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# Novel hollow all-carbon structures ${ }^{\dagger}$ 

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#### Abstract

A new family of cavernous all-carbon structures is proposed. These molecular cage structures, are constructed by edge subdivisions and leapfrog transformations from cubic polyhedra or the: duals. The obtained structures were then optimized at the density functional level. These hollor carbon structures represent a new class of carbon allotropes which could lead to many interesting applications.


## 1 Introduction

Graphene is a hexagonal two-dimensional (2D) lattice connected by trivalent vertices representing $s p^{2}$ carbon atoms. This simple network can be modified by introducing different atoms or more complex molecular units for the vertices, or/and by edge extensions and modifications such as adding extra atoms or replacing them by molecular units with ingoing and outgoing bonds lying on straight lines. ${ }^{1-4}$ Alternatively, one could also work with its dual, i.e., a triangulated planar surface of hexagonal symmetry containing vertices of degree six, and modify its topology accordingly. There are many different combinations and alterations possible to form such 2D molecular networks, which remain mostly unexplored and could have many interesting electronic properties and applications. ${ }^{2,3}$

Graphyne shown in Figure 1 represents such a class of 2D allcarbon allotropes, ${ }^{4-6}$ that is either built from a graphene template or its dual, and some building blocks have already been synthesized by organic chemists. ${ }^{7-13}$ Graphynes are one carbon atom thick and consist of $s p$ and $s p^{2}$ hybridized carbons in contrast to graphene whose 2D structure consists of six-membered rings of $s p^{2}$ hybridized carbons. The $\alpha$-graphyne structure is for-

[^0]mally obtained by inserting $-\mathrm{C} \equiv \mathrm{C}$ - units into every carbon-carbun bond of graphene leading to a 2D carbon structure consisting of large hexagonal rings with frustrated three-coordinated car bons in each corner of the 18 -membered hexagonal carbon rings. This bond assignment reflects well the symmetry of the strur. ture and approximate bond lengths, however, configurations witi only paired electrons are likely to contribute significantly to th electronic structure. The $\beta$-graphyne structure consists of simila hexagonal rings as in $\alpha$-graphyne. However, each of the hexa gonal rings is surrounded by six hexadehydro[12]annulene rings yielding an infinite 2D structure with all carbons formally four valent. The $\gamma$-graphyne structure also shown in Figure 1 consistc of an infinite 2D structure with the six-membered hexagonal carbon (benzoic) rings surrounded by six hexadehydro[12]annulen $: 0$ rings having all carbons four-valent as in $\beta$-graphyne. It is easily seen that this structure can be obtained by replacing certain edges in graphene by acetylene units (in graph theoretical term this is called an edge subdivision), or alternatively by replacing in the dual triangulated network all vertices by benzene unit. and edges between them by $-\mathrm{C} \equiv \mathrm{C}$ - groups. Graphdiynes are derived from the corresponding graphyne structures by replar ing the $-\mathrm{C} \equiv \mathrm{C}$ - groups with $-\mathrm{C} \equiv \mathrm{C}-\mathrm{C} \equiv \mathrm{C}$ - units. Graphdiyne films have been synthesized on copper surfaces. ${ }^{14}$ The graphyne and graphdiyne structures are shown in Figure 1. Of course, there are many other graphyne structures possible, see for example Peng et al. for a recent review. ${ }^{4}$

The graphene structure consisting of an infinite 2D layer of six-membered rings can be wrapped onto a sphere to give cavernous fullerene-like structures, ${ }^{15}$ but with the condition that e.g., 12 six-membered rings are replaced by five-membered ones such that Euler's polyhedral formula is fulfilled. ${ }^{16}$ Carbon nan-

(a)

(c)

(b)

(d)

Fig. 1 The molecular structure of (a) $\alpha$-graphyne, (b) $\beta$-graphyne, (c) $\gamma$-graphyne and (d) $\gamma$-graphdiyne.
otubes are similarly obtained by rolling up graphene sheets onto a cylinder. ${ }^{17}$ Fullerenes, carbon nanotubes, and other carbonbased nanostructures such as graphyne, graphdiyne, graphone, and graphane have been proposed as basic building blocks for a variety of interesting nanotechnological applications. ${ }^{4,18-30}$ As for graphene, hollow graphyne and graphdiyne structures can be obtained by wrapping up graphyne sheets, with modifications of course such that Euler's polyhedral formula is fulfilled. Analogously, graphyne-based and graphdiyne-based carbon nanotubes can be obtained by rolling up the corresponding planar sheets. Fullerene like graphynes (fullerynes) have already been introduced by Baughman et al. in 1993, ${ }^{29}$ and more generally, vertex insertions into cubic polyhedral graphs were already discussed by Fowler and Rogers in $1998 .{ }^{30}$ Here we also note that the insertion of dicarbon units into all bonds of a chemical structure leads to the concept of carbomers (see for example the work of Chauvin and co-workers ${ }^{31-33}$ ).

One of the smallest members of this class of molecules is the recently proposed gaudiene molecule, which is an all-carbon molecule consisting of 72 carbon atoms forming a hollow structure of $O_{\mathrm{h}}$ symmetry (Figure 2). Gaudiene can be constructed from a truncated octahedron with two thirds of the edges replaced by $-\mathrm{C} \equiv \mathrm{C}$ - units. ${ }^{34}$ Quantum chemical calculations showed that $\beta-\mathrm{C}_{72}$ is an aromatic molecule with a rather large optical gap.

Here, a novel class of hollow carbon structures is proposed. We call this class of polyhedral molecules gaudienes, because the initial polyhedron was inspired from the work of the Spanish architect Antoni Gaudí. ${ }^{34}$ Gaudienes are more general than carbomers as insertion of dicarbon units may not take place in every chemical bond.


Fig. 2 The molecular structure of $\beta-\mathrm{C}_{72}$ of $O_{\mathrm{h}}$ symmetry, the smallest $\beta$-gaudiene investigated.

