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## ARTICLE TYPE

# First-principles study of the sodium adsorption and diffusion on phosphorene

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The structural, electronic, electrochemical as well as the diffusion properties of Na doped phosphorene have been investigated based on first-principles calculations. The strong binding energy between Na and phosphorene indicates that Na could be stabilized on the surface of phosphorene without clustering. By cooperating the Na atoms adsorption on one-side and both-sides of phosphorene, it is found the Na-Na

<sup>10</sup> exhibits strongly repulsion with the Na-Na distance less than 4.35 Å. The Na intercalation capacity is estimated to be 324 mAh/g and the calculated discharge curve indicates quite low Na<sup>+</sup>/Na voltage of phosphorene. Moreover, the diffusion energy barrier of Na atoms on phosphorene surface in both low and high Na concentrations are as low as 40~63 meV, which implies high mobility of Na during the charge/discharge process.

#### 15 1. Introduction

Rechargeable solid-state batteries have joined in our daily life and been widely applied in portable electronics, electrical vehicles, and miscellaneous power devices.<sup>1-4</sup> Due to the abundance of sodium (Na) and low redox potential (-

- <sup>20</sup> 2.71 V vs. standard hydrogen electrode),<sup>5,6</sup> sodium-ion batteries (SIBs) have attracted much attention to relieve the urgent need of Li-ion batteries (LIBs), especially for largescale energy storage. As a key component of SIBs, the anode materials are desired to be of high Na capacity, low
- <sup>25</sup> redox potential, high electronic conductivity, high-rate Na diffusivity and robustly structural stability.<sup>7</sup> Graphite, the commercial anode material for LIBs, is no more appropriate to encapsulate the Na effectively, due to the weak interaction between Na and the graphene plane, which affects the
- <sup>30</sup> electrochemical perfermance.<sup>8-10</sup> Other carbon-based structures (hard carbon, porous carbon), as well as porous and layered oxide materials (TiO<sub>2</sub>, K<sub>0.8</sub>Ti<sub>1.73</sub>Li<sub>0.27</sub>O<sub>4</sub>, Na<sub>2</sub>Ti<sub>3</sub>O<sub>7</sub>),<sup>11-16</sup> are developed for SIB anode. However, the Na specific capacity of these materials is limited to 200
- <sup>35</sup> mAh/g. With high surface area and structural flexibility, two-dimensional (2D) material graphene is expected to be advantageous in SIB anodes. Although theoretical study implies that the binding between Na and pristine graphene is too weak for Na storage comparing with the cohesive energy
- <sup>40</sup> of bulk Na, Datta *et al.* reveal that introducing defects in graphene could enhance the binding between Na and graphene and predict an enormous capacity (1450 mAh/g) in case of high defects concentration.<sup>17</sup> Another theoretical work indicates that heteroatoms B doping into graphene
- <sup>45</sup> could boost the Na storage capacity to 762 mAh/g.<sup>18</sup> David *et al.* have experimentally fabricated the reduced graphene oxide (rGO) paper electrode, which exhibits the maximum

sodium charge capacity of ~140 mAh/g at 100mA/g.<sup>19</sup> Another monolayer structure MoS<sub>2</sub>, is investigated as <sup>50</sup> potential candidate of SIB anode and the Na specific capacity is predicted to achieve as high as 335 mAh/g, which is larger than that of bulk MoS<sub>2</sub>.<sup>20,21</sup> Self-standing flexible electrode composed of few-layer MoS<sub>2</sub> and rGO flakes is prepared and shows a stable charge capacity of ~230 mAh/g <sup>55</sup> with good Na cycling ability.<sup>22</sup> However, the inferior carrier mobility of the monolayer MoS<sub>2</sub> limits its further application in SIB anode.

Elemental phosphorus (P) can form Na<sub>3</sub>P compounds with a theoretical capacity of around 2600 mAh/g<sup>23</sup> and has attracted a 60 lot of attentions from science community. Kim et al. have fabricated the red phosphorus/carbon composite which exhibits exceptional high Na storage capacity of about 1800 mAh/g.24-27 However, the over-all performance of these materials is still unsatisfactory mainly due to the low rate capacity which may be 65 attributed to the low electronic conductivity and large volumetric expansion of red phosphorus. Recently, phosphorene, 2D monolayer black phosphorus, has been succeeded prepared by mechanical exfoliation method and exhibits promising electronic properties and high carrier mobility,28-30 which has been studied 70 intensively for its potential application in electronics, optoelectronics, solar cell, photocatalyst and so on.<sup>31-35</sup> Kulish et al. have investigated the adsorption of a series of metal atoms (Li, Na, K, Cu etc.) on phosphorene. They reported that the binding energy of alkali metal atoms to phosphorene is stronger than the 75 cohesive energy of bulk structure, which implies the application of phosphorene on Li and Na storage.<sup>36</sup> A further theoretical study explores the Li doping properties on phosphorene<sup>37</sup> and predicts the Li capacity on monolayer phosphorene can reach 432 mAh/g, which is higher than that of commercial graphite 80 materials. However, the Li diffusion barrier on phosphorene is as high as 0.76 eV, which may cause an inferior rate capacity when

