# Discovery of Conical Intersection Mediated Photochemistry with Growing String Methods 

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# Discovery of Conical Intersection Mediated Photochemistry with Growing String Methods 

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#### Abstract

: Conical intersections (CIs) are important features of photochemistry that determine yields and selectivity. Traditional Cl optimizers require significant human effort and chemical intuition, which typically restricts searching to only a small region of the Cl space. Herein, a systematic approach utilizing the growing string method is introduced to locate multiple Cls. Unintuitive MECI are found using driving coordinates that can be generated using a combinatorial search, and subsequent optimization allows reaction pathways, transition states, products, and seamspace pathways to be located. These capabilities are demonstrated by application to two prototypical photoisomerization reactions and the dimerization of butadiene. In total, many reaction pathways were uncovered, including the elusive stilbene hula-twist mechanism, and a previously unidentified product in butadiene dimerization. Overall, these results suggest that growing string methods provide a predictive strategy for exploring photochemistry.


## Introduction

Photochemistries such as double-bond isomerization and electrocyclic reactions often pass through conical intersections ( CI ) on the pathways leading from initial excitation to the product state. ${ }^{1-5}$ In these reactions, Cls act like funnels that enable ultrafast, nonradiative decay to lowerlying electronic states (Scheme 1). This funneling effect causes the molecule to access nuclear configurations that would otherwise be thermally disallowed, which in turn allows photochemical reactions to reach unique outcomes compared to their ground state counterparts. In a sense, Cls can be envisioned as analogous to ground state transition states (TS), where passing through these regions correspond to important reactive events. Just like TSs, Cls are not single points, but whole regions of space. These regions are called seams, and different sections of the seam can lead to qualitatively different photo products. When molecules are excited with energetic photons, the product distribution will be determined by the presence and accessibility of these seams. ${ }^{6,7}$

Minima on the seam, called minimum energy conical intersections (MECI), are important structures for describing photochemical reactions. ${ }^{8-18}$ Conventional MECI and seam-space optimization algorithms, however, require extensive expert knowledge of photochemistry and Cl geometries, which are far different from stable chemical structures. These techniques therefore do not easily permit the discovery of new types of photochemical reactions or simple ways to explore seam spaces. To explore complex photochemical reaction mechanisms and improve computation's ability to discover photoreactivity, new methods are required.

A few unconventional methods have proposed to enable excited-state reaction discovery. For example, this was attempted by Maeda and Morokuma with the anharmonic downward distortion following (ADDF) and the artificial-force-induced reaction (AFIR) methods, which have
been used to locate MECI. ${ }^{19-25}$ Uncovering complete photochemical reaction mechanismsincluding MECI , the seam, excited-state TS, and photoproducts-is still a challenging task, however, leaving room for new methodologies.

Research in our laboratory has made extensive use of the growing string method (GSM) to determine thermal reaction pathways and transition states (TSs) without prior knowledge of the TS structure. ${ }^{26-28}$ In GSM, qualitative reactive coordinates such as bond additions/breaks and/or angle changes-called driving coordinates-are used to locate TSs, products, and the reaction paths connecting them. When combined with the reaction discovery tool, ZStruct, ${ }^{29-31}$ many TSs, some unexpected, can be found at once in a parallel computation. These features would be equally useful in the context of photochemistry where MECI optimization and seam minimum energy paths are challenging to optimize.

The GSM/ZStruct strategy is herein investigated for the first time for photochemistry, where reaction pathways include Cls and seams as well as TSs and products (Scheme 1). This method includes the integration of GSM with Cl optimizers, penalty function optimization, and Cl topography analysis (see Theoretical Methods). To show that complex photochemical reaction spaces can be explored, photoisomerizations of ethylene and stilbene, and also butadiene dimerization are examined. Photoisomerization pathways are of interest for understanding molecular motors, molecular switches and retinal chromophores, but are notoriously challenging to study because the $S_{1} / S_{0}$ degeneracy persists along the torsional coordinate, leading to complex reaction mechanisms. ${ }^{6}$ Butadiene dimerization was chosen because it can involve several modes of reaction ([2+2], [3+2], [4+2]), which, to our knowledge, has not been completely elucidated. ${ }^{32,33}$ Overall, the results will indicate that GSM/ZStruct provides a thorough, robust and highly predictive method for identifying photochemical reaction mechanisms.

## Background



Combined Strategy for Photoreactivity

1. Location of MECls
2. Evaluation of reaction path
3. Determination of photoproducts
4. Exploration of seam

Scheme 1. Overall of photochemical reactivity search.

The theory of conical-intersection-mediated photochemistry was not widely accepted until modern electronic structure theories and sufficient computational power became available, ${ }^{34}$ whereupon Robb and coworkers developed an MECl optimization algorithm. ${ }^{35}$ Locating MECls has subsequently been performed using other optimizers such as the composed-step and double-Newton-Raphson algorithms. ${ }^{36-40}$ Although there are several variants of MECI solver, these optimizers all operate by minimizing the energy gap between states and total energy simultaneously. These all require an initial starting structure that is geometrically near the MECl to be successful. This article will show that single-ended growing string method (SE-GSM) can be used to generate these structures and optimize the MECI.

Beyond MECIs, the seam ${ }^{8,9,11,12,14-17,41}$ and non-MECI points such as seam TSs (saddle points), minimum energy path $\mathrm{Cls}^{42}$ and minimum distance $\mathrm{Cls}^{43}$ are also vital components of the photochemical reaction landscape. Methods for seam optimization include seam minimum energy paths (e.g. from a seam TS), ${ }^{36}$ constrained MECI optimization, ${ }^{40,44,45}$ and the nudged elastic band (NEB) method which connects two MECIs. ${ }^{46}$ GSM will also be shown capable of connecting two MECIs, and the single-ended GSM will additionally be useful for locating seams starting from just one MECI. Seam mapping with GSM is expected to be advantageous due to its lower cost compared to NEB and standard string methods, ${ }^{47,48}$ and its ability to be easily integrated with the SE-GSM method.

