

Dalton Transactions

Accepted Manuscript



This is an *Accepted Manuscript*, which has been through the Royal Society of Chemistry peer review process and has been accepted for publication.

Accepted Manuscripts are published online shortly after acceptance, before technical editing, formatting and proof reading. Using this free service, authors can make their results available to the community, in citable form, before we publish the edited article. We will replace this *Accepted Manuscript* with the edited and formatted *Advance Article* as soon as it is available.

You can find more information about *Accepted Manuscripts* in the [Information for Authors](#).

Please note that technical editing may introduce minor changes to the text and/or graphics, which may alter content. The journal's standard [Terms & Conditions](#) and the [Ethical guidelines](#) still apply. In no event shall the Royal Society of Chemistry be held responsible for any errors or omissions in this *Accepted Manuscript* or any consequences arising from the use of any information it contains.

**Bond ionicity, lattice energy, bond energy and microwave dielectric properties of $\text{ZnZr}(\text{Nb}_{1-x}\text{A}_x)_2\text{O}_8$
(A=Ta, Sb) ceramics**

Ping Zhang^{a*}, Yonggui Zhao^a, Haitao, Wu^b

^a*School of Electronic and Information Engineering and Key Laboratory of Advanced Ceramics and Machining Technology of Ministry of Education, Tianjin University, Tianjin 300072, P. R. China*

^b*Shandong Provincial Key Laboratory of Preparation and Measurement of Building Materials, University of Jinan, Jinan 250022, China*

Abstract

Dependence of microwaves dielectric properties on the structural characteristics of $\text{ZnZr}(\text{Nb}_{1-x}\text{A}_x)_2\text{O}_8$ (A=Ta, Sb) ($0 \leq x \leq 0.10$) ceramics is investigated. All the compounds are prepared by a conventional solid-state reaction method and analyzed via multiphase structure refinement. The diffraction patterns of $\text{ZnZr}(\text{Nb}_{1-x}\text{A}_x)_2\text{O}_8$ (A=Ta, Sb) shows that the monoclinic wolframite structure of $\text{ZrZrNb}_2\text{O}_8$ which consists of an oxygen octahedral, and with the Nb ion in the center of the oxygen octahedral. For the $\text{ZnZr}(\text{Nb}_{1-x}\text{A}_x)_2\text{O}_8$ (A=Ta, Sb) ceramics, the dielectric constant (ϵ_r) decreased due to decrease in Nb-site bond ionicity. Quality factor ($Q \times f$) of $\text{ZnZr}(\text{Nb}_{1-x}\text{Sb}_x)_2\text{O}_8$ ceramics is found be highest (89,400GHz), which is explained in terms of average of Nb-site lattice energy. With the decreasing of bond energy of Nb-site, the temperature coefficient of resonant frequency ($|\tau_f|$) value increased. The substitution of A^{5+} (A=Ta, Sb) for Nb^{5+} effectively influences the microstructure and the microwave dielectric properties of $\text{ZrZrNb}_2\text{O}_8$ ceramics.

Keywords: Crystal structure; Substitution; Bond ionicity; Lattice energy; Bond energy; ceramics

1. Introduction

1

*Corresponding author. Tel. : +86 13702194791

Email address: zptai@163.com (P. Zhang)

The microwave dielectric ceramics plays an important role in the development of global positioning systems, intelligent transport systems and satellite broadcasting [1, 2]. These materials, which used in the microwave band, are very effective for making smaller devices and improving the packaging density of microwave integrated circuits. Requirements for the microwave dielectric ceramics should have high relative permittivity ($\epsilon_r > 10$), high quality factor ($Q \times f > 10,000$ GHz) and near zero temperature coefficient of resonant frequency ($\tau_f = 0$ ppm/ $^{\circ}$ C) for miniaturization, better selectivity and stability, respectively [3-4]. In order to meet the specifications of current and future development, numbers researchers are focusing on exploring new excellent microwave dielectric materials.

Recently, great attention has been paid to new low dielectric loss materials of $\text{ZnZrNb}_2\text{O}_8$ with monoclinic wolframite crystal structure [5-9]. The $\text{ZnZrNb}_2\text{O}_8$ ceramics, which possessed excellent microwave dielectric properties of $\epsilon_r = 30$, $Q \times f = 61,000$ GHz and $\tau_f = -52$ ppm/ $^{\circ}$ C, were first reported by *Liao. et al* [5]. *Ramarao et al* [6]. investigated the crystal structure refinement and microwave dielectric properties of new low dielectric loss AZrNb_2O_8 (A: Mn, Mg, Zn and Co) and reported the dielectric properties of $\text{ZnZrNb}_2\text{O}_8$ ceramics with $\epsilon_r = 16.5$, $Q \times f = 53,400$ GHz and $\tau_f = -49.8$ ppm/ $^{\circ}$ C. Then *Cheng et al* [7]. reported dielectric properties of $\text{MgZrNb}_2\text{O}_8$ ceramics. *Tang et al* [8]. presented the effects of $\text{BaCu}(\text{B}_2\text{O}_5)$ addition on the microwave dielectric properties of $\text{ZnZrNb}_2\text{O}_8$ ceramics. An maximum $Q \times f$ values of 56,720 GHz was obtained from $\text{ZnZrNb}_2\text{O}_8$ ceramics doped with 3 wt.% $\text{BaCu}(\text{B}_2\text{O}_5)$ additions sintered at 950 $^{\circ}$ C for 4 h. Recently, *Li et al* [9]. have studied the difference of ions substitution on the microwave dielectric properties of $(\text{Zn}_{0.95}\text{M}_{0.05})\text{ZrNb}_2\text{O}_8$ (M=Ni, Mg, Co, Mn), with $x=0.05$ Ni^{2+} ions addition, the optimal $Q \times f$ values (83,558 GHz) for $\text{ZnZrNb}_2\text{O}_8$ ceramics can be obtained. However, the variation of microwave dielectric properties with substitution of different pentavalent ions on Nb-site in

ZnZrNb₂O₈ was not discussed. Moreover, the relationship between bond ionicity, lattice energy, bond energy and microwave dielectric properties of ZnZr(Nb_{1-x}A_x)₂O₈ (A=Ta, Sb) was also not investigated.

Therefore, in this paper, the correlations between microstructure and microwave dielectric properties of ZnZr(Nb_{1-x}A_x)₂O₈ (A=Ta, Sb) were systematically discussed. In addition, the bond ionicity, lattice energy and bond energy were calculated based on the complex chemical bond theory. An available method based on the Rietveld refinement of X-ray techniques was also used to analyze the structures of crystalline phases.

2. Experimental procedure

The ceramics were prepared through a conventional solid-state reaction route. High-purity oxide powders ZnO (99.9%), ZrO₂ (99.0%), Nb₂O₅ (99.9%), Ta₂O₅ (99.9%), and Sb₂O₅ (99.9%) were used as the starting materials. The raw materials were mixed according to the formula of ZnZr(Nb_{1-x}A_x)₂O₈ (A=Ta, Sb) ($x=0.0, 0.02, 0.04, 0.06, 0.08, 0.1$). The mixed powders were milled 6 h with distilled water in a nylon container with ZrO₂ balls. All the slurries were dried and pre-sintered at 1100 °C for 4 h. The pre-sintered powders were re-milled 8 h. After drying, crushed and sieved with an 80 mesh screen, the powders were pressed into disk-type pellets with 10 mm diameter and 5 mm thickness at 100 MPa. Then these pellets were sintered at temperatures of 1250°C for 4 h in air with the heating rate of 5°C/min.

