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Energetics of Lanthanide Cobalt Perovskites: LnCoO$_{3-\delta}$
(Ln = La, Nd, Sm, Gd)

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Abstract

Lanthanide cobalt perovskites LnCoO$_{3-\delta}$ (Ln = La, Nd, Sm, and Gd) are important materials for electroceramics, catalysts, and electrodes in solid oxide fuel cells. Formation enthalpies of LnCoO$_{3-\delta}$ compounds were measured using high temperature oxide melt solution calorimetry. The formation enthalpies of LaCoO$_{2.992}$, NdCoO$_{2.985}$, SmCoO$_{2.982}$ and GdCoO$_{2.968}$ from constituent binary oxides (Ln$_2$O$_3$, CoO) and O$_2$ gas are -111.87 ± 1.36, -98.49 ± 1.33, -91.56 ± 1.46 and -88.16 ± 1.45 kJ/mol, respectively. Thus these perovskites become energetically less stable with decrease in ionic radius of the lanthanide (from La to Gd), which corresponds to a decreasing tolerance factor and increasing oxygen deficiency. The thermodynamic stability of LaCoO$_{2.992}$, NdCoO$_{2.985}$, SmCoO$_{2.982}$ and GdCoO$_{2.968}$ was also assessed considering their oxygen partial pressures for decomposition, with good agreement between thermochemical and equilibrium data.

Keywords: Lanthanide perovskite, catalysis, SOFC materials, oxide melt solution calorimetry, formation enthalpy, oxide stability.

Introduction

Perovskite oxides (ABO$_3$) have attracted attention due to their subtle structural variations and important physical properties. Lanthanide cobalt perovskites, LnCoO$_3$, have applications as electroceramics, catalysts, solid oxide fuel cell (SOFC) electrodes, chemical sensors, and oxygen separation membranes$^{1-3}$. Their properties are sensitive to the ionic radius of Ln$^{3+}$, mainly due to the structural distortion induced by bond length misfit in the perovskite structure$^4$. These
distortions not only affect the crystal structure, but also influence physical properties such as electrical conductivity, catalytic activity and dielectric properties. Distortion in the perovskite (ABO$_3$) can be described by the Goldschmidt tolerance factor ($t$), which assesses the fit of the ‘A-site’ cation in the central site provided by the corner sharing BO$_6$ octahedra, and is defined by:

\[
t = \frac{r_A + r_O}{\sqrt{2(r_B + r_O)}}
\]

where $r_A$, $r_B$ and $r_O$ are the ionic radii of the A-site cation, B-site cation and O$^{2-}$ anion, respectively. Generally, perovskites, with increasing distortion as $t$ deviates from unity, occur for $0.75 \leq t \leq 1.0$. At room temperature, crystallographic distortion of LnCoO$_3$ increases with increasing Ln atomic number, i.e. with decreasing Ln$^{3+}$ ionic radius$^5$. The tolerance factor, $t$ (calculated using the Shannon effective ionic radii for lanthanides in twelvefold coordination and that for high spin Co$^{3+}$ in octahedral coordination$^6$), for LaCoO$_3$, NdCoO$_3$, SmCoO$_3$, and GdCoO$_3$ are 0.97, 0.94, 0.93, and 0.92, respectively. In the series from La to Gd, a symmetry change from rhombohedral to orthorhombic has been seen with decreasing size of the A-site cation$^7,^8$. LaCoO$_3$ has a rhombohedrally distorted perovskite structure, NdCoO$_3$ an almost cubic structure and the perovskites with Sm and Gd show orthorhombic distortions$^9$. In some cases, the structural distortion is accompanied by a spin state transition of the trivalent cobalt ion (Co$^{3+}$). Co ions have different ionic radii in different spin states; hence change in spin state of Co$^{3+}$ results in change in the octahedral Co-O bond length and corresponding change in the volume of the unit cell and the tolerance factor$^{10,11}$. There has been much discussion in the literature of spin transitions in lanthanide cobaltites; the situation is complicated by gradual transitions and the occurrence of intermediate spin, as well as low spin and high spin states$^9$. These transitions begin
below or at room temperature. For consistency, we have used the high spin state as reference for ionic radii of all the lanthanides in our discussion below.

It has been reported that lanthanide cobaltites exhibit small oxygen deficiency\(^{12}\). Thermogravimetric investigations of La\(_{1-x}\)Sr\(_x\)CoO\(_3\)\(_{\delta}\) in the range of \(10^{-5} \leq P_{O_2} / \text{(atm)} \leq 1\) and \(573 – 1273 \text{ K}\) indicate the oxygen non-stoichiometry, \(\delta\), increases with increasing temperature, increasing Sr concentration and decreasing oxygen partial pressure\(^{13}\). At room temperature, \(\delta\) for La\(_{1-x}\)Sr\(_x\)CoO\(_3\)\(_{\delta}\) in air is close to zero and below 1073 K, \(\delta\) of LaCoO\(_3\)\(_{\delta}\) is not detectable\(^{13}\). No oxygen excess compositions have been reported for lanthanide perovskites except for LnMnO\(_3\)\(_{\delta}\)\(^{14}\).

