

Analytical Methods

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On matrix reference materials characterised by proficiency test

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Abstract

This paper examines the status of a matrix reference material characterised by the consensus of the results from a proficiency test. It is shown that the very existence of a consensus in chemical measurement attests to its validity. Unique biases in individual laboratories are largely averaged out in forming the consensus. All of the variation between laboratories' results (including that resulting from the unique biases) will be encompassed by the standard error of the consensus. Any common bias among the laboratories remains unknowable. The supposed absence of traceability in a consensus can be overcome by obtaining appropriate information from the selected participants. More fundamentally it is shown that, in any event, a traceability chain is indeed broken in many types of chemical measurement, without detriment to the validity of the result. The overall conclusion is that, *with carefully considered safeguards*, characterisation of matrix reference materials by proficiency testing is appropriate to establish the concentrations of selected analytes.

Introduction

Proficiency tests are designed principally to enable participant laboratories to detect and remedy shortcomings in their procedures^{1,2}. Nevertheless, other quality-related activities such as method validation³ exploit the results of proficiency tests. Currently in chemical measurement there is interest in the use of proficiency test results for the characterisation of matrix reference materials, with the characterised value identified as the consensus of the participants' results and its standard uncertainty as the standard error of the consensus, both determined by appropriate statistical methods. Several proficiency test providers are currently issuing their surplus materials on the basis of this type of characterisation, so the time is ripe for a detailed examination of the practice. It is the theme of this paper that such a characterisation, if carried out with due consideration, can provide a stand-alone attestation of the material's composition, thus providing a valid and valuable addition to the analyst's armoury alongside certified reference materials.

In order to make this case, it is necessary to show that such characterisation is metrologically sound. Much has been written about how that might be achieved⁴. But fundamentally, metrological soundness does not depend on following a particular documented procedure: it implies only that there exists for a reference material a characterised value, with an associated uncertainty that is realistically estimated for a suitable mass of test portion. An analyst, armed with that information alone, could decide whether or not a reference material of appropriate matrix would be suitable for a particular purpose. Consequently, any approach whatsoever that provides that information is sufficient for characterisation.

It will be shown here that many proficiency tests can, with little or no adjustment, be made to conform to this fundamental requirement. The issue of traceability is often raised in relation to the status of a consensus, but a good case can be made that the apparent problems are insubstantial.

Location, bias and uncertainty

For present purposes we are interested in the 'location' of results from many laboratories participating in a round of a proficiency test. (A 'location', for example a mean, robust mean, median or mode, quantifies the tendency of a set of values.) A participant consensus used as the assigned value in a proficiency test is a location estimate and as such has a standard error. (A 'standard error' is the standard deviation of a statistic (such as a robust mean) as opposed to that of a simple variable (such as a result).) If a location estimate is unbiased, its standard error is by definition equal to its standard uncertainty.

How could we tell whether a consensus is unbiased? Well fundamentally we cannot! In principle all results of measurements of a quantity are biased, and so are locations of sets of results. Moreover, we cannot directly quantify the bias stemming from a specific procedure applied to a matrix material because the estimate is the difference between the location of a set of measurement results and the unknowable true value of the quantity. The key issue is whether the putative bias seems acceptably small. We can, however, estimate the difference between the locations of results obtained by applying two distinct analytical procedures to portions of the same material. From the comparison we can then refine the procedures in ways that we think will reduce bias, according to our knowledge of the physical and chemical principles involved. We tend to do that, using different methods and measurement principles, until we consider any residual bias to be acceptable.