The crystalline phases of the sintered samples were identified by X-ray diffraction (XRD, Rigaku D/max 2550 PC, Tokyo, Japan) with Cu K α radiation generated at 40 kV and 40 mA. The microstructure of the ceramic surfaces were performed and analyzed by a scanning electron microscopy (SEM, MERLIN Compact, Germany). The microwave dielectric properties were measured in the frequency range of 6-10 GHz using a HP8720ES network analyzer [10]. The temperature coefficients of resonant frequency (τ_f)

were measured in the temperature range from 25 °C to 85 °C. The τ_f (ppm/°C) value calculated by noting the change in resonant frequency (Δf)

$$\tau_f = \frac{f_2 - f_1}{f_1(T_2 - T_1)} \quad (1)$$

where f_1 is resonant frequency at T_1 and f_2 is the resonant frequency at T_2 .

The apparent densities of the sintered pellets were measured use the Archimedes method (Mettler ToledoXS64). To study the relative density of the sample, the theoretical density was obtained from the crystal structure and atomic weight by the Eq. (2):

$$\rho_{theory} = \frac{ZA}{V_C N_A} \quad (2)$$

where V_C , N_A , Z , and A are volume of unit cell (cm^3), avogadro number (mol^{-1}), number of atoms in unit cell, and atomic weight (g/mol), respectively. The relative density was obtained by the Eq. (3):

$$\rho_{relative} = \frac{\rho_{bulk}}{\rho_{theory}} \times 100\% \quad (3)$$

3. Results and discussion

3.1 Multiphase refinement

The X-ray diffraction patterns of $\text{ZnZr}(\text{Nb}_{1-x}\text{A}_x)_2\text{O}_8$ ($\text{A}=\text{Ta}, \text{Sb}$) ($0 \leq x \leq 0.10$) ceramics sintered at 1250°C for 4 h are given in Fig. 1. All parameters of interest including scale factors for all phases, zero point, background, half-width, asymmetry parameters, unit-cell parameters, atomic positional coordinates, temperature factors are refined step-by-step for avoiding correlations using the Full-Prof. All the reflections are well matched with the PDF file no. 48-0324 according to the JADE 6, and the refinement is found to belong to the monoclinic wolframite structure with the space group P2/c (no. 13). From the x values of A^{5+} ($\text{A}=\text{Ta}, \text{Sb}$) ionic increases, which decreases the lattice parameters. Therefore, the unit cell volume decreases and causes the reflections to shift to higher angles, which can be seen in the illustration

of the Fig.1 (a), (b) and (c). As shown in the Fig. 1(b), with the Sb^{5+} substitution increase to 0.10, we can found that abnormal peaks were appeared at the position of 002 and 130, it indicates that the solid solubility of the Sb^{5+} substitution is 0.08. Fig. 2 shows the profile fits for the Rietveld refinement of $\text{ZnZrNb}_2\text{O}_8$ ceramic. The starting model for this refinement was taken from *Macavei et al.*[11]. According to the Rietveld refinement, the lattice parameters are calculated as $a=4.813 \text{ \AA}$, $b=5.674 \text{ \AA}$, $c=5.067 \text{ \AA}$, $\beta=91.45^\circ$ and $V=138.56 \text{ \AA}^3$, the Rietveld discrepancy factors R_p and R_{wp} are 11.41% and 12.42%. The part of refinement results such as lattice parameters and bond length given in Table.1, Table.2 (a) and (b). From the refinement results, we can observe that with the increasing of the x values, both of the unit cell volumes for Ta^{5+} and Sb^{5+} substitutions are decreasing. The reason why the unit cell volumes for Sb^{5+} substitution have a smaller value, it could be due to that the substitution of Sb^{5+} (ionic radius, abbr. $r=0.60 \text{ \AA}$, coordination numbers, abbr. CN = 6) ion is smaller than the Ta^{5+} (ionic radius, abbr. $r=0.64 \text{ \AA}$, coordination numbers, abbr. CN = 6) ion. Therefore, the substitution of Nb^{5+} ion by Sb^{5+} could have a smaller unit cell volume.

3.2 Crystal structure analysis

The CdWO_4 reported by *Macavei et al.*[11] is adopted as the starting model of Rietveld refinement. Table.3 shows the refined atomic coordinate of $\text{ZnZrNb}_2\text{O}_8$ ceramics. Based on the atomic coordinate information, a schematic representation of a $\text{ZnZrNb}_2\text{O}_8$ supercell ($1\times 1\times 1$) is given in Fig. 3. In the supercell, there contains one $\text{ZnZrNb}_2\text{O}_8$ molecules per primitive cell and consists of an oxygen octahedron, with the Nb ion at the center of the oxygen octahedron, as shown in Fig. 3. Due to the special structure, the variation of the oxygen octahedron has vital effect on the microwave dielectric properties. In this paper, with the increase of substitution ions, the atomic interactions of $\text{ZnZrNb}_2\text{O}_8$ ceramics are

changed, which could result in bond length of the oxygen octahedron. The change of the bond length of oxygen octahedron has close connection with the bond ionicity, lattice energy and bond energy, which are an intrinsic factor that is found to be affecting the microwave dielectric properties.

3.3. Microstructure analysis

The microstructures of the sintered pellets $ZnZr(Nb_{1-x}A_x)_2O_8$ ($A=Ta, Sb$) ($0 \leq x \leq 0.10$) at $1250^\circ C$ are shown in the Fig. 4. With the increase of the x values, the grain sizes have no obvious change. The grains of all the specimens are homogeneous and the surface is smooth. Moreover, the grain sizes are no significant differences, all in the range of $4-6\mu m$, which clearly indicates well-densified compounds.

3.4. Bond ionicity, lattice energy and bond energy calculation

It is well known that the concepts of chemical bond ionicity are very important for explaining many basic properties in diverse areas [12-14]. The chemical bond ionicity could be evaluated by P-V-L theory, which was generalized to application for complex crystals by *Zhang et al* [15-16]. Based on the complex bond theory and our previous work [17-18], the complex crystals $ZnZrNb_2O_8$ could be decomposed into the sum of binary crystals as follows:

$$\begin{aligned} ZnZrNb_2O_8 &= ZnZrNb_2O(1)_4O(2)_4 \\ &= Zn_{1/3}O(1)_{2/3} + Zn_{2/3}O(2)_{4/3} + Zr_{1/3}O(1)_{2/3} + Zr_{2/3}O(2)_{4/3} + Nb_{4/3}O(1)_{8/3} + Nb_{2/3}O(2)_{4/3} \\ &= Zn_{1/3}O(1)_{2/3} + Zn_{1/3}O(2)_{2/3}^1 + Zn_{1/3}O(2)_{2/3}^2 + Zr_{1/3}O(1)_{2/3} + Zr_{1/3}O(2)_{2/3}^1 \\ &\quad + Zr_{1/3}O(2)_{2/3}^2 + Nb_{2/3}O(1)_{4/3}^1 + Nb_{2/3}O(1)_{4/3}^2 + Nb_{2/3}O(2)_{4/3} \end{aligned}$$

According to the generalized P-V-L theory, the bond ionicity can be calculated using the generalized P-V-L dielectric theory as follows [17]:

$$f_i^\mu = \frac{(C^\mu)^2}{(E_g^\mu)^2} \quad (4)$$

$$f_C^\mu = \frac{(E_h^\mu)^2}{(E_g^\mu)^2} \quad (5)$$

where f_i^μ was the bond ionicity and f_c^μ was bond covalency E_g^μ was the average energy gap for the type bond μ , which was composed of homopolar E_h^μ and heteropolar C^μ parts as follows:

$$(E_g^\mu)^2 = (E_h^\mu)^2 + (C^\mu)^2 \quad (6)$$

where

$$(E_h^\mu)^2 = \frac{39.74}{(d^\mu)^{2.48}} \quad (7)$$

For any binary crystal A_mB_n type compounds, the heteropolar C^μ parts can be calculated from the reference 17.