MECls and seams give key transition regions between electronic states, and further analysis can then determine the photoproducts. First, the existence or absence of TS along the reaction path from the Frank Condon region to the Cl shows whether the Cl is accessible. Given that the Cl is accessible, the topography near the Cl influences the relaxation directions to the photoproducts. ${ }^{4-51}$ One way to find these directions is to plot the energy around the Cl within the branching plane (BP), which breaks the degeneracy to first order. The BP topography can be parametrized through the Cl pitch, tilt, and asymmetry. ${ }^{52}$ Ultimately, dynamical trajectories to and from the Cl dictate photoproduct yields, ${ }^{5,46,53-59}$ and several approaches have been used to approximate such trajectories. ${ }^{60,61}$ Such simulations, however, are highly costly, leaving room for potential energy surface analysis to map out complicated photochemical reaction pathways.

When performing analysis of seams, Cls, and photochemical reaction paths, the results will be sensitive to choice of electronic structure theory. Therefore we note that the methods used here are compatible with any electronic structure theory that treats conical intersections, gradients, and derivative couplings. For methods without derivative coupling vectors already implemented, these vectors can be approximated using the branching plane updating method, ${ }^{62}$ or using the Davidson algorithm recently developed in our lab, which requires only standard gradients. ${ }^{63}$

## Theoretical Methods

The Cl space is a central concept for the proposed methodologies, and is defined ${ }^{64}$ in terms of the coordinate system

$$
\begin{equation*}
\boldsymbol{Q}=\left(\boldsymbol{x}, \boldsymbol{y}, \boldsymbol{Q}_{3}, \boldsymbol{Q}_{4}, \ldots, \boldsymbol{Q}_{3 N-6}\right) . \tag{1}
\end{equation*}
$$

The first subspace $(\boldsymbol{x}, \boldsymbol{y})$ is called branching plane (BP), where $\boldsymbol{x}$ and $\boldsymbol{y}$ are the difference gradient and derivative coupling vectors, respectively. $\boldsymbol{x}$ and $\boldsymbol{y}$ are orthogonal to all other coordinates, $\boldsymbol{Q}_{i}$. At a Cl , motion along $\boldsymbol{x}$ and $\boldsymbol{y}$ changes the energy gap and produces the characteristic cone shape of a Cl between two electronic states. The second subspace $\left(\boldsymbol{Q}_{3} \ldots \boldsymbol{Q}_{3 N-6}\right)$ is denoted the seam space (SS) and corresponds to the $3 \mathrm{~N}-8$ internal coordinates which do not affect the energy gap to first order. Throughout this text, bold font signifies vectors and matrices.

## Composed-Step Optimizer

MECI optimization reduces the SS gradient and energy gap between two electronic states to zero. Most MECI optimizers achieve this by starting with a good guess structure for the MECI, projecting out the BP contributions from the (Cartesian) gradient, and optimizing in the SS. On the other hand, one can directly construct the Cl space in delocalized internal coordinates ( $\boldsymbol{U}$ ),
which are non-redundant vectors that fully span the $3 \mathrm{~N}-6$ degrees of freedom within a molecular system. ${ }^{26,65,66}$

To form the Cl subspaces, $\boldsymbol{U}$ is formed using the standard procedure, ${ }^{65}$ and $\boldsymbol{x}$ and $\boldsymbol{y}$ (originally Cartesian vectors) are projected into the basis of internal coordinates ( $\boldsymbol{U}_{x}, \boldsymbol{U}_{y}$ ), but are not orthonormal. Then, the Gram-Schmidt process is applied to the set $\left\{\left(\boldsymbol{U}_{x}, \boldsymbol{U}_{y}\right),\left(\boldsymbol{U}_{k} ; k=\right.\right.$ $1 \ldots 3 N-6)\}$ to produce the orthonormal vectors

$$
\begin{equation*}
\boldsymbol{V}=\left\{\left(\boldsymbol{U}_{x}, \boldsymbol{V}_{y}\right),\left(\boldsymbol{V}_{k} ; k=3,4,5 \ldots 3 N-6\right)\right\} \tag{2}
\end{equation*}
$$

where the first two vectors represent the BP, orthonormalized with respect to $\boldsymbol{U}_{x}$, and the $\boldsymbol{V}_{k}$ vectors define the SS.

With these vectors, the composed-step optimizer (Scheme 2) ${ }^{36,38}$ consists of two component, the first

$$
\begin{equation*}
\Delta \boldsymbol{v}_{x}=-\frac{\Delta E}{\left|\boldsymbol{g}_{x}\right|} \boldsymbol{U}_{x} \tag{3}
\end{equation*}
$$

moves the geometry closer to the Cl , where $\Delta E$ is the energy gap between the upper and lower surfaces and $\left|\boldsymbol{g}_{\boldsymbol{x}}\right|$ is the magnitude of the difference gradient. The second component minimizes the total energy by an eigenvector optimization in the seam-space:

$$
\begin{equation*}
\Delta \widetilde{\boldsymbol{v}}_{S S, i}=-\frac{\widetilde{g}_{i}}{\widetilde{\boldsymbol{H}}_{i i}+\lambda} \widetilde{\boldsymbol{V}}_{S S, i} \tag{4}
\end{equation*}
$$

where $\widetilde{\boldsymbol{V}}_{S S, i}$ and $\widetilde{\boldsymbol{H}}_{\boldsymbol{i i}}$ are the eigenvectors and eigenvalues of the seam-space Hessian, respectively, $\widetilde{\boldsymbol{g}}_{i}$ is the average gradient, and $\lambda$ a shift factor. After back-transforming equation 4 to the Cl basis $(\boldsymbol{V})$, the optimization step is composed of equations 3 and 4:

$$
\begin{equation*}
\Delta v=\Delta \boldsymbol{v}_{x}+\Delta \boldsymbol{v}_{S S} \tag{5}
\end{equation*}
$$

These steps are taken until the MECl is reached.


