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Can $\mathrm{HN}=\mathrm{NH}, \mathrm{FN}=\mathrm{NH}$, or $\mathrm{HN}=\mathrm{CHOH}$ Bridge the $\sigma$-Hole and the Lone Pair at P in Binary Complexes with $\mathrm{H}_{2} \mathrm{XP}$, for $\mathrm{X}=\mathrm{F}, \mathrm{Cl}, \mathrm{NC}, \mathrm{OH}, \mathrm{CN}, \mathrm{CCH}, \mathrm{CH}_{3}$, and H ? ${ }^{\%}$

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${ }^{\text {\% }}$ Electronic supplementary information (ESI) available: Geometries, total energies, and molecular graphs of all complexes; components of spin-spin coupling constants ${ }^{1 p} \mathrm{~J}(\mathrm{P}-\mathrm{N})$, ${ }^{2 h} \mathrm{~J}(\mathrm{~N}-\mathrm{P}), \mathrm{J}(\mathrm{N}-\mathrm{P})$, and ${ }^{2 \mathrm{~h}} \mathrm{~J}(\mathrm{O}-\mathrm{P})$; plots of energy densities versus corresponding bond distances; plot of ${ }^{2 h} \mathrm{~J}(\mathrm{O}-\mathrm{P})$ versus the O-P distance. See DOI:10.1039/XXXXXX


#### Abstract

Ab initio MP2/aug'-cc-pVTZ calculations have been carried out to investigate the properties of complexes formed between $\mathrm{H}_{2} \mathrm{XP}$, for $\mathrm{X}=\mathrm{F}, \mathrm{Cl}, \mathrm{NC}, \mathrm{OH}, \mathrm{CN}, \mathrm{CCH}, \mathrm{CH}_{3}$, and H , and the possible bridging molecules $\mathrm{HN}=\mathrm{NH}, \mathrm{FN}=\mathrm{NH}$, and $\mathrm{HN}=\mathrm{CHOH} . \mathrm{H}_{2} \mathrm{XP}: \mathrm{HNNH}$ and $\mathrm{H}_{2} \mathrm{XP}: F N N H$ complexes are stabilized by $\mathrm{P} \cdots \mathrm{N}$ pnicogen bonds, except for $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}:$ FNNH and $\mathrm{H}_{3} \mathrm{P}: \mathrm{FNNH}$ which are stabilized by $\mathrm{N}-\mathrm{H} \cdots \mathrm{P}$ hydrogen bonds. $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNCHOH}$ complexes are stabilized by $\mathrm{P}^{\cdots} \mathrm{N}$ pnicogen bonds and nonlinear $\mathrm{O}-\mathrm{H} \cdots \mathrm{P}$ hydrogen bonds. For a fixed $\mathrm{H}_{2} \mathrm{XP}$ molecule, binding energies decrease in the order $\mathrm{HNCHOH}>\mathrm{HNNH}>\mathrm{FNNH}$, except for the binding energies of $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}$ and $\mathrm{H}_{3} \mathrm{P}$ with HNNH and FNNH . Binding energies of complexes with HNCHOH and HNNH increase as the $\mathrm{P}-\mathrm{N}_{1}$ distance decreases, but binding energies of complexes with FNNH show little dependence on this distance. The large binding energies of $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNCHOH}$ complexes arise from a cooperative effect involving electron-pair acceptance by P to form a pnicogen bond, and electron-pair donation by P to form a hydrogen bond. The dominant charge-transfer interaction in these complexes involves electron-pair donation by N across the pnicogen bond, except for complexes in which X is one of the more electropositive substituents, $\mathrm{CCH}, \mathrm{CH}_{3}$, and H . For these, lone-pair donation by P across the hydrogen bond dominates. AIM and NBO data for these complexes are consistent with their bonding characteristics, showing molecular graphs with bond critical points and charge-transfer interactions associated with hydrogen and pnicogen bonds. EOM-CCSD spin-spin coupling constants ${ }^{1 p} \mathrm{~J}(\mathrm{P}-\mathrm{N})$ across the pnicogen bond for each series of complexes correlate with the P-N distance. In contrast, ${ }^{2 h} \mathrm{~J}(\mathrm{O}-\mathrm{P})$ values for complexes $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNCHOH}$ do not correlate with the O-P distance, a consequence of the nonlinearity of these hydrogen bonds.


## INTRODUCTION

Since the publication of two papers on pnicogen bonds in 2011, ${ }^{1,2}$ interest in this bond has grown dramatically, as evidenced not only by the number of research papers published on this subject, but also by the number of review articles which have appeared recently. ${ }^{3,4,5}$ The pnicogen bond is an intermolecular bond formed when a Group 15 atom acts as an electron-pair acceptor. According to Politzer and Murray, ${ }^{6,7}$ bond formation at the pnicogen atom occurs through the $\sigma$-hole, a positive region of the molecular electrostatic potential. In addition to the $\sigma$ hole at P , there is also a lone pair of electrons. That the phosphorus atom can act as both an electron-pair acceptor and an electron-pair donor has been documented in several studies. In a 2013 paper, ${ }^{8}$ we demonstrated that the phosphorus in a pnicogen-bonded complex can simultaneously act as an electron-pair donor to a Lewis acid such as HF to form a hydrogen bond, ClF to form a halogen bond, LiH to form a lithium bond, or $\mathrm{BeH}_{2}$ to form a beryllium bond. The P atom also acts as an electron-pair donor and acceptor in pnicogen-bonded trimers $\left(\mathrm{PH}_{2} \mathrm{X}\right)_{3}$ and tetramers $\left(\mathrm{PH}_{2} \mathrm{X}\right)_{4} .{ }^{9,10}$

In the present paper, we ask whether or not a single small molecule can interact with P at both its $\sigma$-hole and its lone pair, as illustrated in Scheme 1. For this study we have used a series of substituted $\mathrm{H}_{2} \mathrm{XP}$ molecules, for $\mathrm{X}=\mathrm{F}, \mathrm{Cl}, \mathrm{NC}, \mathrm{OH}, \mathrm{CN}, \mathrm{CCH}, \mathrm{CH}_{3}$, and H , in order to vary the electron-accepting and electron-donating abilities of P . The three bridging molecules are $\mathrm{HN}=\mathrm{NH}, \mathrm{FN}=\mathrm{NH}$, and $\mathrm{HN}=\mathrm{CHOH}$ (formamidic acid), which also differ in their electrondonating ability to form a pnicogen bond, and their electron accepting ability to form a hydrogen bond. Can both of these bonds exist simultaneously in these simple binary complexes, or will these complexes be stabilized by either a pnicogen bond or a hydrogen bond? The structures of these complexes, their binding energies, charge-transfer energies, and spin-spin coupling constants ${ }^{1 p}(\mathrm{P}-\mathrm{N}),{ }^{2 \mathrm{~J}} \mathrm{~J}(\mathrm{~N}-\mathrm{P})$, and ${ }^{2 \mathrm{~h}} \mathrm{~J}(\mathrm{O}-\mathrm{P})$, will be used to provide an answer to this question.



Scheme 1. Representation of the lone pair and the $\sigma$-hole in an isolated phosphine (left) and the potential bridging interaction (right) involving atoms Y and H , in blue color.

