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Magnetic structure of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ : Origin of the uniform Heisenberg chain behavior and the magnetic anisotropy of the $\mathbf{C u}^{2+}(S=1 / 2)$ ions

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#### Abstract

The magnetic properties and electric polarization of the organic/inorganic hybrid system $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}=\right.$ piperidinium $)$ were examined on the basis of density functional theory calculations. The spin exchanges of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ evaluated by energymapping analysis show that its uniform Heisenberg antiferromagnetic chain behavior is not caused by the $\mathrm{CuBr}_{3}$ chains made up of edge-sharing $\mathrm{CuBr}_{5}$ square pyramids, but by the twoleg spin ladders resulting from interchain interactions. The magnetic anisotropy of the $\mathrm{Cu}^{2+}$ ions in $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ originates largely from the $\mathrm{Br}^{-}$ligands rather than the $\mathrm{Cu}^{2+}$ ions. The electric polarization of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ arises from the absence of inversion symmetry in the crystal structure, and is weakly affected by the magnetic structure.


## 1. Introduction

Recently a metal organic complex $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}=\right.$ piperidinium $)$ were synthesized, and its crystal and magnetic structures were investigated. ${ }^{1}$ The structural building units of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$, which crystallizes in a monoclinic space group $\mathrm{C}_{2} / \mathrm{c}$, are distorted $\mathrm{CuBr}_{5}$ square pyramids conaining $\mathrm{Cu}^{2+}\left(\mathrm{d}^{9}, \mathrm{~S}=1 / 2\right)$ ions with three nonequivalent Br atoms (Fig. 1a). (Precisely speaking, the four basal Br atoms of each $\mathrm{CuBr}_{5}$ are not coplanar but form a butterfly shape with trans $\angle \mathrm{Br}-\mathrm{Cu}-\mathrm{Br}=151.50^{\circ}$ and $177.95^{\circ}$.) The $\mathrm{CuBr}_{5}$ pyramids share their basal edges to form $\mathrm{Cu}_{2} \mathrm{Br}_{8}$ dimers (Fig. 1a), which in turn share their non-basal edges to form $\mathrm{CuBr}_{3}$ chains ( $\mathbf{F i g} . \mathbf{1 b}$ ) running along the c -direction, and these chains are surrounded by the $\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}$ cations (Fig. 2). $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ has no inversion symmetry in crystal structure, so it would be polar regardless of whether its $\mathrm{Cu}^{2+}$ spins undergo a magnetic ordering or not. However, it is of interest to examine how strongly the electric polarization of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ is infuenced by its magnetic structure.

The temperature-dependent magnetic susceptibility measured for powder samples of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ is well described by a Heisenberg uniform antiferromagnetic (AFM) chain model down to 1.8 K , and $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ undergoes a three-dimensional (3D) magnetic ordering below $\mathrm{T}_{\mathrm{N}}=1.68 \mathrm{~K} .{ }^{1}$ The magnetic orbital of each $\mathrm{CuBr}_{5}$ square pyramid is the $\mathrm{x}^{2}-\mathrm{y}^{2}$ orbital lying in the basal plane of the pyramid (Fig. 3a). Thus, within each $\mathrm{CuBr}_{3}$ chain, there are two different nearest-neighbor spin exchanges. In the exchange path $\mathrm{J}_{1}$, the two magnetic orbitals can interact strongly because they are coplanar (Fig. 1b). In the exchange path $\mathrm{J}_{2}$, the two magnetic orbitals cannot interact strongly because they are not coplanar (Fig. 1b). Consequently, the spin exchanges $\mathrm{J}_{1}$ and $\mathrm{J}_{2}$ cannot be identical so that the $\mathrm{CuBr}_{3}$ chains cannot be responsible for the uniform AFM chain behavior observed in experiments. A chosen spin-lattice such as the Heisenberg uniform AFM chain model should be consistent with its the electronic structure, which determines the magnetic energy spectrum. ${ }^{2,3}$

Experimentally, the spin-exchange parameters of a chosen spin-lattice are determined as the fitting parameters that simulate well the experimental magnetic data. However, the correctness of a chosen spin-lattice is not necessarily guaranteed even if it provides a good fitting as found for $(\mathrm{VO})_{2} \mathrm{P}_{2} \mathrm{O}_{7},{ }^{4,5} \mathrm{Na}_{3} \mathrm{Cu}_{2} \mathrm{SbO}_{6}$ and $\mathrm{Na}_{2} \mathrm{Cu}_{2} \mathrm{TeO}_{6},{ }^{6-10} \mathrm{Bi}_{4} \mathrm{Cu}_{3} \mathrm{~V}_{2} \mathrm{O}_{14},{ }^{11-14}$ and $\mathrm{Cu}_{3}\left(\mathrm{CO}_{3}\right)_{2}(\mathrm{OH})_{2},{ }^{15,16}$ to name a few. To find what spin exchange paths of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ are responsible for its uniform antiferromagnetic AFM chain behavior, it is necessary to evaluate the intrachain as well as the interchain spin exchanges (Fig. 1).