Based on the generalized P-V-L theory [18-19], the lattice energy of a single-bond crystal can be separated into ionic and covalent parts. The ionic contribution to the crystal lattice energy mainly results from electrostatic interactions and repulsive interactions of the ion pairs, and the covalent contribution arises from the overlap of electron clouds. In the following paragraphs, the lattice energy U_{cal} of a complex crystal was written as follows:

$$U_{cal} = \sum_{\mu} U_b^\mu \quad (8)$$

$$U_b^\mu = U_{bc}^\mu + U_{bi}^\mu \quad (9)$$

$$U_{bc}^\mu = 2100m \frac{(Z_+^\mu)^{1.64}}{(d^\mu)^{0.75}} f_c^\mu \quad (10)$$

$$U_{bi}^\mu = 1270 \frac{(m+n)Z_+^\mu Z_-^\mu}{d^\mu} \left(1 - \frac{0.4}{d^\mu}\right) f_i^\mu \quad (11)$$

where U_{bc}^μ was the covalent part and U_{bi}^μ was the ionic part of μ bond. Z_+^μ and Z_-^μ were the valence states of cation and anion which constituted bond μ .

R. T. Sanderson [20-23] reported that the bond energy could be obtained by the chemical bond and the electronegativity. In our recent work, based on the electronegativity and bond energy theory, we have

generalized the Sanderson theory and complex theory[24-25]. The bond energy E of a complex crystal could be written as:

$$E = \sum_{\mu} E_b^{\mu} \quad (12)$$

$$E_b^{\mu} = t_c E_c^{\mu} + t_i E_i^{\mu} \quad (13)$$

where E_b^{μ} was bond energy for the type μ bond. The energy of the ionic form E_i^{μ} was the unit charge product divided by the bond length d^{μ} , adjusted to kcal/ mol by the factor 33200 when the bond length was pm.

$$E_i^{\mu} = \frac{33200}{d^{\mu}} \quad (14)$$

For any binary crystal $A_m B_n$ type compounds, the nonpolar covalence energy E_c^{μ} parts could be calculated as following:

$$E_c^{\mu} = \frac{(r_{cA} + r_{cB})}{d^{\mu}} (E_{A-A} E_{B-B})^{1/2} \quad (15)$$

where r_{cA} and r_{cB} were the covalent radii, E_{A-A} and E_{B-B} were the homonuclear bond energy.

For the Eq. (13), t_c and t_i were the covalent and ionic blending coefficients, respectively. The relationship of t_c and t_i can be described by the following formula:

$$t_c + t_i = 1 \quad (16)$$

The ionic blending coefficient t_i was defined as:

$$t_i = \left| \frac{(S_A - S_B) / \Delta S_B}{2} \right| \quad (17)$$

where S_A and S_B were the electronegativities of A and B ions, in this paper, $S_{Zn}=1.14$, $S_{Zr}=1.33$, $S_{Nb}=1.6$ and $S_O=3.44$. ΔS_B was the change for complete of an electron and had the value of 3.

3.5. Microwave dielectric properties analysis

The microwave dielectric properties of $ZnZr(Nb_{1-x}A_x)_2O_8$ ($A=Ta, Sb$) ($0 \leq x \leq 0.10$) ceramics are

illustrated in Table 4. At microwave frequencies, it is believed that the dielectric constant is affected by the dielectric polarizabilities, as well as the relative density and second phases [26]. In our experiments, ϵ_r is mainly dependent on the changing of the dielectric polarizabilities, due to the densified specimens from the SEM patterns in Fig.4. Moreover, there is no secondary phase in the compound.

Table.5 (a) and (b) shows the calculation of bond ionicity for $\text{ZnZr}(\text{Nb}_{1-x}\text{A}_x)_2\text{O}_8$ (A=Ta, Sb) ($0 \leq x \leq 0.10$) ceramics. According to the calculated results, the bond ionicity of Nb-O bond has a higher value compared with the bond type of Zn-O and Zr-O. It is clarified that the Nb-site bond ionicity has more contribution to the bond ionicity, and the bond ionicity of Nb-O type has dominant effect on the microwave dielectric properties of $\text{ZnZr}(\text{Nb}_{1-x}\text{A}_x)_2\text{O}_8$ (A=Ta, Sb) ceramics. According to the P-V-L theory studied by *Batsanov et al* [27], the relationship between constant and bond ionicity was founded as follows:

$$\epsilon_r = \frac{n^2 - 1}{1 - f_i} + 1 \quad (18)$$

where n is the refractive index. It is suggested that the dielectric constant decreased with the bond ionicity decreasing. The ϵ_r value and the average of Nb-site bond ionicity $Af_{i\text{Nb-O}}$ for $\text{ZnZr}(\text{Nb}_{1-x}\text{A}_x)_2\text{O}_8$ (A=Ta, Sb) ($0 \leq x \leq 0.1$) ceramics are given in Fig.5. As Fig.5 shows, the ϵ_r values keep the same change trend with the average of bond ionicity $Af_{i\text{Nb-O}}$ in the range of $x=0-0.10$. With the decreasing of the $Af_{i\text{Nb-O}}$, the ϵ_r values keep decreasing.

Usually, the $Q \times f$ values are controlled by many factors, and it can be divided into two fields, the intrinsic loss and extrinsic loss. The intrinsic losses are mainly caused by lattice vibration modes, while the extrinsic losses are dominated by such as second phases, oxygen vacancies, grain boundaries, and densification or porosity [28-31]. However, in this study, the effect of extrinsic loss is minimal due to the

densified compounds. In our recent work, we reported that $Q \times f$ values of NdNbO_4 ceramics were closely related to the lattice energy of the structure [17, 24, 25]. With an increase in the lattice energy, the $Q \times f$ values would increase. In this work, the $\text{ZnZrNb}_2\text{O}_8$ ceramics have the same structure with the NdNbO_4 ceramics. Therefore, the $Q \times f$ values of $\text{ZnZrNb}_2\text{O}_8$ ceramics were also closely dependent on the lattice energy. According the Rietveld refinement results, the calculations of lattice energy for $\text{ZnZr}(\text{Nb}_{1-x}\text{A}_x)_2\text{O}_8$ (A=Ta, Sb) ($0 \leq x \leq 0.10$) ceramics shown in Table.6 (a) and (b). Fig.6 shows the $Q \times f$ value and the average of Nb-site lattice energy $AU_{\text{Nb-o}}$ for $\text{ZnZr}(\text{Nb}_{1-x}\text{A}_x)_2\text{O}_8$ (A=Ta, Sb) ($0 \leq x \leq 0.1$) ceramics. With the substitution ions increasing, both the $Q \times f$ values of Ta^{5+} and Sb^{5+} substitution have an increasing trend. When $x = 0.10$, the second phase was formed from the Fig. 1(b). Therefore, with the increase of Sb^{5+} substitution, although the Nb-site lattice energy keeps increasing, the $Q \times f$ values decreased.

