

# Analytical Methods

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4 **Quantitative analysis of the major components of coal ash**  
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7 **by laser induced breakdown spectroscopy coupled with**  
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10 **wavelet neural network (WNN)**  
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41  
42 **Abstract**  
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44 Laser induced breakdown spectroscopy (LIBS) technique was applied to detecting the  
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46 major components of coal ash based on wavelet neural network (WNN). Prior to  
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48 construct the WNN model, the spectra were preprocessed by Wavelet threshold  
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50 de-noising and Kalman filtering, and the principle components (PC) extracted by  
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52 principle component analysis (PCA) were used as input variable. Afterwards, the  
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54 quantitative analysis of the major components in coal ash samples was completed by  
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60 WNN with the optimized WNN model parameters consist of the number of hidden

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4 neurons (NHN), the number of iterations (NI), the learning rate (LR) and the  
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7 momentum based on the root mean square error (RMSE). Finally, artificial neural  
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10 network (ANN) and WNN were evaluated comparatively on their ability to predict the  
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12 content of major components of test coal ash samples in terms of correlation  
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14 coefficient(R) and RMSE, demonstrating that LIBS combined with WNN model  
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17 exhibited better prediction for coal ash, and is a promising technique for combustion  
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20 process control even in online mode.  
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24 **Keywords:** Laser induced breakdown spectroscopy; coal ash; wavelet neural network  
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## 29 30 **1. Introduction**

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32 Boiler slag is one of the main factors affecting safe operation of boiler. However,  
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34 coal ash composition, which refers to the metal and nonmetal oxides and salts  
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36 generated from various minerals in coal combustion, is an important parameter  
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38 determining slagging characteristics.<sup>1-2</sup> The composition of ashes depends on the coal  
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40 quality and the combustion procedure. Therefore, fast and accurate measurement of ash  
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42 content can judge the trend of the boiling coal slagging, and it is conducive to take  
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44 measures to prevent or reduce heating surface slagging and to realize the boiling coal  
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46 ash composition on-line detection. In addition, coal ash was used as partial replacement  
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48 of cement to product concrete due to its advantages of high production and low cost. It  
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50 also can be used as soil conditioner and fertilizer, artificial marbles, light aggregates,  
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52 fine ceramics and so on.<sup>3-5</sup>  
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4 Traditional method for the detection of major components include chemical  
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7 analysis method, X-ray fluorescence, X-ray powder diffraction, inductively coupled  
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10 plasma atomic emission spectrometry (ICP-AES) and atomic absorption spectrometry  
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12 (AAS), and so on<sup>6-9</sup>. Nevertheless, these techniques require much time, costly  
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14 instrumentation and complex sample preparation, thus are not suitable to fast analysis.  
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18 The prompt gamma neutron activation analysis (PGNAA)<sup>10</sup> is based on the  
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20 measurement of gamma rays produced by the main constituents of the mineral matter  
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22 in coal, and has been applied effectively for on-line elemental analysis and proximate  
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24 analysis of coal. But PGNAA technique has strict regulatory requirements and  
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26 requires a big amount of samples, and its neutron source presents potential health  
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28 hazards.  
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35 Laser induced breakdown spectroscopy (LIBS) can be described as a rapid,  
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37 multi-elemental and promising technique with a lot of advantages, mainly including  
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39 minimal or no sample preparation and destruction, low time consumption and on-line  
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41 analysis.<sup>11-12</sup> It is an atomic emission spectroscopy technique based on the analysis of  
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43 spectral lines emitted from the laser-induced plasma, which is obtained by focusing a  
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45 pulsed laser beam on to a sample. It has been widely applied in industrial processes,  
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47 environmental testing and geologic exploration, as well as many other fields.<sup>13-17</sup> This  
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49 technique is first introduced into the on-line detection of coal field, which focuses on  
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51 the qualitative and quantitative analysis of element composition of fly ash and  
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53 fluidized coal particles, by Otesen.ect in 1991.<sup>18</sup> In recent years, LIBS technique has  
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4 been widely used in coal and fly ash. Mateo *et al.*<sup>19</sup> analyzed the influence of  
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7 accessory elements in coal with different laser wavelengths and sample placements in  
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10 measurement procedures. As a result, the short wavelength laser is more conducive to  
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13 accurate measurement. But the accuracy of the repeated measurement needs to be  
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16 improved. Feng *et al.*<sup>20</sup> used partial least squares (PLS) to solve the problem of low  
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19 accuracy of coal quality components, and to some extent, improved measurement  
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22 accuracy. In addition, LIBS combined with PLS has been carried out to extract coal  
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25 ash content information from LIBS spectra with the motivation of developing an  
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28 alternative calibration method for accurate and reliable quantitative analysis of ash  
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31 content in coal by Yao *et al.*<sup>13</sup>. However, it has poor nonlinear fitting ability and  
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34 tolerance faults. Therefore, a method with well nonlinear fitting capability, tolerance  
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37 faults, self-organized learning and self-adaptivity was necessary to be proposed for  
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40 the coal ash analysis. The neural network has the accurate mapping ability to the  
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43 non-linear problem, however, the traditional artificial neural network<sup>21</sup> has slow  
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46 convergence rate and is prone to fall into local extremum. Wavelet neural network  
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49 (WNN) is a combination of wavelet analysis and neural network<sup>22-24</sup>, and makes full  
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52 use of the multi-resolution and partial elaboration of wavelet analysis and  
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55 self-organized learning and adaptive advantage of neural network. It has been widely  
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58 applied in the solubility measurements of dyes and petroleum industry.<sup>25-27</sup> It shows  
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61 wavelet network has stronger adaptive capacity, faster convergence speed and higher  
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64 precision of prediction than traditional artificial neural network.