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3 In considering bias in a consensus, it is useful to break down an individual analytical result into distinct
4 terms as follows: (a) the (unknown) true value; (b) a residual bias common to all participant
5 laboratories; (c) the random variation in the individual laboratory; and (d) a unique bias within the
6 individual laboratory. This is shown schematically in Fig 1 (for an unrealistically small number of
7 laboratories). Both the within-laboratory random variation and the individual laboratory biases can,
8 from the viewpoint of the whole dataset (our present concern), be treated as zero-mean random
9 processes. When we have a long list of results for a particular determination (as in a proficiency test)
10 these variations will be to a considerable degree ‘averaged-out’ in the consensus and be represented by
11 its much smaller standard error. This standard error encompasses all sources of variation in the dataset,
12 be they overt or latent. Only the common bias is present unchanged in the consensus and, as we have
13 seen, the magnitude of that in principle remains unknowable.
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17 **Handling unknowable bias**

18 It is proposed here that, *given reasonable safeguards*, this unknowable common bias must be treated as
19 zero for all practical purposes. The safeguards amount to eliminating all seemingly relevant sources of
20 bias during method validation. Having done that, if subsets of results based on a variety of physical
21 principles converge on a single location (obviously within limits defined by the relevant uncertainties)
22 we have no grounds to suspect bias unless we detect evidence or harbour well-founded suspicions to
23 the contrary. Evidence would be manifested in the form of systematic discrepancy between locations of
24 subsets the data associated with particular analytical procedures or methods. Suspicions would be based
25 on professional experience of the analytical methodology and of the test material, reinforced by the
26 appearance of a strong skew or multimodality in a dataset. Where no evidence or suspicions are
27 forthcoming, we can say *nothing* about the magnitude of any residual bias. However, it is noteworthy
28 that instances of latent bias, either common or unique, are most often discovered *via* the very process of
29 proficiency testing.
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34 Any characterisation procedure (including certification *via* ISO Guide 35⁴) that is based on
35 interlaboratory study is subject to exactly these same problems as proficiency testing. In all cases,
36 known bias is reduced by refining the analytical procedures as far as economically possible, then
37 simply accepting that remaining. The only differences arise in factors affecting the selection of the
38 subset of results regarded as ‘valid’ for characterisation purposes. It is usual in certification studies to
39 attempt to test for bias in the results of individual participants. (This is discussed further under
40 ‘Traceability’.) That intervention does not feature in proficiency testing. There is moreover in the
41 certification of a reference material the capacity for referring discrepant results back to the originators
42 with the possibility of revising them. (In principle that practice introduces a new ‘expectation bias’: if
43 the revised suspect results are further away from the putative consensus, they will be ignored; if they
44 are notably closer they will be included in forming a new consensus.) In proficiency test results, there
45 is no possibility of retrospectively correcting biases in particular results or arising from particular
46 analytical procedures.
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50 A further difficulty is that the number of different measurement principles and methods in use tends to
51 decline with time as certain methods and procedures are taken to be superior and become preferred by
52 an increasing proportion of participants. This process mostly tends to reduce bias. But ultimately, when
53 only one procedure remains in use, any residual bias will be untestable. This latent difficulty also
54 affects all methods of characterising matrix reference materials based on interlaboratory study.
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Traceability

A lack of traceability is often claimed (usually without detailed justification) to be a fundamental shortcoming of consensus values derived from proficiency test datasets. This assertion perhaps stems from an unwarranted distinction between proficiency test assigned values and values certified by interlaboratory study. Scrutiny, however, shows that the two procedures are homologous in their essential respects. Both procedures are based on a participant consensus. Both procedures make an estimate of the location of the results and its uncertainty from the results alone. The most striking difference between them is that certification usually requires each participant to justify the claim of a traceable result, while proficiency testing in the normal course of events does not. This distinction is largely insubstantial but, in any event, could be simply ameliorated.

This assertion rests on several points.

1. An error of consequential magnitude in a chemical measurement usually springs from two sources, (a) loss (or gain) of analyte during the process of chemical treatment of the test portion, and/or (b) loss or gain of net analytical signal brought about by matrix-mismatch between calibrators and treated test solution. It is conceptually incorrect and futile in practice to shoehorn these two effects into a traceability model because, contrary to prevailing doctrine, traceability is incomplete at these two points in a great majority of analytical procedures⁵.