Scheme 2. Composed-step optimizer in delocalized internal coordinates. Each cycle of the optimizer takes a composed step until the gradient and energy gap are converged.

## Locating MECI with GSM

GSM develops a reaction path by iteratively adding and optimizing discrete structures, called nodes, along a specified reaction tangent, ${ }^{26,28}$ and herein will be shown to be useful for locating MECls starting far from the seam space. Figure S2 of the supporting information details the key steps of the GSM algorithm. The reaction tangent of GSM is defined using the standard delocalized internal coordinates $(\boldsymbol{U})$ as

$$
\begin{equation*}
\boldsymbol{U}_{c}=\sum_{k=1}^{3 N-6}\left(\Delta \boldsymbol{q}^{p} \mid \boldsymbol{U}_{\boldsymbol{k}}\right) \boldsymbol{U}_{\boldsymbol{k}} \tag{6}
\end{equation*}
$$

where $\Delta \boldsymbol{q}^{p}$ is the specified change in primitive internal coordinates $(\boldsymbol{q})$ describing the reaction. These vectors, called driving coordinates, allow GSM to explore in a specific direction (e.g. by the arrows of Scheme 1) using the coordinate system

$$
\begin{equation*}
\boldsymbol{V}^{*}=\left\{\left(\boldsymbol{U}_{c}\right),\left(\boldsymbol{V}_{k}^{*} ; k=2,3,4 \ldots 3 N-6\right)\right\} \tag{7}
\end{equation*}
$$

where coordinates $\boldsymbol{V}_{\boldsymbol{k}}^{*}$ are orthogonal to $\boldsymbol{U}_{\boldsymbol{c}}$.
To locate an MECI, single-ended GSM moves along $\boldsymbol{U}_{c}$ and optimizes in all orthogonal directions on the energy surface ${ }^{43}$ defined by

$$
\begin{equation*}
E\left(\boldsymbol{V}^{*}\right)=\bar{E}_{i j}\left(\boldsymbol{V}^{*}\right)+\sigma \frac{\Delta E_{i j}\left(\boldsymbol{V}^{*}\right)^{2}}{\Delta E_{i j}\left(\boldsymbol{V}^{*}\right)+\alpha} \tag{8}
\end{equation*}
$$

where $\bar{E}_{i j}$ is the average energy, $\sigma$ and $\alpha$ are penalty parameters, and $\Delta E_{i j}$ is the energy gap. This strategy therefore permits a simultaneous search and optimization to the nearest conical intersection in the search direction. Once the frontier node of GSM gets close to a Cl , the composed step optimizer fully refines the MECI. The computational details section describes the criteria for switching between driving and optimization steps.

## Seam Space GSM

The seams connecting MECIs will be mapped using GSM as well. This procedure combines the tangent vector (defined using eqn 6) with the two BP vectors in a coordinate system

$$
\begin{equation*}
\boldsymbol{V}^{\prime}=\left\{\left(\boldsymbol{U}_{c}\right),\left(\boldsymbol{V}_{x}, \boldsymbol{V}_{y}\right),\left(\boldsymbol{V}_{k} ; k=4,5,6 \ldots 3 N-6\right)\right\} . \tag{9}
\end{equation*}
$$

As before, the Gram-Schmidt process is applied to produce a nonredundant, orthonormal set, $\boldsymbol{V}^{\prime}$, with $3 \mathrm{~N}-6$ total degrees of freedom. All vectors are orthonormalized with respect to $\boldsymbol{U}_{c}$ to preserve the direction of $\boldsymbol{U}_{\boldsymbol{c}}$. This means that $\boldsymbol{U}_{\boldsymbol{c}}$ will typically overlap with the original BP until the path converges fully to the seam, and in practice this choice results in stable optimization. Node optimization is performed using the composed-step algorithm in the unconstrained part ( $3 \mathrm{~N}-7$ dimensions) of the coordinate space (Scheme 3).


Scheme 3. Multidimensional representation that shows the operation of the growing string method seam mapping. Curved contour plot is the seam space ( $3 \mathrm{~N}-8$ dimensional) represented in the full molecular space ( $3 \mathrm{~N}-6$ dimensions). Minima on the contour plot are minimum energy conical intersections. Purple line is the tangent constraint vector ( $\mathbf{U}_{\mathbf{c}}$ ). A composed step along along ( $\mathbf{V}_{\mathbf{x}}$ ) and ( $\left.\mathbf{V}_{\mathbf{k}} ; \mathrm{k}=4,5,6, \ldots, 3 \mathrm{~N}-6\right)$ is required to optimize the minimum energy seam path (dashed line).

This coordinate system enables two modes of operation for seam optimization in GSM. First, double-ended GSM is available to connect pairs of MECIs, by growing inward and adding additional nodes until the string connects. Alternatively, a single-ended search starting from one MECl can explore via driving coordinates, permitting a search along a seam for a second MECI . After the full string is formed with either method, full optimization of the seam in the coordinate system of equation 9 is performed, providing a minimum energy path along the seam (Scheme $3)$.

## Determining photoproducts

Photoproduct determination and optimization is initialized by taking small displacements (0.1 $\AA$ A) in the BP, based on a cross-section analysis defined in polar coordinates as ${ }^{52}$

$$
\begin{equation*}
E(r, \theta)=E^{M E C I}+\delta_{g h}\left(\sigma \cos \left(\theta-\theta_{s}\right)-\sqrt{1+\Delta_{g h} \cos 2 \theta}\right) \tag{10}
\end{equation*}
$$

where $\delta_{g h}$ is the pitch, $\theta_{s}$ is the tilt heading, and $\Delta_{g h}$ is the asymmetry. These parameters can be calculated given $\boldsymbol{x}, \boldsymbol{y}$ and the average energy gradient. Because the BP vectors can be interchanged at a Cl through rotation of the electronic states, $\boldsymbol{x}, \boldsymbol{y}$ are chosen such that $\Delta_{g h}>0$ and $0<\theta_{s}<\frac{\pi}{2}$.