Reaney et al[32]. reported that the structural characteristics of [BO6] oxygen octahedral has a closely relation with the temperature coefficient of resonant frequency τ_f values, and τ_f values will change with the variations of the bond length of oxygen octahedral. In our previous research, we have investigated that the bond energy and bond length between the octahedral-site cation and oxygen will affect the τ_f values [24, 25]. The τ_f values decreased as the bond energy of oxygen octahedral increased, and the system will tend to stable. According to the calculation results of bond energy from Table.7 (a) and (b), we can find the fact that the substitution ions have more effect on the bond energy of oxygen octahedral, with the increasing of the substitution values, the average of Nb-site bond energy decreased. Fig.7 gives the τ_f value and the average of Nb-site bond energy $AE_{\text{Nb-o}}$ for $\text{ZnZr}(\text{Nb}_{1-x}\text{A}_x)_2\text{O}_8$ (A=Ta, Sb) ($0 \leq x \leq 0.1$) ceramics. As the $AE_{\text{Nb-o}}$ decreased, the τ_f values shift to the negative direction, it indicates that the system tend to instable. The bond energy of the $\text{ZnZr}(\text{Nb}_{1-x}\text{Sb}_x)_2\text{O}_8$ have a bigger value than the bond energy of the

$\text{ZnZr}(\text{Nb}_{1-x}\text{Ta}_x)_2\text{O}_8$, which indicates the $\text{ZnZr}(\text{Nb}_{1-x}\text{Sb}_x)_2\text{O}_8$ system would be more stable and have a small $|\tau_f|$ value.

4. Conclusions

The multiphase refinement was used to analysis the crystal structure of $\text{ZnZrNb}_2\text{O}_8$ ceramics. The bond ionicity, lattice energy and bond energy were calculated from Rietveld refinement results. The effects of Ta^{5+} and Sb^{5+} substitution on the microstructures and microwave dielectric properties of $\text{ZnZrNb}_2\text{O}_8$ ceramics were discussed. The ϵ_r was observed to decreased from 26.70 to 25.73 for Ta^{5+} substitution and 26.70 to 26.03 for Sb^{5+} substitution due to decrease in Nb-site bond ionicity. The $Q \times f$ values have a close relationship with the Nb-site lattice energy. Lower bond energy correlated with instable system, and instable system suggested that there would have a bigger $|\tau_f|$ value.

Acknowledgments

The authors gratefully acknowledged supports from the Key Laboratory of Advanced Ceramics and Machining Technology, Ministry of Education (Tianjin University). In addition, this work was supported by the project of development plan of science and technology of Ji'nan City (No.201303061), Ji'nan City Youth Science and Technology Star Project (No.2013035), and National Natural Science Foundation (No. 51472108).

References

- 1 L. C. Tien, C. C. Chou, D. S. Tsai, J. Am. Ceram. Soc. 83 (2000) 2074.
- 2 D. W. Kim, D. Y. Kim, K. S. Hong, J. Mater. Res. 15 (2000) 1331.
- 3 D. W. Kim, D. K. Kwon, S. H. Yoon, K. S. Hong, J. Am. Ceram. Soc. 89 (2006) 3861.
- 4 P. Zhang, Y. G. Zhao, J. Liu, Z. K. Song, M. Xiao, Y. X. Wang, Dalton. Trans. 44 (2015) 5053.

- 5 Q.W. Liao, L.X. Li, *J. Am. Ceram. Soc.* 95(2012) 3363.
- 6 S.D. Ramarao, V. R. K. Murthy, *Scripta. Mater.* 69 (2013) 274.
- 7 Y. Cheng, R.Z. Zuo, Y. Lv, *Ceram. Int.* 39 (2013) 8681.
- 8 X. Tang, H. Yang, Q. L. Zhang, J. H. Zhou, *Ceram. Int.* 40 (2014) 12875.
- 9 L. X. Li, H. Sun, H. C. Cai, X. S. Lv *J. Alloy. Compd.* 639 (2015) 516.
- 10 W. E. Courtney, *IEEE Trans Microwave Theory Tech.* 18 (1970) 476.
- 11 J. Macavei, H. Schulz, *Z. Krist-Cryst. Mater.* 207(1993) 193.
- 12 D. F. Xue, S. Y. Zhang, *J. Phys. Cond. Mat.* 8 (1996) 1949.
- 13 R. D. Shannon, *Acta. Cryst.* A32 (1976) 751.
- 14 A. F. Kapustinskii, *Rev. Chem. Soc.* 10 (1956) 283.
- 15 Z. J. Wu, Q. B. Meng, S. Y. Zhang, *Phys Rev. B.* 58 (1998) 958.
- 16 Q. B. Meng, Z. J. Wu, S. Y. Zhang, *J. Phys. Cond. Mat.* 10 (1998) 85.
- 17 P. Zhang, Y. G. Zhao, Y. X. Wang, *Dalton. Trans.* 44 (2015) 10932.
- 18 D. T. Liu, S. Y. Zhang, Z. J. Wu, *Inorg. Chem.* 42 (2003) 2465.
- 19 W. S. Xia, L. X. Li, P. F. Ning, Q. W. Liao, *J. Am. Ceram. Soc.* 95 (2012) 1.
- 20 R. T. Sandderson, *Inorg. Nucl. Chem.* 28 (1966) 1553.
- 21 R. T. Sandderson, *Inorg. Nucl. Chem.* 30 (1968) 375.
- 22 R. T. Sandderson, *Chemical Bonds and Bond Energy.* Academic Press: New York 1971.
- 23 R. T. Sandderson, *J. Am. Chem. Soc.* 105 (1983) 2259.
- 24 P. Zhang, Y. G. Zhao, X. Y. Wang, *J. Alloy. Compd.* 644 (2015) 621.
- 25 P. Zhang, Y. G. Zhao, X. Y. Wang, *J. Alloy. Compd.* 647 (2015) 386.

- 26 P. Zhang, Z. K. Song, Y. Wang, L.X. Li, *J. Am. Ceram. Soc.* 97 (2014) 976.
- 27 S. S. Batsanov, *Russ. Chem. Rev.* 51(1982) 684.
- 28 Q. W. Liao, L. X. Li, *Dalton. Trans.* 41(2012) 6963.
- 29 D. Zhou , Li X. Pang, H. Wang, X. Yao, *Solid. State. Sci.* 11 (2009) 1894.
- 30 R. D. Shannon, *J. Appl. Phys.* 73 (1993) 348.
- 31 C, L, Huang, S, S, Liu, *J. Appl. Phys.* 46 (2007) 283.
- 32 I. M. Reaney, E. L. Colla, and N. Setter, *Jpn. Appl. Phys.* 33 (1994) 3984.

A table of contents entry

Bond ionicity, lattice energy and bond energy were calculated from the Rietveld refinement.

