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Structure, Viscoelasticity, and Interfacial Dynamics of a Model Polymeric Bicontinuous Microemulsion

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Abstract

We have systematically studied the equilibrium structure and dynamics of a polymeric bicontinuous microemulsion (B μ E) composed of poly(cyclohexylethylene) (PCHE), poly(ethylene) (PE), and a volumetrically symmetric PCHE-PE diblock copolymer, using dynamic mechanical spectroscopy, small angle X-ray and neutron scattering, and transmission electron microscopy. The B μ E was investigated over an 80 °C temperature range, revealing a structural evolution and a rheological response not previously recognized in such systems. As the temperature is reduced below the point associated with the lamellar-disorder transition at compositions adjacent to the microemulsion channel, the interfacial area per chain of the B μ E approaches that of the neat (undiluted) lamellar diblock copolymer. With increasing temperature, the diblock-rich interface swells through homopolymer infiltration. Time-temperature-superposed linear dynamic data obtained as a function of frequency show that the viscoelastic response of the B μ E is strikingly similar to that of the fluctuating pure diblock copolymer in the disordered state, which we associate with membrane undulations and the breaking and reforming of interfaces. This work provides new insights into the structure and dynamics that characterize thermodynamically stable B μ Es in the limits of relatively weak and strong segregation.

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Introduction

Materials containing bicontinuous morphologies, characterized by discrete phases that percolate in three dimensions forming interpenetrating networks with a large surface area to volume ratio, are desirable for many applications including catalysis, filtration, and energy technologies.¹⁻⁷ To date, a host of ingredients (metals,⁸ oxides,^{9,10} surfactants,⁶ and polymers³) and processing strategies (both kinetic^{11,12} and thermodynamic^{3,6}) have been exploited to control the characteristic length scale and physical properties of such co-continuous structures. Polymers are particularly attractive for this purpose.^{13,14} A variety of approaches afford access to characteristic length scales in co-continuous polymeric systems that range from nanometers to millimeters.^{3,4,12,15-21} For example, recent work has shown that a kinetically controlled co-continuous structure with nanometer scale features can be trapped by *in situ* cross-linking through a process called polymerization-induced microphase separation.^{12,20,22} In contrast, coarsening of a two-phase morphology generated by spinodal decomposition of polymer/solvent blends can lead to bicontinuous structures with micrometer, and even millimeter size domains.^{4,18,21,23,24} Immiscible liquid blends stabilized with surfactants or block polymers enable the formation of thermodynamically stable bicontinuous phases with feature sizes intermediate to these two length scales.^{3,25}

Ternary systems composed of two immiscible liquids and a corresponding amphiphile (e.g., blends of either oil/water/surfactant or A- and B-type homopolymers stabilized with the corresponding AB diblock copolymer) are characterized by rich phase diagrams containing numerous morphologies and exhibiting an extraordinary range of structural dynamics.²⁵⁻³³ Under appropriate conditions such three-component mixtures will self-assemble into a thermodynamically stable bicontinuous microemulsion (B μ E) with structural dimensions ranging from 10 to 500 nm.^{3,25,27} The B μ E is globally isotropic, but contains locally correlated domains of either oil/water or A/B homopolymers mediated respectively by surfactants or AB diblock copolymers at the interface (Figure 1).^{25,27} The interfacial curvature in a perfectly balanced mixture is characterized by zero mean curvature, $H = [R_1 + R_2]/2 = 0$, and negative Gaussian

curvature, $K = R_1R_2 < 0$, where R_1 and R_2 are the principal curvatures of the interface (see Figure 1).²⁷ The detailed structure of a B μ E can be quantitatively characterized using either small-angle neutron or small-angle X-ray scattering (SANS or SAXS) aided by the Teubner-Strey (T-S) model, derived from an order parameter expansion of the free energy density.³⁴ The domain spacing (d), correlation length (ξ), and amphiphilicity factor (f_a) of the B μ E can be extracted by fitting the T-S model to experimental scattering data.^{34,35} This fascinating state of molecular organization forms through a combination of complex interactions involving interfacial dynamics, bending modulus, preferred curvature, and surface tension. Although a variety of theoretical descriptions have been advanced, a complete theory that fully captures the thermodynamic and dynamic features of the B μ E remains elusive.³⁶⁻⁴²

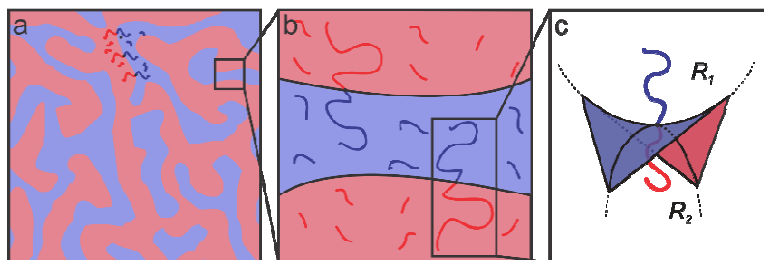


Figure 1. Schematic illustrations representing the varying length scales of the B μ E. (a) The B μ E morphology is globally disordered with (b) domains separated by diblock copolymers at the interface and swollen with homopolymer. (c) The interfacial curvature of a perfectly structured B μ E is characterized by zero mean curvature ($H = [R_1 + R_2]/2 = 0$) and negative Gaussian curvature ($K = R_1R_2 < 0$).

Polymeric systems are very well suited for studying the fundamental nature of the B μ E state. An especially enabling and simplifying attribute is the identical chemistry associated with the A and B homopolymers and the individual blocks in an A-B diblock copolymer, which provides powerful flexibility in designing such mixtures with near perfect structural symmetry. By controlling the composition and molecular weight of the diblock, and molecular weight of the individual homopolymers, the location of the B μ E in the three-dimensional phase space (volume fraction of each component and temperature at constant pressure) can be precisely specified.

Moreover, the dynamics of a B μ E are intimately connected to the viscoelastic properties of the ingredients, which also can be tuned by regulating the molecular weight and glass transition temperature of each component. Judicious choice of the A and B polymers provides additional advantages, including access to isotopic labeling (essential for SANS) and the ability to fix the morphology for investigation by transmission electron microscopy (TEM) through rapid quenching below the glass transition (or melting) temperature. We developed the saturated hydrocarbon system comprised of poly(cyclohexylethylene) (PCHE) and poly(ethylene) (PE) homopolymers, and the corresponding PCHE-PE diblock copolymer, in order to capitalize on these advantages.³² This report describes an in-depth investigation of the structure and dynamics of the B μ E created by mixing these three materials.

Equilibrium and non-equilibrium structure and dynamics of the polymeric B μ E morphology have been studied using a variety of techniques, with a majority of the experimental work involving rheological, scattering, and real-space imaging methods.⁴³⁻⁵¹ Linear viscoelastic studies have shown that the B μ E morphology has “excess” viscosity and elasticity arising from the structured nature of the fluid, similar to the behavior of sponge phases,^{52,53} liquid crystal based blue phases,^{54,55} and worm-like micelles.⁵⁶⁻⁵⁹ The “excess” linear viscoelasticity has been well described by the Pätzold-Dawson model, which anticipates certain general features of polymeric B μ Es, but there are discrepancies in the viscosity and the relaxation times.^{43,44,60} Specifically, the Pätzold-Dawson model contains a single relaxation time, but dynamic light scattering (DLS) and X-ray photon correlation spectroscopy (XPCS) studies of polymeric B μ Es have revealed multiple relaxation mechanisms that are hypothesized to arise from domain diffusion, copolymer dynamics, and undulating interfaces.^{43,46,47} Interestingly, bicontinuous morphologies and membrane structures derived from surfactants also exhibit multiple relaxation times, similar to polymeric systems.⁶¹⁻⁶⁴

Here, we report an extensive experimental study of a PCHE-PE/PCHE/PE B μ E across a broad range of the structural parameters (including d , ξ , and particularly f_a) by investigating this system over a large (80 °C) temperature interval. This work builds upon previous reports related

to other B μ E systems.⁴³⁻⁴⁸ The structural and dynamical features of the B μ E were probed using SANS, SAXS, dynamic mechanical spectroscopy (DMS), and transmission electron microscopy (TEM). We have discovered that at low temperatures, the diblock copolymer located at the interface in the B μ E experiences a molecular environment (interfacial packing) similar to that encountered in the undiluted, neat diblock in the lamellar (LAM) morphology at equivalent temperatures. With increasing temperatures, the homopolymers intermix with the diblock copolymers and swell the B μ E interface, leading to a reduction in domain spacing and increase in the interfacial area per diblock chain. We associate the terminal relaxation response with membrane undulations and the breaking and reforming of interfaces, and draw analogies to the rheological response of worm-like micelles and sponge phases.⁶⁵⁻⁶⁹ Previous reports have involved more limited temperature windows that did not capture in a single sample the full progression of structures reported here. This work highlights the intricate interplay between structure and dynamics in B μ E systems, and provides a better understanding of the underlying mechanisms that drive the fascinating behavior of thermodynamically stable co-continuous morphologies in which the interface controls the properties.

