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Dynamic Scaling of Ferromagnetic Micro-rod Clusters under a Weak Magnetic Field

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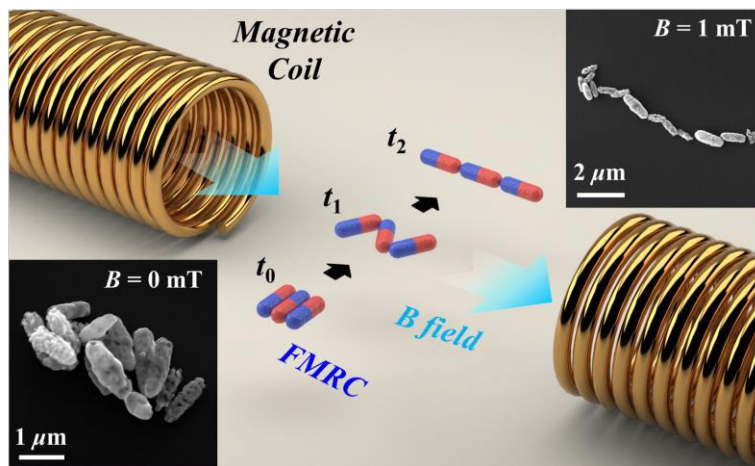
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ABSTRACT

A controlled configurational change of micro-clusters in suspensions is essential for many smart material applications. In this paper, the dynamic process of ferromagnetic microrod clusters (FMRCs) under an external magnetic field was studied as a function of the cluster size N and the applied field B . The FMRCs rearranged from a side-by-side raft-like structure to an end-to-end chain-like structure, originated from coupled motions through the field-driven alignment of both ferromagnetic microrods and FMRCs. A theoretical model based on an extension of a *zig-zag* chain was developed, and both the cluster length and orientation could be characterized by a retardation time constant τ , with a relationship $\tau \sim N^2/B$, which agrees well with the experimental results, $\tau \sim N^{2.2 \pm 0.2}/B^{0.8 \pm 0.1}$. Such a model can be used to predict other cluster dynamics or the magneto-elastic behavior of other soft matters consisting of FMRCs.

TOC GRAPHIC



INTRODUCTION

Dynamic response of magnetic micro-/nano- particles suspended in fluids under an external magnetic field has attracted decades of attentions, because of its potential applications in biosensors,¹⁻³ microfluidic actuators,⁴⁻⁷ tunable optical and thermal filters,⁸⁻¹² micro-fiber fabrication,¹³⁻¹⁵ and programmable smart materials.¹⁶⁻¹⁸ Most of these applications are related to the anisotropic growth of one-dimensional clusters by magnetic particles under an external magnetic field B , which has been studied both experimentally and theoretically.¹⁹⁻³⁰ For superparamagnetic particles, they are treated to be nonmagnetic with the absence of B -field and are uniformly suspended in the liquid due to Brownian motion; when a B -field is applied, the particles are magnetized and their magnetic energy overcomes the thermal energy, leading to the aggregation of the particles along the B -field direction. The average chain length $L(t)$ is found to follow a power law with respect to time t , *e.g.*, $L(t) \propto t^Z$, where Z is the dynamic exponent.^{20-22, 24} When the B -field is removed, the magnetic interaction among the aggregation of particles vanishes and individual particles are re-suspended in the liquid. However, for ferromagnetic particles (FMPs), even without an external B -field, they naturally aggregate to form worm-like clusters due to their remnant magnetization and interactions.^{19, 31-32} When a B -field is applied, the original clusters will experience a configuration change, *i.e.*, there is a tendency for the clusters to uncurl and align in the B -field direction, due to the magnetic interaction between the particles and the external B -field.^{19, 32} Meanwhile, clusters will merge to form longer clusters, which also makes $L(t)$ increase as a power law with respect to t .³³ On the other hand, more complex structures in two dimensions and three dimensions can be formed by spherical particles with decentered magnetism, such as Janus magnetic particles³⁴ and capped magnetic particles.³⁵ Specifically, the orientation of the decentered magnetism can be either in radial direction or in tangential direction of the spherical

particles, whose structural transition from ground state to finite thermal fluctuation has been well studied by theoretical and numerical approaches.³⁶⁻³⁷

In addition, the geometric shape of the fundamental magnetic components plays a very important role in their dynamic response to a magnetic field, possibly leading to unique mechanical properties of the bulk material manipulated in external magnetic fields.³⁸⁻³⁹ In most published works, the magnetic components in a micro cluster are spherical particles with isotropic volume exclusion. As a result, there is no orientation effect of individual particles during particle clustering under an external B -field, though the formed clusters still experience a configuration change. However, when the FMPs become anisotropic, such as a rod shape, the clustering of ferromagnetic rods (FMRs) will become much more complicated compared to that of spherical particles due to their anisotropic magnetic interaction resulting from the uniaxial magnetic isotropy,⁴⁰⁻⁴¹ and anisotropic volume exclusion. Though extensive efforts have focused on their unique properties and applications,^{28, 42-44} the clustering of FMRs is not well understood to the best of our knowledge. Aoshima and Satoh have conducted a two-dimensional (2D) Monte Carlo simulation on the clustering of FMRs without an external B -field.⁴⁵ They found that the FMR aggregations consist of a few fundamental structures, such as anti-parallel particle pairs, raft-like clusters, and triangle-loop-like clusters. Particularly, the raft-like cluster is more stable than other structures when the aspect ratio of FMRs is larger than 2, which has been experimentally obtained by the dispersion of Nickel nanorods in poly (2-vinylpyridine) (PVP) solution.⁴⁶⁻⁴⁷ They also investigated the influence of an external B -field on the rod clustering *via* a 2D Monte Carlo simulation.³² It was found that adjacent FMRs align end-to-end along the B -field direction, forming two types of joints, a step-like structure in high concentration suspension and a chain-like structure in low concentration suspension. According to the simulation results, an appreciable extension of the