Analysts are of course aware of these effects and moderate them in various ways, by correcting for recovery or reducing matrix-mismatch. But they seldom know how effective these attempts are in everyday analysis. Recovery, even when corrected, always differs from 100% by an unknown amount: matrices are always mismatched by an unknown amount. Sometimes these discrepancies are non-trivial. The traceability model therefore cannot help in estimating the often dominant uncertainty contributions brought about by these inescapable features of chemical analysis. This is *inter alia* why traceability-based models of an analytical procedure consistently tend to underestimate combined uncertainty, even in international key comparisons⁶, and why, in properly designed studies, repeatability dispersion is virtually always smaller than (interlaboratory) reproducibility dispersion⁷.

2. We can examine how a demonstration of traceability in certification is conducted and see whether that is rigorous. Certification bodies test for traceability typically by requiring participants in a study to analyse an existing certified reference material (CRM) alongside the candidate reference material and obtain a 'satisfactory' result. However, such a test is neither demanding nor conclusive. It would tend to have a low statistical power—typically a really large discrepancy would be needed to reach statistical significance. In addition, we could seldom guarantee that the candidate reference material and the CRM were effectively matrix-matched. Furthermore, how could we be sure that the certificated value of the reference CRM was itself unbiased? By harking back to successively older (and presumably less-rigorously certified) CRMs in a long regress back to uncertified calibrators? It would be easy for a proficiency test provider to ask participants to provide a comparable degree of reassurance on this point. For instance, participants could be asked to confirm that they have (a) used traceably-calibrated equipment, (b) matrix-matched calibrators prepared from elements or stoichiometric compounds of known purity or from other matrix reference materials, (c) a properly validated procedure, and (d) internal quality control, and furthermore (e) participate in an appropriate proficiency test and

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3 (f) operate in a well-found laboratory operating under appropriate infrastructure features. These
4 conditions would be fulfilled in accredited laboratories, so a statement of accreditation would
5 suffice. (Obviously the typical occurrence of outlying results suggests that a minority of
6 proficiency test participants do not conform to this specification, but such results can be
7 managed by use of common sense and appropriate statistical procedures.) It is an interesting
8 sidelight on this question to note that no ‘demonstration’ of traceability is suggested as necessary
9 in the use of proficiency test data in method validation³.
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13 3. However, even this documentary reassurance may not be strictly necessary, as the very existence
14 of a clear consensus in proficiency test results attests to its appropriate value. Only two
15 circumstances can account for a clear consensus: either (a) the consensus is effectively unbiased,
16 or (b) there exists an unknown common bias (that is, a bias affecting equally each of the
17 participants’ results). Laboratory-specific biases are largely averaged out in the consensus. The
18 location estimate effectively includes only the unknown common bias but that, according to the
19 previous argument, will usually have been reduced to a negligible level during the
20 development/validation of the analytical procedures.
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25 **Uncertainty of the consensus**

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27 The standard error of the proficiency test location encompasses the effects of *all* causes of variation
28 among participants, be they overt or latent. To equate a standard error of a consensus with a standard
29 uncertainty implies that there must be no *known* common bias among participants’ results, otherwise
30 the fundamental idea of uncertainty—that all known sources of bias in the measurement procedure
31 have been removed—is invalidated. Accepting that no known bias is present, it is clear that the
32 standard error of the location estimate is indeed its standard uncertainty. It encompasses *all* variation at
33 the time of the test, including heterogeneity. This identification is sometimes regarded with scepticism
34 by scientists who follow established certification procedures because the value of the standard error
35 often seems to be unexpectedly small. However, that happens partly because the effective number of
36 results available in a proficiency test dataset is usually greater than that economically feasible in
37 certification procedures. The standard error of the location estimate is therefore tantamount to a
38 standard uncertainty at the time of the test. Smallness of uncertainty is of course an invaluable asset in
39 a reference material.
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45 **A note on heterogeneity and instability**

