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## **ARTICLE TYPE**

## Classification of different types of slag samples by Laser-induced breakdown spectroscopy(LIBS) coupled with random forest based on variable importance(VIRF)

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Laser induced breakdown spectroscopy(LIBS) technique coupled with random forest based on variable importance(VIRF) was proposed to perform classification analysis of slag samples. Three types of slag samples(open-hearth furnace slag, converter slag and high titanium slag) were identified and classified by 10 random forest(RF) method with different pre-processing methods(normalized with maximum integrated intensity, first-order derivative and second-order derivative) and different input variables(200-300, 200-400, 200-500, 200-600, 200-700 and 200-800nm), the importance of input variable was employed to improve the classification performance of RF model for slag samples. Averaged OOB(out-of-bag) error, sensitivity, specificity and accuracy were calculated to evaluate the classification performance of RF

15 model for slags. Normalized by maximum integrated intensity LIBS spectra(200-500nm) of slag samples as input variable was constructed the PLS-DA, SVM, RF and VIRF model for the classification analysis of slags. VIRF model shows a better classification performance than other three model. LIBS technique coupled with RF perhaps is a promising approach to achieve the online analysis and process control of slag and even industrial waste recycling.

#### 20 1. Introduction

In steel-making industry, a large amounts of solid co-products is generated in the form of slag and sludge. The world's annual output of slag from iron and steel industries reaches almost 50 million tons.<sup>1</sup> Slag as an significant byproduct in steel industry 25 plays a decisive role in ensuring smelting operation smoothly, steel quality, metal recovery and so on. There are different types of steel industry slags such as blast furnace slag (BF) also called iron slag, basic oxygen furnace slag (BOF), electric arc furnace acid slag (EAF), ladle furnace basic slag (LF) also called refining 30 slag and so on. Slag can be divided into smelting slag, refining slag and synthetic slag according to the difference of metallurgical process; it can be also divided into acid slag, neutral slag and alkaline slag. The major component of slag include CaO, SiO<sub>2</sub>, Al<sub>2</sub>O<sub>3</sub>, MgO, Fe<sub>2</sub>O<sub>3</sub>, TiO<sub>2</sub> and so on. Each 35 type of slag has its typical chemical, mineralogical, and physical properties. Classification and identification of slag contributes to recycling and reuse of metallurgical waste. There are many significant applications on slag such as blast furnace slag can be used as a cement raw material, high phosphorus slag can be used 40 as a fertilizer, vanadium slag can be used as raw materials for the refining of vanadium, and so on. V. Gupta<sup>2</sup> focused on the reuse of slag material as low cost adsorbents for water treatment.

Slag analysis was performed by different techniques<sup>3,4</sup> such as chemical analysis, X-ray fluorescence(XRF), inductively 45 coupled plasma optical emission spectroscopy(ICP-OES), mass spectroscopy(MS) and so on. However, these approaches require complicated sample preparation and much analysis time, which fails to timely obtain the information of steel product, and even hinders their application for real time and fast analysis. Laser

- 50 induced breakdown spectroscopy(LIBS) is a promising and prospect analytical technique based on laser plasma spectroscopy with the advantages of multiple elements simultaneous analysis for all types of the samples(solid, liquid, gas or aerosol).<sup>5-7</sup> At present, the LIBS technique has become the subject of
- 55 metallurgical analysis.<sup>8-10</sup> The application of LIBS technique to metallurgical industry includes iron ore selection,<sup>11,12</sup> process control,<sup>13,14</sup> iron slag analysis<sup>15-18</sup> and so on.

Classification and identification of slag has been the subject of most government environmental agencies in the world.  $^{19,20}$  The

- 60 classification of slags by LIBS can be fulfilled depends on difference of its major component and corresponding concentration. In other words, it was completed by the difference comes from spectra integrated intensity and wavelength of LIBS spectra. The LIBS technique combined with chemometrics
- 65 methods is an effective approach to improve the classification performance of slags. Zhang et al<sup>20</sup> employed LIBS coupled with partial least squares discriminant analysis(PLS-DA) to classify open-hearth furnace slag and high titanium slag. However, PLS-DA has some disadvantages such as low classification accuracy
- 70 and overfitting. Random Forest(RF), a new classification algorithm based on multiple classifier, was proposed by Leo Breiman<sup>21</sup>. It is an ensemble of unpruned classification tree created by using bootstrap samples of the training data and random feature selection in tree introduction. Prediction was

completed by the majority vote of multiple classifiers to determine the final category for the test samples. The train dataset was used to construct the multiple classifier, and the final category of the predictive sample are determined by the major 5 vote of the classification results for each classifier. It has proved that RF classifier has a good tolerance for noise, as well as avoid over-fitting phenomenon.<sup>22</sup> In addition, LIBS combined with RF was applied for identification and classification of rocks, pen ink and iron ore samples.<sup>23,24</sup> LIBS combined with RF also could be 10 used for the quantitative analysis of multiple elements in fourteen steel samples.25