## METHODS

The structures of the monomers $\mathrm{H}_{2} \mathrm{XP}, \mathrm{HN}=\mathrm{NH}, \mathrm{FN}=\mathrm{NH}$, and $\mathrm{HN}=\mathrm{CHOH}$ (formamidic acid), and the complexes $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNNH}, \mathrm{H}_{2} \mathrm{XP}: \mathrm{FNNH}$, and $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNCHOH}$ were optimized at second-order Møller-Plesset perturbation theory (MP2) ${ }^{11,12,13,14}$ with the aug'-cc-pVTZ basis set. ${ }^{15}$ This basis set is derived from the Dunning aug-cc-pVTZ basis set ${ }^{16,17}$ by removing diffuse functions from hydrogen atoms. Frequencies were computed to establish that the optimized structures correspond to equilibrium structures on their potential surfaces. The binding energy of a complex is defined as the negative energy $(-\Delta \mathrm{E})$ for the reaction which forms the complex from the isolated monomers. All calculations were performed using the Gaussian 09 program. ${ }^{18}$

The electron densities of the complexes have been analyzed using the Atoms in Molecules (AIM) methodology ${ }^{19,20,21,22}$ employing the AIMAll ${ }^{23}$ program. The topological analysis of the electron density produces the molecular graph of each complex. This graph identifies the location of electron density features of interest, including the electron density ( $\rho$ ) maxima associated with the various nuclei, saddle points which correspond to bond critical points (BCPs), and ring critical points which indicate a minimum electron density within a ring. The zero gradient line which connects a BCP with two nuclei is the bond path. The electron density at the BCP ( $\rho_{\mathrm{BCP}}$ ), its Laplacian $\left(\nabla^{2} \rho_{\mathrm{BCP}}\right)$, and the total energy density $\left(H_{\mathrm{BCP}}\right)$ can also be used to characterize interactions. ${ }^{24}$ In addition, the Natural Bond Orbital (NBO) ${ }^{25}$ method has been used to analyze the stabilizing charge-transfer interactions employing the NBO-6 program. ${ }^{26}$ Since MP2 orbitals are nonexistent, the charge-transfer interactions have been computed using the B3LYP functional ${ }^{27,28}$ with the aug'-cc-pVTZ basis set at the MP2/aug'-cc-pVTZ complex geometries, so that at least some electron correlations effects could be included.

Spin-spin coupling constants were evaluated using the equation-of-motion coupled cluster singles and doubles (EOM-CCSD) method in the CI (configuration interaction)-like approximation, ${ }^{29,30}$ with all electrons correlated. For these calculations, the Ahlrichs ${ }^{31}$ qzp basis set was placed on ${ }^{13} \mathrm{C},{ }^{15} \mathrm{~N},{ }^{17} \mathrm{O}$, and ${ }^{19} \mathrm{~F}$, and the qz2p basis set on ${ }^{31} \mathrm{P},{ }^{35} \mathrm{C}$, and hydrogenbonded ${ }^{1} \mathrm{H}$ atoms. The Dunning cc-pVDZ basis was placed on all other ${ }^{1} \mathrm{H}$ atoms. The EOMCCSD calculations were performed using ACES $\mathrm{II}^{32}$ on the IBM Cluster 1350 (Glenn) at the Ohio Supercomputer Center.

## RESULTS AND DISCUSSION

The molecular electrostatic potentials on the 0.001 au electron density isosurface of the isolated phosphines show the presence of a maximum and a minimum value around the phosphorous atom associated to the $\sigma$-hole and lone pair, respectively, ${ }^{33}$ as illustrated in Scheme 1. The monomers $\mathrm{HNNH}, \mathrm{FNNH}$, and HNCHOH may act as electron pair donors to the $\mathrm{H}_{2} \mathrm{XP}$ molecules through the $\sigma$-hole to form $\mathrm{P} \cdots \mathrm{N}$ pnicogen bonds, and also as electron-pair acceptors to form $\mathrm{N}-\mathrm{H} \cdots \mathrm{P}$ or $\mathrm{O}-\mathrm{H} \cdots \mathrm{P}$ hydrogen bonds. To distinguish between the two $\mathrm{N}-\mathrm{H}$ bonds in $\mathrm{HNNH}, \mathrm{H}_{1}$ is bonded to the nitrogen $\mathrm{N}_{1}$ that takes part in the pnicogen bond, and $\mathrm{H}_{2}$ is bonded to $\mathrm{N}_{2}$, whether or not the $\mathrm{N}_{2}-\mathrm{H}_{2}$ group is involved in a hydrogen-bonding interaction. Fig. 1 illustrates these designations in the $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}: \mathrm{HNNH}$ complex.


Fig. 1. The molecular graph of the $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}: H N N H$ complex illustrating the labeling of the two $\mathrm{N}-\mathrm{H}$ groups and the locations of bond critical points.

## Structures, Binding Energies, Charge-Transfer Energies, and NBO Data

The structures, total energies, and molecular graphs of the complexes $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNNH}$, $\mathrm{H}_{2} \mathrm{XP}: \mathrm{FNNH}$, and $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNCHOH}$ are reported in Table S 1 of the Supporting Information. The binding energies, intermolecular P- $\mathrm{N}_{1}$ distances, and $\mathrm{N}_{1}-\mathrm{P}-\mathrm{A}$ angles across the pnicogen bonds are reported in Table 1, with A the atom of X that is directly bonded to P . The $\mathrm{H}_{2} \mathrm{XP}$ molecules are listed in Table 1 according to decreasing binding energies of their complexes with HNNH. This is also the order of decreasing binding energies for complexes with HNCHOH , but not for complexes with FNNH. The binding energies range between 13 and $31 \mathrm{~kJ} \mathrm{~mol}^{-1}$ for HNNH complexes and between 20 and $44 \mathrm{~kJ} \cdot \mathrm{~mol}^{-1}$ for HNCHOH complexes, but exhibit a much
narrower range from 12 to $21 \mathrm{~kJ} \cdot \mathrm{~mol}^{-1}$ for complexes with FNNH. For a fixed $\mathrm{H}_{2} \mathrm{XP}$ molecule, binding energies decrease in the order

$$
\mathrm{HNCHOH}>\mathrm{HNNH}>\mathrm{FNNH}
$$

except for the binding energies of $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}$ and $\mathrm{H}_{3} \mathrm{P}$ with HNNH and FNNH. The reason for this reversal will become evident in the following subsections of this paper. Fig. 2 presents a plot of these binding energies versus the $\mathrm{P}-\mathrm{N}_{1}$ distance. As is evident from this figure, binding

