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# Unraveling Luminescence Mechanisms in Zero-Dimensional Halide Perovskites

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## Abstract

Zero-dimensional (0D) halides perovskites, in which anionic metal-halide octahedra ( $\text{MX}_6$ )<sup>4-</sup> are separated by organic or inorganic counteranions, have recently shown promise as excellent luminescent materials. However, the origin of the PL and, in particular, the different photophysical properties in hybrid organic-inorganic and all inorganic halides are still poorly understood. In this work, first-principles calculations were performed to study excitons and intrinsic defects in 0D hybrid organic-inorganic halides  $(\text{C}_4\text{N}_2\text{H}_{14}\text{X})_4\text{SnX}_6$  ( $\text{X} = \text{Br}, \text{I}$ ), which exhibit high photoluminescence quantum efficiency (PLQE) at room temperature (RT), and also in 0D inorganic halide  $\text{Cs}_4\text{PbBr}_6$ , which suffers from strong thermal quenching when  $T > 100\text{K}$ . We show that the excitons in all three 0D halides are strongly bound and cannot be detrapped or dissociated at RT, which leads to immobile excitons in  $(\text{C}_4\text{N}_2\text{H}_{14}\text{X})_4\text{SnX}_6$ . However, the excitons in  $\text{Cs}_4\text{PbBr}_6$  can still migrate by tunneling, enabled by the resonant transfer of excitation energy (Dexter energy transfer). The exciton migration in  $\text{Cs}_4\text{PbBr}_6$  leads to a higher probability of trapping and nonradiative recombination at intrinsic defects. We show that a large Stokes shift and negligible electronic coupling between luminescent centers are important for suppressing exciton migration; thereby, enhancing photoluminescence quantum efficiency.

## I. Introduction

Hybrid organic-inorganic metal halides (HOIMHs) are a large family of materials that consist of 3D, 2D, 1D, or 0D anionic metal halide framework and organic cations.<sup>1</sup> The broad compositional and structural flexibilities of HOIMHs offer great tunability of their physical properties, which have been explored for a wide range of applications, such as photovoltaics,<sup>2-5</sup> light-emitting diode (LED),<sup>6</sup> laser,<sup>6,7</sup> radiation detection,<sup>8</sup> and downconverting phosphors<sup>9-15</sup>. Pb and Sn based 3D halide perovskites exhibit excellent carrier transport properties.<sup>16-19</sup> CH<sub>3</sub>NH<sub>3</sub>PbI<sub>3</sub> and related materials have been extensively studied as solar absorber materials.<sup>2-5</sup> Lowering the dimensionality of the polyanionic inorganic networks from 3D, 2D, 1D, to 0D leads to increasingly more localized electronic states and consequently narrower conduction and valence bands, which promote self-trapping of excitons and stronger exciton emission. As a result, efficient luminescence at a wide range of emission wavelengths has been observed in low-dimensional HOIMHs;<sup>9-15, 20, 21</sup> the highest PLQE were found in 0D compounds<sup>15, 22</sup>. The high attainable PLQE and the tunable emission energy render the 0D metal halides promising luminescent materials for energy-efficient lighting and radiation detection.

Recently, Ma and coworkers reported a series of visible-light-emitting 0D HOIMHs (C<sub>4</sub>N<sub>2</sub>H<sub>14</sub>X)<sub>4</sub>SnX<sub>6</sub> (X = Br, I) with high PLQE [up to unity for (C<sub>4</sub>N<sub>2</sub>H<sub>14</sub>Br)<sub>4</sub>SnBr<sub>6</sub> and 80% for (C<sub>4</sub>N<sub>2</sub>H<sub>14</sub>I)<sub>4</sub>SnI<sub>6</sub>]; the highly efficient luminescence was attributed to self-trapped excitons.<sup>15</sup> In addition, a related 0D inorganic metal halide Cs<sub>4</sub>PbBr<sub>6</sub>, which has the same 4-1-6 composition ratio as the highly luminescent (C<sub>4</sub>N<sub>2</sub>H<sub>14</sub>X)<sub>4</sub>SnX<sub>6</sub> (X = Br, I), has been reported to display strong green luminescence (~520 nm) with high PLQE up to 97%.<sup>23-29</sup> However, the origin of the green luminescence in Cs<sub>4</sub>PbBr<sub>6</sub> has been under intense debate.<sup>27, 29-33</sup> Several luminescence mechanisms have been proposed, such as exciton or defect-related emission in Cs<sub>4</sub>PbBr<sub>6</sub> and emission by CsPbBr<sub>3</sub> impurities.<sup>33</sup> Despite the strong green emission reported by many authors,<sup>23-28</sup> Akkerman et al. showed no significant visible light emission from Cs<sub>4</sub>PbBr<sub>6</sub><sup>30</sup> and Nikl et al., showed that bulk Cs<sub>4</sub>PbBr<sub>6</sub> exhibits UV emission (centered at 375 nm), which suffers from severe reduction of PL intensity when T > 100 K;<sup>34</sup> however, the mechanism of the thermal quenching of luminescence is unknown. The lack of microscopic understanding of the underlying mechanisms behind various photophysical properties observed in 0D HOIMHs and related inorganic metal halides hindered the design and the development of these novel materials towards high PLQE and optimized emission energies for targeted applications.

In this work, hybrid density functional theory (DFT) calculations were performed to study electronic and dielectric properties, exciton dynamics (optical excitation, relaxation, and emission), and exciton trapping by defects in 0D HOIMs, i.e.,  $(C_4N_2H_{14}X)_4SnX_6$  ( $X = Br, I$ ) and the related inorganic  $Cs_4PbBr_6$ . The calculated optical excitation and emission energies of excitons in  $(C_4N_2H_{14}X)_4SnX_6$  ( $X = Br, I$ ) and  $Cs_4PbBr_6$  are in excellent agreement with experimental results, demonstrating the validity of the hybrid DFT method in describing both the electronic structure and the structural relaxation at the excited state of these 0D metal halides. Our results show that excitons are immobile in  $(C_4N_2H_{14}Br)_4SnX_6$  ( $X = Br, I$ ) but can migrate in  $Cs_4PbBr_6$  by tunneling enabled by resonant transfer of excitation energy. The counteranions play a critical role in determining the efficiency of exciton migration and the subsequent trapping at halogen vacancies, which explains the high PLQE in  $(C_4N_2H_{14}X)_4SnX_6$  and the strong thermal quenching in  $Cs_4PbBr_6$ . Furthermore, we show that the frequently observed green emission in  $Cs_4PbBr_6$  is not due to the intrinsic properties of  $Cs_4PbBr_6$  but rather the result of  $CsPbBr_3$  inclusions.

## II. Computational Methods

Electronic band structures, density of states (DOS), and dielectric constants of bulk compounds were calculated using Perdew–Burke–Ernzerhof (PBE) exchange-correlation functional<sup>35</sup> while excitons and defects were treated by using more advanced hybrid PBE0 functional,<sup>36</sup> which has 25% non-local Fock exchange. Previous PBE0 calculations have provided accurate results in exciton excitation and emission energies in hybrid organic-inorganic halide perovskites.<sup>37</sup> Spin-orbit coupling (SOC) was included in the calculations on  $Cs_4PbBr_6$  only because it was shown previously that the SOC has a strong effect on Pb-6p levels.<sup>38</sup> Our tests show that including the SOC reduces the band gaps of  $(C_4N_2H_{14}Br)_4SnBr_6$ ,  $(C_4N_2H_{14}I)_4SnI_6$ , and  $Cs_4PbBr_6$ , by 0.11 eV, 0.18 eV, and 0.69 eV, respectively. (More details of the computational methods are given in Sec. S1 in the Supporting Information.)