Another interesting magnetic property of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ is its magnetic anisotropy. The magnetic susceptibilities measured for single-crystal samples of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ with probe magnetic field applied along the b -, c - and $\mathrm{a}^{*}$-directions ${ }^{1}$ show that the susceptibility is substantially stronger along the $\mathrm{a}^{*}$-direction than along the b - and c -directions. As depicted in Fig. 1c, the basal planes of the $\mathrm{CuBr}_{5}$ square pyramids are approximately parallel to the $\mathrm{bc}^{*}$ plane. Thus, the preferred spin orientation of the $\mathrm{Cu}^{2+}$ ions in $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ is expected to be perpendicular to the basal plane (easy-axis anisotropy), i.e., along the (a-c/2)-direction, although this direction was not probed experimentally. Many magnetic solids containing $\mathrm{Cu}^{2+}$ ions show typically the easy-plane anisotropy as found for $\mathrm{CuCl}_{2} \cdot 2 \mathrm{H}_{2} \mathrm{O},{ }^{17,18} \mathrm{CuCl}_{2},{ }^{19,20}$ $\mathrm{CuBr}_{2}{ }^{21}, \mathrm{LiCuVO}_{4}{ }^{22}$ and $\mathrm{Bi}_{2} \mathrm{CuO}_{4}{ }^{18,23,24}$ For nearly six decades, it had been erroneously believed that spin- $1 / 2$ ions embedded in solids cannot have magnetic anisotropy arising from spin-orbit coupling (SOC), so their magnetic anisotropy is caused either by anisotropic spin exchange or by their magnetic dipole-dipole interactions. ${ }^{25}$ It is true that SOC cannot generate magnetic anisotropy for isolated spin- $1 / 2$ ions. However, it is recently reported that the spin$1 / 2$ ions embedded in solids do possess the SOC-driven magnetic anisotropy because the dstates of such ions are split by the crystal field of their surrounding ligands. ${ }^{18}$ The easy-axis anisotropy, which the $\mathrm{Cu}^{2+}$ ions in $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ appear to exhibit, is found for $\mathrm{Li}_{2} \mathrm{CuO}_{2} .{ }^{26,27}$ Since their magnetic anisotropy is expected to be caused by the SOC-induced
interactions between the crystal-field split d-states, ${ }^{3,18}$ we may speculate that the split d-states of the $\mathrm{Cu}^{2+}$ ions in $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ differ from those of the $\mathrm{Cu}^{2+}$ ions in compounds showing in-plane anisotropy. Furthermore, since the SOC constant is greater for Br than for Cu by a factor of $\sim 2.9{ }^{28}$ we may also speculate that the Br ligands have an important role in the spin orientation of $\mathrm{Cu}^{2+}$ ion.

In the present work we explore the three questions raised above on the basis of density functional theory (DFT) calculations. We evaluate the intrachain and interchain spin exchanges $\left(\mathrm{J}_{1}-\mathrm{J}_{6}\right)$ of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ by performing energy-mapping analysis to find that two-leg-spin ladders with strong AFM rung act effectively as uniform AFM chains. Our DFT calculations show that the easy-axis anisotropy of $\mathrm{Cu}^{2+}$ ions of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ is largely induced by the SOC of $\mathrm{Br}^{-}$ligands rather than that of $\mathrm{Cu}^{2+}$. Finally we show that the electric polarization of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ is not much affected by the change in its magnetic structure.

## 2. Computational details

In our DFT calculations, we employed the frozen-core projector augmented wave method ${ }^{29,30}$ encoded in the Vienna ab initio simulation package (VASP), ${ }^{31}$ and the generalized-gradient approximation of Perdew, Burke and Ernzerhof ${ }^{32}$ for the exchangecorrelation functional with the plane-wave-cut-off energy of 450 eV and a set of 32 k -point for the irreducible Brillouin zone. To examine the effect of the electron correlation in the Cu 3d states, the DFT plus on-site repulsion method (DFT +U ) ${ }^{33}$ was used with the effective $\mathrm{U}_{\text {eff }}$ $=\mathrm{U}-\mathrm{J}$ values of $2,4,6$ and 8 eV . The preferred orientation of the $\mathrm{Cu}^{2+}$ spins in $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ was determined by performing DFT +U calculations including the SOC. ${ }^{34}$