Different thermodynamic techniques have been employed to determine the stability of the rare earth based ternary oxides\(^ {15-17}\). The Gibbs free energies and enthalpies of formation of multicomponent transition metal oxides were obtained using solid electrolyte based galvanic cell methods and calorimetric techniques\(^ {18-25}\). The stability of lanthanide cobaltite perovskites was also determined by thermogravimetry by considering the decomposition reaction, LnCoO\(_3\) \(\rightarrow\) Ln\(_2\)O\(_3\) + CoO + \(\frac{1}{2}\) O\(_2\) (g) in a reducing atmosphere\(^ {14}\). Recent studies on oxygen deficient lanthanide cobaltites, LnCoO\(_3\)\(_{\delta}\) (LaCoO\(_{2.992}\), NdCoO\(_{2.985}\), SmCoO\(_{2.982}\) and GdCoO\(_{2.968}\)), suggest that their conductivity in the semiconducting state and activation energy for the transition to metallic conduction decrease monotonically with increasing ionic radius of the Ln cation\(^9\). The thermodynamic stability against reduction and the conductivity of the rare earth cobaltites correlate with the oxygen non-stoichiometry, \(\delta\), of LnCoO\(_3\)\(_{\delta}\). LaCoO\(_{2.992}\) has the lowest oxygen non-stoichiometry and appears to have the highest thermodynamic stability, whereas GdCoO\(_{2.968}\) has the highest oxygen non-stoichiometry and appears to have the lowest thermodynamic stability\(^9\).
The present study reports enthalpies of formation measured by high temperature oxide melt solution calorimetry for several lanthanide cobalt oxide perovskites, discusses their thermodynamic stability as a function of lanthanide element and oxygen non-stoichiometry and correlates their catalytic properties to their thermodynamic stability. The thermochemical calculations are carried out using (I) the nominal compositions, (II) the analyzed compositions from microprobe experiments, and (III) the oxygen deficient non-stoichiometric compositions. This allows us to conclude that different assumptions concerning these compositional variables do not change the thermochemical properties significantly.

**Experimental methods**

LnCoO$_{3-\delta}$ (LaCoO$_{2.992}$, NdCoO$_{2.985}$, SmCoO$_{2.982}$ and GdCoO$_{2.968}$) were synthesized via the combined citric acid and ethylene diamine tetraacetic acid (EDTA) complexing method, detailed elsewhere. Briefly, EDTA solution were prepared by dissolving EDTA (Acros Organics, ACS reagent) in a 25 % aqueous ammonia solution (Merck, p.a.). Lanthanide nitrates; La(NO$_3$)$_3$, Nd(NO$_3$)$_3$, Sm(NO$_3$)$_3$ (Sigma- Aldrich, 99.9 %), Gd(NO$_3$)$_3$ (ABCR, 99.9 %) and cobalt nitrate, Co(NO$_3$)$_2$ (Fluka, ≥ 98 %) were dissolved in water after determining the exact water content of the starting materials. A clear nitrate solution and citric acid monohydrate (Fluka, ≥ 99.5 %) were added to the EDTA solution under stirring and the solution were heated in an oil bath at 353 - 413 K for 12 h. The resulting dark brown foam was then calcined in a furnace at 1373 K for 2 h in air.

Phase purity of the synthesized samples was analyzed by powder X-ray diffraction (XRD). Patterns were recorded using a Bruker D8 Advance diffractometer (Bruker-AXS Inc.) operated at an accelerating voltage of 40 kV and an emission current of 40 mA with CuKα.
radiation (\(\lambda = 0.15406 \text{ nm}\)). Data were acquired from 10 to 70 ° 2θ with a step size of 0.03 ° and a collection time of 0.5 s/step.

The oxygen non-stoichiometry (\(\delta\)) of the perovskites \(\text{LnCoO}_{3-\delta}\) was obtained from the measured mass loss in a reducing atmosphere (5 vol. % \(\text{H}_2\) in \(\text{He}\)) from 303 K to 1123 K using a Netzsch STA 449 thermal analyzer detailed elsewhere\(^9\). Briefly, all perovskites started to decompose at \(\sim 623 \text{ K}\) in the reducing atmosphere. At higher temperatures (>623 K), pronounced mass losses occurred until a stable mass of roughly 91 wt. % was reached at 923 ± 50 K. The mass losses occur in two steps according to the reaction:

\[
\text{LnCoO}_{3-\delta} \rightarrow \frac{1}{2} \text{Ln}_2\text{O}_3 + \text{CoO} + (0.5 - \delta)/2 \text{O}_2 \rightarrow \frac{1}{2} \text{Ln}_2\text{O}_3 + \text{Co} + (1.5 - \delta)/2 \text{O}_2
\]  

(2)