Following the Franck-Condon principle, the exciton excitation and emission energies were obtained by calculating the total energy differences between the excited and the ground states using PBE0-optimized ground-state and excited-state structures, respectively. For  $(C_4N_2H_{14}X)_4SnX_6$  ( $X = Br, I$ ), a spin-singlet exciton was considered when calculating the excitation energy because this is a spin-allowed transition while a spin-triplet exciton was

considered for calculating the emission energy because the spin-triplet exciton is more stable than the spin-singlet one. The slow PL decay on the order of microsecond observed for  $(\text{C}_4\text{N}_2\text{H}_{14}\text{X})_4\text{SnX}_6$  ( $\text{X} = \text{Br}, \text{I}$ )<sup>15</sup> is consistent with the spin-forbidden transition for the radiative recombination of the spin-triplet exciton. For  $\text{Cs}_4\text{PbBr}_6$ , there is strong mixing between the spin-singlet and -triplet states of the exciton due to the strong SOC effect on Pb; thus, the SOC was included in calculations. The exciton binding energy (relative to a free exciton) was calculated by  $\Delta E_b = E(\text{GS}) + E_g - E(\text{exciton})$ , where  $E(\text{GS})$  and  $E(\text{exciton})$  are the total energies of the ground state and the exciton, respectively, and  $E_g$  is the band gap.

### III. Results and Discussion

#### A. Electronic structure

$(\text{C}_4\text{N}_2\text{H}_{14}\text{X})_4\text{SnX}_6$  ( $\text{X} = \text{Br}, \text{I}$ ) and  $\text{Cs}_4\text{PbBr}_6$  all have the 0D structure that contains isolated anionic metal-halide octahedra  $(\text{MX}_6)^{4-}$  separated by  $(\text{C}_4\text{N}_2\text{H}_{14}\text{X})^+$  or  $\text{Cs}^+$  counteranions (Figure 1); in addition, they have the same 4-1-6 composition ratio. The valence and the conduction bands of all three compounds are dominated by the electronic states derived from anionic  $(\text{MX}_6)^{4-}$  clusters as shown by the DOS in Figure 2. The electronic bands derived from the counteranions are far away from the band gap. The band structure of  $\text{Cs}_4\text{PbBr}_6$  in Fig. 1(e) is in good agreement with the previous PBE calculations.<sup>39</sup> The PBE0 band gaps of  $(\text{C}_4\text{N}_2\text{H}_{14}\text{X})_4\text{SnX}_6$  ( $\text{X} = \text{Br}, \text{I}$ ) and  $\text{Cs}_4\text{PbBr}_6$  are 5.1 eV, 4.43 eV, and 4.80 eV, respectively. (The PBE<sup>35</sup> and PBE0<sup>36</sup> band gaps are compared in the Sec. S2 in the Supporting Information.) Both the conduction and the valence bands of  $(\text{C}_4\text{N}_2\text{H}_{14}\text{X})_4\text{SnX}_6$  are nearly dispersionless [Figures 2(a) and (c)], indicating negligible electronic coupling between  $\text{SnX}_6$  clusters. The shortest inter-cluster Br-Br distance in  $(\text{C}_4\text{N}_2\text{H}_{14}\text{Br})_4\text{SnBr}_6$  is 6.33 Å. On the other hand, the shortest inter-cluster Br-Br distance in  $\text{Cs}_4\text{PbBr}_6$  is only 4.07 Å (due to the relatively small  $\text{Cs}^+$  ion), which leads to inter-cluster wavefunction overlap and the relatively dispersive valence band as shown in Figure 2(e). (This has important consequence on exciton migration, which is to be discussed in Sec. III-D).

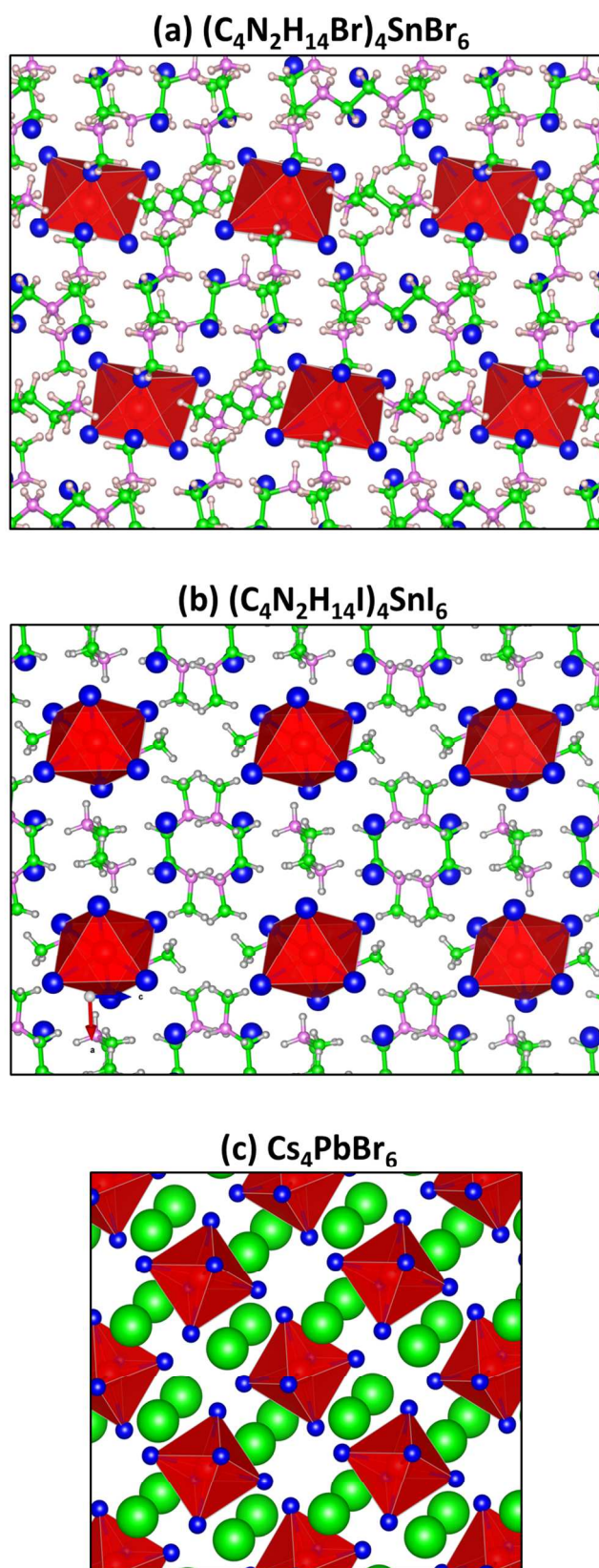


Figure 1. Structures of (a)  $(C_4N_2H_{14}Br)_4SnBr_6$ , (b)  $(C_4N_2H_{14}I)_4SnI_6$ , and (c)  $Cs_4PbBr_6$ .