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4 The objective of this study put forward a method-WNN for accurate and reliable  
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6 quantitative analysis of ash content of coal. At first, to get accurate and useful LIBS  
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8 spectra information, the Wavelet threshold denoising and Kalman filtering were  
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10 applied in data preprocessing. Afterwards, different input variables were used to  
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12 construct the WNN model. Then the quantitative analysis of the major component in  
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14 coal ash samples was completed by WNN with the optimized model parameters (the  
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16 number of hidden neurons (NHN), the number of iterations (NI), the learning rate (LR)  
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18 and the momentum) based on the root mean square error (RMSE).  
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## 25 26 **2. Experimental details**

### 27 28 **2.1. Experimental set-up**

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30 The LIBS experimental set-up (Fig.1) is composed of laser, beam focusing  
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32 system, plasma collecting optics, detection and analysis system device. A Q-switch  
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34 Nd:YAG laser ( $\lambda=1064$  nm, 10 ns pulse FWHM, 100 mJ/pulse, repetition rate of 5  
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36 HZ) was focused with a 50 mm diameter, 100 mm focal length lens to generate the  
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38 plasma in air atmosphere pressure. The plasma emission was collected in the direction  
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40 of a 45° angle by an optical fiber to the entrance slit of an Echelle spectrograph  
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42 Aryelle 200 (LTB, German) coupled to an ICCD camera (iStar, Andor, EU). The  
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44 spectrograph provides a constant spectral resolution (CSR) of 6000 over a wavelength  
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46 range 220-800 nm displayable in a single spectrum. In order to obtain the best  
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48 signal-to-noise ratio, a delay time between the output-triggered signal for the laser and  
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50 the beginning scan of the spectrometer was set as 1.5  $\mu$ s with a gate width of 100  $\mu$ s.  
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“Insert Fig. 1 Here”

## 2.2. Coal ash samples and data acquisition

According to the three ash composition for coal certified reference materials (CRMs) (GSB06-2119-2007, GSB06-2121-2007, GSB06-2122-2007), forty five coal ash samples in powder form with a range of element composition were prepared by mixing the seven major reagents ( $\text{SiO}_2$ ,  $\text{Al}_2\text{O}_3$ ,  $\text{Fe}_2\text{O}_3$ ,  $\text{CaO}$ ,  $\text{MgO}$ ,  $\text{MnO}_2$ ,  $\text{TiO}_2$ ) which reach percent 95%. Table 1 lists the concentration (wt. %) of major component about 45 samples (1-15# for GSB06-2119-2007, 16-30# for GSB06-2121-2007 and 31-45# for GSB06-2122-2007). Each of employed samples was prepared for LIBS analysis separately with KBr binder. At first, 0.35 g KBr was put and flated in a stainless steel mould, followed by the pour of 0.4 g of powdered ash sample. The powder sample was compressed into a pellet with the pressure of 400 Mpa for 5min. During experiments, the pellet was mounted directly on an X-Y-Z manual micrometer stage. Due to shot-to-shot laser fluctuation, thirty laser pulses per location from each sample were accumulated in order to reduce statistical error, and obtained a measured spectrum. Ten different locations were repeated for each sample. So a total of 450 LIBS ( $45 \times 10$ ) spectra were obtained. To reduce the influence of the sample heterogeneity, ten spectra of a sample at 10 different locations were averaged into an analytical spectrum; finally we got 45 LIBS spectra ( $45 \times 1$ ).