## 3. Spin exchange and spin lattice

Spin exchanges in magnetic solids of spin $-1 / 2 \mathrm{Cu}^{2+}$ ions are strongly governed by the arrangement of the square planes containing their magnetic orbitals. ${ }^{2,3} \mathrm{~J}_{1}$ and $\mathrm{J}_{2}$ are of the Cu -$\mathrm{Br}-\mathrm{Cu}$ exchange type, while $\mathrm{J}_{3}-\mathrm{J}_{6}$ are of the $\mathrm{Cu}-\mathrm{Br} \cdots \mathrm{Br}-\mathrm{Cu}$ exchange type. $\mathrm{J}_{1}, \mathrm{~J}_{2}$, and $\mathrm{J}_{3}$ are intrachain exchanges, and the $\mathrm{J}_{4}, \mathrm{~J}_{5}$, and $\mathrm{J}_{6}$ are interchain exchanges. The geometrical arrangements of the exchange paths $\mathrm{J}_{1}-\mathrm{J}_{6}$ is presented in Fig. 5. The geometrical parameters associated with the paths $\mathrm{J}_{1}-\mathrm{J}_{6}$ are summarized in Table 1. In terms of the projected density of states (PDOS) plots the electronic structure calculated for the ferromagnetic (FM) state of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ is presented in Fig. 6. The PDOS plots of the Cu 3 d and Br 4 p orbitals, shown only for the down-spin (minority-spin) states for simplicity, are obtained by using the local Cartesian coordinated defined in Fig. 6a. The contribution to the unoccupied states come primarily from the $x^{2}-y^{2}$ orbital of $C u$, the $4 p_{x}$ orbitals of $\operatorname{Br}(1), 4 p_{y}$ orbitals of $\operatorname{Br}(3)$, as well as the $4 p_{x} / 4 p_{y}$ orbitals of $\operatorname{Br}(2)$. Each $\operatorname{Br}(2)$ has both $4 p_{x}$ and $4 p_{y}$ orbital contributions, because they make $\sigma^{*}$ bonding combinations to the $x^{2}-y^{2}$ orbitals to the two different Cu atoms (Fig. 6a). This is consistent with the nature of the magnetic orbital expected for the $\mathrm{Cu}^{2+}\left(\mathrm{S}=1 / 2, \mathrm{~d}^{9}\right)$ ion of each $\mathrm{CuBr}_{5}$ square pyramid (Fig. 3a).

To extract the values of $\mathrm{J}_{1}-\mathrm{J}_{6}$ by energy-mapping analysis, we first calculate the six relative energies using the seven ordered spin states (FM, AF1 -AF6) of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$, depicted in Fig. S1, on the basis of DFT + U calculations as summarized in the parentheses of Fig. S1. In terms of the spin Hamiltonian

$$
\begin{equation*}
\hat{\mathrm{H}}=-\sum_{i<j} \mathrm{~J}_{\mathrm{ij}} \hat{\mathrm{~S}}_{\mathrm{i}} \cdot \hat{\mathrm{~S}}_{\mathrm{j}}, \tag{1}
\end{equation*}
$$

where $\mathrm{J}_{\mathrm{ij}}=\mathrm{J}_{1}-\mathrm{J}_{6}$, the total spin exchange energies $\mathrm{E}_{\text {spin }}$ of these states per eight formula units (8FUs) are expressed as

$$
\begin{equation*}
\mathrm{E}_{\text {spin }}=\left(\mathrm{n}_{1} \mathrm{~J}_{1}+\mathrm{n}_{2} \mathrm{~J}_{2}+\mathrm{n}_{3} \mathrm{~J}_{3}+\mathrm{n}_{4} \mathrm{~J}_{4}+\mathrm{n}_{5} \mathrm{~J}_{5}+\mathrm{n}_{6} \mathrm{~J}_{6}\right) \mathrm{N}^{2} / 4 \tag{2}
\end{equation*}
$$

by using the energy expressions obtained for spin dimers with N unpaired spins per spin site (in the present case, $\mathrm{N}=1$ ). ${ }^{3,35}$ The values of $\mathrm{n}_{1}-\mathrm{n}_{7}$ for the seven ordered spin states, FM and AF1 - AF6, are summarized in Table S1. Thus, by mapping the relative energies of the spin ordered states obtained from the $\mathrm{DFT}+\mathrm{U}$ calculations onto the corresponding relative energies from the total spin exchange energies, we obtain the values of $J_{1}-J_{6}$ summarized in

