature of calcium 110 phosphate formation and the associated antiscalant effect remains to be understood.

The objectives of this study were to examine the impacts of three widely used antiscalants (*i.e.*, NTMP, EDTMP and DTPMP) in brackish water concentrate on the nucleation process of calcium-containing solids (*i.e.*, $Ca_5(PO_4)_3OH_{(s)}$, $CaSO_{4(s)}$, and $CaCO_{3(s)}$), quantify the precipitation kinetics of calcium solid formation, and the nature of calcium phosphate nucleation in presence of these antiscalants.

116 Materials and methods

117 The solution chemical matrix for the precipitation experiments was selected based on the 118 chemical composition of the brackish RO concentrate. A synthetic concentrate allowed us 119 to precisely control and vary the saturation indices of different calcium minerals. This 120 simplified setup also helped us to understand the fundamentals of nucleation of different 121 calcium minerals in presence of the antiscalants. All solutions were prepared with 122 analytical grade chemicals and deionized (DI) water (resistivity $< 18.2 \text{ M}\Omega/\text{cm}$). To start a precipitation experiment with Ca₅(PO₄)₃OH_(s), stock solutions of 25-50 mM CaCl₂ and 1-123 124 3 mM Na₂HPO₄ were prepared and adjusted to pH 7.8 with droplets of 0.5 M NaOH and 125 0.5 M HClO₄ at a temperature of 20 °C. This pH level is typical of brackish water desalination brine.⁵⁹ Initial ionic strength of the mixing solution was fixed at 0.1 M by 126 127 adding targeted amount of NaClO₄.

128 A 150 mL solution containing CaCl₂ and a 100 mL solution containing Na₂HPO₄ were 129 adjusted to pH 7.8. Following that, 0-10 mM of NTMP, EDTMP or DTPMP prepared from 130 its respective sodium-based salt was added into CaCl₂ and Na₂HPO₄ solutions with equal 131 concentrations. Both solutions were then quickly mixed at a high stirring rate in a batch 132 reactor at 20 °C. This approach of mixing avoided possible interference due to localized 133 concentration spikes. The final mixed solution created a targeted antiscalant concentration 134 typical to a brackish water desalination brine, ranging between 0 and 11 μ M, and a 135 saturation index between 14 and 15 with respect to $Ca_5(PO_4)_3OH_{(s)}$. The saturation index 136 of $Ca_5(PO_4)_3OH_{(s)}$ is defined as:

$$SI_{Ca_{5}(PO_{4})_{3}OH} = \log\left(\frac{\alpha_{Ca^{2}+}^{5} \times \alpha_{PO_{4}^{3}-}^{3} \times \alpha_{OH^{-}}}{K_{sp, Ca_{5}(PO_{4})_{3}OH_{(s)}}}\right)$$
(1)

137 where $\alpha_{PO_4^{3-}}$, $\alpha_{OH^{-}}$ and, $\alpha_{Ca^{2+}}$ are activities of PO₄³⁻, OH⁻ and Ca²⁺, respectively. 138 K_{sp, Ca₅(PO₄)₃OH_(s) is the solubility product of hydroxyapatite (10^{-44.33}). Equilibrium 139 calculations and stability constants were from the Visual MINTEQ software database.⁶⁰}

The precipitation experiments with $CaSO_{4(s)}$ and $CaCO_{3(s)}$ were performed similarly to that of $Ca_5(PO_4)_3(OH)_{(s)}$, except that phosphate was replaced by sulfate and carbonate salt, respectively. The saturation index was controlled between 0.2 to 1.2 for $CaSO_{4(s)}$. The saturation index for $CaCO_{3(s)}$ was varied between 1.3 and 1.8 by adjusting the alkalinity from 10 to 36 mM as carbonate. The saturation index of each solid is defined as:

$$SI_{CaSO_4} = \log\left(\frac{\alpha_{Ca^{2+}} \times \alpha_{SO_4}^{2-}}{K_{sp, CaSO_{4(s)}}}\right)$$
(2)

$$SI_{CaCO_3} = \log\left(\frac{\alpha_{Ca^{2+}} \times \alpha_{CO_3^{2-}}}{K_{sp, CaCO_{3(s)}}}\right)$$
(3)