## 2 Graph theoretical considerations

Before we start with the discussion of the different gaudienes we briefly analyze their topology and introduce a classification scheme. For the moment we do not distinguish between single, double or triple bonding in the polyhedral graph. Formally, gaudienes belong to the class of convex polyhedra (although a quantum theoretical treatment might end up with a locally non-convex structure). ${ }^{35}$ The classification of (non-regular) polytopes is currently an open problem. ${ }^{36}$ For the special class of fullerenes a face-spiral classification scheme has been developed by Manolopoulos et al., ${ }^{37,38}$ which can be generalized for cubic polyhedra. ${ }^{35,39}$ Here, we use the fact that simple insertions (deletions) of divalent vertices into edges (edge subdivisions) of a graph $G$ results in a graph $G^{\prime}$ (which is homeomorphic to $G$ ) with a larger vertex set. Note that even though we have a homeomorphism between $G$ and $G^{\prime}, G$ is not a subgraph of $G^{\prime}$ as the vertex set $E$ is not a subset of $E^{\prime}$.

A polyhedral graph $G$ satisfies Euler's polyhedral formula, and by using the handshaking lemma we obtain

$$
\begin{equation*}
N-E+F=\sum_{n=2}\left(1-\frac{n}{2}\right) N_{n}+\sum_{n=3} F_{n}=2 \tag{1}
\end{equation*}
$$

where $N$ is the number of vertices in the graph $G, E$ the number of edges, $F$ the number of faces, $N_{n}$ the number of $n$-valent vertices, and $F_{n}$ the number of $n$-gons. We see that for $n=2$ the number of divalent vertices is exactly cancelled by the number of extra edges introduced into the graph. In all cases considered here the graph $G$ is cubic, i.e., contains only 3 -valent vertices, and Euler's polyhedral formula for the face count becomes ${ }^{35}$

$$
\begin{equation*}
3 F_{3}+2 F_{4}+F_{5}+\sum_{n \geq 7}(6-n) F_{n}=12 \tag{2}
\end{equation*}
$$

Thus, we conclude that one cannot tile a sphere with hexagons only, i.e., one has to introduce extra $n$-gons (for example 12 pentagons for fullerene graphs; this however does not guarantee that a certain polyhedron exists as for example the fullerene $\mathrm{C}_{22}$ does not exist). Introducing extra $n$-gons can be done in many different ways as we shall see when we discuss the gaudienes in detail.

For the characterization of the various gaudienes we have to describe the cubic graph $G$ or, if $G$ is obtained by some other graph transformation $T$ of the original graph $G_{0}$, i.e., $G=T\left(G_{0}\right)$. We list the vertices and faces according to Pederson ${ }^{36}$ and describe the subsequent list of vertex insertions into edges of each $n$-gon separately. For $G$, or $G_{0}$ with no divalent vertices, we use the notation

$$
\begin{equation*}
\operatorname{PG}\left[N_{3}, N_{4}, N_{5}, N_{6}, \ldots ; F_{3}, F_{4}, F_{5}, F_{6}, \ldots\right] \tag{3}
\end{equation*}
$$

where PG is the ideal point group of the polyhedron. ${ }^{35}$ For example, the well known fullerene $I_{h}$ - $\mathrm{C}_{60}$ is characterized by

$$
\begin{equation*}
I_{h}[60 ; 0,0,12,20] \tag{4}
\end{equation*}
$$

This scheme does not uniquely classify the graph, as there are, for example, many non-isomorphic structures for a fullerene with a certain vertex count and symmetry, ${ }^{35}$ but becomes useful for the gaudienes introduced here as we shall see.
$\alpha$-graphyne based polyhedral structures (in their most general form) can be derived from any polyhedral graph by inserting linear $-\mathrm{C} \equiv \mathrm{C}$ - units into every bond (see Figure 1). It is thus identical to the carbomer concept. This insertion is performed irrespective of the assignment of double bonds in the original structure. For cubic graphs this scheme was already introduced by Fowler in Rogers. ${ }^{30}$ We denote the transformed version of a graph $G_{0}$ according to this scheme as $G=\alpha\left(G_{0}\right)$. For example, if we chose as the graph $G_{0}$ of an $\alpha$-gaudiene a fullerene with $N_{0}$ vertices, denoted as $\operatorname{PG}\left[N_{0} ; 0,0,12,\left(N_{0} / 2-10\right)\right]$ and we insert two divalent vertices into all $3 N_{0} / 2$ edges, we get a total vertex count of $N_{G}=4 N_{0}$, where $N_{G}$ is the number of vertices in the $\alpha$-gaudiene. Such an edge subdivision conserves the point group of $G_{0}$.

It follows from Thurston's proof, which considers the number of non-isomorphic triangulations of a sphere with all $N$ vertices of valency six or smaller, that the number of nonisomorphic cubic graphs with faces up to hexagons grows as $\mathscr{O}\left(N^{9}\right) .{ }^{40}$ As every polyhedral graph can be transformed into an $\alpha$-gaudiene, we can estimate the number of derived $\alpha$-gaudienes.
$\beta$-graphyne analogue carbon cages can be generated starting with any polyhedral (i.e., three connected and planar) graph $G_{0}$. First we perform a leapfrog transformation (LF), which is a $(1,1)$ Goldberg-Coxeter transformation. ${ }^{35,41}$ The Goldberg-

Coxeter transformation of a polyhedral graph is a polyhedral graph itself, implying that the initial graph can be subjected to any number of consecutive leapfrog transformations. In the obtained graph all faces with sizes $\neq 6$ and a subset of all hexagons are selected, such that each vertex is adjacent to exactly one selected face. Such a selection is guaranteed to exist and to be unique for every polyhedral graph that is obtained through a leapfrog transformation. The edges of all selected faces (i.e., two thirds of all edges), are then replaced by a linear segment with two vertices. The leapfrog transformation triples the number $N_{0}$ of vertices of a graph and introduces $N_{0}$ extra hexagons, ${ }^{38}$ while the d scribed replacement triples the number of vertices again. There fore, $\beta$-graphyne cages with $N_{G}=(3 \times 3) N_{0}$ vertices are accessibl? from polyhedra with $N_{0}$ vertices. We denote this sequence of on 5 leapfrog transformation and the following edge subdivision of $G_{\rho}$ as $\beta\left(\operatorname{LF}\left(G_{0}\right)\right)$. We denote $k$ consecutive leapfrog transformation of a graph $G_{0}$ as $\operatorname{LF}^{k}\left(G_{0}\right)$.