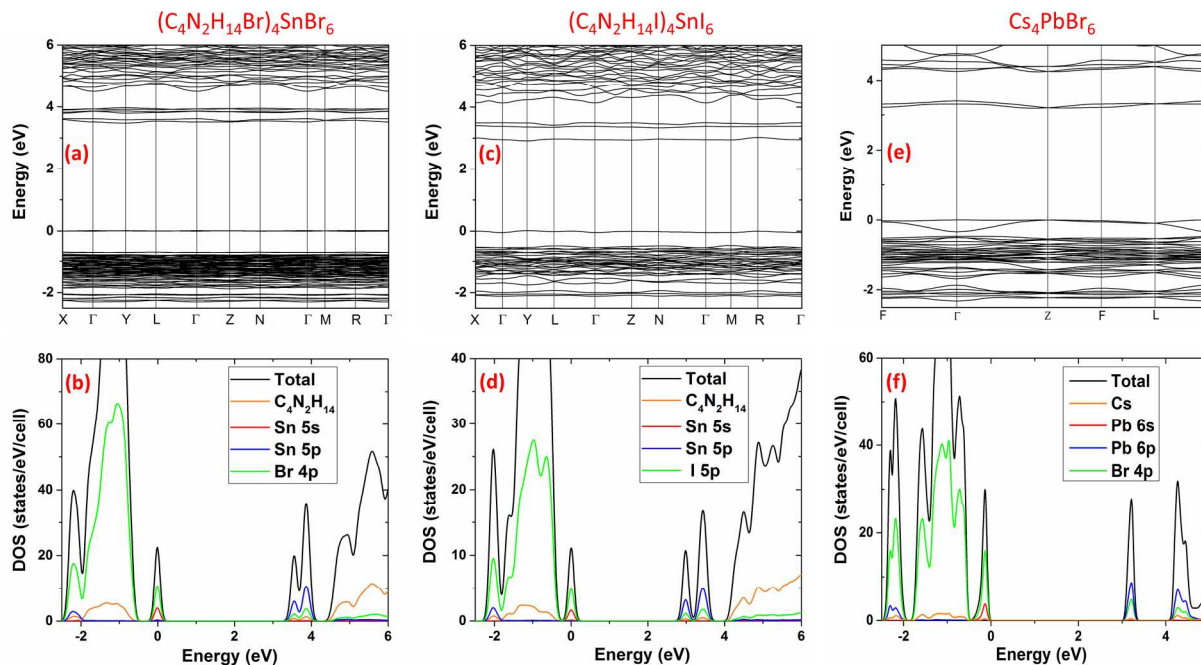


Figure 2. Electronic band structures and density of states (DOS) of  $(\text{C}_4\text{N}_2\text{H}_{14}\text{Br})_4\text{SnBr}_6$  (a-b),  $(\text{C}_4\text{N}_2\text{H}_{14}\text{I})_4\text{SnI}_6$  (c-d), and  $\text{Cs}_4\text{PbBr}_6$  (e-f) calculated using PBE functionals. The spin-orbit coupling (SOC) is included in the calculations for  $\text{Cs}_4\text{PbBr}_6$  due to the strong effect of the SOC on Pb-6p levels. Note that the PBE band gaps are underestimated.

## B. Exciton binding, relaxation, excitation, and emission

The small dispersion in both the valence and the conduction bands of  $(\text{C}_4\text{N}_2\text{H}_{14}\text{X})_4\text{SnX}_6$  ( $\text{X} = \text{Br}, \text{I}$ ) and  $\text{Cs}_4\text{PbBr}_6$  as shown in Figure 2 promote strong localization of excitons at  $(\text{MX}_6)^{4-}$  metal halide octahedra. The calculated binding energies of the relaxed excitons (relative to free excitons) ( $E_B^{\text{relax}}$  in Table 1) in  $(\text{C}_4\text{N}_2\text{H}_{14}\text{Br})_4\text{SnBr}_6$ ,  $(\text{C}_4\text{N}_2\text{H}_{14}\text{I})_4\text{SnI}_6$ , and  $\text{Cs}_4\text{PbBr}_6$  are 2.19 eV, 1.93 eV, and 1.25 eV, respectively. The large exciton binding energies suggest that free excitons do not exist in these 0D halide perovskites in the entire temperature range where these compounds are stable as solids. The electron-hole Coulomb attraction is strong as indicated by the large binding energies ( $> 1$  eV) of unrelaxed excitons ( $E_B^{\text{unrelax}}$  in Table 1). Such strong Coulomb binding is due to the 0D crystal structure, which not only confines the electron and the hole within a metal-halide octahedron but also reduces the dielectric constant substantially from the 3D compounds. The calculated static dielectric constants of  $(\text{C}_4\text{N}_2\text{H}_{14}\text{Br})_4\text{SnBr}_6$ ,  $(\text{C}_4\text{N}_2\text{H}_{14}\text{I})_4\text{SnI}_6$ , and  $\text{Cs}_4\text{PbBr}_6$  are 11.9, 7.7, and 7.7, respectively, much smaller than those of



the 3D halide perovskite counterparts (e.g., 32.0 in  $\text{CH}_3\text{NH}_3\text{SnBr}_3$ , 29.5 in  $\text{CH}_3\text{NH}_3\text{SnI}_3$ , 19.2 in  $\text{CsSnBr}_3$ ). The large ionic contribution to the static dielectric constant commonly seen in halides that contain  $ns^2$  cations (e.g.,  $\text{Sn}^{2+}$ ,  $\text{Pb}^{2+}$ )<sup>40-42</sup> is suppressed by the 0D crystal structure. [See Supporting Information (Sec. S3) for details.] Besides the strong Coulomb binding, the extended excited-state structural relaxation (as evidenced by significant bond length changes shown in Table 1) lowers the exciton energies substantially in  $(\text{C}_4\text{N}_2\text{H}_{14}\text{X})_4\text{SnX}_6$  ( $\text{X} = \text{Br}, \text{I}$ ), i.e., 0.97 eV and 0.75 eV, respectively (Table 1). However, the excited-state structural relaxation lowers the total energy by only 0.08 eV in  $\text{Cs}_4\text{PbBr}_6$ . The calculated exciton relaxation energy and the exciton emission energy in  $\text{Cs}_4\text{PbBr}_6$  are in good agreement with a recent theoretical study.<sup>43</sup> Thus, the excited-state potential energy landscape for  $\text{Cs}_4\text{PbBr}_6$  is much flatter than those for  $(\text{C}_4\text{N}_2\text{H}_{14}\text{X})_4\text{SnX}_6$  ( $\text{X} = \text{Br}, \text{I}$ ) [Figure S1].

Table 1. Binding energies of the unrelaxed ( $E_{\text{B}}^{\text{unrelax}}$ ) and the relaxed ( $E_{\text{B}}^{\text{relax}}$ ) excitons, exciton relaxation energies ( $\Delta E = E_{\text{B}}^{\text{relax}} - E_{\text{B}}^{\text{unrelax}}$ ), and the structural distortion of the metal halide octahedron ( $\text{MX}_6$ )<sup>4+</sup> due to the exciton relaxation: average increase (decrease) of the length of the two (four) metal-halogen (M-X) bonds where the electron (hole) resides within the ( $\text{MX}_6$ )<sup>4+</sup> cluster. All the results are based on hybrid functional PBE0 calculations.