145 Where $\alpha_{SO_4^2-}$, $\alpha_{CO_3^2-}$ and $\alpha_{Ca^{2+}}$ are the activities of SO_4^{2-} , CO_3^{2-} and Ca^{2+} , respectively, 146 while $K_{sp, CaSO_4}$ and $K_{sp, CaCO_3}$ are the solubility products of calcium sulfate and calcium 147 carbonate, respectively ($K_{sp, CaSO_4} = 10^{-4.61}$, $K_{sp, CaCO_3} = 10^{-8.48}$).⁶¹

148 After the mixing of respective solutions, precipitation experiments were conducted in a 149 250 mL batch reactor completely mixed at 400 rpm with a magnetic stir bar. The solid 150 precipitation kinetics were monitored by measuring the change of turbidity at pre-151 determined time intervals using a HACH 2100N turbidimeter. The suspension pH was 152 maintained at 7.8 ± 0.05 with a requisite amount of tris(hydroxymethyl)aminomethane 153 (TRIS) buffer. The presence of TRIS buffer has a negligible impact on the calcium 154 precipitation reaction (Figure S2). The rate of precipitation was calculated by fitting the 155 turbidity-time profile to a Michaelis-Menten type model.⁶² The rate model and the fitting 156 are described in Text S1 and Figure S3. The concentration of antiscalants was confirmed 157 by UV oxidation with H_2O_2 followed by analysis of phosphate using the standard molybdate blue spectrophotometric method.⁶³ Zeta potential of precipitated calcium solids 158 159 was measured using Zetasizer nano ZS90 analyzer (Malvern Panalytical, Inc.). The mineral 160 phases of precipitated solids were analyzed by X-ray diffraction (XRD) and three calcium 161 solids were confirmed (Figure S4).

162 **Results and discussions**

163 Effect of antiscalant type on the precipitation of calcium solids

Figure 1A shows the kinetics of hydroxyapatite precipitation reactions in the presence of three antiscalants. The precipitation kinetics on the basis of the solution turbidity exhibited three distinct phases: an initial lag phase, a rapid precipitation phase and a final equilibrium phase. During the lag stage, hydroxyapatite nuclei underwent a constant formation and dissolution until a critical radius (denoted as $r_{critical}$) was achieved. This initial phase was followed by a rapid precipitation phase where crystals grew quickly until reaching equilibrium and becoming stationary in the end.

In the presence of 1 μ M NTMP, EDTMP or DTPMP, the induction time for hydroxyapatite precipitation to occur ranged between 1 and 5 minutes (Figure 1A). Phosphonate antiscalants can adsorb onto the incipient nuclei generated during the induction period, resulting in a distortion of crystal growth pattern and a delay of nucleation.⁶⁴⁻⁶⁶ Antiscalants can also act as an impurity on the surface of a growing crystal, which slows down its further growth. The presence of antiscalants can increase the surface energy of the growing crystals, which decreases the rate of nucleation and increases the induction time.⁶⁷

The induction time of hydroxyapatite precipitation without an antiscalant was only a few seconds. It significantly increased in the presence of an antiscalant compared to the control (Figure 1A). Calculations showed that a majority of calcium under the brine chemical condition exists as the free ion form rather than aqueous calcium-antiscalant complexes in the presence of antiscalants (Text S2 and Figure S5), indicating that the inhibitive effect by antiscalants likely results from the adsorption of antiscalants onto the incipient nuclei of hydroxyapatite.

In addition, the effectiveness of antiscalant in extending the induction time followed the
order of DTPMP > EDTMP > NTMP (solid lines in Figure 1B). The longer induction time

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187 of hydroxyapatite nucleation in the presence of DTPMP compared to NTMP or EDTMP 188 is likely contributed by two factors. First, antiscalants differ from each other in the number 189 of amine functional groups in their backbone structure and the number of phosphonate 190 groups (Figure S1). High-molecular-weight antiscalants with a larger number of amine 191 groups (e.g., DTPMP) have a bigger molecular structure compared to the relatively low-192 molecular-weight antiscalants (e.g., NTMP). When antiscalants adsorb on the incipient 193 hydroxyapatite nuclei, the high-molecular-weight DTPMP molecules occupy a larger 194 surface area of the nuclei structure, thus extending the induction time considerably.^{31,68}