Table 1. Binding energies $\left(-\Delta \mathrm{E}, \mathrm{kJ} \cdot \mathrm{mol}^{-1}\right), \mathrm{P}-\mathrm{N}_{1}$ distances $(\mathrm{R}, \AA)$, and $\mathrm{N}_{1}-\mathrm{P}-\mathrm{A}$ angles $\left(<,{ }^{\mathrm{o}}\right)^{\mathrm{a}}$ across $\mathrm{P}^{\cdots} \mathrm{N}_{1}$ pnicogen bonds in complexes of $\mathrm{H}_{2} \mathrm{XP}$ with $\mathrm{HNNH}, \mathrm{FNNH}$, and HNCHOH

| Molecule: | HNNH |  | FNNH |  | HNCHOH |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{H}_{2} \mathrm{XP}=$ | $-\Delta \mathrm{E}$ | $\mathrm{R}\left(\mathrm{P}-\mathrm{N}_{1}\right)<$ | $-\Delta \mathrm{E}$ | $\mathrm{R}\left(\mathrm{P}-\mathrm{N}_{1}\right)<$ | - $\Delta \mathrm{E}$ | $\mathrm{R}\left(\mathrm{P}-\mathrm{N}_{1}\right)<$ |
| $\mathrm{H}_{2} \mathrm{FP}$ | 31.3 | $2.512 \quad 173$ | 18.8 | 2.773174 | 44.4 | 2.507170 |
| $\mathrm{H}_{2} \mathrm{ClP}$ | 26.9 | $2.651 \quad 173$ | 15.0 | 2.894173 | 37.4 | $2.620 \quad 168$ |
| $\mathrm{H}_{2}(\mathrm{NC}) \mathrm{P}$ | 25.2 | $2.646 \quad 174$ | 15.7 | 2.939177 | 36.5 | $2.615 \quad 170$ |
| $\mathrm{H}_{2}(\mathrm{OH}) \mathrm{P}$ | 21.4 | $2.755 \quad 174$ | 16.6 | 3.054179 | 33.0 | 2.778169 |
| $\mathrm{H}_{2}(\mathrm{CN}) \mathrm{P}$ | 19.7 | $2.882 \quad 173$ | 12.0 | 3.071176 | 27.1 | 2.874167 |
| $\mathrm{H}_{2}(\mathrm{CCH}) \mathrm{P}$ | 17.0 | 3.009176 | 15.2 | 3.293172 | 25.2 | $3.021 \quad 170$ |
| $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}$ | 14.4 | $3.210 \quad 179$ | 20.9 | 4.013140 | 23.8 | 3.211172 |
| $\mathrm{H}_{3} \mathrm{P}$ | 13.1 | 3.189176 | 15.9 | 3.974145 | 20.1 | 3.211169 |

a) A is the atom of X that is directly bonded to P .


Fig. 2. Binding energies $(-\Delta \mathrm{E})$ versus the $\mathrm{P}-\mathrm{N}_{1}$ distance across the pnicogen bond for complexes of $\mathrm{H}_{2} \mathrm{XP}$ with $\mathrm{HNNH}, \mathrm{FNNH}$, and HNCHOH
energies of $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNNH}$ and $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNCHOH}$ complexes increase exponentially as the intermolecular $\mathrm{P}-\mathrm{N}_{1}$ distance decreases, with correlation coefficients of 0.977 and 0.944 , respectively. In contrast, the binding energies of the $\mathrm{H}_{2} \mathrm{XP}: \mathrm{FNNH}$ complexes show little dependence on the $\mathrm{P}-\mathrm{N}_{1}$ distance. Among the complexes with FNNH, $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}$ :FNNH and $\mathrm{H}_{3} \mathrm{P}$ :FNNH have the longest $\mathrm{P}-\mathrm{N}_{1}$ distances, but relatively large binding energies of 21 and 16 $\mathrm{kJ} \mathrm{mol}^{-1}$, respectively. In order to understand these relationships, it is necessary to examine the structures of these complexes and the charge-transfer interactions which contribute to their stabilization.

Complexes with HNNH. The molecule HNNH may act as an electron-pair donor to form a $\mathrm{P}^{\cdots} \mathrm{N}_{1}$ pnicogen bond, or a proton donor to form a $\mathrm{N}_{2}-\mathrm{H}_{2} \cdots \mathrm{P}$ hydrogen bond. That the binding energies of $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNNH}$ complexes correlate with the $\mathrm{P}-\mathrm{N}_{1}$ distance is a strong indication that the pnicogen bond is by far the dominant interaction stabilizing these complexes. The values of the $N_{1}-\mathrm{P}-\mathrm{A}$ angles which are reported in Table 1 vary from 173 to $179^{\circ}$, indicating that these three atoms approach a linear arrangement, as expected for complexes stabilized by pnicogen bonds. The question that remains is whether $\mathrm{N}_{2}-\mathrm{H}_{2} \cdots \mathrm{P}$ hydrogen bonds exist in these complexes, and if so, what role do they play in stabilization? Some insight into the answer to
this question may be found from the data of Table 2, which reports values of the $\mathrm{H}_{2}-\mathrm{N}_{2}-\mathrm{P}$ angles. These angles vary between 51 and $59^{\circ}$ for all complexes except $\mathrm{H}_{2}(\mathrm{CCH}) \mathrm{P}: \mathrm{HNNH}$, $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}: \mathrm{HNNH}$, and $\mathrm{H}_{3} \mathrm{P}: \mathrm{HNNH}$. Since binding energies of complexes with $\mathrm{X}-\mathrm{H} \cdots \mathrm{Y}$ hydrogen bonds decrease as the hydrogen bond becomes nonlinear, $\mathrm{H}-\mathrm{X}-\mathrm{Y}$ angles greater than about $30^{\circ}$ suggest that hydrogen bonds are very weak or essentially nonexistent in these complexes. As the substituent $X$ becomes more electropositive, the $\mathrm{H}_{2}-\mathrm{N}_{2}-\mathrm{P}$ angle decreases to 45,38 , and $40^{\circ}$ in $\mathrm{H}_{2}(\mathrm{CCH}) \mathrm{P}: \mathrm{HNNH}, \mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}: \mathrm{HNNH}$, and $\mathrm{H}_{3} \mathrm{P}: \mathrm{HNNH}$, respectively. The interaction between P and $\mathrm{H}_{2}-\mathrm{N}_{2}$ may have some significance, even though the hydrogen bond is still nonlinear and weak.

The charge-transfer interactions in complexes $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNNH}$ are depicted in Scheme 2. The charge-transfer energies which are reported in Table 3 are consistent with the description of the bonding in these complexes given above. In all complexes except $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}: \mathrm{HNNH}$, the dominant charge-transfer interaction occurs across the pnicogen bond from the nitrogen lone pair to the antibonding $\sigma^{*}$ P-A orbital. There is also a second much weaker charge-transfer interaction across the pnicogen bond, with electron donation from P to the $\sigma^{*} \mathrm{~N}_{1}-\mathrm{H}_{1}$ orbital. The third charge-transfer interaction occurs across the $\mathrm{N}_{2}-\mathrm{H}_{2} \cdots \mathrm{P}$ hydrogen bond. The $\mathrm{P}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{H}_{2}-\mathrm{N}_{2}$ charge-transfer energy is greatest in complexes $\mathrm{H}_{2}(\mathrm{CCH}) \mathrm{P}: \mathrm{HNNH}, \mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}: \mathrm{HNNH}$, and $\mathrm{H}_{3} \mathrm{P}: \mathrm{HNNH}$ which have the more electropositive subsituents. However, only in the $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}: \mathrm{HNNH}$ complex is the $\mathrm{P}_{1 \mathrm{p}} \rightarrow \sigma^{*} \mathrm{H}_{2}-\mathrm{N}_{2}$ charge-transfer energy greater than the $\mathrm{N}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{P}-\mathrm{A}$ energy, but it is still only $9 \mathrm{~kJ} \cdot \mathrm{~mol}^{-1}$.