	$(\text{C}_4\text{N}_2\text{H}_{14}\text{Br})_4\text{SnBr}_6$	$(\text{C}_4\text{N}_2\text{H}_{14}\text{I})_4\text{SnI}_6$	$\text{Cs}_4\text{PbBr}_6$
$E_{\text{B}}^{\text{unrelax}}$ (eV)	1.22	1.18	1.17
$E_{\text{B}}^{\text{relax}}$ (eV)	2.19	1.93	1.25
$\Delta E$ (eV)	0.97	0.75	0.08
Two elongated M-X bonds	19.8%	17.0%	15.6%
Four shortened M-X bonds	-9.9%	-6.5%	-3.7%

Here, we use  $(\text{C}_4\text{N}_2\text{H}_{14}\text{Br})_4\text{SnBr}_6$  as an example to show the details of exciton dynamics revealed by our calculations. Upon excitation of one electron, the unrelaxed spin-singlet exciton is localized on only one ( $\text{SnBr}_6$ )<sup>4+</sup> cluster and inserts deep electron and the hole levels inside the band gap [Figure S2(a)]. The spin-singlet exciton undergoes the intersystem crossing and becomes a more stable spin-triplet exciton. Our calculations show that the spin-triplet exciton is

more stable than the spin-singlet exciton by 0.28 eV without structural relaxation. The structural relaxation of both the spin-triplet and singlet excitons increases the triplet-singlet energy splitting to 0.33 eV. This is supported by the observed slow emission decay (on the order of  $\mu\text{s}$ ),<sup>15</sup> which is characteristic for the spin-forbidden triplet exciton emission. Since only one of the three Sn-5p orbitals is occupied by the excited electron, the structure relaxation of the spin-triplet exciton causes the elongation of two Sn-Br bonds within the  $(\text{SnBr}_6)^{4-}$  octahedron; the other four Sn-Br bonds are shortened due to the hole centered at Sn, which attracts the four  $\text{Br}^-$  ions. Thus, the electron state is a Sn-5p-Br-4p-hybridized orbital while the hole state is a Sn-5s-Br-4p-hybridized orbital and both are of antibonding character. These are demonstrated by the calculated partial density contours of the electron and the hole wavefunctions in the relaxed spin-triplet exciton (Figure 3). The exciton relaxation enhances localization as both the electron and the hole levels are moved deeper into the band gap as shown in the DOS (Figure S2). The two Sn-Br bonds where the excited electron resides are elongated by 19.8% in average while the four Sn-Br bonds where the hole resides are shortened by 9.9% in average. In  $(\text{C}_4\text{N}_2\text{H}_{14}\text{I})_4\text{SnI}_6$  and  $\text{Cs}_4\text{PbBr}_6$ , the similar structural distortion occurs upon exciton excitation as shown in Table 1. We also tested a different exciton structure, in which the hole is localized by forming a halogen-halogen bond like a  $V_k$  center.<sup>44</sup> However, such exciton structure is not stable in all three compounds. Table 2 shows the calculated exciton excitation and emission energies in  $(\text{C}_4\text{N}_2\text{H}_{14}\text{X})_4\text{SnX}_6$  ( $\text{X} = \text{Br}, \text{I}$ ) and  $\text{Cs}_4\text{PbBr}_6$ ; the excellent agreement between theory and experiment demonstrates that the electron-hole Coulomb binding in the exciton and the excited-state structural relaxation are described very well by the PBE0 calculation.

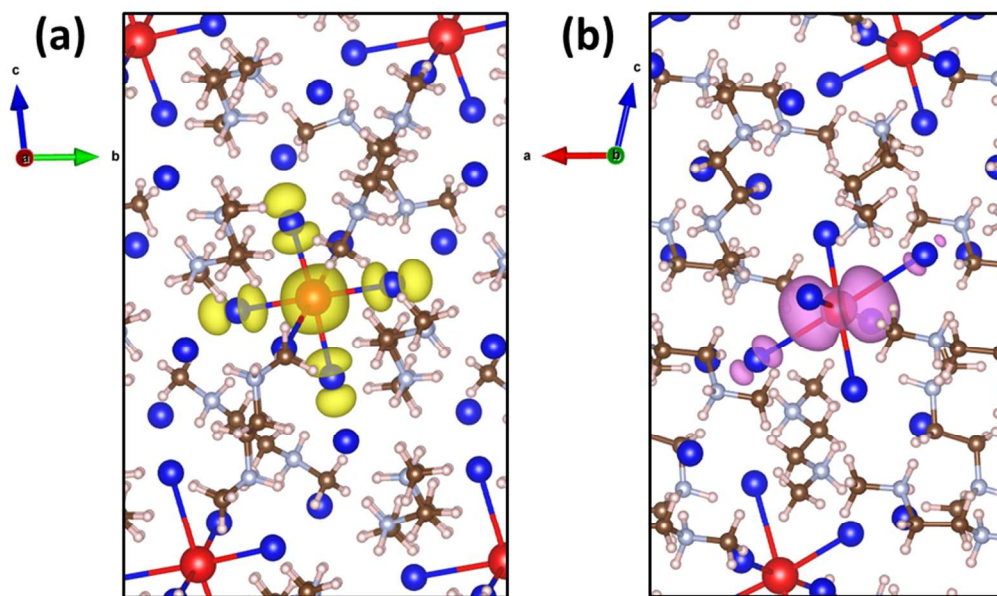


Figure 3. Partial density contours of the hole (a) and the electron (b) in a relaxed exciton in  $(\text{C}_4\text{N}_2\text{H}_{14}\text{Br})_4\text{SnBr}_6$ ; (a) and (b) are viewed from the directions of axes a and b, respectively.

Table 2. Exciton excitation and emission energies as well as Stokes shifts in  $(\text{C}_4\text{N}_2\text{H}_{14}\text{Br})_4\text{SnBr}_6$ ,  $(\text{C}_4\text{N}_2\text{H}_{14}\text{I})_4\text{SnI}_6$ , and  $\text{Cs}_4\text{PbBr}_6$ , calculated using hybrid PBE0 functionals. The experimentally measured excitation and emission energies are shown in parentheses.

	Excitation Energy (eV)	Emission Energy (eV)	Stokes Shift (eV)
$(\text{C}_4\text{N}_2\text{H}_{14}\text{Br})_4\text{SnBr}_6$	3.88 (3.49 <sup>†</sup> )	2.15 (2.34 <sup>†</sup> )	1.73 (1.15 <sup>†</sup> )
$(\text{C}_4\text{N}_2\text{H}_{14}\text{I})_4\text{SnI}_6$	3.25 (3.03 <sup>†</sup> )	1.93 (1.98 <sup>†</sup> )	1.32 (1.05 <sup>†</sup> )
$\text{Cs}_4\text{PbBr}_6$	3.63 (4.00 <sup>‡</sup> ; 3.95 <sup>‡,*</sup> )	3.05 (3.31 <sup>‡</sup> )	0.58 (0.69 <sup>‡</sup> )

<sup>†</sup>Ref. 15; <sup>‡</sup>Ref. 34; <sup>‡</sup>Ref. 30; <sup>\*</sup>Ref. 45.

### C. Exciton trapping at halogen vacancies

Photoexcited excitons can be trapped by native defects and undergo nonradiative recombination; thereby, causing loss of photon emission. The dominant native defects in halides are usually vacancies.<sup>46, 47</sup> Among vacancies, halogen vacancies are known to be deep centers in halides. However, halogen vacancies in several 3D halide perovskites (such as  $\text{CH}_3\text{NH}_3\text{PbI}_3$  and  $\text{CsPbBr}_3$ ) were found to be shallow.<sup>42, 48, 49</sup> To clarify this issue in 0D metal halides, we

calculated the exciton trapping energies at the most stable  $V_X^+$  in  $(C_4N_2H_{14}Br)_4SnBr_6$ ,  $(C_4N_2H_{14}I)_4SnI_6$ , and  $Cs_4PbBr_6$ ; they were found to be 0.41 eV, 0.22 eV, and 0.59 eV (Table 3), respectively, indicating deep trapping. [See the Supporting Information (Sec. S4) for details of the structure and the electronic structure of the bound excitons at halogen vacancies.] Thus, these halogen vacancies are effective exciton traps, which are abundant in solution-grown halide perovskites, and may cause nonradiative recombination of excitons. However, if the excitons are immobile, the probability of excitons getting trapped by halogen vacancies and other defects would be significantly reduced. Thus, the mobility of excitons is the key to the efficiency of the non-radiative recombination at defects.