Equivalently, $\beta$-graphynes can be created from the same original graph $G_{0}$ by first taking its dual $G_{0}^{*}$. Then, each $n$-valen: vertex in the triangulation is replaced by an $n$-gon in which into each edge a $-\mathrm{C} \equiv \mathrm{C}$ - unit has been inserted. For every pair of vertices connected by an edge in the original graph, the resulting tw', expanded polygons are connected by an edge.

In a similar fashion, $\gamma$-graphyne analogue carbon cages $\mathrm{a}_{1}$ generated starting with any polyhedral graph $G_{0}$. Transforma tion and selection of faces are performed in the same fashion a: 3 above. Then, all edges that are not adjacent to any selected fac: (one third of the edge set), i.e., the complement of the previ. ously picked edges, are replaced by two additional vertices. Thic replacement scheme doubles the number of vertices, transforming polyhedral graphs with $N_{0}$ vertices into $N_{G}=(3 \times 2) N_{0}$ verte. cages. Analogously to the previous transformation this is denoted as $\gamma\left(\operatorname{LF}\left(G_{0}\right)\right)$.

Alternatively, we can start with the dual graph $G_{0}^{*}$, and replac. every $n$-valent vertex by an $n$-gon. These $n$-gons are then con- $?$ nected - according to the connectivity of the vertices they orig. inated from - by bonds into which $-\mathrm{C} \equiv \mathrm{C}$ - units have been in serted.
$\alpha$-, $\beta$-, and $\gamma$-graphdiyne like cages are generated in the samn way as the respective graphynes but by replacing edges by lin ear four-vertex segments instead of two-vertex segments. $N_{0}$ vertex polyhedral graphs are then transformed into $N_{G}=7 N_{0}$, $N_{G}=(3 \times 5) N_{0}$, and $N_{G}=(3 \times 3) N_{0}$ vertex cages respectively. Transformations of graphs $G_{0}$ to graphdiynes are written with a prepended ' $\mathrm{C}_{4}$ ', e.g., $\mathrm{C}_{4}-\alpha\left(G_{0}\right)$.

## 3 Computational methods

Computationally, all structures were generated with a modified version of the program Fullerene. ${ }^{42}$ Selected small polyhedral graphs were hard coded. These graphs were subjected to leapfrog
transformations as detailed in the previous section. The generation of all the gaudienes considered here are summarized in Table 1.

| $N$ | $T$ | $G_{0}$ | polyhedron $\left(G_{0}\right)$ |
| ---: | :--- | :--- | :--- |
| 80 | $\alpha$ | $I_{\mathrm{h}}[20 ; 0,0,12]$ | dodecahedron |
| 72 | $\beta(\mathrm{LF})$ | $O_{\mathrm{h}}[8 ; 0,6]$ | cube |
| 216 | $\beta\left(\mathrm{LF}^{2}\right)$ | $O_{\mathrm{h}}[8 ; 0,6]$ | cube |
| 648 | $\beta\left(\mathrm{LF}^{3}\right)$ | $O_{\mathrm{h}}[8 ; 0,6]$ | cube |
| 120 | $\mathrm{C}_{4}-\beta(\mathrm{LF})$ | $O_{\mathrm{h}}[8 ; 0,6]$ | cube |
| 360 | $\mathrm{C}_{4}-\beta\left(\mathrm{LF}^{2}\right)$ | $O_{\mathrm{h}}[8 ; 0,6]$ | cube |
| 162 | $\beta(\mathrm{LF})$ | $C_{2 \mathrm{v}}[18 ; 0,2,8,1]$ | $\mathrm{FS}(45556555545)$ |
| 288 | $\beta(\mathrm{LF})$ | $C_{2}[32 ; 0,0,12,6]$ | fullerene $\mathrm{C}_{32}(1)$ |
| 288 | $\beta(\mathrm{LF})$ | $D_{2}[32 ; 0,0,12,6]$ | fullerene $\mathrm{C}_{32}(2)$ |
| 288 | $\beta(\mathrm{LF})$ | $D_{3 \mathrm{~d}}[32 ; 0,0,12,6]$ | fullerene $\mathrm{C}_{32}(3)$ |
| 288 | $\beta(\mathrm{LF})$ | $C_{2}[32 ; 0,0,12,6]$ | fullerene $\mathrm{C}_{32}(4)$ |
| 288 | $\beta(\mathrm{LF})$ | $D_{3 \mathrm{~h}}[32 ; 0,0,12,6]$ | fullerene $\mathrm{C}_{32}(5)$ |
| 288 | $\beta(\mathrm{LF})$ | $D_{3}[32 ; 0,0,12,6]$ | fullerene $\mathrm{C}_{32}(6)$ |
| 72 | $\gamma(\mathrm{LF})$ | $D_{6 \mathrm{~h}}[12 ; 0,6,0,2]$ | hexagonal prism |
| 648 | $\left.\gamma(\mathrm{LF})^{3}\right)$ | $D_{6 \mathrm{~h}}[12 ; 0,6,0,2]$ | hexagonal prism |
| 108 | $\mathrm{C}-\gamma(\mathrm{LF})$ | $D_{6 \mathrm{~h}}[12 ; 0,6,0,2]$ | hexagonal prism |
| 432 | $\gamma\left(\mathrm{LF} \mathrm{F}^{2}\right)$ | $D_{6 \mathrm{~d}}[24 ; 0,0,12,2]$ | fullerene $\mathrm{C}_{24}(1)$ |
| 288 | $\gamma(\mathrm{LF})$ | $D_{2 \mathrm{~h}}[48 ; 0,0,12,14]$ | fullerene $\mathrm{C}_{48}(15)$ |
| 288 | $\gamma(\mathrm{LF})$ | $C_{2 \mathrm{v}}[48 ; 0,0,12,14]$ | fullerene $\mathrm{C}_{48}(17)$ |
| 288 | $\gamma(\mathrm{LF})$ | $D_{2 \mathrm{~h}}[48 ; 0,0,12,14]$ | fullerene $\mathrm{C}_{48}(41)$ |
| 288 | $\gamma(\mathrm{LF})$ | $C_{2 \mathrm{v}}[48 ; 0,0,12,14]$ | fullerene $\mathrm{C}_{48}(56)$ |
| 288 | $\gamma(\mathrm{LF})$ | $C_{2 \mathrm{~h}}[48 ; 0,0,12,14]$ | fullerene $\mathrm{C}_{48}(80)$ |
| 288 | $\gamma(\mathrm{LF})$ | $C_{2 \mathrm{~h}}[48 ; 0,0,12,14]$ | fullerene $\mathrm{C}_{48}(138)$ |
| 288 | $\gamma(\mathrm{LF})$ | $D_{6 \mathrm{~d}}[48 ; 0,0,12,14]$ | fullerene $\mathrm{C}_{48}(186)$ |
| 288 | $\gamma(\mathrm{LF})$ | $D_{6 \mathrm{~d}}[48 ; 0,0,12,14]$ | fullerene $\mathrm{C}_{48}(189)$ |