**“Insert Table 1 Here”**

## 2.3. Wavelet neural network (WNN)

WNN is the combination of wavelet theory and neural networks<sup>22-24</sup>, the fusion

of wavelet decomposition and feed forward neural network. WNN is a new network based on wavelet transformation<sup>27</sup>, in which wavelet function is used as node activation function. It has been proposed as a novel universal tool for functional approximation, which shows surprising effectiveness in solving the conventional problems of poor convergence or even divergence encountered in other kinds of neural network. The typical network model with three layers (input, hidden and output layers) of WNN is shown as Fig.2. Here, due to excellent local performance in time-frequency domain, the Morlet wavelet function  $\psi$  is used as excitation function of hidden layer nodes instead of the traditional incentive function such as Sigmoid function. The corresponding weights of input layer to hidden layer and hidden layer threshold respectively by the adjustable parameters of wavelet function and translation parameter  $b$  is replaced, and usually a linear output layer neurons, it will be hidden layer wavelet scale is linear superposition to form the output. The dilation and translation parameters take the place of the weights of hidden layer and hidden layer threshold, respectively. Generally, output layer is linear neuron, the output can be obtained with the linear superposition of wavelet dilation coefficient. It is assumed to have  $\mathbf{p}$  samples,  $m$  is the number of input nodes, the wavelet network output as follows:

$$y^k = \sum_{i=1}^n W_i \psi \left[ \frac{\sum_{j=1}^m \omega_{ij} X_j^k - b_i}{a_i} \right]$$

$W_i$  means the weights of wavelet unit  $i$ , ( $i = 1, 2, \dots, n$ ),  $n$  is the amount of intermediate layers,  $\omega_{ij}$  is the weights connected the input  $j$ -th input  $X_j$  to the wavelet

unit  $i$ ;  $a_i$  and  $b_i$  are the dilation and translation parameters, respectively.

“Insert Fig.2 Here”

In the WNN, the Propagation Algorithm is employed, and with the error function, the values of network parameters ( $W_i$ ,  $a_i$ ,  $b_i$ ,  $\omega_{ij}$ ) can be optimized. The error function  $E$  is taken as

$$E = \frac{1}{2p} \sum_{k=1}^p (y^k - Y^k)^2$$

Where  $Y^k$  and  $y^k$  are the experimental and calculated values, respectively.

The training process and procedure of WNN as follows:

- a) Initialize the values of dilation factor  $a_i$ , translation parameter  $b_i$ , and the network connection weights  $\omega_{ij}$  and  $W_i$  with a random initial value nearby zero.
- b) Input the learning samples  $\{X_j^k\}$ , ( $k = 1, 2, \dots, p$ ) ( $j = 1, 2, \dots, m$ ),  $Y^k$ ,  $p$  and  $m$ ;
- c) Learning course of WNN. Compute the output values of the model.
- d) With the use of steepest descent method, to modify the network parameters.
- e) End the course when the error is less than the presumed value or the steps are more than the max training step, otherwise return b).

### 3 Results and discussion

#### 3.1. LIBS spectra and data pre-processing

In the collected LIBS spectra data, there are bits of interference information caused by noise and other factors. It can be seen from local amplification figure in Fig. 3 that many interference peaks exists around analysis Al. Therefore, to get useful information from large amounts of data and accurate results, the data preprocessing is a significant step for the WNN model.

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4 **“Insert Fig.3 Here”**  
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7 Here two pre-processing methods (Wavelet threshold denosing<sup>28-29</sup> and Kalman  
8 filtering<sup>30</sup>) are employed to filter the noise. The performance of the two methods are  
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10 estimated by the signal to noise ratio (SNR) and peak distortion combined with the  
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12 spectra of denoising before and after. The peak distortion can be calculated as follows:  
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$$\Delta H(\%) = |H_i - H_o|/H_o \times 100$$

