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A novel method for kinetics analysis of pyrolysis of hemicellulose, cellulose, and lignin in TGA and macro-TGA

Hui Zhou, Yanqiu Long, Aihong Meng, Shen Chen, Qinghai Li and Yanguo Zhang*

The pyrolysis of three biomass components (hemicellulose, cellulose, and lignin) was investigated in both thermogravimetric analyzer (TGA) and self-designed macro-TGA. Slow and fast pyrolysis experiments were carried out in macro-TGA. A novel peak analysis-least square method (PA-LSM) was developed to analyze the kinetics. The results showed that a complex pyrolysis reaction could be described by a series of parallel reactions, and each reaction could be described by a Gaussian peak. The kinetic parameters could be calculated via least square method, and the Gaussian peak could be simulated very well. The slow pyrolysis in TGA and macro-TGA is different, because of heat transfer process. The pyrolysis and fast pyrolysis in macro-TGA also had considerable differences.

Introduction

With the crisis of energy shortage and global warming, biomass, such as wood and agricultural waste, is regarded as a promising energy to ease these two issues. The thermochemical conversion of biomass, including incineration, pyrolysis and gasification is a research topic that has obtained increasing concerns. Pyrolysis is regarded as the fundamental process of thermal chemical conversion of biomass. Through pyrolysis, syngas, oil, and char can be generated and further used as transportation fuel or chemical materials.

There are three main components of biomass, i.e. hemicellulose, cellulose, and lignin. Generally, hemicellulose accounts for 16-23 wt%; cellulose accounts for 42-49 wt%; while lignin accounts for 21-39 wt% of biomass.

A fundamental study of pyrolysis kinetics can help us to predict the pyrolysis behavior of biomass materials as well as design efficient pyrolytic reactors for engineering applications. Several models have been developed to study the kinetics of biomass pyrolysis, such as single reaction model, segmented reaction model, and distributed activation energy model (DAEM). Single reaction model is the original and simplest model, which is suitable to describe single-step reactions, but has difficulties to simulate complex multi-step reactions such as the pyrolysis of real biomass. The segmented reaction model is widely used in recent years, which divided a complicated reaction into several steps according to temperature range. However, the kinetic parameters are sensitive to temperature demarcation point, while the temperature demarcation point is usually determined with subjectivity. In addition, it is supposed that only one reaction happens in one temperature range, which is not scientific sometimes. The DAEM is the up-to-date method for modelling the thermal decomposition of biomass. The method assumes that a series of irreversible first order parallel reactions occur simultaneously, which have a range of activation energies. Nevertheless, the activation energies are described as tens of numbers and even a figure, which makes them difficult to utilize and compare.

Thermogravimetric analyzer (TGA) is the most common apparatus to study kinetics of biomass pyrolysis. Many researchers chose derivative thermogravimetric (DTG) curves to determine the kinetic parameters, because DTG curves are more convenient to identify the kinetic process. Meanwhile, DTG curves are more sensitive than TG curves, thus some changes in the TG curves will be magnified in the DTG curves. Under the ideal conditions, the pyrolysis kinetic parameters of a pure chemical reaction should be the same. However, for the research of thermochemical conversion of fuel, the kinetics parameters are apparent, which means it is usually related to the operation conditions. At this time, the main purpose of the kinetic parameters is to predict the reaction rate under specific conditions. In the TGA experiments, the temperature is elevated only after the samples are put in the TGA. Therefore, the heating rate is limited to tens of degrees per minute. The heating rate is known to have significant influence on the kinetic characteristics. Meanwhile, since the heat and mass transfer in TGA is ignored, the gap between TGA and real furnace is conspicuous.
In this paper, the pyrolytic kinetics of biomass components (hemicellulose, cellulose, and lignin) are investigated in the TGA and self-designed lab-scale macro-TGA. For the macro-TGA, slow pyrolysis and fast pyrolysis are both investigated. A novel peak analysis-least square method (PA-LSM) is applied to study the kinetics of biomass pyrolysis. In addition, the pyrolysis characteristics in different conditions are compared.