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47 CRM producers include in the uncertainty budget terms relating to heterogeneity and long-term
48 instability. This approach is correct in principle, but there are practical shortcomings in adequately
49 implementing the idea. The high cost of certifying a reference material ensures that only materials
50 expected to have a long shelf-life are likely to be candidates. This in turn means that affordable tests for
51 deterioration by direct determination of the analyte will tend to be ineffectual when the reference
52 material is stored under normal working conditions: such tests will usually have low statistical power
53 (be unable to demonstrate relevant levels of instability) and will provide estimated uncertainty
54 contributions that are unreliable⁸. Producers are warned against the possibility of underestimation⁹
55 under these circumstances but, remarkably, not against over-estimation. The latter is the more likely
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3 eventual outcome because estimates of zero will be common but will be discounted in favour of higher
4 values. That feature could contribute to inflated uncertainty estimates on certified values.
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7 Proficiency testing *per se* does not rely on long-term stability of the test materials, whereas that is a key
8 property of certified reference materials. However, an alternative strategy to preliminary instability
9 tests is long-term monitoring of the material. Of course, the issuing body, at the time when the
10 reference material was released, would have to be convinced that the material was going to be
11 effectively stable, by virtue of prior experience with similar materials. Deterioration if any could then
12 be followed over an extended period. Proficiency test providers, however, are in a uniquely powerful
13 position to do that, simply by a participant-blind re-issue of the same material at future dates and a
14 comparison of the consensus values¹⁰. The use of consensus values derived from a large body of
15 participants obviates the problem of analytical run bias that potentially confounds results from a single
16 laboratory repeated after an interval of time. (A valuable corollary of this idea is that, for stable
17 reference materials, the consensus itself is shown to be stable.)
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20 21 **Conclusions**

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23 A substantial case has been presented for the recognition of matrix reference materials, characterised
24 by the judicious consideration of proficiency test results, as stand-alone exemplars of chemical
25 composition. The characterised value for an analyte and its standard uncertainty would be identified as
26 the assigned value and its standard error. Such materials would comprise an invaluable and relatively
27 inexpensive supplement to certified reference materials in the analyst's toolkit. It seems advisable for
28 the moment to maintain a distinction between 'characterised reference materials' and certified
29 reference materials, at least until a large body of experience in their preparation and use has
30 accumulated.
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34 The much-raised question of traceability in a consensus could be accommodated where necessary
35 simply by a relevant statement from each qualifying participant. However, in most instances the very
36 existence of a clear consensus is evidence of an appropriate value. This follows because in validated
37 procedures any remaining bias must perforce be taken to be of negligible magnitude. Finally it has been
38 shown that, in any event, metrological traceability is usually unavoidably incomplete in chemical
39 measurement without detriment to the validity of the result.
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43 Of course, a bald proficiency test consensus with no further support would be grossly insufficient to
44 comprise 'characterisation'. A detailed documented study of each dataset would be required, involving
45 expert consideration of the test material, the analytical procedures used, the statistical methodology
46 and, indeed, the results themselves. Oversight of characterisation should be provided by accreditation
47 agencies. A short informal guide to good practice would be a helpful development for this purpose.
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52 ¹ The International Harmonised Protocol for the proficiency testing of analytical chemistry laboratories. *Pure Appl. Chem.*
53 2006, **78**, 145-196.

54 ² ISO 17043:2010. *Conformity assessment—general requirements for proficiency testing*.

55 ³ Analytical Methods Committee. *Accred. Qual. Assur.* 2010, **15**, 73-79.

56 ⁴ ISO Guide 35:2006. *Reference materials—general and statistical principles for certification*.

57 ⁵ M. Thompson. *Anal. Methods*, 2016, **8**, 940-941.