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18 Here,  $\Delta H$  represents the peak distortion,  $H_i$ ,  $H_o$ , are the filtered peak intensity  
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20 and original peak intensity, respectively. In this study, the wavelet basis function db6  
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22 with hard threshold is applied, and the optimal wavelet decomposition level is 5.  
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29 **“Insert Table 2 Here”**  
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32 Table 2 shows the results of the two denoising methods. It can be concluded that the  
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34 SNR of analysis line of Al by Wavelet threshold is higher than that by Kalman  
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36 filtering, and the peak distortion by the wavelet threshold is much lower than the  
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38 Karman filter, which affect the quantitative analysis. Therefore, the wavelet threshold  
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40 is selected to filter the noise.  
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46 As data preprocessing, input variable is also important for the WNN model. It  
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48 can affect the convergence rate and the result of quantitative analysis of the neural  
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50 network. As seen from Fig.3, the most spectra lines of major elements in coal ash are  
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52 distributed in the range of 200-500 nm, which contains key features of the specific  
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54 element, so the spectra of the feature band (200-500 nm) can be selected as input  
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56 variable. Principal component analysis (PCA)<sup>31-32</sup> as a popular data compression  
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4 method can not only guarantee the accuracy of the input data and reduce the training  
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7 time, but also can simplify network structure for WNN. The optimal principal  
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10 component (PC) is obtained based on the variance captured. Table 3 shows the  
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13 contribution rate of eleven principal components. It can be seen that the variance  
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16 captured can be up to 99.97%, when the PC is 9. So the nine principle components are  
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19 selected as input variable for quantitative analysis.

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21 **“Insert Table 3 Here”**  
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24 Here, the full spectra, the feature band and PC are all used as input variables to  
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27 construct the model. The performances of WNN model with different input variables  
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30 are investigated by correlation coefficient (R), root mean square error (RMSE) and  
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33 time. Table 4 list the results of different input variables, It can be seen that the R  
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36 obtained by the full spectra, feature band and PC are 0.8973, 0.9468 and 0.9850,  
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39 respectively. They both show better liner relationship than the full spectra. However,  
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42 the RMSE (0.0354) generated by the PC is smaller than feature band, and take much  
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45 less training time. This result owed much to the major information extracted  
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48 accurately from huge LIBS spectra data by PCA. It can eliminate the interference from  
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51 other information, and improve the robustness and quantitative performance of WNN  
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54 calibration model. Thus, the extracted components are regarded as the input variable to  
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57 construct the model for the analysis of ash content.

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59 **“Insert Table 4 Here”**  
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### 3.2. Quantitative analysis of major component of coal ash

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4 Coal ash is a complex sample containing many chemical elements and thus related  
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7 to LIBS spectra characterized by hundreds of atomic lines. The extracted components  
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10 are used as the input variable to construct the model for the quantitative analysis of coal  
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13 ash. The data set was divided into calibration set and prediction set. 36 samples (1-4#,  
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15 6-9#, 11-14#, 16-19#, 21-24#, 26-29#, 31-34#, 36-39#, 41-44#) were selected as  
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18 calibration set for the construction of calibration model and the rest samples (5#, 10#,  
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21 15#, 20#, 25#, 30#, 35#, 40#, 45#) was used as prediction set.  
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24 Before constructing the WNN model, the WNN model parameters (NHN, NI, LR  
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26 and the momentum) are need to be optimized by the gradient descent method<sup>33</sup> based  
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29 on RMSE. Fig.4a shows the RMSE against the number of neurons in the hidden layer  
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32 for the calibration set. It can be seen that the optimized NHN is 9 based on the minimum  
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35 RMSE for the calibration set to prevent the over-fitting of the model. The RMSE  
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38 against different NI, LV and the momentum are also plotted in Fig.4. It can be seen  
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41 from Fig. 4b that the RMSE decreases sharply when the NI is in the range of 100-200.  
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44 However, with the increase of the NI, the RMSE decreases gradually. When the NI is  
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47 600, the RMSE is the lowest. So the optimum NI is 600. From Fig.4c and Fig.4d, based  
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50 on the minimum RMSE, the LR and the momentum are selected to be 0.005 and 0.06,  
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53 respectively. For fair comparison WNN and ANN, the same parameters of ANN were  
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56 optimized based on RMSE. The NHN, NI, LR and the momentum are 10, 6000,  
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59 0.05 and 0.9, respectively.  
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4 Under the optimized WNN and ANN parameters, the WNN and ANN model  
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7 were constructed using 36 training samples. The predictive ability of WNN and ANN  
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10 calibration model for coal ash was validated by 5-folds cross validation (CV). Fig.5  
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12 shows the RMSE and R of major component in coal ash by WNN and ANN calibration  
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14 model. It can be seen that the RMSE of major component obtained by WNN model is  
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16 lower than that by ANN calibration model. Moreover, the R of major components  
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18 obtained by WNN model is much larger than ANN. Therefore, the results show that the  
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24 WNN model for coal ash is better than ANN.