phosphorene is used as LIB anode. Since it is reported that Na ions are faster than Li ions diffusing in the layered structures,<sup>38,39</sup> phosphorene is expected to be more suitable to be used as the SIB anode. Up to now, the Na doping properties on phosphorene are s still open and the evaluation of phosphorene as the SIB anode

should be of great interest. In this work, we have systemically studied the structural, electronic, electrochemical as well as the diffusion properties of Na doped phosphorene based on first-principles calculations.

- <sup>10</sup> Our results show that the phosphorene is able to accommodate the Na atoms. The calculated band structures and density of states (DOS) suggest that the adsorption of Na can enhance the electronic conductivity of phosphorene. Na atoms adsorbed on one-side and both-side of phosphorene are systematically studied.
- <sup>15</sup> It is found that the Na-Na interaction closely relates to the distance between Na atoms. A critical distance of about 4.35 Å for strong Na-Na repulsion is identified and the Na specific capacity can be estimated to be 324 mAh/g by a close packing of Na on the surface of phosphorene. The Na<sup>+</sup>/Na discharge curve
- <sup>20</sup> related to the Na concentrations on phosphorene is simulated and several low and mild voltage plateaus are observed, which means a stead and high work voltage can be achieved when phosphorene is used as SIB anode. The diffusion barriers of Na atoms on phosphorene in both low and high Na concentrations are reported
- <sup>25</sup> as 40~63 meV, which implies that it may possess outstanding rate capacity during charge/discharge process. Our calculations provide a comprehensive understanding of the interaction between Na and phosphorene.

#### 2. Computational models and methods

- All calculations are performed within density functional theory  $(DFT)^{40,41}$  framework by using the projector-augmented-wave  $(PAW)^{42}$  method, as implemented in the Vienna *ab initio* simulation package (VASP)^{43-45}. The exchange and correlation energy was treated by generalized gradient approximation (GGA)
- <sup>35</sup> with Perdew-Burke-Ernzerhof (PBE)<sup>46</sup> form. An energy cutoff of 400 eV is employed on the plane wave basis. The geometry optimization is performed till the Hellmann-Feynman force on each atom is smaller than 0.05 eV/Å. We adopt a 3  $\times$  4 phosphorene supercell of 13.89 Å  $\times$  13.20 Å with a vacuum
- <sup>40</sup> thickness of 15 Å to avoid the interaction between images slabs. The numerical integration in the first Brillouin zone is performed using a Monkhorst-Pack<sup>47</sup> grid of  $5 \times 5 \times 1$ . To check the convergence, we have compared the total energy to the ones calculated with finer *k*-mesh and find the difference of total <sup>45</sup> energy is smaller than 1 meV. A climbing image nudged elastic
- band (CI-NEB)<sup>48</sup> calculation is used to calculate the minimum energy path (MEP) of Na migration on phosphorene and to find the saddle point between two local minima for the system. Eight intermediate images are used for all CI-NEB calculations, which <sup>50</sup> can map the MEP with reasonable accuracy.

#### 3. Results and discussion

As shown in Fig. 1(a), different from pristine graphene, phosphorene is puckered with four P atoms in a unit cell (the red dash framework). The optimized lattice constants are 4.63 Å in x ss axis and 3.30 Å in y axis, which are in good agreement with

