

PCCP

Accepted Manuscript



This is an *Accepted Manuscript*, which has been through the Royal Society of Chemistry peer review process and has been accepted for publication.

Accepted Manuscripts are published online shortly after acceptance, before technical editing, formatting and proof reading. Using this free service, authors can make their results available to the community, in citable form, before we publish the edited article. We will replace this *Accepted Manuscript* with the edited and formatted *Advance Article* as soon as it is available.

You can find more information about *Accepted Manuscripts* in the [Information for Authors](#).

Please note that technical editing may introduce minor changes to the text and/or graphics, which may alter content. The journal's standard [Terms & Conditions](#) and the [Ethical guidelines](#) still apply. In no event shall the Royal Society of Chemistry be held responsible for any errors or omissions in this *Accepted Manuscript* or any consequences arising from the use of any information it contains.

Nuclear quantum tunnelling in enzymatic reactions – an enzymologist's perspective

Linus O. Johannissen, Sam Hay* & Nigel S. Scrutton*

SYNBIOCHEM, Manchester Institute of Biotechnology, Faculty of Life Sciences, The University of Manchester, Manchester M1 7DN

* Correspondence to Sam Hay or Nigel Scrutton

Abstract. Enzyme-catalysed H-transfer are ubiquitous, yet fundamental details of these reactions remain unresolved. In this perspective, we discuss the roles of nuclear quantum tunnelling and (compressive) dynamics during these reactions. Evidence for the coupling of specific substrate and/or protein vibrations to the chemical coordinate is considered and a case is made for the combination of multiple experimental and computational / theoretical approaches when studying these reactions.

1. Introduction. The ability to design and control enzymatic reactions is essential as synthetic biology and industrial biotechnology becomes increasingly important for the production of sustainable fuels, pharmaceuticals and other chemicals.¹⁻³ A thorough understanding of enzyme catalysis is therefore of paramount importance, yet after over a century of research, since the first enzyme lock-and-key model,⁴ the importance of certain fundamental principles remain unresolved. While it is well established that electrostatic stabilisation of the transition state is of key importance for rapid biochemical reactions,⁵⁻⁷ the roles of dynamics and nuclear quantum tunnelling (NQT) are more contentious. Since the first experimental evidence of NQT in an enzyme-catalysed reaction⁸ there have been a plethora of publications arguing both for and against the relative importance of this effect.⁹⁻²⁵ Much of the discussion has arisen from the experimental characterisation of enzymatic H-transfer reactions (where H = hydride, hydrogen atom or proton), which exhibit a wide range of (kinetic) isotope effects (KIEs) on observed and/or intrinsic rate constants and steady state velocities, as well as on key thermodynamic parameters such as Arrhenius prefactors (i.e. A_H/A_D) and activation energies ($\Delta E_a = E_{aD} - E_{aH}$). New theory has been developed and adapted in concert with experiment to rationalise these data, and while classical reactions are governed by barrier height, the importance of barrier shape on NQT has become apparent. Consequently, it has been suggested that factors other than transition state stabilisation are important to these reactions, in particular the concept of compressive dynamics – defined below – which has been successful in rationalising a range of temperature- and pressure-dependent KIEs.^{19, 26-30} Here, we will discuss our perspective on the potential role of (compressive) dynamics and NQT on selected enzymatic reactions.

2. The tunnelling contribution and rate enhancement. While there is currently no direct experimental measure for the degree of NQT in a chemical reaction, the magnitude of the primary kinetic isotope effect (KIE) is likely to be a reasonable first approximation (e.g. Figure 1B,C).³¹ Using computational techniques however, it is fairly straight-forward to calculate a reaction barrier and related parameters such as recrossing coefficients, zero point energies and tunnelling coefficients,

which can then be benchmarked against experimental rate constants and KIEs.³²⁻³⁴ For NQT reactions, methods of note include ensemble-averaged variational transition state theory with multidimensional tunnelling corrections (EA-VTST/MT),^{11, 35} the quantum classical path (QCP) method^{36, 37} and the molecular dynamics with quantum transitions (MDQT) method.¹²

Within the framework of semiclassical transition state theory (TST; Eq 1), the rate of reaction depends exponentially on the energy difference between reactant and transition state, ΔG_{TST}^\ddagger , the barrier height, and depends linearly on the pre-exponential frequency term, A , which encompasses terms such as recrossing and the transmission coefficient.³⁸

$$k_{TST} = A \exp(-\Delta G_{TST}^\ddagger / RT) \quad (1)$$

It is well established that enzyme catalysis is primarily due to the decrease in the barrier height, which in turn mainly arises from electrostatic effects.⁵⁻⁷ However, the effective barrier can be significantly smaller than ΔG_{TST}^\ddagger : there is always a certain probability of NQT occurring through the classical barrier, particularly for transfer of a light particle such as the H nucleus whose de Broglie wavelength ($\lambda = h/mv$) is on the same order as a bond length. According to the Wentzel-Kramers-Brillouin (WKB) approximation, the probability of NQT at any point q along the reaction coordinate is of the form:^{31, 39}

$$P_{\text{tun}}(q) = \left(1 + \exp \left[\left(2 / \hbar \right) \int_{x_1}^{x_2} \sqrt{2\mu(V(x) - V(q))} dx \right] \right)^{-1} \quad (2)$$