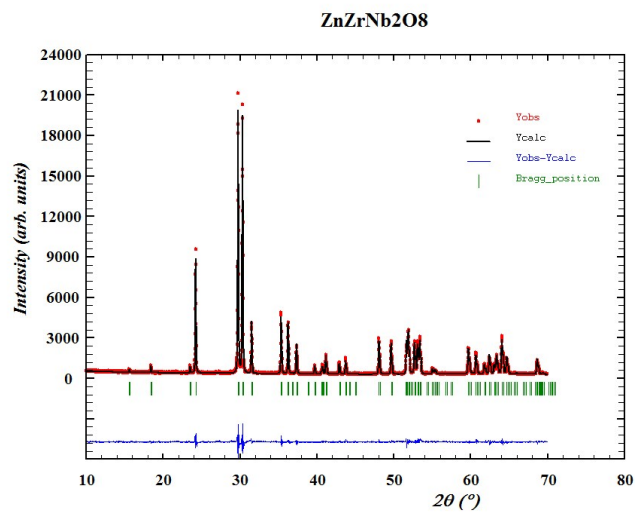


Figure captions

Fig.1 (a) The XRD patterns of $\text{ZnZr}(\text{Nb}_{1-x}\text{Ta}_x)_2\text{O}_8$ ($0.02 \leq x \leq 0.10$) ceramics sintered at 1250 °C for 4h; (b) The XRD patterns of $\text{ZnZr}(\text{Nb}_{1-x}\text{Sb}_x)_2\text{O}_8$ ($0.02 \leq x \leq 0.10$) ceramics sintered at 1250 °C for 4h; (c) The XRD patterns of $\text{ZnZrNb}_2\text{O}_8$, $\text{ZnZr}(\text{Nb}_{0.92}\text{Ta}_{0.08})_2\text{O}_8$, and $\text{ZnZr}(\text{Nb}_{0.92}\text{Sb}_{0.08})_2\text{O}_8$ ceramics sintered at 1250 °C for 4h.

Fig.2 The profile fits for the Rietveld refinement of $\text{ZnZrNb}_2\text{O}_8$ ceramic.

Fig.3 The crystal structure patterns ($1 \times 1 \times 1$) supercell of monoclinic wolframite structured $\text{ZnZrNb}_2\text{O}_8$.

Fig.4 The SEM photographs of $\text{ZnZr}(\text{Nb}_{1-x}\text{A}_x)_2\text{O}_8$ (A=Ta, Sb) ($0 \leq x \leq 0.1$) ceramics.

Fig.5 The ϵ_r value and the average of Nb-site bond ionicity $Af_{i\text{Nb-O}}$ for $\text{ZnZr}(\text{Nb}_{1-x}\text{A}_x)_2\text{O}_8$ (A=Ta, Sb) ($0 \leq x \leq 0.1$) ceramics.

Fig.6 The $Q \times f$ value and the average of Nb-site lattice energy $AU_{\text{Nb-o}}$ for $\text{ZnZr}(\text{Nb}_{1-x}\text{A}_x)_2\text{O}_8$ (A=Ta, Sb) ($0 \leq x \leq 0.1$) ceramics.

Fig.7 The τ_f value and the average of Nb-site bond energy $AE_{\text{Nb-o}}$ for $\text{ZnZr}(\text{Nb}_{1-x}\text{A}_x)_2\text{O}_8$ (A=Ta, Sb) ($0 \leq x \leq 0.1$) ceramics.

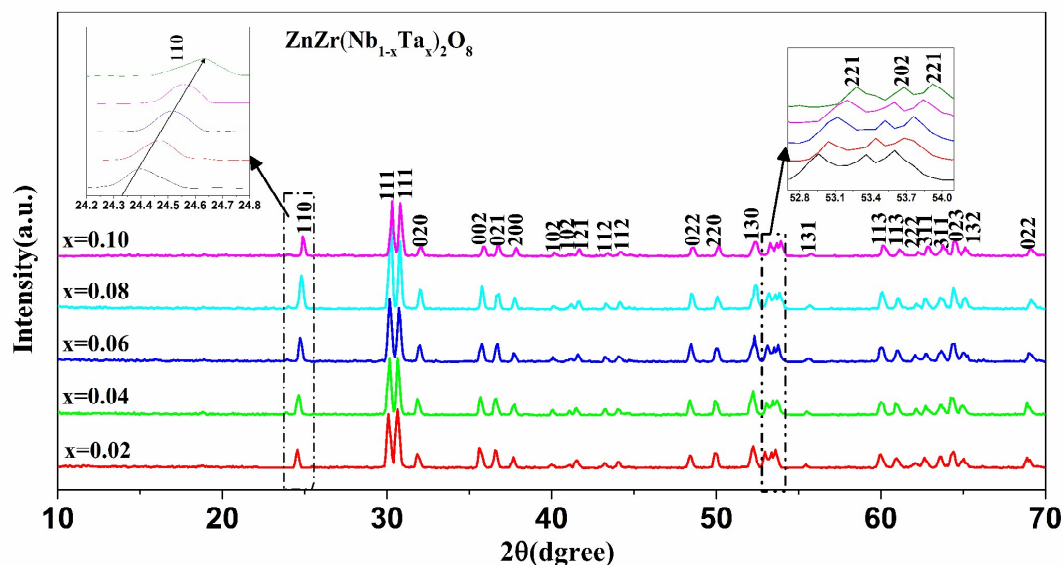


Fig.1 (a)

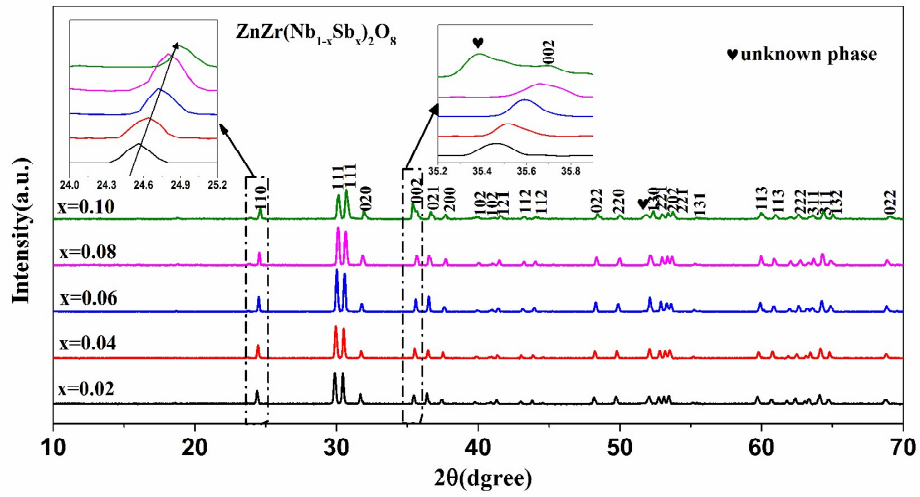


Fig.1 (b)

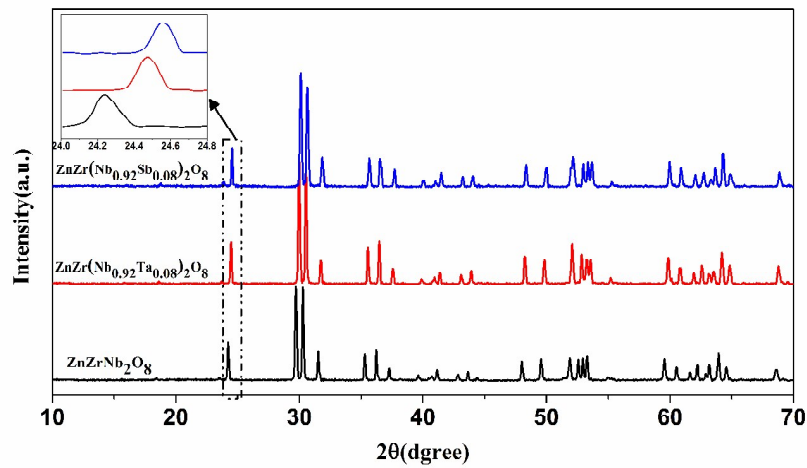


Fig.1 (b)