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27 Based on calibrated WNN and ANN model, the quantitative analysis of coal ash  
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29 was performed. The performance of WNN and ANN model in terms of RMSE and R  
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31 were shown in Table 5. As it can be seen, the RMSE of major component in coal ash by  
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34 WNN model is obvious lower than by ANN model and the R of the major components  
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36 by WNN is higher than ANN. For  $\text{SiO}_2$ ,  $\text{Al}_2\text{O}_3$ , and  $\text{Fe}_2\text{O}_3$ , the two methods show  
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38 good linear relationship, while the RMSE obtained by WNN is lower than that by  
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41 ANN. For  $\text{MnO}_2$ , the R obtained by WNN significantly improved from 0.5815 to  
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44 0.9839,  $\text{MgO}$  and  $\text{TiO}_2$  are the same. In addition, the time of WNN model is much less  
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47 than that of ANN model. Therefore, the WNN model for coal ash samples was superior  
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52 to the method of ANN on convergence speed and prediction precision.

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55 **“Insert Fig.4 Here”**

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58 **“Insert Fig.5 Here”**

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60 **“Insert Table 5 Here”**

#### 4. Conclusions

In this work, the quantitative analysis of coal ash was completed by means of LIBS technique combined with WNN model. The LIBS spectra were preprocessed by wavelet transform. The extracted principal components by PCA as input variable were used to construct the WNN model, and the optimized number of hidden layer neural, iterations, the learning rate and the momentum were optimized by the gradient descent method based on the RMSE. In terms of RMSE, R and training time, the WNN model for quantitative analysis of coal ash presents a better performance than that of ANN. This work reveals the capability of the WNN in modeling, and it can be concluded that LIBS technique coupled with WNN method based on PCA is a promising and potential approach for combustion process control even in online mode.

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15 **Captions:**  
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18 **Fig.1 LIBS experimental set-up for coal ash**  
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21 **Fig.2 The WNN structure**  
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24 **Fig.3 The averaged spectrum of the 20# in the range 200-500 nm**  
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27 **Fig.4 Variation of RMSE vs. (a) NHN, (b) NI, (c) LR and (d) different values of**  
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29 **momentum**  
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32 **Fig.5 The performance of WNN and ANN calibration model with 5-fold**  
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34 **cross-validation**  
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**Table 1. The concentration (wt %) of the major components in coal ash samples**

Sample number	SiO <sub>2</sub>	Al <sub>2</sub> O <sub>3</sub>	Fe <sub>2</sub> O <sub>3</sub>	CaO	MgO	MnO <sub>2</sub>	TiO <sub>2</sub>
1#	15.76	7.30	39.48	18.09	5.87	0.48	0.30
2#	15.42	7.23	39.44	18.06	5.97	0.41	0.29
3#	15.52	7.44	39.75	17.93	6.18	0.47	0.27
4#	15.56	7.37	39.76	18.39	5.98	0.48	0.26
5#	15.95	7.41	39.84	18.09	6.12	0.47	0.27
6#	15.74	7.22	39.83	18.63	9.19	0.45	0.28
7#	15.65	7.35	39.64	18.02	5.99	0.42	0.27
8#	15.43	7.20	39.74	18.16	5.90	0.44	0.22
9#	15.93	7.28	39.18	17.90	6.00	0.48	0.30
10#	15.58	7.39	39.89	18.72	6.29	0.45	0.29
11#	15.94	7.26	39.64	18.69	6.03	0.46	0.25
12#	15.86	7.29	39.58	18.58	5.83	0.48	0.31
13#	15.61	7.37	39.80	18.64	6.08	0.47	0.30
14#	15.56	7.41	39.32	18.74	6.03	0.45	0.22
15#	15.47	7.26	39.51	18.08	6.27	0.46	0.28
16#	37.18	32.73	4.61	10.28	1.16	0.028	1.41
17#	37.73	33.09	4.83	10.68	1.21	0.021	1.38
18#	37.54	32.78	4.73	10.11	1.17	0.016	1.24
19#	37.32	32.46	4.72	11.20	1.19	0.029	1.23
20#	37.93	32.40	4.91	10.94	1.14	0.040	1.39
21#	37.61	32.83	4.67	10.83	1.27	0.024	1.26
22#	37.22	32.70	4.81	11.21	1.07	0.025	1.41
23#	37.36	32.97	4.65	10.84	1.15	0.017	1.31
24#	37.69	32.89	4.84	11.05	1.20	0.020	1.25
25#	37.76	32.98	4.82	10.86	1.18	0.022	1.31
26#	37.34	32.67	4.70	11.09	1.13	0.019	1.38