The probability of tunnelling therefore depends on the shape of the barrier, $V(x)$, rather than the height, V_{max} , suggesting the possibility that modulating the barrier shape can also be an important strategy for rate enhancement. Since tunnelling can occur at any point along the reaction coordinate, the rate of tunnelling is obtained by integrating over the entire barrier:

$$k_{\text{tun}} = (2\pi\hbar)^{-1} \int_0^{V_{\text{max}}} Q(V) P_{\text{tun}}(V) dV \quad (3)$$

where $Q(V)$ is the Boltzmann probability of achieving energy V relative to the reactant energy. The observed rate of reaction can then be given by the sum of $k_{TST} + k_{\text{tun}}$, with the tunnelling contribution κ defined as:

$$\kappa = 1 + k_{\text{tun}} / k_{TST} \quad (4)$$

In this description, a reaction with a κ of 100 proceeds 100 times faster than the equivalent reaction without tunnelling, as for every over-barrier classical transfer, the transferred H will tunnel through the barrier 99 times. It has been argued that this is an incorrect interpretation as the reaction follows a single pathway rather than two competing pathways (*i.e.* with and without tunnelling) and that as this amount of NQT might correspond to a reduction in apparent barrier height of only a few percent, then the reaction path is not significantly altered and the NQT contribution is not significant.²⁵ However, it is well known that chemical reactions do follow many competing pathways – hence why we do not define a single transition state for biochemical reactions but a hypersurface that divides the reactant and product sides of the free energy surface.⁴⁰ Furthermore, when NQT is involved there are an infinite number of tunnelling pathways for every classical pathway. The

distribution of pathways will depend on the interplay between the Boltzmann probability of ascending the barrier by a given amount and the probability of tunnelling at any point along the barrier. If the representative tunnelling energy (RTE in Figure 1A, the energy at which maximal tunnelling occurs) is significantly below the top of the barrier, then the majority of transfers will occur via a tunnelling pathway.

In any case, evolutionary pressure does not operate on the degree of NQT but on absolute rates. It is often pointed out that NQT contributes at most 3 orders of magnitude to the rate enhancement,¹⁵ while 10-12 orders magnitude are achieved by lowering the free energy of activation.¹⁵ However, a rate enhancement of even one order of magnitude can be vitally important for cellular metabolism; e.g. if the chemical step is rate limiting, and the enzyme contributes to the flux through a metabolic pathway, then any rate enhancement will directly influence the rate of metabolism and thus cell viability. Given the ubiquitous nature of H-transfers in biology, any metabolic pathway will involve multiple H-transfer steps and thus NQT could in principle have a major effect on metabolic flux as these rate enhancements will become multiplicative. The importance of NQT in biology is therefore not limited to its contribution to the “catalytic effect” (see next Section) but its contribution to metabolic rates essential for life.⁴¹ Furthermore, the tunnelling contribution κ does not reflect the *absolute amount* of NQT, i.e. the rate at which the transferring nucleus tunnels from the reactant to product well, but the rate *relative* to that of classical over-barrier transfer. This is an important distinction, as only looking at κ can lead to the interpretation that NQT is in fact anticatalytic²⁵ – after all, the rate enhancement due to NQT is typically smaller for a lower barrier.^{24, 25, 31, 42} However, as is evident from equation (2), the *absolute* tunnelling probability and hence k_{tun} increases with a decrease in barrier height/width. This decreases the *relative* NQT contribution, since k_{TST} increases more drastically, as illustrated in Figure 1, which shows how k_{tun} and k_{TST} change as a function of barrier height as the distance between donor and acceptor atoms is altered for a model reaction.

3. The catalytic effect and evolution. One of the key arguments against the importance of enzymatic NQT is that the KIE and tunnelling contribution for enzymatic reactions are similar to the equivalent “reference” reaction in solution. There are a limited number of examples where experimental data is available for both reactions,⁴³⁻⁴⁵ as comparable uncatalysed reactions typically do not occur on tractable timescales. However, this is also the conclusion from most computational comparisons, where the reference reaction in water is also analysed.⁴⁵⁻⁴⁷ In the case of nitroalkane oxidase, where experimental evidence does exist,²³ the NQT contribution increases 3-fold in the enzyme-catalysed reaction, although the NQT contribution in the enzyme is still relatively small ($\kappa = 3.5$). Therefore, while tunnelling can enhance the rate of enzymatic reactions relative to a classical over-barrier reaction, these data suggest this may not be a significant part of the catalytic effect, *i.e.* the rate enhancement over the uncatalysed reaction.

These data raise another interesting question: why are the enzymatic KIEs and NQT contribution not significantly smaller? Given that enzymes considerably lower the barrier height, one would expect the enzyme-catalysed reactions to have significantly smaller NQT contributions. Therefore, it is entirely possible that while enzymes may not have evolved to increase NQT contributions relative to the uncatalysed reaction, evolution has favoured H-transfer reactions that, at least, maintain the same relative NQT contribution (κ). Furthermore, comparisons to the uncatalysed reaction are not necessarily useful for understanding the evolution of enzymes, as organisms did not start out utilising the uncatalysed reactions – these often have half-times approaching the age of the earth⁴⁸ –

so much of the chemistry that enzymes carry out today could not have been part of the metabolism of early life. From an enzymologist's perspective, it is therefore more interesting to ask how NQT contributions have changed during the course of evolution. This question could be addressed within the growing field of paleoenzymology,⁴⁹⁻⁵² by comparing NQT in modern enzymes to those from less-evolved or extinct organisms, using e.g. ancestral reconstruction. When discussing evolutionary pressure, it is also important to consider the conditions under which organisms evolved. For example mammalian enzymes evolved under conditions of tight thermal regulation while many other organisms did not, and thus experience relatively larger temperature fluctuations. Further, one might expect thermophilic enzymes to have larger NQT contributions than meso- or psychrophilic enzymes, as thermophilic enzymes typically have larger barriers,^{53, 54} which are likely to relatively larger associated κ values. In the case of hydride transfer in DHFR, however, the mesophilic (EcDHFR),⁵⁵ thermophilic (BsDHFR)⁵⁶ and hyperthermophilic (TmDHFR)¹⁴ enzymes have near identical KIEs despite the wide range in activation energies ($E_a(\text{H}) = 13, 23 \text{ \& } 50 \text{ kJ mol}^{-1}$, respectively).*