Scheme 2. Representation of the charge-transfer interactions $\mathrm{P}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{H}_{2}-\mathrm{N}_{2}$ across the $\mathrm{N}_{2}-\mathrm{H}_{2} \cdots \mathrm{P}$ hydrogen bond and $\mathrm{N}_{1 \mathrm{p}} \rightarrow \sigma^{*} \mathrm{P}-\mathrm{A}$ and $\mathrm{P}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{~N}_{1}-\mathrm{H}_{1}$ across the $\mathrm{P}^{\cdots} \mathrm{N}$ pnicogen bond

The molecular graphs of the complexes illustrated in Fig. 1 and Fig. S1 of the Supporting Information exhibit a single intermolecular $\mathrm{P} \cdots \mathrm{N}$ BCP except in complexes with $\mathrm{X}=\mathrm{CCH}, \mathrm{CH}_{3}$ and H . For these, there is a second BCP associated with the $\mathrm{N}_{2}-\mathrm{H}_{2} \cdots \mathrm{P}$ hydrogen bonds. The electron densities at the $\mathrm{P} \cdots \mathrm{N}$ BCPs reported in Table S2 have values between 0.009 au for the $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}: \mathrm{HNNH}$ complex with the longest P-N distance, to 0.035 au for the $\mathrm{H}_{2} \mathrm{FP}: \mathrm{HNNH}$ complex which has the shortest P-N distance. The Laplacians are always positive, but the total energy densities are negative for the complexes with $\mathrm{X}=\mathrm{F}, \mathrm{Cl}, \mathrm{OH}$, and NC , which indicates that these $\mathrm{P}^{\cdots} \mathrm{N}$ bonds have some covalent character. For the three cases with a BCP associated with the $\mathrm{N}_{2}-\mathrm{H}_{2} \cdots \mathrm{P}$ hydrogen bonds, $\rho_{\mathrm{BCP}}$ values are 0.01 au and both the Laplacians and the energy densities are positive.

Table 2. The $\mathrm{Y}_{2}-\mathrm{P}$ and $\mathrm{H}_{2}-\mathrm{P}$ distances ( $\mathrm{R}, \AA$ ), and $\mathrm{H}_{2}-\mathrm{Y}_{2}-\mathrm{P}$ angles $\left(<,{ }^{\circ}\right)$ in complexes of $\mathrm{H}_{2} \mathrm{XP}$ with HNNH, FNNH, and $\mathrm{HNCHOH}^{\mathrm{a}}$
Molecule: HNNH FNNH HNCHOH

| $\mathrm{H}_{2} \mathrm{XP}=$ | $\mathrm{R}\left(\mathrm{N}_{2}-\mathrm{P}\right)<$ | $\mathrm{R}\left(\mathrm{H}_{2}-\mathrm{P}\right)$ | $\mathrm{R}\left(\mathrm{N}_{2}-\mathrm{P}\right)<$ | $\mathrm{R}\left(\mathrm{H}_{2}-\mathrm{P}\right)$ | $\mathrm{R}(\mathrm{O}-\mathrm{P})<$ | $\mathrm{R}\left(\mathrm{H}_{2}-\mathrm{P}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{H}_{2} \mathrm{FP}$ | 3.20459 | 2.809 | $3.475 \quad 57$ | 3.040 | $3.218 \quad 27$ | 2.386 |
| $\mathrm{H}_{2} \mathrm{ClP}$ | 3.29857 | 2.864 | 3.59957 | 3.165 | $3.332 \quad 28$ | 2.506 |
| $\mathrm{H}_{2}(\mathrm{NC}) \mathrm{P}$ | 3.29657 | 2.862 | 3.52651 | 2.988 | $3.282 \quad 26$ | 2.442 |
| $\mathrm{H}_{2}(\mathrm{OH}) \mathrm{P}$ | 3.32852 | 2.819 | 3.47342 | 2.799 | 3.27121 | 2.383 |
| $\mathrm{H}_{2}(\mathrm{CN}) \mathrm{P}$ | 3.42051 | 2.887 | 3.63250 | 3.070 | $3.432 \quad 23$ | 2.564 |
| $\mathrm{H}_{2}(\mathrm{CCH}) \mathrm{P}$ | 3.43245 | 2.804 | 3.53434 | 2.739 | $3.364 \quad 18$ | 2.451 |
| $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}$ | 3.47338 | 2.729 | 3.5590 | 2.520 | $3.321 \quad 12$ | 2.371 |
| $\mathrm{H}_{3} \mathrm{P}$ | 3.49240 | 2.776 | 3.615 5 | 2.586 | $3.377 \quad 13$ | 2.435 |

a) Y is $\mathrm{N}_{2}$ of HNNH and FNNH , and O bonded to $\mathrm{H}_{2}$ in HNCHOH.

Table 3. Charge-transfer energies $\left(\mathrm{kJ}^{-} \mathrm{mol}^{-1}\right)$ across pnicogen bonds and possible hydrogen bonds in complexes of $\mathrm{H}_{2} \mathrm{XP}$ with HNNH , FNNH , and HNCHOH