previous studies.<sup>49,50</sup> The calculated P-P distances and  $\angle$ P-P-P angles in (P<sub>A</sub>-P<sub>B</sub>,  $\angle$ P<sub>E</sub>P<sub>A</sub>P<sub>B</sub>) and out (P<sub>B</sub>-P<sub>C</sub>,  $\angle$ P<sub>B</sub>P<sub>C</sub>P<sub>D</sub>) of the plane are 2.22 Å, 96.0° and 2.26 Å, 104.2°, respectively. Moreover, the first Brillouin zone and symmetric *k* points of the <sup>60</sup> phosphorene supercell cell have also been presented in Fig. 1(a). According to the symmetry of phosphorene, there are four inequivalent sites for Na doping in the unit cell on one-side of phosphorene, which are labelled as *T* (on top of a P atom), *B* (on top of a P-P bond), *Br* (above the bridge site of two neighboring <sup>65</sup> unbonded P atoms) in Fig. 1(a). Table 1 summarizes the calculated binding energies (*E*<sub>b</sub>), the optimized bond lengths between Na and the nearest P (d<sub>Na-P</sub>) and the charge transfer of adsorbed Na atom ( $\Delta$ Q). The *E*<sub>b</sub> is defined as:

 $_{0} \qquad E_{b} = E_{phosphorene+Na} - E_{phosphorene} - nE_{Na,bcc} \qquad (1)$ 

where,  $E_{phosphorene+Na}$ ,  $E_{phosphorene}$  and  $E_{Na,bcc}$  are the total energies of Na-adsorbed phosphorene, pristine phosphorene and single Na atom in bulk structure (bcc), respectively. Therefore, the more negative of E<sub>b</sub> means the stronger adsorption of Na on <sup>75</sup> phosphorene compared with bulk structure. Note that the d<sub>Na-P</sub> in all cases are about 2.80 Å, similar to previous reported distance of Na adsorbed on graphene and MoS<sub>2</sub>.<sup>20,51</sup> Among the four adsorption sites, the H site is the most favorable for Na with the  $E_{\rm b}$  of -0.28 eV and the optimized structure of Na adsorbed on H so site is presented in Fig. 1(b) (the other three adsorption configurations are presented in Fig. S1 in supporting information (SI)). The distances between the adsorbed Na atom and the nearest P atoms are 2.83 Å (d<sub>1</sub>) and 2.92 Å (d<sub>2</sub>), respectively. The negative binding energies of Na onto the H and Br sites 85 reveal that Na atoms prefer to reside on the surface of phosphorene instead of clustering, suggesting that the phosphorene would be superior than graphene when used as SIB anode.<sup>17,18</sup> The charge transfer between the Na atom and the phosphorene,  $\Delta Q$ , is described by Bader charge analysis.<sup>52</sup> The 90 results in Table 1 show that the Na atoms adsorbed on H and Br site involve the larger charge transfer to phosphorene, which would be responsible for the stronger binding energy.



**Fig.1** Top-view and side-view of (a) possible doping sites on pristine <sup>95</sup> phosphorene, (b) single Na atom adsorbed on *H*-site of phosphorene. The phosphorus atoms in upper and bottom layers are highlighted by dark and light gray, respectively. The red dash square denotes the unit cell of phosphorene.

**Table 1.** Calculated binding energies ( $E_b$ ), distances between Na and the nearest P of the optimized structures ( $d_{Na-P}$ ) and the charge transfer of adsorbed Na atoms ( $\Delta Q$ ).

	В	Br	Н	Т
$E_{\rm b}({\rm eV})$	0.07	-0.24	-0.28	0.11
d <sub>Na-P</sub> (Å)	2.85	2.80	2.83	2.73
$\Delta Q( e )$	0.81	0.83	0.83	0.80

Since the 2D monolayer phosphorene exhibits two sides of surfaces, we further explore the Na-Na interaction in the cases of one-side and both-side adsorptions on phosphorene. Fig. 2(a)-(d) illustrate that two Na atoms adsorbed on the same side, while (e)-(h) depict the two Na atoms adsorbed on the opposite sides <sup>10</sup> individually. In each case, we have calculated  $E_{\rm b}$  with different Na-Na distances. The optimized configurations (d<sub>Na-Na</sub>), average binding energies ( $\langle E_b \rangle$ ) as well as average charge transfer ( $\langle \Delta Q \rangle$ ) per adsorbed Na atom are summarized in Fig. 2 and Table 2. To get a clear view of the binding energy and charge transfer to the 15 Na-Na distance, they are plotted in Fig. 3(a) with the left and right parts denoting two Na atoms adsorbed on one-side and bothside of phosphorene. We notice the overall average binding energy per Na atom is slightly weaker than that of single adsorbed Na atom (red dash line) due to the Na-Na repulsion. In <sup>20</sup> addition,  $\langle E_b \rangle$  for both-side adsorption is stronger than that of

one-side due to the weaker repulsion between the Na atoms in a larger distance. The important feature of Fig. 3(a) is that  $\langle E_b \rangle$  of

one-side adsorption increases sharply when d<sub>Na-Na</sub> is shorter than 4.35 Å, which indicates the repulsion between neighboring Na atoms becomes drastically strong within the critical distance. It is interesting that the average charge transfer between Na and phosphorene follows a reverse trend with the binding energy, which is reasonable since the binding strength is mainly determined by the electronic interaction between them. It seems an exception for both-side adsorption that shorter Na-Na distance (6.4 Å) yields a lower binding energy, which is probably attributed to the screening effect of the phosphorene towards the Na-Na repulsion.