4. Promoting vibrations and barrier compression. Atomistic understanding of the temperature-dependence of KIEs remains an important challenge in enzymology, and it is difficult to account for both temperature independent and strongly temperature dependent KIEs using semiclassical TST. The wide range in Arrhenius prefactor ratios observed in many cases^{18, 57, 58} cannot also be accounted for within the Bell correction model,⁵⁹ which incorporates a relatively small NQT correction within a TST formalism. However, these data are readily accommodated within non-adiabatic, vibronic formalisms,^{13, 14, 42, 57, 58, 60-67} which were initially introduced to deal with the strongly quantised ($\hbar\omega \gg k_B T$) C–H bonds broken in many enzymatic H-transfers.⁶⁸ Within such models, the NQT probability depends on the nuclear wavefunction overlap, $\langle \phi_\nu | \phi_\mu \rangle$, between the reactant and product states, e.g.:^{58, 68, 69}

$$k = \left(\frac{1}{2\pi}\right) |V_{ET}|^2 \sqrt{\frac{4\pi^3}{\lambda k_B T \hbar^2}} \exp\left(\frac{-\Delta G^\ddagger}{k_B T}\right) \times \left\langle \phi_\nu | \phi_\mu \right\rangle^2 \quad (5)$$

The reaction coordinate can be separated into two orthogonal components: a global reorganisation energy term and the H-coordinate. The former, which is orders of magnitude slower than barrier crossing, is required to achieve an electrostatic environment suitable for tunnelling – the “tunnelling ready configuration” (TRC⁷⁰) – where coherence between reactant and product states is achieved. Motion along the H-coordinate is much more rapid than reorganisation, as it occurs by definition on the timescale of barrier crossing. At the TRC, the tunnelling probability depends on parameters such as the reactant and product bond dissociation energies, the vibrational frequencies of the breaking and forming bonds, and well separation: together these terms define the nuclear wavefunctions and their overlap. Within this context, we define promoting vibrations as rapid vibrational modes that lead to donor-acceptor (D-A) compression on the timescale of barrier crossing, and hence increase the absolute NQT probability (by increasing $\langle \phi_\nu | \phi_\mu \rangle$ in equation (5)). This does not imply that the promoting vibration necessarily extends into, or arises from, the protein itself – although there are computational studies which suggest this might be the case in certain enzymes⁷¹⁻⁷⁵ – but may be highly localised.^{61, 62} Within this framework, an increase in temperature causes an increase in the

* Note that these KIEs were not reported at the enzymes' optimal temperatures, but at 25, 25, & 40°C, respectively; however, accounting for this would give the EcDHFR the largest KIE (EcDHFR has the least temperature-dependent KIE while the KIE of the other two decrease with temperature).

amplitude of motion along the H-coordinate, leading to a shorter average tunnelling distance and a decrease in the magnitude of the KIE.^{58, 69} When discussing promoting vibrations, we sometimes employ the term “barrier compression,” referring to the change in the near-instantaneous potential energy barrier through which tunnelling occurs, not the overall free energy barrier which implicitly accounts for these effects.^{31, 76, 77}

Vibronic models rely on the non-adiabatic assumption of weak coupling between reactant and product states. However, it should be pointed out that this breaks down for very short transfer distances (near the top of the barrier from a TST correction perspective), so we tend to use these models phenomenologically to rationalise differences between very similar enzymatic reactions, *e.g.* in a range of enzyme variants⁶⁴ or as a function of hydrostatic pressure.^{77, 78} Nevertheless, it has been shown that a vibronic treatment gives the same general trend as the quantum classical path (QCP)^{36, 37} method for H-transfer in dihydrofolate reductase (DHFR),⁴² and we have shown that our vibronic model performs well for proton transfer in aromatic amine dehydrogenase (AADH) when compared to the WKB model.³¹ This is not surprising, given the similarities between equation (3) and equation (5): in both cases a classical activation term represents the Boltzmann probability of achieving a conformation at which tunnelling can occur, at which point the tunnelling probability depends on the width of the barrier at that conformation.

The concept of promoting vibrations remains highly contentious and, for example, it has been argued that catalytically important vibrational modes are the same in solution as in an enzyme.²⁰ While this may be the case, a fundamental differences between enzymatic and solution chemistry is that enzyme catalysis typically involves a high degree of preorganisation, which minimises the reorganisation energy for individual chemical steps as well as the atomic fluctuations necessary for the transition between consecutive steps.^{7, 79} The latter was elegantly illustrated in a recent computational study of serine esterases and idealised forms of their transition states,⁸⁰ which found that the active site geometry is optimised to minimise the degree of rearrangement required between consecutive steps, and not necessarily that which is most optimal for a given chemical step. Enzymes therefore impose significant restrictions along most degrees of freedom; at the same time, however, effective barrier crossing requires facile motion along the H-coordinate. Molecules in solution can explore conformational space until relevant vibrational motion can carry the system from reactant to transition state (or TRC), while the enzyme-substrate complex is conformationally restricted. Efficient use of specific compressive modes / promoting vibrations might represent the best strategy for ensuring that dynamical excursions from the ground state are as productive as possible given the high degree of restriction. The nature of the dynamic coupling to the H-coordinate may involve utilising vibrational modes of active site residues,^{72, 73} restraining the substrate in a conformation which favours specific modes,⁸¹ or simply binding the substrates in an orientation where inherent normal modes coincide with the H-coordinate (Figure 2).⁷⁷ For example, the conformation of the substrate in aromatic amine dehydrogenase was found to be crucial for the effectiveness of a promoting vibration: in a variant form of the enzyme, the alternative substrate conformation was such that the promoting vibration was occluded (Figure 3), leading to an increase in barrier height and a 3-orders-of-magnitude decrease in the observed rate constant.⁸¹ If both catalysed and uncatalysed reactions utilise similar vibrational modes, the difference being that these are more likely to be productive in the enzyme, then the rate enhancement solely arising from preorganisation.⁶ Nevertheless, this does not diminish the importance of promoting vibrations to the enzymatic reaction or their effect on observable activation parameters.