Table 1 Investigated gaudienes with $N$ vertices resulting from a transformation $T$ of an origin graph $G_{0}$, i.e. $T\left(G_{0}\right)$. A description of the polyhedral graph $G_{0}$ is provided as well. For one of the non-regular and less common polyhedron used we give the face spiral (FS) indices $n$ of the $n$-gons for identification. For the fullerenes (Goldberg polyhedra) we provide the canonical index derived from the list of ring-spiral pentagon indices. ${ }^{35,37,38}$

As the force field in program Fullerene can only operate on cubic graphs and triangulations, polyhedra were generated at this stage and optimized to bond lengths that correspond to the polyhedron after replacing a subset of bonds by elongated linear segments. After the optimization of the Cartesian coordinates, atoms were inserted and placed in 3D by linear interpolation.

The molecular structures were then further optimized at the density functional theory (DFT) level using the Becke-Perdew generalized gradient approximation (GGA) functional (BP86) in combination with the Karlsruhe split-valence polarization (SVP) basis sets. ${ }^{43-46}$ Since calculations at the BP86 level slightly underestimate the gap between the highest occupied molecular orbital (HOMO) and the lowest unoccupied molecular orbital (LUMO), single-point calculations were performed at the DFT level using Becke's three-parameter functional (B3LYP) together with a

SVP basis set. ${ }^{46-48}$ The semi-empirical dispersion correction of Grimme has been employed in the molecular structure optimization. ${ }^{49,50}$ The DFT calculations were performed with Turbomole version 6.5. ${ }^{51-53}$ The Cartesian coordinates of the atomic positions of all studied structures are given as Supporting Information. Improving the basis set to a triple-zeta split-valence polarization set for $\beta-\mathrm{C}_{72}$ leads only to a small change in geometry (change in bond distances $\left|\Delta r_{e}\right|<0.012 \AA$ and bond angles $\left|\Delta \alpha_{e}\right|$ $<0.04$ degrees). These errors are within the accuracy of DFT and therefore does not warrant more computer extensive calculations for the discussion of the structures presented here.

## 4 Molecular structures

## $4.1 \quad \alpha$-Gaudienes

The optimized structure of the smallest fullerene-like carbomer based on $\alpha$-graphyne, the gaudiene $\alpha-\mathrm{C}_{80}$, is shown in Figure 3. The structure belongs to the icosahedral ( $I_{\mathrm{h}}$ ) point group as does its origin, the dodecahedron represented by the smallest fullerene $I_{h}-\mathrm{C}_{20}$. Hence, this gaudiene consists of 12 pentagonal 15 -membered carbon rings forming a cage. The atoms shared by three rings are formally $s p^{3}$ hybridized carbons with only three neighbor carbons leading to a relatively small HOMO-LUMO gap of 0.740 eV at the BP86 level, which can be compared with the HOMO-LUMO gaps of $1.66 \mathrm{eV}, 1.45 \mathrm{eV}$ and 1.23 eV for the $\mathrm{C}_{60}$, $\mathrm{C}_{180}$ and $\mathrm{C}_{240}$ fullerenes calculated at the GGA level. ${ }^{54}$ For comparison, DFT calculations using the BP86 functional yield HOMOLUMO gaps of 1.24 eV and 0.21 eV for $\beta-\mathrm{C}_{72}$ and $\gamma-\mathrm{C}_{72}$, respectively. At the B3LYP level the HOMO-LUMO gap for $\alpha-\mathrm{C}_{80}$ is 1.22 eV . The adjacency spectrum of fullerene-like carbomers and their open/closed shell character have been analyzed in detail by Fowler and Rogers. ${ }^{30}$


Fig. 3 The molecular structure of $\alpha-\mathrm{C}_{80}$ of $I_{h}$ symmetry, which is the smallest $\alpha$-gaudiene investigated.

A very stable molecule with a HOMO-LUMO gap of 5.17 eV is obtained when adding 20 hydrogens to the corners of the $\alpha$ $\mathrm{C}_{80}$ icosahedron. Larger $\alpha$-gaudienes can easily be constructed
by using fullerenes as templates and replacing each carboncarbon bond with a $-\mathrm{C} \equiv \mathrm{C}-$ moiety. All $\alpha$-gaudienes have threecoordinated carbons in the intersections between three carbon rings. More stable molecules can be obtained by adding substituents to these three-coordinated carbons.
We should mention that Eq. (2) also allows to use other cubic polyhedra. For example, if we chose the truncated octahedron belonging to the Archimedean solids, $O_{h}[24 ; 0,8,0,6]$, containing six squares according to Eq. (2), we can expand this graph for all edges in a similar way and we arrive at $O_{h}-\mathrm{C}_{96}$, another type of $\alpha$-gaudiene. Hence the playing field is huge for the construction of new 3D polyhedral molecular structures.