Experimental

Materials and molecular characterization Detailed synthetic procedures and molecular characterization methods employed in this work are described elsewhere.³² Briefly, polyethylene (PE, $M_n = 2.1$ kg/mol,) and polycyclohexylethylene (PCHE, $M_n = 2.6$ kg/mol) homopolymers and a symmetric poly(cyclohexylethylene-*b*-ethylene) (PCHE-PE-14, $M_n = 13.6$ kg/mol, volume fraction of the PCHE block $f_c = 0.52 \pm 0.01$) diblock copolymer were prepared by catalytic hydrogenation of the corresponding unsaturated precursors (poly(1,4-butadiene), poly(styrene), and poly(styrene-*b*-1,4-butadiene), respectively) synthesized by anionic polymerization. See Table 1 for additional molecular details. For neutron scattering experiments, the poly(styrene) precursor was saturated using deuterium gas, resulting on average in 4.5 deuterium atoms per repeat unit of the d-PCHE homopolymer, determined gravimetrically; full deuteration (*i.e.*, 6

deuterons per repeat unit) was not obtained due to hydrogen-deuterium solvent-polymer exchange.⁷⁰

Table 1. Molecular characterization of homopolymers and diblock copolymer.

Polymer	M_n (kg/mol) ^a	N^b	$D = M_w/M_n^c$	f_{PCHE}^d	T_{ODT} (°C) ^e
PCHE	2.6	39	1.06	-	-
PE	2.1	38	1.05	-	-
PCHE-PE-14 ^f	13.6	230	1.08	0.52	189 ⁷¹

a) Number average molecular weight, determined from SEC performed on unsaturated precursors. b) Volumetric degree of polymerization, based on 118 Å³ reference volume and published densities at 140 °C.⁷² c) Molecular weight dispersity measured for unsaturated precursors by size exclusion chromatography (SEC) in tetrahydrofuran at 25 °C (no evidence of broadening was evident in SEC of the fully saturated polymers. However, SEC of polyethylene containing polymers was done at elevated temperatures in a separate instrument with significant instrument smearing. Therefore, we believe the dispersities measured for the unsaturated precursors more accurately reflect the true dispersity.) d) Volume fraction PCHE calculated from ¹H-NMR spectroscopy on the unsaturated precursors and based on melt densities at 140 °C. e) Order-disorder transition temperatures, measured by DMS. f) PCHE-PE-14 contained a small amount (≤ 3 vol. %) of residual PCHE homopolymer.

Blend preparation The B μ E-forming blend was prepared by co-dissolving the appropriate quantity of each polymer in hot benzene (just below the boiling temperature ~ 80 °C), followed by quenching the solution in liquid nitrogen and freeze-drying under dynamic vacuum for 24 h to remove the solvent. The total homopolymer volume fraction (ϕ_H) for the ternary blend studied was $\phi_H = 0.86$, with the volume ratio between the PCHE and PE homopolymers $\phi_{\text{PCHE}}/\phi_{\text{PE}} = 1$.

Dynamic mechanical spectroscopy (DMS) Most DMS measurements were conducted using the 25 mm diameter, stainless steel, parallel plate geometry on a Rheometrics Scientific ARES strain-controlled rheometer equipped with a forced convection oven (inert nitrogen atmosphere). For increased torque on selected samples, we employed 40 mm diameter plates on a TA Instruments Discovery Hybrid Rheometer with a forced convection oven (inert nitrogen

atmosphere). All polymer samples were loaded to give a gap of approximately 1 mm, heated above any thermal transitions (*e.g.*, glass, melting, or order-disorder transitions), cooled at 1 °C/min to specific temperatures and held for 1 h before collecting data as a function of frequency over the range $0.01 \leq \omega \leq 100$ rad/s. Thermal expansion of the plates was accounted for to ensure that the gap dimension remained constant throughout all DMS measurements. Strains were chosen to maximize torque while remaining in the linear viscoelastic regime (see Supporting Information). Steady shear experiments were conducted between 0.001 and 100 s⁻¹ in the temperature range 120 – 220 °C (see Supporting Information). Zero-shear viscosity was determined in the limit of low shear rate.

Small angle X-ray scattering (SAXS) Synchrotron SAXS experiments were conducted at the DND-CAT 5-ID-D beamline at the Advanced Photon Source (Argonne National Laboratory, Argonne, IL USA) using the triple-detector system, which simultaneously records small-, middle-, and wide-angle X-ray scattering (SAXS/MAXS/WAXS).⁷³ An X-ray wavelength of 1.24 Å was used with SAXS, MAXS, and WAXS sample-to-detector distances of approximately 8.5, 1 and 0.2 m, respectively. 2D data were collected with Rayonix area CCD detectors; for brevity we will refer to all such experiments simply as SAXS. All scattering patterns were nearly azimuthally isotropic and were azimuthally integrated to obtain 1D plots of scattered intensity (in arbitrary units) versus scattering wave vector $q = 4\pi\lambda^{-1}\sin(\theta/2)$. The B μ E ($\phi_H = 0.86$) sample was contained in a 1.5 mm nominal diameter quartz capillary (Charles Supper Company) and the temperature was controlled during scattering experiments with a modified Linkam HFS91 heating stage. Prior to the SAXS experiments, the sample was heated to 200 °C to facilitate equilibration and to remove any processing history, slowly cooled (*ca.* 1 °C/min) to 120 °C, annealed at 120 °C under vacuum for 15 h, and then rapidly quenched to room temperature by immersion in a water bath to kinetically trap the equilibrium structure. At the beamline, the sample was quickly (*ca.* ~ 10 seconds) reheated to 120 °C to record the structure at this temperature. The sample was then heated to 200 °C and cooled back to 120 °C, pausing at several temperatures to collect scattering patterns. The sample was equilibrated at each

temperature for approximately 2 min prior to data collection while changes in temperature between measurements were rapid (> 20 °C/min).

Small angle neutron scattering (SANS) SANS experiments were performed at the National Institute of Standards and Technology (NIST), Gaithersburg, Maryland, on the 30 m NG-7 (University of Minnesota/ExxonMobil/NIST) beam line using a neutron wavelength of $\lambda = 8.09$ nm and $\Delta\lambda/\lambda = 0.115$. Three different configurations were used with sample-to-detector distances of 15.3 m (lenses inserted), 4 m, and 1 m. PE, deuterated PCHE, and B μ E samples were loaded into custom quartz banjo cells with 1.0 mm nominal path length (precise path length was determined by subtracting known quartz window thickness from the measured total cell thickness). The 2D scattering data were corrected for background and empty cell scattering, sample transmission, sample thickness, and detector sensitivity and converted to an absolute intensity scale using measurements of the direct beam flux. All measured scattering patterns were essentially azimuthally isotropic and were averaged to produce 1D plots of scattered intensity vs. q . Incoherent scattering, estimated based on the volume fraction weighted average scattering intensity at high- q from pure homopolymer samples (PE and d-PCHE), was subtracted from the B μ E scattering data. Data reduction was performed using the NCNR software package for Igor Pro provided by NIST.⁷⁴ Isotope effects are ignored in this study, as these are insignificant at the molecular weights employed.^{75,76}

Transmission electron microscopy (TEM) TEM specimens were prepared by heating the sample to 200 °C for 30 min, then cooling to the temperature of interest (120 °C, 150 °C, and 180 °C) at 1 °C/min and annealing for a minimum of 16 h. Samples were then plunged into a mixture of dry ice and 2-propanol to rapidly cool and solidify the material ($T_{g,PCHE} \cong T_{m,PE} \cong 100$ °C), fixing the blend morphology present at the annealing temperature. We estimate that the specimens are cooled below the solidification temperature in roughly 5 s.³² All samples were stained with ruthenium tetroxide vapor for 4 h to enhance contrast between microphases. Microtoming was performed at room temperature using a Leica EM UC6 ultramicrotome and a MicroStar diamond knife. B μ E sample sections were microtomed to a thickness of approximately 70 nm, and

collected on a tabbed copper grid (PELCO, 300 mesh) and imaged using a FEI Tecnai G² Spirit BioTWIN transmission electron microscope operating at a 120 kV accelerating voltage.

