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A MASTER DYNAMIC FLOW DIAGRAM FOR THE SHEAR THICKENING TRANSITION IN MICELLAR SOLUTIONS

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Graphical Abstract

Highlights
- Shear thickening of micellar solutions of hexadecyltrimethylammonium-type surfactants and alkyltetradecylammonium bromide surfactants
- Master flow diagram of the shear thickening transition
- Intensity of shear thickening and a Hofmeister-like anion series
ABSTRACT

The shear thickening behavior of dilute micellar solutions of hexadecyltrimethylammonium-type surfactants with different counterions (tosylate, 3- and 4-fluorobenzoate, vinylbenzoate and salicylate) and of n-alkyltetradecylammonium bromide (C_nTAB), with n = 14, 16 and 18, is examined here. These solutions undergo a shear thickening transition due to the formation of shear-induced structures (SIS) in the shear range studied. Here we report a relationship among the shear thickening intensity and the differences among the counterions hydrophobicity according to the Hofmeister-like anion series, which leads to a Master Flow Diagram. This Master Flow diagram is produced by plotting a normalized shear thickening intensity (I_η - 1)/(I_{max} - 1) versus C_D/C_{D,max}, where I_η is the shear-thickening intensity, defined as the largest viscosity obtained in the shear-thickening transition (STT) at a given surfactant concentration C_D divided by the Newtonian viscosity η_0, and I_{max} is the largest intensity value obtained in the STT at a surfactant concentration C_{D,max}. The Master Flow Diagram is built using several cetyltrimethylammonium-type surfactants with different counterions, according to a Hofmeister-like series, and by n-alkyltetradecylammonium bromide surfactants with different alkyl chain lengths.

Keywords: Master dynamic flow diagram; micellar growth; shear-induced structures; shear thickening; Hofmeister-like series.
INTRODUCTION

Micellar solutions are complex fluids that exhibit a fascinating rheological behavior in the dilute, semi-dilute and concentrated regimes. In the dilute regime, shear thickening develops above a critical shear rate ($\gamma_c$) after an induction time ($t_i$); this induction time lasts from seconds to minutes and becomes shorter as the applied shear rate departs from $\gamma_c$. In the semi-dilute and concentrated regimes in which polymer-like (or wormlike) micelles form, the rheological response is controlled by either reptation (slow-breaking regime) or by breaking-and-recombination (fast-breaking regime). In the last case, Maxwell behavior with a single relaxation time is commonly observed in linear viscoelastic measurements, whereas shear-banding flow appears between two critical shear rates in nonlinear rheological measurements.

Most of the research on shear thickening behavior has been performed with cationic surfactants in the presence of inorganic electrolytes or of salts containing strongly binding counterions such as salicylate or tosylate. The reason is that micellar growth in ionic surfactant solutions is promoted by electrostatic screening that reduces the repulsion between the charged polar heads upon addition of electrolytes or by reduction of the micellar surface charge-density by adding salts with strongly binding counterions. As a consequence, the presence of electrolytes decreases the concentration at which rod-like micelles develop, $cmc$, and the overlap concentration, $c^*$, which have a strong effect on the shear thickening transition (STT) in dilute micellar solutions.

Few works have been reported in electrolyte-free ionic micellar solutions. The early work of Hoffmann and co-workers with hexadecylpyridinium salicylate (CPyS) and tetradeyltrimethylammonium salicylate (TTAS) demonstrated that these micellar solutions showed shear thickening behavior and viscoelasticity at low concentrations in the absence of...
electrolytes or other additives. Several reports on the STT of electrolyte-free cationic surfactants micellar solutions have appeared.\textsuperscript{21-26}

Sometime ago, Berret et al.\textsuperscript{27} proposed a \textit{Generalized Flow Phase Diagram} for micellar solutions for which shear-banding flow develops. In this diagram, in which the shear-stress divided by the plateau modulus ($\sigma/G_0$) is plotted against the shear-rate times the main relaxation time ($\gamma \tau_R$), the flow curves overlap at low normalized shear rates, i.e., $\gamma \tau_R < 1$; at higher normalized shear rates, a stress plateau forms that shifts to larger values of the normalized shear stress with increasing temperature or surfactant concentration. This generalized flow diagram has been reported for other micellar solutions as a function of surfactant concentration or temperature.\textsuperscript{25,28,29}

