

**A Computational Survey of Semiconductors for Power Electronics**

Journal:	<i>Energy & Environmental Science</i>
Manuscript ID	EE-ART-05-2019-001529.R1
Article Type:	Paper
Date Submitted by the Author:	23-Jul-2019
Complete List of Authors:	Gorai, Prashun; Colorado School of Mines; National Renewable Energy Laboratory, McKinney, Robert ; Colorado School of Mines Haegel, Nancy; National Renewable Energy Laboratory Zakutayev, Andriy; National Renewable Energy Laboratory; Colorado School of Mines Stevanovic, Vladan; Colorado School of Mines; National Renewable Energy Laboratory



A Computational Survey of Semiconductors for Power Electronics[†]

Prashun Gorai,^{a,b,c} Robert W. McKinney,^a Nancy M. Haegel,^b Andriy Zakutayev,^{a,b,c} and Vladan Stevanovic^{a,b,c}

Received 00th January 20xx,
Accepted 00th January 20xx

DOI: 10.1039/x0xx00000x

www.rsc.org/

Power electronics (PE) are used to control and convert electrical energy in a wide range of applications from consumer products to large-scale industrial equipment. While Si-based power devices account for the vast majority of the market, wide band gap semiconductors such as SiC, GaN, and Ga₂O₃ are starting to gain ground. However, these emerging materials face challenges due to either non-negligible defect densities, high synthesis and processing costs, or poor thermal properties. Here, we report on a broad computational survey aimed to identify promising materials for future power electronic devices beyond SiC, GaN, and Ga₂O₃. We consider 863 oxides, sulfides, nitrides, carbides, silicides, and borides that exhibit finite calculated band gaps. We utilize *ab initio* methods in conjunction with models for intrinsic carrier mobility, and critical breakdown field to compute the widely used Baliga figure of merit. We also compute the lattice thermal conductivity and use it as an additional screening parameter. In addition to correctly identifying known PE materials, our survey has revealed a number of promising candidates exhibiting the desirable combination of high figure of merit and high lattice thermal conductivity, which we propose for further experimental investigations.

1. Introduction

Power electronics (PE) enable conversion and control of energy in a wide range of applications, including consumer products, electricity generation from wind and solar, electric vehicles, and long-distance communications. For instance, rectifiers used in mobile chargers, inverters and converters of electricity generated from solar and wind energy, and variable-frequency drives in electric vehicles and industrial motors all employ power electronics.^{1, 2} It is estimated that the global market for power electronics will swell to >\$50 billion by 2023.³ Despite their diverse applications, only a handful of materials, including Si, SiC, and GaN, account for the vast majority of the PE market.^{1, 2} Silicon is the incumbent material – cheap and compatible with existing fabrication technology but not efficient.⁴ In particular, silicon-based PE devices are not suitable for high-power applications because of a trade-off: low breakdown field at low on-state resistance, or high on-state resistance at high breakdown field.⁵ Low breakdown field limits the range of possible applications, and high on-state resistance reduces the efficiency of power conversion. Despite these drawbacks, Si presently constitutes ~95% of the PE devices.⁴ SiC and GaN address this trade off but their non-negligible defect densities and high synthesis costs have been a limiting factor for large-scale applications. More recently, Ga₂O₃ has emerged as a low-cost^{6, 7} alternative, but its poor thermal properties have been a critical impediment.⁸ Materials such as diamond-C⁹, cubic-BN¹⁰, AlN¹¹, ZnO¹¹ have also been considered,

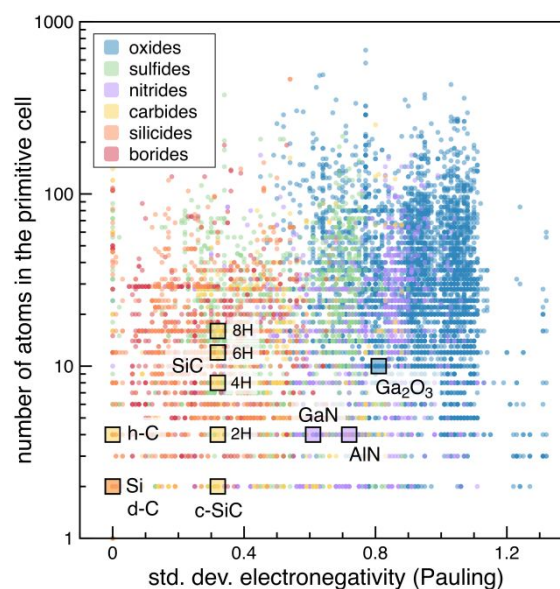


Fig. 1 Stoichiometric and ordered structures (10,600) from the ICSD, comprising oxides, sulphides, nitrides, carbides, silicides, and borides, are represented by the number of atoms in the primitive cell and the standard deviation in Pauling electronegativity of the constituent elements. Si, SiC, GaN, and Ga₂O₃ are prominent power electronic (PE) materials while diamond-C and AlN have been considered in lab-scale studies. For SiC, 2H-8H denote polytypes.

but power electronic devices based on these compounds either have not been attempted or have not reached their full potential. Some of these PE materials are highlighted in **Fig. 1**, in addition to 10,600 stoichiometric and ordered structures reported in the Inorganic Crystal Structure Database (ICSD) spanning oxide,

^a Colorado School of Mines, Golden, CO 80401, USA.

^b National Renewable Energy Laboratory, Golden, CO 80401, USA.

^c Email: pgorai@mines.edu, andriy.zakutayev@nrel.gov, vstevano@mines.edu

[†] Electronic Supplementary Information (ESI) available

sulphide, nitride, carbide, silicide, and boride chemistries. Presently employed PE materials constitute only a minuscule fraction of known materials, as illustrated in Fig. 1, which is the key reason to explore for alternatives beyond the handful of materials that dominate current power electronics.

One potential approach to such exploration is a broad computational search to identify novel materials for power electronics. Computations have proven to be a powerful tool in accelerating materials discovery beyond the conventional trial-and-error approach. With continued improvements in *ab initio* methods and software, and the rapid advances in computational resources, high-throughput (HT) computations have become a viable tool to explore large material spaces and identify promising candidates.¹² Such HT computational approaches rely on material descriptors and/or figures of merit that can be rapidly determined from first-principles calculations and from simplified models.^{12, 13} To expedite searches, often various approximations are employed without overly sacrificing accuracy. Assumptions such as those related to material dopability *i.e.* whether a semiconductor can be doped with a desired charge carrier type and concentration, may also be needed for computational tractability. In spite of the assumptions and approximations, HT computations have been quite successful in unravelling novel materials for solid-state batteries^{14, 15}, thermoelectrics^{13, 16}, photovoltaics^{14, 17} etc. The deployment of HT computations in materials discovery has also popularized the public sharing of data and development of open-access materials databases,¹⁸⁻²¹ including properties necessary to enable materials discovery for a wide variety of applications. In spite of the promise of computations, surprisingly, no such efforts exist within power electronics.

Here, we computationally screen materials from the ICSD and compute the Baliga figure of merit (FOM) of 863 materials with finite calculated band gaps. Since the Baliga FOM does not account for heat dissipation as a performance factor, we also explicitly calculate the lattice thermal conductivity (κ_L) as a screening parameter in our search. As such, we focus on the performance of the pristine material that depends on the intrinsic properties; extrinsic factors such as doping would have to be appropriately tuned for the most promising candidates that are identified from the screening. To compute the parameters that determine the Baliga FOM and lattice thermal conductivity, we utilized *ab initio* methods in conjunction with semi-empirical models of transport properties and phenomenological model of critical breakdown field. Our computational search has revealed several promising candidates that exhibit the desirable combination of high figure of merit and high lattice thermal conductivity. Candidates include 9 oxides, 4 nitrides, and 3 carbides with *n*-type Baliga FOMs and lattice thermal conductivities larger than that of Ga₂O₃. We propose the identified materials as candidates for further experimental and computational investigations.