## Table 2.

Among the intrachain spin exchanges, $\mathrm{J}_{1}$ is strongly AFM, $\mathrm{J}_{2}$ is ferromagnetic (FM), and $\mathrm{J}_{3}$ is negligible. Given that $\angle \mathrm{Cu}-\mathrm{Br}-\mathrm{Cu}=95^{\circ}$ and $90^{\circ}$ for the $\mathrm{J}_{1}$ and $\mathrm{J}_{2}$ paths, respectively, it is not surprising that $\mathrm{J}_{1}$ is AFM while $\mathrm{J}_{2}$ is $\mathrm{FM} .{ }^{36}$ Clearly, then, the $\mathrm{CuBr}_{3}$ chains do not form uniform AFM chains as anticipated. Among the interchain exchanges, $\mathrm{J}_{4}$ and $\mathrm{J}_{6}$ are weak, but $\mathrm{J}_{5}$ is strongly AFM although the $\mathrm{Cu} . . . \mathrm{Cu}$ distance is very long compared to the intrachain case. Note that uniform AFM chains should be formed along the b-direction with the $\mathrm{J}_{5}$ exchange. In the $\mathrm{Cu}-\mathrm{Br}$... $\mathrm{Br}-\mathrm{Cu}$ exchange $\mathrm{J}_{5}$, the two magnetic orbitals are arranged as depicted in Fig. 3b. Thus, the overlap between the two magnetic orbitals across the $\mathrm{Br} . . . \mathrm{Br}$ contact via the Br 4 p magnetic orbital tails is strong, thereby leading to a strong AFM exchange. Note that two adjacent uniform chains made up of the interchain exchanges $\mathrm{J}_{5}$ are linked by the intrachain exchanges $\mathrm{J}_{1}$ to form two-leg spin ladders. Such ladders are linked by the FM intrachain exchanges $\mathrm{J}_{2}$ to form 2D layers of the two-leg spin ladders parallel to the bc-plane, and these 2D layers are stacked along the a-direction (Fig. 5) with very weak interlayer exchange $\mathrm{J}_{6}$ between them. $\mathrm{J}_{6}$ is weakly FM for $\mathrm{U}^{\text {eff }}<5 \mathrm{eV}$, but is weakly AFM for $\mathrm{U}^{\text {eff }}>5 \mathrm{eV}$. In any event, the existence of a nonzero $\mathrm{J}_{6}$ allows $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ to undergo a 3D AFM ordering at low temperature as observed experimentally. ${ }^{1}$

For our discussion of the two-leg spin ladders, it is convenient to employ the new notations $\mathrm{J}_{\|}=\mathrm{J}_{5}$ for the leg and $\mathrm{J}_{\perp}=\mathrm{J}_{1}$ for the rung. Table 2 shows that the $\mathrm{J}_{\perp} / \mathrm{J}_{\|}$ratio changes from 4.7 to 0.95 as $U^{\text {eff }}$ varies from 2 to 8 eV . When the rung exchange $\mathrm{J}_{\perp}$ is considerably
greater than the leg exchange $\mathbf{J}_{\|}$, the two-leg spin ladder would behave like a uniform AFM chain, because the low-energy excitation spectrum would be dominated by the excitations associated with the weaker exchange (i.e., $\mathrm{J}_{\|}$), not with the stronger exchange (i.e., $\mathrm{J}_{\perp}$ ).

To verify this point, we simulate the magnetic susceptibility using the Monte Carlo method. ${ }^{37,38}$ In this simulation we employed the values of the spin exchanges obtained from the DFT +U calculations with $\mathrm{U}^{\text {eff }}=6 \mathrm{eV}$. As shown in Fig. 4, the calculated magnetic susceptibility is in good agreement with the experimental one. It is interesting to note that the uniform AFM chain is formed along the interchain direction instead of the intrachain direction.

## 4. Preferred spin orientation

To determine the preferred orientation of the $\mathrm{Cu}^{2+}$ spins in $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$, we carry out DFT+U calculations including the SOC for sevel different spin orientations defined with respect to the local Cartesian coordinate defined in Fig. 1a,6a. There are eight identical $\mathrm{Cu}^{2+}$ ions per unit cell in $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ but we simplify our calculations by replacing all but one $\mathrm{Cu}^{2+}$ ions with nonmagnetic $\mathrm{Mg}^{2+}$ ions. Results of our $\mathrm{DFT}+\mathrm{U}+\mathrm{SOC}$ calculations for this model are summarized in Table 3, which shows that the spin orientation along the local zdirection is lower in energy, though slightly, than that any other direction. That is, the $\mathrm{Cu}^{2+}$ $\left(d^{9}\right)$ ions in $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ have easy-axis anisotropy, as aready anticipated.

We now examine how the above result can be explained from the viewpoint of the crystal-field split $d$-states of the $\mathrm{CuBr}_{5}$ square pyramid. By employing the coordinate ( $\mathrm{x}, \mathrm{y}, \mathrm{z}$ ) for the orbital momentum and the coordinate ( $\mathrm{x}^{\prime}, \mathrm{y}^{\prime}, \mathrm{z}^{\prime}$ ) for the spin momentum, the SOC term $\lambda \hat{\mathbf{S}} \cdot \hat{\mathrm{L}}$ is written as ${ }^{3,39-41}$