For shear thickening micellar systems, however, few attempts to describe a generalized relationship have been presented in the literature. Hu et al. reported kinetics studies of micellar solutions of tetradecyldimethylammonium oxide (TMADO) mixed with sodium dodecyl sulfate (SDS) that exhibit slow viscosity build-up and follow time-dependent stress growth upon application of a shear stress, probing changes in microstructure with optical methods. They found that the unusually slow stress build-up occurs only when the applied shear rate exceeded a critical value above which shear thickening occurs.\textsuperscript{30} Prötzl and Springer reported that three stages conformed the SIS formation: induction, aggregations and orientation and, more interestingly, that the time needed to reach the orientation stage minus the induction time ($t_o - t_i$) was independent of the applied shear-rate to induce shear-thickening.\textsuperscript{31} Oda et al. observed that $\gamma_c$ strongly depended on the gap distance of the Couette cell employed, which ruled out the SIS phenomenon as a phase transition.\textsuperscript{32}
More recently, we examined the shear thickening behavior of cetyltrimethylammonium tosylate (CTAT) micellar solutions as a function of surfactant concentration and ionic strength using electrolytes with different counterion valence, and found that the shear thickening diminishes with increasing surfactant concentration and ionic strength. From those results we proposed a generalized master flow-diagram that indicated two controlling regimes: one in which electrostatic screening dominates and induces micellar growth, and another at higher surfactant and electrolyte concentration, where chemical equilibrium among surfactant counterions and electrolyte ions controls the rheology by altering micellar breaking and recombination. More interestingly, in that paper we proposed a Hofmeister-like series of headgroups together with a predictive theory of interactions between different types of ions and head-groups.

In this paper, a Master Flow Diagram for shear thickening micellar solutions is obtained by plotting the normalized shear intensity, \( \frac{I_\eta - 1}{I_{\text{max}} - 1} \), versus the normalized surfactant concentration, \( \frac{C_D}{C_{D,\text{max}}} \), for surfactants with the same hydrophobic tail (C\textsubscript{16}) and head (trimethylammonium) but different counterions (tosylate, vinylbenzoate, salicylate and fluorobenzoate) as well as for surfactants of n-alkyltetradecylammonium bromide (C\textsubscript{n}TAB), with \( n = 14, 16 \) and \( 18 \); all of them were examined at several surfactant concentrations. Here \( I_\eta = \frac{\eta}{\eta_0} \), being \( I_{\text{max}} \) the largest intensity value obtained in the STT at a surfactant concentration, \( C_{D,\text{max}} \).

**EXPERIMENTAL SECTION**

Hexadecyltrimethylammonium tosylate (CTAT), 99% pure from Sigma, was re-crystallized from a chloroform (Aldrich) solution prior to experiments. Hexadecyltrimethylammonium salycilate (CTAS), hexadecyltrimethylammonium vinylbenzoate (CTAVB), hexadecyltrimethylammonium 3-fluorobenzoate (CTA3FB) and hexadecyltrimethylammonium 4-fluorobenzoate (CTA4FB)
were synthesized as reported elsewhere.\textsuperscript{25,34,35} Samples were prepared by weighing the appropriated amounts of surfactant and water in 20-ml glass vials, homogenized and placed in a temperature-controlled chamber at 30 °C for a week before performing the rheological tests. Diluting a 0.1 wt.% stock surfactant solution produced samples with smaller concentrations.