2. Figures of Merit

Figures of merit have been derived for thermoelectrics,¹⁶ topological insulators,²² photovoltaics,¹⁷ power electronics²³ etc. As mentioned in the Introduction, FOMs can serve as practical material

descriptors in HT computational searches, provided that the input material parameters can be rapidly and reliably determined with computational methods and models. In this section, we briefly review the desirable traits of materials for power electronics, the various FOMs that are cast in terms of the desirable properties, and the computational models to determine the input parameters.

2.1. Desirable Traits of Materials for Power Electronics

Most critically, the semiconductor must possess a large breakdown field (E_b), which depends on intrinsic as well as extrinsic factors.⁵ Typically, semiconductors with wide ($E_g > 3$ eV) to ultra-wide ($E_g > 5$ eV) band gaps, large dielectric constants ($\epsilon_{\text{static}} > 10$), and strong electron-phonon coupling (as described in the electron avalanche theory by Hippe²⁴, Frohlich²⁵) exhibit large intrinsic breakdown field. Next, the semiconductor must support large current densities (J), especially for high-power devices. Since J is directly proportional to the electrical conductivity $\sigma = \mu ne$ (where μ is the charge carrier mobility, n the concentration of charge carriers, and e the fundamental electronic charge), materials with high carrier mobilities and large carrier concentrations are desirable.⁴ While μ can be treated as an intrinsic material property, n is typically controlled by extrinsic doping. Finally, the material must efficiently dissipate the thermal energy produced by Joule heating in the device²⁶ – a high lattice thermal conductivity (κ_L) is, therefore, advantageous.

2.2. Power Electronic Figures of Merit

Several FOMs have been used to quantify the intrinsic performance of materials for power electronics, including those proposed by Johnson,²⁷ Baliga,^{23, 28} Kim,²⁹ and Huang.³⁰ These FOMs are generally applicable to unipolar switching power devices. Baliga proposed FOMs for low-frequency²³ and high-frequency²⁸ power electronic devices. The widely used low-frequency Baliga FOM (BFOM) is given by $\mathbf{BFOM} = \epsilon \mu E_b^3$. The BFOM is derived assuming that the power losses are solely due to power dissipation in the on-state of the device. Thus, the BFOM applies to materials operating at lower frequencies, where the conduction losses are dominant.²³ Given its widespread usage, we consider only the low-frequency BFOM for the computational search in this work.

Efficient thermal management *i.e.* heat dissipation, is necessary to avoid overheating and consequently, mechanical failure of the power electronic material and associated contacts and interfaces. The BFOM does not take into account the role of thermal conductivity that is critical for dissipation of Joule heating. In this study, we explicitly calculate the lattice thermal conductivity and consider it as one of the screening parameters along with the BFOM. Carrier concentrations in power electronic materials are generally low enough (non-degenerate) so the electronic component of thermal conductivity can be neglected.

2.3. Models for Evaluating FOM Parameters

To computationally evaluate the Baliga FOM of a material, we need to determine the dielectric constant, charge carrier mobility, and

the critical breakdown field. Dielectric constant (ϵ), including both ionic and electronic contributions, is calculated with first-principles density functional theory perturbation theory,⁵ as described in detail in the Methods section.

In doped semiconductors, depending on the temperature, both electron-phonon and ionized impurity scattering limit carrier mobility.³¹ Here, we focus on the intrinsic, phonon-limited carrier mobility because it represents the upper limit of mobility. The intrinsic mobility (μ) can be directly calculated with *ab initio* methods by computing the electron-phonon coupling matrix.^{5, 32} However, these calculations are computationally intensive and have so far been demonstrated only for simple elemental and binary semiconductors.⁵ To circumvent the challenges associated with direct calculation of μ , we have previously developed a computationally-tractable, semi-empirical model of μ by combining measured room-temperature μ and density functional theory (DFT) calculations for a range of materials.¹⁶ Motivated by the relationships describing electron-phonon scattering in band conductors, the charge carrier mobility is modelled as:

$$\mu = AB^s(m_b^*)^{-t} \quad (1)$$

where B is the bulk modulus, m_b^* the band effective mass, and A , s , and t are fitted constants. To compute the electron and hole mobilities using the semi-empirical model (Eq. 1), one needs to compute B , and m_b^* of conduction (electron) and valence (hole) bands. m_b^* is obtained from the density-of-states (DOS) effective mass (m_{DOS}^*) and band degeneracy (N_b) as $m_{DOS}^* = N_b^{2/3} m_b^*$, assuming parabolic carrier pockets and isotropic transport. B is determined by fitting the Birch-Murnaghan equation of state to a set of energies and volumes computed with DFT.^{33, 34} We have demonstrated that this model predicts the room temperature μ within half an order of magnitude of the measured values.¹⁶ Knowing that even measured μ can exhibit orders of magnitude variations depending on the synthesis conditions and sample preparation, the prediction accuracy of the semi-empirical model is acceptable for rapid screening of intrinsic properties of large number of materials.

We also need to evaluate the critical breakdown field (E_b) to determine BFOM. Like μ , it is possible to directly compute E_b with *ab initio* methods but this involves the computationally intensive calculations of electron-phonon coupling matrices,⁵ which makes it computationally intractable for broad searches. Empirical models that solely depend on the band gap of the material have been developed to estimate E_b .^{35, 36} These empirical models were fitted to a small number of materials belonging to specific material families; extrapolation to other materials may not be as accurate. A more general and accurate phenomenological model of E_b has been recently proposed by fitting material parameters such as band gaps and phonon frequencies to critical breakdown fields calculated from fully *ab initio* calculations.^{5, 32} The fitted model for E_b is:

$$E_b = 24.442 \exp(0.315 \sqrt{E_g \omega_{max}}) \quad (2)$$

where, E_g is the band gap in eV, ω_{max} is the phonon cutoff frequency in THz, and E_b is the breakdown field in MV/m. The band gap is related to the electronic excitations and the cutoff frequency to the scattering of excited electrons by phonons. E_g is calculated with DFT-GGA functional and generally underestimated (see Methods for computational details). Here, the cut off frequency ω_{max} is taken as the frequency of the highest optical mode at Γ (see Methods for details). It must be noted that both the empirical and phenomenological models of E_b ignore the effects of impurity doping that can lower the breakdown field. Here, we focus on evaluating the performance of the intrinsic material. As is typically done in broad computational searches, extrinsic factors can be assessed in detail on a case-by-case basis *via* follow-up computational and experimental investigations.