## $4.2 \quad \beta$-Gaudienes

The smallest member of the $\beta$-gaudiene class of molecules with four- and six-membered rings involved is the previously proposed $\beta-\mathrm{C}_{72}$ shown in Figure $2 .{ }^{34}$ It belongs to the $O_{\mathrm{h}}$ point group and can be generated from the simple cube $G_{0}=O_{h}[8 ; 0,6]$ or its dual, the octahedron $G_{0}^{*}=O_{h}[0,6 ; 8]$. When folding $\beta$ graphyne to the hollow $\mathrm{C}_{72}$ structure, the edges of eight hexadehydro[12]annulene rings of $\beta$-graphyne form six four-sided rings having four carbons on each side with alternating triple and single bonds. Even though hexadehydro[12]annulene is formally antiaromatic, ${ }^{55-57} \beta-\mathrm{C}_{72}$ is aromatic according to the ring-current criterion sustaining a ring current strength of $44.3 \mathrm{nA} / \mathrm{T}$ around the molecule, which can be compared to the ring-current strength for benzene of $11.8 \mathrm{nA} / \mathrm{T} .{ }^{34,58}$ Since all carbons have formally four bonds, $\beta-\mathrm{C}_{72}$ is a stable molecule with a HOMO-LUMO gap of 1.82 eV at the B3LYP/SVP level.
A number of $\beta$-gaudiene structures were constructed using small polyhedral graphs as starting points. The smallest one constructed using that procedure was $\beta-\mathrm{C}_{162}\left(C_{2 \mathrm{v}}\right)$, which was obtained using an 18 -vertex graph as initial structure, $C_{2 \mathrm{v}}[18 ; 0,2,8,1]$, belonging to a non-regular polyhedron (see Figure 4). This polyhedron does not belong to the common solids and we therefore give the face spiral in Table 1. The optimized molecular structure of $\beta-\mathrm{C}_{162}\left(C_{2 \mathrm{v}}\right)$ is shown in Figure 5a. It has a rather small HOMO-LUMO gap of 0.48 eV as obtained at the B3LYP level.


Fig. 4 Graph of the non-regular $C_{2 v}[18 ; 0,2,8,1]$ polyhedron.

Since the topological method ensures that the symmetry of the


Fig. 5 The molecular structure of the energetically lowest isomers of $\beta$-gaudienes: (a) $\beta$ - $\mathrm{C}_{162}\left(C_{2 \mathrm{v}}\right)$, (b) $\beta-\mathrm{C}_{216}\left(O_{\mathrm{h}}\right)$, (c) $\beta-\mathrm{C}_{288}\left(D_{3 \mathrm{~d}}\right)$, and (d) $\beta-\mathrm{C}_{648}\left(O_{\mathrm{h}}\right)$.
seed structure is conserved, many different isomers can be constructed when the corresponding fullerene structures are avail able. The next larger $\beta$-gaudiene structures of $O_{\mathrm{h}}$ symmetry are $\beta-\mathrm{C}_{216}$ and $\beta-\mathrm{C}_{648}$, which have HOMO-LUMO gaps of 0.415 eV and 0.225 eV at the B3LYP level, respectively. These are also shown in Figure 5.

A large number of $\beta$-gaudienes consisting of 288 carbons cal. be constructed by using different fullerene isomers such as thos,' of $\mathrm{C}_{32}$ as starting structures. The energetically lowest $\beta-\mathrm{C}_{28}:$ structure of all investigated isomers (see Table 1) belongs to tin $D_{3 \mathrm{~d}}$ point group. The energetically lowest $\beta$-gaudiene structures obtained in this work are shown in Figure 5. The rest of the studied $\beta-\mathrm{C}_{288}$ structures are shown in the Supporting Information. The energetically lowest $\beta-\mathrm{C}_{288}$ isomers are $48.8 \mathrm{~kJ} / \mathrm{mol}$ $\left(D_{3}\right), 51.9 \mathrm{~kJ} / \mathrm{mol}\left(D_{2}\right), 53.2 \mathrm{~kJ} / \mathrm{mol}\left(C_{2}\right), 65.6 \mathrm{~kJ} / \mathrm{mol}\left(C_{2}\right)$, and $146.6 \mathrm{~kJ} / \mathrm{mol}\left(D_{3 \mathrm{~h}}\right)$ above the $D_{3 \mathrm{~d}}$ structure. The $\beta-\mathrm{C}_{288}\left(O_{\mathrm{h}}\right)$ isomer consisting of a $\beta-\mathrm{C}_{72}$ molecule inside $\beta-\mathrm{C}_{216}\left(\beta-\mathrm{C}_{72} @ \beta-\mathrm{C}_{216}\right)$ is $683 \mathrm{~kJ} / \mathrm{mol}$ above the lowest $\beta-\mathrm{C}_{288}$ isomer of $D_{3 \mathrm{~d}}$ symmetry. The HOMO-LUMO gaps of the $\beta-\mathrm{C}_{288}$ structures are in the range of $0.27-0.42 \mathrm{eV}$, with the largest gap for the most stable isomer. The two $\beta-\mathrm{C}_{288}$ structures of $\mathrm{C}_{2}$ symmetry have negative HOMO-

LUMO gaps at the BP86 level
The largest molecule considered in this study was an onion-like $\beta-\mathrm{C}_{72} @ \beta-\mathrm{C}_{216} @ \beta-\mathrm{C}_{648}$ cluster of $O_{\mathrm{h}}$ symmetry. The structure is shown in the Supporting Information.

## $4.3 \quad \gamma$-Gaudienes

The smallest $\gamma$-gaudiene $\left(\gamma-\mathrm{C}_{72}\right)$ studied belongs to the $D_{6 \mathrm{~h}}$ point group and has a HOMO-LUMO gap of 0.519 eV . The optimized molecular structure is shown in Figure 6. The benzoic six-membered carbon ring is surrounded by six hexadehydro[12]annulene rings that are fused at the molecular edge. The correct topology of the closed surface is ensured by the six fourmembered carbon rings between the hexadehydro[12]annulenes at the edge of the molecule. The next larger $\gamma$-gaudiene structure of $O_{\mathrm{h}}$ symmetry is $\gamma$-C $\mathrm{C}_{432}\left(O_{\mathrm{h}}\right)$ with a HOMO-LUMO gap of 0.491 eV . The largest $\gamma$-gaudiene studied in this work is $\gamma$ $\mathrm{C}_{648}$, which has $D_{6 \mathrm{~h}}$ symmetry and a small HOMO-LUMO gap of 0.253 eV at the B3LYP level.


Fig. 6 The molecular structure of $\gamma-\mathrm{C}_{72}$ of $D_{6 \mathrm{~h}}$ symmetry, which is the smallest $\gamma$-gaudiene investigated.