Steady and transient shear rate measurements were performed at 30 °C in an ARES strain-controlled rheometer, using a double wall Couette geometry with bob internal and outer diameters of 29.5 and 32 mm, respectively; cup: \(D_i = 27.94\) cm, \(D_o = 34\) cm, and a humidification chamber to minimize water losses by evaporation. For CTA3FB, steady and transient rheological measurements were carried out in a stress-controlled ARG2 rheometer from TA Instruments with parallel plate geometry of 60-mm in diameter. The rheological data of the \(n\)-alkyltetradecylammonium bromide (C\textsubscript{n}TAB) surfactants with an equimolar ratio of sodium salicylate added were taken from Dehmoune et al.\textsuperscript{36,37}

**RESULTS AND DISCUSSION**

Figure 1 depicts the apparent shear viscosity as a function of \(\dot{\gamma}\) for CTAT and CTAVB; in this Figure three concentrations of these two surfactants were included. The plots are similar but shear thickening occurs at lower shear rates in CTAVB solutions compared to the CTAT ones, which (as shown below) is consequence of the ordering of the counterions according to the Hofmeister series proposed by us elsewhere.\textsuperscript{33} The plots exhibit similar characteristics, mainly that (1) the zero-shear rate viscosity, \(\eta_0\), increases with surfactant concentration, (2) when the applied shear rate becomes equal or exceeds \(\gamma_c\), \(\eta\) begins to increase after an induction time, \(t_i\), has elapsed, and (3) the rise ends in another plateau that decreases at larger shear rates, signaling the onset of the shear thinning regime.
Figure 1. Apparent shear viscosity versus shear rate measured at 30 °C at different surfactant concentrations for CTAT: (*) 0.2, (+) 0.6 and (x) 0.8 wt. %; CTAVB: (□) 0.03, (○) 0.05 and (∆) 0.1 wt. %.

It has been documented for several cationic surfactant micellar systems, which exhibit the STT, that their induction time, $t_i$, obeys a power law-dependence with shear rate of the form $\dot{\gamma} \sim t_i^{-m}$, where $1 \leq m \leq 2^{2,3,30,35}$; however, no dependence of $t_i$ with the normalized alkyl chain length of the surfactants, $|l| = l_n / l_{C14}$, has been reported as far as we know; here, we choose the tail length of the $C_{14}$ surfactant $l_{C14}$ for the normalization procedure. Figure 2 depicts a plot of $t_i$ versus the normalized alkyl chain length of the alkyltetradecylammonium bromide surfactants examined. This figure reveals that the induction time increases almost linearly with tail length, although dispersion of data is apparent. Only three surfactants were examined because the $C_{12}$
surfactant does not form road like micelles and it does not exhibit shear-thickening\textsuperscript{36,37}; and the C\textsubscript{20} surfactant cannot exhibit the shear thickening transition probably because this surfactant tends to form hexagonal liquid crystals instead of wormlike micelles and, in fact, no reports on SIS using this surfactant have appeared in the current literature as far as we know.

**Figure 2.** Induction-time versus normalized alkyl chain-length for the C\textsubscript{n}TAB surfactants. Inset: estimated average micellar length versus the normalized alkyl chain-length of the C\textsubscript{n}TAB surfactants.

To understand the growth behavior from short to large wormlike micelles, we invoke the mean-field theory of the micellar growth process for neutral or highly screened micelles. This theory predicts the average contour-length of the wormlike micelles ($
L_c$
) in terms of surfactant concentration ($c$) and the scission energy required to produce two hemispherical end caps ($E_c$) as

$$
\overline{L_c} \sim c^{1/2} \exp \left[ E_c / k_B T \right].
$$

For charged micelles in the absence of electrolytes, the scission energy has an additional electrostatic component, $E_e$, due to the repulsion of the charges along the
backbone that favors shorter cylindrical micelles. For this situation, the mean size in the semi-dilute regime is
\[ \bar{L}_c \sim \phi^{1/2} \exp \left[ \frac{(E_c - E_e)}{2k_B T} \right] \]
with \( E_e \) expressed as \( E_e \sim k_B T l_B r_{cs} \nu^2 \phi^{1/2} \).
Here, \( l_B \) is the Bjerrum length, \( r_{cs} \) the radius of the cylindrical micelles, \( \nu \) the effective charge per unit length, and \( \phi \) the micellar volume-fraction. For the series of alkyltetradecylammonium bromide surfactants examined, the tail length of the alkyl chain is related to \( r_{cs} \) via the electrostatic contribution to \( E_c \) since all of them have the same head. Hence, following the arguments given by Schubert et al.,\(^{39}\) as the surfactant tail length increases, \( E_e \) augments as well, diminishing the net contribution of \( E_c \) and thus reducing the micellar length \( \bar{L}_c \). This tendency is observed in the inset of Figure 2 where the estimated average micellar length (|\( \bar{L}_c \)|) versus the normalized alkyl chain length of the C\(_n\)TAB surfactants is depicted. This inset reveals that the average length of the wormlike micelles decreases almost linearly with tail length. Furthermore, according to the kinetics of breaking and recombination of wormlike micelles developed by Cates,\(^{40}\) the times for breaking and recombination in our systems are expected to be similar and inversely proportional to the average length of the micelles; hence, such times can be related to \( t_i \). A further examination of Figure 2 and its inset reveals that indeed, \( t_i \) diminishes with the average micellar length.