Materials and methods

Materials

Xylan (commonly representative of hemicellulose, from beech wood) and cellulose (microcrystalline) were obtained from Sigma-Aldrich. Lignin (dealkaline) used in this research was obtained from a dealkalization process of alkaline lignin provided by Tokyo Chemical Industry (TCI). The samples were in granular form with a size of less than 150 µm. Before the experiments, all the samples were dried at 105 °C to obtain the samples on a dry basis. The proximate and ultimate analyses of the samples are shown in Table 1. Cellulose shows the highest amount of volatile content, and no ash is found in cellulose. Lignin shows the highest amount of ash and fixed carbon content, and the sulfur content in lignin is also very high. The high volatile content of cellulose and high sulfur content of lignin have been reported by others.\textsuperscript{19,20}

<table>
<thead>
<tr>
<th>Samples</th>
<th>Proximate Analysis\textsuperscript{d} (%)</th>
<th>Ultimate Analysis\textsuperscript{daf} (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>A</td>
<td>V</td>
</tr>
<tr>
<td>Xylan</td>
<td>2.11</td>
<td>78.57</td>
</tr>
<tr>
<td>Cellulose</td>
<td>0.00</td>
<td>95.21</td>
</tr>
<tr>
<td>Lignin</td>
<td>16.15</td>
<td>54.61</td>
</tr>
</tbody>
</table>

A: ash; V: volatile; FC: fixed carbon; d: dry basis; daf: dry ash free basis.

Thermogravimetric analysis

The TGA experiments were performed by a NETZSCH STA 449F with a flow rate of 100 ml min\textsuperscript{-1} of N\textsubscript{2}. Temperature rose from room temperature to 1000 °C at a heating rate of 10 °C min\textsuperscript{-1}. Repeated experiments showed that TG curves had good reproducibility.

Macro-TGA experiments

The samples investigated in TGA were also tested in a batch reactor (macro-TGA), shown in Fig. 1. The reaction system was composed of a pyrolysis reactor and a mass monitoring system. The pyrolysis reactor included a three-section furnace, a quartz reactor and a basket. During the experiment, approximate 1.5 g sample was placed in the basket, and the mass of the basket was monitored by a balance through the nichrome wire. The data of the balance and the temperature of the furnace could be collected by a computer online. During the experiment, N\textsubscript{2} (1 L min\textsuperscript{-1}) was used as carrier gas.

Two types of experiments were carried out in macro-TGA: slow pyrolysis and fast pyrolysis. In the slow pyrolysis experiments, the basket loaded with the sample was first placed in the cold reactor. Then the furnace was heated from room temperature to 1000 °C at a heating rate of 10 °C min\textsuperscript{-1}, which was consistent with that in TGA. In the fast pyrolysis experiments, the reactor was initially heated to the set point (800 °C). Once the temperature had stabilized, the sample was put into the hot zone of the reactor and rapidly pyrolysed. The reactor was kept at the reaction temperature until the mass of the sample was stabilized.
Before the experiments, blank test was carried out to obtain the background of the signal. For each pyrolysis experiment, the background signal was subtracted to obtain the real pyrolysis results. Repeated experiments showed that macro-TGA had good reproducibility for both slow pyrolysis and fast pyrolysis.

**Kinetics analysis**

**Kinetics analysis of slow pyrolysis**

The pyrolysis of the samples is too complex to be described by one single kinetic differential reaction. In the kinetic model of independent parallel reactions, the pyrolysis is regarded as a sum of several independent reactions, i.e.:

\[
\frac{dm}{dn} = \sum_{i=1}^{N} \frac{dm_i}{dn_i}
\]

(1)

where \(m\) denotes the conversion of sample at time \(\tau\) (%).

To obtain the normalization result, \(\alpha_i\) is used to denote the normalized conversion of Reaction \(i\), i.e.:

\[
\alpha_i = m_i / m_{i,e}
\]

(2)

where \(m_{i,e}\) denotes the final conversion of Reaction \(i\). Therefore, for Reaction \(i\), \(\alpha_{i,e} = 100\%\).