Displacements in the direction of the minima and maxima of equation 10 are chosen as starting pathways to photoproducts. Optimization from the minima is analogous to the minimum energy pathways proceeding downhill from the Cl , whereas optimization from the maxima in the cross-section are also investigated because they sometimes lead to minima not in the immediate vicinity of the Cl cross-section. ${ }^{49}$ Therefore, photoproduct optimization can be initialized given the BP vectors, and the sensitivity of the decay channels to the topography (e.g. minimum versus maximum) will be captured by sampling of both types of pathways.

## Computational Details:

GSM methods are implemented in C++, and will be made available online on Github. ${ }^{67}$ The Hessian is formed at each step of the optimization, from the Hessian in primitive coordinates

$$
\begin{equation*}
\boldsymbol{H}=\boldsymbol{U}^{T} \boldsymbol{H}^{p} \boldsymbol{U}^{\prime} \tag{11}
\end{equation*}
$$

but only the non-constrained seam space coordinates are diagonalized and used in the NewtonRaphson optimization. The Broyden-Fletcher-Goldfarb-Shanno (BFGS) method is used to update a diagonal initial Hessian in primitive coordinates, which is transformed into a delocalized internal coordinate Hessian at each step. ${ }^{68-71}$ The MECl is considered converged when the energy gap between the two states is less than $0.01 \mathrm{kcal} \mathrm{mol}^{-1}$ and the seam-space root-mean-squared (RMS) average gradient is less than $0.0005 \mathrm{Ha} / \AA \AA$. For seam mapping the calculation terminates when all the nodes are converged to within a predefined threshold or the total gradient is below a predefined threshold that is dependent on the system size and number of nodes. Each node is considered converged when the energy gap between the two states is less than $1.0 \mathrm{kcal} \mathrm{mol}^{-1}$ and the gradient is converged to $0.0025 \mathrm{Ha} / \AA$. The total gradient convergence criterion was chosen to be $(M-2) * 0.0025 * \sqrt{3 N-6}$, where M is the number of GSM nodes.

Knowing where to stop the SE-GSM algorithm and initiate the composed step optimizer is an important criterion for the successful location of MECI. Since SE-GSM should be generally moving closer to the Cl -not further away—string growth terminates when $\Delta E_{i j}$ increases at the frontier node. Alternatively, if the string reaches the "product" specified by $\Delta \mathbf{q}$ (eqn 6), this indicates that
no further growth of the string is possible, and the composed step optimizer is turned on immediately.

MECI SE-GSM calculations employed a maximum of 5 iterations per node, and a maximum growth step size (dqmax) of 0.4 Å-radians. Larger dqmax generally decreases the number of nodes in a calculation and therefore decreases the number of total gradients. In the small systems investigated here, however, a small dqmax is beneficial for MECI optimization because the final node is usually closer to the seam. The last node before MECI optimization is optimized for at most 60 steps, or until converged within $0.001 \mathrm{Ha} / \AA ̊$. The penalty function optimizer utilized $\sigma$ as 1.0, for all nodes except for the final guess node, which is optimized using $\sigma$ as 3.5. Staggering $\sigma$ from small to large helps SE-GSM correctly find the desired MECI.

Seam mapping GSM calculations employed 3-5 optimization iterations per node per cycle, and dqmax values from 0.2 to $0.8 \AA$ Aradians. The optimization success is sensitive to these parameters and string growth should be monitored. In general, a smaller dqmax should be used for small molecules and/or short seam paths to ensure a refined reaction pathway.

The ZStruct method generates driving coordinates consisting of add and break coordination changes between reactive atoms. This is usually subject to the constraint that the driving coordinate can have up to two adds and one break, and the coordination of the atoms doesn't exceed a maximum and minimum coordination number. ${ }^{30}$ In this work, however, add connection moves are used exclusively, leading to $N^{4}$ scaling in the number of generated driving coordinates, where N is the number of reactive atoms.

The methods invoke MOLPRO CASSCF to provide the quantum mechanical energies, gradients and derivative coupling vectors. ${ }^{72}$ Active space selection was performed by considering the electrons involved in the excitation and reaction coordinate. Active space choices are listed in the figures below.

## Results and Discussion

## Exploratory via SE-GSM

In many photoreactions the qualitative reaction coordinates are known but not precisely quantified. For example, in the photoisomerization of ethylene the qualitative reaction coordinate is double bond torsion, but the Cl also introduces pyramidalization of the carbon. $\mathrm{SE}-$ GSM captures this behavior by adding nodes along a driving coordinate (torsion) and optimizing in orthogonal directions (pyramidalization). Therefore SE-GSM identifies and follows directions to MECI that are not necessarily specified prior to the search. Importantly, different MECI within the same reactive system can be found by sampling a variety of driving coordinates. To show the capabilities of these methods, photoisomerization pathways for ethylene and stilbene are investigated as the initial test cases.

## Ethylene Conical intersections

The well-known twisted-pyramidalized (also called H -bridging ${ }^{73}$ ) and ethylidene-like MECIs between $S_{0}$ and $S_{1}$ are reproduced here using SE-GSM (Figure 1). ${ }^{74}$ While both MECIs were found by driving a torsional coordinate, the second case also used two driving coordinates, one of which specified H -atom transfer (Table 1).