In a recent attempt to explain the temperature-dependence of the KIE without invoking promoting vibrations, an alternative framework invoking conformational complexity was proposed where the KIE depends on the temperature-dependent equilibrium between multiple reactive conformations, each leading to a different KIE.⁸² Of course, conformational complexity does occur and can affect the observed KIE.^{83, 84} However, while this model has successfully been used to fit the temperature-dependence of the KIE on several enzymatic H-transfers, it predicts that the magnitude of the KIE can either increase or decrease with temperature, depending on the relative free energy of each conformer. In enzymatic H-transfers, the magnitude of significantly temperature-dependent KIEs is always observed to decrease with increasing temperature (i.e. we are not aware of any enzymatic KIEs that significantly decrease with increasing temperature), a trend which does not arise within this model. On the other hand, it is well known that rapid D-A fluctuations modulate the barrier height such that the KIE will always decrease as distance sampling increases with increasing temperature.^{42, 77, 85}

5. Experimental evidence for NQT and promoting vibrations? There is currently no direct experimental evidence that the temperature-dependence of the KIE arises from vibrational modes coupled to NQT and this remains a major challenge in the field. However, there is compelling evidence from combined experimental and computational studies that this may be the case. Typically these focus on the temperature-dependence of the KIE (see above), but we have also looked at the effect of hydrostatic pressure.^{27, 77, 78, 84, 86, 87} In the absence of NQT, KIEs arise from differences in zero-point energy and thus the stretching frequency of the transferred ¹H, ²D or ³T, which are typically taken to be invariant to changes in pressure over the experimental range.^{88, 89} Consequently, pressure-dependent KIEs have been used as evidence for the involvement of NQT.^{90, 91} Within the vibronic framework (Eq 5), pressure can perturb the KIE on the reaction by changing the equilibrium H-transfer distance and/or the frequency of (promoting) vibrational modes as other changes are likely to cancel in the KIE calculation.²⁷ These perturbations can be modelled using MD simulations, and may be monitored experimentally in rare cases. In the case of hydride transfer in Morphinone Reductase (MR), MD simulations predicted a decrease in D-A distance with increasing pressure,^{77, 92} which was confirmed experimentally through the observation of an increased strength in the charge-transfer (CT) complex between the donor and acceptor groups (nicotinamide of NADH and isoalloxazine of FMN, respectively).⁹² Experiments revealed that pressure causes an increase in the magnitude of the KIE with a concomitant increase in the observed rate of H-transfer, which can be rationalised if the decrease in D-A distance is accompanied by an increase in the frequency of the promoting vibration:²⁹ although the average D-A distance decreases, the shorter, more productive pathways with higher tunnelling probabilities become more difficult to attain (Figure 2C). The increase in promoting vibration force constant was confirmed through MD simulations both by the narrower distribution of D-A distances at high pressure⁹² and by spectral density^{72, 93} analysis which revealed an increase in the putative promoting vibration frequency with pressure.⁷⁷

Pressure acts to anisotropically perturb enzyme structure⁹⁴ and no simple trends have emerged between the pressure- and temperature-dependence of KIEs.⁹⁵ Pressure experiments can nevertheless be highly informative on a case-by-case basis, and while phenomenological models have been derived for these reactions,^{90, 91, 27} structural data and/or molecular dynamics simulations are essential to understand the atomistic origin of observed effects. For example, proton transfer in AADH with phenylethylamine as substrate exhibits complex pressure-dependent H-transfer kinetics, which we were able to explain within our vibronic formalism after analysis of MD simulations. In

contrast to MR, these revealed no change in equilibrium D-A distance, which is readily rationalised given that one key effect of hydrostatic pressure on proteins is that additional water molecules are forced into cavities.⁹⁶ and the cofactor in MR is much more solvent exposed than the substrate in AADH. On the other hand, interpreting pressure data for light-driven NQT in protochlorophyllide oxidoreductase (POR)⁹⁵ or proton transfer during ascorbate oxidation by ferricyanide⁹⁷ has proven difficult in the absence of structural data and MD simulations.

In recent years “heavy-protein” experiments have become popular for studying the link between dynamics and NQT: if dynamics are important, then isotopic substitution with ¹³C, ¹⁵N and ²H should perturb these dynamics and cause observable perturbations to H-transfer. We have performed experiments on the MR homologue pentaerythritol tetranitrate reductase (PETNR) where the temperature dependence of the KIE is much larger when H-transfer occurs from NADPH than from NADH.⁶⁰ In triple-labelled “heavy” PETNR, the temperature dependence of the KIE on both reactions increased,⁹⁸ although this increase is much stronger with NADPH, consistent with an underlying promoting vibration involved in the NADH reaction that does not give rise to a strongly temperature-dependent KIE in the light enzyme.⁶² Similar experiments have been carried out on other enzymes,⁹⁹⁻¹⁰³ and the rate of H-transfer tends to decrease in the heavy enzyme (though not always¹⁰¹). This can be attributed to a number of effects,¹⁰⁴ including a small change in electrostatics due to slight difference in bond lengths.¹⁰⁵ In the case of DHFR, EA-VTST calculations have suggested that the decrease in rate of the heavy protein is due to a decrease in the recrossing coefficient arising from an increase in coupling between protein motion and the reaction coordinate.¹⁰⁰ [Do we need to add something to explain that this does not mean that all coupling is necessarily bad?]

4. Conclusions and future outlook.

Since the majority of enzyme reactions involve at least one H-transfer step, which will involve some degree of NQT, it is essential to understand the factors that govern enzymatic NQT. While significant progress has been made in this field since NQT was first reported in an enzyme over 25 years ago,⁸ questions remain unanswered and controversies persist. Experimental probes for the involvement of NQT include deviations from classical behaviour for the temperature- and pressure-dependence of the primary KIE. It is more challenging to directly measure the role of dynamics in NQT reactions, although much insight has been gained from combined pressure and temperature-dependence measurements coupled with MD simulations and modelling. Perhaps the most promising new development in this field is the advent of “heavy-protein” experiments, which allows a direct and titratable perturbation of protein dynamics. From our perspective, it is clear that rapid compressive dynamics can play an important role in facilitating enzymatic NQT reactions, although the precise nature and ubiquity of such modes is not established: to what extent is the protein involved and how has evolution directed/selected these modes?