Since there are some peaks in the DTG curves of slow pyrolysis, imagining each reaction has a peak in DTG curve (including shoulder peak), peak analysis were applied to divide the overall reaction into several reactions. The progress of each reaction was regarded as a Gaussian peak, which is very common for peak analysis.

The kinetics of each reaction can be expressed as:

\[
\frac{d\alpha_i}{d\tau} = k_i (1 - \alpha_i)^n
\]

(3)

\[
k_i = A_i \exp(-\frac{E_i}{RT})
\]

(4)

Here, \(k_i\) is the reaction rate content of Reaction \(i\); \(E_i\) is the apparent activation energy (kJ mol\(^{-1}\)); \(A_i\) is the pre-exponential factor (min\(^{-1}\)); \(n_i\) is the reaction order; \(R\) is universal gas constant (kJ (mol K\(^{-1}\)); \(T\) is the absolute temperature (K).

In the slow pyrolysis experiments, the heating rate \(\beta\) was constant:

\[
\beta = \frac{dT}{dn}
\]

(5)

Thus,

\[
\frac{d\alpha_i}{dT} = \frac{A_i}{\beta} \exp(-\frac{E_i}{RT})(1 - \alpha_i)^n
\]

(6)

To calculate \(E_i\), \(A_i\), and \(n_i\), least square method (LSM) was used:

\[
S = \sum_{j=1}^{N}\left(\frac{d\alpha_i}{dT}_j - \frac{d\alpha_i}{dT}_{j,\text{exp}}\right)^2
\]

(7)

where \(N\) denotes the number of data; \((d\alpha/dT)_{\text{exp}}\) denotes experimental results; \((d\alpha/dT)_{\text{cal}}\) denotes calculation results. Average deviation index (ADI) was applied as an index to evaluate the accuracy of the calculation results.

\[
\text{ADI} = \frac{\sqrt{S/\text{den}}}{(d\alpha_i/dT)_{\text{exp}}^{\text{max}}} \times 100\%
\]

(8)

In this equation, \((d\alpha_i/dT)_{\text{exp}}^{\text{max}}\) denotes the maximum among the experimental data.

**Kinetics analysis of fast pyrolysis**

Since the process of fast pyrolysis is finished in a short time, many peaks of the slow pyrolysis will be coincident. The peak analysis can still be applied if necessary. The Avrami-Erofeev Equation is widely used to describe the fast pyrolysis behavior.\(^{25,26}\) For each peak, it can be expressed by

\[
1 - \alpha_i = \exp(-k_i \tau^{n_i})
\]

(9)

where \(k_i\) and \(n_i\) are determined by the experimental data; \(\tau\) is the time; and \(i\) is the number of peak.

Taking the natural logarithm of Eq. (9) results in

\[
\ln(1 - \alpha_i) = -k_i \tau^{n_i}
\]

(10)

Therefore, LSM can be used to determine the optimal \(k_i\) and \(n_i\).