We estimated the lattice thermal conductivity (κ_L) with a computationally tractable semi-empirical model that we have previously developed,³⁷ and is expressed as

$$\kappa_L = A_1 \frac{M v_s^\gamma}{T \gamma^2 V^z n^x} + A_2 \frac{v_s}{V^z} \left(1 - \frac{1}{n^{2/3}} \right) \quad (3)$$

where, M is the average atomic mass, v_s is the speed of sound, V is the volume per atom, n is the number of atoms in the primitive cell, γ is the Gruneisen parameter, T is the temperature, and A_1 , A_2 , x , y , and z are fitted parameters. The speed of sound is approximated from the bulk modulus (B) and the density (d), as $v_s \cong \sqrt{B/d}$. This model predicts κ_L within an average factor of 1.5 of the experimental value, over 4 orders of magnitude in κ_L .³⁷

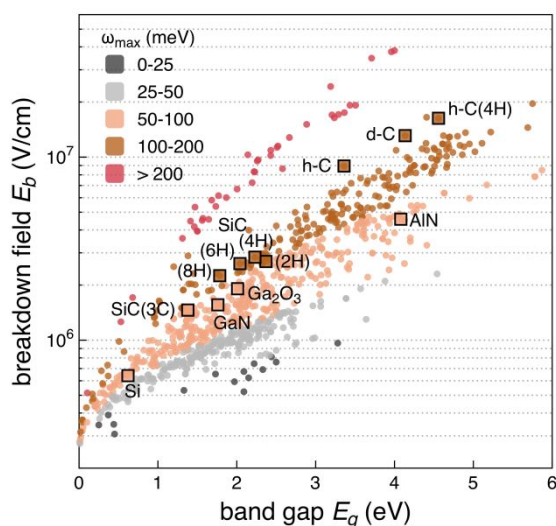


Fig. 2. Critical breakdown field (E_b) of 863 materials calculated with a phenomenological model, given by Eq. (2). In this model, E_b depends on the band gap E_g (x-axis) and the phonon cutoff frequency ω_{max} (color). E_b strongly depends on both E_g and ω_{max} . Known power electronic materials are labelled for reference. Marker labels: d-C = diamond-C, h-C = lonsdaleite C, SiC(3C) = cubic SiC. Symbols within parenthesis denote the polytype.

3. Results

We performed the computational search among materials documented in the Inorganic Crystal Structure Database (ICSD). In this search, we considered only stoichiometric, and ordered compounds with less than 50 atoms in the unit cell. Additionally, we limited the search to oxides, sulphides, nitrides, carbides, silicides, and borides for the following reasons: (1) known power electronic materials (Fig. 1) span these chemistries, and (2) they are generally expected to exhibit larger band gaps and higher lattice thermal conductivities compared to other pnictides (P, As, Sb, Bi), and chalcogenides (Se, Te). Even though halides are typically wide band gap materials, doping is known to be quite challenging. For this reason, we excluded halides from this search. Compounds containing transition metals (except Sc, Y, Ti, Zr, Hf, Cu, Zn, Cd, Ag, Au, Hg) are also not included in this search – the ground-state structure of these materials may be magnetic *i.e.* exhibit magnetic ordering. At typical operational temperatures, magnetic disorder can deteriorate carrier transport,³⁸ which is detrimental for power electronic applications.

Based on these restrictions, in total we considered 863 materials from the ICSD that have finite DFT-calculated band gaps in their lowest-energy crystal structures (based on total energies reported in NREL Materials Database, materials.nrel.gov). For some compounds, we found that the DFT-calculated total energies to be equal in two different structures. In such cases, we considered both structures in our search. Note that the well-known underestimation of band gaps in DFT-based methods can lead to erroneous closing of band gap. However, this does not pose significant problems here because it usually occurs in relatively small band gap materials, typically with $E_g < 1$ eV, which are not of interest in this study. To be

clear, this analysis does not include stability against decomposition

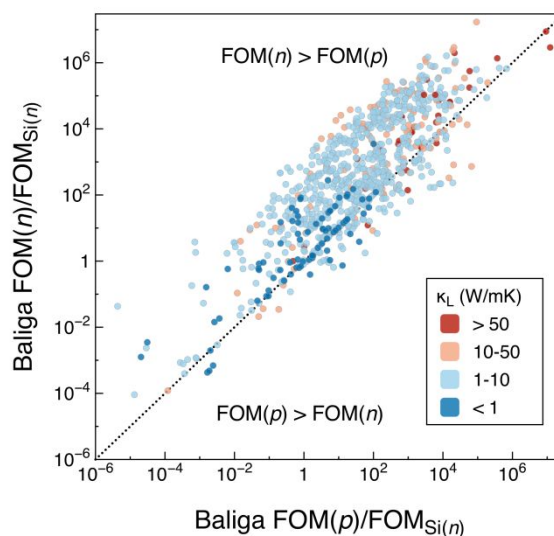


Fig. 3. A comparison of the computed Baliga figure of merit (FOM) of 863 materials, assuming the materials are doped n -type (y-axis) and p -type (x-axis). The Baliga FOMs are normalized with the FOM of n -type Si, a widely used power electronic material. Marker colours denote the lattice thermal conductivity. Materials in the upper (lower) triangle *i.e.* above (below) the $y = x$ line, have higher n -type (p -type) Baliga FOM. For most materials considered in this study, the n -type FOM is higher because electron mobilities are generally higher than hole mobilities.

into competing phases, but such decomposition can be avoided because the materials are reported in ICSD (mostly experimental). The complete list of the 863 materials along with their computed properties and BFOM are provided in the electronic supplementary information.

3.1 Trends in Figure of Merit and Material Properties

The performance of power electronic materials, as quantified by the figure of merit, depends on several inter-dependent material properties. It is, therefore, instructive to examine the trends in these material properties to understand the composition-property-performance relations.

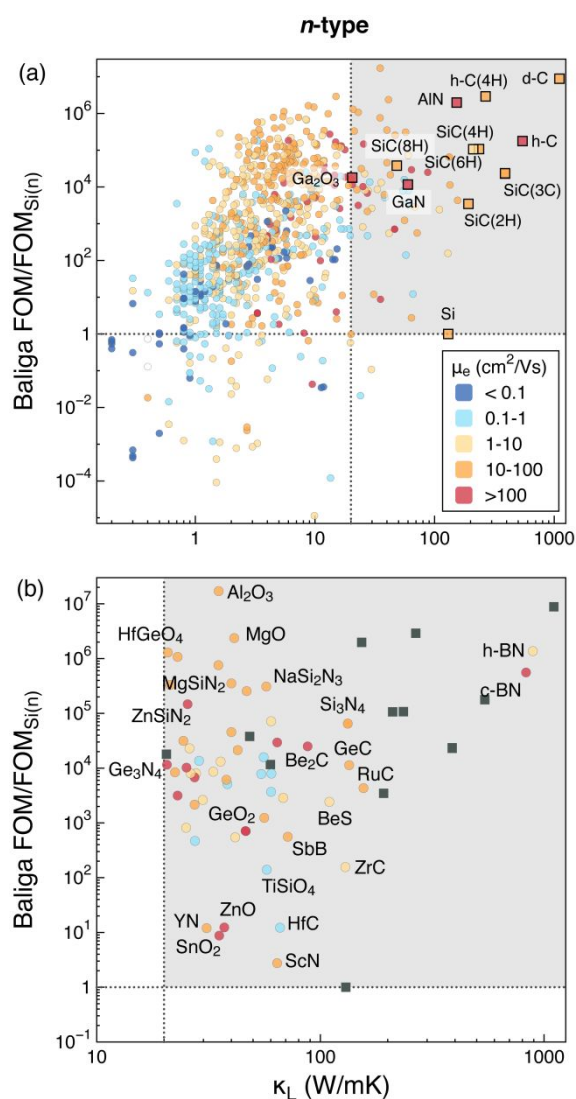


Fig. 4 (a) Calculated Baliga figure of merit (normalized with the FOM of *n*-type Si) of 863 materials shown in relation to the computed lattice thermal conductivity (κ_L) and assumed to be doped *n*-type. The colour schema represents the electron mobility. Known power electronic materials, bounded by the grey shaded region, are labelled for reference. (b) Zoomed-in view of the shaded region. A selected list of candidate materials is labelled. Known power electronic materials are marked by grey squares. Marker labels: d-C = diamond-C, h-C = lonsdaleite C, h-BN = hexagonal BN, c-BN = cubic BN, SiC(3C) = cubic SiC. Symbols within parenthesis denote the polytype.