In the first step, the lanthanide cobaltite decomposes into the corresponding lanthanide oxide and cobalt (II) oxide. In the second step, the cobalt (II) oxide is reduced to metallic cobalt. The non-stoichiometry (\(\delta\)) in \(\text{LnCoO}_{3-\delta}\) is determined from the observed mass loss in TGA measurements and the uncertainties in \(\delta\) were obtained by propagating the uncertainties in mass change. Obtained \(\delta\) values for \(\text{LaCoO}_{3-\delta}\), \(\text{NdCoO}_{3-\delta}\), \(\text{SmCoO}_{3-\delta}\) and \(\text{GdCoO}_{3-\delta}\) are 0.0081 ± 0.0002, 0.0152 ± 0.0003, 0.0179 ± 0.0003, and 0.0318 ± 0.0008; respectively. The calculation of oxygen non-stoichiometry of the original perovskites is based on the total decomposition reaction and the masses measured at 473 and 1073 K. In the rest of the manuscript, \(\text{LnCoO}_{3-\delta}\) has been presented as \(\text{LaCoO}_{2.992}\), \(\text{NdCoO}_{2.985}\), \(\text{SmCoO}_{2.982}\) and \(\text{GdCoO}_{2.968}\), by rounding off the oxygen non-stoichiometry to three decimal places without indicating the uncertainties, which are in the fourth place.

The compositions (Ln/Co ratios) of the synthesized samples were measured using wavelength dispersive electron microprobe analysis with a Cameca SX100 instrument operated
at an accelerating voltage of 15 kV, a beam current of 20 nA, and a beam size of 1 μm. Sample homogeneity was investigated using back-scattered electron images. For the microprobe analysis, powders were pelletized and annealed at 1073 K. The sintered pellets were polished and carbon-coated. Co metal and lanthanide orthophosphate standards were used. The compositions were calculated from an average of 10 data points per sample and the uncertainties were calculated as two standard deviations of the mean.

High temperature oxide melt drop solution calorimetry was performed in a custom-made isoperibol Tian-Calvet twin microcalorimeter described previously. The calorimeter was calibrated against the heat content of 5 mg pellets of high purity α-Al₂O₃ (99.997 %). The calorimetric assembly was flushed with oxygen at 43 ml/min with oxygen bubbling through the solvent at 4.5 ml/min to aid dissolution. The experiments were also carried out using high purity argon as flushing and bubbling gas. ~5 mg sample pellets were loosely pressed, weighed and dropped from room temperature into 3Na₂O·4MoO₃ solvent in a platinum crucible at 1075 K in the calorimeter. The final state was CoO and Ln₂O₃ dissolved in sodium molybdate in both oxygen and argon environments. Transposed temperature drop calorimetry (no solvent present) was performed using the same calorimeter to determine the enthalpy increment of LnCoO₃₋δ from room temperature to 1075 K.

Results and Discussion

XRD analyses of LaCoO₂.₉₉₂, NdCoO₂.₉₈₅, SmCoO₂.₉₈₂ and GdCoO₂.₉₆₈ confirm the phase purity of the samples, with pseudo-cubic lattice constants of 3.831 ± 0.003, 3.773 ± 0.003, 3.76 ± 0.002, and 3.74 ± 0.002 Å, respectively. The microprobe analyses confirm that the samples are generally stoichiometric with respect to metal content within experimental error and the Ln/Co
ratios are 1.018 ± 0.003, 1.018 ± 0.004, 0.984 ± 0.012 and 1.012 ± 0.017 for La/Co, Nd/Co, Sm/Co and Gd/Co, respectively. One can write the microprobe compositions of the Ln-cobaltites from the exact analyzed compositions of lanthanides, cobalt and with three oxygen atoms per formula unit as; La$_{1.009±0.002}$Co$_{0.991±0.002}$O$_{3.000±0.006}$, Nd$_{1.009±0.003}$Co$_{0.991±0.003}$O$_{3.000±0.010}$, Sm$_{0.992±0.008}$Co$_{1.008±0.009}$O$_{3.000±0.025}$, and Gd$_{1.006±0.012}$Co$_{0.994±0.012}$O$_{3.000±0.035}$. The compositions were calculated from an average of 10 data points per sample and the uncertainties were calculated as two standard deviations of the mean. No secondary phases were observed on the back-scattered electron images of the sintered samples.

The thermochemical calculations were carried out using (I) the nominal compositions (II) the analyzed compositions from microprobe experiments, and (III) the oxygen deficient nonstoichiometric compositions, as discussed in the previous section. This allowed us to conclude that the different assumptions of these compositional variables do not change the thermochemical properties significantly.

The enthalpies of drop solution, $\Delta_{ds}H$, of Ln-cobaltites are shown in Table 1. The enthalpies of formation from component oxides and elements were obtained using thermodynamic cycles shown in Table 2. Similarly, different appropriate balanced thermochemical cycles were used to derive the formation enthalpies of Ln-cobaltites with microprobe compositions and with nominal compositions. For a given Ln-cobaltite perovskite, the drop solution enthalpy of nominal, microprobe and oxygen non-stoichiometric compositions were calculated based on their formula weights.