Results

This ternary polyolefin blend contains a mixture of PCHE and PE homopolymers with nearly equal molecular volumes ($N_{\text{PCHE}} = 39$ and $N_{\text{PE}} = 38$ are the number average degrees of polymerization based on a 118 \AA^3 reference volume and published densities) and a volumetrically symmetric PCHE-PE-14 diblock copolymer ($f_{\text{PCHE}} = 0.52 \pm 0.01$, $N_{\text{PCHE-PE}} = 230$).³² Figure 2 summarizes the PCHE-PE/PCHE/PE phase diagram for the volumetrically symmetric isopleth ($\phi_{\text{H}} = \phi_{\text{PCHE}} + \phi_{\text{PE}}$ versus T , where $\phi_{\text{PCHE}} / \phi_{\text{PE}} = 1$) for this system. A B μ E channel splits the isopleth into two distinctly different regions: (1) a diblock-rich portion of the phase diagram characterized by microphase separation into ordered lamellae (LAM) at low temperature, and (2) a homopolymer-rich region of the phase diagram characterized by macrophase separation at temperatures below a line of second-order phase transitions (Figure 2).³²

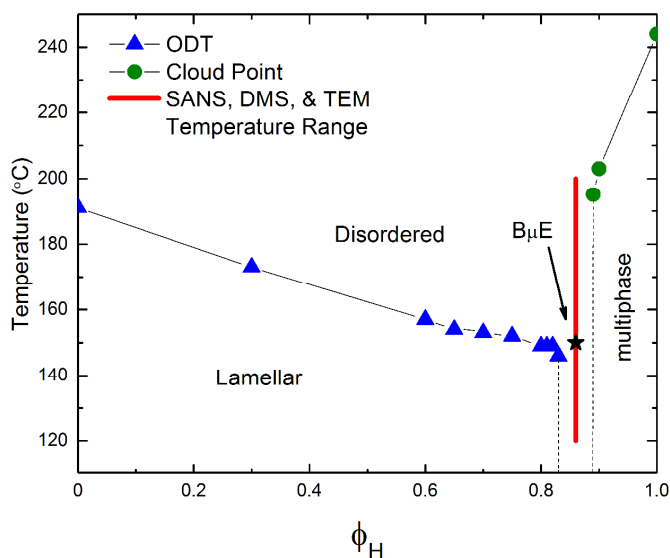


Figure 2. Phase diagram of the volumetrically symmetric isopleth for the ternary PCHE-PE-14/PCHE/PE blend where ϕ_{H} represents the total fraction of homopolymer. Blue triangles and green circles identify T_{ODT} and phase separation temperatures, respectively. The red line indicates the experimental temperature range (120 – 200 °C) and composition ($\phi_{\text{H}} = 0.86$) for

SANS, DMS, and TEM experiments on the B μ E. The black star corresponds to $T_x = 150$ °C, which is associated with the crossover from intermediate to strong segregation. All lines connecting data points are to guide the eye.

In the LAM region of phase space, DMS and SAXS were used to determine the line of order-disorder transition temperatures (T_{ODT}) and to assign the morphology, respectively.³² As previously reported, addition of PCHE and PE homopolymers to PCHE-PE-14 swells the LAM domains and results in a small concomitant decrease in T_{ODT} .³² The line of order-disorder transitions (ODT) terminates at the B μ E channel. (The character of the line of ODTs associated with the LAM-disorder transition will be the subject of a future report). In this system, the B μ E channel occurs in the homopolymer range $0.85 \leq \phi_{\text{H}} \leq 0.88$, somewhat below the theoretical Lifshitz composition ($\phi_{\text{H,L}} = 0.95$) and the associated line of unbinding transitions predicted by mean-field theory.³² Macroscopic phase separation occurs, at temperatures below the envelope of upper critical solution temperatures (UCSTs) located at homopolymer contents greater than those for the B μ E channel ($\phi_{\text{H}} \geq 0.89$), as confirmed by cloud point measurements.³² The experiments were conducted on a ternary mixture with $\phi_{\text{H}} = 0.86$ (and $\phi_{\text{PCHE}} / \phi_{\text{PE}} = 1$) as identified by the red vertical line in Figure 2. This places the material within (or above) the B μ E channel at all measurement temperatures.

Structure Real space TEM imaging was performed at room temperature on specimens quenched after annealing at various temperatures between 120 and 180 °C, as shown in Figure 3. The combined effects of PCHE vitrification and PE crystallization fixes the morphology present in the melt state and renders a material suitable for microtoming into thin (*ca.* 70 nm thick) sections. The PE domains in the images shown in Figure 3 appear lighter since semicrystalline polymers such as PE do not stain as heavily as amorphous polymers like PCHE.⁷⁷ These micrographs show no evidence of LAM and B μ E coexistence; the B μ E morphology is disordered and globally isotropic, with well-defined domains and a local periodicity of about 30 to 60 nm.

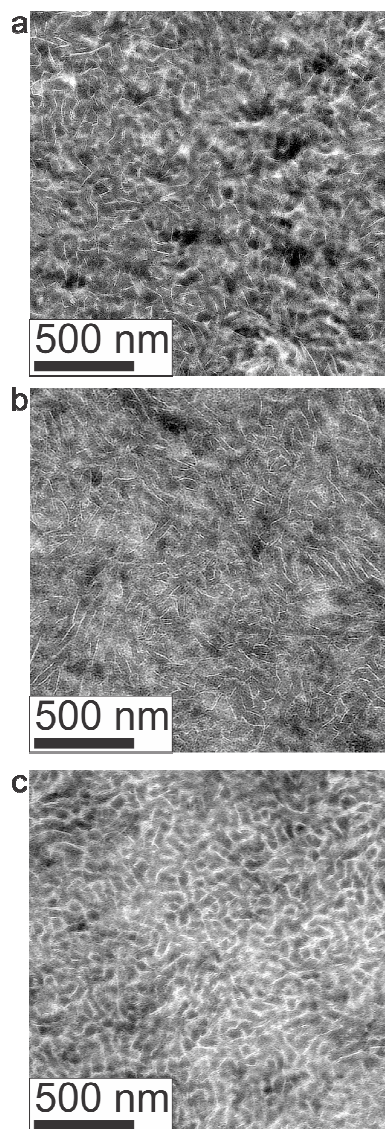


Figure 3. Transmission electron micrographs confirming a bicontinuous morphology for temperatures (a) 120 °C, (b) 150 °C, and 180 °C. All samples were annealed for at least 16 h at the indicated temperature, quenched to room temperature, stained with ruthenium tetroxide vapors and microtomed to a thickness of approximately 70 nm.

The static structure of the B μ E was evaluated over the temperature range 125–200 °C using SANS (and SAXS, see Supporting Information). As seen in Figure 4, the mixture produces a single prominent peak at all temperatures, which changes in intensity by two orders of magnitude and broadens between the highest and lowest temperatures. A nearly flat incoherent background intensity, estimated based on the weighted average of the scattering obtained from

the pure homopolymers (see Figure 4), was subtracted from these data, which are re-plotted in Figure 5. The background corrected scattering patterns were fit with the Teubner-Strey (T-S) structure factor,

$$I(q) = \frac{1}{a_2 + c_1 q^2 + c_2 q^4} \quad (1)$$

where $q = 4\pi\lambda^{-1}\sin(\theta/2)$ (λ is the wavelength, and θ is the scattering angle), and a_2 , c_1 , and c_2 are fitting coefficients.³⁴ We obtained good agreement between the SANS results and the T-S model over a large q -range, as seen in Figure 5. The model fails to quantitatively reproduce the coherent scattering intensity for $q > 0.04 \text{ \AA}^{-1}$, which is attributed to Gaussian coil scattering ($I(q) \sim q^{-2}$) from the h-PCHE blocks of PCHE-PE-14, a consequence of the lack of contrast matching with the d-PCHE homopolymer.^{43,47}

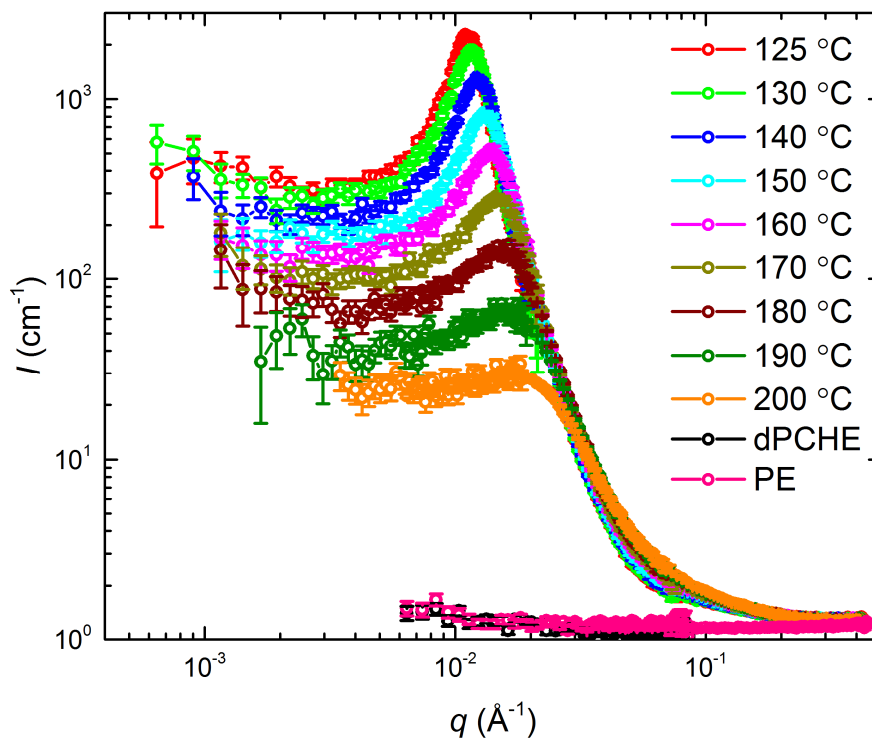


Figure 4. SANS data in units of absolute intensity acquired as a function of temperature for the B μ E; dPCHE (black) and PS (red) homopolymer data were obtained at 140 °C.

