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# Boronated Holey Graphene: A case of 2D Ferromagnetic Metal ${ }^{\dagger}$ 

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#### Abstract

In search of new candidates for two-dimensional ferromagnets, we consider boronated monolayer holey graphene $\left(\mathrm{C}_{2} \mathrm{~B}\right)$, akin to recently synthesized and extensively studied nitrogenated monolayer holey graphene ( $\mathrm{C}_{2} \mathrm{~N}$ ). In contrast to $\mathrm{C}_{2} \mathrm{~N}$ which is semiconducting and nonmagnetic, our first-principles calculations show that $\mathrm{C}_{2} \mathrm{~B}$ is metallic and ferromagnetic. The microscopic origin of this interesting behavior is found to be related to the hole doping of $\pi-\pi^{*}$ network of C -B which produces metallicity while the unpaired electron on the dangling bond of $s p^{2}$ hybridized state of two-coordinated B produces magnetism. Calculated cohesive energy of boronated holey graphene indicates that the formation of this structure is energetically feasible as is the case with its nitrogenated counterpart. The dynamic and thermal stability of the predicted boronated holey graphene are checked in terms of phonon calculations and finite temperature molecular dynamics simulations. We further investigate the electronic and magnetic properties of embedded transition-metal single atom and pairs on $\mathrm{C}_{2} \mathrm{~B}$ and $\mathrm{C}_{2} \mathrm{~N}$ structures.


## 1 Introduction

The discovery of graphene and its wealth of exciting properties such as high carrier mobility, ${ }^{11}$ gate-tunable charge concentration,,$^{[2]}$ and anomalous quantum hall effect ${ }^{\sqrt[3]{3}}$ have stimulated considerable interest in the study of atomically thin two-dimensional (2D) materials as well as quasi-2D materials of a few atomiclayers. Because of the potential applications of these materials, the field has subsequently expanded in terms of synthesis of graphene-based derivatives with a goal to further improve their properties. In this connection, holey graphene, ${ }^{4]}$ which consists of a periodic array of nanosized holes within the backbone of graphene, has attracted a great deal of attention. The presence of holes leads to the formation of one-dimensional channels which enables holey graphene with good semiconducting properties. ${ }^{5}$ In addition, the dependence of the band gap on the size of the nanohole ${ }^{[5}$ makes it a suitable candidate for band gap engineering. Continuing in this direction, in 2015, a new 2D holey-graphene derivative known as nitrogenated holey graphene was successfully synthesized.6 This material has a $\mathrm{C}_{2} \mathrm{~N}$ stoichiometry and consists of a 2D sheet formed by periodic arrangement of pair of benzene rings bridged by a pyrazine ring. It is found to be non-

[^0]magnetic and a direct band gap semiconductor with a band gap of $1.96 \mathrm{eV} \cdot{ }^{66} \mathrm{C}_{2} \mathrm{~N}$ based field effect transistors have already been demonstrated to show a good ON/OFF ratio of 107. 7 Possible applications of this material in opto-electronic devices and photocatalysis ${ }^{[8]}$ have further fuelled interest in doped holey graphene.

While all the above-mentioned progress is remarkable in its own right, what is missing is the intrinsic magnetic order in a single 2D carbon based layer. The importance of this topic is highlighted in the title of the Editorial in Nature Nanotechnology, ${ }^{9}$ "2D magnetism gets hot". The 2D magnetism can appear in localized spin system through inclusion of magnetic anisotropy in a Heisenberg model as found in case of $\mathrm{Cr}_{2} \mathrm{Ge}_{2} \mathrm{Te}_{6}{ }^{10}$ or $\mathrm{CrI}_{3}{ }^{111}$. It can also appear in metallic layered material due to enhanced density of states at the Fermi level leading to magnetic order governed by the Stoner criterion. ${ }^{[12]}$ Recently, ${ }^{[13]}$ ferromagnetic (FM) order in monolayers of $\mathrm{VSe}_{2}$ grown on either graphite or $\mathrm{MoSe}_{2}$ substrate has been demonstrated which has been suggested due to enhanced density of states at the Fermi level. Following these exciting developments, there is a surge of activity to find other candidate materials exhibiting 2D ferromagnetism. In this context, metal-free $p$-electron based ferromagnets form attractive choices as they are expected to have a long spin relaxation time owing to the presence of weak spin-orbit coupling. ${ }^{14}$ Along this idea, edge magnetism in graphene has been discussed, 17 whose usefulness and applicability still remains to be established on a firm ground. Ab-initio studies ${ }^{18[19]}$ considering carrier doping via additional C atoms or gating of nitrogenated holey graphene have predicted metallic ferromagnetism. Other than ni-
trogenation, alloying of holey graphene with other elements has not been reported, although theoretical study has been carried out for phosphorated and arsenicated holey graphenes. ${ }^{20]}$ Calculated cohesive energy indicated that, similar to the $\mathrm{C}_{2} \mathrm{~N}$ monolayer, formation of phosphorated and arsenicated holey structures are also energetically feasible, making the situation promising.