Table 3. Excitation and emission energies of halogen-vacancy-bound excitons and Stoke shifts as well as the exciton binding energy at the halogen vacancies in  $(C_4N_2H_{14}Br)_4SnBr_6$ ,  $(C_4N_2H_{14}I)_4SnI_6$ , and  $Cs_4PbBr_6$ , calculated using hybrid PBE0 functionals.

	Excitation Energy (eV)	Emission Energy (eV)	Stokes Shift (eV)	Exciton Trapping Energy (eV)
$(C_4N_2H_{14}Br)_4SnBr_6$	3.58	1.81	1.77	0.41
$(C_4N_2H_{14}I)_4SnI_6$	3.11	1.65	1.46	0.22
$Cs_4PbBr_6$	3.32	2.53	0.79	0.59

#### D. Exciton migration by resonant energy transfer and thermal quenching of luminescence in $Cs_4PbBr_6$

The exciton diffusion by thermal activation should be inefficient in  $(C_4N_2H_{14}X)_4SnX_6$  ( $X = Br, I$ ) and  $Cs_4PbBr_6$  at room temperature due to the large exciton binding energies (Table 1) and the weak inter-cluster electronic and vibrational coupling. Exciton tunneling between inorganic clusters should be more efficient if the resonant condition is satisfied, i.e., there is a spectral overlap between exciton excitation and emission and significant interaction between  $MX_6$  clusters through wavefunction overlap or multi-polar interaction.<sup>50, 51</sup> Clearly, a large Stokes shift is critically important for suppressing the resonant transfer of excitation energy in 0D halide perovskites as discussed below.

Stronger excited-state structural relaxation leads to a larger Stokes shift as shown in Tables 1 and 2. The volumes for one formula unit of  $(C_4N_2H_{14}Br)_4SnBr_6$ ,  $(C_4N_2H_{14}I)_4SnI_6$ , and

$\text{Cs}_4\text{PbBr}_6$  are  $974.945 \text{ \AA}^3$ ,  $1124.94 \text{ \AA}^3$ , and  $470.585 \text{ \AA}^3$ , respectively. Clearly, among these three 0D compounds,  $\text{Cs}_4\text{PbBr}_6$  has the most compact structure [Figure 1(c)], which results in the smallest exciton relaxation energy (Table 1) and the smallest Stokes shift (Table 2) (see a schematic in Figure S1). The experimentally measured exciton excitation and the emission energies in  $\text{Cs}_4\text{PbBr}_6$  are 4.00 eV (310 nm) and 3.31 eV (375 nm), respectively. The Stokes shift of 65 nm is relatively small compared to the typical broad exciton emission bands (FWHM > 100 nm) observed in 0D metal halides.<sup>15</sup> At 4.2 K, the exciton excitation and emission bands in  $\text{Cs}_4\text{PbBr}_6$  do not overlap and the UV emission at 375 nm was observed.<sup>34</sup> With increasing temperature, both the excitation and the emission bands are expected to be broadened due to the phonon participation in the optical transitions. The phonon broadening should be significant in low-dimensional metal halides due to the soft phonons involved.<sup>32</sup> For example, as temperature rises from 77 K to RT, the FWHM of the exciton emission band increases from 63 nm (0.276 eV) to 105 nm (0.409 eV) for  $(\text{C}_4\text{N}_2\text{H}_{14}\text{Br})_4\text{SnBr}_6$  and from 63 nm (0.198 eV) to 118 nm (0.373 eV) for  $(\text{C}_4\text{N}_2\text{H}_{14}\text{I})_4\text{SnI}_6$ .<sup>15</sup> The exciton emission band for Pb compounds appear to be even broader than those in Sn compounds shown above. For 1D  $\text{C}_4\text{N}_2\text{H}_{14}\text{PbBr}_4$ , the FWHM of the emission band due to the self-trapped exciton (STE) is already broad at 77K, i.e., 103 nm (0.455 eV);<sup>14</sup> at RT, the FWHM is estimated to be about 149 nm (0.836 eV). The exciton excitation band for the low-dimensional metal halides is also broad at RT. For example, the FWHM of the exciton excitation bands in  $(\text{C}_4\text{N}_2\text{H}_{14}\text{Br})_4\text{SnBr}_6$  and  $(\text{C}_4\text{N}_2\text{H}_{14}\text{I})_4\text{SnI}_6$  at RT are 81 nm (0.896 eV) and 116 nm (0.979 eV), respectively. Based on the above results, it is expected that the excitation and the emission bands of excitons in  $\text{Cs}_4\text{PbBr}_6$  are both broadened with increasing temperature and overlap at RT due to the relatively small Stokes shift of 65 nm (0.69 eV). This is supported by the observed broad and overlapping excitonic absorption and emission bands in the UV region in the optical absorption and PL spectra in  $\text{Cs}_4\text{PbBr}_6$ .<sup>32</sup> The spectral overlap and the significant electronic coupling among  $(\text{PbBr}_6)^{4-}$  octahedra in  $\text{Cs}_4\text{PbBr}_6$  [evidenced by the relatively dispersive valence band (Figure 2(e))] should enable nonradiative resonant transfer of the excitation energy (Dexter energy transfer<sup>51</sup>), which leads to exciton migration (Figure 4).<sup>50, 51</sup> Thus, the mechanism of thermal quenching of the UV emission (when  $T > 100 \text{ K}$ ) in  $\text{Cs}_4\text{PbBr}_6$ <sup>34</sup> is likely the concentration quenching (rather than the exciton dissociation), which is frequently observed in heavily activator-doped phosphors.<sup>50</sup>, i.e., the high concentration of luminescent centers with spectral overlap between excitation and emission enables resonant transfer of

excitation energy among luminescent centers and the subsequent energy loss at defects. The role of rising temperature is to increase the spectral overlap.