Acknowledgments

This is a contribution from the BBSRC/EPSRC Centre for Synthetic Biology of Fine and Speciality Chemicals (SYNBIOCHEM). SH is a BBSRC David Phillips Research Fellow. NSS is an EPSRC Established Career Fellow.

1. M. T. Smith, K. M. Wilding, J. M. Hunt, A. M. Bennett and B. C. Bundy, *Febs Lett.*, 2014, 588, 2755-2761.

2. A. V. Bryksin, A. C. Brown, M. M. Baksh, M. G. Finn and T. H. Barker, *Acta Biomaterialia*, 2014, 10, 1761-1769.
3. V. Singh, *Gene*, 2014, 535, 1-11.
4. E. Fischer, *Ber. Dtsch. Chem. Ges.*, 1894, 27, 2985-2993.
5. *Transition States of Biochemical Processes*, Plenum Press, New York, 1978.
6. A. Warshel, *J. Biol. Chem.*, 1998, 273, 27035-27038.
7. A. Warshel, P. K. Sharma, M. Kato, Y. Xiang, H. Liu and M. H. Olsson, *Chem. Rev.*, 2006, 106, 3210-3235.
8. Y. Cha, C. J. Murray and J. P. Klinman, *Science*, 1989, 243, 1325-1330.
9. B. J. Bahnon, T. D. Colby, J. K. Chin, B. M. Goldstein and J. P. Klinman, *Proc. Natl. Acad. Sci. USA*, 1997, 94, 12797-12802.
10. J. Basran, M. J. Sutcliffe and N. S. Scrutton, *Biochem.*, 1999, 38, 3218-3222.
11. C. Alhambra, J. Corchado, M. L. Snchez, M. Garcia-Viloca, J. Gao and D. G. Truhlar, *J. Phys. Chem. B*, 2001, 105, 11326-11340.
12. S. R. Billeter, S. P. Webb, P. K. Agarwal, T. Jordanov and S. Hammes-Schiffer, *J. Am. Chem. Soc.*, 2001, 123, 11262-11272.
13. M. J. Knapp and J. P. Klinman, *Eur. J. Biochem.*, 2002, 269, 3113-3121.
14. G. Maglia and R. K. Allemann, *J. Am. Chem. Soc.*, 2003, 125, 13372-13373.
15. M. Garcia-Viloca, J. Gao, M. Karplus and D. G. Truhlar, *Science*, 2004, 303, 186-195.
16. Z. X. Liang and J. P. Klinman, *Curr. Opin. Struct. Biol.*, 2004, 14, 648-655.
17. Z. X. Liang, T. Lee, K. A. Resing, N. G. Ahn and J. P. Klinman, *Proc. Natl. Acad. Sci. USA*, 2004, 101, 9556-9561.
18. L. Masgrau, A. Roujeinikova, L. O. Johannissen, P. Hothi, J. Basran, K. E. Ranaghan, A. J. Mulholland, M. J. Sutcliffe, N. S. Scrutton and D. Leys, *Science*, 2006, 312, 237-241.
19. Z. D. Nagel and J. P. Klinman, *Chem. Rev.*, 2006, 106, 3095-3118.
20. M. H. Olsson, W. W. Parson and A. Warshel, *Chem. Rev.*, 2006, 106, 1737-1756.
21. J. Z. Pu, J. L. Gao and D. G. Truhlar, *Chem. Rev.*, 2006, 106, 3140-3169.
22. S. Hay, C. R. Pudney and N. S. Scrutton, *FEBS J.*, 2009, 276, 3930-3941.
23. D. T. Major, A. Heroux, A. M. Orville, M. P. Valley, P. F. Fitzpatrick and J. L. Gao, *Proc. Natl. Acad. Sci. USA*, 2009, 106, 20734-20739.
24. S. C. L. Kamerlin, J. Mavri and A. Warshel, *FEBS Lett.*, 2010, 584, 2759-2766.
25. S. C. L. Kamerlin and A. Warshel, *J. Phys. Org. Chem.*, 2010, In print.
26. S. Hay and N. S. Scrutton, *Nat. Chem.*, 2012, 4, 161-168.
27. S. Hay and N. S. Scrutton, *Biochem.*, 2008, 47, 9880-9887.
28. S. Hay, C. Pudney, P. Hothi, L. O. Johannissen, L. Masgrau, J. Pang, D. Leys, M. J. Sutcliffe and N. S. Scrutton, *Biochem. Soc. Trans.*, 2008, 36, 16-21.
29. S. Hay, M. J. Sutcliffe and N. S. Scrutton, *Proc. Natl. Acad. Sci. U.S.A.*, 2007, 104, 507-512.
30. A. Kohen, *Prog. React. Kinet. Mech.*, 2003, 28, 119-156.
31. S. Hay, L. O. Johannissen, M. J. Sutcliffe and N. S. Scrutton, *Biophys. J.*, 2010, 98, 121-128.
32. J. Gao and D. G. Truhlar, *Annu. Rev. Phys. Chem.*, 2002, 53, 467-505.
33. *Chemical Modelling: Applications and Theory, Vol 4*, 2006, 4, 1-528.
34. M. W. van der Kamp, K. E. Shaw, C. J. Woods and A. J. Mulholland, *J. Roy. Soc. Interface*, 2008, 5, S173-S190.
35. D. G. Truhlar, J. L. Gao, M. Garcia-Viloca, C. Alhambra, J. Corchado, M. L. Sanchez and T. D. Poulsen, *Int. J. Quant. Chem.*, 2004, 100, 1136-1152.
36. J. K. Hwang and A. Warshel, *J. Phys. Chem*, 1993, 97, 10053-10058.
37. J. Mavri, H. Liu, M. H. Olsson and A. Warshel, *J. Phys. Chem. B*, 2008, 112, 5950-5954.
38. M. Garcia-Viloca, D. G. Truhlar and J. Gao, *Biochem.*, 2003, 42, 13558-13575.
39. W. H. Miller, *Science*, 1986, 233, 171-177.
40. P. Pechukas, *Annu. Rev. Phys. Chem.*, 1981, 32, 159-177.