**Table 2.** Calculated distances between Na atoms of the optimized <sup>35</sup> structures ( $d_{Na-Na}$ ) average binding energies ( $< E_b >$ ), and average the charge transfer ( $< \Delta Q >$ ) of adsorbed Na atoms.

	d <sub>Na-Na</sub> (Å)	$< E_b > (eV)$	$<\Delta Q>( e )$
One-side adsorption	3.86	-0.15	0.74
	4.35	-0.22	0.78
	4.64	-0.23	0.79
	5.72	-0.23	0.81
Both-side	6.74	-0.29	0.80
	6.84	-0.28	0.80
adsorption	7.17	-0.26	0.81
	8.18	-0.25	0.82



Fig.2 Top-view and side-view of two Na atoms adsorbed on (a)-(d) one-side and (e)-(h) both-side of phosphorene with different neighboring Na-Na distances.

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**Fig.3** (a) Average binding energies ( $\langle E_b \rangle$ ) and charge transfer ( $\langle \Delta Q \rangle$ ) of two Na atoms adsorbed on phosphorene as a function of the Na-Na distance. The black and red dash lines represent the  $\Delta Q$  and  $E_b$  of one Na <sup>5</sup> adsorbed on phosphorene, respectively. (b) and (c) are the top and side views of the isosurface of the differential charge density of the structures shown in Fig. 2(d) and 2(e) with the increment level of  $0.001a_0^{-3}$ , where  $a_0$  is the Bohr radius. The yellow and the grey-blue represent the positive and negative charge, respectively. (d) and (e) are corresponding contours <sup>10</sup> of the differential charge density in side-views.

Fig. 3(b) and (c) show the isosurface of differential charge density ( $\Delta \rho$ ) of two Na atoms on phosphorene with one-side (Fig. 2(d)) and both-side (Fig. 2(e)) adsorption, respectively. The  $\Delta \rho$  is defined as:

$$5 \qquad \Delta \rho = \rho_{phosphorene+2Na} - \rho_{phosphorene} - \rho_{Na-Na} \tag{2}$$

where  $\rho_{phosphorene+2Na}$ ,  $\rho_{phosphorene}$  and  $\rho_{Na-Na}$  are the charge densities of phosphorene with two adsorbed Na atoms, pristine phosphorene and an isolated Na dimer, respectively. There is obvious charge aggregation near the three nearest P atoms and

- <sup>20</sup> charge dissipation around the Na-Na dimer, which indicates the formation of ion bonds between Na and phosphorene. The contours of  $\Delta \rho$  for the two cases are shown from side-views in Fig. 3(d) and (e) to clarify this point. Since most charge of Na atoms are transferred to phosphorene, there should be repulsive
- <sup>25</sup> interaction between the two Na ions in such a short distance. For the both-side adsorption, the negative charged phosphorene locates between the two Na ions and thus has a more effective screening effect compared to the case of one-side adsorption, where no screening medium exists between the two Na ions.
- The band structure and density of states (DOS) have been calculated to investigate the electronic properties of phosphorene

by Na intercalation. The band structure and DOS of the pristine phosphorene are shown in Fig. 4(a) and it exhibits semiconducting behavior with a direct band gap of 0.94 eV, <sup>35</sup> which agrees with the results of previous study.<sup>29</sup> Upon one Na atom doping, the change of the band structure follows a rigid band picture and the Fermi level upshift to cross the conductive band of phosphorene in Fig. 4(b), which implies a metallic behavior for the doped phosphorene. The partial density of state 40 (PDOS) of Na atoms shows that the 2s electron of Na contributes the DOS near the Fermi level. The injection of 2s electron from the Na atom into the conduction bands of phospherene pushes the Fermi level upward, which corresponds to the charge transfer as mentioned above. Fig. 4(c) shows the band structure and DOS of <sup>45</sup> two Na atoms doped phosphorene with both-side adsorption. The change is similar with that of one Na atom adsorption. Additionally, the energy gap between the original conduction band minimum and valence band maximum of phosphorene decreases upon Na atoms doping, which may be attributed to the 50 enhanced orbital hybridization between Na 2s and P 2p. Our band structure and DOS calculations indicate that the Na doping could promote the electronic conductivity of the phosphorene.