195 Second, different antiscalants possess different surface charges. Calculations showed that 196 DTPMP is the most negatively charged molecule among the three antiscalants (Text S3 197 and Figure S6). Meanwhile, the point of zero charge for hydroxyapatite in the brine 198 solution was measured as 8.21 (Figure S7A), consistent with prior literature.^{69,70} At pH 7.8, 199 the surface of hydroxyapatite nuclei is positively charged and promotes the electrostatic 200 adsorption of DTPMP. Consequently, it enhanced the effectiveness of DTPMP in delaying 201 the induction time. Experimental data also confirmed that the surface charge of 202 hydroxyapatite was reduced upon DTPMP adsorption (Figure S7B).

The mechanism of antiscalant inhibition on hydroxyapatite nucleation was further investigated by quantifying the steady-state nucleation rates, which is calculated as:

$$J_{\rm s} = F \times \exp\left(\frac{-\beta \gamma_{\rm s}^3 N_{\rm A} f(\theta)}{(RT)^3 {\rm SI}^2}\right) \tag{4}$$

where *F* is the pre-exponential factor and has a theoretical value of 10^{33} nuclei·L⁻³·s⁻¹, β is the shape factor (16 $\pi/3$ for spherical nuclei), γ_s is the surface energy of crystallization 207 (J/m²), N_A is the Avogadro's number (mol⁻¹), $f(\theta)$ is the correction factor (value=1 for 208 homogeneous nucleation),⁵⁸ *R* is the gas constant (8.3 J·mol⁻¹·K⁻¹), *T* is the absolute 209 temperature (K), and SI is the saturation index. Results showed that the nucleation rate 210 dropped with an increasing antiscalant dosage (dashed lines in Figure 1B). This trend is 211 also consistent with the extension of induction time (solid lines Figure 1B). A decrease in 212 the nucleation rate consequentially increases the time required for the crystal to grow and 213 delays the onset of precipitation.

214 Furthermore, with the same saturation index of hydroxyapatite, the induction time 215 increased with the antiscalant dosage (Figure 2A). For instance, an increase of EDTMP 216 dosage from 0.5 to 3 µM increased the duration of induction time from 1.5 to 5 minutes. 217 thus delaying the onset of homogeneous crystallization. A higher antiscalant concentration 218 in the solution resulted in a higher surface adsorption of the nuclei and less surface area 219 was available for the nucleation to take place. In addition, the effects of antiscalant on the 220 induction time also depends on the extent of calcium supersaturation. For example, a higher 221 saturation index of hydroxyapatite reduced the induction time at the same dosage of 222 EDTMP (Figure 2B).

Typically, as the dosage of antiscalant increased, it became more effective in delaying the onset of hydroxyapatite precipitation with a more oversaturated solution, as shown by the extension of induction time with an increasing antiscalant dosage at a fixed saturation index (Figure 3). Furthermore, the three antiscalants exhibited different effectiveness in delaying hydroxyapatite precipitation, which is evaluated based on the critical saturation index (CSI). For a given antiscalant dosage, CSI is defined as the maximum saturation index below which a decrease in the saturation index shows a significant increase in the induction 230 time. This was quantified by measuring the slope of induction time vs. the saturation index 231 (Figure 3) and the CSI was the saturation index below which the average slope shows more 232 than 40% change compared to its previous value. A higher CSI suggests a stronger 233 inhibiting effect by antiscalant in precipitation. For example, at a dosage of 0.5μ M, NTMP 234 only became effective in delaying hydroxyapatite precipitation at a saturation index less 235 than 14.40 (Figure 3A), whereas EDTMP became effective with a saturation index less 236 than 14.55 (Figure 3B), and DTPMP was effective when saturation index was below 14.69 237 (Figure 3C). A similar trend was also observed for $CaSO_{4(s)}$ and $CaCO_{3(s)}$ precipitation, 238 respectively (Figure S8). These critical saturation indices are significant in defining the 239 inhibitive effects of antiscalants on scale formation in desalination concentrate. These 240 trends are also consistent with the observation that inhibition effects on calcium solids 241 precipitation follow the order of DTPMP > EDTMP > NTMP.