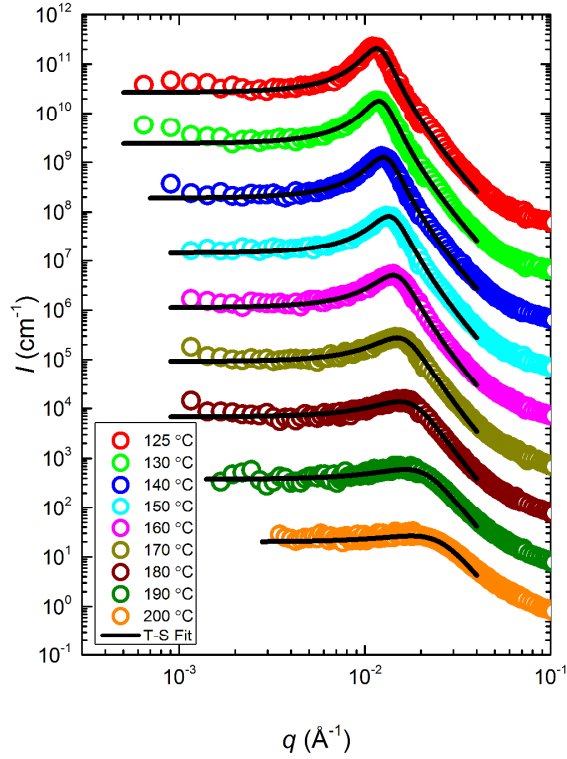


Figure 5. SANS data (corrected for incoherent background scattering) with optimized fits to the 3-parameter Teubner-Strey model (solid curves). The data at 200 °C is in absolute units. The other scattering patterns (190 –125 °C) have been vertically shifted successively by factors of 10.

Two structural length scales are associated with the fitting coefficients of the T-S model, the domain spacing (d) and the correlation length (ξ),

$$d = 2\pi \left[\frac{1}{2} \left(\frac{a_2}{c_2} \right)^{1/2} - \frac{1}{4} \left(\frac{c_1}{c_2} \right) \right]^{-1/2}, \quad (2)$$

and

$$\xi = \left[\frac{1}{2} \left(\frac{a_2}{c_2} \right)^{1/2} + \frac{1}{4} \left(\frac{c_1}{c_2} \right) \right]^{-1/2}, \quad (3)$$

where d describes the periodicity ($d/2$ is the average distance between adjacent PCHE or PE domains), and ξ is the correlation length, a measure of the spatial coherence of the interfaces between domains.³⁴ The third parameter, the amphiphilicity factor (f_a),

$$f_a = \frac{c_1}{\sqrt{4a_2c_2}} \quad , \quad (4)$$

characterizes the strength of the diblock copolymer as an interfacial agent; when $f_a = -1$, the structure is an ordered lamellar morphology, while $-1 < f_a \leq 0$ corresponds to a well-structured microemulsion.³⁵ Over the experimental temperature range of the SANS measurements (125–200 °C), d and ξ decrease with increasing temperature (Figure 6). Two limiting behaviors are found for the amphiphilicity factor, also shown in Figure 6. Above 160 °C f_a increases linearly with temperature, while below about 150 °C this parameter asymptotically approaches the strongly structured and well-segregated limit ($f_a = -1$).

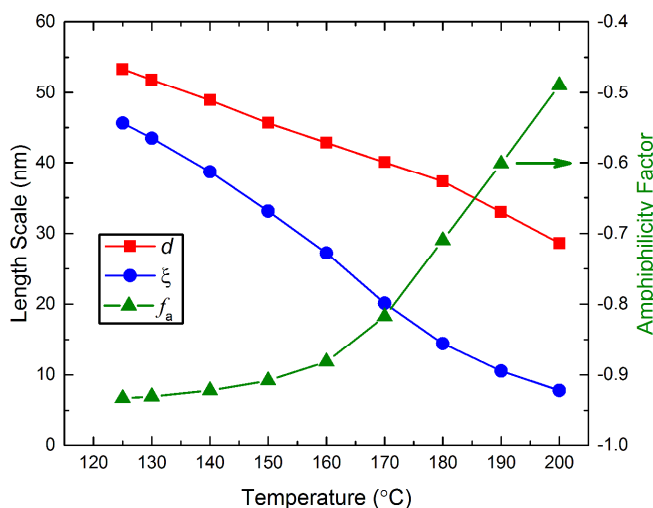


Figure 6. Domain spacing (d), correlation length (ξ), and amphiphilicity factor (f_a) as a function of temperature associated with the best fits of the Teubner-Strey model (Equation 1) to the SANS data shown in Figure 5.

Dynamics The viscoelastic properties associated with the structural features documented above were studied using DMS. Dynamic frequency sweeps ($0.01 \leq \omega \leq 100$ rad/s) were acquired over the temperature range $120 \leq T \leq 180$ °C in the linear viscoelastic regime (see Supporting Information for dynamic strain sweeps used to determine the linear regime). Recognizing the likelihood of thermorheological complexity (three different polymer components and a complex temperature dependent mesostructure), we first plotted the temperature dependent frequency data in a modified Cole-Cole format (Figure 7). This treatment of the data, which involves no arbitrary shifting factors, results in a surprisingly effective collapse of the rheological data onto a mostly temperature independent master curve, particularly at high modulus (*i.e.*, low temperature or high frequency). This motivated us to apply the time-temperature superposition (tTS) principle in order to extract additional insight into the underlying dynamical processes through comparison of the responses of the B μ E and the individual components on a common basis (*i.e.*, a single master plot). Figure 8 shows a tTS master plot for the B μ E constructed by placing an emphasis on the high modulus (*i.e.*, high frequency) data using a reference temperature of $T_{\text{ref}} = 140$ °C. The corresponding shift factors (a_T) were fit to the Williams-Landel-Ferry (WLF) equation, $\log(a_T) = -C_1(T - T_{\text{ref}}) / (C_2 + T - T_{\text{ref}})$, where $C_1 = 16.09$, and $C_2 = 164.13$ °C, based on $T_{\text{ref}} = 140$ °C (Table 2, and Supporting Information). As seen in Figure 8, there is good superposition of the data for the B μ E over a majority of the frequency and temperature ranges. Non-terminal behavior for the storage (G') and loss (G'') moduli ($G' \sim G'' \sim \omega^{1/2}$) is apparent at high frequencies ($a_T \omega > 1$ rad/s), while for $a_T \omega < 0.1$ rad/s a terminal response is evident ($G' \sim \omega^2$ and $G'' \sim \omega^1$). Below about 160 °C there is a subtle but systematic failure of superposability in G' with decreasing temperature (inset of Figure 8), similar to what has been reported in dynamically symmetric disordered diblock copolymer melts and attributed to composition fluctuations.^{71,78} Unfortunately, we could not fully establish this trend due to an inability to access the terminal regime below 145 °C at manageable frequencies ($\omega \geq 0.01$ rad/s).

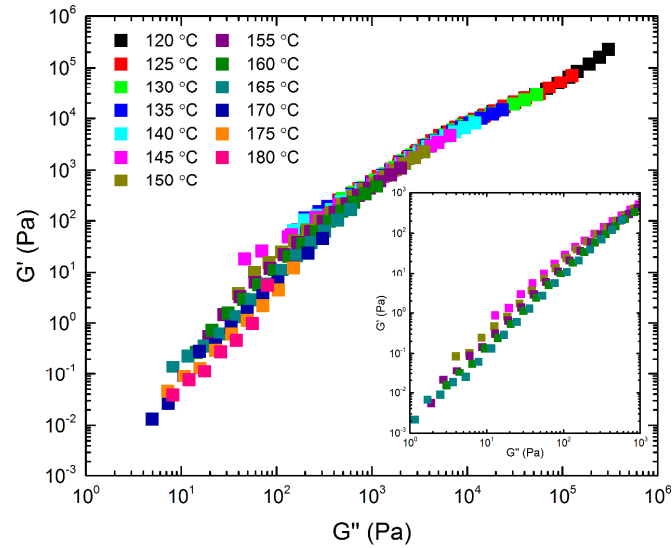


Figure 7. Dynamic elastic (G') and loss (G'') moduli obtained from the B μ E over the range of frequencies $0.01 \leq \omega \leq 100$ rad/s and indicated temperatures plotted in modified Cole-Cole format. The inset highlights failure of the data to superpose at the lowest moduli values.

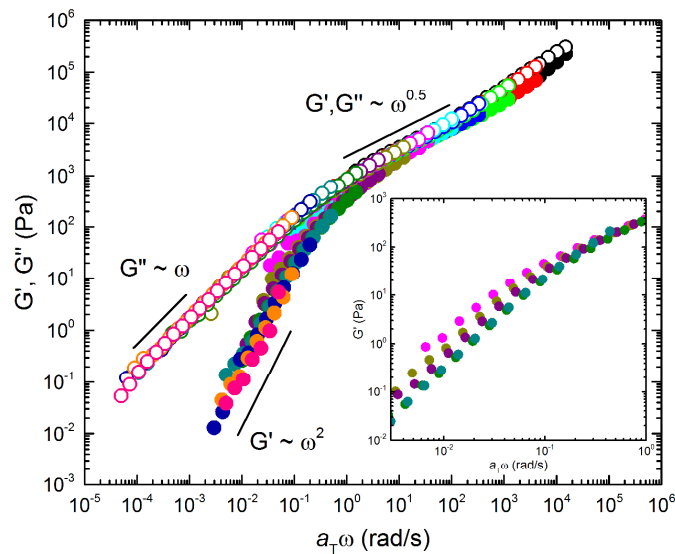


Figure 8. Master plot of the linear dynamic elastic (G') and loss (G'') moduli for the B μ E. Time-temperature shift factors (a_T) were obtained by shifting on G'' with $T_{\text{ref}} = 140$ °C giving WLF parameters of $C_1 = 16.09$ and $C_2 = 164.13$ °C. The inset reveals a failure to superpose G' in the terminal regime. The inset data were obtained by extending the frequency region using a stress controlled TA Instruments Discovery Hybrid Rheometer. G' and G'' are indicated with closed and open symbols, respectively. Color of symbols represent temperatures indicated in Figure 7.