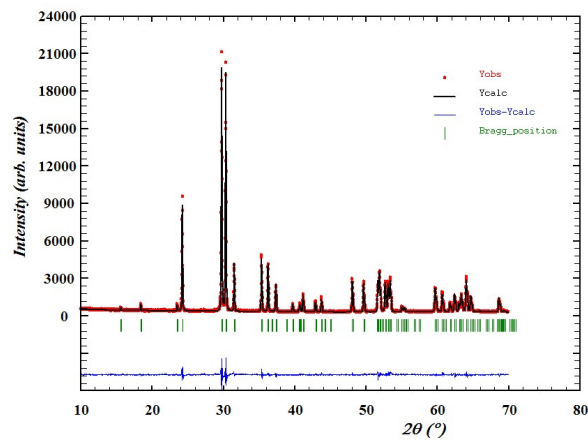
ZnZrNb₂O₈

Fig.2

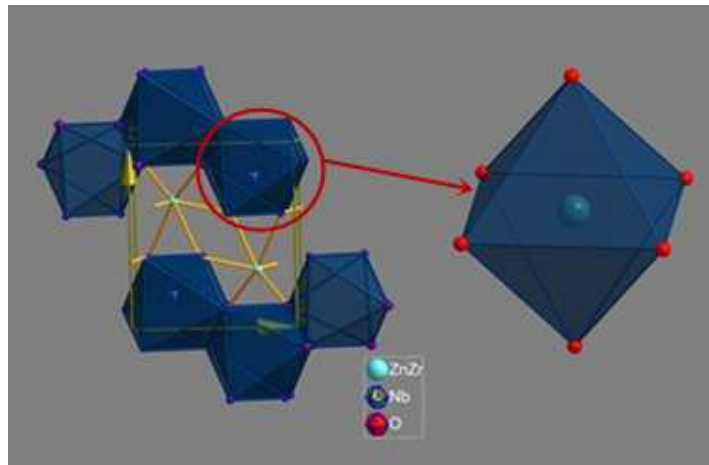


Fig.3

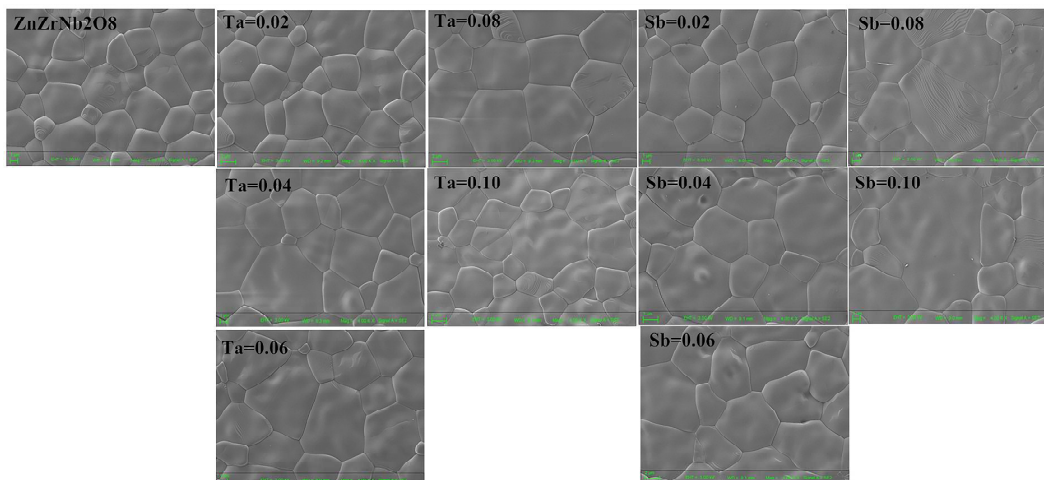


Fig. 4

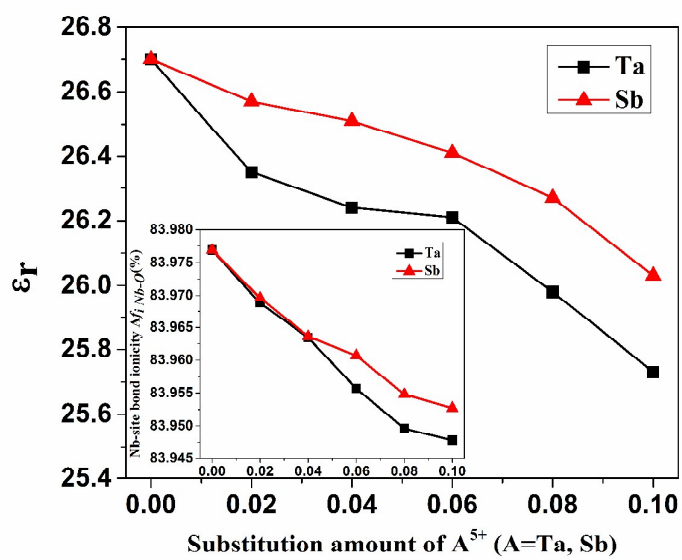


Fig.5

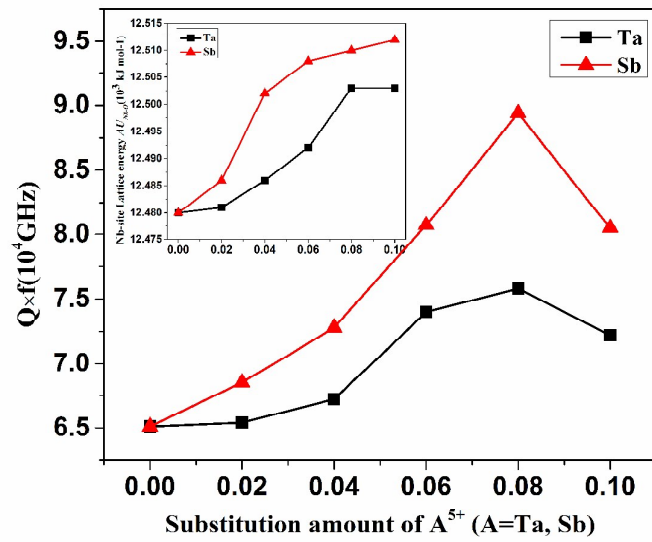


Fig.6

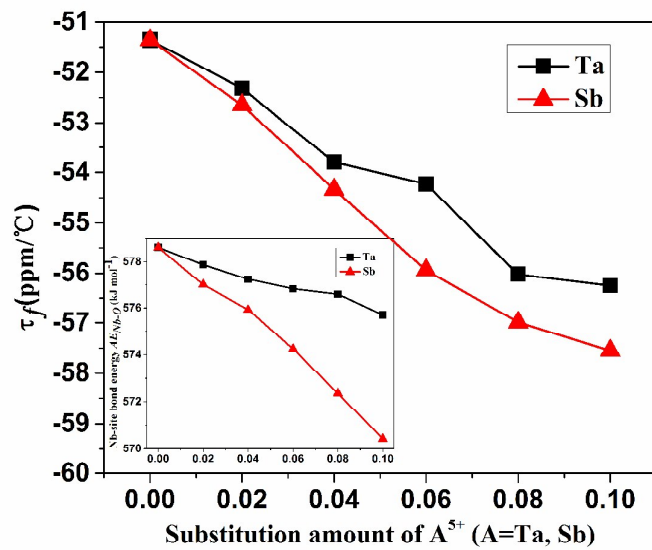


Fig.7

Table.1 Crystallographic data from Rietveld refinement for $\text{ZnZr}(\text{Nb}_{1-x}\text{A}_x)_2\text{O}_8$ (A=Ta, Sb)