41. S. Hay and N. S. Scrutton, *22nd Solvay Conference on Chemistry: Quantum Effects in Chemistry and Biology*, 2011, 3.
42. H. Liu and A. Warshel, *J. Phys. Chem. B*, 2007, 111, 7852-7861.
43. K. M. Doll, B. R. Bender and R. G. Finke, *J. Am. Chem. Soc.*, 2003, 125, 10877-10884.
44. K. M. Doll and R. G. Finke, *Inorg. Chem.*, 2003, 42, 4849-4856.
45. I. Feierberg, V. Luzhkov and J. Aqvist, *J. Biol. Chem.*, 2000, 275, 22657-22662.
46. I. H. Williams, *J. Phys. Org. Chem.*, 2010, 23, 685-689.
47. M. H. M. Olsson, J. Mavri and A. Warshel, *Phil. Trans. Roy. Soc. B - Biol. Sci.*, 2006, 361, 1417-1432.
48. R. Wolfenden and M. J. Snider, *Acc. Chem. Res.*, 2001, 34, 938-945.
49. S. A. Benner, S. O. Sassi and E. A. Gaucher, *Adv. Enzymol. Relat. Areas. Mol. Biol.*, 2007, 75, 1-132, xi.
50. B. G. Hall, *Proc. Natl. Acad. Sci. USA*, 2006, 103, 5431-5436.
51. R. Perez-Jimenez, A. Ingles-Prieto, Z. M. Zhao, I. Sanchez-Romero, J. Alegre-Cebollada, P. Kosuri, S. Garcia-Manyes, T. J. Kappock, M. Tanokura, A. Holmgren, J. M. Sanchez-Ruiz, E. A. Gaucher and J. M. Fernandez, *Nat Struct Mol Biol*, 2011, 18, 592-596.
52. J. W. Thornton, *Nat Rev Genet*, 2004, 5, 366-375.
53. G. Feller and C. Gerday, *Nat. Rev. Microbiol.*, 2003, 1, 200-208.
54. K. S. Siddiqui and R. Cavicchioli, *Annual Review of Biochem.*, 2006, 75, 403-433.
55. R. S. Sikorski, L. Wang, K. A. Markham, P. T. R. Rajagopalan, S. J. Benkovic and A. Kohen, *J. Am. Chem. Soc.*, 2004, 126, 4778-4779.
56. H. S. Kim, S. M. Damo, S. Y. Lee, D. Wemmer and J. P. Klinman, *Biochem.*, 2005, 44, 11428-11439.
57. A. Kohen, R. Cannio, S. Bartolucci and J. P. Klinman, *Nature*, 1999, 399, 496-499.
58. M. J. Knapp, K. Rickert and J. P. Klinman, *J. Am. Chem. Soc.*, 2002, 124, 3865-3874.
59. R. P. Bell, in *The Tunnel Effect in Chemistry*, Chapman and Hall, London, 1980, pp. 51-140.
60. J. Basran, R. J. Harris, M. J. Sutcliffe and N. S. Scrutton, *J. Biol. Chem.*, 2003, 278, 43973-43982.
61. E. Hatcher, A. V. Soudackov and S. Hammes-Schiffer, *J. Am. Chem. Soc.*, 2007, 129, 187-196.
62. L. O. Johannissen, S. Hay, N. S. Scrutton and M. J. Sutcliffe, *J. Phys. Chem. B*, 2007, 111, 2631-2638.
63. V. Stojkovic, L. L. Perissinotti, D. Willmer, S. J. Benkovic and A. Kohen, *J. Am. Chem. Soc.*, 2012, 134, 1738-1745.
64. C. R. Pudney, L. O. Johannissen, M. J. Sutcliffe, S. Hay and N. S. Scrutton, *J. Am. Chem. Soc.*, 2010, 132, 11329-11335.
65. C. R. Pudney, S. Hay, C. Levy, J. Pang, M. J. Sutcliffe, D. Leys and N. S. Scrutton, *J. Am. Chem. Soc.*, 2009, 131, 17072-17073.
66. M. P. Meyer, D. R. Tomchick and J. P. Klinman, *Proc Natl Acad Sci U S A*, 2008, 105, 1146-1151.
67. D. J. Heyes, M. Sakuma, S. P. de Visser and N. S. Scrutton, *J. Biol. Chem.*, 2009, 284, 3762-3767.
68. A. M. Kuznetsov and J. Ulstrup, *Can. J. Chem.*, 1999, 77, 1085-1096.
69. L. O. Johannissen, T. Irebo, M. Sjöin, O. Johansson and L. Hammarström, *J. Phys. Chem. B*, 2009, 113, 16214-16225.
70. C. R. Pudney, S. Hay, M. J. Sutcliffe and N. S. Scrutton, *J. Am. Chem. Soc.*, 2006, 128, 14053-14058.
71. D. Antoniou and S. D. Schwartz, *J. Phys. Chem. B*, 2001, 105, 5553-5558.
72. S. Caratzoulas, J. S. Mincer and S. D. Schwartz, *J. Am. Chem. Soc.*, 2002, 124, 3270-3276.
73. S. Nunez, D. Antoniou, V. L. Schramm and S. D. Schwartz, *J. Am. Chem. Soc.*, 2004, 126, 15720-15729.
74. S. L. Quaytman and S. D. Schwartz, *Proc. Natl. Acad. Sci. USA*, 2007, 104, 12253-12258.