Performance metrics for SE-GSM with these two MECI are reported in Table 1. Driving cycles represent the computational costs (eqn 8) of generating the MECI guess


Figure 1. Ethylene minimum energy conical intersections calculated using CAS $(4,4) / 6-31 \mathrm{G}^{*}$ with SE-GSM. Energy is reported in kcal/mol with respect to Franck-Condon point. Paths to the MECI are barrierless. ${ }^{60}$. Atom numbers in figure are driving coordinate indices (see Table 1). structures. Once this initial structure is found, the MECl optimization quickly reaches accurate MECIs because the RMS distance from the guess to the true MECl is small, under $0.07 \AA$. Compared to a standard MECl optimizer in Molpro, ${ }^{35}$ the final geometries agree well (to within $0.01 \AA \mathrm{RMS}$ ) and the energies to within $0.05 \mathrm{kcal} / \mathrm{mol}$. These examples demonstrate that the SE-GSM process for MECI optimization provides reasonable results for ethylene, at computational costs of less than 100 gradients for each MECI.

Table 1. Ethylene MECI Results from SE-GSM, compared to standard optimizers.

| MECI | Driving Coordinates ${ }^{\text {a }}$ | Driving <br> Cycles | MECI <br> Cycles | Guess to MECI <br> Distance <br> $(\text { RMSD } \AA)^{b}$ | Calc. MECI vs. <br> Ref. MECI, <br> $(\text { RMSD } \AA)^{c}$ | Calc. E(MECI) - <br> Ref. E(MECI) <br> (kcal/mol) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1a | TORSION $(1,2,3,4)=90$ | 56 | 10 | 0.0611 | 0.0011 | 0.01 |
| 1b | TORSION $(1,2,3,4)=120, ~$ <br> $\operatorname{ADD}(4,2), \operatorname{BREAK}(3,4)$ | 55 | 39 | 0.0658 | 0.0076 | -0.03 |

a TORSION $(1,2,3,4)=90$, refers to a driving coordinate to push angle 1-2-3-4 towards 90 degrees, starting from its current position. ${ }^{\text {b }}$ root-mean squared distance in Å from penalty optimized structure to composed-step (CS) optimized MECI. ${ }^{\text {c }}$ rootmean squared distance in $\AA$ from composed-step (CS) optimized MECI to MECI from MOLPRO, see computational details.

Three seam reaction pathways and corresponding TSs were found for the ethylene system using the GSM seam optimization approach, and these are reported in Figure 2. Among these three, a tilted seam TS (2a) between 1a and $\mathbf{1 b}$ has been previously reported and is reproduced here. ${ }^{46} \mathbf{2 a}$ can be found using 7 or 9 GSM nodes and has energy relative to the FC point of -66.5 $\mathrm{kcal} / \mathrm{mol}$. A second, unexpected low energy seam TS was also found between $\mathbf{1 a}$ and $\mathbf{1 b}$, which occurs along a roaming atom reaction pathway (2b). ${ }^{21,75}$ Seam TS $\mathbf{2 b}$ was found using 11 or 13 GSM nodes, and has energy relative to the FC point of $-84.5 \mathrm{kcal} / \mathrm{mol}$. Two seam TSs were located (using the same string endpoints) due to a difference in step size during GSM growth, with 7 nodes having a larger step size than 11 nodes. Interestingly, GSM is able to locate the two paths of this bifurcating potential energy surface, a "long" path and a "short" path, by just adjusting the step size during string growth. Lastly, a seam TS $\mathbf{2 c}$ between tilt isomers of 1a has been reported ${ }^{46}$ and is reproduced here. This conical intersection is distinguished by a pyramidalized,
but not tilted methylene group. Seam TS 2c was found using 11 GSM nodes, and has an energy relative to the FC point of -84.1 $\mathrm{kcal} / \mathrm{mol}$.

The tests on the ethylene system demonstrate that GSM has significant exploratory ability, providing not only the Cl structures that are previously known, but an additional seam-space TS that has not been reported. The tests that follow will affirm these initial indications.

## Stilbene Conical Intersections

Compared to ethylene, stilbene has additional available photoreaction pathways due to the asymmetry around its central double bond. Stilbene is most stable in the trans conformation but can isomerize after absorption of a photon to cis via one-bond flip, cis via hula-twist, or ring-close to dihydrophenanthrene (DHP). The hula twist


Figure 2. Ethylene seam TS (STS) calculated using CAS(4,4)SCF/6-31G* with DE-GSM. Energies in $\mathrm{kcal} / \mathrm{mol}$ with respect to the Franck-Condon point. mechanism, which preserves the relative position of the phenyl groups has been hypothesized as favored for cis-trans isomerization in constrained media, as this mechanism reasonably preserves the molecular volume. ${ }^{73,76,77}$

For stilbene, cis-kinked (twisted pyramidalized ${ }^{78}$ ) and DHP-like MECI have been reported. ${ }^{79}$ For related polyene systems, such as butadiene and hexatriene, additional Cls have been found such as cis-kinked diene, trans-kinked diene and $\mathrm{H} /$ vinyl (H-bridging) MECl , as well as seam saddle points hypothesized to be responsible for the hula-twist mechanism. ${ }^{80}$ Analogies for all of these structures were found for stilbene using SE-GSM starting from a trans geometry. The driving coordinates and structures are shown Table 2 and Figure 3, respectively.