27#	37.53	32.88	4.81	10.85	1.22	0.021	1.30
28#	37.16	32.99	4.79	11.19	1.16	0.016	1.40
29#	37.56	32.56	4.89	10.93	1.20	0.017	1.32
30#	37.28	32.95	4.76	11.01	1.24	0.026	1.38
31#	47.85	35.86	2.71	3.23	0.64	-	1.28
32#	48.19	36.08	2.88	3.36	0.76	-	1.38
33#	47.87	35.89	2.75	3.27	0.74	-	1.27
34#	47.66	35.85	2.91	3.24	0.72	-	1.36
35#	47.86	35.95	2.86	3.30	0.73	-	1.35
36#	48.28	36.13	2.90	3.19	0.71	-	1.34
37#	48.13	36.00	2.71	3.34	0.75	-	1.27
38#	47.66	35.88	2.85	3.29	0.67	-	1.24
39#	48.22	35.70	2.83	3.39	0.68	-	1.35
40#	47.72	35.95	2.89	3.25	0.72	-	1.20
41#	48.04	35.67	2.84	3.23	0.75	-	1.38
42#	48.01	36.71	2.86	3.24	0.74	-	1.24
43#	47.92	35.91	2.74	3.23	0.71	-	1.35
44#	48.23	35.97	2.73	3.28	0.69	-	1.19
45#	47.68	35.71	2.72	3.25	0.74	-	1.32

**Table 2. SNR and peak distortion of different methods**

Denoising method	SNR	$\Delta H$ (%)
Original spectra	5.37	-
Wavelet threshold	5.51	4.9
Kalman filtering	2.55	54.7

**Table 3. The contribution rate of eleven principal components**

PC	Contribution (%)	Cumulative contribution (%)
1	90.69	90.69
2	1.45	92.14
3	1.35	93.49
4	1.31	94.80
5	1.08	95.88
6	1.05	96.93
7	1.02	97.95
8	1.01	98.96
9	1.01	99.97
10	0.01	99.98
11	0.00	99.99

**Table 4. The result of WNN with different input variables**

Input data	R	RMSE	Time(s)
Full spectra	0.8973	0.0854	900
200-500nm	0.9468	0.0535	480
PC	0.9850	0.0354	2

**Table 5. The prediction performance of WNN and ANN for coal ash sample**

Component	WNN			ANN		
	R	RMSE	Time(s)	R	RMSE	Time(s)
SiO <sub>2</sub>	0.9967	0.2591		0.8844	0.6650	
Al <sub>2</sub> O <sub>3</sub>	0.9979	0.1129		0.9305	0.7678	
Fe <sub>2</sub> O <sub>3</sub>	0.9992	0.0934		0.9248	0.8867	
CaO	0.9725	0.1672	14	0.9531	0.1970	27
MgO	0.9989	0.0231		0.7706	0.1621	
MnO <sub>2</sub>	0.9839	0.0028		0.5815	0.0209	
TiO <sub>2</sub>	0.9802	0.0080		0.7694	0.0414	

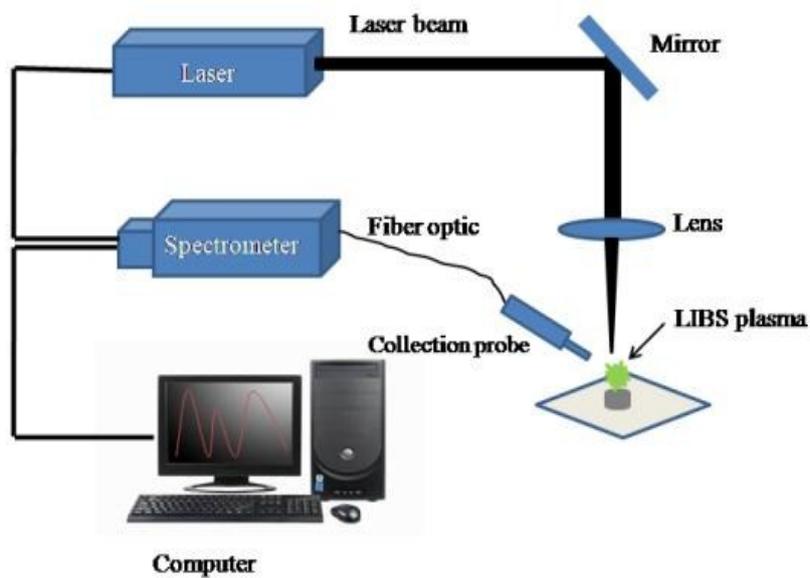
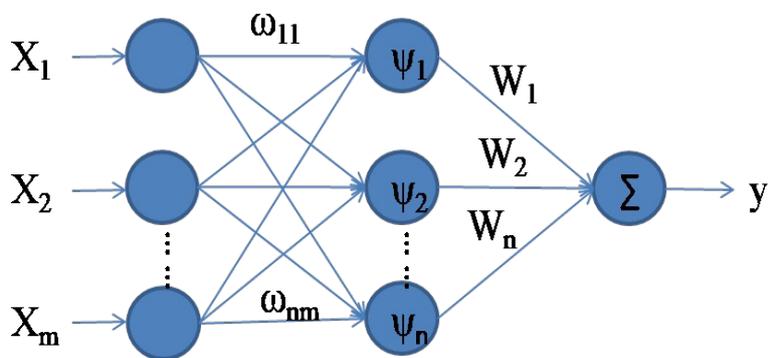