75. S. D. Schwartz and V. L. Schramm, *Nat. Chem. Biol.*, 2009, 5, 551-558.
76. S. Hay, C. R. Pudney, T. A. McGrory, J. Y. Pang, M. J. Sutcliffe and N. S. Scrutton, *Angew. Chem. Int. Ed.*, 2009, 48, 1452-1454.
77. L. O. Johannissen, N. S. Scrutton and M. J. Sutcliffe, *Angew. Chem. Int. Ed. Engl.*, 2011, 50, 2129-2132.
78. S. Hay, M. J. Sutcliffe and N. S. Scrutton, *Proc. Natl. Acad. Sci. USA*, 2007, 104, 507-512.
79. A. J. Adamczyk, J. Cao, S. C. L. Kamerlin and A. Warshel, *Proc. Natl. Acad. Sci. USA*, 2011, 108, 14115-14120.
80. A. J. T. Smith, R. Muller, M. D. Toscano, P. Kast, H. W. Hellinga, D. Hilvert and K. N. Houk, *J. Am. Chem. Soc.*, 2008, 130, 15361-15373.
81. L. O. Johannissen, N. S. Scrutton and M. J. Sutcliffe, *J R Soc Interface*, 2008, 5 Suppl 3, S225-232.
82. D. R. Glowacki, J. N. Harvey and A. J. Mulholland, *Nat. Chem.*, 2012, 4, 169-176.
83. C. R. Pudney, S. Hay, J. Pang, C. Costello, D. Leys, M. J. Sutcliffe and N. S. Scrutton, *J. Am. Chem. Soc.*, 2007, 129, 13949-13956.
84. C. R. Pudney, T. McGrory, P. Lafite, J. Y. Pang, S. Hay, D. Leys, M. J. Sutcliffe and N. S. Scrutton, *ChemBioChem*, 2009, 10, 1379-1384.
85. D. Antoniou and S. D. Schwartz, *J. Chem. Phys.*, 1998, 108, 3620-3625.
86. S. Hay, L. O. Johannissen, P. Hothi, M. J. Sutcliffe and N. S. Scrutton, *J. Am. Chem. Soc.*, 2012, 134, 9749-9754.
87. S. Hay, C. R. Pudney, M. J. Sutcliffe and N. S. Scrutton, *J. Phys. Org. Chem.*, 2010, 23, 696-701.
88. N. S. Isaacs, in *Isotope Effects in Organic Chemistry*, eds. E. Buncler and C. C. Lee, Elsevier, London, 1984, vol. 6, pp. 67-105.
89. D. B. Northrop, *Phil. Trans. Royal Soc. B*, 2006, 361, 1341-1349.
90. N. S. Isaacs, K. Javaid and E. Rannala, *Nature*, 1977, 268, 372-372.
91. D. B. Northrop, *J. Am. Chem. Soc.*, 1999, 121, 3521-3524.
92. S. Hay, C. R. Pudney, T. A. McGrory, J. Pang, M. J. Sutcliffe and N. S. Scrutton, *Angew. Chem. Int. Ed. Engl.*, 2009, 48, 1452-1454.
93. S. Caratzoulas and S. D. Schwartz, *J. Chem. Phys.*, 2001, 114, 2910-2918.
94. D. A. Ledward, *High Pressure Research*, 2000, 19, 391-400.
95. R. Hoeven, D. J. Heyes, S. Hay and N. S. Scrutton, *FEBS J.*, 2015, In press.
96. J. Roche, J. A. Caro, D. R. Norberto, P. Barthe, C. Roumestand, J. L. Schlessman, A. E. Garcia, B. Garcia-Moreno and C. A. Royer, *Proc. Natl. Acad. Sci. USA*, 2012, 109, 6945-6950.
97. S. M. Kandathil, M. D. Driscoll, R. V. Dunn, N. S. Scrutton and S. Hay, *Physical Chemistry Chemical Physics*, 2014, 16, 2256-2259.
98. C. R. Pudney, A. Guerriero, N. J. Baxter, L. O. Johannissen, J. P. Waltho, S. Hay and N. S. Scrutton, *J. Am. Chem. Soc.*, 2013, 135, 2512-2517.
99. D. Antoniou, X. X. Ge, V. L. Schramm and S. D. Schwartz, *J. Phys. Chem. Lett.*, 2012, 3, 3538-3544.
100. L. Y. P. Luk, J. J. Ruiz-Pernia, W. M. Dawson, M. Roca, E. J. Loveridge, D. R. Glowacki, J. N. Harvey, A. J. Mulholland, I. Tunon, V. Moliner and R. K. Allemann, *Proc. Natl. Acad. Sci. USA*, 2013, 110, 16344-16349.
101. L. Y. Luk, E. J. Loveridge and R. K. Allemann, *J. Am. Chem. Soc.*, 2014, 136, 6862-6865.
102. J. E. Masterson and S. D. Schwartz, *J. Phys. Chem. A*, 2013, 117, 7107-7113.
103. Z. Wang, P. Singh, C. M. Czekster, A. Kohen and V. L. Schramm, *J. Am. Chem. Soc.*, 2014, 136, 8333-8341.
104. K. Swiderek, J. J. Ruiz-Pernia, V. Moliner and I. Tunon, *Curr. Opin. Chem. Biol.*, 2014, 21, 11-18.
105. A. Kohen, *Acc Chem Res*, 2015, In Press.
106. R. B. Sessions, P. Dauber-Osguthorpe and D. J. Osguthorpe, *J. Mol. Biol.*, 1989, 210, 617-633.