The enthalpy of drop solution of binary oxides, La$_2$O$_3$, Nd$_2$O$_3$, Sm$_2$O$_3$, and Gd$_2$O$_3$ and CoO in 3Na$_2$O·4MoO$_3$ at 1075 K were taken from prior measurements$^{32, 33}$. For calculation of enthalpies of formation from the elements, the enthalpies of formation of binary oxides from
Robie et al. were used. The calculated formation enthalpies from corresponding oxides, (Ln$_2$O$_3$, CoO) plus O$_2$ gas at 298 K, $\Delta_fH^{ox}$, for LaCoO$_{2.992}$, NdCoO$_{2.985}$, SmCoO$_{2.982}$ and GdCoO$_{2.968}$ are shown in Table 1. Similarly, $\Delta_fH^{ox}$ of perovskites with nominal compositions and microprobe compositions were determined from the appropriate thermochemical cycles and are shown in Table 1. The calculated $\Delta_fH^{ox}$ from constituent oxides and oxygen gas of Ln-cobaltites with nominal compositions, measured oxygen non-stoichiometric compositions, and the microprobe compositions are the same within the reported uncertainties (Table 1). The calculated formation enthalpies for LaCoO$_{2.992}$, NdCoO$_{2.985}$, SmCoO$_{2.982}$ and GdCoO$_{2.968}$ from elements are given in Table 3). These are the first set of experimental data on enthalpies of formation for Ln-cobaltites derived by solution calorimetry.

The obtained enthalpy increments ($H_{1075 \text{K}}-H_{298 \text{K}}$) for LaCoO$_{2.992}$, NdCoO$_{2.985}$, SmCoO$_{2.982}$ and GdCoO$_{2.968}$ are reported in Table 3. The measured enthalpy increments ($H_{1075 \text{K}}-H_{298 \text{K}}$) generally compare reasonably well (agreement within 6 % or better) with the reported values by Patil et al. from heat capacity measurements (Table 3). Because LaCoO$_{2.992}$, NdCoO$_{2.985}$, SmCoO$_{2.982}$ and GdCoO$_{2.968}$ are only slightly oxygen deficient, the configurational entropy terms arising from mixing of oxygen ions and vacancies on the oxide sublattice and of Co$^{2+}$ and Co$^{3+}$ on octahedral sites can be neglected. The entropy of formation of LnCoO$_{3-\delta}$ (s) from elements Ln (s), Co(s) and O$_2$ (g) at 298 K were determined by combining the Gibbs energy of formation of LnCoO$_3$ reported in the literature from electrochemical measurements and enthalpy of formation from constituent elements in the present calorimetric work (Table 3). The obtained formation enthalpies and entropies at 298 K for LaCoO$_{2.992}$, and SmCoO$_{2.982}$ compares well with those reported by Patil et al. However for NdCoO$_{2.985}$ and GdCoO$_{2.968}$, differences of 20 - 30 kJ/mol for $\Delta_fH^\circ$ and about 100 J/(Kmol) for $\Delta_fS^\circ$, were seen. It has to be noted that uncertainties
of the reported $\Delta_f H_m^\circ$ (298 K) values were not provided. Patil et al.$^{35}$ calculated $\Delta_f H_m^\circ$ (298 K) from the reported $\Delta_f G_m^\circ$ (LnCoO$_3$, s, T), the enthalpy of the electronic transition of LnCoO$_3$, the electronic transition temperature, and heat capacity for Ln (s), Co(s), and O$_2$ (g) and LnCoO$_3$ using appropriate relations. Bringing down the $\Delta_f H_m^\circ$ at the mean temperature of the e.m.f. measurements (from which $\Delta_f G_m^\circ$ of LnCoO$_3$, were determined) to room temperature, can be associated with larger uncertainties. Again the uncertainties in the values of $\Delta_f H_m^\circ$ (298 K) carry the uncertainties involved in all terms. The difference of 20 - 30 kJ/mol for $\Delta_f H_m^\circ$ (298 K) is in agreement within 2 %, which might be within the uncertainties of the $\Delta_f H_m^\circ$ (298 K) value reported by Patil et al.$^{35}$ It must be pointed out that the difference of 2 % in $\Delta_f H^\circ$ for NdCoO$_3$ and GdCoO$_3$, leads to 30 % difference in $\Delta_f S^\circ$. However, we believe, even the propagated uncertainty in going from enthalpy to entropy is high, it is useful to have a comparison. Furthermore we note that it is difficult to assign absolute errors to the temperature slope of electrochemical data because there can be potential sources of systematic error and the temperature range of measurements is frequently small.

The Gibbs free energies of the reaction ($\Delta_f G_m^{\exp}$), LnCoO$_3$ $\rightarrow$ $\frac{1}{2}$ Ln$_2$O$_3$ + CoO + $\frac{1}{4}$ O$_2$, were reported over a wide range of temperatures by electromotive force (e.m.f.) methods.$^{15,17,35,36}$ From the reported $\Delta_f G_m^{\exp}$, enthalpies of reactions ($\Delta_f H^{\exp}$) at the mean temperature of the e.m.f. measurements were determined (Table 4). In the present work, $\Delta_f H^{\exp}$ at the mean temperature of the e.m.f. measurements was calculated by adding the necessary enthalpy increment terms to the $\Delta_f H^{\exp}$ at room temperature determined by the calorimetric techniques, as follows