individual rod clusters is expected due to the anisotropic volume exclusion between rods when an external B -field is applied. However, the dynamic extension of ferromagnetic rod clusters (FMRCs) has not been investigated either experimentally or theoretically under the external B -field and the mechanism is unknown. In this paper, we conducted a systematic study on the dynamic behavior of individual FMRCs under an external B -field. For the same cluster, the dynamic changes of both the cluster length and the orientation follow the same retardation time, and the retardation time obeys a scaling law of the maximum cluster size and the applied B -field. Based on a *zig-zag* chain structure, a theoretical model is proposed which can predict the experimental dynamics very well.

EXPERIMENTAL METHODS

The precursors of ferromagnetic micro-rods were synthesized by a solvent-thermal method,⁴⁸ then annealed in air to remove the organic compounds, and in ethanol/ N_2 to reduce to Fe_3O_4 . $Fe(NO_3)_3 \cdot 9H_2O$ (0.7575 g) and glucose (0.5 g) were thoroughly dissolved into ethylene glycol (75 ml). Then the mixture was transferred into a 100 ml Teflon-lined stainless steel autoclave and maintained at a temperature of 220°C for 12 h. The product was collected by centrifugation, and washed twice with absolute ethanol then dried in an oven at 65°C overnight. Secondly, the microrod-shaped precursors were annealed at 600°C for 2 h in air to obtain α - Fe_2O_3 microrods. Finally, the Fe_3O_4 microrods were prepared by annealing the α - Fe_2O_3 rods at 350°C for 1 h in ethanol-carried N_2 flow. The crystal structures of as synthesized FMRs were characterized by an X-ray diffractometer (XRD; PANalytical X'Pert PRO MRD) with a Cu $K\alpha$ source ($\lambda = 1.5405980 \text{ \AA}$) at 45 kV and 40 Ma (see the Supporting Information S1). The scanning electron microscope (SEM) image in Figure 1a reveals that each rod is a porous cylinder with hemispherical ends. The length of the rods $l = 1.0 \pm 0.3 \text{ }\mu\text{m}$, the diameter of the rods $d = 0.35 \pm 0.09 \text{ }\mu\text{m}$, and the

aspect ratio of the rods $\gamma = l/d = 2.9 \pm 0.4$ (see the Supporting Information Fig. S1). According to Butler and Banerjee's theory, the size of a single-domain particle with aspect ratio of $\gamma = 3$ is up to $0.8 \mu\text{m}$.⁴⁹ It implies that some of the FMRs in our experiments may have multiple-domains with a field dependent magnetization process. However, the dynamic response of the domain walls (rotation or reorientation) to an external magnetic field is normally less than 100 ns.⁵⁰⁻⁵² Comparing with the time scale of the cluster motion (~ 100 ms), we can safely neglect the influence of the rod magnetization process on the cluster motion and consider the rod as a single-domain magnetic particle in our model. A measurement by a vibrating sample magnetometer (VSM) (Figure 1b) demonstrated that the residual magnetization of each rod was $m = 20 \text{ emu} \cdot \text{g}^{-1}$ (or 10^5 A/m) and the saturated magnetization was $70 \text{ emu} \cdot \text{g}^{-1}$ (or $3.5 \times 10^5 \text{ A/m}$). The hysteresis ratio of the saturated magnetization to the residual magnetization is around 0.3, which is lower than the theoretical value of 0.5 predicted by the Stoner-Wohlfarth model. This could be caused by the existence of small particles ($< 100 \text{ nm}$) that were broken down from the rods during the annealing process in the test sample (see the Supporting Information Fig. S2).⁵³

The rods were suspended in deionized water to achieve a mass concentration of $0.1 \text{ mg} \cdot \text{ml}^{-1}$, corresponding to a volume fraction $\phi \approx 2 \times 10^{-5}$. A $10 \mu\text{l}$ droplet of rod suspension was dispensed in a well on a clean silicon substrate and covered by a glass slide. The well was made of a $100\text{-}\mu\text{m}$ thick ring-shaped plastic spacer and had a 12.7 mm inner diameter. Through an optical microscope (Mitituya FS110), most of the rod clusters were suspended uniformly in the suspension like black scattered dots when $B = 0 \text{ mT}$ (Figure 1c). When a B -field ($B = 0.2 \text{ mT}$) was applied, the clusters were quickly transformed from circle dots into linear chains lying along the B -field direction (Figure 1d). Such a dynamic process was recorded at 200 fps by a CCD camera (SLAM Solutions,

Phantom v9.1). From the video (see the Supporting Information Movie), the clusters maintained separation from each other and no cluster-cluster aggregation was observed.