(0≤x≤0.10) ceramics

Type	<i>a</i> (Å)	<i>b</i> (Å)	<i>c</i> (Å)	β (°)	<i>V</i> (Å ³)	<i>R_p</i> (%)	<i>R_{wp}</i> (%)
<i>ZnZrNb₂O₈</i>	4.813	5.674	5.076	91.45	138.56	11.41	12.42
<i>ZnZr(Nb_{1-x}Ta_x)₂O₈</i>							
<i>x=0.02</i>	4.793	5.706	5.063	90.96	138.44	9.29	14.90
<i>x=0.04</i>	4.770	5.688	5.092	90.27	138.15	9.46	13.67
<i>x=0.06</i>	4.757	5.716	5.072	90.57	137.91	8.67	14.87
<i>x=0.08</i>	4.754	5.715	5.061	90.92	137.49	9.12	14.46
<i>x=0.10</i>	4.739	5.678	5.105	90.20	137.35	7.69	10.36
<i>ZnZr(Nb_{1-x}Sb_x)₂O₈</i>							
<i>x=0.02</i>	4.810	5.690	5.050	90.68	138.20	10.27	13.60
<i>x=0.04</i>	4.798	5.662	5.067	91.48	137.61	9.06	11.15
<i>x=0.06</i>	4.796	5.655	5.065	91.39	137.33	9.98	10.74
<i>x=0.08</i>	4.777	5.665	5.069	90.83	137.16	8.73	11.73
<i>x=0.10</i>	4.775	5.662	5.069	90.48	137.04	7.64	13.84

Table.2 (a) Bond length (Å) for $\text{ZnZr}(\text{Nb}_{1-x}\text{Ta}_x)_2\text{O}_8$ (0≤x≤0.10) ceramics

Type	x=0	Ta(0.02)	Ta(0.04)	Ta(0.06)	Ta(0.08)	Ta(0.10)
<i>Zn-O(1)×2</i>	2.0195	2.0130	2.0018	2.0042	2.0064	1.9954
<i>Zn-O(2)¹×2</i>	2.0852	2.0877	2.1038	2.0922	2.0831	2.1046
<i>Zn-O(2)²×2</i>	2.2177	2.2186	2.2084	2.2144	2.2156	2.2026
<i>Ti-O(1)×2</i>	2.0195	2.0130	2.0018	2.0042	2.0064	1.9954

<i>Ti-O(2)¹×2</i>	2.0852	2.0877	2.1038	2.0922	2.0831	2.1046
<i>Ti-O(2)²×2</i>	2.2177	2.2186	2.2084	2.2144	2.2156	2.2026
<i>Nb-O(1)¹×2</i>	1.9815	1.9688	1.9626	1.9609	1.9630	1.9608
<i>Nb-O(1)²×2</i>	2.1825	2.1905	2.1921	2.1927	2.1885	2.1882
<i>Nb-O(2)×2</i>	1.8858	1.8902	1.8923	1.8893	1.8846	1.8871

Table.2 (b) Bond length (Å) for ZnZr(Nb_{1-x}Sb_x)₂O₈ (0.02≤x≤0.10) ceramics

Type	Sb(0.02)	Sb(0.04)	Sb(0.06)	Sb(0.08)	Sb(0.010)
<i>Zn-O(1)×2</i>	2.0100	2.0149	2.0125	2.0044	1.9999
<i>Zn-O(2)¹×2</i>	2.0904	2.0803	2.0808	2.0889	2.0942
<i>Zn-O(2)²×2</i>	2.2141	2.2128	2.2101	2.2064	2.2030
<i>Ti-O(1)×2</i>	2.0100	2.0149	2.0125	2.0044	1.9999
<i>Ti-O(2)¹×2</i>	2.0904	2.0803	2.0808	2.0889	2.0942
<i>Ti-O(2)²×2</i>	2.2141	2.2128	2.2101	2.2064	2.2030
<i>Nb-O(1)¹×2</i>	1.9632	1.9775	1.9753	1.9657	1.9601
<i>Nb-O(1)²×2</i>	2.1901	2.1774	2.1762	2.1813	2.1833
<i>Nb-O(2)×2</i>	1.8930	1.8809	1.8804	1.8839	1.8865

Table.3 The refined atomic coordinate of ZnZrNb₂O₈ ceramic.

Element	Wyckoff site	x	y	z	OCC
Zn	2f	0.50000	0.68856	0.25000	0.5
Zr	2f	0.50000	0.68856	0.25000	0.5
Nb	2e	0.00000	0.18317	0.25000	1.0
O1	4g	0.22452	0.10786	0.93916	1.0

O2	4g	0.26568	0.38588	0.40895	1.0
----	----	---------	---------	---------	-----

Table.4 The microwave dielectric properties of $\text{ZnZr}(\text{Nb}_{1-x}\text{A}_x)_2\text{O}_8$ (A=Ta, Sb) ($0 \leq x \leq 0.10$) ceramics

Type	ϵ_r	$Q \times f$ (10^4 GHz)	τ_f (ppm/ $^\circ\text{C}$)
$\text{ZnZrNb}_2\text{O}_8$	26.70	6.51	-51.36
$\text{ZnZr}(\text{Nb}_{1-x}\text{Ta}_x)_2\text{O}_8$			
$x=0.02$	26.35	6.54	-52.31
$x=0.04$	26.24	6.72	-53.80
$x=0.06$	26.21	7.40	-54.23
$x=0.08$	25.98	7.58	-56.02
$x=0.10$	25.73	7.22	-56.25
$\text{ZnZr}(\text{Nb}_{1-x}\text{Sb}_x)_2\text{O}_8$			
$x=0.02$	26.57	6.85	-52.65
$x=0.04$	26.51	7.28	-54.34
$x=0.06$	26.41	8.07	-55.94
$x=0.08$	26.27	8.94	-56.99
$x=0.10$	26.03	8.05	-57.55

Table.5 (a) Bond ionicity for $\text{ZnZr}(\text{Nb}_{1-x}\text{Ta}_x)_2\text{O}_8$ ($0 \leq x \leq 0.10$) ceramics

Bond type	Bond Ionicity f_i (%)					
	$x=0$	$x=0.02$	$x=0.04$	$x=0.06$	$x=0.08$	$x=0.10$
$\text{Zn-O}(1) \times 2$	63.3780	63.3116	63.2064	63.2242	63.2442	63.1402
$\text{Zn-O}(2)^1 \times 2$	63.9399	63.9521	64.0784	63.9809	63.9066	63.0772
$\text{Zn-O}(2)^2 \times 2$	64.9372	64.9349	64.8604	64.8980	64.9063	64.8121

<i>Ti-O(1)</i> ×2	80.2169	80.1845	80.1358	80.1426	80.1517	80.1035
<i>Ti-O(2)¹</i> ×2	80.4642	80.4667	80.5196	80.4764	80.4444	80.5165
<i>Ti-O(2)²</i> ×2	80.8777	80.8737	80.8428	80.8562	80.8595	80.8206
<i>Nb/Ta-O(1)¹</i> ×2	83.9203	83.8762	83.8545	83.8465	83.8531	83.8428
<i>Nb/Ta-O(1)²</i> ×2	84.4072	84.4166	84.4170	84.4153	84.4075	84.4045
<i>Nb/Ta-O(2)</i> ×2	83.6032	83.6137	83.6188	83.6053	83.5882	83.5950
<i>Af_{i Nb-O}</i> *	83.9769	83.9688	83.9634	83.9557	83.9496	83.9478

*The *Af_{i Nb-O}* was the average of the Nb/Ta-O bond ionicity.