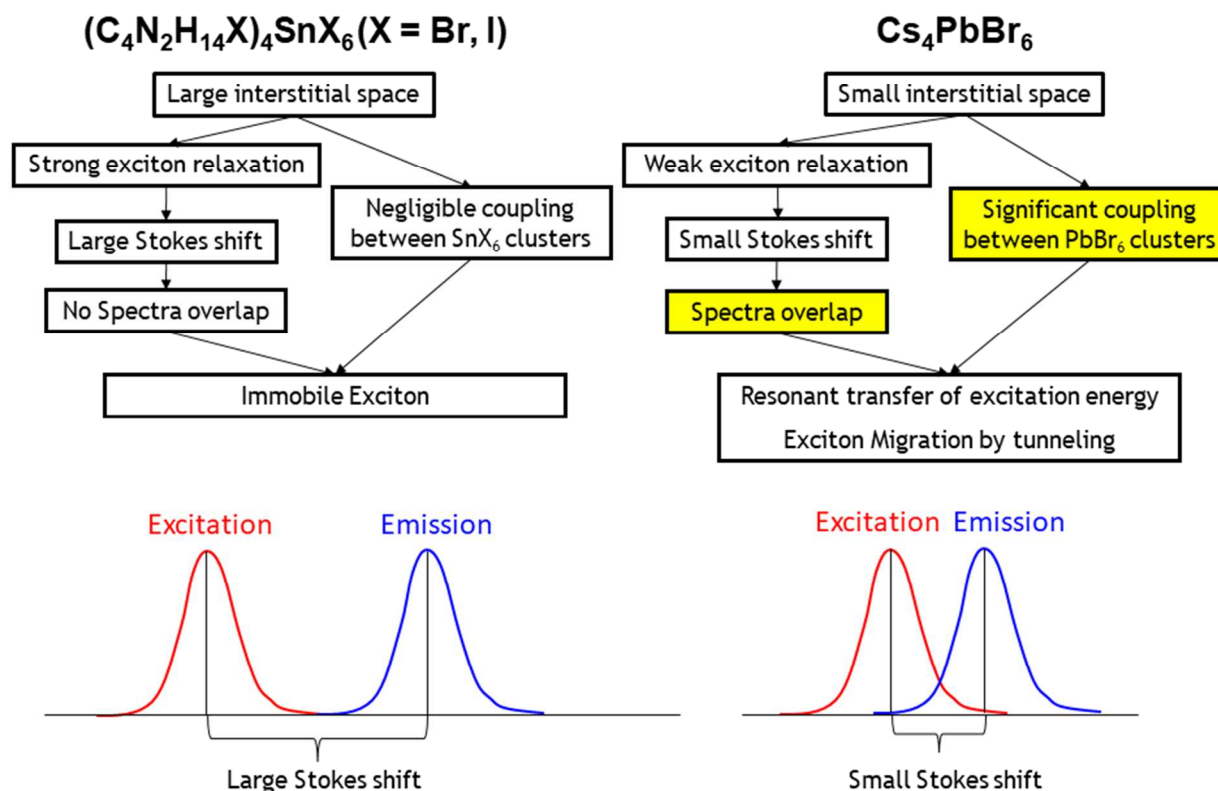


Figure 4. Illustration of the mechanisms that lead to the immobile excitons in  $(\text{C}_4\text{N}_2\text{H}_{14}\text{X})_4\text{SnX}_6$  ( $\text{X} = \text{Br}, \text{I}$ ) and the mobile excitons in  $\text{Cs}_4\text{PbBr}_6$ . Excitons are deeply bound in all three compounds. However, the excitons in  $\text{Cs}_4\text{PbBr}_6$  can migrate by tunneling.

### E. Immobile excitons and high PLQE in $(\text{C}_4\text{N}_2\text{H}_{14}\text{X})_4\text{SnX}_6$ ( $\text{X} = \text{Br}, \text{I}$ )

In contrast to  $\text{Cs}_4\text{PbBr}_6$ , the large Stokes shifts in  $(\text{C}_4\text{N}_2\text{H}_{14}\text{Br})_4\text{SnBr}_6$  (215 nm) and  $(\text{C}_4\text{N}_2\text{H}_{14}\text{I})_4\text{SnI}_6$  (210 nm)<sup>15</sup> prevent the spectral overlap; in addition, the presence of large organic cations suppresses electronic coupling among  $(\text{SnX}_6)^{4-}$  octahedra as shown by the nearly dispersionless valence and conduction bands [Figures 2(a) and (c)]. Therefore, no significant resonant transfer of the excitation energy is expected (Figure 4). The resulting immobile excitons in  $(\text{C}_4\text{N}_2\text{H}_{14}\text{X})_4\text{SnX}_6$  ( $\text{X} = \text{Br}, \text{I}$ ) have a low probability of interacting with intrinsic defects, thereby leading to high PLQE as observed in experiment.<sup>15</sup> The immobility of excitons is important because the defect density in solution-grown hybrid halide perovskites is likely high as

suggested by the significant absorption tail below the optical absorption edge in  $(C_4N_2H_{14}X)_4SnX_6$  ( $X = Br, I$ ).<sup>15</sup> The defect-related optical emission is absent from the PL spectra. The PL intensity in  $(C_4N_2H_{14}Br)_4SnBr_6$  displays linear dependence on the excitation power<sup>15</sup> instead of a saturation behavior that is expected when the defects are filled by photo-excited electrons. This behavior indicates that the emission is due to excitons not defects.<sup>46, 47</sup> Direct optical excitation at the energies within the absorption tail (below the absorption edge) does not lead to any observable emission. Our calculated excitation and emission due to bound excitons at halogen vacancies (Table 3) were not observed in experiment. These results suggest that the rate of nonradiative recombination at defects may be high, which suppresses the optical emission from excitons excited locally at defects. Therefore, suppressing exciton migration and exciton-defect interaction is essential to efficient luminescence, which highlights the importance of large organic cations that prevents the transport of excitation energy.

#### F. Green Emission in $Cs_4PbBr_6$

We have explained the thermal quenching of the UV emission in  $Cs_4PbBr_6$  above. Next, we discuss the origin of the frequently observed green emission ( $\sim 520$  nm or 2.39 eV) in  $Cs_4PbBr_6$ . The calculated fundamental band gap (4.8 eV) and excitonic absorption energy (3.63 eV) are both substantially higher than the optical absorption edge (2.3 eV- 2.4 eV) in green-emitting  $Cs_4PbBr_6$ , which suggest that the green emission is not due to the exciton emission in  $Cs_4PbBr_6$ . The Br vacancy ( $V_{Br}$ )<sup>31</sup> and the Pb antisite defect [ $Pb_{Cs}$  (Pb occupying a Cs site)]<sup>32</sup> have also been suggested to be the origin of green emission in  $Cs_4PbBr_6$ . However, the calculated Stokes shift of 0.79 eV of the bound exciton at  $V_{Br}^+$  (Table 3) is substantially larger than that observed in green-emitting  $Cs_4PbBr_6$  ( $< 0.1$  eV) [due to the strong excited-state structural relaxation (see Sec. S4 in Supporting Information)]; the calculated emission energy of the bound exciton at  $Pb_{Cs}^+$  (0.99 eV) is too small to account for the green emission (2.3 eV – 2.4 eV). Therefore, our calculations do not support the  $V_{Br}^+$  - or  $Pb_{Cs}^{2+}$  -induced green emission mechanism.

In fact, the experimentally observed onset of the optical absorption,<sup>23, 28 26, 31</sup> excitation and the emission energies (2.3 eV – 2.4 eV), the narrow emission band (15 nm – 24 nm)<sup>23-25, 28, 31</sup>, and the fast PL decay (a few to a few tens of ns)<sup>23-25, 28, 31</sup> observed in green-emitting

$\text{Cs}_4\text{PbBr}_6$  all agree well with those observed in  $\text{CsPbBr}_3$ .<sup>52,53</sup> Several papers reported that the emission energy is slightly higher than the optical absorption edge,<sup>27,26,31</sup> which is also consistent with the above-band-gap emission observed in bulk  $\text{CsPbBr}_3$ .<sup>52,53</sup> A recent review of the experimental studies of  $\text{Cs}_4\text{PbBr}_6$  supported the view that the green emission is due to  $\text{CsPbBr}_3$  nanocrystals embedded in bulk  $\text{Cs}_4\text{PbBr}_6$ .<sup>33</sup> We give additional discussion on the experimental measurements on the band gap, the exciton binding energy, and the dependence of the PL intensity on excitation power in green-emitting  $\text{Cs}_4\text{PbBr}_6$  in the Supporting Information (Sec. S5).