Fig.1



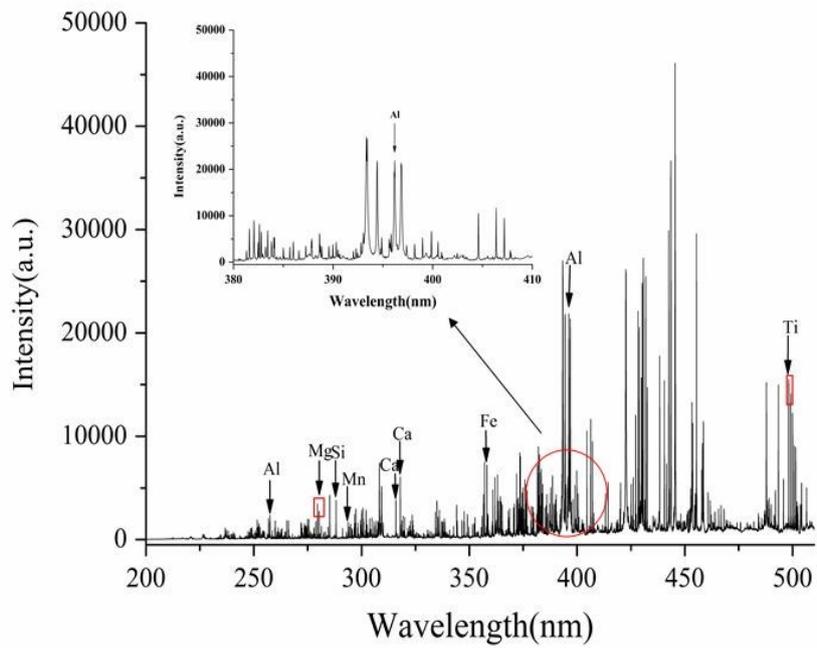


Fig.3

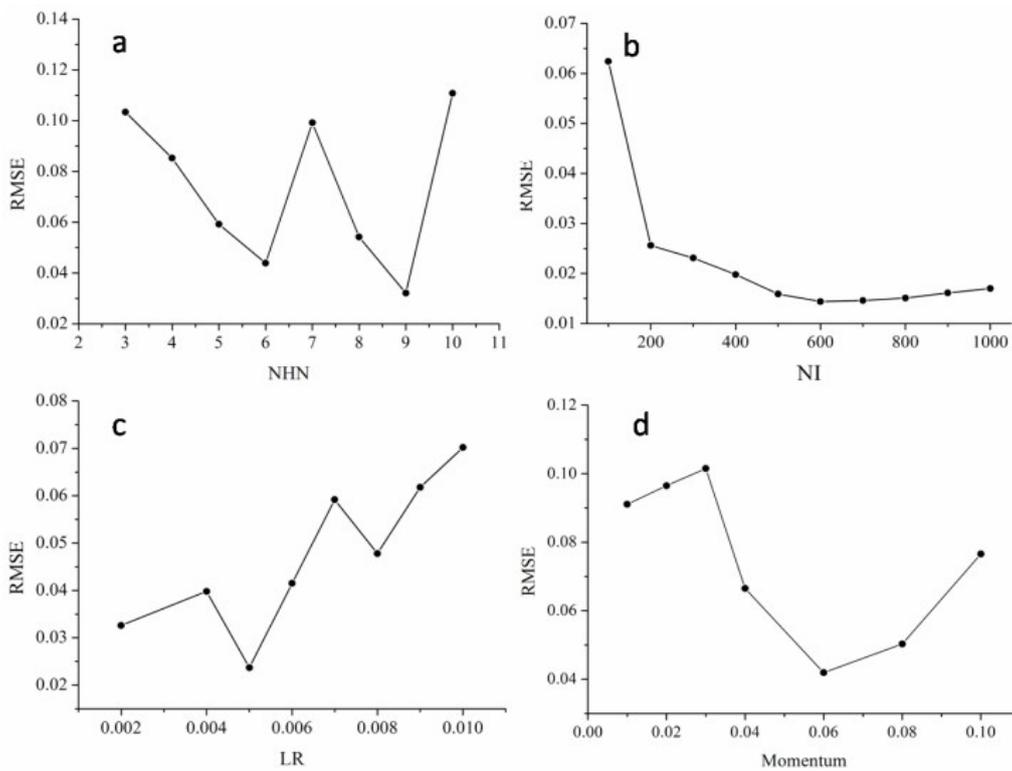


Fig.4

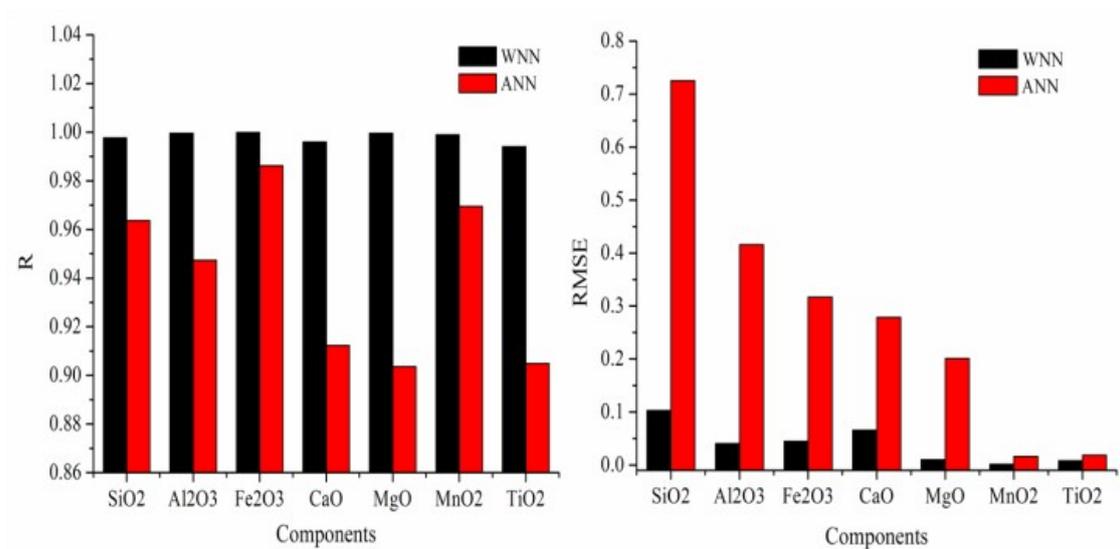
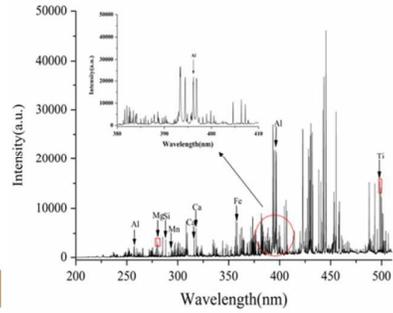


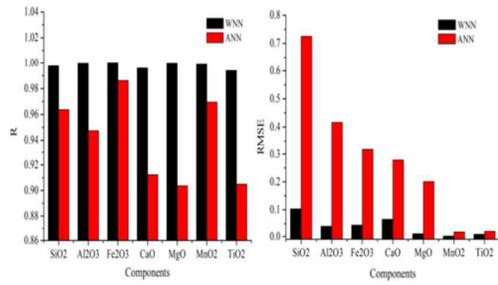
Fig.5



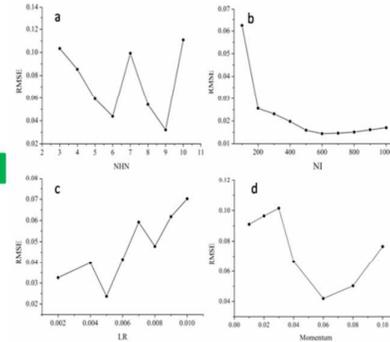
LIBS



Parameter optimization



WNN  
ANN



Laser induced breakdown spectroscopy (LIBS) technique combined with wavelet neural network (WNN) was proposed for the quantitative analysis of the major components of coal ash.

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