|  | $\mathrm{ZB}^{\text {a }}$ | $\mathrm{ZB}^{\text {b }}$ | $\mathrm{HB}^{\text {c }}$ |
| :---: | :---: | :---: | :---: |
| $\begin{aligned} & \mathrm{HNNH}: \mathrm{H}_{2} \mathrm{XP} \\ & \mathrm{H}_{2} \mathrm{XP}= \\ & \hline \end{aligned}$ | $\mathrm{N}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{P}-\mathrm{A}$ | $\mathrm{P}_{1 \mathrm{p}} \rightarrow \sigma^{*} \mathrm{~N}_{1}-\mathrm{H}_{1}$ | $\mathrm{P}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{H}_{2}-\mathrm{N}_{2}$ |
| $\mathrm{H}_{2} \mathrm{FP}$ | 58.3 | 8.4 | 4.3 |
| $\mathrm{H}_{2} \mathrm{ClP}$ | 45.1 | 5.4 | 3.1 |
| $\mathrm{H}_{2}(\mathrm{NC}) \mathrm{P}$ | 45.3 | 5.6 | 3.3 |
| $\mathrm{H}_{2}(\mathrm{OH}) \mathrm{P}$ | 28.3 | 4.6 | 4.7 |
| $\mathrm{H}_{2}(\mathrm{CN}) \mathrm{P}$ | 21.4 | 2.9 | 3.2 |
| $\mathrm{H}_{2}(\mathrm{CCH}) \mathrm{P}$ | 13.7 | 2.2 | 5.4 |
| $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}$ | 6.3 | 1.2 | 9.0 |
| $\mathrm{H}_{3} \mathrm{P}$ | 8.1 | 1.3 | 6.7 |
| $\begin{aligned} & \text { FNNH: } \mathrm{H}_{2} \mathrm{XP} \\ & \mathrm{H}_{2} \mathrm{XP}= \\ & \hline \end{aligned}$ | $\mathrm{N}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{P}-\mathrm{A}$ | $\mathrm{P}_{1 \mathrm{p}} \rightarrow \sigma^{*} \mathrm{~N}_{1}-\mathrm{F}$ | $\mathrm{P}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{H}_{2}-\mathrm{N}_{2}$ |
| $\mathrm{H}_{2} \mathrm{FP}$ | 24.0 | 5.9 | 2.2 |
| $\mathrm{H}_{2} \mathrm{ClP}$ | 15.5 | 3.5 | 2.7 |
| $\mathrm{H}_{2}(\mathrm{NC}) \mathrm{P}$ | 20.1 | 3.6 | 1.4 |
| $\mathrm{H}_{2}(\mathrm{OH}) \mathrm{P}$ | 9.2 | 2.7 | 7.7 |
| $\mathrm{H}_{2}(\mathrm{CN}) \mathrm{P}$ | 10.9 | 2.4 | 2.3 |
| $\mathrm{H}_{2}(\mathrm{CCH}) \mathrm{P}$ | 4.5 | 1.3 | 11.0 |
| $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}$ |  |  | 35.9 |
| $\mathrm{H}_{3} \mathrm{P}$ |  |  | 25.7 |
| $\begin{aligned} & \mathrm{HNCHOH}: \mathrm{H}_{2} \mathrm{XP} \\ & \mathrm{H}_{2} \mathrm{XP}= \end{aligned}$ | $\mathrm{N}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{P}-\mathrm{A}$ |  | $\mathrm{P}_{1 \mathrm{p}} \rightarrow \sigma^{*} \mathrm{H}_{2}-\mathrm{O}$ |
| $\mathrm{H}_{2} \mathrm{FP}$ | 65.6 |  | 38.9 |
| $\mathrm{H}_{2} \mathrm{ClP}$ | 56.7 |  | 26.9 |
| $\mathrm{H}_{2}(\mathrm{NC}) \mathrm{P}$ | 55.0 |  | 22.0 |
| $\mathrm{H}_{2}(\mathrm{OH}) \mathrm{P}$ | 29.8 |  | 43.8 |
| $\mathrm{H}_{2}(\mathrm{CN}) \mathrm{P}$ | 25.1 |  | 17.9 |
| $\mathrm{H}_{2}(\mathrm{CCH}) \mathrm{P}$ | 15.4 |  | 32.3 |
| $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}$ | 7.6 |  | 49.3 |
| $\mathrm{H}_{3} \mathrm{P}$ | 8.8 |  | 35.3 |

a) $\mathrm{N}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{P}-\mathrm{A}$ refers to charge transfer across the pnicogen bond from $\mathrm{N}_{1}$ to the antibonding P-A orbital of $\mathrm{H}_{2} \mathrm{XP}$, with A the atom of X directly bonded to P .
b) $\mathrm{P}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{~N}_{1}-\mathrm{H}_{1}$ and $\mathrm{P}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{~N}_{1}-\mathrm{F}$ refer to charge transfer across the pnicogen bond from P to the antibonding $\mathrm{N}_{1}-\mathrm{H}_{1}$ orbital of HNNH , and the antibonding $\mathrm{N}_{1}-\mathrm{F}$ orbital of FNNH.
c) $\mathrm{P}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{H}_{2}-\mathrm{N}_{2}$ and $\mathrm{P}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{H}_{2}-\mathrm{O}$ refer to charge transfer from P to the possible proton donor $\mathrm{N}_{2}-\mathrm{H}_{2}$ of HNNH and FNNH , and $\mathrm{O}-\mathrm{H}_{2}$ of HNCHOH .

Complexes with FNNH. The replacement of H by F makes FNNH a poorer electron-pair donor through $\mathrm{N}_{1}$ than HNNH for the $\mathrm{P}^{\cdots} \mathrm{N}$ pnicogen bond. This is evident from the reduced binding energies and the longer $\mathrm{P}-\mathrm{N}_{1}$ distances reported in Table 1 for complexes of FNNH with $\mathrm{H}_{2} \mathrm{XP}$ when X is one of the more electronegative substituents $\mathrm{F}, \mathrm{Cl}, \mathrm{NC}, \mathrm{OH}$, and CN . When X is one of the more electropositive groups, the bonding picture begins to change. Although the P-N distance of $3.293 \AA$ in $\mathrm{H}_{2}(\mathrm{CCH}) \mathrm{P}: \mathrm{FNNH}$ is longer than the distance of $3.009 \AA$ in $\mathrm{H}_{2}(\mathrm{CCH}) \mathrm{P}: \mathrm{HNNH}$, the binding energies of these two complexes are similar at 15 and $17 \mathrm{~kJ} \cdot \mathrm{~mol}^{-}$ ${ }^{1}$, which suggests that the $\mathrm{N}_{2}-\mathrm{H}_{2} \cdots \mathrm{P}$ hydrogen bond may have increased importance. This is also suggested by the reduced value of $34^{\circ}$ for the $\mathrm{H}_{2}-\mathrm{N}_{2}-\mathrm{P}$ angle, and the increase in the $\mathrm{P}-\mathrm{N}_{1}$ distance. This distance increases further to 4.013 and $3.974 \AA$ in $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}: \mathrm{FNNH}$ and $\mathrm{H}_{3} \mathrm{P}$ :FNNH, yet these two complexes have relatively large binding energies of 21 and $16 \mathrm{~kJ} \cdot \mathrm{~mol}^{-}$ ${ }^{1}$, respectively. There is no pnicogen bond in these two complexes, but rather $\mathrm{N}_{2}-\mathrm{H}_{2} \cdots \mathrm{P}$ hydrogen bonds, as illustrated in Fig. 3 for $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}: \mathrm{FNNH}$. In the $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}$ :FNNH and $\mathrm{H}_{3} \mathrm{P}$ :FNNH complexes, the $\mathrm{H}_{2}-\mathrm{P}$ distances are short and the hydrogen bonds are linear, with $\mathrm{H}_{2}-$ $\mathrm{N}_{2}-\mathrm{P}$ angles of 0 and $5^{0}$, respectively. It is not surprising that no correlation is seen in Fig. 2 between the binding energies of $\mathrm{H}_{2} \mathrm{XP}$ :FNNH complexes and the $\mathrm{P}-\mathrm{N}_{1}$ distance across the pnicogen bond.


Fig. 3. Molecular graph of $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}: \mathrm{FNNH}$ with a linear $\mathrm{N}_{2}-\mathrm{H}_{2} \cdots \mathrm{P}$ hydrogen bond.