The calculated critical breakdown fields (E_b) as a function of band gap (E_g) of the 863 materials are shown in Fig. 2. Known power electronic materials such as diamond-C, Si, SiC, GaN, and Ga₂O₃ are marked for reference. The predicted E_b are in fairly good agreement with experimentally measured values. For instance, calculated E_b for diamond-C is 1.3×10^7 V/cm; in comparison, the measured value⁹ is 1.3×10^7 V/cm. The calculated E_b of Si is 6.4×10^5 V/cm, which is in good agreement with the upper bound of measured E_b (6×10^5 V/cm).³² The computed E_b shown in Fig. 2 span 2.5 orders of magnitude (~ 0.2 - 250×10^6 V/cm). While previous empirical models of E_b depend solely on the band gap, the

phenomenological model³² used here provides additional nuance by including features of the phonon dispersion, through the cutoff frequency (ω_{max}). While E_b still correlates with the band gap, the effect of the phonon frequency contribution is quite evident in Fig. 2. For a given band gap, E_b can vary over 1.5 orders of magnitude because of the differences in the cutoff frequency. Materials with $\omega_{max} > 200$ meV (48.4 THz), consisting of carbides and nitrides, exhibit unusually large breakdown fields. Since materials with higher cutoff frequency are expected to be stiffer, ω_{max} may be correlated to the bulk modulus (B).

In Fig. 3, the Baliga FOMs of the 863 materials are compared if the materials are doped *n*-type (*y*-axis) and *p*-type (*x*-axis). Whether a material can be actually doped with the desired charge carriers and to the necessary concentrations will depend on the defect and dopant formation energetics, as discussed in more detail in Section 4. We observe in Fig. 3 that more materials lie in the upper triangle above the dotted line (represents equal FOM of *n*- and *p*-type) – the Baliga FOM of most *n*-type doped materials is higher than that of *p*-type doped. The differences in *n*- and *p*-type Baliga FOM arise from the differences in electron and hole mobilities (ϵ , E_b are same for both doping types). Electron mobilities are generally higher than hole mobilities,^{16, 18} which result in higher *n*-type Baliga FOM for most materials.

Materials that lie on or near the dotted $y = x$ line in Fig. 3 and have high BFOM are particularly promising: (1) if a material is ambipolar *i.e.* can be doped both *n*- and *p*-type, junction devices can be fabricated with the same material, and (2) if the material is unipolar doped, *i.e.* only *n*- or *p*-type, it still leads to the identification of high-performing materials for specific doping types.

Commercially used power devices utilize *n*-type Si, SiC, and GaN.⁴ Therefore, it is useful to focus on *n*-type doped materials for future power electronics for two reasons: (1) they will likely exhibit a higher FOM compared to their *p*-type doped counterparts, and (2) provide replacement for the *n*-type material in existing power device architectures. In the following sections, we focus on materials assuming only *n*-type doping. We also identify and discuss some of the promising *p*-type candidates in Section 3.4.

3.2 Validation of Computational Approach

While the predicted breakdown fields (E_b) are in good agreement with measured values, we must also validate the computational approach by assessing if the computed FOMs correctly identify and appropriately rank the known power electronic materials. In Fig. 4(a), the *n*-type Baliga FOM, normalized by the FOM of *n*-type Si, is plotted as a function of the lattice thermal conductivity. The marker colours denote the intrinsic electron mobilities. For power electronics, materials with high FOM and high lattice thermal conductivity are desirable. Materials in the upper right quadrant of Fig. 4(a) exhibit these traits. We find that *all* known power electronic materials, that are either used in commercial devices (Si, SiC, GaN) or have been considered (Ga₂O₃, BN, AlN, ZnO), fall inside the shaded upper right quadrant in Fig. 4(a), which provides credence to the computational approach utilized in this work. The shaded region is extended in a way to include Si, which has the lowest normalized Baliga FOM of 1, and Ga₂O₃ with the lowest

lattice thermal conductivity of ~ 20 W/mK among the materials in this validation set.

Table 1 Computed and measured lattice thermal conductivity (κ_L) in W/mK and computed Baliga FOM of known power electronic materials. SG denotes the space group number. The Baliga FOM values are normalized by the Baliga FOM of *n*-type Si, a widely used power electronic material. Refs. a,³⁹ b,⁴⁰ c,⁴¹ d,⁴² e,⁴³ f.⁴⁴

Material	SG	κ_L (calc.)	κ_L (exp.)	FOM (<i>n</i>)	FOM (<i>p</i>)
Si	227	130	130 ^a	1×10^0	4.9×10^{-1}
4H-SiC	186	235	330 ^b	1.1×10^5	6.0×10^3
GaN	186	60	130 ^c	1.2×10^4	6.1×10^1
β -Ga ₂ O ₃	12	21	14 ^d	1.8×10^4	8.3×10^0
<i>d</i> -C	227	1106	1050 ^e	8.8×10^6	9.2×10^6
AlN	186	153	285 ^f	2.0×10^6	2.2×10^4

The computed FOM of known power electronic materials seem to capture the general performance expectations expressed in the experimental literature (Table 1). For instance, the FOMs of all other well-known power electronic materials are higher than that of Si. Diamond-C has the highest computed FOM as well as lattice thermal conductivity (Table 1). This material has been long recognized and pursued as one of the most promising power electronic materials⁹ but growth of large single crystals remains a major bottleneck. Both *n*- and *p*-type doping of diamond has been experimentally demonstrated in CVD-grown diamond thin films.⁴⁵ While *n*-type Ga₂O₃ has a similar or higher FOM compared to SiC and GaN, the lattice thermal conductivity is much lower, which is known to present challenges for thermal management of Ga₂O₃-based devices.⁷

Unlike thermoelectric materials,¹³ both high carrier mobilities and high lattice thermal conductivities are desirable for power electronics. In general, materials that exhibit high carrier mobilities tend to also have high lattice thermal conductivities.^{16, 18} Fig. 4(a) illustrates this trend – materials with high κ_L (on the right side) also generally have higher μ .

3.4 Emerging Candidates for Power Electronics

To identify promising *n*-type candidates, we focus on the materials that reside inside the shaded region in Fig. 4(a). In Fig. 4(b), we present a zoomed-in view of only the shaded region. For clarity, the known power electronic materials are shown in Fig. 4(b) as grey squares. We observe that there are a large number of materials with FOMs and lattice thermal conductivities that surpass those of Si, and even SiC, GaN, and Ga₂O₃. The top 30 *n*-type candidates identified from this search are listed in Table S1 in the descending order of their normalized *n*-type Baliga FOM, and the full list of screened materials and their properties is also provided in the ESI. The top candidates are dominated by oxides (14 out of 30) comprising primarily silicates and germanates, followed by carbides (9/30) and nitrides (7/30), with chemistries spanning binaries to quaternaries.