**Results and discussion**

**Slow pyrolysis of xylan, cellulose and lignin in TGA**

**TG and DTG results of slow pyrolysis in TGA.** The TG and DTG results of pyrolysis of three biomass components in TGA are shown in Fig. 2a and b. The pyrolysis of xylan and lignin begins at a low temperature (~200 °C). As reported by Yang et al.,\(^{7}\) the pyrolysis of hemicellulose mainly happened at 220-315 °C. The pyrolysis of cellulose begins at a higher temperature (~300 °C). Lignin has the highest solid residue content (46.2 %), followed by xylan (27.3%) and cellulose (8.6%). As shown in Fig. 2b, the pyrolysis of xylan has two obvious peaks at 244.9 and 296.1 °C, respectively. The pyrolysis of cellulose has the highest peak at 344.2 °C, which means the pyrolysis of cellulose occurs intensively in a short time. Zhang et al. has reported that the pyrolysis of cellulose occurs between 287 and 387 °C.\(^{7}\) However, the pyrolysis of lignin is a slow process, as shown in Fig. 2a. There are two obvious DTG peaks at 337.9 and 767.9 °C in Fig. 2b, respectively. Yang et al. studied the pyrolysis of lignin in TGA and reported that the degradation of lignin occurred in a wide temperature range (100-900 °C).\(^{27}\)
Kinetics of slow pyrolysis in TGA. The kinetics of pyrolysis of xylan, cellulose, and lignin were analyzed by PA-LSM, as shown in Fig. 3. The DTG curves of xylan can be fitted by three peaks, with the $R^2=0.9977$. In addition to the two peaks at 244.9 and 296.1 °C, there is an obtuse peak at 366.1 °C. Cellulose can be fitted well by single peak ($R^2=0.9925$), which also proved that Gaussian peak is suitable for the simulation of pyrolysis peak. Since the pyrolysis of lignin is a slow process, five independent peaks have to be used to fit the DTG curve ($R^2=0.9918$). In addition to the two peaks at 337.9 and 767.9 °C, there are three peaks at 227.7, 478.4, and 649.3 °C, respectively.
Fig. 3. PA-LSM for kinetics calculation of pyrolysis of xylan, cellulose, and lignin in TGA (a-c: peak fit results; d-f: comparison of calculation from kinetic parameters and experimental results).

The kinetic parameters calculated from PA-LSM are shown in Table 2. The percentage is the relatively mass loss of each peak, calculated from the peak area. As is well known, activated energy is an important parameter for a chemical reaction. As shown in Table 2, the activated energies of different reactions are various, from 26 to 1090 kJ mol$^{-1}$. It can also be noted that the value of activated energy is related to the shape of the peak. The sharper the peak is, the larger the activated energy is.

### Table 2. Kinetic parameters of pyrolysis of xylan, cellulose, and lignin in TGA.

<table>
<thead>
<tr>
<th>Sample</th>
<th>Reaction</th>
<th>Percentage (%)</th>
<th>Peak temperature (°C)</th>
<th>$E$ (kJ/mol)</th>
<th>$A$ (min$^{-1}$)</th>
<th>$n$</th>
<th>ADI</th>
</tr>
</thead>
<tbody>
<tr>
<td>Xylan</td>
<td>1</td>
<td>27.9</td>
<td>244.8</td>
<td>146</td>
<td>3.37×10$^{14}$</td>
<td>1.49</td>
<td>1.58</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>36.1</td>
<td>293.5</td>
<td>164</td>
<td>6.58×10$^{14}$</td>
<td>1.49</td>
<td>1.58</td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>40.0</td>
<td>366.1</td>
<td>26</td>
<td>9.19</td>
<td>1.08</td>
<td>0.23</td>
</tr>
<tr>
<td>Cellulose</td>
<td>1</td>
<td>100.0</td>
<td>340.8</td>
<td>279</td>
<td>4.41×10$^{23}$</td>
<td>1.54</td>
<td>1.64</td>
</tr>
<tr>
<td>Lignin</td>
<td>1</td>
<td>13.6</td>
<td>227.7</td>
<td>62</td>
<td>8.61×10$^{5}$</td>
<td>1.35</td>
<td>1.32</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>52.8</td>
<td>344.3</td>
<td>73</td>
<td>3.05×10$^{5}$</td>
<td>1.34</td>
<td>1.29</td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>9.0</td>
<td>478.4</td>
<td>144</td>
<td>3.04×10$^{9}$</td>
<td>1.43</td>
<td>1.48</td>
</tr>
<tr>
<td></td>
<td>4</td>
<td>13.9</td>
<td>649.3</td>
<td>81</td>
<td>3.91×10$^{3}$</td>
<td>1.27</td>
<td>1.13</td>
</tr>
<tr>
<td></td>
<td>5</td>
<td>10.7</td>
<td>767.1</td>
<td>1090</td>
<td>5.85×10$^{54}$</td>
<td>1.60</td>
<td>1.87</td>
</tr>
</tbody>
</table>

The index $n$ is the order of the reaction, which is related to the reaction mechanisms. For different reactions, $n$ varies from 1.08 to 1.60. The ADI is less than 2, which indicates that the DTG curves can be reproduced from kinetics parameters very well. The comparison of calculation results from kinetic parameters and the experimental results shown in Fig. 3d, e, and f also proves this point.