$$\Delta_f H_{TK}^{\exp} \langle \text{LnCoO}_3 \rangle = \Delta_f H_{298.15K}^{\exp} \langle \text{LnCoO}_3 \rangle + \int_{298.15K}^{TK} \Delta C_p \, dT$$  \hspace{1cm} (3)
where, $\Delta_f H_{\text{ox}}^{\text{TK}} < \text{LnCo}_3 >$ is the calorimetrically determined formation enthalpies of lanthanide cobaltites at the mean temperature of e.m.f measurements, $\Delta_f H_{298.15K}^{\text{ox}} < \text{LnCo}_3 >$ is the enthalpies of formation at room temperature determined by calorimetric techniques. \[ \int_{298.15K}^{TK} \Delta C_p \, dT \]

is the enthalpy increment term. $\Delta C_p$ is the difference in the heat capacities of LnCo$_3$ and its constituent oxides and oxygen gas, $(\frac{1}{2} \text{Ln}_2\text{O}_3 + \text{CoO} + \frac{1}{4} \text{O}_2)$. \[ \int_{298.15K}^{TK} \Delta C_p \, dT \]

were calculated as follows,

\begin{equation} \int_{298.15K}^{TK} \Delta C_p \, dT = \int_{298.15K}^{TK} \left[ C_p^{\text{LnCo}_3} - \left( \frac{1}{2} \right) C_p^{\text{Ln}_2\text{O}_3} + C_p^{\text{CoO}} + \left( \frac{1}{4} \right) C_p^{\text{O}_2} \right] \, dT = \int_{TK}^{T_1} \Delta C_p \, dT + \Delta u H_{\text{LnCo}_3} + \int_{T_1}^{TK} \Delta C_p \, dT \tag{4} \end{equation}

In equation (4), $T_1$ is the electronic transition temperature of the Ln-cobaltites; $\Delta u H_{\text{LnCo}_3}$. $T_1$ for LaCo$_3$, NdCo$_3$, SmCo$_3$ and GdCo$_3$ are 554 K, 610 K, 619 K, and 675 K with an uncertainty of ±2 K, respectively$^{16}$. The heat capacity and electronic transition enthalpies of LaCo$_3$, NdCo$_3$, SmCo$_3$ and GdCo$_3$ were taken from Patil et al.$^{16}$ The heat capacity expression of corresponding binary oxides and oxygen gas were taken from Pankratz$^{37}$. Calculated enthalpies of formations of LnCo$_3$ from the constituent oxides plus O$_2$ gas by calorimetric technique and e.m.f. techniques are reported in Table 4. The obtained $\Delta_f H^{\text{ox}}$ for LaCo$_3$$_{2.992}$, and GdCo$_3$$_{2.982}$ compares well with those reported by Patil et al$^{35}$. However for NdCo$_3$ and SmCo$_3$, differences of about 20 kJ/mol was observed, which can be explained based on the associated error in $\Delta_f G^{\text{ox}}(T)$, from which $\Delta_f H^{\text{ox}}$ is derived. Patil et al$^{35}$ determined a single $\Delta_f G^{\text{ox}}(T)$ expression for each LnCo$_3$ system by combined the data reported by previous investigators, separately by least squares analysis method in the temperature range 1000 – 1500 K. We believe such methods of calculation of $\Delta_f G^{\text{ox}}(T)$ can have large error, which in turn will be reflected in $\Delta_f H^{\text{ox}}$ of LnCo$_3$. Hence, again we suggest that the associated error in the $\Delta_f G^{\text{ox}}$
(T) will accommodate the observed difference of the calculated and reported values $\Delta_fH^{\text{ox}}$.

Scherrer et al.\textsuperscript{9} determined thermodynamic stability of LnCoO$_{3-\delta}$ perovskites from the Gibbs free energy change corresponding to decomposition of LnCoO$_{3-\delta}$ perovskites ($\Delta_\delta G^0$) for reaction (2) employing an e.m.f. technique, where 12.84 wt.% yttria stabilized zirconia (YSZ) and Fe/FeO served as the solid electrolyte and reference electrode, respectively. The obtained oxygen partial pressure ($P_{O_2}$) at 1123 K corresponding to the decomposition reaction (2) are plotted against the oxygen non-stoichiometry $\delta$ of LnCoO$_{3-\delta}$ (Fig. 1). Also the $\Delta_fH^{\text{ox}}$ values of LnCoO$_{3-\delta}$, determined by calorimetry in the present work are plotted against the non-stoichiometry $\delta$ of LnCoO$_{3-\delta}$ (Fig. 1). With increase in non-stoichiometry, the formation enthalpy becomes less exothermic and the oxygen partial pressure for the decomposition of the LnCoO$_{3-\delta}$ increases. For the compounds with smaller radii of the Ln cation, the non-stoichiometry $\delta$ and log $P_{O_2}$ are higher and the formation enthalpy is less exothermic and therefore the thermodynamic stability is lower. Hence based on the present investigation and previous literature information\textsuperscript{9}, it can be concluded that the thermodynamic stability as well as the oxygen non-stoichiometry in LnCoO$_{3-\delta}$, depend on the crystal structure, which is specified through the tolerance factor and distortion which determines the Co–O–Co bond angle.