In total, five MECI (3a-3e) and one seam TS (3f) were located using SE-GSM (Figure 3). Additional seam TSs for the tilt seam coordinate (between 3a and 3c) and hydrogen transfer coordinate (between 3c and 3d) were found using DE-GSM (see Supporting Information). 3a and 3c are cis-kinked MECI analogous to twisted-pyramidalized MECI 1a, but differ from each other by the tilt of their phenyl ring with respect to the central double bond. $\mathbf{3 b}$ is the trans-kinked MECI related to CIs in polyenes, ${ }^{80}$ and was found by a one-bond flip of the central double bond. $\mathbf{3 d}$ is analogous to the ethylidene-like conical intersection $\mathbf{1 b}$ and leads to a reactive carbene intermediate or cis- and trans-stilbene. $3 \mathbf{e}$ is the DHP-like MECI which can ring-close to DHP. Lastly, $\mathbf{3 f}$ is related to the volume conserving hula-twist Cl reported by Houk et al for dienes, ${ }^{80}$ and was found using SE-GSM by rotation of the phenyl ring in $\mathbf{3 c}$. 3a and 3 e agree with structures reported in the literature. ${ }^{78,79}$ To our knowledge $\mathbf{3 b}$-3d and $\mathbf{3 f}$ have not been reported for stilbene, but they do resemble conical intersection geometries in dienes. ${ }^{73,80}$

Thus, a wide range of tilt and dihedral angles as well as degree of hydrogen bond transfer are present in the MECI and seam TSs, and these lead to different reaction possibilities. As can be

$\Delta \mathrm{E}\left(\mathrm{MECI}-\mathrm{S}_{1} \min \right)=-2.9$
3c

$\Delta \mathrm{E}\left(\right.$ MECI-S $\mathrm{S}_{1}$ min $)=-1.1$
3a

$\Delta E\left(\right.$ MECI-S $\left.{ }_{1} \min \right)=-29.9$
3d

$\triangle \mathrm{E}\left(\mathrm{MECI}-\mathrm{S}_{1} \min \right)=13.1$
3b

$\Delta \mathrm{E}\left(\right.$ MECI-S $\left.\mathrm{S}_{1} \min \right)=-9.2$
3e

$\Delta \mathrm{E}($ Seam TS-S min$)=7.7$

Figure 3. Stilbene conical intersections calculated using CAS(2,2)SCF/6-31G with SE-GSM. Energies in kcal/mol with respect to the $\mathrm{S}_{1}$ minimum. Atom numbers are driving coordinate indices (see Table 2).
seen in the Cl structures, $\mathbf{3 a - 3 c}$ flip the orientation of the phenyl groups (i.e. atoms 1 and 6 will land on the same side), whereas $3 f$ preserves the relative orientation of the phenyl groups with respect to each other. Therefore, $\mathbf{3 a - 3 c}$ are important for the one-bond flip mechanism, and $\mathbf{3 f}$ is predicted to be important for the hula-twist mechanism.

Importantly, a comparison of the driving coordinates (which are qualitative) to the (quantitative) dihedral angles of the MECIs (Figure 3) shows that prior quantitative details of these MECl geometries are unnecessary for their optimization via SE-GSM. Instead, the driving coordinates take the Franck-Condon initial geometry, perturb it in the direction of each of these MECls , and thus permit facile discovery of all 5 MECIs from the same starting structure. Together with the results from ethylene, the stilbene simulations demonstrate that GSM is effective at optimizing MECls and seam-space reaction pathways. In the next section, a more complex photoreaction will be studied to show the full power of MECl exploration using GSM.

Table 2. Stilbene MECI results from SE-GSM.

| Minimum Energy <br> Conical Intersection | Driving Coordinates | Driving <br> Cycles | MECI <br> cycles | $\phi(2,3,4,5)$ | $\phi(\mathrm{H} 3,2,3, \mathrm{H} 4)$ | $\phi(3,4,5,6)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3a | $\operatorname{TORSION}(2,3,4,5)=90$, <br> TORSION $(\mathrm{H} 3,3,4, \mathrm{H} 4)=0$ | 83 | 25 | 114.3 | 41.5 | -98.1 |
| 3b | $\operatorname{TORSION}(2,3,4,5)=90$ | 81 | 20 | 93.9 | 140.9 | 36.3 |


|  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $3 c$ | $\operatorname{TORSION}(2,3,4,5)=180$, <br> $\operatorname{TORSION}(H 3,3,4 \mathrm{H} 4)=90$ | 77 | 41 | 146.6 | 61.1 | -53.1 |
| 3d | $\operatorname{TORSION}(2,3,4,5)=120$, <br> $\operatorname{ADD}(\mathrm{H} 4,3), \mathrm{BREAK}(\mathrm{H} 4,4)$ | 95 | 18 | 84.5 | 114.4 | 179.4 |
| 3e | $\operatorname{TORSION}(\mathrm{H} 3,3,4, \mathrm{H} 4)=0$, <br> $\operatorname{TORSION}(2,3,4,5)=0, \operatorname{ADD}(1,6)$ | 119 | 11 | 21.4 | 16.7 | 10.7 |
| 3fa | $\operatorname{TORSION}(3,4,5,6)=-50$ | - | - | 137.9 | 71.1 | 47.9 |

aSeam transition state found from $\mathrm{MECI} \mathbf{3 c}$.

## Butadiene dimerization reaction discovery

Photochemical reactions with changes in covalent bonding are key challenges for simulation. In this space, reaction path discovery is possible with SE-GSM using driving coordinates that are systematically generated to sample many possible changes in bonding. To do this, the ZStruct reaction discovery method ${ }^{29-31}$ is used to combinatorially sample search directions based on bond addition and breaking coordinates, where SE-GSM completes the MECI optimizations. ZStruct has seen extensive use in ground-state reactions, ${ }^{81-87}$ and is applied here for the first time to photo-induced reactivity.

As a challenging test case, the dimerization of butadiene is studied ${ }^{32,33}$ as a complex photoreaction with many product channels. Under direct UV irradiation, butadiene has been observed to form 50\% 2-vinylbicyclo[3.1.0]hexane and/or 3-vinylbicyclo[3.1.0]hexane (I), 30\% 1,2-divinylcyclobutane (II), and 8\% cycloocta-1,5-diene (III). A fourth species accounting for the remaining product ( $\sim 10 \%$ ) was unidentified. While 1,3-divinylcyclobutane was not mentioned in the original study, it is possible that this was not separated from 1,2-divinylcyclobutane. Interestingly, this product distribution is markedly different than seen in triplet sensitization and thermal reactions. For example, 4-vinylcyclohex-1-ene ( V ) is a major product in triplet-sensitized reactions of butadiene and has also been observed in the thermal dimerization but does not appear in the UV chemistry. This diversity of products provides a great opportunity for reaction discovery simulations to provide details about the photoproduct generation mechanisms and corresponding Cl space.