The above experimental and theoretical results suggest that the observed optical absorption (2.3 eV – 2.4 eV) and the subsequent green emission in  $\text{Cs}_4\text{PbBr}_6$  is likely due to  $\text{CsPbBr}_3$  inclusions trapped in  $\text{Cs}_4\text{PbBr}_6$ . The small  $\text{CsPbBr}_3$  inclusions serve as efficient luminescent centers in  $\text{Cs}_4\text{PbBr}_6$ , which trap excitons due to the much smaller band gap of  $\text{CsPbBr}_3$  than that of  $\text{Cs}_4\text{PbBr}_6$ . The encapsulating  $\text{Cs}_4\text{PbBr}_6$  may play the role of surface passivation for the  $\text{CsPbBr}_3$  inclusions, which enhances the PLQE. The PLQE of the green-emitting  $\text{Cs}_4\text{PbBr}_6$  was measured using sub-band-gap excitation energies below the excitonic absorption energy of  $\text{Cs}_4\text{PbBr}_6$ <sup>27,24,27,31</sup> and, therefore, should be the PLQE of  $\text{Cs}_4\text{PbBr}_6$ -encapsulated  $\text{CsPbBr}_3$  (in analogy to core-shell structured quantum dots). A recent experimental study demonstrated the high PLQE of 97% in green-emitting  $\text{Cs}_4\text{PbBr}_6$  and showed  $\text{CsPbBr}_3$  nanocrystals embedded in  $\text{Cs}_4\text{PbBr}_6$  based on high-resolution transmission electron microscopy.<sup>29</sup>

#### IV. Summary and Outlook

Hybrid DFT calculations have been performed to gain fundamental understanding of the different photophysical properties of 0D hybrid organic-inorganic halides  $(\text{C}_4\text{N}_2\text{H}_{14}\text{X})_4\text{SnX}_6$  (X = Br, I) and inorganic metal halide  $\text{Cs}_4\text{PbBr}_6$ . The calculated exciton excitation and emission energies agree very well with the experimental results. These 0D halides all have strongly bound excitons, which cannot be detrapped or dissociated at RT. As a result, excitons in  $(\text{C}_4\text{N}_2\text{H}_{14}\text{Br})_4\text{SnX}_6$  (X = Br, I) are immobile. However, excitons can migrate in  $\text{Cs}_4\text{PbBr}_6$  by tunneling enabled by resonant transfer of excitation energy (Figure 4). The relatively small  $\text{Cs}^+$  cation in  $\text{Cs}_4\text{PbBr}_6$  leads to electronic coupling between luminescent centers ( $\text{PbBr}_6$  clusters) and spectra overlap between excitation and emission – the two conditions that enable the resonant



energy transfer (exciton tunneling). The exciton migration in  $\text{Cs}_4\text{PbBr}_6$  results in energy loss at defects. Thus, these results explain the high PLQE in  $(\text{C}_4\text{N}_2\text{H}_{14}\text{X})_4\text{SnX}_6$  and the strong thermal quenching of the UV emission in  $\text{Cs}_4\text{PbBr}_6$ . The frequently observed green emission ( $\sim 520$  nm) in  $\text{Cs}_4\text{PbBr}_6$  is not due to the exciton or defect-induced emission in  $\text{Cs}_4\text{PbBr}_6$  but rather the result of exciton trapping and emission by  $\text{CsPbBr}_3$  inclusions in bulk  $\text{Cs}_4\text{PbBr}_6$ . We suggest that a large Stokes shift and negligible electronic coupling between luminescent centers in 0D metal halides are important for suppressing exciton migration; thereby, enhancing photoluminescence quantum efficiency. Although the all-inorganic halide  $\text{Cs}_4\text{PbBr}_6$  is not emissive at RT, efficient luminescence may be found in 0D inorganic halides, which have more effective exciton traps such as  $\text{Eu}^{2+}$ , or in double perovskite halides, in which the distance between luminescent centers is long. These insights are useful for the future development of highly luminescent 0D metal halides as bright phosphors (for lighting) and scintillators (for radiation detection).

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**References:**

1. B. Saparov and D. B. Mitzi, *Chemical Reviews*, 2016, **116**, 4558-4596.
2. M. A. Green, A. Ho-Baillie and H. J. Snaith, *Nature Photonics*, 2014, **8**, 506-514.
3. J. Berry, T. Buonassisi, D. A. Egger, G. Hodes, L. Kronik, Y.-L. Loo, I. Lubomirsky, S. R. Marder, Y. Mastai, J. S. Miller, D. B. Mitzi, Y. Paz, A. M. Rappe, I. Riess, B. Rybtchinski, O. Stafsudd, V. Stevanovic, M. F. Toney, D. Zitoun, A. Kahn, D. Ginley and D. Cahen, *Advanced Materials*, 2015, **27**, 5102-5112.
4. C. Zuo, H. J. Bolink, H. Han, J. Huang, D. Cahen and L. Ding, *Advanced Science*, 2016, **3**, n/a-n/a.
5. [https://www.nrel.gov/ncpv/images/efficiency\\_chart.jpg](https://www.nrel.gov/ncpv/images/efficiency_chart.jpg).
6. S. A. Veldhuis, P. P. Boix, N. Yantara, M. Li, T. C. Sum, N. Mathews and S. G. Mhaisalkar, *Advanced Materials*, 2016, **28**, 6804-6834.
7. P. Li, Y. Chen, T. Yang, Z. Wang, H. Lin, Y. Xu, L. Li, H. Mu, B. N. Shivananju, Y. Zhang, Q. Zhang, A. Pan, S. Li, D. Tang, B. Jia, H. Zhang and Q. Bao, *ACS Applied Materials & Interfaces*, 2017, **9**, 12759-12765.
8. H. Wei, Y. Fang, P. Mulligan, W. Chuirazzi, H.-H. Fang, C. Wang, B. R. Ecker, Y. Gao, M. A. Loi, L. Cao and J. Huang, *Nat Photon*, 2016, **10**, 333-339.
9. E. R. Dohner, E. T. Hoke and H. I. Karunadasa, *Journal of the American Chemical Society*, 2014, **136**, 1718-1721.
10. E. R. Dohner, A. Jaffe, L. R. Bradshaw and H. I. Karunadasa, *Journal of the American Chemical Society*, 2014, **136**, 13154-13157.
11. T. Hu, M. D. Smith, E. R. Dohner, M.-J. Sher, X. Wu, M. T. Trinh, A. Fisher, J. Corbett, X. Y. Zhu, H. I. Karunadasa and A. M. Lindenberg, *The Journal of Physical Chemistry Letters*, 2016, **7**, 2258-2263.
12. Z. Yuan, Y. Shu, Y. Tian, Y. Xin and B. Ma, *Chemical Communications*, 2015, **51**, 16385-16388.
13. Z. Yuan, Y. Shu, Y. Xin and B. Ma, *Chemical Communications*, 2016, **52**, 3887-3890.
14. Z. Yuan, C. Zhou, Y. Tian, Y. Shu, J. Messier, J. C. Wang, L. J. van de Burgt, K. Kountouriotis, Y. Xin, E. Holt, K. Schanze, R. Clark, T. Siegrist and B. Ma, 2017, **8**, 14051.
15. C. Zhou, H. Lin, Y. Tian, Z. Yuan, R. J. Clark, B. Chen, B. van de Burgt, J. C. Wang, Y. Zhou, K. Hanson, Q. Meisner, J. Neu, T. Besara, T. Siegrist, E. Lambers, P. I. Djurovich and B. Ma, *Chemical Science*, 2017, DOI: 10.1039/C7SC04539E.
16. Q. Dong, Y. Fang, Y. Shao, P. Mulligan, J. Qiu, L. Cao and J. Huang, *Science*, 2015, **347**, 967-970.
17. S. D. Stranks, G. E. Eperon, G. Grancini, C. Menelaou, M. J. P. Alcocer, T. Leijtens, L. M. Herz, A. Petrozza and H. J. Snaith, *Science*, 2013, **342**, 341-344.
18. G. Xing, N. Mathews, S. Sun, S. S. Lim, Y. M. Lam, M. Grätzel, S. Mhaisalkar and T. C. Sum, *Science*, 2013, **342**, 344-347.
19. D. Shi, V. Adinolfi, R. Comin, M. J. Yuan, E. Alarousu, A. Buin, Y. Chen, S. Hoogland, A. Rothenberger, K. Katsiev, Y. Losovyj, X. Zhang, P. A. Dowben, O. F. Mohammed, E. H. Sargent and O. M. Bakr, *Science*, 2015, **347**, 519-522.
20. H. Lin, C. Zhou, Y. Tian, T. Siegrist and B. Ma, *ACS Energy Letters*, 2017, DOI: 10.1021/acsendergylett.7b00926, 54-62.
21. C. Zhou, H. Lin, H. Shi, Y. Tian, C. Pak, M. Shatruk, Y. Zhou, P. Djurovich, M. Du and B. Ma, *Angewandte Chemie International Edition*, DOI: 10.1002/anie.201710383, n/a-n/a.
22. W. Liu, K. Zhu, S. J. Teat, G. Dey, Z. Shen, L. Wang, D. M. O'Carroll and J. Li, *Journal of the American Chemical Society*, 2017, **139**, 9281-9290.
23. M. I. Saidaminov, J. Almutlaq, S. Sarmah, I. Dursun, A. A. Zhumeckenov, R. Begum, J. Pan, N. Cho, O. F. Mohammed and O. M. Bakr, *ACS Energy Letters*, 2016, **1**, 840-845.