WLF parameters also were determined for pure PCHE-PE, and the PCHE and PE homopolymers, and these values are listed in Table 2 (see Supporting Information for the raw and shifted data). In order to avoid ambiguities associated with the ODT we have assigned the shift factors for PCHE-PE-14 diblock copolymer based on values obtained from another symmetric, ordered sample, PCHE-PE-18 ($M_n = 18.9$ kg/mol, $f_{\text{PCHE}} = 0.51$, and $T_{\text{ODT}} = 317$ °C);⁷¹ previous reports demonstrate the validity of this approach with symmetric diblock copolymers of similar molecular weight.^{78,79} Interestingly, the WLF parameters calculated for the B μ E differ significantly from both the PCHE and PE homopolymers and the diblock copolymer (Table 2). Naively, one might expect the WLF parameters for the B μ E to be close to those for the diblock and the PCHE homopolymer, since $T_{g,\text{PCHE}} \gg T_{g,\text{PE}}$, *i.e.* PCHE should dominate the temperature dependence of all three systems. However, neither set of C_1 and C_2 parameters adequately superposes the B μ E DMS data (see Supporting Information). We return to this point in the Discussion Section.

Table 2. WLF parameters for the B μ E, PCHE-PE-14, and PCHE and PE homopolymers at $T_{\text{ref}} = 140$ °C.

Sample	T_{ref} (°C)	C_1	C_2 (°C)
B μ E	140	16.1	164
PCHE-PE-14 ^a	140	8.37	64.3
PCHE ^a	140	8.82	90.4
PE	140	2.43	295

a) PCHE-PE-14 and PCHE WLF parameters for $T_{\text{ref}} = 140$ °C were calculated using the relationships $C_{1,140} = C_{1,\text{ref}} C_{2,\text{ref}} / (C_{2,\text{ref}} + T_{140} - T_{\text{ref}})$ and $C_{2,140} = C_{2,\text{ref}} + T_{140} - T_{\text{ref}}$ (see Supporting Information).

Temperature-independent master plots of G' and G'' for the B μ E and PCHE-PE-14 based on $T_{\text{ref}} = 140$ °C and the shift factors listed in Table 2 are presented in Figure 9. There is remarkable similarity between the reduced viscoelastic properties of the B μ E and disordered PCHE-PE-14 exposed by this master plot. (The low frequency response of the ordered branch of the PCHE-PE-14 data reflects a solid-like response due to the polycrystalline long-range ordered

LAM morphology).⁸⁰ To a close approximation, both sets of G' and G'' data can be superimposed by vertically shifting the B μ E results upward by about two orders of magnitude. Most strikingly, the reduced relaxation time $\tau_c = (a_T\omega)_c^{-1}$ of the pure PCHE-PE-14 is essentially identical to that of the B μ E, which contains 86% by volume homopolymer, where $(a_T\omega)_c$ represents the reduced frequency associated with the transition to terminal behavior. The molecular relaxation time constants for the homopolymers are smaller by three or more orders of magnitude than τ_c for the diblock copolymer and microemulsion (see Supporting Information). These results unambiguously demonstrate that the dynamical behavior of the disordered state is controlled by sheets of diblock copolymers that constitute the interfaces separating PE and PCHE in both the fluctuating pure diblock and bicontinuous microemulsion. We expand on this finding in the following section.

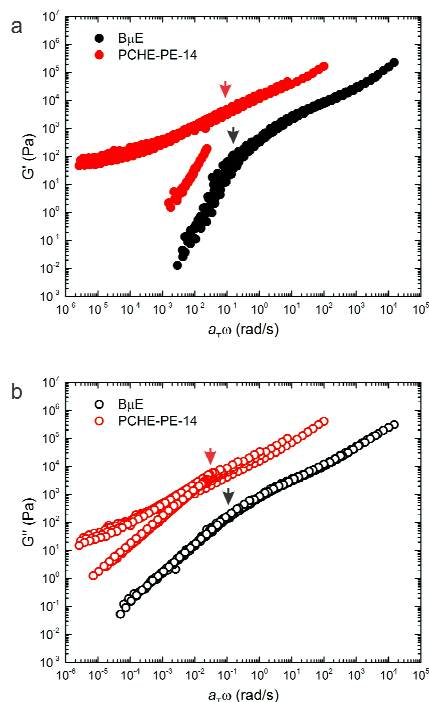


Figure 9. Master plots of the (a) storage (G') and (b) loss (G'') moduli for the B μ E and PCHE-PE-14 with $T_{\text{ref}} = 140$ °C. Time-temperature shift factors (a_T) for the B μ E were obtained from shifting on G'' with $T_{\text{ref}} = 140$ °C. PCHE-PE-14 data were shifted using WLF parameters acquired from another symmetric PCHE-PE diblock copolymer and corrected to $T_{\text{ref}} = 140$ °C. Arrows indicate terminal relaxation frequencies for the B μ E and PCHE-PE-14 samples.

The temperature dependence of the zero shear viscosity (η_0) for the B μ E, PCHE-PE-14, and the PCHE and PE homopolymers, are presented in Figure 10. This property was determined using two procedures: linear oscillatory shear ($\eta_0 = \eta'(\omega \rightarrow 0) = G''/\omega$, filled symbols) and steady shear (open symbols) experiments. Within experimental uncertainty both methods yield identical results (also see Supporting Information). The temperature dependence of the viscosity of the B μ E is clearly different from those of both the diblock and the homopolymers, consistent with the results listed in Table 2.

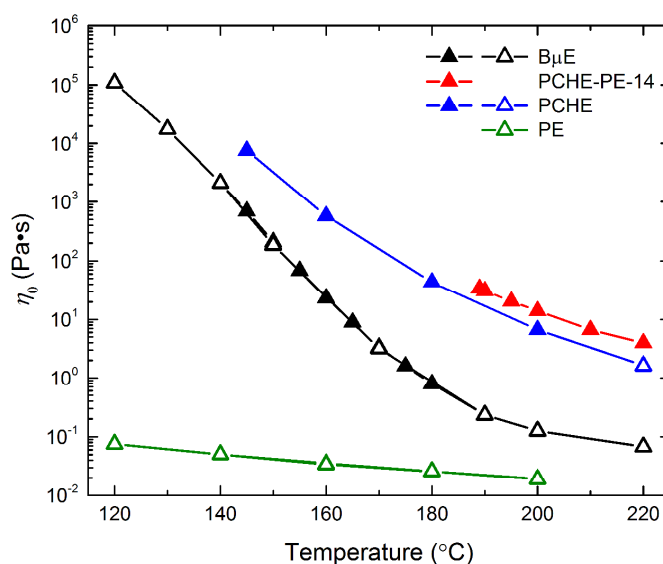


Figure 10. Temperature dependence of the zero shear viscosity (η_0) for the B μ E, PCHE-PE-14, and PCHE and PE homopolymers. The zero shear viscosity was determined using linear dynamic ($\eta_0 = \eta' = G''/\omega$ in the limit of $\omega \rightarrow 0$; closed triangles) and steady shear (open triangles) experiments.

Discussion

The experimental results presented in the previous section reveal the structural and dynamical features that govern this fascinating state of condensed matter. Figure 11 summarizes schematically what we have deduced regarding the equilibrium structure that emerges as the ternary mixture is cooled from a mean-field homogeneous state at high temperatures, to a

fluctuating, highly structured, bicontinuous morphology at temperatures below approximately 150 °C. The transition temperature, $T_x = 150$ °C, identified by a black star in Figure 2, coincides with two seemingly independent features: (1) as the temperature within the B μ E channel extrapolated from the line of LAM-disorder transitions at lower homopolymer concentrations, and (2) the point that defines the low temperature behavior of f_a (Figure 6). This section describes the rationale behind the illustrations in Figure 11 and the associated dynamic consequences.