58 ⁶ M. Thompson and S.L.R. Ellison. *Accred. Qual. Assur.* 2011, **16**, 483-487.
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⁷ M. Thompson and R. Wood. *Anal. Methods*, 2015, **7**, 375-379.

⁸ M. Thompson. *Anal. Methods*, 2015, **7**, 1627-1629.

⁹ ISO Guide 35 paragraph 7.3

¹⁰ M. Sykes and M. Thompson. *Anal. Methods*, 2015, **7**, 9753-9755.

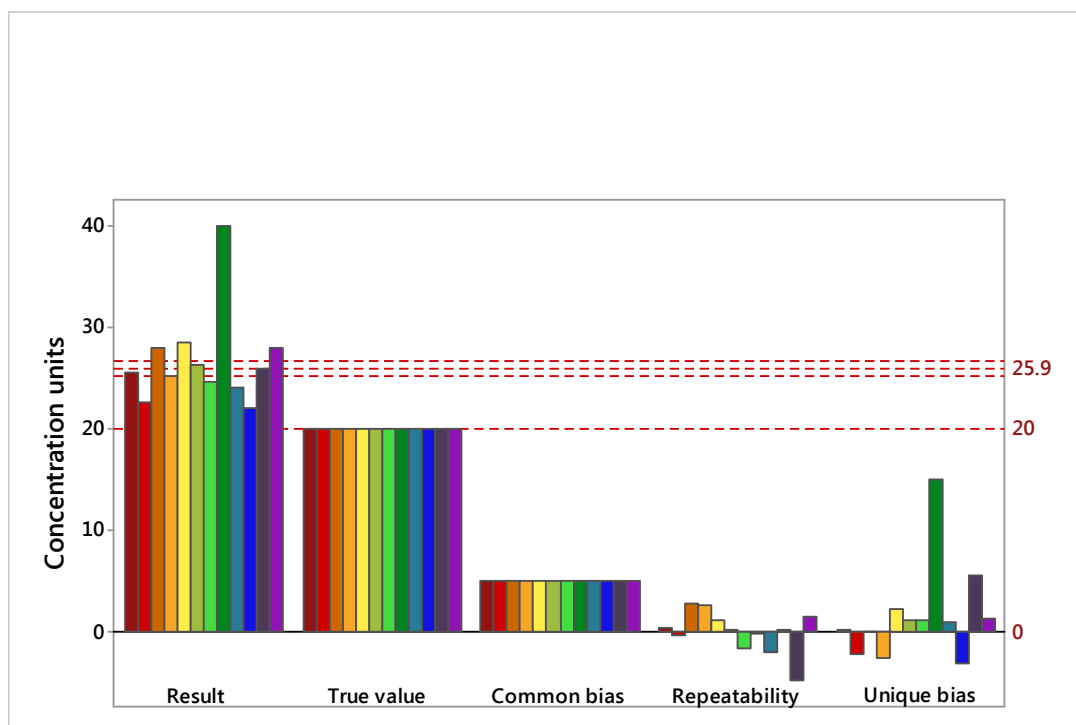
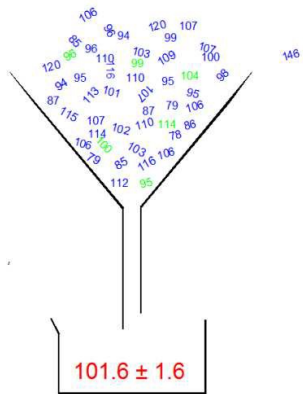


Fig 1. Schematic breakdown of analytical results (bars) in a proficiency test, into the true value (20), the common bias (5), the zero-mean repeatability variation and zero-mean unique bias. Individual participant laboratories coded by colour. The upper reference lines show the robust mean (a consensus) and its 95% confidence limits. The common bias (shown relatively large here for clarity) is included in the consensus.

A properly-determined consensus from a proficiency test is a metrologically-sound indication of chemical composition.



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