242 Thermodynamics of calcium crystallization in the presence of antiscalants

According to the theory of homogenous nucleation, the duration of induction time is intrinsically associated with the thermodynamics of nucleation reaction and crystal growth process. Specifically, the logarithm of induction time is linearly related to the square root of the saturation index of the corresponding solid as described in the equation below:^{71,72}

$$\log(t_{\rm ind}) = A T^{-3}(SI)^{-2} + B \tag{5}$$

where t_{ind} is the induction time (second), *T* is the solution temperature (Kelvin), SI is the saturation index of the solution with respect to a calcium-containing solid (dimensionless), and both *A* and *B* are fitting parameters. This linear relationship was observed during the precipitation of Ca₅(PO₄)₃OH_(s), CaCO_{3(s)} and CaSO_{4(s)} (Figure S9).

- 251 The surface energy of crystallization, γ_s (J/m²), was calculated using the equation 6 below
- using the value of *A* obtained from equation 5:

$$\gamma_{\rm s} = \left(\frac{A \left(2.3R\right)^3}{\beta V_{\rm m}^2 N_{\rm A} f(\theta)}\right)^{1/3} \tag{6}$$

where β is the geometry factor and has a value of $16\pi/3$ for a spherical nucleus, $V_{\rm m}$ is the molecular volume of the crystal (1.2×10^{-28} m³/molecule for gypsum,⁷³ 6.1×10^{-29} m³/molecule for vaterite,⁷⁴ and 2.6×10^{-28} m³/molecule for hydroxyapatite^{75,76}).

The Gibbs free energy of homogenous nucleation with respect to the radius of the nucleus is calculated as:⁷⁷⁻⁷⁹

$$\Delta G = -\frac{4\pi r^3 k T(\mathrm{SI})}{3V_{\mathrm{m}}} + 4\pi r^2 \gamma \tag{7}$$

where *k* is the Boltzmann constant $(1.38 \times 10^{-23} \text{ J} \cdot \text{K}^{-1})$. The first term in Equation 7 represents the change in the bulk free energy. The second term is the change in the surface free energy that results from the formation of new interface between the new nuclei and the aqueous phase.

When the Gibbs free energy of nucleation reaches a maximum, the radius of the nucleus is defined as the critical radius of nucleation ($r_{critical}$), and the corresponding Gibbs free energy is defined as the activation energy of nucleation ($\Delta G_{critical}$). $r_{critical}$ is the minimal radius of the nucleus that is required for the initiation of crystal growth and precipitation. A typical calculated trend of the nucleation process is shown in Figure 4A. For Equation 7, when r $r_{critical}$, ($d\Delta G/dr$) = 0. Therefore,

$$r_{\rm critical} = \frac{2\gamma V_{\rm m}}{kT({\rm SI})} \tag{8}$$

Accordingly, a combination of Equations 7 and 8 results in the following expression:

$$\Delta G_{\rm critical} = \frac{16\pi\gamma^3 V_{\rm m}^2}{3\,k^2 T^2 {\rm SI}^2} \tag{9}$$

Calculations show that values of $\Delta G_{\text{critical}}$ and r_{critical} decreased with an increase in saturation index (Figures S10-S11). A higher oversaturation level increases the probability of collisions between nuclei, and exerts a stronger driving force for nucleation, therefore decreasing the requirement on the size of subcritical nuclei reaching the r_{critical} .

273 To understand the effect of antiscalants on the precipitation thermodynamics, the effect of 274 antiscalant dosage on the activation energy of calcium solid nucleation was investigated. 275 Figure 4B shows a plot of relative changes in activation energy of nucleation ($\Delta G_{\text{critical}}$) as 276 a function of EDTMP dosage for different calcium solids. $CaCO_{3(s)}$ and $CaSO_{4(s)}$ showed 277 a linear increase in the activation energy with an increasing EDTMP dosage. 278 $Ca_5(PO_4)_3OH_{(s)}$, however, only showed a similar trend at a low EDTMP dosage up to 1 279 μ M, and its activation energy decreased with a further increase in the EDTMP dosage from 280 $1 \mu M$ to $4 \mu M$ (open circles, Figure 4B).