107. L. O. Johannissen, S. Hay, N. S. Scrutton and M. J. Sutcliffe, *J. Phys. Chem. B*, 2007, 111, 2631-2638.

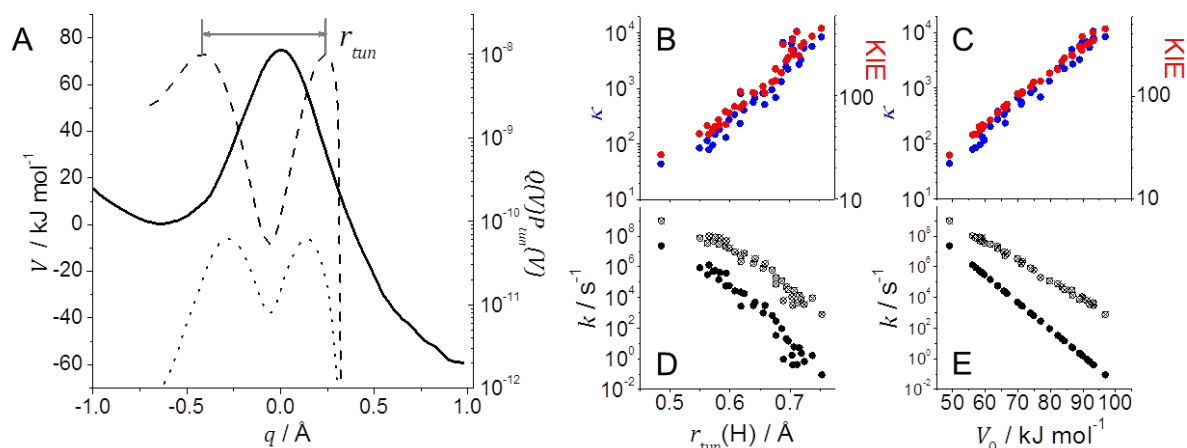


Figure 1. Effect of barrier shape on H-transfer in AADH with tryptamine; barriers were calculated for structures taken from QM/MM MD simulations. (A) Typical adiabatic potential energy barrier (solid line) and transfer probability, $Q(V)P_{tun}(V)$ from equation (3) for H (dashed line) and D (dotted line). The RTE is the representative tunnelling energy where the transfer probability is maximised and r_{tun} is the tunnelling distance at this energy; (B,D) effect of tunnelling distance (r_{tun}) and (C,E) effect of barrier height (V_0). κ (for H; blue circles) and the KIE (red circles) are shown in panels B and C. k_{TST} (black circles), k_{tun} (open circles) and k_{obs} (crosses) are shown in panels D and E. (Adapted from ref. 31)

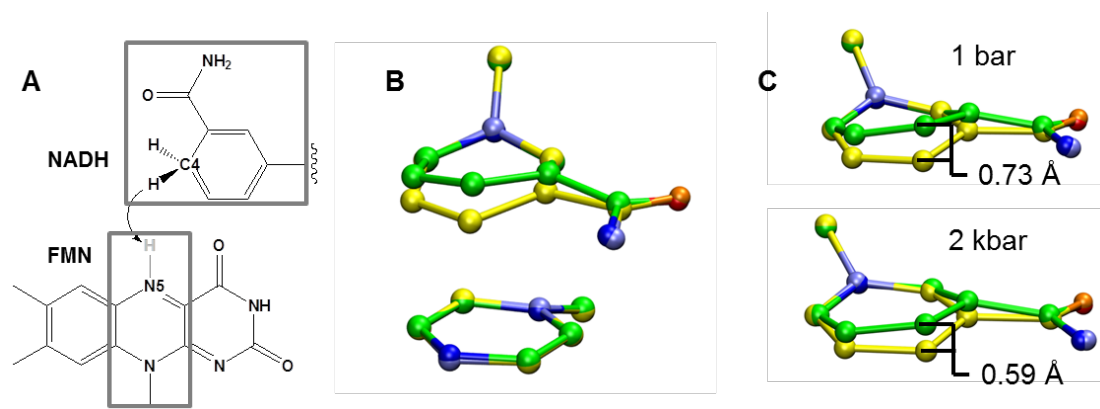


Figure 2. (A) Hydride transfer from NADH to FMN in Morphinone Reductase. (B) Promoting vibration illustrated for the heavy atoms in the grey boxes in (A), identified from constant pressure MD simulations and digital filtering by frequency deconvolution.^{106, 107} The overlaid structures correspond to the average structures at the minimum and maximum displacements. (C) Effect of hydrostatic pressure on the degree of done-acceptor compression. (Adapted from ref. 77).

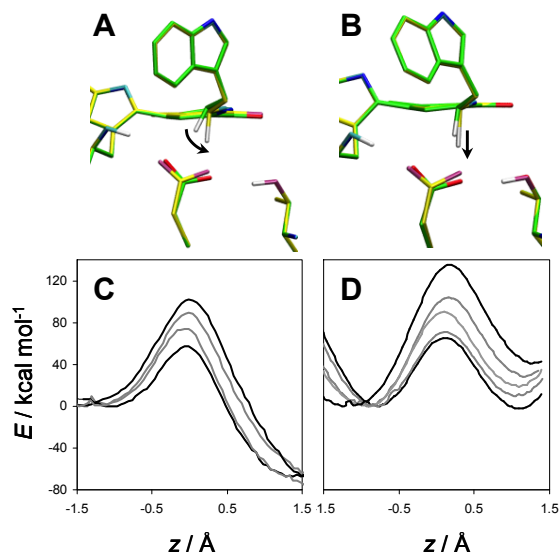


Figure 3. Substrate conformations in AADH with bound tryptamine. (A) The promoting vibration illustrated by the curved arrow moves the system towards the representative structure for tunnelling (RTE structure, yellow carbon atoms) in the native enzyme, while (B) the same O-H compression in the isolated small subunit requires a significant degree of C-H stretching. (C,D) Representative adiabatic potential energy scans, spanning the full range of observed activation energies, with the reaction coordinate $z = d(\text{C-H}) - d(\text{O-H})$ for (C) the native enzyme and (D) the isolated small subunit. The stiffer C-H stretching in the small subunit leads to a narrower reactant well, which allows less fluctuation along the reaction coordinate. (Adapted from ref. 81)