Oxides: Among the candidate binary oxides, ZnO has been extensively considered for various applications,⁴⁶ including photovoltaics, and transparent electronics (thin-film transistors).

ZnO is also an interesting material for high-temperature, high-power electronics.^{11, 47, 48} In particular, good *n*-type dopability and reasonable electron mobility of ZnO are favourable for power electronics, but its lack of stable *p*-type doping is less desirable compared to SiC and GaN, and the presently available single-crystal fabrication procedures⁴⁹ are more complicated than for Ga₂O₃.^{50, 51} Other binary oxides that emerge as candidate materials are MgO, CaO, and Al₂O₃, which are all insulators; MgO exhibits low hole conductivity only at elevated temperatures.⁵² Among the ternary oxides, IVA-IVB oxides such as HfGeO₄, HfSiO₄, and ZrGeO₄ are identified as promising candidates. Silicates with 2-2-7 chemistries (Y₂Si₂O₇, In₂Si₂O₇, Sc₂Si₂O₇) and their derivatives (CaZrSi₂O₇) are the other notable ternary oxide candidates. Both of these oxide classes are studied as scintillator host materials.^{53, 54} Ba₂ZrO₄, Al₂MgO₄, ZnSiO₃, and Al₄CaO₇ are the other oxides among the top 30 *n*-type candidates (Table S1). While we have identified a number of candidate oxides, we must be cognizant of the fact that extrinsic doping of wide-gap oxides is often challenging. It is possible that many of these candidate oxides are insulators and cannot be suitably doped to introduce sufficient charge carriers. The role of dopability of materials in realizing the predicted power electronic performance is discussed in more detail in Section 4.

Carbides: SiC derivatives – GeC and SnC, emerge as the most promising binary carbides, if they can be doped *n*-type. While GeC, that has been studied for tribological and mechanical coatings,⁵⁵ may not be an economically viable candidate due to the high cost of Ge, SnC is composed of earth-abundant elements. However, the breakdown field (E_b) of SnC is lower than SiC, primarily due to its smaller band gap. Other promising binary carbides include B₄C, Be₂C, and its ternary derivative BeB₂C. Both B₄C and Be₂C are known for their superior mechanical properties.^{56, 57} Interestingly, Sc₃C₄ is identified as a *p*-type candidate while Al₃C₄ as *n*-type; the Baliga FOM of *p*-type Sc₃C₄ is comparable to the best *n*-type candidates (Table S2). Among the best candidate ternary carbides are the two polymorphs of ScAl₃C₃, which are derivatives of their binary counterpart Al₄C₃.

Nitrides: Hexagonal and cubic BN have been previously considered as promising materials for high-power electronics,¹⁰ although not routinely discussed in the power electronics literature. We identify both polymorphs of BN as candidate materials in our search. Both polymorphs exhibit Baliga FOM higher than that of SiC, GaN, and Ga₂O₃. Fabrication of cubic-BN is known to be quite challenging because of the high synthesis temperatures and pressures;⁵⁸⁻⁶⁰ it is more practical to consider the ground-state hexagonal-BN as a candidate material for power electronics. The predicted breakdown fields of BN polymorphs are comparable to that of diamond-C and therefore, can be considered for high-performance applications. Spinel-type group IV nitrides, including the two polymorphs of Si₃N₄, and Ge₃N₄ are among the predicted candidate binary nitrides. Both Si₃N₄ and Ge₃N₄ have been previously investigated for application to light emitting diodes (LEDs)⁶¹ and photoelectrochemical water splitting.⁶² Ternary II-IV-N₂ materials related to III-N compounds, such as ZnGeN₂ and MgSiN₂ are identified as promising *n*-type candidates;⁶³ ZnGeN₂ is an emerging material for optoelectronic applications.⁶⁴ Other notable

candidates are silico-nitrides such as $\text{Ca}_2\text{Si}_5\text{N}_8$, which have also been studied for application in LEDs.⁶⁵

Decomposition into competing phases is an important consideration for material synthesis. To assess the stability of the candidate materials, we extracted the first-principles calculated stability and the energy above the convex hull (ΔE_{hull}) from the data available in computational databases, including the NREL Materials database (materials.nrel.gov) and the Materials Project database (materialsproject.org).¹⁹ ΔE_{hull} are reported in Tables S1 and S2 for the *n*- and *p*-type candidate materials, respectively. We find that out of the 30 candidate materials in Table S1, 5 carbides and 2 oxides lie above the convex hull – these materials are predicted to be unstable against decomposition into competing phases. All 5 materials in Table S2 lie on the convex hull and are stable.

4. Discussion

The purpose of the computational search presented in this work is to perform down selection of candidate materials from a large search space of thousands of materials to a few tens of promising candidates. So that the search is computationally tractable, we focus on the performance of the pristine material that depends on the intrinsic material properties; however, additional factors related to defects and doping of the material that can influence the performance need to be considered. Subsequent to the down selection, these additional factors can be evaluated for the candidate materials with detailed calculations and experiments. Here, we discuss three such critical factors:

Minimizing deep defects states by single-crystal growth: The phenomenological model (as well the empirical models) of breakdown field (Eq. 2) depends only on intrinsic material properties, such as band gap and phonon frequency. However, the breakdown field of a material may be lowered by the presence of appreciable concentrations of deep defects with mid-gap states, which facilitate carrier hopping. Deep levels can arise from both native defects as well as extrinsic impurities. Identifying materials with only shallow native defects⁶⁹ or adopting synthesis routes to fabricate single crystals with low concentrations of deep defects can mitigate the detrimental effect of deep levels. In particular, materials that lend themselves to simple and inexpensive crystal growth methods can produce high-quality crystals of particular interest. As an example from established power electronic semiconductors, large-size, high-quality Ga_2O_3 wafers can be fabricated by crystal growth from the melt,^{50, 51} whereas far more complicated methods are required for GaN (amothermal synthesis)⁶⁶ and SiC (physical vapor transport).⁶⁷ Besides lower defect density and large wafer size, such melt-grown methods are projected to be less expensive (e.g. 3-5x less for Ga_2O_3 compared to SiC),⁶ leading to lower cost and broader adoption of wide gap power electronics.

Selecting defect-tolerant materials from electronic structure and defect calculations: Another approach to deal with deep defects is to avoid them all together by identifying “defect-tolerant” materials⁶⁸⁻⁷⁰ that contain only shallow defect levels. The concept of defect tolerance has been explored primarily in the context of searching for novel photovoltaic absorbers,⁶⁸ where the absence of

deep levels is beneficial in suppressing Shockley-Read-Hall recombination rates.^{71, 72} Since the absence of deep levels is also beneficial for power electronics, “defect-tolerant” materials are suitable candidates provided they possess the desired intrinsic properties *i.e.* high Baliga FOM and high κ_2 . Defect concentrations can be estimated through state-of-the-art first-principles defect calculations.⁷³⁻⁷⁵ These defect calculations will also reveal the presence/absence of deep defect levels such that the “defect tolerance” of a material can be assessed. While defect calculations are computationally expensive, recent methodological advances⁷³ and emergence of software for defect calculations⁷⁴ has enabled assessment of defect properties of larger number of materials.