Figure 2a depicts the variation of formation enthalpy of LnCoO$_{3-\delta}$ from their constituent oxides plus oxygen with ionic radius of the lanthanide ions (Ln$^{3+}$). They become more endothermic with decrease in ionic radius of the lanthanides, which corresponds to decrease of the Goldschmidt tolerance factor ($t$) (Fig. 2b). Thus the largest ion in the lanthanide series forms the most stable perovskite.
It is clear from the present investigation that for compounds with smaller Ln$^{3+}$ radii, the non-stoichiometry δ is higher and the formation enthalpy is less exothermic and therefore the thermodynamic stability is lower. However the individual contribution of non-stoichiometry and lanthanide cation size to the overall thermodynamic stability can not be separated at present.

According to the literature data on basicity of Ln$_2$O$_3$ with increase in size of the lanthanide ions, the basicity increases in the order Gd$_2$O$_3$ < Sm$_2$O$_3$ < Nd$_2$O$_3$ < La$_2$O$_3$. Since this is the same order as increasing ionic radius, it is clear that thermodynamic stability of the Ln-cobaltite perovskite increases with increasing basicity of the lanthanide oxide, or increasing difference in basicity between the lanthanide oxide and cobalt oxide.

The observed trend on energetics of lanthanide cobaltite perovskites in the present work compares well with energies of the reduction reaction; LnCoO$_3$ → 0.5 Ln$_2$O$_3$ + CoO + ½ O$_2$ (g), observed by Lago et al.$^{38}$ and Arakawa et al.$^{39}$ The reduction reactions were assumed to be thermodynamically controlled. Among the considered series, LaCoO$_3$, with highest thermodynamic stability, reduces at the highest temperatures$^{38}$. Reoxidation of cobalt to form the parent perovskite structure is thermodynamically more favorable for larger lanthanides$^{38}$.

The Gibbs free energy of the reaction; 0.5 Ln$_2$O$_3$ + CoO + ½ O$_2$ (g) → LnCoO$_3$, at 1273 K measured by Patil et al.$^{16}$ indicates a linear change with the ionic radius of the lanthanide elements with 12 coordination. The value for LaCoO$_3$ fits well despite the difference of the crystal system from other LnCoO$_3$ perovskite structures, suggests that the crystal system has a smaller effect on $\Delta G^{\text{expt}}$ than the ionic radius. E.m.f. studies and heat capacity measurements revealed the presence of first order endothermic phase transformation of LaCoO$_3$ at 1212 K with $\Delta_{f}H = 15.275$ kJ/ mol$^{16,40}$. 

The observed energetic trend of the lanthanide cobaltite perovskites, where stability increases in the order GdCoO$_{2.968}$ < SmCoO$_{2.982}$ < NdCoO$_{2.958}$ < LaCoO$_{2.992}$ can elucidate the observed trends of their physical properties. The catalytic activity of LnCoO$_3$ (which depends on easy reduction of its cobalt ion to metallic cobalt) increases in the order LaCoO$_3$ < NdCoO$_3$ < SmCoO$_3$ < GdCoO$_3$\cite{38,41}. The thermodynamically less stable GdCoO$_{2.968}$ favors easier reduction of Co$^{3+}$ to metallic cobalt (Co) on the surface of Gd$_2$O$_3$. On the other hand, the most stable perovskite LaCoO$_{2.992}$, disfavors the reduction of Co$^{3+}$ to Co and this limits the catalytic activity. Analogous trends were observed by Lago et al.\cite{38} where Gd yields the highest quantities of CO and H$_2$ from methane, whereas with the catalyst containing La, no syngas formation was observed.

**Conclusions**

Energetics of lanthanide cobaltite perovskites (Ln = La, Nd, Sm, Gd) have been determined for the first time employing oxide melt solution calorimetry. Enthalpies of formation of the LnCoO$_{3-\delta}$ perovskites from their constituent oxides become less exothermic with decrease in the ionic radius of lanthanides and increase in oxygen non-stoichiometry. The thermodynamic stability correlates well with that expected from their tolerance factors and oxygen partial pressures corresponding the decomposition.

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References


List of Tables

Table 1. Calorimetric data and formation enthalpies from oxides for lanthanide cobaltites with all possible compositions (nominal, oxygen non-stoichiometry and microprobe compositions. Enthalpy of drop solution, $\Delta_d H$, were measured in sodium molybdate at 1075 K. The average value and associated error (two standard deviations of the mean) are calculated from nine experiments.

Table 2. Thermochemical cycle to determine the enthalpies of formation of LaCoO$_{2.992}$, NdCoO$_{2.985}$, SmCoO$_{2.982}$ and GdCoO$_{2.968}$ perovskites from constituent oxides and elements.

Table 3. Derived thermodynamic parameters for LaCoO$_{2.992}$, NdCoO$_{2.985}$, SmCoO$_{2.982}$ and GdCoO$_{2.968}$.

Table 4. Comparison of enthalpies of formation of LnCoO$_3$
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Figure 1. Non-stoichiometry $\delta$ of $\text{LnCoO}_3{-}\delta$, oxygen partial pressure$^9$ at 1123 K and formation enthalpy of $\text{LnCoO}_3{-}\delta$ from oxides ($\Delta_f^{\text{ox}}$).

Figure 2a. Formation enthalpies of $\text{LaCoO}_3{-}\delta$, $\text{NdCoO}_3{-}\delta$, $\text{SmCoO}_3{-}\delta$ and $\text{GdCoO}_3{-}\delta$ versus ionic radius of the lanthanides$^6$.