$$
\begin{equation*}
\hat{\mathrm{H}}_{\mathrm{SO}}=\lambda \hat{\mathrm{S}} \cdot \hat{\mathrm{~L}} \approx \hat{\mathrm{H}}_{\mathrm{SO}}^{0}=\lambda \hat{\mathrm{S}}_{\mathrm{z}^{\prime}}\left(\hat{\mathrm{L}}_{z} \cos \theta+\frac{1}{2} \hat{\mathrm{~L}}_{+} \mathrm{e}^{-\mathrm{i} \mathrm{\phi}} \sin \theta+\frac{1}{2} \hat{\mathrm{~L}}_{-} \mathrm{e}^{+\mathrm{i} \mathrm{\phi}} \sin \theta\right) \tag{3}
\end{equation*}
$$

where we omitted the terms that allow interactions between different spin states. The preferred spin orientation is given by the orientation of the $z^{\prime}$-axis. If the $z^{\prime}$-axis is along the z-axis (i.e., $\theta=0^{\circ}$ ), the magnetic ion has easy-axis anisotropy. If the $z^{\prime}$-axis lies in the $x y$ plane (i.e., $\theta=90^{\circ}$ ), the magnetic ion has easy-plane anisotropy.

When an occupied up-spin (down-spin) $d$-state $\psi_{o} \uparrow\left(\psi_{o} \downarrow\right)$ of energy $\mathrm{e}_{0}$ interacts with an unoccupied up-spin (down-spin) $d$-state $\psi_{\mathrm{u}} \uparrow\left(\psi_{\mathrm{u}} \downarrow\right)$ of energy $\mathrm{e}_{\mathrm{u}}$ via the matrix element $\left\langle\psi_{o}\right| \hat{\mathrm{H}}_{\mathrm{SO}}^{0}\left|\psi_{\mathrm{u}}\right\rangle$, the associated energy lowering $\Delta \mathrm{E}_{\text {SoC }}$ is given by

$$
\begin{equation*}
\Delta \mathrm{E}_{\mathrm{SOC}}=-\frac{\left.\left|\left\langle\psi_{\mathrm{o}}\right| \hat{\mathrm{H}}_{\mathrm{SO}}^{0}\right| \psi_{\mathrm{u}}\right\rangle\left.\right|^{2}}{\left|\mathrm{e}_{\mathrm{o}}-\mathrm{e}_{\mathrm{u}}\right|} . \tag{4}
\end{equation*}
$$

Provided that the matrix elements $\left\langle\psi_{o}\right| \hat{\mathrm{H}}_{\mathrm{so}}^{0}\left|\psi_{\mathrm{u}}\right\rangle$ are comparable in magnitude, the most important interaction is the one involving the highest occupied (HO) and the lowest unoccupied (LU) states. To predict the preferred spin orientation using Eqs. (3) and (4), it is necessary to know at what spin orientation the term $\left\langle\psi_{\mathrm{o}}\right| \hat{\mathrm{H}}_{\mathrm{so}}^{0}\left|\psi_{\mathrm{u}}\right\rangle$ is nonzero and can be maximized. The preference for the $\| z$ direction (easy-axis anisotropy) requires a nonzero $\left\langle\psi_{o}\right| \hat{\mathrm{L}}_{\mathrm{z}}\left|\psi_{\mathrm{u}}\right\rangle$, while that for the $\| \mathrm{xy}$ plane (easy-plane anisotropy) requires a nonzero $\left\langle\psi_{o}\right| \hat{\mathrm{L}}_{+}\left|\psi_{\mathrm{u}}\right\rangle$ or a nonzero $\left\langle\psi_{\mathrm{o}}\right| \hat{\mathrm{L}}_{-}\left|\psi_{\mathrm{u}}\right\rangle$. In terms of the spherical harmonics $\quad \mathrm{Y}_{2}^{\mathrm{m}} \quad(\mathrm{m}=0, \pm 1$, $\pm 2)$, the angular behaviors of the $d$-orbitals are given by $3 \mathrm{z}^{2}-\mathrm{r}^{2} \propto \mathrm{Y}_{2}^{0}, \mathrm{xz} \propto\left(\mathrm{Y}_{2}^{-1}-\mathrm{Y}_{2}^{1}\right), \mathrm{yz} \propto$ $\left(\mathrm{Y}_{2}^{-1}+\mathrm{Y}_{2}^{1}\right), \mathrm{xy} \propto\left(\mathrm{Y}_{2}^{-2}-\mathrm{Y}_{2}^{2}\right)$, and $\mathrm{x}^{2}-\mathrm{y}^{2} \propto\left(\mathrm{Y}_{2}^{-2}+\mathrm{Y}_{2}^{2}\right)$. Namely, the difference in the magnetic quantum numbers m (i.e., $|\Delta \mathrm{m}|$ ) is 0 between xz and yz and between xy and $\mathrm{x}^{2}-\mathrm{y}^{2}$, $|\Delta \mathrm{m}|=1$ between $3 z^{2}-\mathrm{r}^{2}$ and $\{\mathrm{xz}, \mathrm{yz}\}$ and between $\{\mathrm{xz}, \mathrm{yz}\}$ and $\left\{\mathrm{xy}, \mathrm{x}^{2}-\mathrm{y}^{2}\right\}$, and $|\Delta \mathrm{m}|=2$ between $3 z^{2}-r^{2}$ and $\left\{x y, x^{2}-y^{2}\right\}$. Then, according to the relationship