Motivated by these findings, we consider in the present study boronated holey graphene. Substitution of carbon by boron, has been demonstrated to be an extremely useful route to introduce flexibility in 2D MXene structure ${ }^{21 \mid 22}$ and in the manipulation of Stone-Wales defect in fullerene. ${ }^{[23}$ It is to be noted that nitrogenation, phosphoration, or arsenication of holey graphene leads to electron doping, while boronation leads to hole doping. Pairing of $p_{z}$ electrons of C atoms and $\mathrm{N} / \mathrm{P} / \mathrm{As}$ atoms, with the lone pair being located on the dangling bond of two-coordinated N/P/As sites in the nitrogenated, phosphorated or arsenicated structures leads to nonmagnetic and semiconducting ground state. ${ }^{624}$ On the other hand, introduction of B atoms in the two-coordinated positions of the holey structure having one electron less than that of $C$ atoms, increases the possibility of magnetism as well as metallicity. This may cause stabilization of 2D magnetism in a metallic system through Stoner criterion. ${ }^{[12]}$ In the following, we explore this possibility in $\mathrm{C}_{2} \mathrm{~B}$ through first-principles calculations, and compare the results to that of $\mathrm{C}_{2} \mathrm{~N}$. We also explore the properties of boronated holey graphene structure by embedding single and pairs of 3d transition metal (TM) atoms such as Sc and Mn in the nano-holes.

## 2 Computational Details

The first principle calculations are carried out within the framework of density functional theory (DFT) based on projector augmented wave (PAW) pseudopotentials as implemented within the Vienna $A b$-Initio Simulation Package. ${ }^{[25]}$ The wave functions are expanded within the plane-wave basis set with a kinetic energy cut-off of 500 eV . Full geometry relaxations, involving both volume and atomic coordinates, are performed within the generalized gradient approximation (GGA) as parametrized by Perdew-Burke-Ernzerhof (PBE). ${ }^{26}$ Possible Van-der-Waals interactions, which may be important for 2D materials, are included within DFT-D2 approach. ${ }^{[27}$ The structures are relaxed towards equilibrium until the Hellmann-Feynman forces becomes less than $0.0001 \mathrm{eV} / \AA^{3}$. А Г-centered k-mesh of $32 \times 32 \times 1$ is used for the unit cell calculations.

The dynamical and thermal stability of $\mathrm{C}_{2} \mathrm{~B}$ structure are verified using phonon calculations and molecular dynamics (MD) simulation at 300 K , respectively. Phonons are calculated using density functional perturbation theory (DFPT). Molecular dynamic simulations are conducted using the $N V T$ ensemble, where the shape of the cell is allowed to change. A time step of 1 fs is used. The simulation lasts for a total of 7 ps , with the first 2 ps for the system to reach thermal equilibrium.

For the calculations of transition metal(s) in embedded structures, supercells of size $2 \times 2 \times 1$ for single TM atom and $3 \times 2 \times$ 1 for TM atom pair are used and calculations are carried out using $8 \times 8 \times 1 \mathrm{k}$-mesh. A Gaussian smearing with smearing value of 0.005 eV is used for the Brillouin Zone integration. In order
to take into account the strong correlation effect beyond GGA, a supplemented on-site Coulomb interaction, U of 4 eV is applied at the TM sites within the GGA+U framework. ${ }^{[88}$ In order to estimate the correct site preference of the TM atoms embedded in the hole, the TM atoms are initially placed at the centre of the hole and subsequently kicked off-centre in five incremental steps along the $b$ and $a$ directions of the hexagonal lattice.


Fig. 1 Optimized crystal structure of $\mathrm{C}_{2} \mathrm{~B}$ (left panel) and $\mathrm{C}_{2} \mathrm{~N}$ (right panel), viewed along the hexagonal $c$-axis. Marked are the diameters of the holes in the structures, the lattice constants of the 2D hexagonal lattices, and the unit cells with dashed lines.

## 3 Results and Discussion

### 3.1 Properties of $C_{2} B$

We start our discussion by considering the structural, electronic and magnetic properties of $\mathrm{C}_{2} \mathrm{~B}$ in comparison to that of the well studied case of $\mathrm{C}_{2} \mathrm{~N}$. This discussion brings out the contrast between hole doping and electron doping at the two-coordinated sites of holey graphene.

### 3.1.1 Structure and the Stability.

The optimized structure of monolayer $\mathrm{C}_{2} \mathrm{~B}$ compared to that of $\mathrm{C}_{2} \mathrm{~N}$ is shown in Fig. 1. The computed structure of $\mathrm{C}_{2} \mathrm{~N}$ is found to be in good agreement with that reported previously ${ }^{29}$ First of all, the lattice constant is found to be expanded by about $9 \%$ upon replacement of N by B, with C-B bondlength more than $10 \%$ longer than C-N bondlength (see Table I). Furthermore the Bcontaining ring connecting two benzene rings in $\mathrm{C}_{2} \mathrm{~B}$ is squeezed, as opposed to the N -containing ring connecting two benzene rings in $\mathrm{C}_{2} \mathrm{~N}$ which is elongated. This is due to the fact the C-B (N) bond is longer (shorter) than C-C bond(s) in the boronated (nitrogenated) holey structure. Together, these cause the radius of the hole in $\mathrm{C}_{2} \mathrm{~B}$ to expand substantially (by about $19 \%$ ) compared to that in $\mathrm{C}_{2} \mathrm{~N}$. The distortion of the benzene ring is found to be similar between the two structures.