A large number of $\gamma-\mathrm{C}_{288}$ structures were constructed with different fullerene isomers of $\mathrm{C}_{48}$ as the origin graph. The energetically lowest $\gamma-\mathrm{C}_{288}$ belongs to the $C_{2 \mathrm{v}}$ point group. The structure of the energetically lowest $\gamma-\mathrm{C}_{288}\left(C_{2 \mathrm{v}}\right)$ isomer is shown in Figure 7. The structures and atomic coordinates of the remaining studied $\gamma-\mathrm{C}_{288}$ clusters are shown in the Supporting Information. The energetically lowest $\gamma-\mathrm{C}_{288}$ isomers are $44.3 \mathrm{~kJ} / \mathrm{mol}$ $\left(D_{2 \mathrm{~h}}\right), 47.8 \mathrm{~kJ} / \mathrm{mol}\left(C_{2 \mathrm{~h}}\right), 160.0 \mathrm{~kJ} / \mathrm{mol}\left(D_{6 \mathrm{~d}}\right), 167.5 \mathrm{~kJ} / \mathrm{mol}$ $\left(C_{2 \mathrm{v}}\right), 287.2 \mathrm{~kJ} / \mathrm{mol}\left(C_{2 \mathrm{v}}\right), 565.5 \mathrm{~kJ} / \mathrm{mol}\left(D_{2 \mathrm{~h}}\right)$, and $873.1 \mathrm{~kJ} / \mathrm{mol}$ ( $D_{6 \mathrm{~d}}$ ) above the lowest $C_{2 \mathrm{v}}$ structure. The calculations show that there are only three low-lying $\gamma$ - $\mathrm{C}_{288}$ isomers among the studied ones.

The HOMO-LUMO gaps of the lowest $\gamma-\mathrm{C}_{288}$ structure is 0.36 eV at the B3LYP level, whereas the HOMO-LUMO gap of the $\gamma-\mathrm{C}_{288}$ are in the range of $0.18-0.47 \mathrm{eV}$, with the largest gap for $\gamma-\mathrm{C}_{288}$


Fig. 7 The molecular structure of the energetically lowest isomers of (a) $\gamma$ - $\mathrm{C}_{288}\left(C_{2 \mathrm{v}}\right)$, (b) $\gamma$ - $\mathrm{C}_{432}\left(O_{\mathrm{h}}\right)$, and (c) $\gamma$ - $\mathrm{C}_{648}\left(D_{6 \mathrm{~h}}\right)$ gaudienes.
$\left(D_{2 \mathrm{~h}}\right)$. The energetically lower isomer of $D_{6 \mathrm{~d}}$ symmetry has a negative HOMO-LUMO gap at the BP86 level. The molecular structure of the energetically lowest $\gamma$-gaudienes obtained in this work are shown in Figure 7.

### 4.4 Graphdiyne-based gaudienes

Graphdiyne-based gaudienes are obtained by replacing the $-\mathrm{C} \equiv \mathrm{C}$ - units of gaudienes with the twice longer $-\mathrm{C} \equiv \mathrm{C}-\mathrm{C} \equiv \mathrm{C}-\left(\mathrm{C}_{4}\right)$ group.

Even though the obtained molecules have a larger number of triple bonds, the HOMO-LUMO gap is wider than for the corresponding graphyne-based molecules. The HOMO-LUMO gaps calculated at the B3LYP level are $0.877 \mathrm{eV}, 1.356 \mathrm{eV}$, and 1.168 eV for $\mathrm{C}_{4}-\gamma-\mathrm{C}_{108}, \mathrm{C}_{4}-\beta-\mathrm{C}_{120}$, and $\mathrm{C}_{4}-\beta-\mathrm{C}_{360}$, respectively. The larger stabilization of the graphdiyne-based gaudienes can be traced back to the molecular properties of dodecadehydro[18]annulene, which is an aromatic molecule. ${ }^{56}$ The HOMO-LUMO gap of $\mathrm{C}_{4}-\gamma$ $\mathrm{C}_{108}$ is smaller than for the two other studied $\mathrm{C}_{4}$-gaudienes due to the significantly larger bond strain of the small four-membered carbon rings at the edge of the molecule. For the $\mathrm{C}_{4}-\beta$-gaudienes, the correct topology is obtained by the six 20 -membered carbon rings. The molecular structures of the studied $\mathrm{C}_{4}$-gaudienes are shown in Figure 8. The Cartesian coordinates of the atomic posi-
tions are given as Supporting Information.


Fig. 8 The molecular structure of the investigated graphdiyne-based ( $\mathrm{C}_{4}$ ) gaudienes: (a) $\mathrm{C}_{4}-\gamma-\mathrm{C}_{108}\left(D_{6 \mathrm{~h}}\right)$, (b) $\mathrm{C}_{4}-\beta-\mathrm{C}_{120}\left(O_{\mathrm{h}}\right)$, and (c) $\mathrm{C}_{4}-\beta-\mathrm{C}_{360}\left(O_{\mathrm{h}}\right)$.

## 5 Discussion and Conclusions

The $\gamma$-gaudienes are generally significantly lower in energy than the $\beta$-gaudienes for the same number of carbon atoms. The most important exception is $\beta-\mathrm{C}_{72}$, which is $128.9 \mathrm{~kJ} / \mathrm{mol}$ below $\gamma-\mathrm{C}_{72}$ due to the ring strain of the four-membered carbon rings of $\gamma-\mathrm{C}_{72}$ and maybe also due to the aromatic stabilization of $\beta-\mathrm{C}_{72} .{ }^{34}$ The HOMO-LUMO gap of $\beta-\mathrm{C}_{72}$ of 1.82 eV calculated at the B3LYP level is also much larger than the HOMO-LUMO gap of 0.52 eV for $\gamma-\mathrm{C}_{72}$. For the small $\gamma-\mathrm{C}_{72}$ cage, the bond strain of the fourmembered carbon rings is not compensated by the energetically favorable structure of $\gamma$-graphyne. For the larger gaudienes, the $\gamma$-graphyne structure have significantly lower energies than the corresponding $\beta$-gaudiene structures. The lowest isomer of $\gamma$ $\mathrm{C}_{288}$ is more than $5000 \mathrm{~kJ} / \mathrm{mol}$ (!) below the energy of the lowest $\beta$ - $\mathrm{C}_{288}$ structure. For larger gaudienes, the energy difference between the $\gamma$-gaudiene and $\beta$-gaudiene is even bigger. For the largest studied gaudienes, $\gamma-\mathrm{C}_{648}$ is about $11000 \mathrm{~kJ} / \mathrm{mol}$ below $\beta$ - $\mathrm{C}_{648}$.