SE-GSM and ZStruct method were applied to a pair of cis-butadiene molecules, which were promoted to their lowest energy excited state. ZStruct generated 120 combinations of driving coordinates for the dimerization reaction, considering all carbon, but not hydrogen, as reactive. Of these combinations, 37 produced unique MECI based upon root-mean-squared


Scheme 4. Experimental photoproduct distributions from ref. [42]. distances and coordinate connectivity metrics.

Because existence of an MECI does not guarantee its accessibility, multiple reaction paths to each MECl were considered, starting from the handful of local minima of the excited state surface

$\Delta \mathrm{E}\left(\mathrm{S}_{1}-\mathrm{S}_{1} \mathrm{~min}\right)=0.0$

## 4a


$\Delta \mathrm{E}\left(\mathrm{S}_{1}-\mathrm{S}_{1} \mathrm{~min}\right)=2.0$

$\Delta \mathrm{E}\left(\mathrm{S}_{1}-\mathrm{S}_{1} \mathrm{~min}\right)=9.8$


4d

$\Delta \mathrm{E}\left(\mathrm{S}_{1}-\mathrm{S}_{1} \min \right)=10.1$

Figure 4. Optimized geometries for $S_{1}$ minima located with $\operatorname{CAS}(8,8)$ SCF/6-31G* from aligned ZStruct structures. Energies in $\mathrm{kcal} / \mathrm{mol}$ with respect to the global $\mathrm{S}_{1}$ minimum, structure 4 a .
near the Franck-Condon points. From the initial ZStruct-aligned structures, five excited-state minima were located (Figure 4). $S_{1}$ minima $4 a$ and $4 b$ are tetraradicaloid and the lowest in energy. $\mathbf{4 b}$ is related to the so-called pericyclic minimum. ${ }^{33} 4 \mathrm{c}-4 \mathrm{e}$ minima have one radical from each molecule interacting with the other.

The reaction paths from the lower energy intermediates, $\mathbf{4 a}$ and $\mathbf{4 b}$, typically result in higher activation energies to reach the MECIs, compared to $4 \mathrm{c}-4 \mathrm{e}$. A typical case is shown in Figure 5. From 4b to the 5 -coordinate MECI ( $\mathbf{c - 1}$ in Supporting Information), the reaction


Figure 5. Reaction path analysis reveals that excited-state barrier depends on the binding of the dimers before reaching the MECI. Reaction paths were computed using DE-GSM with CAS $(8,8) \mathrm{SCF} / 6-31 \mathrm{G}^{*}$. The FC point is the aligned, but unoptimized planar monomers. path has an activation barrier of 12.0 $\mathrm{kcal} / \mathrm{mol}$, which is in agreement with previous results calculated using CAS(4,4)SCF/4-31G. ${ }^{33}$ The pathway, in contrast, is largely downhill from 4c, with a small barrier of $7.8 \mathrm{kcal} / \mathrm{mol}$. A similar effect is found in other pathways to reach the various MECI (see reaction pathways in SI section 3).

From the accessible MECI, photoproducts were optimized from the minima and maxima of the MECI branching plane cross-sections. In total, 12 energetically accessible constitutional isomers and their diastereomers were identified (Figure 6). Additional photoproducts were also identified but are not accessible due to having high energy MECI or large excited state activation barriers with respect to the $\mathrm{S}_{1}$ local minima.

All experimentally observed photoproducts, (I), (II), and (III) have at least one low energy pathway, as well as additional, higher energy pathways arising from differences in $\mathrm{S}_{1}$ minima, MECl or stereochemistry. Diastereomers of (I) form from a [3+2] cycloaddition, which upon ringclosing form an unstable methylene. The methylene carbon promptly ring-closes to form the resulting three-membered ring (see Figure 7). If the methylene and vinyl group are on the opposite sides of the 5 -membered ring, then (1S,2R,5R)-(I) or ( $1 \mathrm{~S}, 2 \mathrm{~S}, 5 \mathrm{R}$ )-(1) forms. When these groups are on same side, (1R,3s,5S)-(I) or (1R,3r,5S)-(I) forms. 4-vinylcyclohex-1-ene (V) also

(1S,2R,5R)-(I)
$\mathrm{Ea}(4 \mathrm{c})$ : 7.8
$\mathrm{Ea}(4 \mathrm{~b}): 12.0$

(1R,2S)-(II)
$\mathrm{Ea}(4 \mathrm{a}): 6.0$

(1Z,5Z)-(III)
Ea(4d): 2.8
$\mathrm{Ea}(4 \mathrm{~b}): 6.6$
$\mathrm{Ea}(4 \mathrm{e}): 11.3$

(1S,2S,5R)-(I)
$\mathrm{Ea}(4 \mathrm{a}): 11.9$

(1S,2S)-(II)
$\mathrm{Ea}(4 \mathrm{e}): 14.7$
$\mathrm{Ea}(4 \mathrm{a}): 22.1$

(1Z,5Z)-(III)
Ea(4a): 7.6
Ea(4b)': 38.8

(1R,3s,5S)-(I)
$\mathrm{Ea}(4 \mathrm{c}): 16.8$
$\mathrm{Ea}(4 \mathrm{a}): 28.5$

(1r,3r)-(II)
$\mathrm{Ea}(4 \mathrm{e}): 9.7$
Ea(4d): 16.2
$\mathrm{Ea}(4 \mathrm{e})$ ': 13.7