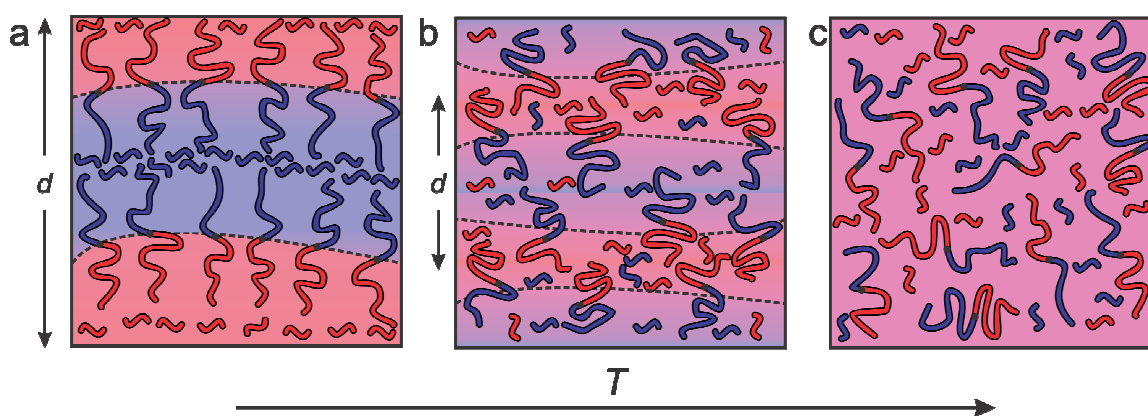


Figure 11. Scheme representing the change in the interfacial area per chain, domain spacing (d), and degree of polymer intermixing with respect to temperature (T) for the B μ E sample. (a) At low temperatures ($T \ll T_x$), the PCHE-PE-14 diblock copolymer packs at the interface with the same crowded areal density as the neat LAM forming diblock copolymer. In this temperature regime, homopolymers are largely excluded from the interfacial region. (b) At intermediate temperatures ($T \approx T_x$) homopolymers penetrate into the interfacial region, leading to an increase in the surface area per diblock chain and a reduction in d . (c) At significantly increased temperatures ($T \gg T_x$), the system reaches a mean-field homogeneously mixed state.

Structure We first estimate the interfacial area per diblock copolymer chain (A_c) from estimates of the interfacial area per unit volume (S) of the B μ E. A_c is related to S for the B μ E (and the LAM and DIS states in PCHE-PE-14) by

$$A_c = \frac{SM_n}{(1-\phi_H)\rho N_{av}} \quad (5)$$

where N_{av} is Avogadro's number, ρ is the density and M_n is the molecular weight of the block copolymer chain.⁴⁷ In principle, S can be extracted from any 2-phase system using Porod's law⁸¹

$$S = q^4 I(q \rightarrow \infty) / 2\pi (\Delta\rho)^2 \quad (6)$$

where $\Delta\rho$ is the difference in scattering length density. We can eliminate $\Delta\rho$ by invoking the scattering invariant, Q_I , given by⁸¹

$$Q_I = \int_0^\infty q^2 I(q) dq = 2\pi^2 (\Delta\rho)^2 \phi_{PCHE} (1 - \phi_{PCHE}) \quad (7)$$

where ϕ_{PCHE} is the total volume fraction of PCHE (0.5 for the B μ E). Combining equations 6 and 7 yields

$$S = q^4 I(q) \pi \phi_{PCHE} (1 - \phi_{PCHE}) / Q_I \quad (8)$$

Here we note that equations 6, 7 and 8 are based on the assumption of an ideal two-phase structure in which compositionally uniform domains are separated by sharp interfaces, *i.e.*, the scattering length density profile normal to an interface is a step function. This condition is not strictly satisfied for the B μ E studied here. At temperatures around T_x the true scattering length density profile varies smoothly, with a finite interfacial width that approaches the domain dimension d with increasing temperature. This also reduces the average magnitude of $\Delta\rho$ below what would be calculated for the pure homopolymers. Both of these effects impact the quantitative application of Porod's law. Nevertheless, the qualitative trends that result from changing the temperature of the B μ E are captured by this simple analysis.

The experimental SANS data at high q (Figure 5) are dominated by contributions from the incoherent background and scattering arising from the h-PCHE blocks within the d-PCHE homopolymer domains. This precludes reliable extraction of S using a direct application of Porod's law. Therefore, we have taken advantage of the excellent quality of the T-S fits to the SANS data and used these fitted functions to estimate Q_I and calculate S and A_c , assuming these functions apply over all values of q . As seen in Figure 12, A_c thus calculated increases from 4.1 nm² at 125 °C to 24.7 nm² at 200 °C. A similar trend was reported previously for another polymeric BμE.⁴⁷

We have estimated A_c for the neat PCHE-PE-14 diblock copolymer in the LAM and DIS states for comparison with the BμE, using $S_{\text{LAM}} = q^* / \pi$ and $S_{\text{DIS}} = 0.5q^*$.^{82,83} The relationship $S_{\text{DIS}} = 0.5q^*$ is an approximation drawn by analogy with the structure of the bicontinuous morphology that results from spinodal decomposition of a mixture of two immiscible liquids.⁸²⁻⁸⁴ Values of q^* were determined from SAXS data obtained from previously reported work⁷¹ and the associated S values were converted to A_c using equation 5 and are plotted in Figure 12. (The jump in A_c with disordering, at virtually constant q^* , reflects an increase in the interfacial area associated with the transition from lamellae to a fluctuating bicontinuous state, as discussed elsewhere.⁸²) Remarkably, the area per block copolymer chain for the BμE asymptotically approaches that of the PCHE-PE-14 chains in the undiluted LAM morphology in the low temperature limit. Hence, we conclude that cooling the ternary mixture deep into the bicontinuous channel, $T \ll T_x$, leads to the expulsion of homopolymer from the interfacial region as illustrated in Figure 11a.

The T-S fits to the SANS data also allow an estimate of the extent of segregation between PCHE and PE (proportional to $\Delta\rho$) as a function of temperature based on the invariant Q_I (equation 7). The relative amplitude of the composition profile can be expressed as,

$$\Delta\rho / \Delta\rho_{\text{cal}} = \sqrt{\left[Q_I / 2\pi^2 \phi_{\text{PCHE}} (1 - \phi_{\text{PCHE}}) \right]} / \Delta\rho_{\text{cal}} , \quad (9)$$

where $\Delta\rho_{cal} = 2.7 \times 10^{-6} \text{ \AA}^{-2}$ represents the maximum scattering contrast that would be obtained from pure d-PCHE and PE domains. The results of this analysis, plotted in Figure 13, reveal that the average amplitude of the composition profile changes by a factor of 2 as the mixture is cooled from 200 °C to 125°C. We have illustrated this feature schematically in Figure 11 by separating the purple background color evident at the highest temperature (Figure 11c) into a continuously graded background at intermediate temperature (Figure 11b) and the constituent red and blue domains in the low temperature limit (Figure 11a).

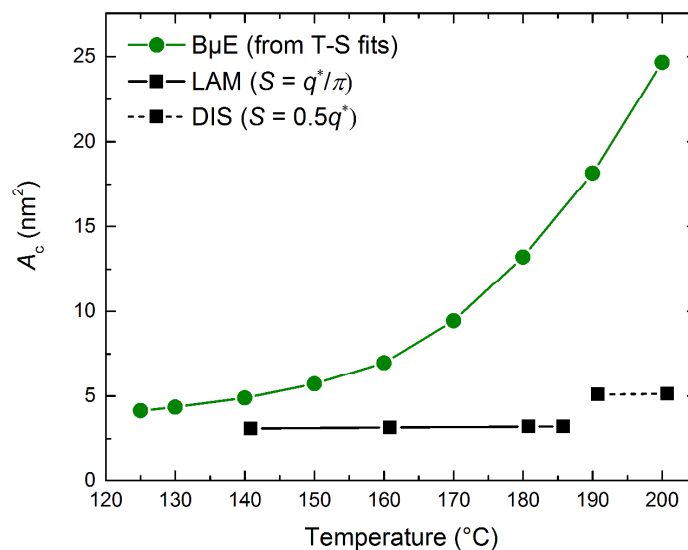


Figure 12. Temperature dependence of the interfacial area per PCHE-PE-14 chain (A_c) for the BμE and neat PCHE-PE-14 samples. A_c was calculated for the BμE sample from the Teubner-Strey functions shown in Figure 5. A_c was calculated for the neat PCHE-PE-14 sample using the relationships $S_{LAM} = q^*/\pi$ and $S_{DIS} = 0.5q^*$ for the LAM and DIS states, respectively. S is the interfacial area per volume and q^* was determined from previously reported SAXS data.^{32,71}

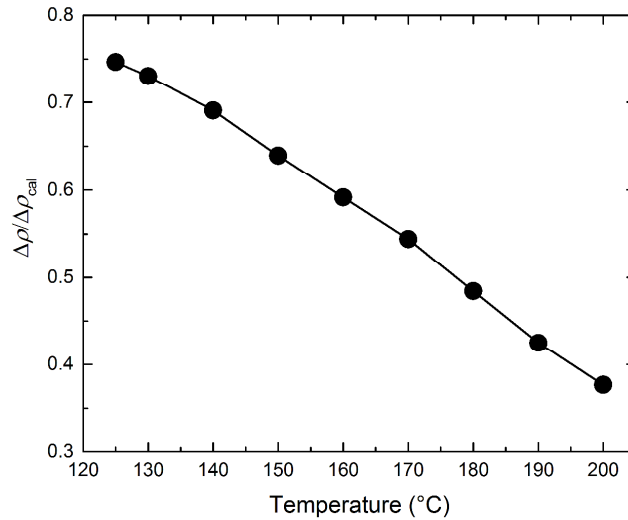


Figure 13. The ratio of the scattering length density ($\Delta\rho$) and the calculated maximum possible scattering length density ($\Delta\rho_{\text{cal}}$) with respect to temperature for the B μ E sample determined from the invariant (Q_1) using the Teubner-Strey fits to the SANS data.