Tuning carrier concentrations by doping: High-power electronics necessitate high carrier mobility as well as high electrical conductivity. Since electrical conductivity depends on both the carrier mobility as well as the carrier concentrations, extrinsic doping is typically employed to enhance the carrier concentrations. For sufficient electrical conductivity, it is imperative that the material can be at least moderately doped, typically higher than $\sim 10^{17} \text{ cm}^{-3}$. Whether a material can be actually doped with the desired charge carriers and to the necessary concentrations is dictated by the native defect and dopant formation energetics. In this work, we assume that the materials can be doped. However, material dopability needs to be additionally assessed on a case-by-case basis. First-principles defect calculations can be used to gauge material dopability and reliably estimate defect/dopant and carrier concentrations of the candidate materials. The success of first-principles defect calculations in assessing dopability has been extensively demonstrated in thermoelectrics, photovoltaics^{73, 76} etc.

We performed initial computational assessment of the dopability of three candidate materials from Table S1 with high Baliga FOM, namely, HfGeO_4 , MgSiN_2 , and $\text{Y}_2\text{Si}_2\text{O}_7$. The calculated formation energetics of native defects in these materials are shown in Figures S1, S2, and S3, respectively. Details of the computational methodology for the defect calculations are also provided in the supplementary information. We predict the existence of low formation energy native donor and acceptor defects with deep transition levels in HfGeO_4 and MgSiN_2 . The equilibrium Fermi energy is pinned around mid-gap suggesting these candidate materials will be insulators, like MgO and Al_2O_3 . The existence of low formation energy native donors and acceptors also limits the possibility of extrinsic *n*- or *p*-type doping.

In $\text{Y}_2\text{Si}_2\text{O}_7$ (Fig. S3), the native defect energetics is such that the equilibrium Fermi energy is pinned closer to the conduction band under Y-rich, Si-rich, and O-poor growth conditions. As a result, $\text{Y}_2\text{Si}_2\text{O}_7$ is predicted to be natively lightly *n*-type under these growth conditions. Furthermore, the native defect energetics allows for extrinsic doping. We estimate that under equilibrium conditions, approximately 10^{17} cm^{-3} free electron concentration could be achieved provided an effective extrinsic dopant is identified. The doping challenges of wide to ultra-wide band gap materials are well known and the calculated defect energetics of HfGeO_4 , MgSiN_2 , and $\text{Y}_2\text{Si}_2\text{O}_7$ further emphasize the historical trends. To overcome the doping limits of wide band gap semiconductors, it may be necessary to use non-equilibrium growth techniques. For example, *p*-type doping of GaN for blue light emitting diodes (LEDs) was achieved by non-equilibrium hydrogen passivation.^{77, 78} For other materials, recent studies have shown that non-equilibrium growth techniques for thin film fabrication can produce defect concentrations, and presumably, carrier concentrations that are orders of magnitude larger than expected from thermodynamic equilibrium.⁷⁹ Resolving the doping challenge holds the key to realizing the predicted performance of the candidate materials.

5. Conclusions

Utilizing *ab initio* methods in conjunction with semi-empirical and phenomenological models, we undertook a broad computational survey to identify novel semiconducting materials for future power electronic devices. Through this search, we re-discover materials such as SiC, GaN and Ga_2O_3 that are being currently investigated for power electronics applications, and reemphasize the promise of a few related compounds such as ZnO and BN. More importantly, we identify several novel oxides, carbides, and nitrides that are promising candidates based on their Baliga FOMs and lattice thermal conductivities. Future efforts will have to include first-principles defect calculations in conjunction with experiments to assess the material dopability. Some of the identified candidate materials have ternary chemical compositions, which may offer additional chemical knobs to tune the material properties compared to the well-known binary semiconductors. We hope that our computational survey will inspire both deeper investigations and broader searches to discover novel power electronic materials.

Conflicts of interest

There are no conflicts of interest to declare.

Acknowledgements

This work was authored by the National Renewable Energy Laboratory (NREL), operated by Alliance for Sustainable Energy, LLC, for the U.S. Department of Energy (DOE) under Contract No. DE-AC36-08GO28308. Funding provided by the Laboratory Directed Research and Development (LDRD) Program at NREL. The research was performed using computational resources sponsored by the Department of Energy's Office of Energy Efficiency and Renewable Energy and located at the National Renewable Energy. The views

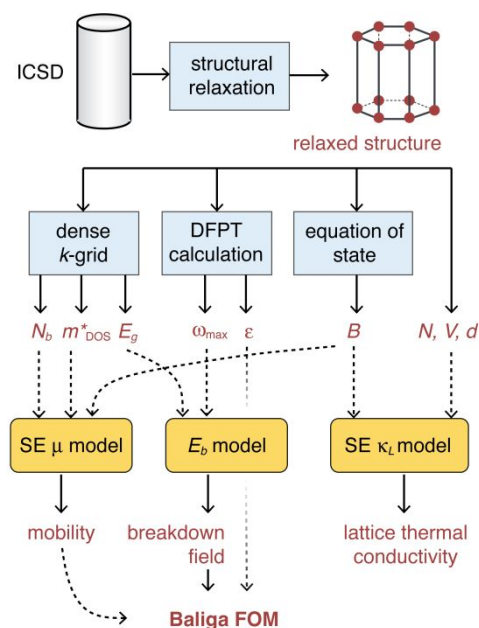


Fig. 5 Workflow for the calculation of Baliga figure of merit (FOM) and lattice thermal conductivity (κ_L). N_b denotes band degeneracy, m_{DOS}^* the density of states effective mass, E_g the band gap, and μ the carrier mobility, ω_{\max} the phonon cutoff frequency at Γ , ϵ the dielectric constant, E_b the critical breakdown field, B the bulk modulus, N the number of atoms in the primitive cell, V the primitive cell volume, and d the density. SE stands for semi-empirical, DFPT for density functional perturbation theory. The Baliga FOM and κ_L are used as screening parameters to identify candidate power electronic materials.

expressed in the article do not necessarily represent the views of the DOE or the U.S. Government.

Methods

The computational workflow is schematically presented in Fig. 5. The crystal structures from the Inorganic Crystal Structure Database (ICSD)⁸⁰ were relaxed with the generalized gradient approximation (GGA) of Perdew-Burke-Ernzerhof (PBE)⁸¹ in the projector augmented wave (PAW) formalism⁸² as implemented in the plane-wave Vienna Ab-initio Simulation Package (VASP).⁸³ A plane-wave cut-off energy of 340 eV was used. A suitable on-site correction in the form of Hubbard U in the rotationally invariant form⁸⁴ was applied for transition elements, following the methodology in Ref. ⁸⁵. The dense k -grid, density functional perturbation theory (DFPT), and equation of state calculations were all performed for the relaxed structures.

Calculation of the band degeneracy (N_b), density of states (DOS) effective mass (m_{DOS}^*), and band gap (E_g) were all undertaken on a dense k -point grid with a fixed number of k -points per atom, as determined by the equation $N \times n_{kpts} = 8000$, where N is the number of atoms in the primitive cell and n_{kpts} are the number of k -points. The k -point grid is equivalent to a $14 \times 14 \times 14$ k -point grid for diamond Si, which is sufficiently dense for determining effective masses and band degeneracy. The DOS effective mass was determined from the electronic density of states within the

parabolic band approximation¹⁶ such that the equivalent parabolic band reproduces the same number of states as the computed DOS within a 100 meV energy window from the relevant band edges. An energy window of 100 meV is chosen in this study because the same energy range is used in Ref. 16 to fit the semi-empirical model to measured room-temperature carrier mobilities (Eq. 1). To provide insights into how the calculated electronic structure properties vary with the choice of the energy window, we report the DOS and band effective masses and band degeneracies for the 6 known power electronic materials listed in Table 1 for different energy windows (100 meV, 150 meV, 200 meV). The results are provided in Table S4 of the supplementary information. Ultimately, the band effective mass (m_b^*) is the key electronic structure parameter that determines carrier mobility (Eq. 1). For the choice of different energy windows, we observe relatively small (factor of 2 or less) changes in m_b^* ; consequently, the predicted mobilities are not expected to change appreciably.