Since there are many equivalent *H* sites on both-side surface, it is expected that the phosphorene may exhibit high Na storage <sup>55</sup> capacity. Knowing the critical distance for Na-Na strong repulsion is about 4.35 Å as discussed above, one can roughly estimate the upper limit of Na capacity. In order to avoid the strong interaction between Na atoms, each Na atom should exclusively occupy in an area of 4.35 Å × 4.35 Å, where there <sup>60</sup> contains 4.95 P atoms. Thus the maximum Na concentration with both-side adsorption could reach Na<sub>2</sub>P<sub>4.95</sub>, corresponding to a theoretical capacity of 350 mAh/g since the capacity (*C*) can be calculate by:

$$C = \frac{\lambda F}{M_P} \tag{3}$$



**Fig.4** Band structure and DOS of (a) pristine, (b) one Na adsorbed, (c) two Na with both-side adsorbed and (d) 18 Na atoms adsorbed phosphorene. The total DOS, partial DOS (PDOS) of P and Na atoms are plotted with black, red and blue lines, respectively. Note that the PDOS 70 of Na atoms in (b) and (c) have been scaled up ten times.



**Fig.5** (a) Colorful symbols give the calculated Na binding energies of different configurations and constructed black line of convex hull indicates the ground states of phosphorene with different Na <sup>5</sup> concentrations. (b) The most stable configurations of Na-doped phosphorene with formula of Na<sub>18</sub>P<sub>48</sub>. (c) Corresponding voltage profile and the average distance between neighboring Na atoms as a function of Na uptake. The red dash line represents the estimated critical distance of Na-Na strong repulsion.

- <sup>10</sup> where  $\lambda$  is the atomic ratio of Na and P atoms, *F* is the Faraday constant (26.8 Ah/mol), and  $M_P$  is the atomic mass of P (31g/mol). On the other hand, we calculate the binding energies of Na doped phosphorene with different concentrations ranging from Na<sub>1</sub>P<sub>48</sub> to Na<sub>24</sub>P<sub>48</sub>. For each concentration, several <sup>15</sup> configurations (Fig. S2-S10 in SI) are considered to yield the most stable one. Fig. 5 shows all calculated binding energies and the hull line (the black solid line). The hull curve is a convex polyline within the whole range of the coverage, with its vertexes corresponding to all the true ground configurations of Na<sub>x</sub>P<sub>48</sub>. <sup>20</sup> The total binding energy initially decreases with the increasing
- <sup>20</sup> The total binding energy initially decreases with the increasing Na concentration and eventually saturates. Further Na intercalation would cause the weakening of the binding energy due to strong Na-Na repulsion. One should note that even with the highest Na stoichiometry  $Na_{24}P_{48}$ , in which all *H* site
- $_{25}$  occupied by Na atoms on both sides of phosphorene (Fig. S10 in SI), the binding energy still is negative. However, its binding energy is about 0.41 eV less stable than the lowest point with formula of Na<sub>18</sub>P<sub>48</sub> in Fig. 5(a) and the corresponding most stable configuration is shown in Fig. 5(b). Thus the largest Na

<sup>30</sup> concentration corresponds to a capacity of 324 mAh/g, which agrees well with our above estimation. We further plot the band structure and DOS of  $Na_{18}P_{48}$  in Fig. 4(d) and find the multiple Na atoms doping would increase the DOS of phosphorene near the Fermi level. The structural stability of the  $p(2\times2)$  supercell of <sup>35</sup>  $Na_{18}P_{48}$  has also been considered during the charge/discharge processes by *ab initio* molecule dynamics simulation and the results show that the whole structure of phosphorene could be well-retained except for few atoms undergoing conversion-type reaction in some local region (Fig. S12 in SI). Moreover, the <sup>40</sup> simulated result of fully discharged phosphorene with Na atoms removed can self-repair and be well recovered to the initial structure (Fig. S13 in SI).