Table 1 Various bondlengths of the theoretically calculated $\mathrm{C}_{2} \mathrm{~B}$ and $\mathrm{C}_{2} \mathrm{~N}$ monolayers

| Bondlength $(\AA)$ | $\mathbf{C}_{2} \mathbf{B}$ | $\mathbf{C}_{2} \mathbf{N}$ |
| :--- | :--- | :--- |
| C-C(along hexagonal $b$ axis) | 1.422 | 1.429 |
| C-C(along hexagonal $a$ axis) | 1.466 | 1.469 |
| C-N(B) | 1.475 | 1.336 |

The calculated cohesive energy of the optimized $\mathrm{C}_{2} \mathrm{~B}$ structure turns out to be 6.61 eV , compared to 7.54 eV for $\mathrm{C}_{2} \mathrm{~N}$. This


Fig. 2 Left: Calculated phonon spectrum for $\mathrm{C}_{2} \mathrm{~B}$ showing no imaginary frequencies indicating the structure is lattice dynamically stable. Right: Molecular dynamics simulation at room temperature on the structure for 5 ps , showing good thermal stability.
strongly indicates that formation of $\mathrm{C}_{2} \mathrm{~B}$ structure is feasible like $\mathrm{C}_{2} \mathrm{~N}$. We note that the cohesive energy of proposed $\mathrm{C}_{2} \mathrm{~B}$ structure is smaller than that of $\mathrm{C}_{2} \mathrm{~N}$, while it is comparable to that of $\mathrm{C}_{2} \mathrm{P} .{ }^{20}$ The formation energy for the boronated holey graphene, defined as, 30

$$
\begin{equation*}
\Delta E=\frac{1}{m_{B}}\left[E_{t}(B G)-E_{t}(P G)-m_{B} \mu_{B}+m_{B} \mu_{C}\right] \tag{1}
\end{equation*}
$$

is further calculated, and compared to that of B-doped graphene and B-doped diamond alloy, where $E_{t}(B G)$ and $E_{t}(P G)$ are the total energies of holey graphene/graphene/diamond with and without doped B atom and $m_{B}$ is the number of doped B atoms. $\mu_{B}$ and $\mu_{C}$ are the chemical potentials of the boron atom and carbon atom respectively, which are taken as total energies per atom of $\alpha$-boron crystal and pristine holey graphene/graphene/diamond. The calculation show the stability of boronated holey graphene to be comparable to B-doped diamond ( 0.86 eV for B-doped holey graphene and 0.91 eV for B doped diamond) while the formation energy of B-doped graphene is found to be 1.87 eV .

Monolayer $\mathrm{C}_{2} \mathrm{~B}$ is found to be lattice dynamically stable as shown by the calculated phonon spectrum in left panel of Fig. 2, where no imaginary frequencies are found. Molecular dynamics simulations at room temperature ( 300 K ) also show good thermal stability of the structure at room temperature (Fig. 2, right panel). The in-plane stiffness constant $C$, for the stable $\mathrm{C}_{2} \mathrm{~B}$ monolayer structure, calculated from the slope of the linear region of the stress-strain curve is found to be 269.9 GPa , compared to the value of 340.8 GPa estimated for pristine graphene. ${ }^{[31] 32}$ The inplane stiffness of $\mathrm{C}_{2} \mathrm{~B}$, is thus found to be somewhat less than that of graphene, though of same order, suggesting more flexibility of 2D boronated holey graphene structure, compared to that of graphene.

### 3.1.2 Electronic Structure and Magnetism.

Since the possible magnetism of $\mathrm{C}_{2} \mathrm{~B}$ is expected to originate from instability in a metallic system, we first examine the non-magnetic electronic structure of $\mathrm{C}_{2} \mathrm{~B}$, to check the instability of the non-


Fig. 3 The calculated non spin-polarized density of states (left) and band structure (right) of $\mathrm{C}_{2} \mathrm{~B}$ (top panels) and $\mathrm{C}_{2} \mathrm{~N}$ (bottom panels). The zero of the energy is set at Fermi energy, $\mathrm{E}_{F}$. In the density of states plots, shown are the total density of states (solid line), and that projected to $\mathrm{B} / \mathrm{N}$ states (shaded) and C states (hatched). The direct band-gap of $\mathrm{C}_{2} \mathrm{~N}$ is marked.
magnetic solution. For comparison, we also present the results for $\mathrm{C}_{2} \mathrm{~N}$ which is known to be non-magnetic and semiconducting.

The electronic structure of $\mathrm{C}_{2} \mathrm{~B}$, namely the band structure and the density of states (DOS) calculated within the non spinpolarized scheme of calculation, is shown in Fig. 3 and compared to that of $\mathrm{C}_{2} \mathrm{~N}$. In agreement with previous literature, ${ }^{29}$ it is noted that $\mathrm{C}_{2} \mathrm{~N}$ is a direct band-gap semiconductor as both the valence band maxima (VBM) and conduction band minima (CBM) lie at the $\Gamma$-point. Our estimated value of 1.64 eV for the band gap agrees well with previously reported theoretical values ${ }^{29}$ but is smaller than the experimental gap of 1.96 eV .6 Such a discrepancy between the experimental and theoretical value is expected due underestimation of the DFT band gap. The VBM dominated by N states, arises due to the formation of flat bands contributed by highly localized lone pair in $s p^{2}$ hybridized $\sigma$ orbital. As pointed out previously, this remains non-bonded at the two-coordinated N site. ${ }^{6 \mid 24]}$ The CBM, on the other hand, is contributed by dispersive $\pi^{*}$ orbital of C , delocalized over plane, together with flat band originating from localized $\pi^{*}$ state at N atom site.