Figure 2b. Formation enthalpies of $\text{LaCoO}_3{-}\delta$, $\text{NdCoO}_3{-}\delta$, $\text{SmCoO}_3{-}\delta$ and $\text{GdCoO}_3{-}\delta$ versus tolerance factor of the lanthanides.
Table 1

<table>
<thead>
<tr>
<th>Lanthanide cobaltites</th>
<th>Drop solution enthalpies, $\Delta_{dH}^*$, kJ/mol</th>
<th>Formation enthalpies $\Delta_{fH}^{ox}$, kJ/mol</th>
</tr>
</thead>
<tbody>
<tr>
<td>LaCoO$_3$</td>
<td>28.73±0.34</td>
<td>-111.78±1.36</td>
</tr>
<tr>
<td>LaCoO$_{2.992}$</td>
<td>28.72±0.34</td>
<td>-111.87±1.36</td>
</tr>
<tr>
<td>La$<em>{1.009±0.002}$Co$</em>{0.991±0.002}$O$_{3.000±0.006}$</td>
<td>28.83±0.34</td>
<td>-113.40±1.45</td>
</tr>
<tr>
<td>NdCoO$_3$</td>
<td>47.77±1.05</td>
<td>-98.33±1.33</td>
</tr>
<tr>
<td>NdCoO$_{2.985}$</td>
<td>47.73±1.05</td>
<td>-98.49±1.33</td>
</tr>
<tr>
<td>Nd$<em>{1.009±0.003}$Co$</em>{0.991±0.003}$O$_{3.000±0.010}$</td>
<td>47.73±1.05</td>
<td>-99.36±1.34</td>
</tr>
<tr>
<td>SmCoO$_3$</td>
<td>53.25±0.86</td>
<td>-91.39±1.46</td>
</tr>
<tr>
<td>SmCoO$_{2.982}$</td>
<td>53.19±0.86</td>
<td>-91.56±1.46</td>
</tr>
<tr>
<td>Sm$<em>{0.992±0.008}$Co$</em>{1.008±0.009}$O$_{3.000±0.025}$</td>
<td>53.83±0.91</td>
<td>-90.34±1.48</td>
</tr>
<tr>
<td>GdCoO$_3$</td>
<td>48.45±0.95</td>
<td>-87.83±1.45</td>
</tr>
<tr>
<td>GdCoO$_{2.968}$</td>
<td>48.36±0.95</td>
<td>-88.16±1.45</td>
</tr>
<tr>
<td>Gd$<em>{1.006±0.012}$Co$</em>{0.994±0.012}$O$_{3.000±0.035}$</td>
<td>48.55±0.95</td>
<td>-88.51±1.46</td>
</tr>
</tbody>
</table>

*The uncertainties were calculated as two standard deviations of the reported mean value.
Table 2

<table>
<thead>
<tr>
<th>#Eq</th>
<th>Reactions</th>
<th>Enthalpies (KJ/mol)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Ln₂O₃ (xl, 298 K) → Ln₂O₃ (solⁿ, 1075 K)</td>
<td>ΔH₁</td>
</tr>
<tr>
<td>2</td>
<td>CoO (xl, 298 K) → CoO (solⁿ, 1075 K)</td>
<td>ΔH₂</td>
</tr>
<tr>
<td>3</td>
<td>O₂ (g, 298 K) → O₂ (g, 1075 K)</td>
<td>ΔH₃</td>
</tr>
<tr>
<td>4</td>
<td>LnCoO₃₋δ (xl, 298 K) → ½ Ln₂O₃ (solⁿ, 1075 K) + CoO (solⁿ, 1075 K) + (1-2δ)/4 O₂ (solⁿ, 1075 K)</td>
<td>ΔH₄</td>
</tr>
<tr>
<td>5</td>
<td>½ Ln₂O₃ (xl, 298 K) + CoO (xl, 298 K) + (1-2δ)/4 O₂ → LnCoO₃₋δ (xl, 298 K)</td>
<td>ΔH₅ = ½ ΔH₁+ΔH₂+(1-2δ)/4ΔH₃-ΔH₄</td>
</tr>
<tr>
<td>6</td>
<td>Co(xl, 298 K) + ½ O₂(g, 298 K) → CoO(xl, 298 K)</td>
<td>ΔH₆</td>
</tr>
<tr>
<td>7</td>
<td>2Ln(xl, 298 K) + 3/2 O₂(g, 298 K) → Ln₂O₃(xl, 298 K)</td>
<td>ΔH₇</td>
</tr>
<tr>
<td>8</td>
<td>Ln (xl, 298 K) + Co (xl, 298 K) + (3- δ)/2 O₂ → LnCoO₃₋δ (xl, 298 K)</td>
<td>ΔH₈ = ΔH₅+ ΔH₆+ ½ ΔH₇</td>
</tr>
</tbody>
</table>