The relative energy per carbon atom is given as a function of $1 / N$ in Figure 9, where $N$ is the number of carbon atoms. The relative energy depends roughly linearly on $1 / N$ leading to the
three straight lines in Figure 9 showing that $\gamma$-gaudiene is the most stable structure and that $\mathrm{C}_{4}$-gaudienes are the energetically highest ones. Extrapolation to $1 / N \rightarrow 0$ yields the relative energy of $\beta$-graphyne, $\gamma$-graphyne, and $\beta$-graphdiyne. The calculations show that $\beta$-graphyne is $17 \mathrm{~kJ} / \mathrm{mol} /$ carbon higher in energy than $\gamma$-graphyne and that $\beta$-graphdiyne is only $7 \mathrm{~kJ} / \mathrm{mol} /$ carbon above $\beta$-graphyne.


Fig. 9 The relative energy (in $\mathrm{kJ} / \mathrm{mol}$ ) as a function of $1 / N$ of the studier ${ }_{1}$ molecular classes. $N$ is the number of atoms. The relative energies are fitted to a line. The outlier at $37 \mathrm{~kJ} / \mathrm{mol}$ for $\gamma-\mathrm{C}_{72}$ is not considered in the fit.

The HOMO-LUMO gaps calculated at the B3LYP level are plotted as a function of $1 / N$ in Figure 10 yielding three straight line. for three gaudiene classes. Extrapolation of the HOMO-LUMC gap to the limit of $1 / N \rightarrow 0$ yields estimated HOMO-LUMO $\mathrm{ga}_{1} \checkmark$ of the $\beta$-graphyne, $\gamma$-graphyne and $\beta$-graphdiyne sheets. The three lines suggest that the HOMO-LUMO gaps for the infinit ${ }^{( }$ planar structures are larger than zero. The extrapolated HOMOLUMO gap of $\beta$-graphyne is 0.17 eV . For $\gamma$-graphyne we obtain an extrapolated HOMO-LUMO gap of 0.33 eV . The extrapolatea HOMO-LUMO gap of 1.25 eV for $\beta$-graphdiyne agrees well witl. the previously reported value of 1.22 eV , which was calculated a the DFT level using a hybrid functional ${ }^{59}$ and it is significantl $\Gamma$ larger than the HOMO-LUMO gap of 0.46 eV calculated at th : DFT level using the generalized gradient approximation. ${ }^{60}$ EvLı though the error bars of the present extrapolated values are large due to the few number of points used in the fit, the present calculations suggest that the HOMO-LUMO gap of graphdiyne is larger than 1 eV .

The hollow gaudiene structures might open the avenue to novel materials with interesting properties. For example, triple bonds provide possibilities for functionalizing the molecules with different kinds of substituents that even might couple several gaudiene molecules to polymers or solid-state materials. The gaudiene structures can also be fully or partially saturated with hydrogens without destroying their cage structures. Such molecules are or-


Fig. 10 The HOMO-LUMO gap (ineV) as a function of $1 / N$ of the studied molecular classes. $N$ is the number of atoms. The relative energies are fitted to a line. The outlier at 1.82 eV for $\beta-\mathrm{C}_{72}$ is not considered in the fit.
dinary saturated hydrocarbons with extraordinary hollow structures. By attaching substituents to the corners of $\alpha$-gaudienes, molecules with a very large HOMO-LUMO gap are obtained. The optical gap for the $\mathrm{C}_{4}$-gaudienes is significantly larger than for the two other classes of molecules. Extrapolation to infinitely large clusters suggests that planar graphdiyne has indeed a HOMOLUMO gap that is significantly larger than zero, which might provide novel possibilities for carbon-based mono-layer structures. ${ }^{4}$

Finally, we point out that there are also other graph theoretical procedures for obtaining cavernous all-carbon structures that have not been discussed here. ${ }^{61,62}$ For example, one can insert $-\mathrm{C} \equiv \mathrm{C}$ - units into edges running parallel to the main axis of a fullerene nanotube. One can also use other building blocks beside carbon which fit the required topologies, e.g., building units which are used in metal-organic frameworks. This opens up a whole new area of interesting cage structures and materials which could be useful in many interesting applications.

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## References

1 H. S. S. Ramakrishna Matte, A. Gomathi, A. K. Manna, D. J. Late, R. Datta, S. K. Pati and C. N. R. Rao, Angew. Chem. Int. Ed., 2010, 122, 4153-4156.
2 A. L. Ivanovskii, Russ. Chem. Rev., 2012, 81, 571-605.
3 M. Xu, T. Liang, M. Shi and H. Chen, Chem. Rev., 2013, 113, 3766-3798.
4 Q. Peng, A. K. Dearden, J. Crean, L. Han, S. Liu, X. Wen and S. De, Nanotechnol. Sci. Appl., 2014, 7, 1-29.

5 R. H. Baughman, H. Eckhardt and M. Kertesz, J. Chem. Phys., 1987, 87, 6687-6699.
6 V. Georgakilas, J. A. Perman, J. Tucek and R. Zboril, Chem. Rev., 2015, 115, 4744-4822.
7 F. Diederich, Nature, 1994, 369, 199-207.
8 M. M. Haley, S. C. Brand and J. J. Pak, Angew. Chem. Int. Ed., 1997, 36, 836-838.
9 U. H. F. Bunz, Y. Rubin and Y. Tobe, Chem. Soc. Rev., 1999, 28, 107-119.
10 E. L. Spitler, C. A. Johnson and M. M. Haley, Chem. Rev., 2006, 106, 5344-5386.
11 M. M. Haley, Pure Appl. Chem., 2008, 80, 519-532.
12 F. Diederich and M. Kivala, Adv. Mater., 2010, 22, 803-812.
13 K. Tahara, Y. Yamamoto, D. E. Gross, H. Kozuma, Y. Arikuma, K. Ohta, Y. Koizumi, Y. Gao, Y. Shimizu, S. Seki, K. Kamada, J. S. Moore and Y. Tobe, Chem. Eur. J., 2013, 19, 1125111260.