RESULTS AND DISCUSSION

Figure 2a shows the snapshots of an extension process of a FMRC at every 10 ms under $B = 1$ mT. The first frame shows the initial appearance of the FMRC, which was a circular shape ($t = 0$ ms); when $B = 1$ mT was applied (in the direction of the white arrow), the cluster was first transformed into a crescent shape ($t = 10$ and 20 ms), then the crescent was opened to form a short arc ($t = 30, 40$, and 50 ms), and eventually the arc was extended to a straight chain ($t = 60, 70, 80$, and 90 ms). During this configurational change, the orientation of the cluster kept approaching the B -field direction as indicated by red arrows in Figure 2a. To quantitatively characterize the dynamics of the cluster, we defined λ to be the normalized length of the cluster at time t , $\lambda = \frac{L}{L_s}$,

where L is the instant length and L_s is the saturated (maximum) length of the cluster, and the orientation of the cluster φ is the included angle between the cluster (indicated as red arrows) and the B -field. Figure 2b plots λ and φ versus time t extracted from the movie's frames (Figure 2a) (similar plots can be extracted from the movie frames of different clusters under different B -field, in the Supporting Information S2). When t increases from 0 to 60 ms, λ increases sharply from its initial value around 0.3 to 0.9. When $t > 60$ ms, λ gradually approaches to a constant value of 0.971. Eventually ($t > 100$ ms), λ fluctuates around this constant value. On the other hand, φ decreases from 1.3 concavely, approaching to 0, when t changes from 0 ms to 150 ms. At $t > 150$ ms, φ fluctuates around $\varphi = 0$. Both the fluctuations of λ and φ at large t are caused by the Brownian diffusion of the magnetic chain.⁵⁴ Both Figure 2a and 2b reveal the dynamic transformation of the cluster to be an extension-rotation coupled motion. Such a cluster extension and reorientation are

caused by the re-arrangement of the rods in the cluster during the application of the external B -field, and is indirectly confirmed by the SEM images of FMRCs with and without the presence of B -field, shown in Figure 2c and 2d, respectively. These SEM samples were prepared by air-drying the FMRC suspensions on the silicon substrates under $B = 0$ mT and $B = 1$ mT, respectively. When $B = 0$ mT, Figure 2c shows that the rods are stacked side by side to form a raft-like cluster while some rods may form multiple layers on top of the “raft”. This indicates that the rods prefer to pack closely along their long axes, and form a relatively small cluster size. Such a structural feature is consistent to the previous experimental observation and simulation.⁴⁵⁻⁴⁷ When $B = 1$ mT, the cluster in Figure 2d is composed mostly of a single chain with adjacent rods linked end to end, which is predicted by the Monte Carlo simulation.³² Only a few small rods are packed side by side at the ends of the chain, either due to the capillary effect during the drying process, or their interaction is so strong that the $B = 1$ mT field cannot extend them.

Clearly, the dynamic behavior under an external B -field shown in Figure 2b is due to the configuration change of FMRCs revealed by Figure 2c and 2d, which can be treated as an unfolding process. Such unfolding dynamics of scaffolding structures widely exists in biomaterials from micrometer scale to molecular level, such as polymers⁵⁵⁻⁵⁶ and proteins⁵⁷⁻⁵⁹, and has been closely connected to their viscoelasticity. Theoretically, the unfolding process of these biomaterials are described by either a freely-jointed chain model⁶⁰ or a worm-like chain model⁶¹. Similarly, the λ and φ curves (Figure 2b) exhibit the typical viscoelastic features in response to the external B -field, and the SEM images shown in Figure 2d implies that the extended cluster behaves like a freely-jointed chain based on magnetic interaction. Thus, we propose a freely-jointed chain model to describe this dynamic process. Figure 3a illustrates the basic idea of the model with a cluster of three FMRs. When $B = 0$ mT, the three FMRs form a side-by-side cluster, with the

adjacent magnetic moment \vec{m} pointing to the opposite direction (left sketch in Figure 3a, magnetic charge indicated by the + and - signs). When an external B -field is applied, both the FMRs and the orientation of the cluster (center-to-center direction of FMRs as indicated by the dash-dotted lines in the middle sketch of Figure 3a) are driven to be aligned towards the B -field direction, and the cluster becomes a *zig-zag* chain. After sufficient time, the cluster is extended to a linear chain cluster as shown in the right sketch of Figure 3a. Thus, the extension and reorientation of the FMRCs is essentially caused by the spinning of each FMR and the rotation of the entire cluster, respectively. The two rotatory motions are associated with two angles, the angle between the cluster axis and the B -field direction ϕ and the included angle between the long axis of the rod and the principle axis of the chain θ , as indicated in Figure 3(a). During the extension, both ϕ and θ keep decreasing while the cluster translates from a side-by-side chain to an end-to-end chain aligned in the direction of the B -field. To account for the magnetic interactions between FMRs and to simplify the mathematical treatment, we also make the following assumptions: (i) Each rod is treated as a single domain particle with the same shape, dimension and magnetic moment m along its long axis; (ii) All the rods in one cluster are arranged in a *zig-zag* chain structure with the same θ at any time t ; (iii) There is no translational motion of the entire magnetic cluster due to the uniformity of magnetic field ($\nabla B = 0$); (iv) The magnetic interactions among clusters are neglected due to the low volume fraction of rods ($\phi \approx 2 \times 10^{-5}$) and the thermal fluctuation of the particle is neglected due to the dominance of the magnetic energy during the structural transition ($mB / \kappa_B T \geq 500$, where κ_B is Boltzmann's constant and T is the room temperature); (v) Each cluster consists of $2N+1$ FMRs, so that we only need to analyze the dynamics of FMRs in one half of the cluster due to the symmetry of the *zig-zag* chain (a similar derivation for $2N$ FMRs has also been developed in the Supporting Information S3).