That the pnicogen bond in the complexes with FNNH is weaker than the pnicogen bond in HNNH complexes can be inferred from the reduced values of the $\mathrm{N}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{P}-\mathrm{A}$ and $\mathrm{P}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{~N}-\mathrm{F}$ charge-transfer energies in the Table 3. Moreover, the large values of the $\mathrm{H}_{2}-\mathrm{N}_{2}-\mathrm{P}$ angles and the small $\mathrm{P}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{H}_{2}-\mathrm{N}_{2}$ charge-transfer energies are indicative of very weak $\mathrm{N}_{2}-\mathrm{H}_{2} \cdots \mathrm{P}$ interactions in complexes $\mathrm{H}_{2} \mathrm{XP}$ :FNNH when X is one of the more electronegative substituents. However, in the complex $\mathrm{H}_{2}(\mathrm{CCH}) \mathrm{P}: F N N H$, the $\mathrm{P}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{H}_{2}-\mathrm{N}_{2}$ charge-transfer energy increases to $11 \mathrm{~kJ}^{\text {Jmol }}{ }^{-}$
${ }^{1}$, which is greater than the charge-transfer energies across the pnicogen bond in this complex. These changes are even more pronounced in the complexes $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right)$ P:FNNH and $\mathrm{H}_{3}$ P:FNNH which have $P_{l p} \rightarrow \sigma^{*} H_{2}-N_{2}$ charge-transfer energies of 36 and $26 \mathrm{~kJ} \cdot \mathrm{~mol}^{-1}$, respectively, and $\mathrm{N}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{P}-\mathrm{A}$ and $\mathrm{P}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{~N}_{1}-\mathrm{F}$ charge-transfer energies which are less than $1{\mathrm{~kJ} \cdot \mathrm{~mol}^{-1} \text {. Thus, }}^{\text {. }}$ these latter two complexes are stabilized solely by $\mathrm{N}_{2}-\mathrm{H}_{2} \cdots \mathrm{P}$ hydrogen bonds.

The molecular graphs of these complexes are illustrated in Table S1 of the Supporting Information. These graphs exhibit only one BCP for the more electronegative X groups, except for the $\mathrm{H}_{2}(\mathrm{OH}) \mathrm{P}$ :FNNH which also has a BCP corresponding to the $\mathrm{N}_{2}-\mathrm{H}_{2} \cdots \mathrm{P}$ hydrogen bond. Complexes with the more electropositive groups $\mathrm{CCH}, \mathrm{CH}_{3}$ and H have only one BCP associated with the $\mathrm{N}_{2}-\mathrm{H}_{2} \cdots \mathrm{P}$ hydrogen bond. Electron densities at $\mathrm{P} \cdots \mathrm{N}$ BCPs are less than those of the corresponding $\mathrm{H}_{2} \mathrm{XP}$ :HNNH complexes. The values of $\nabla^{2} \rho_{\mathrm{BCP}}$ and $\mathrm{H}_{\mathrm{BCP}}$ are always positive. In contrast, electron densities at BCPs for the $\mathrm{N}_{2}-\mathrm{H}_{2} \cdots \mathrm{P}$ hydrogen bonds range from 0.01 to 0.02 au for the complexes with $\mathrm{X}=\mathrm{OH}, \mathrm{CCH}, \mathrm{CH}_{3}$, and H . The Laplacians and total energy densities are positive except for the complexes with $\mathrm{X}=\mathrm{H}$ and $\mathrm{CH}_{3}$, which have very small but negative values of the energy densities.

Complexes with HNCHOH. HNCHOH should have an electron-pair donating strength similar to that of HNNH , but it should also be a better proton donor through the O-H group. Table 1 shows that the binding energy of a given $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNCHOH}$ complex is at least $7{\mathrm{~kJ} \cdot \mathrm{~mol}^{-1} \text { greater }}^{\text {a }}$ than the binding energy of the corresponding complex with HNNH. Fig. 2 shows that the binding energies of $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNCHOH}$ complexes increase exponentially as the $\mathrm{P}-\mathrm{N}$ distance decreases, with a correlation coefficient of 0.944 . Moreover, at any given distance, the binding energy of an $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNCHOH}$ complex is greater than that of an $\mathrm{H}_{2} \mathrm{XP}$ : HNNH complex, which suggests that the $\mathrm{P}^{\cdots} \mathrm{N}$ pnicogen bond is also stronger. Nevertheless, part of the increase in the binding energies of HNCHOH complexes is due to the approach to linearity of the $\mathrm{O}-\mathrm{H}_{2} \cdots \mathrm{P}$ hydrogen bond, with $\mathrm{H}_{2}$-O-P angles between 12 and $28^{\circ}$. The structure of $\mathrm{H}_{2}(\mathrm{CN}) \mathrm{P}: \mathrm{HNCHOH}$ is illustrated in Fig. 4.


Fig. 4. Molecular graph of $\mathrm{H}_{2}(\mathrm{CN}) \mathrm{P}: \mathrm{HNCHOH}$ illustrating the $\mathrm{P}^{\cdots \cdots} \mathrm{N}$ pnicogen bond and the $\mathrm{O}-\mathrm{H}_{2}{ }^{\cdots} \mathrm{P}$ hydrogen bond

There is another factor which increases the stabilities of $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNCHOH}$ complexes, and that is the enhancement of the electron-donating and electron-accepting abilities of the phosphorus in these complexes. Donation of a lone pair by N to P to form the pnicogen bond makes P a better electron-pair donor to $\mathrm{O}-\mathrm{H}_{2}$ to form the hydrogen bond, while electron donation by P to $\mathrm{O}-\mathrm{H}_{2}$ makes P a better electron-pair acceptor for the pnicogen bond. This cooperativity is supported by the charge-transfer energies reported in Table 3. The $\mathrm{N}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{P}$-A chargetransfer energy in a given $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNCHOH}$ complex is always greater than it is in the corresponding $\mathrm{H}_{2} \mathrm{XP}: H N N H$ complex. Moreover, there is no back-donation from P to $\mathrm{N}_{1}-\mathrm{H}_{1}$ as these charge-transfer energies are less than $1 \mathrm{~kJ}^{J} \mathrm{~mol}^{-1}$. The increased strength of the hydrogen bond is indicated by the $\mathrm{P}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{H}_{2}$-O charge-transfer energies, which are significantly greater than the $\mathrm{P}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{H}_{2}-\mathrm{N}_{2}$ energies of corresponding $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNNH}$ and $\mathrm{H}_{2} \mathrm{XP}: F N N H$ complexes, even including $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}: \mathrm{FNNH}$ and $\mathrm{H}_{3} \mathrm{P}: F N N H$ which are stabilized solely by $\mathrm{N}_{2}-\mathrm{H}_{2} \cdots \mathrm{P}$ hydrogen bonds. In the three complexes $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNCHOH}$ with the more electronegative substituents, the $\mathrm{N}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{P}-\mathrm{A}$ charge-transfer energies are greater than the $\mathrm{P}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{H}_{2}-\mathrm{O}$ energies, while in the three complexes with the more electropositive substituents, the $\mathrm{P}_{\mathrm{lp}} \rightarrow \sigma^{*} \mathrm{H}_{2}-\mathrm{O}$ charge-transfer energies are greater.

The presence of two BCPs in the molecular graphs of these complexes illustrated in Table S1 is another indication that these complexes are stabilized by both pnicogen bonds and hydrogen bonds. The $\mathrm{P} \cdots \mathrm{N}$ bond properties at BCPs reported in Table S 3 for $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNCHOH}$ complexes are similar to those of the $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNNH}$ complexes, with $\rho_{\mathrm{BCP}}$ values between 0.010 and 0.034 au , positive values of $\nabla^{2} \rho_{\mathrm{BCP}}$, and negative $\mathrm{H}_{\mathrm{BCP}}$ for the complexes with $\mathrm{X}=\mathrm{F}, \mathrm{Cl}, \mathrm{NC}$ and OH which have the shorter P-N distances. The $\mathrm{O}-\mathrm{H}_{2} \cdots \mathrm{P}$ electron densities at BCPs are
greater than the BCP electron densities for $\mathrm{N}_{2}-\mathrm{H}_{2} \cdots \mathrm{P}$ hydrogen bonds. For the $\mathrm{O}-\mathrm{H}_{2} \cdots \mathrm{P}$ hydrogen bonds, $\nabla^{2} \rho_{\mathrm{BCP}}$ values are positive and $H_{\mathrm{BCP}}$ values are negative except for $\mathrm{H}_{2}(\mathrm{CN}) \mathrm{P}: \mathrm{HNCHOH}$ and $\mathrm{H}_{2}(\mathrm{NC}) \mathrm{P}: \mathrm{HNCHOH}$.