Interestingly, in contrast to pristine $\mathrm{C}_{2} \mathrm{~N}$, the electronic structure calculation of $\mathrm{C}_{2} \mathrm{~B}$ yields metallic solution. This arises due to the fact that the out-of-plane $\pi\left(p_{z}\right)$ orbital of the B atom is empty as opposed to being singly occupied as in the case of C or N . This leads to hole-doping of the delocalized $\pi-\pi^{*}$ bond network of $\mathrm{C}_{2} \mathrm{~B}$ resulting in the shifting down of the Fermi level below the valence band. Consequently, the system becomes metallic in character. The presence of substantial density of states at the Fermi energy ( $\mathrm{E}_{F}$ ) is noted in non spin-polarized DOS of $\mathrm{C}_{2} \mathrm{~B}$, with a value of 8.49 states $/ \mathrm{eV}$. This suggests the instability of the non-


Fig. 4 Calculated total energy of $\mathrm{C}_{2} \mathrm{~B}$, plotted as a function of constrained values of the magnetic moment in the unit cell. The solid line is the fit to the calculated data points. The inset shows the plot of the magnetization density with a chosen isovalue of $0.005 \mathrm{e}^{-} / \AA^{3}$.
magnetic solution towards a stable magnetic solution following Stoner's criteria ${ }^{[12] 33}$ of band magnetism.

In order to ascertain the magnetic properties of $C_{2} B$, fixed moment calculations are carried out constraining the total moment in the cell to fixed values. This gives rise to estimates of total energy as a function of magnetic moment, as presented in Fig. 4. The calculated data points are fitted to the curve given by the polynomial equation

$$
\begin{equation*}
E=E_{0}+a_{2} M^{2}+a_{4} M^{4} \tag{2}
\end{equation*}
$$

where $E$ is the energy for a given magnetic moment $M, E_{0}$ is the energy of the non-magnetic solution and $a_{2}, a_{4}$ are the fitting parameters. The value of $a_{2}$ is directly related to the Stoner parameter $I_{S}$ by the formula $a_{2}=\frac{1}{N\left(E_{F}\right)}-I_{S}$ where $N\left(E_{F}\right)$ is the density of states at $\mathrm{E}_{F}$. Using the estimates of $a_{2}$ as obtained from the fitting and the $N\left(E_{F}\right)$ value read from the non spin polarized DOS, the calculated value of $I_{S} N\left(E_{F}\right)$ turns out to be 1.2 which satisfies the Stoner criteria for a magnetic solution.

The spin-polarized calculation gives rise to a total magnetic moment of $2.49 \mu_{B}$ /unit-cell, the minimum in $E$ versus $M$ curve. The inset in Fig. 4 shows the plot of the magnetization density, which shows that the magnetization is primarily contributed by B atoms. This is corroborated by the calculated magnetic moment of $\approx 0.16 \mu_{B}$ at B site and a tiny moment of $0.01 \mu_{B}$ at C site. The spin-polarized DOS projected onto $\mathrm{B} / \mathrm{C} s, p_{x} / p_{y}$ and $p_{z}$ states is presented in Fig. 5, which shows a large contribution of $\mathrm{B} p_{x} / p_{y}$, together with $\mathrm{B} s$ states in producing the spin-splitting, while $\mathrm{B} p_{z}$ admixed with $\mathrm{C} p_{z}$ gives rise to metallicity. The microscopic understanding of this curious metallic magnetism is schematically shown by the side of Fig. 5. As shown in the top schematic panel, similar to carbon and nitrogen, the boron atom, having electron configuration $[\mathrm{He}] 2 s^{2} 2 p^{1}$, also undergoes $s p^{2}$ hybridization. However, since boron has one and two electrons less compared to carbon and nitrogen, respectively, the out-of-plane $p_{z}$ orbital becomes empty. Consequently the $p_{z}$ orbital of B becomes empty, and the dangling bond is occupied by one electron instead


Fig. 5 Spin polarized density of states of $C_{2} B$, projected to $B$ (top panel) and C (bottom panel) $s$ (shaded blue), $p_{x}$ (hatched green), $p_{y}$ (black) and $p_{z}$ (brown) states. The zero of energy is fixed at $\mathrm{E}_{F}$. Shown by the side are the schematics of the nature of bonding and occupancies of $B$ atom in the $\mathrm{C}_{2} \mathrm{~B}$ network. Two out of three electrons of B occupy the $s p^{2}$ hybridized $\sigma$ bonded state with in plane C atoms (marked in green), the remaining electron occupy the $s p^{2}$ hybridized dangling bond (marked in yellow), and the out-of-plane $p_{z}$ orbital (marked in blue) forming $\pi$ bonding with C atoms remains empty.
of two, as in case of N in $\mathrm{C}_{2} \mathrm{~N}$. This results in hole doping of the $\pi-\pi^{*}$ bonded network of C and B in $\mathrm{C}_{2} \mathrm{~B}$, giving rise to metallicity, as mentioned above. Furthermore, the unpaired electron occupying the non-bonded $s p^{2}$ (marked in yellow in the Fig. 5) within the two coordinated geometry of $B$ in $C_{2} B$ being localized, gives rise to magnetism. Antiferromagnetic configuration is found to be less favorable than the ferromagnetic configuration.