Since the magnetic moment \vec{m} of two neighboring rods has different orientation, we shall consider the rods in pairs, i.e., the p^{th} rod and the $(p+1)^{\text{th}}$ rod as shown in Figure 3b. At the center of the p^{th} ($(p+1)^{\text{th}}$) rod, there are hydrodynamic force components $\vec{F}_{D_{\perp}}^p$ ($\vec{F}_{D_{\perp}}^{p+1}$) and $\vec{F}_{D_{\parallel}}^p$ ($\vec{F}_{D_{\parallel}}^{p+1}$), which are perpendicular and parallel to the principle axis of the cluster. Here $\vec{F}_{D_{\parallel}}^p = -\eta \varepsilon_{\parallel} \vec{U}_{\parallel}^p$ and $\vec{F}_{D_{\perp}}^p = -\eta \varepsilon_{\perp} \vec{U}_{\perp}^p$, where η is the viscosity of the carrier liquid, ε_{\parallel} and ε_{\perp} is the hydrodynamic drag coefficients in the direction of \vec{U}_{\parallel}^p and \vec{U}_{\perp}^p , and \vec{U}_{\parallel}^p and \vec{U}_{\perp}^p is parallel and perpendicular velocity with respect to the chain axis, respectively, $\vec{U}_{\parallel}^p = -pl\dot{\theta} \sin \theta \hat{x}$ and $\vec{U}_{\perp}^p = -pl\dot{\phi} \cos \theta \hat{y}$. Based on a magnetic charge model,³² two magnetic force \vec{F}_m^{p+} and \vec{F}_m^{p-} (note that $F_m^{p+} = F_m^{p-} = F_m$) at the + and - ends are presented due to the magnetic polar attraction of the adjacent ends. There are also a normal force \vec{F}_n^{p+} (or \vec{F}_n^{p-}) and a frictional force \vec{F}_f^{p+} (or \vec{F}_f^{p-}) exerted at the interfaces of the + (or -) end due to the contacting interaction and relative motional tendency between the neighboring rods. Under hydrodynamic equilibrium for a low Reynold number fluid, we have,

$$\vec{F}_n^{p+} + \vec{F}_n^{p-} + \vec{F}_{D_{\parallel}}^p = 0, \quad (1)$$

$$\vec{F}_f^{p+} + \vec{F}_f^{p-} + \vec{F}_{D_{\perp}}^p = 0, \quad (2)$$

$$\vec{\Gamma}_m^p + \vec{\Gamma}_r^p = 0, \quad (3)$$

where $\vec{\Gamma}_m^p$ is the magnetic driven torque $\vec{\Gamma}_m^p = \vec{m} \times \vec{B} = mB \sin(\varphi + \theta) \hat{z}$, and $\vec{\Gamma}_r^p$ is the resistant

torque, $\vec{\Gamma}_r^p = -\left\{ (F_f^{p-} + F_f^{p+}) \frac{l}{2} \cos \theta + \left[(F_n^{p-} - F_m^{p-}) + (F_n^{p+} - F_m^{p+}) \right] \frac{l}{2} \sin \theta \right\} \hat{z}$. Similarly

equations can be derived for the $(p+1)^{\text{th}}$ rod, but with different expressions for

$\vec{\Gamma}_m^{p+1} = mB \sin(\varphi - \theta) \hat{z}$ and

$$\vec{\Gamma}_r^{p+1} = - \left\{ \left(F_f^{(p+1)-} + F_f^{(p+1)+} \right) \frac{l}{2} \cos \theta - \left[\left(F_n^{(p+1)-} - F_m^{(p+1)-} \right) + \left(F_n^{(p+1)+} - F_m^{(p+1)+} \right) \right] \frac{l}{2} \sin \theta \right\} \hat{z} .$$

Furthermore, for the p^{th} and $(p+1)^{\text{th}}$ rod pair, one has $\vec{\Gamma}_m^p + \vec{\Gamma}_m^{p+1} = -(\vec{\Gamma}_r^p + \vec{\Gamma}_r^{p+1})$ and

$\vec{\Gamma}_m^p - \vec{\Gamma}_m^{p+1} = -(\vec{\Gamma}_r^p - \vec{\Gamma}_r^{p+1})$. By considering the fact that $F_f^{p+} = F_f^{(p+1)-}$, $F_n^{p+} = F_n^{(p+1)-}$, $F_m^{p+} = F_m^{(p+1)-}$,

we have

$$2mB \sin \varphi \cos \theta = \left(F_f^{p-} + 2F_f^{(p+1)-} + F_f^{(p+1)+} \right) \frac{l}{2} \cos \theta - \left(F_n^{(p+1)+} - F_n^{p-} \right) \frac{l}{2} \sin \theta , \quad (4)$$

$$2mB \cos \varphi \sin \theta = \left[\left(F_n^{(p+1)+} - F_m^{(p+1)+} \right) + 2 \left(F_n^{(p+1)-} - F_m^{(p+1)-} \right) + \left(F_n^{p-} - F_m^{p-} \right) \right] \frac{l}{2} \sin \theta - \left(F_f^{(p+1)+} - F_f^{p-} \right) \frac{l}{2} \cos \theta . \quad (5)$$

In addition, by summarizing Eqs. (1) and (2) from the $(p+1)^{\text{th}}$ rod to the N^{th} rod, respectively, and

considering the force equilibrium at the N^{th} rod as shown Figure 3b, we have $-\vec{F}_f^{(p+1)-} = \sum_{k=p+1}^N \vec{F}_{D_{\perp}}^k$ and

$-\vec{F}_n^{(p+1)-} + \vec{F}_m^{(p+1)-} = \sum_{k=p+1}^N \vec{F}_{D_{\parallel}}^k$. Therefore, Eqs. (4) and (5) becomes

$$2mB \sin \varphi \cos \theta = \left(\sum_{k=p+2}^N F_{D_{\perp}}^k + 2 \sum_{k=p+1}^N F_{D_{\perp}}^k + \sum_{k=p}^N F_{D_{\perp}}^k \right) \frac{l}{2} \cos \theta - \left(F_n^{(p+1)+} - F_n^{p-} \right) \frac{l}{2} \sin \theta , \quad (6)$$

$$2mB \cos \varphi \sin \theta = \left(\sum_{k=p}^N F_{D_{\parallel}}^k + 2 \sum_{k=p+1}^N F_{D_{\parallel}}^k + \sum_{k=p+2}^N F_{D_{\parallel}}^k \right) \frac{l}{2} \sin \theta - \left(F_f^{(p+1)+} - F_f^{p-} \right) \frac{l}{2} \cos \theta . \quad (7)$$