24. Y. Zhang, M. I. Saidaminov, I. Dursun, H. Yang, B. Murali, E. Alarousu, E. Yengel, B. A. Alshankiti, O. M. Bakr and O. F. Mohammed, *The Journal of Physical Chemistry Letters*, 2017, **8**, 961-965.
25. S. Seth and A. Samanta, *The Journal of Physical Chemistry Letters*, 2017, **8**, 4461-4467.
26. J.-H. Cha, J. H. Han, W. Yin, C. Park, Y. Park, T. K. Ahn, J. H. Cho and D.-Y. Jung, *The Journal of Physical Chemistry Letters*, 2017, **8**, 565-570.
27. H. Fu, H. Zhang, Q. Liao, Y.-S. Wu, J. Chen and Q. Gao, *Physical Chemistry Chemical Physics*, 2017, DOI: 10.1039/C7CP06097A.
28. D. Chen, Z. Wan, X. Chen, Y. Yuan and J. Zhong, *Journal of Materials Chemistry C*, 2016, **4**, 10646-10653.
29. X. Chen, F. Zhang, Y. Ge, L. Shi, S. Huang, J. Tang, Z. Lv, L. Zhang, B. Zou and H. Zhong, *Advanced Functional Materials*, 2018, **28**, 1706567.
30. Q. A. Akkerman, S. Park, E. Radicchi, F. Nunzi, E. Mosconi, F. De Angelis, R. Brescia, P. Rastogi, M. Prato and L. Manna, *Nano Letters*, 2017, **17**, 1924-1930.
31. M. De Bastiani, I. Dursun, Y. Zhang, B. A. Alshankiti, X.-H. Miao, J. Yin, E. Yengel, E. Alarousu, B. Turedi, J. M. Almutlaq, M. I. Saidaminov, S. Mitra, I. Gereige, A. AlSaggaf, Y. Zhu, Y. Han, I. S. Roqan, J.-L. Bredas, O. F. Mohammed and O. M. Bakr, *Chemistry of Materials*, 2017, **29**, 7108-7113.
32. J. Yin, Y. Zhang, A. Bruno, C. Soci, O. M. Bakr, J.-L. Brédas and O. F. Mohammed, *ACS Energy Letters*, 2017, DOI: 10.1021/acscenergylett.7b01026, 2805-2811.
33. Q. A. Akkerman, A. L. Abdelhady and L. Manna, *The Journal of Physical Chemistry Letters*, 2018, DOI: 10.1021/acs.jpcclett.8b00572, 2326-2337.
34. M. Nikl, E. Mihokova, K. Nitsch, F. Somma, C. Giampaolo, G. P. Pazzi, P. Fabeni and S. Zazubovich, *Chemical Physics Letters*, 1999, **306**, 280-284.
35. J. P. Perdew, K. Burke and M. Ernzerhof, *Physical review letters*, 1996, **77**, 3865.
36. J. P. Perdew, M. Ernzerhof and K. Burke, *Journal of Chemical Physics*, 1996, **105**, 9982-9985.
37. C. Zhou, H. Lin, H. Shi, Y. Tian, C. Pak, M. Shatruk, Y. Zhou, P. Djurovich, M.-H. Du and B. Ma, *Angewandte Chemie International Edition*, 2018, **57**, 1021.
38. J. Even, L. Pedesseau, J.-M. Jancu and C. Katan, *Journal of Physical Chemistry Letters*, 2013, **4**, 2999-3005.
39. J. Yin, P. Maity, M. De Bastiani, I. Dursun, O. M. Bakr, J.-L. Brédas and O. F. Mohammed, *Science Advances*, 2017, **3**.
40. M.-H. Du and D. J. Singh, *Physical Review B*, 2010, **81**, 144114
41. M.-H. Du and D. J. Singh, *Physical Review B*, 2010, **82**, 045203.
42. M. H. Du, *Journal of Materials Chemistry A*, 2014, **2**, 9091-9098.
43. B. Kang and K. Biswas, *The Journal of Physical Chemistry Letters*, 2018, **9**, 830-836.
44. K. Biswas and M. H. Du, *Physical Review B*, 2012, **86**, 014102.
45. S. Kondo, K. Amaya and T. Saito, *Journal of Physics: Condensed Matter*, 2002, **14**, 2093.
46. W. Ming, S. Chen and M.-H. Du, *Journal of Materials Chemistry A*, 2016, **4**, 16975-16981.
47. A. Walsh, D. O. Scanlon, S. Y. Chen, X. G. Gong and S. H. Wei, *Angewandte Chemie-International Edition*, 2015, **54**, 1791-1794.
48. M. H. Du, *Journal of Physical Chemistry Letters*, 2015, **6**, 1461-1466.
49. H. Shi and M.-H. Du, *Physical Review B*, 2014, **90**, 174103.
50. G. Blasse and B. C. Grabmaier, *Luminescent Materials*, Springer-Verlag, Berlin Heidelberg, 1994.
51. D. L. Dexter, *The Journal of Chemical Physics*, 1953, **21**, 836-850.
52. M. Sebastian, J. A. Peters, C. C. Stoumpos, J. Im, S. S. Kostina, Z. Liu, M. G. Kanatzidis, A. J. Freeman and B. W. Wessels, *Physical Review B*, 2015, **92**, 235210.
53. Q. A. Akkerman, M. Gandini, F. Di Stasio, P. Rastogi, F. Palazon, G. Bertoni, J. M. Ball, M. Prato, A. Petrozza and L. Manna, 2016, **2**, 16194.