The electron densities at bond critical points correlate exponentially with the corresponding distances across pnicogen and hydrogen bonds, in agreement with previous studies. ${ }^{34,35,36,37,38,39,40,41,42}$ As observed previously, the Laplacians for $\mathrm{P}^{\cdots} \mathrm{N}$ pnicogen bonds tend to be positive for most interatomic distances, even for relatively short distances in bonds that have some covalent character. ${ }^{43,44,45}$ The variation of the energy densities with the P-N distance for $\mathrm{P}^{\cdots} \mathrm{N}$ pnicogen bonds is illustrated in Fig. S1. Fig. S2 illustrates the energy density variation with the $\mathrm{P}-\mathrm{H}_{2}$ distance for hydrogen bonds.

## Spin-Spin Coupling Constants

The PSO, DSO, FC, and SD components of the one-bond spin-spin coupling constants ${ }^{1 p} \mathrm{~J}\left(\mathrm{P}-\mathrm{N}_{1}\right)$ across the $\mathrm{P}^{\cdots} \mathrm{N}_{1}$ pnicogen bond are given in Table S 3 of the Supporting Information. The two-bond coupling constants across the hydrogen bond, ${ }^{2 h} \mathrm{~J}\left(\mathrm{~N}_{2}-\mathrm{P}\right)$ for $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right)$ P:FNNH and $\mathrm{H}_{3} \mathrm{P}: \mathrm{FNNH}$, and ${ }^{2 \mathrm{~h}} \mathrm{~J}(\mathrm{O}-\mathrm{P})$ for $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNCHOH}$, can be found in Table S 4 . $\mathrm{J}\left(\mathrm{N}_{2}-\mathrm{P}\right)$ values for complexes $\mathrm{H}_{2} \mathrm{XP}$ :HNNH and $\mathrm{H}_{2} \mathrm{XP}$ :FNNH are also given for comparison. The data of Tables S3 and S 4 indicate that the Fermi-contact terms are very good approximations to total J values.
Coupling constants ${ }^{1 \mathrm{p}} \mathbf{J}\left(\mathbf{P}-\mathbf{N}_{\mathbf{1}}\right)$ across pnicogen bonds. Table 4 presents values of the spin-spin coupling constants ${ }^{1 p} \mathrm{~J}\left(\mathrm{P}-\mathrm{N}_{1}\right)$ for coupling across the pnicogen bond. Excluding the complexes $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}$ : FNNH and $\mathrm{H}_{3} \mathrm{P}$ :FNNH which are not pnicogen bonded, ${ }^{1 \mathrm{p}} \mathrm{J}\left(\mathrm{P}-\mathrm{N}_{1}\right)$ is always negative, and ranges from -8 Hz in $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}: \mathrm{HNNH}$ to -59 Hz in $\mathrm{H}_{2} \mathrm{ClP}: \mathrm{HNCHOH}$. For a fixed $\mathrm{H}_{2} \mathrm{XP}$, the absolute values of these coupling constants decrease in the order

$$
\mathrm{HNCHOH}>\mathrm{HNNH}>\mathrm{FNNH}
$$

except for the complexes with $\mathrm{H}_{2} \mathrm{FP}$. Figure 5 presents plots of ${ }^{1 p} \mathrm{~J}\left(\mathrm{P}-\mathrm{N}_{1}\right)$ versus the $\mathrm{P}-\mathrm{N}_{1}$ distance for these complexes. The second-order trendlines have correlation coefficients of 0.968 , 0.968 , and 0.953 for complexes with HNNH, FNNH, and HNCHOH , respectively.

Table 4. Spin-spin coupling constants $(\mathrm{Hz})$ for complexes of $\mathrm{H}_{2} \mathrm{XP}$ with $\mathrm{HNNH}, \mathrm{FNNH}$, and HNCHOH
Molecule: HNNH FNNH HNCHOH HNNH FNNH HNCHOH

| $\mathrm{H}_{2} \mathrm{XP}$ | ${ }^{\mathrm{p}} \mathrm{J}\left(\mathrm{P}-\mathrm{N}_{1}\right)$ | ${ }^{\mathrm{p}} \mathrm{J}\left(\mathrm{P}-\mathrm{N}_{1}\right)$ | ${ }^{{ }^{1} \mathrm{p}} \mathrm{J}\left(\mathrm{P}-\mathrm{N}_{1}\right)$ | $\mathrm{J}\left(\mathrm{N}_{2}-\mathrm{P}\right)$ | $\mathrm{J}\left(\mathrm{N}_{2}-\mathrm{P}\right)$ | ${ }^{2 \mathrm{~h}} \mathrm{~J}(\mathrm{O}-\mathrm{P})$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{H}_{2} \mathrm{FP}$ | -55.8 | -57.9 | -52.3 | -5.6 | 0.4 | -17.9 |
| $\mathrm{H}_{2} \mathrm{ClP}$ | -55.9 | -41.9 | -58.5 | -4.5 | -0.1 | -11.2 |
| $\mathrm{H}_{2}(\mathrm{NC}) \mathrm{P}$ | -49.8 | -47.3 | -52.4 | -4.0 | 0.4 | -6.9 |
| $\mathrm{H}_{2}(\mathrm{OH}) \mathrm{P}$ | -37.1 | -21.6 | -39.3 | -5.0 | -2.5 | -19.1 |
| $\mathrm{H}_{2}(\mathrm{CN}) \mathrm{P}$ | -30.9 | -28.0 | -36.7 | -3.1 | 0.1 | -4.8 |
| $\mathrm{H}_{2}(\mathrm{CCH}) \mathrm{P}$ | -21.0 | -8.7 | -27.5 | -4.3 | -3.9 | -14.0 |
| $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}$ | -8.3 | 1.2 | -15.9 | -5.3 | $-18.0^{\mathrm{a}}$ | -23.8 |
| $\mathrm{H}_{3} \mathrm{P}$ | -10.2 | 1.6 | -16.8 | -4.1 | $-12.1^{\mathrm{a}}$ | -16.2 |

a) ${ }^{2 \mathrm{~h}} \mathrm{~J}\left(\mathrm{~N}_{2}-\mathrm{P}\right)$ values for coupling across the $\mathrm{N}_{2}-\mathrm{H}_{2} \cdots \mathrm{P}$ hydrogen bonds


Fig. 5. ${ }^{1 \mathrm{p}} \mathrm{J}\left(\mathrm{P}-\mathrm{N}_{1}\right)$ versus the $\mathrm{P}-\mathrm{N}_{1}$ distance for complexes of $\mathrm{H}_{2} \mathrm{XP}$ with HNNH , FNNH, and HNCHOH