Then, eventually by simply summarizing Eqs. (6) and Eq. (7) over all the rod pairs throughout the

cluster, all the $F_n^{(p+1)+}$, F_n^{p-} , $F_f^{(p+1)+}$, and F_f^{p-} terms are vanished, and the expressions can be

further simplified as (see details in the Supporting Information S3)

$$\begin{cases} \dot{\theta} = -\left(\frac{3mB}{\varepsilon_{\parallel}\eta l^2 N^2}\right) \frac{\cos \varphi}{\sin \theta} \\ \dot{\varphi} = -\left(\frac{3mB}{\varepsilon_{\perp}\eta l^2 N^2}\right) \frac{\sin \varphi}{\cos \theta} \end{cases}. \quad (8)$$

When Stokes flow passes a circular cylinder of small aspect ratio ($\gamma \leq 10$), like the rod in our experiment, the ratio of the hydrodynamic drag coefficients in its long axial direction and in its short axial direction is about 1,⁶²⁻⁶³ i.e., $\varepsilon_{\parallel} = \varepsilon_{\perp} = \varepsilon$. According to the geometrical relations in Figure 3b, the normalized length of the chain is approximately estimated to be $\lambda \approx \cos \theta$. Therefore, Eq. (8) is furtherly simplified as

$$\begin{cases} \dot{\lambda} = \frac{\cos \varphi}{\tau} \\ \dot{\varphi} = -\frac{\sin \varphi}{\tau \lambda} \end{cases}, \quad (9)$$

where $\tau = \frac{\varepsilon \eta l^2 N^2}{3mB}$. Clearly, the extending and the rotating motions of the rod cluster are coupled together and both of their transient speeds depend on the same parameter τ . Equation (9) can be solved analytically (see details in the Supporting Information S4)

$$\begin{cases} \lambda(t) = \sqrt{\left[\left(\frac{t}{\tau}\right) + c_1\right]^2 + c_2}, \lambda(t) \leq 1 \\ \varphi(t) = \cot^{-1} \left[c_3 \left(\frac{t}{\tau}\right) + c_4 \right] \end{cases}, \quad (10)$$

where $c_1 = \lambda_0 \cos \varphi_0$, $c_2 = \lambda_0^2 \sin^2 \varphi_0$, $c_3 = \lambda_0^{-1} \csc \varphi_0$ and $c_4 = \cot \varphi_0$, and λ_0 and φ_0 are the initial values for the cluster. The parameter τ has an apparent physical meaning, which describes the competition between the hydrodynamic drag torque and the magnetic torque on a FMRC. It decides the speed of FMRC structural transition by a B -field and is more complicated than the classic Brownian relaxation time constant of a single magnetic particle.⁶⁴⁻⁶⁵ The larger τ suggests

the longer elapsed time for the coupled motion of the cluster. When $t \ll \tau$, $\lambda(t)$ increases slowly from λ_0 and $\varphi(t)$ decreases rapidly from φ_0 . When $t \gg \tau$, $\lambda(t)$ increases linearly with respect to t until it reaches 1 and $\varphi(t)$ slowly approaches to 0. Equation (10) is used to fit the data in Figure 2b, and both the blue and pink dash curves represent the best fittings for $\lambda(t)$ and $\varphi(t)$, respectively. The retardation time τ_λ extracted from the $\lambda(t)$ fitting is 30 ± 2 ms, and the retardation time τ_φ extracted from the $\varphi(t)$ fitting is 29 ± 2 ms, i.e., $\tau_\lambda \approx \tau_\varphi$. Thus the theoretical prediction agrees with experimental data very well.

According to our model, the retardation time τ is proportional to N^2 and inversely proportional to B . Figures 4a and 4b plot the τ_λ (red circle) and τ_φ (black square) extracted from different magnetic cluster with different length at $B = 0.2$ mT and 1.0 mT, respectively. Both figures show that τ_λ and τ_φ increases monotonically with $N_{rod} = L_s / l$. A power law relationship, $\tau(N) \sim N^\alpha$, is used to fit these data. For $B = 0.2$ mT, one obtains $\alpha_\lambda = 2.1 \pm 0.3$ (red dash curve) and $\alpha_\varphi = 2.4 \pm 0.3$ (black dash curve); for $B = 1.0$ mT, $\alpha_\lambda = 2.0 \pm 0.2$ (red dash curve) and $\alpha_\varphi = 1.9 \pm 0.2$ (black dash curve). Clearly the exponent α fluctuates around 2.0. In fact, experimentally we extract α_λ and α_φ for $B = 0.2, 0.4, 0.6, 0.8$ and 1.0 mT, and they are plotted against B in Figure 4c. Both α_λ (red circle) and α_φ (black square) remain constant and the statistical average of all exponent values (including α_λ and α_φ) is $\alpha = 2.2 \pm 0.2$ (pink dash line), which agrees well with the theoretical value, $\alpha = 2$ (blue dash line). The relation of τ versus B is also plotted in Figure 4d. Here we select two groups of clusters with $N_{rod} = 11 \pm 0.5$ and $N_{rod} = 12 \pm 0.5$, and τ is the average value of the retardation time constants from both τ_λ and τ_φ . The τ decreases monotonically with B . By fitting the two data sets with a power law, $\tau(B) \sim B^\beta$, we obtain that $\beta = -0.8 \pm 0.1$, which is quite close to the theoretical expectation of $\beta = -1$. Thus, the model based on the *zig-zag* chain extension and rotation describes the dynamic extension of the magnetic cluster of FMRs very well.