Where xl = crystalline, solⁿ = solution
<table>
<thead>
<tr>
<th>Compound</th>
<th>Enthalpies of formation, kJ/mol from elements</th>
<th>Enthalpy increments ($H_{1073 \text{ K}}-H_{298 \text{ K}}$), kJ/mol</th>
<th>Formation entropies at 298 KJ/(K mol)</th>
</tr>
</thead>
<tbody>
<tr>
<td>LaCoO$_2$</td>
<td>-1247.68 ± 2.71</td>
<td>108.14 ± 0.77</td>
<td>-294.08</td>
</tr>
<tr>
<td></td>
<td>-1250.2$^{35}$</td>
<td>113.7$^{35}$</td>
<td>-302.53$^{35}$</td>
</tr>
<tr>
<td>NdCoO$_2$</td>
<td>-1241.62 ± 3.53</td>
<td>114.56 ± 1.69</td>
<td>-218.41</td>
</tr>
<tr>
<td></td>
<td>-1271.3$^{35}$</td>
<td>109.1$^{35}$</td>
<td>-317.96$^{35}$</td>
</tr>
<tr>
<td>SmCoO$_2$</td>
<td>-1246.83 ± 4.90</td>
<td>124.86 ± 0.99</td>
<td>-298.27</td>
</tr>
<tr>
<td></td>
<td>-1249.0$^{35}$</td>
<td>125.9$^{35}$</td>
<td>-305.55$^{35}$</td>
</tr>
<tr>
<td>GdCoO$_2$</td>
<td>-1235.45 ± 8.75</td>
<td>99.04 ± 1.18</td>
<td>-229.58</td>
</tr>
<tr>
<td></td>
<td>-1256.8$^{35}$</td>
<td>105.5$^{35}$</td>
<td>-301.19$^{35}$</td>
</tr>
</tbody>
</table>
Table 4: Comparison of enthalpies of formation of LnCoO$_3$

<table>
<thead>
<tr>
<th>Samples</th>
<th>Temp./K</th>
<th>$\Delta_f H^{\text{ox}}$ Calorimetry (kJ/mol)</th>
<th>$\Delta_f H^{\text{ox}}$ Petrov et al$^{17,36}$ (kJ/mol)</th>
<th>$\Delta_f H^{\text{ox}}$ Patil et al$^{15,35}$ (kJ/mol)</th>
</tr>
</thead>
<tbody>
<tr>
<td>LaCoO$_3$</td>
<td>1141.5</td>
<td>-109.38 ± 1.85</td>
<td>-120</td>
<td>--</td>
</tr>
<tr>
<td></td>
<td>1250</td>
<td>-107.07 ± 1.85</td>
<td>--</td>
<td>-110.5</td>
</tr>
<tr>
<td>NdCoO$_3$</td>
<td>1141.5</td>
<td>-80.44 ± 2.24</td>
<td>-79.02</td>
<td>--</td>
</tr>
<tr>
<td></td>
<td>1250</td>
<td>-78.39 ± 2.24</td>
<td>--</td>
<td>-100.7</td>
</tr>
<tr>
<td>SmCoO$_3$</td>
<td>1141.5</td>
<td>-71.62 ± 2.75</td>
<td>-70.83</td>
<td>--</td>
</tr>
<tr>
<td></td>
<td>1250</td>
<td>-70.04 ± 2.75</td>
<td>--</td>
<td>-92.4</td>
</tr>
<tr>
<td>GdCoO$_3$</td>
<td>1141.5</td>
<td>-63.70 ± 2.50</td>
<td>-65.04</td>
<td>--</td>
</tr>
<tr>
<td></td>
<td>1250</td>
<td>-61.79 ± 2.50</td>
<td>--</td>
<td>-65.04</td>
</tr>
</tbody>
</table>
Figure 1

![Graph showing the relationship between oxygen pressure at 1123 K (atm) and nonstoichiometry (δ) for different cobalt oxide compounds.

- **GdCoO$_{2.968}$**: High Δ$f^\text{ox}$ (kJ/mol) value.
- **SmCoO$_{2.982}$**: Medium Δ$f^\text{ox}$ (kJ/mol) value.
- **NdCoO$_{2.985}$**: Low Δ$f^\text{ox}$ (kJ/mol) value.
- **LaCoO$_{2.992}$**: Very low Δ$f^\text{ox}$ (kJ/mol) value.

The graph highlights the trend where higher oxygen pressures at 1123 K correlate with lower nonstoichiometry values, except for GdCoO$_{2.968}$ which shows an exception due to its high Δ$f^\text{ox}$ value. The points for each compound are marked with either a dot or a square, indicating the specific data points for each condition.
Figure 2 (a)

![Graph showing the relationship between ionic radius of Ln$^3+$ and $\Delta_f^{OX}$ for LnCoO$_2$. The graph includes points for GdCoO$_{2.968}$, SmCoO$_{2.982}$, NdCoO$_{2.985}$, and LaCoO$_{2.992}$. The x-axis represents the ionic radius of Ln$^3+$ in Å, and the y-axis represents $\Delta_f^{OX}$ in kJ/mol. The points are connected by a line, indicating a trend.]
Figure 2 (b)

![Graph showing the relationship between tolerance factor and $\Delta H^{ox}$ kJ/mol for different compounds: GdCoO$_{2.968}$, SmCoO$_{2.982}$, NdCoO$_{2.985}$, and LaCoO$_{2.992}$]
Graphical Abstract