$$
\begin{align*}
& \left\langle\mathrm{Y}_{2}^{\mathrm{n}}\right| \hat{\mathrm{L}}_{\mathrm{z}}\left|\mathrm{Y}_{2}^{\mathrm{m}}\right\rangle=\delta_{\mathrm{nm}} \\
& \left\langle\mathrm{Y}_{2}^{\mathrm{n}}\right| \hat{\mathrm{L}}_{+}\left|\mathrm{Y}_{2}^{\mathrm{m}}\right\rangle=\delta_{\mathrm{n}(\mathrm{~m}+1)}  \tag{5}\\
& \left\langle\mathrm{Y}_{2}^{\mathrm{n}}\right| \hat{\mathrm{L}}_{-}\left|\mathrm{Y}_{2}^{\mathrm{m}}\right\rangle=\delta_{\mathrm{n}(\mathrm{~m}-1)}
\end{align*}
$$

the interaction between two $d$-states under the SOC induces easy-axis anisotropy if $|\Delta \mathrm{m}|=0$, but easy-plane anisotropy if $|\Delta \mathrm{m}|=1$.

Therefore, the easy-axis anisotropy found for the $\mathrm{Cu}^{2+}$ ions of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ is explained if the SOC-induced interaction of the empty $x^{2}-y^{2} \downarrow$ states with the filled $\mathrm{xy} \downarrow$ states is stronger than that with the filled $\mathrm{xz} / \mathrm{yz} \downarrow$ states. The PDOS plots of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ in $\mathbf{F i g}$. $\mathbf{6 b}$ show that the empty $x^{2}-y^{2} \downarrow$ orbitals are well separated from the filled $x z / y z \downarrow$ orbitals, and equally well separated from the filled xy $\downarrow$ orbitals. Using Eq. 4 and the PDOS plots of Fig. $\mathbf{6 b}$, however, it is difficult to conclude that the preferred spin orientation is the local zdirection (i.e., easy-axis anisotropy). The latter implies that the SOC of Cu is not responsible for the easy-axis anisotropy. Since the SOC constant of Br is about three times greater than that of Cu , one might wonder if the SOC of Br plays a role in determining the prefered spin orientation of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$. Thus we examine the Br 4 p orbitals combined into the $\mathrm{xy} \downarrow$ and $x^{2}-y^{2} \downarrow$ states (Fig. 6c). The $\operatorname{Br} 4$ p orbitals make $\pi^{*}$ antibonding to the Cu xy orbital in the $\mathrm{xy} \downarrow$ state (Fig. 3c), but make $\sigma^{*}$ antibonding to the $\mathrm{Cu} x^{2}-y^{2}$ orbitals in the $\mathrm{x}^{2}-y^{2} \downarrow$ states (Fig. 3a). Thus, at any Br site of the $\mathrm{CuBr}_{5}$ basal plane, the Br 4 p orbital of the $\mathrm{xy} \downarrow$ is orthogonal to that of the $\mathrm{x}^{2}-\mathrm{y}^{2} \downarrow$ state. At a given Br atom, these $\operatorname{Br} 4 \mathrm{p}$ orbitals can be taken to be $4 p_{x}$ and $4 p_{y}$ orbitals without loss of generality. As can be seen from Fig. 6c, the energy gap between the occupied and unoccupied Br 4 p orbitals is much smaller than that between the occupied and unoccupied Cu d-orbitals. Thus, according to Eq. 4, the SOC effect of Br is more important than that of Cu . This conclusion is further reinforced by the facts that the

SOC constant is much greater for Br than for Cu , and that there are more Br than Cu aoms in $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$.

The only nonzero matrix element for the SOC between the $4 p_{x}$ and $4 p_{y}$ orbitals occurs for $\hat{\mathrm{L}}_{z}$, namely, $\langle\mathrm{y}| \hat{\mathrm{L}}_{\mathrm{z}}|\mathrm{x}\rangle=\mathrm{i} .{ }^{40}$ Because this term comes with the factor $\cos \theta$ (Eq. 3), it is maximized when $\theta=0^{\circ}$. Therefore, the Br ligands associated with the SOC between the $x^{2}-y^{2} \downarrow$ and $x y \downarrow$ states predict easy-axis anisotropy for $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$. Obviously, from the SOC of the $\mathrm{x}^{2}-\mathrm{y}^{2} \downarrow$ states with the $\mathrm{xz} \downarrow$ or $\mathrm{yz} \downarrow$, one predicts in-plane anisotropy by considering the SOC of the associated Br 4 p orbitals. This explains why the magnetic anisotropy is weak in $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$.