CONCLUSIONS

In summary, we have studied in detail the dynamic process of FMRCs under an external magnetic field, and developed a theoretical model based on a *zig-zag* chain to explain the extending-rotating coupled motion of FMRCs. The origins of this coupled motion come from the field-driven alignment of both FMRs and FMRCs, accompanied with the rearrangement of FMRCs from the side-by-side raft-like structure to the end-to-end chain-like structure. The retardation time constant τ derived from the dynamic data of FMRCs of different chain length is inversely proportional to B -field, and is a square function of the chain length N , which are consistent with the theoretical prediction. It is expected that this model can be adapted for the dynamics of magnetic clusters consisted of other anisotropic magnetic particles as well as magneto-elastic behavior of other soft matters consisting of FMRCs.

SUPPORTING INFORMATION

Details of the FMRs synthesis, XRD and statistic dimensions of the FMRs, more representative plots of the FMRCs' dynamics, and the mathematical derivation of FMRC governing equations. This material is available free of charge via the Internet at <http://pubs.acs.org>.

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FIGURE LIST

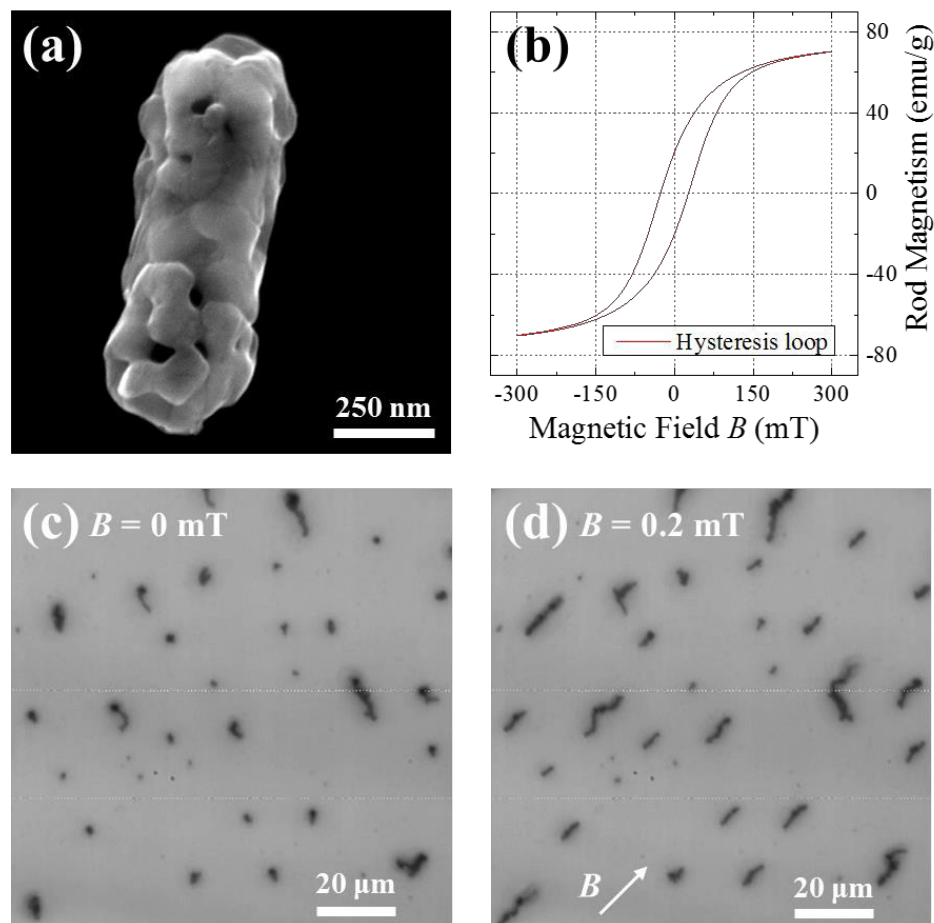


Figure 1 (a) A representative SEM image of a single Fe_3O_4 microrod. (b) The magnetic hysteresis loop of Fe_3O_4 microrods. An optical microscope image of rod clusters at (c) $B = 0$ mT and (d) $B = 0.2$ mT. The B -field direction is indicated as a white arrow.