### 3.2 Effect of embedding 3d TM atom

As suggested in previous studies, ${ }^{24}$ embedding of 3d TM atoms in holey graphene systems can significantly affect their properties. Depending on the choice of the embedded TM atom and its site preference, metallic, semi-metallic and semiconducting behaviors have been reported. ${ }^{34}$ In the following, we discuss the effect of embedding Sc and Mn, representatives of early and late 3d TM atoms, respectively. Calculated work functions for Sc and Mn coverage on $\mathrm{C}_{2} \mathrm{~B}$ and $\mathrm{C}_{2} \mathrm{~N}$ result in values 4.39 eV for $\mathrm{Sc}-\mathrm{C}_{2} \mathrm{~N}$, 4.45 eV for $\mathrm{Sc}-\mathrm{C}_{2} \mathrm{~B}, 4.37 \mathrm{eV}$ for $\mathrm{Mn}-\mathrm{C}_{2} \mathrm{~N}$ and 4.47 for $\mathrm{Mn}-\mathrm{C}_{2} \mathrm{~B}$.

Note that bulk Sc is nonmagnetic while bulk Mn is antiferromagnetic. In addition, Mn with an electronic configuration of $3 d^{5} 4 s^{2}$ has a magnetic moment of $5 \mu_{B}$. Our objective is to see if these transition metal atoms retain their atomic magnetic moment upon embedding? If so, how do they couple to an adjacent transition metal atom.

### 3.2.1 $\quad$ Single TM

We study TM embedding in boronated (nitrogenated) holey graphene structures by considering $2 \times 2 \times 1$ supercells of $\mathrm{C}_{2} \mathrm{~B}$ $(\mathrm{N})$, and positioning the TM atom in the central hole of the cell. This makes the periodic images of TM atoms separated by distance of $17-18 \AA$, which minimizes their interactions, mimicking the isolated limit.

The first step is to find the preferred site of TM inside the hole,

Table 2 The off-centering ( $\delta$ ) of the TM atom within the hole, the binding energy ( $B E$ ) of TM embedding, the $C-X(X=N, B$ ) bondlength for the $X$ atom facing the TM atom $\left(b_{C-X}\right)$, the magnetic moments at the TM site, $N / B$ site and the total moment in the $2 \times 2 \times 1$ cell. The last column shows the spin-polarization, $P(\%)$, of the TM embedded systems.

| System | $\delta$ <br> $(\AA)$ | BE <br> $(\mathrm{eV})$ | $b_{C-X}$ <br> $(\AA)$ |  | Mag. Mom. <br> $\left(\mu_{B}\right)$ | $P$ <br> $(\%)$ |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  | TM | $\mathrm{N} / \mathrm{B}$ | Cell |  |
| $\mathrm{Sc}-\mathrm{C}_{2} \mathrm{~N}$ | 0.26 | 7.04 | 1.393 | 0.72 | $0.02-0.05$ | 1.92 | 50.1 |
| $\mathrm{Mn}-\mathrm{C}_{2} \mathrm{~N}$ | 0.59 | 4.08 | 1.375 | 4.75 | $-0.04-0.05$ | 4.99 | 94.9 |
| $\mathrm{Sc}-\mathrm{C}_{2} \mathrm{~B}$ | 0.00 | 8.24 | 1.559 | 0.62 | $0.01-0.11$ | 5.74 | 24.7 |
| $\mathrm{Mn}-\mathrm{C}_{2} \mathrm{~B}$ | 0.00 | 5.12 | 1.532 | 4.64 | $0.04-0.09$ | 7.13 | 16.9 |



Fig. 6 The spin-polarized density of states (top and middle panels) and the charge density differences along with magnetization density (bottom panels) of Sc (left panels) and Mn (right panels) embedded $\mathrm{C}_{2} \mathrm{~N}$. The top panels show the DOS projected on to TM $d$ states, with $d$ states of $d_{x^{2}-y^{2}}$, $d_{3 z^{2}-r^{2}}, d_{x y}, d_{x z}, d_{y z}$ symmetries colored as yellow, magenta, black, green and blue, respectively. Insets in top panels show the zoomed plot to total DOS close to $E_{F}$. The middle panels show the DOS projected to $C$ (blue) and B (red) states. The zero of the energy is set at $\mathrm{E}_{F}$. The bottom panels show the plot of charge density difference plotted at isovalue $0.03 e^{-} / \AA^{3}$ (blue represents positive charge density difference(left panel) and red represents negative charge density difference), and the magnetization density (right panel, with isovalue $0.005 e^{-} / \AA^{3}$ ) of the systems.
since the properties are influenced by its position. For example, semiconducting behavior is reported when Sc atom is positioned at the center of the hole in pristine $\mathrm{C}_{2} \mathrm{~N}$ while metallic behavior is reported when the Sc atom is embedded in $\mathrm{C}_{2} \mathrm{~N}$ at an off-centered position. ${ }^{34}$ Apart from the central site in the hole, two other possible sites exist. These are, between the central site of the hole and the bridge site of the benzene ring, and that site between the central site and the hollow site of the C-B/N ring. ${ }^{34}$ Our detailed calculation shows that Sc prefers to occupy the central site of the hole for $\mathrm{C}_{2} \mathrm{~B}$, while it prefers to occupy the off centered site lying between the central site and the bridge site of the carbon ring (See Fig. 6 and 7, and Table II) in case of $\mathrm{C}_{2} \mathrm{~N} \cdot{ }^{35}$