The electrochemical properties of the phosphorene as SIB anode are investigated by Faraday laws. The discharge process <sup>45</sup> can be described as Eq.(4), in which  $\Delta x$  indicates the number of intercalated Na atoms in each step:

 $Na_x P_{48} + \Delta x Na \rightarrow Na_{x+\Delta x} P_{48}$  (4)

The voltage given by Faraday laws is:

$$V(x) = \frac{-\Delta G}{e\Delta x} \tag{5}$$

50 where  $\Delta G$  is the change of Gibbs free energy, which consists of three parts:  $\Delta G = \Delta E + P \Delta V - T \Delta S$ . In a solid-state reaction,  $P\Delta V$  is in order of  $10^{-5}$  eV and  $T\Delta S$  is in order of the thermal energy (~0.026 eV). Thus  $\Delta G$  can be well-approximated by the change of total energies ( $\Delta E$ ) obtained directly from first-55 principles calculations.<sup>53</sup> As shown in Fig. 5(c), there are two visible voltage plateaus during the discharge process. The first plateau is short with the Na<sup>+</sup>/Na potential about 0.3 eV. The second one exhibits a relative low and wide range plateau, which implies a high and stable working voltage when used as SIB 60 anode. The red curve in Fig. 5(c) presents the average distances between neighboring Na atoms with different Na concentrations. According to the most thermodynamically stable structure of compound Na<sub>18</sub>P<sub>48</sub>, the critical distance for strong Na-Na repulsion should be about 4.3 Å and is in good agreement with 65 the result of two Na atoms adsorption.



**Fig.6** (a) and (c) are the possible diffusion paths and calculated minimum energy paths of Na on the surface of phosphorene for low Na concentrations, (b) and (d) are those diffusion paths and minimum energy paths for high Na concentrations.

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Na-ion diffusion is an important factor affecting the rate capability of the SIBs. We focus on Na-ion diffusion on one-side of phosphorene plane. Fig. 6(a) shows three possible diffusion paths for Na according to the structural symmetry. Path 1

- s illustrates the Na migrating along the zigzag channel in y direction. In paths 2, Na-ion will cross over a protruding P-P bond to the neighboring channel norm to the y axis. Path 3 indicates a Na-ion migration over a protruding P atom to the neighboring channel aside path 2. The corresponding MEPs of
- <sup>10</sup> Na diffusion in these three paths are shown in Fig. 6(c). Clearly, path 1 has the lowest energy barrier of 41 meV, only 1/8 and 1/10that of path 2 and path 3. This indicates that Na ions mainly diffuse along in *y* direction. When the Na ion migrates between different channels, it would preferentially adopt path 2 by
- <sup>15</sup> climbing over a P-P bond instead of a P atom since the latter exhibits a 50 meV higher energy barrier. The Na diffusion in high concentrations has also been considered. We chose the highest doping concentration  $Na_{18}P_{48}$  as example and employ the model of  $Na_{17}P_{48}$  where a Na vacancy is created to investigate the
- <sup>20</sup> neighboring Na atoms migration. Two paths of Na diffusion along and across the channel are depicted as path 4 and path 5 in Fig. 6(b). The corresponding MEPs are calculated by CI-NEB and plotted in Fig. 6(d). The energy barriers for the two paths are also extremely low with barriers of 33 meV and 62 meV,
- <sup>25</sup> respectively. It is interesting that the energy barrier of Na diffusion along path 5 is about half of that in path 1 when the Na atom migrates to another channel, which indicates the Na-Na repulsion benefits the Na diffusion in closely aligned patterns. We note that the Na diffusion barriers in both low and high
- <sup>30</sup> concentrations are less than 70 meV, which is much lower than that of Li on phosphorene and Na on other reported 2D materials.<sup>18,20,37,54</sup>

#### 4. Conclusions

- Based on first-principles calculations, we have systemically <sup>35</sup> studied the adsorption and diffusion behaviors of Na on phosphorene. Our results indicate that phosphorene is able to accommodate the Na storage. By investigating the Na-Na interaction on phosphorene, a critical Na-Na repulsion distance is found and the Na intercalation capacity can be estimated to be
- <sup>40</sup> 324 mAh/g. The calculated discharge curve of Na<sup>+</sup>/Na reveals that phosphorene exhibits a stable voltage profile within a wide range. The diffusion energy barrier of Na on phosphorene is extremely low (~40 meV), which implies the phosphorene may exhibit outstanding rate capacity when used as SIB anode.

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#### Notes and references

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The structural, electronic, electrochemical as well as the diffusive properties of Na doped phosphorene have been investigated, which indicates the phosphorene could be a promising sodium-ion battery anode based on first-principles study. 676x509mm (96 x 96 DPI)