Notwithstanding the assumptions involved in generating Figures 12 and 13, these results offer new insights regarding the local properties of the interface and the extent of polymer intermixing in the B μ E, as summarized in Figure 11. Although the B μ E is globally disordered at all levels of segregation, the molecular environment of the interface resembles that of the neat PCHE-PE-14 in the LAM morphology at lower temperatures. As T is reduced below T_x , the interface becomes “saturated” (“crowded”) with block copolymer, largely excluding the PCHE and PE homopolymers from the interfacial region, creating a situation analogous to the “dry-brush” regime encountered when a dense array of polymer chains are anchored to a surface in contact with an athermal melt of polymers. This exclusion of homopolymer leads to stiffening of the interface and an increase in the correlation length. Interestingly, as the B μ E interface becomes saturated with diblock copolymer and A_c approaches that of neat PCHE-PE-14, the lamellar ordering anticipated by mean-field theory does not occur.⁸⁵ Apparently, fluctuation effects, associated with a finite diblock copolymer molecular weight, overwhelm the tendency to order at reduced temperatures as opposing diblock copolymer rich interfaces become decoupled through the expulsion of homopolymer. Obviously, diblock decoupling cannot happen when ϕ_H

$\rightarrow 0$, nor at the lamellar unbinding transition in the mean-field limit (coincident with the Lifshitz composition)⁸⁵ when $N_{AB} \rightarrow \infty$.

Dynamics The temperature dependence of the zero shear viscosity of the B μ E reinforces the structural interpretations discussed in the previous section. As is evident in Figure 10, the temperature dependence of the viscosity of the B μ E differs significantly from PCHE-PE-14 and the two homopolymers. At low temperatures, the behavior of the B μ E approaches that of the diblock (and PCHE homopolymer), consistent with a morphology of two 3-dimensional interpenetrating networks of well-segregated domains enriched with each homopolymer (Figure 11a). However, with increasing temperature the opposite trend is evident, where at the highest measurement temperatures the viscosity of the B μ E more closely resembles that of the PE homopolymer. This behavior conforms to expectation for an increased state of mixing (Figure 11c) where the flow behavior is most dominated by the low viscosity component. Between these two limits, the viscosity of the B μ E is more strongly dependent on temperature than either homopolymer or the pure diblock (which is relatively strongly segregated over the entire temperature range), as reflected in the WLF parameters listed in Table 2. These dynamic phenomena are a direct consequence of the substantial differences in the viscoelastic behavior (also referred to as mechanical contrast) between PCHE and PE, due primarily to the large difference in T_g ($\Delta T_g \approx 260$ °C). To the best of our knowledge this aspect of bicontinuous microemulsion dynamics has not been recognized in previous studies.^{43-45,48}

Similarities in the frequency dependence of the linear viscoelastic properties of the B μ E and the pure disordered PCHE-PE-14 diblock, evident in the time-temperature superposed master plots (Figure 9), also supports this interpretation. At low temperatures, the diblock copolymer molecules in the B μ E morphology experience a local (crowded) environment similar to that encountered in the pure, fluctuating diblock copolymer melt above T_{ODT} . In both cases, we expect G' and G'' at reduced frequencies, $a_T\omega \geq (a_T\omega)_c$, to be dominated by interfacial dynamics, where $\tau_c^{-1} = (a_T\omega)_c$ defines the time constant associated with terminal behavior. Apparently, the presence of PCHE and PE homopolymer in the B μ E serves only to dilute the

amount of interface, which has the effect of reducing the absolute magnitude of the measured moduli, but without significantly influencing τ_c or the frequency dependence of G' and G'' for $a_T\omega \geq \tau_c^{-1}$. We have included the superposed dynamic moduli of the PCHE and PE homopolymers in the Supporting Information for comparison. (Note that G' for PE was too low to be recorded by these measurements). Clearly, the 2-dimensional sheets of diblocks control the magnitude of G' and G'' in pure PCHE-PE-14 and the B μ E; the terminal time constants for the homopolymers are orders of magnitude smaller than τ_c for the microstructured materials. However, more quantitative comparison of the homopolymer and diblock-based materials is not warranted since partial mixing of PE and PCHE greatly influences the quantitative values of the moduli in the structured materials.

Upon ordering, the low frequency ($a_T\omega < \tau_c^{-1}$) behavior of PCHE-PE-14 changes dramatically, reflecting the correlated response of periodically stacked flat interfaces ($G' \sim G'' \sim \omega^{1/2}$) as described in numerous earlier studies.^{71,78} This mode of viscoelastic response is not accessed by the B μ E, which remains disordered and liquid-like ($G' \sim \omega^2$ and $G'' \sim \omega^1$) at $a_T\omega < \tau_c^{-1}$ and all measurement temperatures.

In the terminal regime of the master plot for the B μ E (Figure 8), the G' data fail to superpose precisely, resembling previously reported work in which rheological evidence of composition fluctuations are evident in dynamically symmetric disordered diblock copolymer melts.^{71,78} Curiously, we did not find this behavior with pure PE-PCHE diblock copolymer in the vicinity of T_{ODT} , a result which was attributed to a large mechanical contrast.⁷¹ As rationalized in the previous paragraphs, we infer that the terminal regime of the B μ E reflects purely interfacial dynamics. At low temperatures ($T \ll T_x$), the system is relatively well-segregated, with saturated interfaces, and increased correlation lengths (*i.e.*, the structure is stiffer). With increasing temperature, the homopolymers mix into and “soften” the interfaces, with a concomitant reduction in the correlation length. These changes in the interfacial properties with temperature are reflected in τ_c , which increases as the temperature is reduced, leading to a reduction in $(a_T\omega)_c$ and the apparent failure of tTS. Because both homopolymers have terminal relaxation times that

are orders of magnitude shorter than the bicontinuous blend, the system is essentially mechanically “contrast matched”, which explains the similarity with the behavior of dynamically symmetric diblocks⁷¹ such as PtBS-PMMA⁷⁸ and PEP-PEE.⁸⁶

General Remarks We have characterized the structural evolution of the B μ E from the high temperature regime ($T \gg T_x$), where the system approaches the homogeneously mixed mean-field state, to low temperatures ($T \ll T_x$) where the components segregate into well-correlated domains enriched in PCHE and PE homopolymer, separated by an interface crowded with diblock copolymer. In this section we draw connections to related soft material systems, specifically, worm-like micelles and sponge phases.

Previous investigations involving B μ E systems have shown that there are multiple diffusion modes related to domain structure, amphiphile dynamics, and undulating interfaces.^{43,46,47} An X-ray photon correlation spectroscopy (XPCS) study on a polymeric B μ E demonstrated that a stretched-exponential function was required to model autocorrelation functions, indicating that a single structural relaxation time is not adequate to describe the equilibrium dynamics.⁴³ The stretched exponent values for the B μ E were found to be similar to those predicted theoretically and determined experimentally for membrane systems such as sponge phases, lamellae, and vesicles.^{61-64,87} Similarly, worm-like micelles subjected to shear deformation exhibit stretched exponential relaxation behavior, where reptation is the major mode of stress relaxation.^{59,65,66,88} Additionally, worm-like micelles exhibit a relaxation spectrum that is dependent on the relative ratio between the reptation (τ_{rep}) and cylinder breaking and reforming (τ_{break}) time constants.^{65,66} In the $\tau_{\text{rep}} \ll \tau_{\text{break}}$ regime, an ‘entanglement plateau’ is present^{65,66} and relaxation occurs by diffusion of the micelles in the entanglement network accompanied by ‘Rouse modes’ that occur along the contour of the worm-like micelle.^{59,65,66,88} This behavior is similar to stress relaxation *via* reptation of linear entangled polymer melts as described by Doi and Edwards.⁸⁹ Conversely, there is no entanglement plateau when $\tau_{\text{rep}} \gg \tau_{\text{break}}$.^{65,66} In real systems, worm-like micelles display a combination of these two relaxation mechanisms.^{59,88,90}

With lyotropic sponge phases, the topological relaxation time, or the time required for breaking and reforming of the bilayer structure, has been found experimentally to occur on fast time scales (~ 0.01 s).^{68,69} For the B μ E addressed in this study, we expect that breaking and reforming of the bicontinuous domains is thwarted at low temperatures as a result of increased segregation and rigid lamellar-like interfaces. Similar behavior is seen during the shear alignment of lamellar diblock copolymers: it is more difficult to align block copolymers well below the ODT because of slower chain relaxation dynamics and higher energy barriers.⁹¹⁻⁹⁴ As homopolymers intermix with the diblock copolymer at higher temperatures, the B μ E interface becomes more flexible, and the energetic barrier for breaking and reforming of interfaces should diminish. Therefore, we expect the B μ E to have a strongly temperature dependent interfacial relaxation spectrum, as observed experimentally. The mode of stress relaxation at high frequencies in Figure 8 appears to be Rouse-like with no ‘entanglement plateau’. Yet the B μ E contains a sheet-like diblock copolymer rich interface that is folded into an interpenetrating manifold that spans the entire volume. It is hard to imagine a mechanism analogous to reptation with this topology. Breaking and reforming the bicontinuous morphology likely involves multiple processes, including membrane undulations⁹⁵ and out-of-plane fluctuations that are common in fluid membranes formed by lipids and surfactants.^{67,96-99} For these reasons, we speculate that at time scales longer than the longest relaxation time, τ_c , the interfacial dynamics of the B μ E reflect a competition between interfacial undulations and the breaking and reforming of the interfaces, as depicted schematically in Figure 14. Further insight into this fascinating aspect of B μ Es awaits additional theory and simulation.