This is at first surprising because the hole size in $\mathrm{C}_{2} \mathrm{~B}$ is substantially larger compared to $\mathrm{C}_{2} \mathrm{~N}$. This is attributed to the fact that the electron cloud of B atoms around the edge of the hole in $\mathrm{C}_{2} \mathrm{~B}$ is more delocalized than that of N in $\mathrm{C}_{2} \mathrm{~N}$, as evident from the plots of the magnetization density and the charge density differ-


Fig. 7 Same as Figure 6, but shown for $\mathrm{TM}(\mathrm{s})$ embedded in $\mathrm{C}_{2} \mathrm{~B}$.
ence in $\mathrm{C}_{2} \mathrm{~B} / \mathrm{C}_{2} \mathrm{~N}$ with and without embedded atom (see bottom panels in Fig. 6 and 7). This effectively reduces the size of the hole, thus preventing Sc atom to occupy an off-centered position due to $e^{-}-e^{-}$repulsion.

On the other hand, in the case of semiconducting $\mathrm{C}_{2} \mathrm{~N}$ with localized states, the size of Sc atom (covalent radius $=1.84 \AA$ ) is much smaller than size of the hole ( $5.52 \AA$ ), which results in the Sc atom preferring to occupy an off-centered position. This allows formation of asymmetric covalent bonding with some of the N atoms at the edge of the hole, as seen in the magnetization density plots presented in bottom panels of Fig. 6. Very similar trend is observed for embedding of Mn atom (see Table II). It is interesting to note, that the embedding energy, defined as $E_{b}=E_{T M}+E_{C_{2} B / N}-E_{T M-C_{2} B / N}$, where $E_{T M}, E_{C_{2} B / N}, E_{T M-C_{2} B / N}$ are the energies of the isolated metal atom in the same volume, $\mathrm{C}_{2} \mathrm{~B} / \mathrm{C}_{2} \mathrm{~N}$ and metal embedded $-\mathrm{C}_{2} \mathrm{~B} / \mathrm{C}_{2} \mathrm{~N}$, receptively, is substantially high for $\mathrm{C}_{2} \mathrm{~B}$ compared to $\mathrm{C}_{2} \mathrm{~N}$, driven by stronger covalency between TM atom and relatively delocalized unpaired electron of B , compared to localized lone pair of N . The binding energies for Sc embedded in $\mathrm{C}_{2} \mathrm{~B}$ turned to be $17 \%$ larger than that of $\mathrm{C}_{2} \mathrm{~N}$, while it is about $26 \%$ larger than that of $\mathrm{C}_{2} \mathrm{~N}$ for Mn embedding. This in turn causes significant change in the TM-embedded $\mathrm{C}_{2} \mathrm{~B}$ network with stretching of C-B bonds, as shown in Table II.

The top and middle panels of Fig. 6 and Fig. 7, show the spin-polarized density of states of Sc-embedded $\mathrm{C}_{2} \mathrm{~N}$ and $\mathrm{C}_{2} \mathrm{~B}$ (left panels) and Mn-embedded $\mathrm{C}_{2} \mathrm{~N}$ and $\mathrm{C}_{2} \mathrm{~B}$ (right panels), respec-
tively. The states are projected to TM $d$ states (top panels) and C and N/B states (middle panels). Within the $\mathrm{Sc}-\mathrm{C}_{2} \mathrm{~N} / \mathrm{B}$ network, the $\mathrm{Sc} d$ states are hybridized with the N or $\mathrm{B} s p^{2}$ states, the hybridization being much stronger for $B$ with unpaired electron at dangling bond, compared to that for N with localized lone-paired electron. Due to higher electro-negativity of the nitrogen/boron atoms, charge is transferred from the Sc atom to the $\mathrm{C}_{2} \mathrm{~N}$ or $\mathrm{C}_{2} \mathrm{~B}$ sheet. This is supported by the fact, that the local moment on Sc is reduced to 0.72 (for $\mathrm{C}_{2} \mathrm{~N}$ ) or $0.62 \mu_{B}$ (for $\mathrm{C}_{2} \mathrm{~B}$ ), compared to fully localized estimate of $1.0 \mu_{B}$ (see Table II). The crystal field splitting introduced at the TM sites by the six surrounding B atoms splits the TM sites $d$ states, making the $d_{x^{2}-y^{2}} / d_{x y}$ the lowest in energy, followed by $d_{3 z^{2}-r^{2}}$ and others. In the case of TM embedding in $\mathrm{C}_{2} \mathrm{~B}$, bonding $d_{x^{2}-y^{2}} / d_{x y}$ state of Sc atom becomes occupied in majority spin channel, keeping other $d$ states empty. All the $d$ states of Mn gets occupied in majority spin channel and remains empty in minority spin channel, in accordance with $d^{5}$ occupancy of Mn . In contrast, the off-centering of Sc and Mn atoms, makes the crystal field splitting of $d$ states at TM site different in case of $\mathrm{C}_{2} \mathrm{~N}$ (see Fig. 7).

The net moment in the cell for Sc and Mn embedded $\mathrm{C}_{2} \mathrm{~B}$ is largely enhanced compared to $\mathrm{C}_{2} \mathrm{~N}$ due to additional magnetic contribution of $B$ atoms. It is interesting to note incorporation of external atom in the network causes distribution of magnetic moments at N or B sites. For TM embedded in $\mathrm{C}_{2} \mathrm{~N}$ this primarily happens due to off-centred position of TM atoms, which naturally lowers the symmetry. For $\mathrm{C}_{2} \mathrm{~B}$ system this also happens, even though the TM sites occupy the central position in the hole. As is evident from the magnetization density plots (cf Fig. 7), upon incorporation of the TM atom, the magnetic moment at B sites in the vicinity of TM atom decreases substantially compared to that at B sites far away from TM site. In fact, the moment at B sites in the vicinity of the embedded atom vanishes completely in case of Mn.