(IV)

Same as (III)

(1R,3r,5S)-(I)
$\mathrm{Ea}(4 \mathrm{c}): 18.7$
$\mathrm{Ea}(4 \mathrm{~b}): 26.6$

(1s,3s)-(II)
$\mathrm{Ea}(4 \mathrm{~d}): 10.0$
$\mathrm{Ea}(4 \mathrm{c})$ ': 13.4
$\mathrm{Ea}(4 \mathrm{a})^{\prime}: 23.3$

(V)

Same as (I)
Innaccessible photoproducts


Figure 6. Reaction products discovered using combinatorial reactive hypothesis generator ZStruct and single-ended GSM. Activation energies are in kcal/mol with respect to the labeled local minima. Ea' correspond to different MECI leading to the same product. Inaccessible products due to large reaction pathway barriers and high MECI energies.
arises from all MECI leading to the diastereomers of $(I)$ and therefore is produced from the same reaction pathways. (V) forms, however, from different initial directions leading away from the MECI funnel. Diastereomers of (II) form from rhomboidal [2+2] cycloaddition MECI which agree with previously reported MECI. ${ }^{33}$ The boat and chair conformations of cyclo-1,5-octadiene (III) arise from [4+4] cycloaddition MECl close to the initial geometries of $\mathbf{4 a}$ and $\mathbf{4 b}$. Bicyclo[5.1.0]oct-3-ene forms from the same MECI of (III) along different initial relaxation coordinates. Based on the results in Figure 6, the unidentified dimer (IV) from experiment is likely bicyclo[5.1.0]oct-3ene, which shares the same conical intersection as (III), and has similar yield ( $\sim 10 \%$ ).

These results are largely in agreement with available experimental results, but lead to an important question: why are there energetically accessible 4-vinylcyclohex-1-ene (V) pathways, but this species is not observed in experiment? A possible explanation comes from a reaction path to the MECl that gives $(\mathrm{V})$ and ( I$)-(1 \mathrm{R}, 3 r, 5 \mathrm{~S})$, which contains a nearby extended seam (Figure $7 a)$. The first accessible Cl along this seam is a minimum distance conical intersection (MDCI), ${ }^{43}$ which would be the first Cl approached along this path starting from the S 1 minimum.

The photoproducts of this $(\mathrm{V}) /(\mathrm{I})$ reaction path are shown in Figure 7b. (I)-(1R, $3 \mathrm{r}, 5 \mathrm{~S}$ ) arises from the maxima of the MECI cross-section, and $(\mathrm{V})$ from the minima. In the latter case, the biradical recouples in a [4+2] arrangement. At the MDCI, which considerably differs in bond length A from the MECI, forms (I) or returns to the reactant structure without producing photoproduct. The MDCI can revert to reactants because carbon-carbon bond $\mathbf{A}$ has not yet been formed and therefore the geometry does not recouple to form (V). Thus, we hypothesize that decay at the MDCl , rather than the MECI , prevents the formation of (V).

In arene-alkene cycloaddition, the seam TS connecting [3+2] cycloaddition MECI has been hypothesized to be responsible for para ([4+2]) selectivity. ${ }^{10}$ In butadiene dimerization, however, it is possible that the seam contains high energy points that prevent [4+2] dimerization (Figure 7b). Therefore, to provide additional insight, a SE-GSM seam calculation was performed (Figure 7c) from the MECI in Figure 7a using a breaking carbon-carbon bond $\mathbf{A}$ and a forming carbon-carbon bond $\mathbf{B}$ as driving coordinates. The SE-GSM seam method was necessary since the $[3+2] \mathrm{MECl}$ with carboncarbon bond $\mathbf{A}$ was not found in the MECI search using ZStruct, and therefore no DE-GSM seam could be optimized. Notably, unlike the seam in arene-alkene cycloaddition that contains a lowlying seam TS and MECI along this coordinate, ${ }^{10}$ no such TS or MECI was located, which is consistent with the SE-GSM and ZStruct findings. Thus, the seam landscape is significantly different from the arene-alkene cycloaddition
(a)

(b)


(c)


Figure 7. (a) Reaction path from $\mathbf{4 c}$ to MECI leading to (I)$1 \mathrm{r}, 3 \mathrm{~s}, 5 \mathrm{~s}$ and $(\mathrm{V})$ products that shows ground and excitedstate merging to form a seam and a minimum distance CI (MDCI) (b) photoproducts from the minimum and maximum of the CI branching plane cross-section for the MECI and MDCI (c) SE-GSM seam using breaking bond A and adding bond B driving coordinate. and may be the source of the difference in reactivity. Future studies including dynamics will be valuable to better investigate how the extended seam affects photoproduct distributions.

## Conclusions

The growing string method is a powerful tool for reaction path optimization, and this tool has been herein enabled to search for conical intersections and seam space reaction pathways. These methods provide a useful platform for studying photochemical reactions and have the important
distinction of being useful even when little prior knowledge of the photochemical reaction pathways is available.

GSM located new excited state reaction pathways even in the well-understood ethylene and stilbene isomerization reactions. In addition, a combination of GSM with ZStruct was able to systematically explore reaction possibilities for the photodimerization of butadiene. The major, experimental photoproducts were found in the set of computed, energetically accessible products. The unidentified product in the experiment is likely bicyclo[5.1.0]oct-3-ene, since it shares the same conical intersection as cycloocta-1,5-diene and has similar yield. Interestingly, a non-stationary point on the seam, explored using GSM, is found to be important in the formation (or lack thereof) of 4 -vinylcyclohex-1-ene. We anticipate that continued applications of the ZStruct/GSM combination will be useful to map Cl spaces in emerging, complex photoreactions.

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## Table of contents



A new reaction discovery technique for photochemical reactions is herein used to explore complex intersections and predict product selectivity.