Figure 3 depicts the shear thickening intensity, \( I_\eta \), versus surfactant concentration, \( C_D \), for all surfactants examined here, i.e., CTAT, CTAS, CTAVB, CTA3FB, CTA4Fb and C\(_n\)TAB (with \( n = 14, 16 \) and 18). For each surfactant, \( I_\eta \) first increases, reaches a maximum and then it decreases at larger surfactant concentrations, attaining values of one for some of the systems, indicating the disappearance of the STT.
Figure 3. Shear-thickening intensity as function of surfactant concentration for micellar solutions containing: CTAT (closed square), CTAVB (closed diamond), CTA3FB (closed inverted triangle), CTA4FB (closed circle), CTASal (closed triangle), and data adapted from Dehmoune et al.: C14TAB (open triangle), C16TAB (open circle), and C18TAB (open square).

The concentration range where the shear thickening region appears largely depends on the surfactant type (see Fig. 3). Depending on the counterion structure for the hexadecyltrimethylammonium-type surfactants, the \( I_\eta \) curves shift to larger concentrations in the counterions’ order: S\(^-\) < VB\(^-\) < T\(^-\) < 3FB\(^-\) < 4FB\(^-\), which suggest that 4FB\(^-\) and 3FB\(^-\) are hydrophobic anions according to the Hofmeister series and that they only promote the growth of the surfactant aggregates by reducing the electrostatic repulsion among the surfactant headgroups. These hydrophobic anions stay at the surface of the surfactant aggregates rather than penetrating into the hydrophobic core, allowing strong electrostatic repulsions between the surfactant headgroups at the interface and consequently increasing the curvature of the micelle surface and the \( cmc \) values.\(^9\,34\) At the other end of the series, S\(^-\), VB\(^-\) and T\(^-\) bind very strongly,
i.e., they penetrate into the hydrophobic core, which results in smaller cmc’s and in larger micellar surface curvature, inducing micellar growth and the formation of long wormlike micelles at substantial lower surfactant concentrations.\textsuperscript{25,34} It is noteworthy the screening effect of the sodium salicylate added to the alkyltetradecylammonium bromide (C\textsubscript{n}TAB) surfactants that shifts the \( I_\eta \) curves to lower concentration than the one exhibited by CTAS.