The plots of total DOS (see insets in Fig. 6 and 7) suggest high degree of spin polarization of the carriers in certain cases. We thus compute the degree of spin-polarization, defined as $P=\frac{N_{\uparrow}-N_{\downarrow}}{N_{\uparrow}+N_{\downarrow}}$, where $N_{\uparrow}$ and $N_{\downarrow}$ represent DOS at $\mathrm{E}_{F}$ in the majority and minority spin channels, respectively. The results are listed in the last column of Table II. The degree of spin-polarization in general is found to be higher for $\mathrm{C}_{2} \mathrm{~N}$ compared to $\mathrm{C}_{2} \mathrm{~B}$, which once again demonstrates that the delocalized character of $\mathrm{C}_{2} \mathrm{~B}$ interacting with TM atoms is stronger than that in $\mathrm{C}_{2} \mathrm{~N}$. As is seen, the system is found to be at the verge of being half-metallic for $\mathrm{Mn}-\mathrm{C}_{2} \mathrm{~N}$, indicating the possible application of Mn embedded $\mathrm{C}_{2} \mathrm{~N}$ monolayers in spintronics application.

We thus conclude that while embedding of TM atoms in boronated holey graphene is effective for producing 2D magnets with large moment, the degree of carrier spin-polarization achieved is generally larger for $\mathrm{C}_{2} \mathrm{~N}$.

### 3.2.2 TM pair

We next consider placing two TM atoms in two neighboring holes along hexagonal $a$-direction within a $3 \times 2 \times 1$ cell. This results in intra-pair separation of around $7.5 \AA$ separated by distance of $17-18 \AA$ from their periodic images. This is in contrast to the cal-

Table 3 The exchange energies ( $\mathrm{E}_{e x}$ ) for Sc- and Mn-pairs embedded in $3 \times 2 \times 1$ cell of $\mathrm{C}_{2} \mathrm{~N}$ and $\mathrm{C}_{2} \mathrm{~B}$. Magnetic moments refer to the total moment in the $3 \times 2 \times 1$ cell.

| Systems | $\mathrm{E}_{e x}$ <br> $(\mathrm{meV})$ | Mag. Mom <br> $\left(\mu_{B}\right)$ |
| :--- | :--- | :--- |
| $\mathrm{Sc}_{2}-\mathrm{C}_{2} \mathrm{~N}$ | 9.31 | 2.04 |
| $\mathrm{Mn}_{2}-\mathrm{C}_{2} \mathrm{~N}$ | 17.62 | 8.00 |
| $\mathrm{Sc}_{2}-\mathrm{C}_{2} \mathrm{~B}$ | 2.13 | 15.78 |
| $\mathrm{Mn}_{2}-\mathrm{C}_{2} \mathrm{~B}$ | 2.06 | 22.77 |

culations carried out in Ref. 20 where a supercell of $2 \times 2 \times 1$ was used, thereby making a chain of TM atoms running along the hexagonal $a$-direction. Considering two TM embedded configurations, we compute the energies for the FM, and antiferromagnetic (AFM) alignment of TM spins. The difference of the total energies in two cases ( $E_{A F M}-E_{F M}$ ) is defined as the exchange energy ( $\mathrm{E}_{e x}$ ). Table III lists the exchange energies of $\mathrm{Sc}_{2}-\mathrm{C}_{2} \mathrm{~N}$, $\mathrm{Mn}_{2}-\mathrm{C}_{2} \mathrm{~N}, \mathrm{Sc}_{2}-\mathrm{C}_{2} \mathrm{~B}$ and $\mathrm{Mn}_{2}-\mathrm{C}_{2} \mathrm{~B}$. Ferromagnetic coupling is preferred in all cases, as evidenced from positive values of $\mathrm{E}_{e x}$ 's. This is in accordance with the results reported earlier ${ }^{24}$ for $\mathrm{C}_{2} \mathrm{~N}$, although the configuration considered was a chain configuration, as mentioned above. We find our computed exchange energies for $\mathrm{C}_{2} \mathrm{~N}$ systems to be significantly smaller than that reported in Ref. 20 which evidently stems from the consideration of two different systems (isolated pair versus chain) in two studies. This is in line with the ferromagnetic characters of atomic chains of TM atoms from Sc to Co , absorbed on monolayer $\mathrm{MX}(\mathrm{M}=\mathrm{Si} / \mathrm{Ge}, \mathrm{X}$ $=\mathrm{P} / \mathrm{As}) .{ }^{36}$ We further notice that the exchange energies in case of TM pairs embedded in $\mathrm{C}_{2} \mathrm{~B}$ are much smaller compared to that in $\mathrm{C}_{2} \mathrm{~N}$, justified by the fact that due to off-centring of TM atoms within the hole of $\mathrm{C}_{2} \mathrm{~N}$, the intra-pair distance of TM atoms in $\mathrm{C}_{2} \mathrm{~N}$ is much smaller compared to that in $\mathrm{C}_{2} \mathrm{~B}$ ( $7.6 \AA$ in $\mathrm{C}_{2} \mathrm{~N}$ versus 8.7 $\AA$ in $C_{2} B$ ).