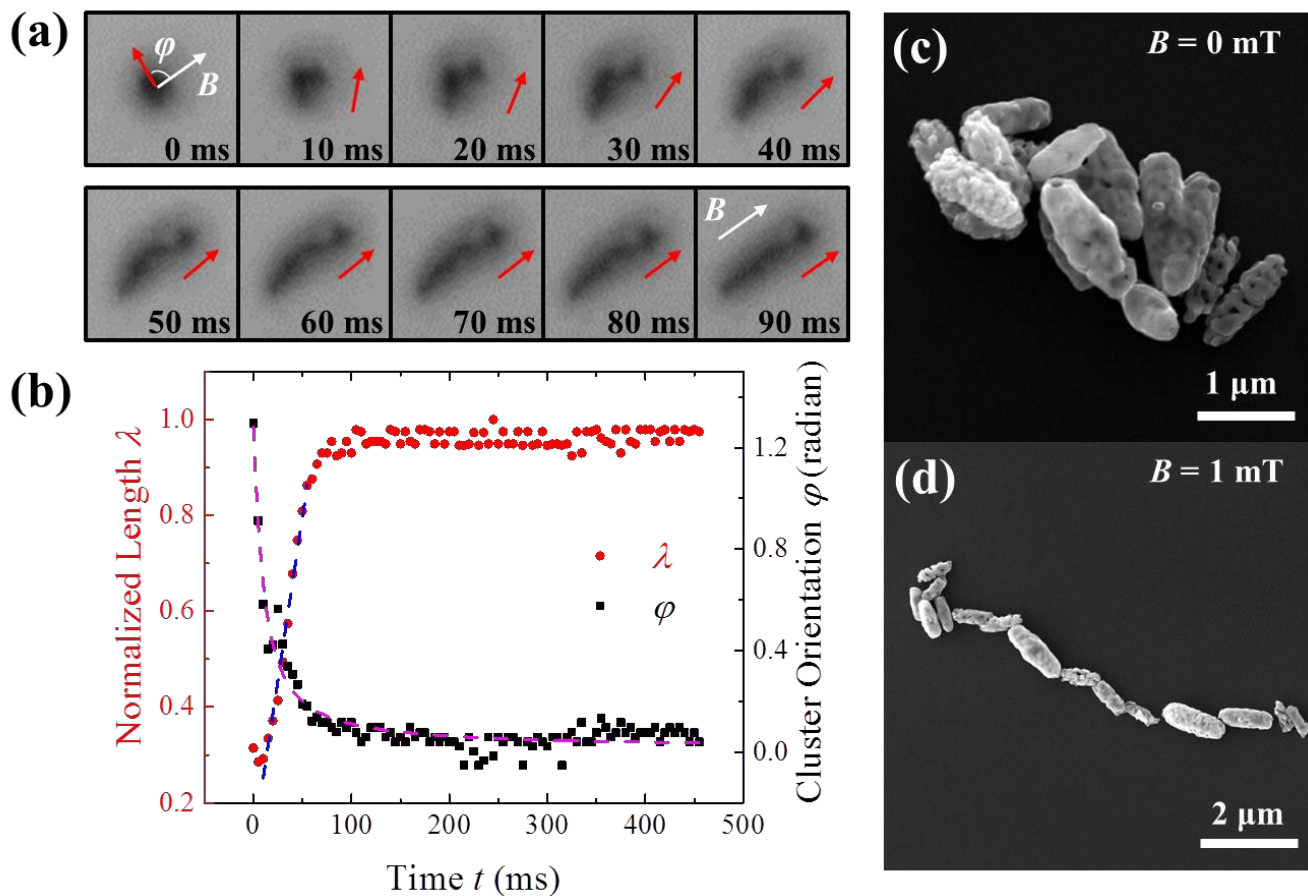


Figure 2 (a) Representative video frames of the extension-rotation coupling motion of a FMRC with $L_s = 9 \mu\text{m}$ at $B = 1$ mT. (b) The plots of the normalized length λ (red circle) and the orientation ϕ (black square) with respect to time t , extracted from the magnetic cluster shown in (a). The dash curves are the fitting results. Representative SEM images of a FMRC at (c) $B = 0$ mT, and (d) $B = 1$ mT.