**Slow pyrolysis of xylan, cellulose and lignin in macro-TGA**

**TG and DTG results of slow pyrolysis in macro-TGA.** Slow pyrolysis in TGA and macro-TGA has the same heating rate and atmosphere, but the scale is different. As shown in Fig. 2a and c, the TG curves in macro-TGA are different from that in TGA. The pyrolysis start temperature in macro-TGA is higher than that in TGA. The reason may be that TGA is regarded as the technique with no limitations in heat and mass transfer, while the heat transfer process in lab-scale furnace such as macro-TGA cannot be ignored. The residue content of cellulose pyrolysis in macro-TGA (17.4%) is much higher than that in TGA (8.6%). The reason may be that in macro-TGA, larger mass of sample was used (~1.5 g). During the pyrolysis, there was a larger chance that the raw sample was wrapped by the inert char. Therefore, part of cellulose sample remained unreacted in the end.
The pyrolysis of xylan can be divided into two stages: the first stage is a fast process, while the second one is a slow process. It should be noted that the three peaks in TGA merged into two peaks in macroxTGA. The pyrolysis of cellulose in macroxTGA has only one peak at 385.1 °C, as shown in Fig. 2d. The pyrolysis of lignin has two obvious peaks, as shown in Fig. 2d. The peak temperature of DTG in macroxTGA is higher than the corresponding peak temperature in TGA, because of the heat transfer process in macro-TGA.

Kinetics of slow pyrolysis in macro-TGA. The kinetic parameters of slow pyrolysis in macro-TGA were calculated by PA-LSM. The pyrolysis of xylan can be simulated by two peaks, as shown in Fig. 4a. The pyrolysis of cellulose can be fitted by only one peak, with the related coefficient 0.9942. The pyrolysis of lignin can be fitted by three peaks, as shown in Fig. 4c.

![Fig. 4. PA-LSM for kinetics calculation of slow pyrolysis of xylan, cellulose, and lignin in macroxTGA (a-c: peak fit results; d-f: comparison of calculation from kinetic parameters and experimental results).](image)

The kinetic parameters are shown in Table 3. The ADIs are all less than 2, which are similar to that of TGA. The activated energies vary from 18 to 588 kJ mol\(^{-1}\). The third peak of lignin has the maximum activated energy, while the second one has the minimum activated energy. The index \(n\) is between 0.94 and 1.57. The comparison of calculation from kinetic parameters and experimental results is shown in Fig. 4d-f. The Gaussian peaks can be simulated well from the kinetic parameters shown in Table 3.

<table>
<thead>
<tr>
<th>Sample</th>
<th>Reaction</th>
<th>Percentage (%)</th>
<th>Peak temperature (°C)</th>
<th>(E) (kJ/mol)</th>
<th>(A) (min(^{-1}))</th>
<th>(n)</th>
<th>ADI</th>
</tr>
</thead>
<tbody>
<tr>
<td>Xylan</td>
<td>1</td>
<td>76.1</td>
<td>301.5</td>
<td>350</td>
<td>(8.34\times10^{31})</td>
<td>1.57</td>
<td>1.65</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>23.9</td>
<td>427.3</td>
<td>50</td>
<td>(5.89\times10^{2})</td>
<td>1.22</td>
<td>0.93</td>
</tr>
<tr>
<td>Cellulose</td>
<td>1</td>
<td>100.0</td>
<td>385.1</td>
<td>291</td>
<td>(8.57\times10^{22})</td>
<td>1.53</td>
<td>1.64</td>
</tr>
<tr>
<td>Lignin</td>
<td>1</td>
<td>46.3</td>
<td>373.0</td>
<td>113</td>
<td>(4.16\times10^{8})</td>
<td>1.41</td>
<td>1.46</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>41.5</td>
<td>456.6</td>
<td>18</td>
<td>(8.76\times10^{-1})</td>
<td>0.94</td>
<td>0.78</td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>12.2</td>
<td>807.3</td>
<td>588</td>
<td>(1.42\times10^{28})</td>
<td>1.55</td>
<td>1.78</td>
</tr>
</tbody>
</table>