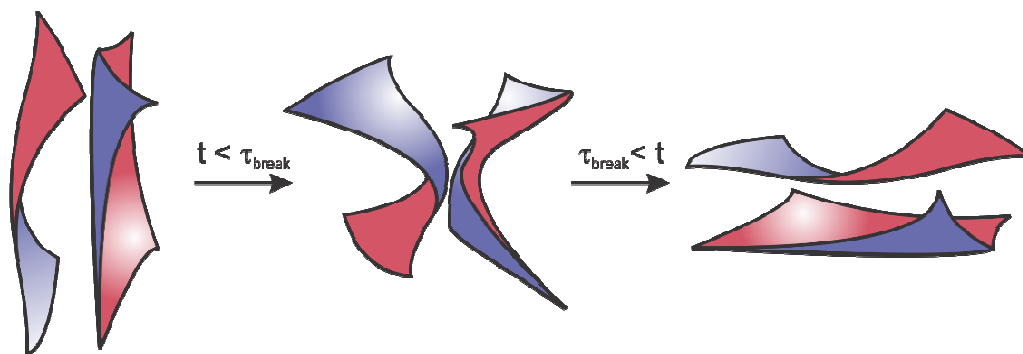


Figure 14. Scheme illustrating a proposed mechanism for the interfacial dynamics of the B μ E undergoing shear deformation. The B μ E interface is continually breaking (τ_{break}) and reforming, and is therefore fluid-like at long time scales.

This work helps to elucidate the fundamental thermodynamic driving forces for the formation of the B μ E morphology. Adding homopolymer to diblock lamellae swells the domains non-linearly, as predicted by mean-field theory and established experimentally.^{25,85} Mean-field theory anticipates that the lamellar domain spacing diverges at an unbinding transition coincident with the Lifshitz composition ($\phi_{H,L}$).⁸⁵ This prediction is not realized experimentally because thermally driven composition fluctuations preempt the unbinding transition, giving rise to the B μ E channel.²⁵ The B μ E displays structural relaxation mechanisms including interfacial undulations and the breaking and reforming of interfaces. The magnitude of membrane undulations, to a first approximation, is related to the interlayer spacing of the interfaces. If layers of membranes have a sufficiently small interlayer spacing, steric hindrance will drive the membranes to order into a lamellar morphology as a result of repulsive forces.^{67,96-99} As the interlayer spacing increases, and the interfaces decouple, the effects of steric hindrance will be reduced and permit the formation of a microemulsion phase, as predicted by de Gennes and Taupin.³⁷ We hypothesize that adding homopolymer to the diblock copolymer, which increases the domain spacing, amplifies interfacial dynamics. Exactly how this stabilizes the B μ E is an open question. We have shown in this study that interfacial dynamics are temperature dependent, and that the interface becomes stiffer at lower temperatures while simultaneously decoupling

from neighboring sheets by expulsion of homopolymer. Application of simultaneous SANS and neutron spin echo scattering, as employed by Holderer *et al.*^{100,101} to characterize the bending rigidity of surfactant based B μ Es, might provide additional insights into this aspect of the dynamics.

These considerations raise the question: Will an ordered LAM structure form as $T \rightarrow 0$? Fortunately, this pivotal question can be addressed using cleverly designed AB/A/B polymeric B μ Es. This will require precisely tuning the ratio ϕ_A / ϕ_B , and perhaps f_A , to account for the effects of conformational asymmetry, along with the establishment of efficient experimental methods to identify the exact composition that perfectly balances the mean (H) and Gauss (K) interfacial curvature. Perfect balance in real polymer systems will not occur in general at $\phi_A / \phi_B = 1$ and $f_A = 1/2$, and significant deviation from ideal interfacial symmetry will likely lead to multiphase behavior as $T \rightarrow 0$. These issues are currently under investigation.

Finally, we comment briefly on how this work relates to the large literature on surfactant/water/oil microemulsions. In the case of non-ionic surfactant systems, the B μ E window is narrow in both composition and temperature, appearing at the tip of what is referred to as the ‘fish cut’ in the phase prism.²⁷ Increasing or decreasing temperature by just a few degrees at the optimal composition leads to macroscopic phase separation. This complex phase behavior is intrinsically tied to the dual upper and lower critical solution temperature behaviors (UCST and LCST, respectively) of the hydrophobic and hydrophilic constituents of the amphiphile. Moreover, such systems are inherently structurally asymmetric due to the nature of the interactions of oil, and especially water, with the surfactant, making it difficult if not impossible to perfectly tune the overall bicontinuous morphology. These deficiencies are fully overcome with properly designed ternary AB/A/B polymeric systems as outlined in the previous paragraph.

Summary

We have presented the results and an analysis of a comprehensive study of a bicontinuous microemulsion ($B\mu E$) formed from equal volumes of poly(cyclohexylethylene) (PCHE), poly(ethylene) (PE) and 14% by volume of the corresponding PCHE-PE diblock copolymer. Small-angle neutron and X-rays scattering (SANS and SAXS) measurements, obtained over an 80 °C temperature range, were modeled using the Teubner-Strey structure factor. These experiments provide detailed information regarding the extent of segregation and the interfacial area per block copolymer molecule (A_c) well above and below the temperature extrapolated from the line of lamellar-disorder transition temperatures established at lower homopolymer concentrations denoted T_x . As the system is cooled deep into the $B\mu E$ channel ($T \ll T_x$) A_c decreases, asymptotically approaching the value that characterizes undiluted PCHE-PE in the lamellar state. This interfacial crowding of diblock copolymer and expulsion of homopolymer from the interfacial region results in a stronger state of segregation, accompanied by increases in the domain spacing and correlation length. Mechanical spectroscopy experiments reinforce this picture. Vastly different homopolymer relaxation times, attributable to disparate glass transition temperatures ($\Delta T_g \approx 260$ °C), lead to zero-shear viscosities that reflect enhanced mixing at high temperatures and stronger segregation at low temperatures. Remarkably, the time constant associated with the transition to terminal (liquid-like) behavior in the $B\mu E$, determined by linear dynamic mechanical spectroscopy, coincides with the behavior of the pure disordered diblock copolymer at a common reduced temperature. These results indicate that the rheological properties of the $B\mu E$ are controlled by the same interfacial dynamics that govern the behavior of undiluted fluctuating disordered diblock copolymer melts near the order-disorder transition. These findings offer fresh insights into the thermodynamic driving forces responsible for the formation of $B\mu E$ s and the resulting properties, and highlight opportunities to better understand this fascinating state of self-assembly.

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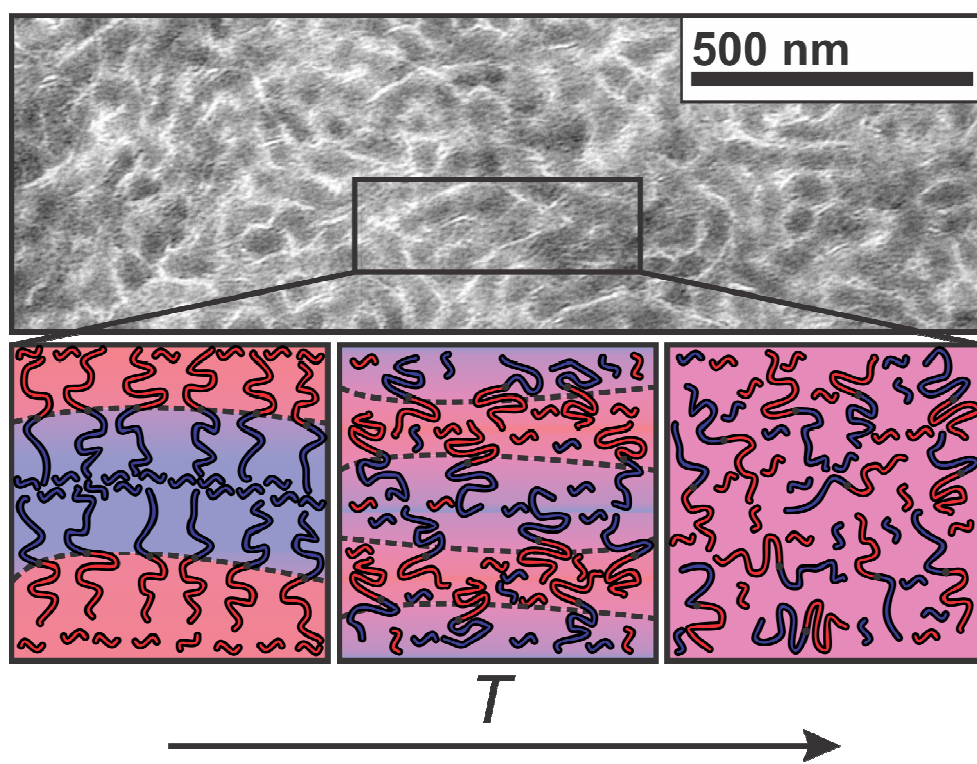
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The properties of polymeric B μ Es are controlled by the same interfacial dynamics that govern the behavior of undiluted diblock copolymer melts.