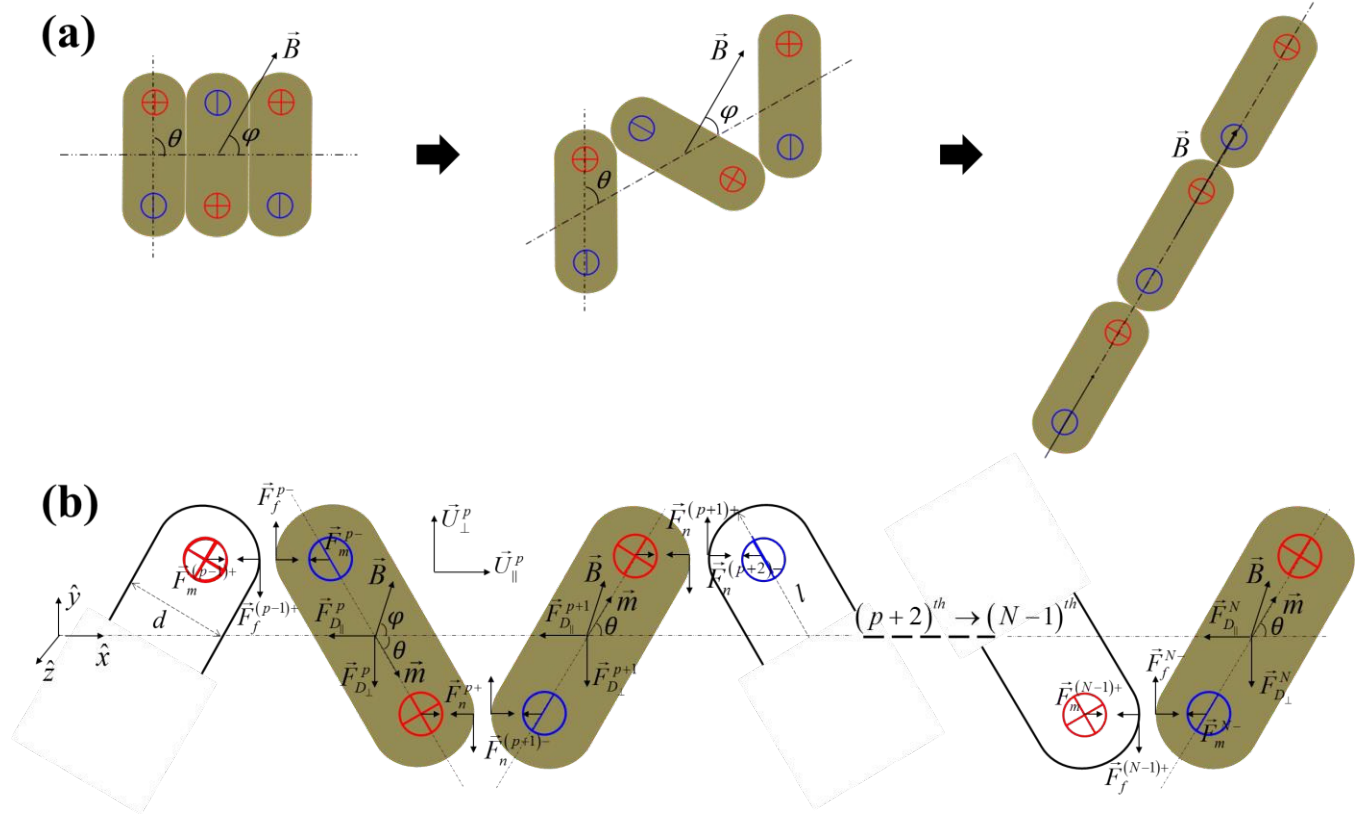


Figure 3 (a) The proposed dynamic process for a side-by-side chain to be extended to an end-to-end chain *via* a zig-zag chain model triggered by an external B -field. (b) Force and torque analysis on a pair of the p^{th} and $(p+1)^{\text{th}}$ rods (color filled, $1 \leq p \leq N - 2$), and the N^{th} rod in the half chain at any time t .

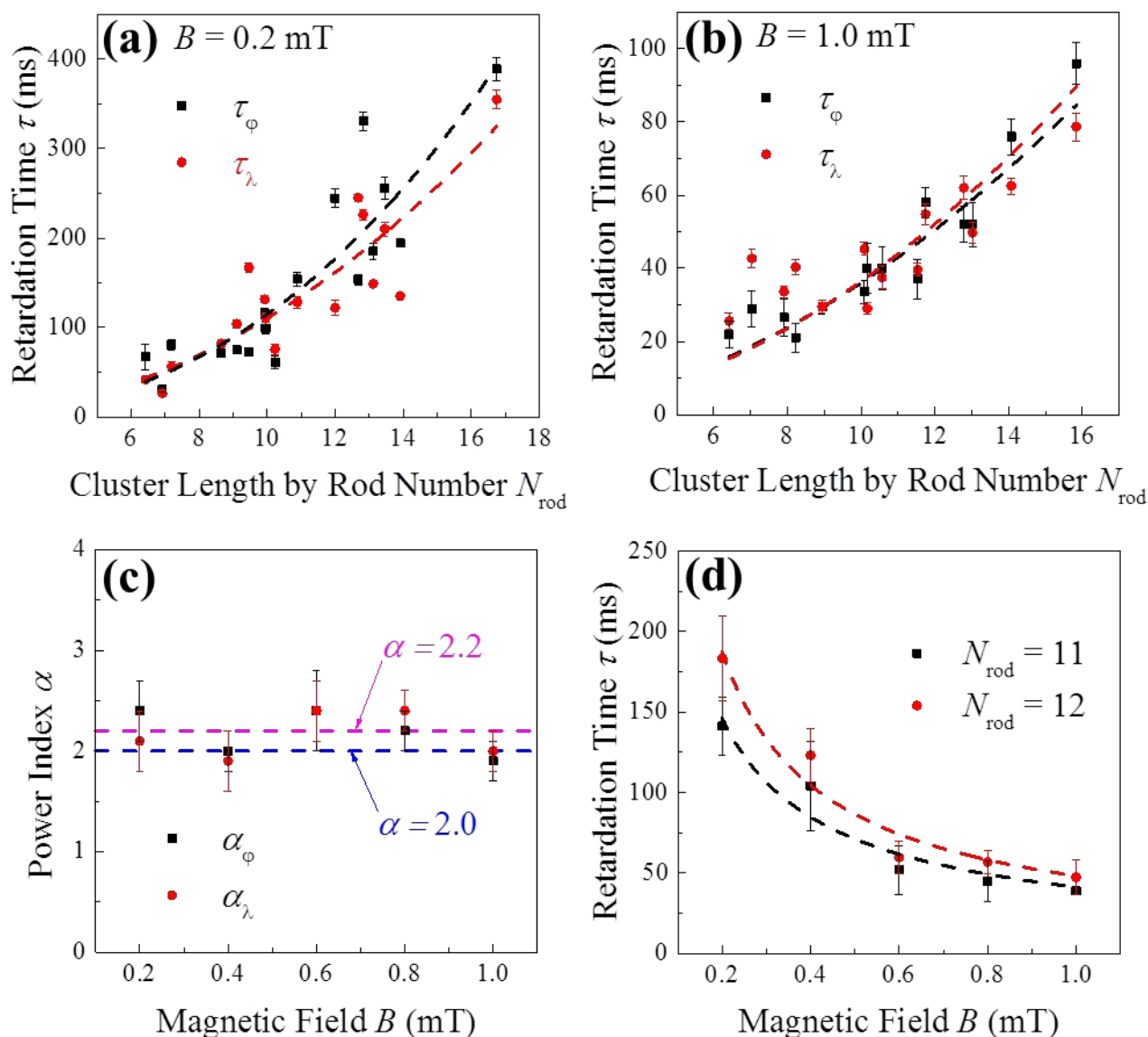


Figure 4 The plots of retardation time τ_λ (red circle) and τ_ϕ (black square) versus chain length N_{rod} at (a) $B = 0.2$ mT and (b) $B = 1.0$ mT. The dash curves are the fitting by a power law. (c) The plot of exponents α_λ (red circle) and α_ϕ (black square) for $B = 0.2, 0.4, 0.6, 0.8, 1.0$ mT. The average $\alpha = 2.2$ (pink dash line) is close to the theoretical prediction $\alpha = 2$ (blue dash line). (d) The plots of the average retardation time τ versus B for $N_{\text{rod}} = 11$ (black square) and 12 (red circle). The dash curves are the fittings *via* a power law.

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