14 G. Li, Y. Li, H. Liu, Y. Guo, Y. Li and D. Zhu, Chem. Commun., 2010, 46, 3256-3258.
15 K. S. Novoselov, A. K. Geim, S. V. Morozov, D. Jiang, Y. Zhang, S. V. Dubonos, I. V. Grigorieva and A. A. Firsov, Science, 2004, 306, 666-669.
16 H. W. Kroto, J. R. Heath, S. C. O'Brien, R. F. Curl and R. E. Smalley, Nature, 1985, 318, 162-163.
17 S. Iijima, Nature, 1991, 354, 56-58.
18 S. Ihara and S. Itoh, Carbon, 1995, 33, 931-939.
19 M. Meyyappan and D. Srivastava, Handbook of Nanoscience, Engineering, and Technology, CRC Press, Boca Raton Fl, 2003, ch. 18, pp. 1-26.
20 T. C. Dinadayalane and J. Leszczynski, Struct. Chem., 2010, 21, 1155-1169.
21 A. N. Enyashin and A. L. Ivanovskii, Phys. Stat. Sol. B, 2011, 248, 1879-1883.
22 R. Mas-Ballesté, C. Gómez-Navarro, J. Gómez-Herrero and F. Zamora, Nanoscale, 2011, 3, 20-30.

23 D. Malko, C. Neiss, F. Viñes and A. Görling, Phys. Rev. Letters, 2012, 108, 086804.
24 S. Zhang, Y. Zhang, S. Huang and C. Wang, Nanoscale, 2012, 4, 2839-2842.

25 L. Zoppi, J. S. Siegel and K. K. Baldridge, WIREs Comput. Mol. Sci., 2013, 3, 1-12.
26 J.-J. Zheng, X. Zhao, Y. Zhao and X. Gao, Sci. Rep., 2013, 3, 1271.

27 J. Xi, D. Wang and Z. Shuai, WIREs Comput. Mol. Sci., 2015, 5, 215-227.
28 Z. Li, M. Smeu, A. Rives, V. Maraval, R. Chauvin, M. A. Ratner and E. Borguet, Nature Commun., 2015, 6, 6321.
29 R. H. Baughman, D. S. Galvão, C. Cui, Y. Wang and D. Tománek, Chem. Phys. Lett., 1993, 204, 8-14.

30 P. W. Fowler and K. M. Rogers, J. Chem. Soc. Faraday Trans., 1998, 94, 1019-1027.
31 R. Chauvin, Tetrahedron Lett., 1995, 36, 401-404.
32 R. Chauvin, Tetrahedron Lett., 1995, 36, 397-400.
33 V. Maraval and R. Chauvin, New J. Chem., 2007, 31, 18531873.

34 D. Sundholm, Phys. Chem. Chem. Phys., 2013, 15, 9025-9028.
35 P. Schwerdtfeger, L. N. Wirz and J. Avery, WIREs Comput. Mol. Sci., 2015, 5, 96-145.
36 J. J. Pedersen, California Math., 1977, 2, 21-28.
37 D. E. Manolopoulos, J. C. May and S. E. Down, Chem. Phys. Lett., 1991, 181, 105-111.
38 P. W. Fowler and D. E. Manolopoulos, An Atlas of Fullerenes, Dover Publications Inc., Mineola, New York, 2nd edn, 2006.
39 L. N. Wirz, R. Tonner, J. Avery and P. Schwerdtfeger, J. Chem. Inf. Model., 2014, 54, 121-130.
40 W. P. Thurston, Geometry \& Topology Monographs, 1998, 1, 511-549.
41 J. Avery, to be submitted, 2015.
42 P. Schwerdtfeger, L. Wirz and J. Avery, J. Comp. Chem., 2013, 34, 1508-1526.
43 S. H. Vosko, L. Wilk and M. Nusair, Can. J. Phys, 1980, 58, 1200-1211.
44 J. P. Perdew, Phys. Rev. B, 1986, 33, 8822-8824.
45 A. D. Becke, Phys. Rev. A, 1988, 38, 3098-3100.
46 A. Schäfer, H. Horn and R. Ahlrichs, J. Chem. Phys., 1992, 97, 2571-2577.
47 C. Lee, W. Yang and R. G. Parr, Phys. Rev. B, 1988, 37, 785789.

48 A. D. Becke, J. Chem. Phys., 1993, 98, 5648-5652.
49 S. Grimme, J. Comput. Chem., 2006, 27, 1787-1799.
50 S. Grimme, J. Antony, S. Ehrlich and H. Krieg, J. Chem. Phys., 2010, 132, 154104:1-19.
51 R. Ahlrichs, M. Bär, M. Häser, H. Horn and C. Kölmel, Chem. Phys. Lett., 1989, 162, 165-169.
52 TURBOMOLE V6.5 2013, a development of University of Karlsruhe and Forschungszentrum Karlsruhe GmbH, 19892007, TURBOMOLE GmbH, since 2007; available from
http://www.turbomole.com.
53 F. Furche, R. Ahlrichs, C. Hättig, W. Klopper, M. Sierka and F. Weigend, WIREs Comput. Mol. Sci., 2014, 4, 91-100.

54 G. Casella, A. Bagno and G. Saielli, Phys. Chem. Chem. Phys., 2013, 15, 18030-18038.
55 J. A. Pople and K. G. Untch, J. Am. Chem. Soc., 1966, 88, 4811-4815.
56 J. Jusélius and D. Sundholm, Phys. Chem. Chem. Phys., 2001, 3, 2433-2437.
57 J. Jusélius and D. Sundholm, Phys. Chem. Chem. Phys., 2008, 10, 6630-6634.
58 H. Fliegl, D. Sundholm, S. Taubert, J. Jusélius and W. Klopper J. Phys. Chem. A, 2009, 113, 8668-8676.

59 Y. Jiao, A. Du, M. Hankel, Z. Zhu, V. Rudolph and S. C. Smith, Chem. Commun., 2011, 47, 11843-11845.
60 M. Long, L. Tang, D. Wang, Y. Li and Z. Shuai, ACS Nanc 2011, 5, 2593-2600.
61 D. Sebastiani and M. A. Parker, Symmetry, 2009, 1, 226-239
62 A. Ivanovskii, Prog. Solid State Chem., 2013, 41, 1-19.

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    $\dagger$ Electronic Supplementary Information (ESI) available: Cartesian coordinates of the studied molecules.