## 5. Polariztion

Since $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ has the crystal structure with no inversion symmetry, it should have a nonzero electric polarization. We calculate the electric polarization of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ for the magnetic ground state (i.e., the AF4 state) as well as hypothetical FM state by using the Berry phase method ${ }^{41,42}$ encoded in the VASP. For the electric polarization of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$, our DFT+U+SOC calculations give 0.17 and $0.19 \mu \mathrm{C} / \mathrm{m}^{2}$ for FM and AFM states, respectively. Thus, the electric polarization of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ is weakly affected by its magnetic structure.

## 6. Concluding remarks

Our study shows that the uniform Heisenberg antiferromagnetic chain behavior of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ is not caused by the $\mathrm{CuBr}_{3}$ chains, but by the two-leg spin ladders resulting from interchain interactions. The $\mathrm{Cu}^{2+}$ ions in $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ have easy-axis anisotropy, which arises largely from the $\mathrm{Br}^{-}$ligands rather than the $\mathrm{Cu}^{2+}$ ions. $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ has a
nonzero electric polarization, which is weakly affected by its magnetic structure.

## Supporting information

Table S1 as well as Figure S1 are available free of charge via the Internet at http://

## Acknowledgments

This work was supported by Basic Science Research Program through the National Research Foundation of Korea (NRF) funded by the Ministry of Education, Science and Technology (NRF-2013R1A1A2060341, 2013R1A1A2006416) and by the resource of Supercomputing Center/Korea Institute of Science and Technology Information with supercomputing resources including technical support (KSC-2014-C1-52). This research used resources of the National Energy Research Scientific Computing Center, a DOE Office of Science User Facility supported by the Office of Science of the U.S. Department of Energy under Contract No. DE-AC02-05CH1 1231.

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Table 1. Geometrical parameters associated with the exchange paths $\mathrm{J}_{1}-\mathrm{J}_{6}$ in $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$. The lengths and angles are in units of $\AA$ and degrees, respectively.

|  | $\mathrm{Cu}-\mathrm{Cu}$ | $\mathrm{Cu}-\mathrm{Br}$ | Br... Br | $\angle \mathrm{Cu}-\mathrm{Br}-\mathrm{Cu}$ | $\angle \mathrm{Cu}-\mathrm{Br}-\mathrm{Br}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{J}_{1}$ | 3.622 | $\begin{aligned} & 2.462(\times 2) \\ & 2.449(\times 2) \end{aligned}$ |  | 95.0 |  |
| $\mathrm{J}_{2}$ | 3.712 | $\begin{aligned} & \hline 2.423(\times 2) \\ & 2.802(\times 2) \end{aligned}$ |  | 90.2 |  |
| $\mathrm{J}_{3}$ | 6.673 | $\begin{aligned} & 2.423 \\ & 2.462 \end{aligned}$ | 4.009 |  | $\begin{gathered} 100.5 \\ 93.9 \end{gathered}$ |
| $\mathrm{J}_{4}$ | 7.348 | $\begin{aligned} & 2.412(\times 2) \\ & 2.463(\times 2) \end{aligned}$ | $\begin{gathered} 4.220(\times 2) \\ 3.929 \end{gathered}$ |  | $\begin{aligned} & 104.0 \\ & 161.9 \\ & 113.8 \\ & \hline \end{aligned}$ |
| $\mathrm{J}_{5}$ | 8.835 | 2.449(×2) | 4.220 |  | $\begin{aligned} & \hline 154.6 \\ & 161.9 \end{aligned}$ |
| $\mathrm{J}_{6}$ | 9.357 | $\begin{aligned} & 2.412 \\ & 2.423 \end{aligned}$ | 6.560 |  | $\begin{aligned} & 119.5 \\ & 117.6 \end{aligned}$ |

Table 2. Values of the spin exchanges $\mathrm{J}_{1}-\mathrm{J}_{6}\left(\right.$ in $\left.\mathrm{k}_{\mathrm{B}} \mathrm{K}\right)$ of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ obtained from the DFT + U Calculations with effective $U^{\text {eff }}$ (in eV ).

|  | $\mathrm{U}^{\mathrm{eff}}=2$ | $\mathrm{U}^{\mathrm{eff}}=4$ | $\mathrm{U}^{\mathrm{eff}}=6$ | $\mathrm{U}^{\mathrm{eff}}=8$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{~J}_{1}$ | -197.6 | -105.9 | -52.3 | -21.4 |
| $\mathrm{~J}_{2}$ | 12.1 | 14.4 | 15.1 | 14.6 |
| $\mathrm{~J}_{3}$ | -5.7 | -4.1 | -3.1 | -2.5 |
| $\mathrm{~J}_{4}$ | -9.5 | -4.5 | -4.5 | -3.5 |
| $\mathrm{~J}_{5}$ | -41.8 | -33.7 | -27.1 | -22.6 |
| $\mathrm{~J}_{6}$ | 0.05 | 0.02 | -0.04 | -0.25 |