For the DFPT calculations, the structures were further relaxed with stricter energy and force convergence criteria by using larger plane-wave cut-off energies (540 eV), and denser k -point grids ($N \times n_{kpts} \sim 1000$). Bulk modulus (B) was calculated by fitting the Birch-Murnaghan equation of states [c] to a set of total energies computed at different volumes. The number of atoms in the primitive cell (N), volume (V), and density (d) were obtained from directly computed from the relaxed structure.

The calculated electronic structure properties (band gaps, effective masses) and therefore, the predicted performance of the candidate materials may be sensitive to the choice of the computational methodology. To further refine our predictions, we calculated the electronic structure of 7 n -type candidate materials (Table S1) with more accurate many-body GW method. GW calculations are performed with VASP using the set of PAW pseudopotentials supplied with the VASP. Following the methodology in Ref. 86, we use DFT wavefunctions as inputs to the GW calculations. The GW eigen-energies are iterated to self-consistency to remove the dependency of the G_0W_0 result on the initial DFT single-particle energies. The input DFT wavefunctions kept constant during the GW calculations, which allows interpretation of the GW quasi-particle energies in terms of shifts relative to the DFT Kohn-Sham single particle energies. In defect calculations, this allows the correction of the underestimated band gap by applying individual band edge shifts, as demonstrated in Ref. 86. For the 7 candidate materials listed in Tables S3, we find that, compared to PBE values, the GW-calculated band gaps are significantly larger, relevant density-of-states effective masses are smaller, and the band degeneracies remain unchanged, except for HfSiO_4 (increases). Consequently, the calculated critical breakdown fields will be larger (Eq. 2) and the carrier mobilities higher (Eq. 1), and overall, the Baliga FOM will be even larger for those candidate materials. This provides further confidence in the robustness of the predicted performance of the candidates.

References

1. M. H. Rashid, *Power Electronics Handbook*, Butterworth-Heinemann, 2017.
2. R. W. Erickson and D. Maksimovic, *Fundamentals of power electronics*, Springer Science & Business Media, 2007.
3. www.marketsandmarkets.com/Market-Reports/power-electronics-market-204729766.html.
4. H. Okumura, *MRS Bulletin*, 2015, **40**, 439.
5. Y. Sun, S. A. Boggs and R. Ramprasad, *Appl. Phys. Lett.*, 2012, **101**, 132906.
6. S. B. Reese, T. Remo, J. Green and A. Zakutayev, *Joule*, 2019, **3**, 903.
7. M. Higashiwaki, K. Sasaki, A. Kuramata, T. Masui and S. Yamakoshi, *Physica Status Solidi (a)*, 2014, **211**, 21.
8. M. A. Mastro, A. Kuramata, J. Calkins, J. Kim, F. Ren and S. J. Pearton, *ECS J. Solid State Sci. Tech.*, 2017, **6**, P356.
9. C. J. H. Wort and R. S. Balmer, *Mater. Today*, 2008, **11**, 22.
10. R. F. Davis, *Proceedings of the IEEE*, 1991, **79**, 702.
11. T. P. Chow and R. Tyagi, *IEEE Trans. Electron Devices*, 1994, **41**, 1481.
12. S. Curtarolo, G. L. W. Hart, M. B. Nardelli, N. Mingo, S. Sanvito and O. Levy, *Nature Mater.*, 2013, **12**, 191.
13. P. Gorai, V. Stevanović and E. S. Toberer, *Nature Rev. Mater.*, 2017, **2**, 17053.
14. G. Ceder, G. Hautier, A. Jain and S. P. Ong, *MRS Bulletin*, 2011, **36**, 185.
15. G. Ceder, *MRS Bulletin*, 2010, **35**, 693.
16. J. Yan, P. Gorai, B. Ortiz, S. Miller, S. A. Barnett, T. Mason, V. Stevanović and E. S. Toberer, *Energy Environ. Sci.*, 2015, **8**, 983.
17. L. Yu and A. Zunger, *Phys. Rev. Lett.*, 2012, **108**, 068701.
18. P. Gorai, D. Gao, B. Ortiz, S. Miller, S. A. Barnett, T. Mason, Q. Lv, V. Stevanović and E. S. Toberer, *Comp. Mater. Sci.*, 2016, **112**, 368.
19. A. Jain, S. P. Ong, G. Hautier, W. Chen, W. D. Richards, S. Dacek, S. Cholia, D. Gunter, D. Skinner, G. Ceder and K. A. Persson, *APL Mater.*, 2013, **1**, 011002.
20. S. Curtarolo, W. Setyawan, G. L. W. Hart, M. Jahnatek, R. V. Chepulskii, R. H. Taylor, S. Wang, J. Xue, K. Yang, O. Levy, M. J. Mehl, H. T. Stokes, D. O. Demchenko and D. Morgan, *Comp. Mater. Sci.*, 2012, **58**, 218.
21. J. E. Saal, S. Kirklin, M. Aykol, B. Meredig and C. Wolverton, *JOM*, 2013, **65**, 1501.
22. K. Yang, W. Setyawan, S. Wang, M. Buongiorno Nardelli and S. Curtarolo, *Nature Mater.*, 2012, **11**, 614.
23. B. J. Baliga, *J. Appl. Phys.*, 1982, **53**, 1759.
24. A. Von Hippel, *J. Appl. Phys.*, 1937, **8**, 815.
25. H. Fröhlich and F. Mott Nevill, *Proceedings of the Royal Society of London. Series A - Mathematical and Physical Sciences*, 1937, **160**, 230.
26. A. L. Moore and L. Shi, *Mater. Today*, 2014, **17**, 163.
27. E. Johnson, *IRE Inter. Conv. Record*, 1966, **13**, 27.
28. B. J. Baliga, *IEEE Electron Device Letters*, 1989, **10**, 455.
29. K. Il-Jung, S. Matsumoto, T. Sakai and T. Yachi, 1995.
30. A. Q. Huang, *IEEE Electron Device Letters*, 2004, **25**, 298.
31. M. Cardona and Y. Y. Peter, *Fundamentals of semiconductors*, Springer, 2005.
32. C. Kim, G. Pilania and R. Ramprasad, *Chemistry of Materials*, 2016, **28**, 1304-1311.
33. F. Birch, *Physical Review*, 1947, **71**, 809-824.