Fig. 8 The spin-polarized density of states projected to $\mathrm{Mn} d$ states in $\mathrm{Mn}_{2}-\mathrm{C}_{2} \mathrm{~N}$ system. The insets magnetization density (top) with blue and red colors signifying up and down spin densities, and the plot of total density of states zoomed at $\mathrm{E}_{F}$ (bottom).

The ferromagnetic exchange between pair of Mn atoms em-
bedded in $\mathrm{C}_{2} \mathrm{~B}$ or $\mathrm{C}_{2} \mathrm{~N}$ is interesting and needs separate mention. The half-filled 3d shell of Mn, according to Hund's rule, gives an atomic magnetic moment of $5 \mu_{B}$. Introduction of ferromagnetic coupling between Mn atoms is thus expected to produce a large net moment, which is of technological importance. The magnetic moments of $\mathrm{Mn}_{2}$ embedded in a rare gas matrix, however, are coupled antiferromagnetically. ${ }^{37}$ In medium to large sized Mn clusters containing 11 to 100 atoms, the magnetic coupling is ferrimagnetic, with net magnetic moments less than $1.5 \mu_{B} /$ atom. On the other hand ferromagnetic coupling of $\mathrm{Mn}_{5}$ cluster isolated in rare gas matrix and carrying a total moment of $25 \mu_{B}$ has been observed in electron spin resonance. ${ }^{38}$ A giant magnetic moment of $22 \mu_{B}$ has also been theoretically predicted for nitrogen-doped $\mathrm{Mn}_{5}$ cluster. ${ }^{39}$

Our predicted ferromagnetic exchange between pair of Mn atoms embedded in nitrogenated or boronated holey graphene would be another possible means to achieve large moment by ferromagnetic alignment of spins. Indeed, our calculations revealed ferromagnetic coupling between Mn pair embedded in $\mathrm{C}_{2} \mathrm{~B}$ produces a giant moment of $22.8 \mu_{B}$ in the $3 \times 2 \times 1$ cell. Considering a $3 \times 2 \times 1$ supercell of pristine boronated holey graphene, a magnetic moment of $14.94 \mu_{B}\left(6 \times 2.49 \mu_{B}\right)$ is obtained which gets further enhanced to $22.8 \mu_{B}$ due to parallel alignment of embedded Mn pairs in the high spin state.

Interestingly, pair of Mn atoms embedded in $\mathrm{C}_{2} \mathrm{~N}$ are not only ferromagnetically coupled, with the scale of ferromagnetic exchange being about 200 K , but also possess an integer net moment. Mn atoms contribute a moment of $9.2 \mu_{B}$, with $4.6 \mu_{B}$ moment on each Mn , while the moments at N atoms in the vicinity of Mn atoms aligning antiparallel to that of Mn spins (cf. Fig. 8), contribute $-1.2 \mu_{B}$, making a net magnetic moment of $8 \mu_{B}$ in the cell. The total DOS of the system shows half-metallic behavior, as shown in Fig. 8. This interesting situation calls for further investigation.

## 4 Conclusions

In summary, inspired by recent success in the synthesis of nitrogenated holey graphene, ${ }^{6}$ we explore the effect of boronation at the two coordinated site of monolayered holey graphene. Introduction of B in place of N , introduces drastic change in the properties of these monolayers. Calculations of total energies show that the proposed boronated compound is stable. The dynamical and thermal stability of this compound is also established from calculations of phonon band structure and ab initio molecular dynamics at 300 K . Thus, it should be possible to synthesize boronated holey graphene.

Based on our first-principles calculations, we propose that boronated holey graphene is a candidate material for 2D ferromagnetism. This is in marked contrast with properties of $\mathrm{C}_{2} \mathrm{~N}$, which is nonmagnetic and semiconducting. The origin of this metallic 2D magnetism is traced to hole doping of $\pi-\pi^{*}$ network of C-B together with creation of unpaired electron in the $s p^{2}$ hybridized orbital on the dangling bond of B. Encouraged by the observation of 2 D metallic ferromagnetism in pristine $\mathrm{C}_{2} \mathrm{~B}$, we study embedding of transition metal atoms in the holes of the boronated holey graphene. We use Sc, as an example of early
transition metal, and Mn , as an example of late transition metal. We consider embedding of both isolated atom and atom pairs at two neighboring holes.

In contrast to the situation with $\mathrm{C}_{2} \mathrm{~N}$, we find embedded atoms occupy the central site inside the hole in $\mathrm{C}_{2} \mathrm{~B}$, driven by the electrostatic repulsion from the unpaired electron at the dangling bond of the B site. The metal atom-embedded boronated systems show large magnetic moments, contributed by both the metal atom(s) and the boron atoms, while the metal atom-embedded nitrogenated systems show larger degree of spin-polarization, being at verge of being half-metallic when Mn is embedded. The exchange interaction between metal pairs turned out to ferromagnetic both for $\mathrm{C}_{2} \mathrm{~N}$ and $\mathrm{C}_{2} \mathrm{~B}$, with gigantic net moment for $\mathrm{Mn}_{2}-\mathrm{C}_{2} \mathrm{~B}$, and half-metallic ferromagnetism with large exchange for $\mathrm{Mn}_{2}-\mathrm{C}_{2} \mathrm{~N}$.

## Conflicts of interest

There are no conflicts to declare.

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