The decrease in the activation energy of nucleation of $Ca_5(PO_4)_3OH_{(s)}$ at higher EDTMP dosages can be attributed to a transition from homogenous to heterogeneous nucleation. Plotting the log of induction time of hydroxyapatite in presence of EDTMP against the saturation ratio exhibited two distinct linear correlations (Figure S9A), suggesting a transition from homogenous to heterogenous nucleation when the saturation index 286 decrease. This effect was only observed with lower saturation indices and higher 287 antiscalant dosages. Similar findings were reported for the precipitation of calcium solids 288 changing from homogeneous to heterogenous nucleation at lower saturation indices.⁷² The 289 heterogeneous nucleation can take place due to the presence of freshly formed 290 hydroxyapatite acting as seeds for nucleation.⁸⁰ The free energy barrier is smaller for 291 heterogeneous nucleation compared to that for homogeneous nucleation.⁸¹ Thus, to 292 calculate the homogeneous activation energy of hydroxyapatite nucleation the results with 293 higher antiscalant dosage and lower saturation indices conditions were discarded. The 294 recalculated results showed a linear increase with EDTMP dosage (closed circles, Figure 295 4B).

296 Effect of antiscalant on the kinetics of calcium solids precipitation

The rate of hydroxyapatite precipitation depended on the antiscalant dosage and the saturation index (Figure 5). In general, at a fixed level of oversaturation, the rate of precipitation decreased with an increasing antiscalant dosage. Meanwhile, the rate of precipitation increased with a higher saturation index for any given antiscalant dosage.

301 In addition, different antiscalants exhibited distinct dosage-response behaviors on the 302 precipitation rate. For example, NTMP showed a very strong dosage effect that highly 303 depends on the level of oversaturation (Figure 5A). At a fixed NTMP dosage, as the 304 saturation index increased beyond a critical value, the precipitation rate increased 305 significantly. On the contrary, the dosage effect of EDTMP on the precipitation rate was 306 moderate (Figure 5B), and that of DTPMP was insensitive to the saturation index (Figure 307 5C). The use of EDTMP or DTPMP at a low dosage of 0.5 μ M is as effective as higher 308 dosages in slowing down the precipitation kinetics regardless of calcium saturation, but 309 NTMP at 0.5 µM was only effective at a low calcium saturation level. These trends suggest 310 that EDTMP and DTPMP are more effective than NTMP in suppressing the rate of 311 hydroxyapatite precipitation. This difference likely resulted from a higher surface blockage 312 of nuclei by the larger antiscalant molecules of EDTMP and DTPMP, and the consequently 313 stronger inhibitive effects on the growth of calcium crystals.

314 Conclusion

315 These findings show that although all three of the antiscalants considered have active 316 phosphonate functional groups, they affect the precipitation kinetics of calcium solids 317 differently. Antiscalants are only effective in temporarily stabilizing the oversaturated 318 desalination brine and delay the scale-forming substances (in this case, calcium solids) 319 from precipitation. Results from this study established a quantitative relationship between 320 the nucleation rate of three most commonly observed calcium-scaling solids and three most 321 widely used antiscalants. Accordingly, it provided guidance on the threshold dosage of 322 these antiscalants that can hold a certain duration of time to prevent the oversaturated brine 323 waste from scale formation. Furthermore, with an ever-increasing dependence on 324 desalination, especially in inland areas, and more desalination facilities targeting a near 325 zero liquid discharge, brine demineralization (*i.e.*, TDS removal) is the key to increasing 326 water recovery and managing the concentrate waste. The modeling of precipitation rates 327 from this study provided crucial information on the relationships among the rate of 328 precipitation, the antiscalant dosage, and the critical saturation index; together these can 329 help to determine the targeted amount of antiscalant that needs to be removed to achieve a 330 high rate of demineralization. The optimization of an efficient demineralization technique 331 is crucial and will be further investigated in the future.

332 Acknowledgement

333 This research was supported by grants to H.L. from the National Science Foundation

334 (Grant #1611306) and to T.J. from the National Water Research Institute. We thank the

assistance of John Orta at UCR, Jesus Trujillo from San Bernardino Middle College High

336 School and Osvaldo Mireles from San Bernardino Valley College on participation.

337 Supporting Information Section

Additional description of molecular structures of the antiscalants, calculation procedure for kinetic modeling, XRD spectra, free calcium ion calculations in each antiscalant system and antiscalant molecular charge calculations, figures on induction time and activation energy dependence on antiscalant concentration and saturation index are available in the SI section.