34. F. D. Murnaghan, *American Journal of Mathematics*, 1937, **59**, 235-260.
35. J. L. Hudgins, G. S. Simin, E. Santi and M. A. Khan, *IEEE Transactions on Power Electronics*, 2003, **18**, 907-914.
36. S. M. Sze and G. Gibbons, *Applied Physics Letters*, 1966, **8**, 111-113.
37. S. A. Miller, P. Gorai, B. R. Ortiz, A. Goyal, D. Gao, S. A. Barnett, T. O. Mason, G. J. Snyder, Q. Lv, V. Stevanović and E. S. Toberer, *Chemistry of Materials*, 2017, **29**, 2494-2501.
38. P. Gorai, E. S. Toberer and V. Stevanović, *Physical Chemistry Chemical Physics*, 2016, **18**, 31777-31786.
39. H. R. Shanks, P. D. Maycock, P. H. Sidles and G. C. Danielson, *Physical Review*, 1963, **130**, 1743-1748.
40. G. L. Harris, *Properties of silicon carbide*, let, 1995.
41. E. K. Sichel and J. I. Pankove, *Journal of Physics and Chemistry of Solids*, 1977, **38**, 330.
42. Z. Guo, A. Verma, X. Wu, F. Sun, A. Hickman, T. Masui, A. Kuramata, M. Higashiwaki, D. Jena and T. Luo, *Applied Physics Letters*, 2015, **106**, 111909.
43. R. Berman, P. R. W. Hudson and M. Martinez, *Journal of Physics C: Solid State Physics*, 1975, **8**, L430-L434.
44. G. A. Slack, R. A. Tanzilli, R. O. Pohl and J. W. Vandersande, *Journal of Physics and Chemistry of Solids*, 1987, **48**, 641-647.
45. R. Kalish, *Carbon*, 1999, **37**, 781-785.
46. A. Janotti and C. G. Van de Walle, *Reports on Progress in Physics*, 2009, **72**, 126501.
47. P. Siddiqua, W. A. Hadi, M. S. Shur and S. K. O'Leary, *MRS Proceedings*, 2015, **1805**, mrs15-2133804.
48. M. Benlamri, B. D. Wiltshire, Y. Zhang, N. Mahdi, K. Shankar and D. W. Barlage, *ACS Applied Electronic Materials*, 2019, **1**, 13-17.
49. E. Ohshima, H. Ogino, I. Niikura, K. Maeda, M. Sato, M. Ito and T. Fukuda, *Journal of Crystal Growth*, 2004, **260**, 166-170.
50. H. Aida, K. Nishiguchi, H. Takeda, N. Aota, K. Sunakawa and Y. Yaguchi, *Japanese Journal of Applied Physics*, 2008, **47**, 8506-8509.
51. Z. Galazka, R. Uecker, K. Irmischer, M. Albrecht, D. Klimm, M. Pietsch, M. Brützmam, R. Bertram, S. Ganschow and R. Fornari, *Crystal Research and Technology*, 2010, **45**, 1229-1236.
52. M. M. Tardío, R. Ramírez, R. González and Y. Chen, *Physical Review B*, 2002, **66**, 134202.
53. D. D. Tuschel and P. M. Lambert, *Chemistry of Materials*, 1997, **9**, 2852-2860.
54. P. Zhou, X. Yu, L. Yang, S. Yang and W. Gao, *Journal of Luminescence*, 2007, **124**, 241-244.
55. C. Q. Hu, W. T. Zheng, J. J. Li, Q. Jiang, H. W. Tian, X. Y. Lu, J. W. Liu, L. Xu and J. B. Wang, *Applied Surface Science*, 2006, **252**, 8135-8138.
56. W. H. Gust and E. B. Royce, *Journal of Applied Physics*, 1971, **42**, 276-295.
57. J. L. Corkill and M. L. Cohen, *Physical Review B*, 1993, **48**, 17138-17144.
58. P. B. Mirkarimi, K. F. McCarty and D. L. Medlin, *Materials Science and Engineering: R: Reports*, 1997, **21**, 47-100.
59. R. H. Wentorf, *The Journal of Chemical Physics*, 1961, **34**, 809-812.
60. V. L. Solozhenko, O. O. Kurakevych and Y. Le Godec, *Advanced Materials*, 2012, **24**, 1540-1544.
61. T. D. Boyko, A. Hunt, A. Zerr and A. Moewes, *Physical Review Letters*, 2013, **111**, 097402.
62. C. M. Caskey, J. A. Seabold, V. Stevanović, M. Ma, W. A. Smith, D. S. Ginley, N. R. Neale, R. M. Richards, S. Lany and A. Zakutayev, *Journal of Materials Chemistry C*, 2015, **3**, 1389-1396.
63. A. D. Martinez, A. N. Fioretti, E. S. Toberer and A. C. Tamboli, *Journal of Materials Chemistry A*, 2017, **5**, 11418-11435.
64. S. Limpijumngong, S. N. Rashkeev and W. R. L. Lambrecht, *MRS Internet Journal of Nitride Semiconductor Research*, 1999, **4**, 600-605.
65. K. Van den Eeckhout, P. F. Smet and D. Poelman, *Journal of Luminescence*, 2009, **129**, 1140-1143.
66. R. Dwiliński, R. Doradziński, J. Garczyński, L. P. Sierzputowski, A. Puchalski, Y. Kanbara, K. Yagi, H. Minakuchi and H. Hayashi, *Journal of Crystal Growth*, 2008, **310**, 3911-3916.
67. P. Wellmann, G. Neubauer, L. Fahlbusch, M. Salamon and N. Uhlmann, *Crystal Research and Technology*, 2015, **50**, 2-9.
68. R. E. Brandt, V. Stevanović, D. S. Ginley and T. Buonassisi, *MRS Communications*, 2015, **5**, 265-275.
69. R. C. Kurchin, P. Gorai, T. Buonassisi and V. Stevanović, *Chemistry of Materials*, 2018, **30**, 5583-5592.
70. A. Zakutayev, C. M. Caskey, A. N. Fioretti, D. S. Ginley, J. Vidal, V. Stevanovic, E. Tea and S. Lany, *The Journal of Physical Chemistry Letters*, 2014, **5**, 1117-1125.
71. W. Shockley and W. T. Read, *Physical Review*, 1952, **87**, 835-842.
72. R. N. Hall, *Physical Review*, 1952, **87**, 387-387.
73. C. G. Van de Walle and J. Neugebauer, *Journal of Applied Physics*, 2004, **95**, 3851-3879.
74. A. Goyal, P. Gorai, H. Peng, S. Lany and V. Stevanović, *Computational Materials Science*, 2017, **130**, 1-9.
75. P. Gorai, B. R. Ortiz, E. S. Toberer and V. Stevanović, *Journal of Materials Chemistry A*, 2018, **6**, 13806-13815.
76. A. Goyal and V. Stevanović, *Physical Review Materials*, 2018, **2**, 084603.
77. S. Nakamura, T. Mukai and M. Senoh, *Applied Physics Letters*, 1994, **64**, 1687-1689.
78. S. Nakamura, T. Mukai and M. Senoh, *Journal of Applied Physics*, 1994, **76**, 8189-8191.
79. A. Zakutayev, N. H. Perry, T. O. Mason, D. S. Ginley and S. Lany, *Applied Physics Letters*, 2013, **103**, 232106.
80. M. Hellenbrandt, *Crystallography Reviews*, 2004, **10**, 17-22.
81. J. P. Perdew, K. Burke and M. Ernzerhof, *Physical Review Letters*, 1996, **77**, 3865-3868.
82. P. E. Blöchl, *Physical Review B*, 1994, **50**, 17953-17979.
83. G. Kresse and J. Furthmüller, *Physical Review B*, 1996, **54**, 11169-11186.
84. S. L. Dudarev, G. A. Botton, S. Y. Savrasov, C. J. Humphreys and A. P. Sutton, *Physical Review B*, 1998, **57**, 1505-1509.
85. V. Stevanović, S. Lany, X. Zhang and A. Zunger, *Physical Review B*, 2012, **85**, 115104.
86. H. Peng, D. O. Scanlon, V. Stevanovic, J. Vidal, G. W. Watson and S. Lany, *Physical Review B*, 2013, **88**, 115201.