Table 3. Relative energies (in $\mathrm{k}_{\mathrm{B}} \mathrm{K}$ per Cu ) of various orientations of the $\mathrm{Cu}^{2+}$ spin in $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ obtained from the DFT+U+SOC calculations with effective $\mathrm{U}^{\text {eff }}$ (in eV ). The spin orientation is defined using the local Cartesian coordinate (Fig. 1a, 5a).

| Orientation | $\mathrm{U}^{\mathrm{eff}}=2$ | $\mathrm{U}^{\mathrm{eff}}=4$ | $\mathrm{U}^{\mathrm{eff}}=6$ |
| :---: | :---: | :---: | :---: |
| x | 0.0 | 0.0 | 0.0 |
| y | -0.3 | -0.4 | -0.5 |
| z | -1.4 | -1.7 | -2.1 |
| $\mathrm{x}+\mathrm{z}$ | -0.5 | -0.7 | -0.9 |
| $\mathrm{y}+\mathrm{z}$ | -0.6 | -0.8 | -1.0 |

## Figure captions

Figure 1. Structural features of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$, where the Cu and Br atoms are represented by blue and grey spheres, respectively (a) $\mathrm{Cu}_{2} \mathrm{Br}_{8}$ dimer unit made up of two $\mathrm{CuBr}_{5}$ square pyramids by sharing their basal edges, where the numbers 1,2 and 3 refer to $\operatorname{Br}(1)$, $\operatorname{Br}(2)$ and $\operatorname{Br}(3)$, respectively. (b) $\mathrm{CuBr}_{3}$ chain obtained from $\mathrm{Cu}_{2} \mathrm{Br}_{8}$ dimers by sharing their non-basal edges. (c) Arrangements of $\mathrm{Cu}_{2} \mathrm{Br}_{8}$ dimer units in the bc*-plane, where the apical Br atoms are removed for clarity. (d) Arrangement of two $\mathrm{CuBr}_{3}$ chains. The numbers 1-6 in (b) - (d) refer to the spin exchange paths $J_{1}-J_{6}$, respectively.

Figure 2. Two views of how the $\mathrm{CuBr}_{3}$ chains are packed with $\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}^{+}$cations in $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ : Projection views (a) along the c-direction and (b) along the b-direction. The pink polyhedra, black, gray, and blue circles are represent the $\mathrm{CuBr}_{5}$ units, $\mathrm{H}, \mathrm{C}$, and C atoms, respectively.

Figure 3. (a) The $\mathrm{x}^{2}-y^{2}$ state of a $\mathrm{Cu}^{2+}$ ion at a square planar, a square pyramidal or an octahedral site. (b) Arrangement of two $x^{2}-y^{2}$ magnetic orbitals leading to a strong antiferromagnetic interaction. (c) The xy state of $\mathrm{Cu}^{2+}$ ion at a square planar, a square pyramidal or an octahedral site.

Figure 4. Temperature-dependent magnetic susceptibility of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$, $\chi$, calculated by using the Monte Carlo method on the basis of the classical spin Hamiltonian defined in terms of the spin exchange constants obtained from DFT +U calculations $\left(\mathrm{U}^{\text {eff }}=6.0 \mathrm{eV}\right)$. The inset shows the experimental magnetic susceptibility taken from ref. 1.

Figure 5. Arrangements of the spin exchange paths in $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ : (a) A layer made up of the exchange paths $\mathrm{J}_{1}-\mathrm{J}_{5}$. (b) Arrangement of the exchanges $\mathrm{J}_{1}-\mathrm{J}_{6}$ forming a 3D lattice.

Figure 6. PDOS plots obtained for the down-spin d-states in the FM state of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ from the DFT +U calculations with $\mathrm{U}^{\text {eff }}=4 \mathrm{~V}$ : (a) The local Cartesian coordinate used to obtain the PDOS plots. (b) The PDOS plots obtained for the Cu 3 d orbitals. (c) The PDOS plots obtained for the Br 4 p orbitals.
(a)



(b)
(c)


Figure 1.


Figure 2.
(a)

(c)

(b)


Figure 3


Figure 4


Figure 5.


Figure 6

## Table of contents

The magnetic structure and magnetic anisotropy of $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ were examined on the basis of density functional calculations. The uniform antiferromagnetic chain behavior observed for $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ is not caused by the $\mathrm{CuBr}_{3}$ chains, but by the interchain exchanges leading to two-leg spin ladders. The $\mathrm{Cu}^{2+}$ ions in $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{~N}\right) \mathrm{CuBr}_{3}$ have easy-axis anisotropy, and this arises largely from the spin-orbit coupling of the $\mathrm{Br}^{-}$ligands.