Figure 1 (A) Comparison among three antiscalants on their effects on the kinetics of hydroxyapatite precipitation. $[Ca^{2+}] = 10 \text{ mM}; [PO_4^{3-}] = 26 \text{ mg P/L};$ saturation index = 346 347 14.2; [antiscalant] = 1 μ M. pH = 7.8; ionic strength = 100 mM; [TRIS buffer] = 20 mM. 348 (B) Impact of different antiscalant dosage on the induction time (solid lines) and the nucleation rate (dashed lines) of hydroxyapatite. $[Ca^{2+}] = 10 \text{ mM}; [PO_4^{3-}] = 30 \text{ mg P/L};$ 349 350 saturation index = 14.6; pH = 7.8; ionic strength = 100 mM; [TRIS buffer] = 20 mM.





Figure 2 The effects of EDTMP dosage and saturation index on induction time of precipitation of hydroxyapatite. (A) $[Ca^{2+}] = 10 \text{ mM}; [PO_4^{3-}] = 26 \text{ mg P/L};$ saturation index = 14.2; EDTMP = 0-3 μ M; pH = 7.8; ionic strength = 100 mM; [TRIS buffer] = 20 mM. (B) $[Ca^{2+}] = 10 \text{ mM}; [PO_4^{3-}] = 22-25 \text{ mg P/L};$ EDTMP = 2 μ M; pH = 7.8; ionic strength = 100 mM; [TRIS buffer] = 20 mM.

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Figure 3 The effect of antiscalant dosage on induction time of precipitation of hydroxyapatite. (A) $[Ca^{2+}] = 10 \text{ mM}$; $[PO_4^{3-}] = 17-34 \text{ mg-P/L}$; saturation index = 14.1-14.9; pH = 7.8; ionic strength = 100 mM; [TRIS buffer] = 20 mM. (B) $[Ca^{2+}] = 10 \text{ mM}$;

363 $[PO_4^{3-}] = 22-31 \text{ mg-P/L}$; saturation index = 14.3-14.8; pH = 7.8; ionic strength = 100 mM;

364 [TRIS buffer] = 20 mM. (C) $[Ca^{2+}] = 10$ mM; $[PO_4^{3-}] = 24-35$ mg P/L; saturation index =

365 14.5-14.9; pH = 7.8; ionic strength = 100 mM; [TRIS buffer] = 20 mM.



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368 Figure 4 (A) Gibbs free energy for homogeneous nucleation of $CaSO_{4(s)}$ at varying NTMP dosages. $[Ca^{2+}] = 37 \text{ mM}; [SO_4^{2-}] = 564 \text{ mM};$ Saturation index = 0.84; pH = 7.8. (B) Impact 369 370 of EDTMP dose on activation energy of different calcium solids; Experimental conditions for CaCO_{3(s)}: $[Ca^{2+}] = 10 \text{ mM}$; $[CO_3^{2-}] = 10 \text{ mM}$; $[EDTMP] = 0-21 \mu M$; saturation index 371 = 1.32; pH = 7.8; ionic strength = 100 mM; [TRIS buffer] = 50 mM; Experimental 372 373 conditions for CaSO_{4(s)}: $[Ca^{2+}] = 37 \text{ mM}$; $[SO_4^{2-}] = 564 \text{ mM}$; $[EDTMP] = 0.21 \mu \text{M}$; 374 saturation index = 7; pH = 7.8; ionic strength = 1M. Experimental conditions for 375 Ca₅(PO₄)₃OH_(s): homogeneous nucleation (closed circles), heterogeneous nucleation (open 376 circles); $[Ca^{2+}] = 10 \text{ mM}$; $[PO_4^{3-}] = 0.6 \text{ mM}$; $[EDTMP] = 0.4 \mu \text{M}$; saturation index = 14.2; 377 pH = 7.8; ionic strength = 100 mM; [TRIS buffer] = 20 mM.







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