Table.5 (b) Bond ionicity for ZnZr(Nb_{1-x}Sb_x)₂O₈ (0≤x≤0.10) ceramics

Bond type	Bond Ionicity <i>f_i</i> (%)					
	<i>x=0</i>	<i>x=0.02</i>	<i>x=0.04</i>	<i>x=0.06</i>	<i>x=0.08</i>	<i>x=0.10</i>
<i>Zn-O(1)</i> ×2	63.3780	63.2896	63.3368	63.3163	63.2376	63.1955
<i>Zn-O(2)¹</i> ×2	63.9399	63.9792	63.8996	63.9047	63.9658	64.0077
<i>Zn-O(2)²</i> ×2	64.9372	64.9091	64.9033	64.8855	64.8542	64.8293
<i>Ti-O(1)</i> ×2	80.2169	80.1762	80.1984	80.1895	80.1523	80.1329
<i>Ti-O(2)¹</i> ×2	80.4642	80.4801	80.4468	80.4493	80.4739	80.4916
<i>Ti-O(2)²</i> ×2	80.8777	80.8654	80.8643	80.8576	80.8431	80.8327
<i>Nb/Sb-O(1)¹</i> ×2	83.9203	83.8623	83.9082	83.9022	83.8692	83.8510
<i>Nb/Sb-O(1)²</i> ×2	84.4072	84.4193	84.3974	84.3958	84.4019	84.4049
<i>Nb/Sb-O(2)</i> ×2	83.6032	83.6272	83.5852	83.5841	83.5934	83.6021
<i>Af_{i Nb-O}</i> *	83.9769	83.9696	83.9636	83.9607	83.9548	83.9527

*The *Af_{i Nb-O}* was the average of the Nb/Sb-O bond ionicity.

Table.6 (a) Lattice energy for ZnZr(Nb_{1-x}Ta_x)₂O₈ (0≤x≤0.10) ceramics

Bond type	Lattice energy U (eV)					
	$x=0$	$x=0.02$	$x=0.04$	$x=0.06$	$x=0.08$	$x=0.10$
$Zn-O(1)\times 2$	1111	1114	1119	1117	1117	1122
$Zn-O(2)^1\times 2$	1082	1082	1076	1080	1084	1075
$Zn-O(2)^2\times 2$	1031	1030	1034	1032	1032	1037
$Ti-O(1)\times 2$	4030	4040	4058	4054	4051	4067
$Ti-O(2)^1\times 2$	3934	3931	3907	3924	3937	3906
$Ti-O(2)^2\times 2$	3752	3751	3765	3757	3756	3772
$Nb/Ta-O(1)^1\times 2$	12620	12680	12710	12718	12708	12719
$Nb/Ta-O(1)^2\times 2$	11732	11698	11692	11689	11706	11708
$Nb/Ta-O(2)\times 2$	13088	13066	13055	13070	13094	13081
AU_{Nb-O}^*	12480	12481	12486	12492	12503	12503

*The AU_{Nb-O} was the average of the Nb/Ta-O lattice energy.

Table.6 (b) Lattice energy for $ZnZr(Nb_{1-x}Sb_x)_2O_8$ ($0\leq x\leq 0.10$) ceramics

Bond type	Lattice energy U (eV)					
	$x=0$	$x=0.02$	$x=0.04$	$x=0.06$	$x=0.08$	$x=0.10$
$Zn-O(1)\times 2$	1111	1115	1113	1114	1117	1119
$Zn-O(2)^1\times 2$	1082	1081	1085	1085	1081	1079
$Zn-O(2)^2\times 2$	1031	1032	1032	1034	1035	1036
$Ti-O(1)\times 2$	4030	4044	4037	4041	4053	4060
$Ti-O(2)^1\times 2$	3934	3926	3941	3940	3929	3921
$Ti-O(2)^2\times 2$	3752	3757	3759	3762	3768	3772

$Nb/Sb-O(1)^1 \times 2$	12620	12707	12639	12649	12695	12723
$Nb/Sb-O(1)^2 \times 2$	11732	11700	11753	11758	11736	11729
$Nb/Sb-O(2) \times 2$	13088	13051	13113	13116	13098	13084
$A U_{Nb-O}^*$	12480	12486	12502	12508	12510	12512

*The $A U_{Nb-O}$ was the average of the Nb/Sb-O lattice energy.

Table.7 (a) Bond energy for $ZnZr(Nb_{1-x}Ta_x)_2O_8$ ($0 \leq x \leq 0.10$) ceramics

Bond type	Bond energy E (kJ/mol)					
	$x=0$	$x=0.02$	$x=0.04$	$x=0.06$	$x=0.08$	$x=0.10$
$Zn-O(1) \times 2$	271.25	272.13	273.65	273.33	273.03	274.53
$Zn-O(2)^1 \times 2$	262.71	262.39	260.39	261.83	262.97	260.29
$Zn-O(2)^2 \times 2$	247.01	246.91	248.05	247.38	247.25	248.71
$Ti-O(1) \times 2$	510.33	511.98	514.85	514.23	513.66	516.50
$Ti-O(2)^1 \times 2$	494.25	493.66	489.88	492.60	494.75	489.70
$Ti-O(2)^2 \times 2$	464.72	464.53	466.68	465.42	465.16	467.91
$Nb/Ta-O(1)^1 \times 2$	586.69	589.59	590.56	590.18	588.65	588.42
$Nb/Ta-O(1)^2 \times 2$	532.66	529.91	528.73	527.79	528.00	527.27
$Nb/Ta-O(2) \times 2$	616.46	614.10	612.50	612.54	613.14	611.40
$A E_{Nb-O}^*$	578.60	577.87	577.26	576.84	576.60	575.70

*The $A E_{Nb-O}$ was the average of the Nb/Ta-O bond energy.

Table.7 (b) Bond energy for $ZnZr(Nb_{1-x}Sb_x)_2O_8$ ($0 \leq x \leq 0.10$) ceramics

Bond type	Bond energy E (kJ/mol)					
	$x=0$	$x=0.02$	$x=0.04$	$x=0.06$	$x=0.08$	$x=0.10$
$Zn-O(1) \times 2$	271.25	272.54	271.87	272.20	273.30	273.91

<i>Zn-O(2)¹×2</i>	262.71	262.05	263.33	263.26	262.24	261.58
<i>Zn-O(2)²×2</i>	247.01	247.41	247.56	247.86	248.28	248.66
<i>Ti-O(1)×2</i>	510.33	512.74	511.50	512.11	514.18	515.33
<i>Ti-O(2)¹×2</i>	494.25	493.02	495.42	495.30	493.38	492.13
<i>Ti-O(2)²×2</i>	464.72	465.48	465.75	466.32	467.10	467.82
<i>Nb/Sb-O(1)¹×2</i>	586.69	590.10	583.79	582.38	583.13	582.69
<i>Nb/Sb-O(1)²×2</i>	532.66	528.97	530.19	528.61	525.50	523.13
<i>Nb/Sb-O(2)×2</i>	616.46	611.99	613.77	611.77	608.45	605.43
<i>A E_{Nb-O} *</i>	578.60	577.02	575.92	574.25	572.36	570.42

*The *A E_{Nb-O}* was the average of the Nb/Sb-O bond energy.