Coupling Constants ${ }^{\mathbf{2 h}} \mathbf{J}\left(\mathbf{Y}_{\mathbf{2}}-\mathbf{P}\right)$ across Hydrogen Bonds. Coupling constants ${ }^{2 h} \mathrm{~J}(\mathrm{O}-\mathrm{P})$ across the $\mathrm{O}-\mathrm{H}_{2} \cdots \mathrm{P}$ hydrogen bonds in complexes $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNCHOH}$ are reported in Table 4. These range from -5 Hz in the complex with $\mathrm{H}_{2}(\mathrm{CN}) \mathrm{P}$ to -24 Hz in the complex with $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}$. Fig. S3 of the Supporting Information shows that the expected correlation between two-bond coupling constants across the hydrogen bond and the hydrogen bond distance is not found. There are two factors which undoubtedly influence the values of these coupling constants: the intermolecular O-P distance and the nonlinearity of the $\mathrm{H}_{2}-\mathrm{O}-\mathrm{P}$ hydrogen bond. Figure S 3 indicates that $\mathrm{H}_{2} \mathrm{FP}: \mathrm{HNCHOH}$ and $\mathrm{H}_{2}(\mathrm{OH}) \mathrm{P}: \mathrm{HNCHOH}$ have the two shortest O-P distances, and
they do have absolute values of ${ }^{2 \mathrm{~h}} \mathrm{~J}(\mathrm{O}-\mathrm{P})$ that are greater than the remaining complexes, except for $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}: \mathrm{HNCHOH}$. This latter complex has an intermediate O-P distance, but a hydrogen bond that is linear. The fourth complex in the list of decreasing ${ }^{2 h} J(O-P)$ is $H_{3} \mathrm{P}: \mathrm{HNCHOH}$, which has the next to longest $\mathrm{O}-\mathrm{P}$ distance, but an H-O-P angle similar to that of $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}: \mathrm{HNCHOH}$.

As noted above, $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}$ : FNNH and $\mathrm{H}_{3} \mathrm{P}$ :FNNH are stabilized solely by essentially linear $\mathrm{N}_{2}-\mathrm{H}_{2} \cdots \mathrm{P}$ hydrogen bonds. ${ }^{2 \mathrm{~h}} \mathrm{~J}\left(\mathrm{~N}_{2}-\mathrm{P}\right)$ values for these two complexes are -18 and -12 Hz at $\mathrm{N}_{2}-\mathrm{P}$ distances of 3.559 and $3.615 \AA$, respectively. The remaining complexes in this series have absolute values of $\mathrm{J}\left(\mathrm{N}_{2}-\mathrm{P}\right)$ which are less than 4 Hz . Values of coupling constants $\mathrm{J}\left(\mathrm{N}_{2}-\mathrm{P}\right)$ vary between -3 and -6 Hz for complexes $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNNH}$, and also show no correlation with the $\mathrm{N}_{2}-\mathrm{P}$ distance.

## CONCLUSIONS

Ab initio MP2/aug'-cc-pVTZ calculations have been carried to investigate the properties of complexes formed between $\mathrm{H}_{2} \mathrm{XP}$, for $\mathrm{X}=\mathrm{F}, \mathrm{Cl}, \mathrm{NC}, \mathrm{OH}, \mathrm{CN}, \mathrm{CCH}, \mathrm{CH}_{3}$, and H , and the molecules HNNH, FNNH, and HNCHOH. These molecules can potentially act as both electronpair donors to P to form pnicogen bonds, and electron-pair acceptors to form hydrogen bonds, thereby bridging the $\sigma$-hole and the lone pair of electrons at P . The results of these calculations support the following statements.

1. Complexes with HNNH and FNNH are stabilized by $\mathrm{P}^{\cdots} \mathrm{N}_{1}$ pnicogen bonds, except for $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}:$ FNNH and $\mathrm{H}_{3} \mathrm{P}$ :FNNH which are stabilized solely by $\mathrm{N}_{2}-\mathrm{H}_{2} \cdots \mathrm{P}$ hydrogen bonds. In the $\mathrm{H}_{2}(\mathrm{CCH}) \mathrm{P}: \mathrm{FNNH}$ complex, the hydrogen bond makes a small contribution to stability. Complexes with HNCHOH are stabilized by $\mathrm{P}^{\cdots} \mathrm{N}$ pnicogen bonds and nonlinear $\mathrm{O}-\mathrm{H}^{\cdots} \mathrm{P}$ hydrogen bonds. Thus, HNCHOH can bridge the $\sigma$-hole and the lone pair at P .
2. For a fixed base, binding energies of complexes decrease in the order $\mathrm{HNCHOH}>\mathrm{HNNH}>$ FNNH, except for the binding energies of $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}$ and $\mathrm{H}_{3} \mathrm{P}$ with HNNH and FNNH. Binding energies of complexes with HNCHOH and HNNH increase as the $\mathrm{P}-\mathrm{N}_{1}$ distance decreases, but binding energies of complexes with FNNH show little dependence on this distance.
3. The large binding energies of the complexes $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNCHOH}$ are due to a cooperative effect involving the bonding at P . Electron-pair donation by N to P across the pnicogen bond makes
the P atom a better electron-pair donor for hydrogen bonding, while electron-donation by P across the hydrogen bond makes P a better electron-pair acceptor for pnicogen bonding.
4. Consistent with the dominant role of the pnicogen bond in stabilizing these complexes, the dominant charge-transfer interaction involves electron-pair donation by N across the pnicogen bond to the antibonding $\mathrm{P}-\mathrm{A}$ orbital of $\mathrm{H}_{2} \mathrm{XP}$, with A the atom of X directly bonded to P . The only exceptions are found for $\mathrm{H}_{2}\left(\mathrm{CH}_{3}\right) \mathrm{P}: \mathrm{HNNH}$ and the complexes $\mathrm{H}_{2} \mathrm{XP}$ :FNNH and $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNCHOH}$ with the more electropositive substituents $\mathrm{CCH}, \mathrm{CH}_{3}$, and H . The dominant charge-transfer interaction for these is lone-pair donation by P across the hydrogen bond.
5. The molecular graphs for complexes show the existence of pnicogen bonds and hydrogen bonds. Values of electron densities at bond critical points correlate with the corresponding bond distances. Energy densities illustrate that the $\mathrm{P}^{\cdots} \mathrm{N}$ bonds in some of these complexes have partial covalent character.
6. EOM-CCSD spin-spin coupling constants ${ }^{1 \mathrm{p}} \mathrm{J}(\mathrm{P}-\mathrm{N})$ across the pnicogen bond for each series of complexes correlate with the $\mathrm{P}-\mathrm{N}$ distances. In contrast, ${ }^{2 h} \mathrm{~J}(\mathrm{O}-\mathrm{P})$ values across the $\mathrm{O}-\mathrm{H}^{\cdots} \mathrm{P}$ hydrogen bond for complexes $\mathrm{H}_{2} \mathrm{XP}: \mathrm{HNCHOH}$ do not correlate with the O-P distance, most probably due to the nonlinearity of these bonds.

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