The trend of the surfactant counterions of hexadecyltrimethylammonium-type surfactants reported in Figure 3 can be explained by applying the concept of matching water affinities proposed by Collins\textsuperscript{41} and the surfactant head group’s Hofmeister series reported by Vlachy et al.\textsuperscript{42} Following the Hofmeister’s approach, ions have been classified according to their relative abilities to change the structure of surrounding water molecules into kosmotropes (structure makers) or chaotropes (structure breakers). Vlachy and co-workers propose the same classification for the surfactant head groups and the counterions.\textsuperscript{42} Following Collins’ concept, chaotrope head groups can form direct ion pairs with other chaotrope counterions, similarly as kosmotrope head-groups with other kosmotrope counterions. But chaotropes do not come into close contact with kosmotropes counterions. According to matching water affinities, the surfactant head group CTA\textsuperscript{+} is considered chaotrope, the counterions S\textsuperscript{-}, VB\textsuperscript{-}, and T\textsuperscript{-} can also be classified as chaotropes, whereas the counterions 3FB\textsuperscript{-} and 4FB\textsuperscript{-} can be considered as kosmotropes.\textsuperscript{42} Israelachvili’s packing parameters were calculated for the surfactants reported in Fig. 6 according to \( v/l_c a_0 \), where \( v \) is the volume of the hydrocarbon chain in the surfactant, \( l_c \) is the critical chain length and \( a_0 \) is optimal surface area per molecule.\textsuperscript{38} Values of the packing parameters obtained for the CTA-counterion surfactants were 0.49, 0.46, 0.38, and 0.37, for CTASal, CTAVB, CTAT, CTA3FB, respectively; and for all the C\textsubscript{n}TAB were 0.37. The packing parameters fall in the range \( 1/3 < v/l_c a_0 < 1/2 \) that corresponds to the formation of
cylindrical micelles. Since large packing parameters correspond to small optimal surface area for surfactants of the same chain length, Figure 6 reveals that for surfactants with smaller $a_0$, higher concentrations are required for the SIS to occur. Once again, the screening effect of the sodium salicylate added to the alkyltetradecylammonium bromide ($C_n$TAB) surfactants is evident from the shifting to smaller $I_\eta$'s; however, the $I_\eta$ curves for $C_n$TAB are shifted to lower concentration than the one exhibited by CTASal.

Data shown in Figure 3 for the different surfactants and concentrations employed can be comprised in a Master Flow Diagram (Fig. 4) by plotting the normalized shear intensity, $(I_\eta - 1)/(I_{max} - 1)$, versus the normalized surfactant concentration, $C_D/C_{D,max}$. Within experimental error, all data collapse in the shear thickening region where $C_D/C_{D,max} \leq 1$. A similar plot was reported elsewhere for CTAT solutions with several electrolytes. Figure 4 was built accordingly because it allows defining the mechanism that controls the shear thickening transition, i.e., micellar growth by electrostatic screening or micellar scission or branching and/or scission-reformation due to chemical equilibrium among surfactant molecules, as detailed elsewhere. Notice that smaller surfactant concentrations of the chaotrope counterions are needed compared to those of the kosmotrope counterions, as a consequence of the arguments given above.
Figure 4. Generalized diagram of normalized shear-thickening intensity as function of normalized surfactant concentration for micellar solutions containing CTAT (closed square), CTA3FB (closed inverted triangle), CTA4FB (closed circle), CTASal (closed triangle), and data adapted from Dehmoune et al.\textsuperscript{32,33} C\textsubscript{14}TAB (open triangle), C\textsubscript{16}TAB (open circle), and C\textsubscript{18}TAB (open square).

CONCLUSIONS

Here we report the shear thickening behavior of electrolyte-free micellar solutions of hexadecyltrimethylammonium-type surfactants with different counterions (tosylate, vinylbenzoate, salicylate, and 3- and 4-fluorobenzoate) to examine the effect of the counterion as well as of n-alkyltetradecylammonium bromide with different alkyl chain length to elucidate the influence of the alkyl chain length upon the shear thickening development in the dilute regime. The STT induction time and the magnitude of the viscosity growth as functions of shear rate, depend strongly on surfactant concentration, counterion type and alkyl chain length. Moreover, the critical shear rate for the viscosity growth can be correlated with surfactant concentration.
The induction time decreases strongly with shear rate when the surfactant concentration is fixed, according to a power law. The induction time of the C_nTAB surfactants increases almost linearly with surfactant tail length and diminishes with the average wormlike micellar length. This behavior is expected according to the mean field theory and the kinetics of breaking and recombination of the micellar growth process. According to the intensity of shear thickening, we propose that the hydrophobicity of the counterions can be qualitatively determined by rheological measurements and by the fact that the counterions studied here follow a Hofmeister-like sequence. Furthermore, shear-thickening data for all the systems reported here fall into a single curve in a Master Flow Diagram of normalized shear thickening intensity as function of normalized surfactant concentration.

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Highlights

• Shear thickening of micellar solutions of hexadecyltrimethylammonium-type surfactants and alkyltetradecylammonium bromide surfactants
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**Keywords:** Master dynamic flow diagram; micellar growth; shear-induced structures; shear thickening; Hofmeister-like series.