Fast pyrolysis of xylan, cellulose, and lignin in macro-TGA

TG and DTG results of fast pyrolysis in macro-TGA. The TG and DTG curves of fast pyrolysis in macro-TGA are shown in Fig. 2e and f. The pyrolysis of xylan ended very soon (~ 50 s); the pyrolysis of cellulose ended in 75 s; while the pyrolysis of lignin was quite slow (more than 300 s). The final residue content of fast pyrolysis is lower than that of slow pyrolysis for these three components, especially for cellulose. This result is consistent to the report of Wu et al. that the residue yield
decreases from 25.45 to 21.21 wt.\% with the increase of heating rate from 5 to 40 °C min\(^{-1}\). There may be two reasons. Firstly, the heat transfer delay for slow pyrolysis is much longer for fast pyrolysis, which means, the core of the sample may keep unreacted during the reaction of the outer part. Then the char is formed in the outer part to prevent the reaction of the inner part at a higher temperature. On the other hand, larger amount of soot may be formed during the fast pyrolysis, because of the extreme high heating rate and drastic perturbation of the sample. Therefore, the residue content for fast pyrolysis is lower than that of slow pyrolysis.

To evaluate the mass loss of fast pyrolysis quantitatively, some indexes are introduced,\(^\text{29}\) as shown in Table 4. \(\tau_{\text{end}}\) is the end time of the reaction, when \(\alpha=95\%\); \((d\alpha/d\tau)_{\text{max}}\) is the maximum mass loss rate; \(\tau_{\text{max}}\) is the maximum mass loss time; \(F\) is the pyrolysis factor, which is defined as

\[
F = \frac{(d\alpha/d\tau)_{\text{max}}}{\tau_{\text{end}} \times \tau_{\text{max}}} \tag{11}
\]

**Table 4.** Indexes of fast pyrolysis of xylan, cellulose, and lignin in macro-TGA.

<table>
<thead>
<tr>
<th>Sample</th>
<th>(\tau_{\text{end}}) (s)</th>
<th>((d\alpha/d\tau)_{\text{max}}) (% s(^{-1}))</th>
<th>(\tau_{\text{max}}) (s)</th>
<th>(F) (% s(^{-1}))</th>
</tr>
</thead>
<tbody>
<tr>
<td>Xylan</td>
<td>48.3</td>
<td>2.7</td>
<td>17.9</td>
<td>3.1\times10(^{-3})</td>
</tr>
<tr>
<td>Cellulose</td>
<td>69.5</td>
<td>2.4</td>
<td>39.9</td>
<td>8.6\times10(^{-4})</td>
</tr>
<tr>
<td>Lignin</td>
<td>208.4</td>
<td>1.0</td>
<td>30.7</td>
<td>1.6\times10(^{-4})</td>
</tr>
</tbody>
</table>

The pyrolysis factor \(F\) was determined by the maximum mass loss rate, the maximum mass loss time and the end time, which represented the degree of difficulty of component pyrolysis. A larger \(F\) means easier pyrolysis of a component.

**Fig. 5.** PA-LSM for kinetics calculation of fast pyrolysis of xylan, cellulose, and lignin in macro-TGA.
Conclusions

Three main biomass components are pyrolyzed in TGA and self-designed macro-TGA at both low and high heating rates. A novel peak analysis-least square method is developed to investigate the kinetics of pyrolysis reactions. A complex pyrolysis reaction can be divided into several parallel reactions according to the number of peaks. The DTG curves can be fitted by the superposition of peaks with high related coefficients. Then each peak can be simulated well from the kinetic parameters.

Acknowledgements

The financial support from National Basic Research Program of China (973 Program, No. 2011CB201502) is gratefully acknowledged.

Notes and references

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