12 The present work explores the combination of LIBS technique 13 and RF based on variable importance(VIRF) for classification 14 analysis of slags. A series of 60 slag samples were compressed 15 15 into pellets and prepared for LIBS measurement. Three types of 16 slag samples(open-hearth furnace slag, converter slag and high 17 titanium slag) were identified and classified by RF method with 18 different pre-processing methods (normalized with maximum 19 integrated intensity, first-order derivative and second-order 20 20 derivative) and different input variables(200-300, 200-400, 200-21 500, 200-600, 200-700 and 200-800nm), the variable importance 22 was employed to improve classification performance of RF 23 model for slag samples. Averaged OOB(out-of-bag) error, 24 sensitivity, specificity and accuracy were calculated to evaluate 25 25 the classification performance of RF model for slags. 26

#### 2. Methodology

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#### 2.1. LIBS setup and acquisition conditions

29 The detailed description of LIBS setup was shown in the 30 previous works.<sup>29</sup> A Q-switched Nd: YAG laser( $\lambda$ =1064nm, 10 31 30 ns pulse FWHM, 80 mJ/pulse, repetition rate of 5 Hz) was used 32 to generate the plasma in air at atmosphere pressure on the 33 pellets. The pulse laser beam was focused onto the slag sample 34 surface vertically by a 50mm focal-distance lens, which was 35 generated a spot of about 0.2 mm diameter. The emission from 36 35 the plasma created was collected with a 4-mm aperture, with a 37 7mm focus fused silica collimator placed at 45° angel with 38 respect to the laser pules and a distance of 3 cm from the sample, 39 and then focused into an optical fiber, which was coupled to the 40 entrance of the Echelle spectrometer Aryelle 400(LTB, German). 41 40 The spectrometer provides a constant spectral resolution (CSR) 42 of 6000 over a wavelength range 200-800nm displayable in a 43 single spectrum. An electron-multiplying CCD(EMCCD) camera 44 (OImaging, UV enhanced, 1004 ×1002 Pixels, USA) coupled to 45 the spectrometer was used for detection of the dispersed light. 46 45 The overall linear dispersion of the spectrometer camera system 47 ranges from 37 pm/pixel(at 220nm) to 133 pm/pixel (at 800nm). 48 To prevent the EMCCD from detecting the early plasma 49 continuum, a mechanical chopper is used in front of the entrance 50 slit. The experiments were carried out under atmosphere 51 50 condition, and the gate width of spectrometer was set to 2 ms. 52 The detector was set to 1.5 µs delay time between the laser pulse 53 in order to prevent the detection of bremsstrahlung radiation.

#### 2.2. Slag samples and LIBS measurements

55 A total of 60 slag samples for three types of slag(open-hearth 56 55 furnace slag(OHFS), converter slag(CS) and high titanium 57 slag(HTS)) were provided by Pangang group Chengdu ore & 58 steel Co., Ltd(China) in the form of slag powder. Each slag 59

Table 1 The concentration(wt%) of the major components in slag samples

slags	Fe <sub>2</sub> O <sub>3</sub>	SiO <sub>2</sub>	TiO <sub>2</sub>	CaO	MgO	MnO <sub>2</sub>	Al <sub>2</sub> O <sub>3</sub>
open-hearth	16.15-	16.41-	0.40-	20.56-	15.68-	12.35-	6.18-
furnace slag	19.66	20.22	1.06	27.81	21.27	15.85	7.80
converter	13.96-	12.05-		47.95-	8.01-		0.69-
slag	14.88	12.66		48.38	8.38		0.95
high titanium	2.90-	2.12-	81.57-	0.43-	2.52-	1.07-	3.29-
slag	5.98	4.20	85.57	0.77	3.05	1.45	3.97

60 sample was homogenized to produce a very fine powder until all of the powder passed through a 200-mesh stainless steel sieve using a ball grinding mill. Table 1 lists the concentration(wt. %) of major component of three types of slag samples. There are 20 slag samples for each type of slags. The slag pellet was made

65 with a tablet press at 400 Mpa for 5 min. LIBS spectra of 20 different position of each sample surface are gathered. In order to decrease the effects of shot to shot fluctuations, each measure spectrum was obtained by accumulation of 50 laser pulses. The total of the spectra for 60 slag sample was 1200(20 LIBS spectra

70 for each slag sample). The training set and test set were selected by Kennard-Stone algorithm<sup>26</sup> with the ratio of the number of train samples to the whole data is 0.7. The number of training samples is 42, and the number of test samples is 18. The data processing and classification analysis of slag samples were 75 performed on Matlab2007a(Mathworks).

#### 2.3 Random forest(RF)

RF is an advanced classification and regression method based on statistical learning theory. A resampling technique based on bootstrap method was used to continuously generates training

- 80 and test samples; the training sample generates multiple classification tree form with random forest, the final predictions results based on the combination are received by a simple majority voting of the single classification tree. The process of RF training model described in previous work.<sup>27</sup> There are two
- 85 significant parameters in RF: (1) the number of ensemble trees in the forest (ntree) and (2) the number of peaks randomly selected as the candidates for splitting at each node  $(\mathbf{m}_{try})$ . The ideal random forest model not only has higher classification accuracy and stability, but also has higher efficiency. Theoretically, the
- 90 generalization error of the classifier tends to a finite upper bound when ntree reaches a certain value. In other words, if ntree is increased above the optimum, there is a general increase in the computational expense, but the results do not improve significantly. In this work, ntree was set as 500. m<sub>try</sub> is one of
- 95 the most major characteristic through each division that introduces random nodes for randomly selected attributes. It was assumed that there were M attributes(wavelengths) in the training sample, and  $\mathbf{m}_{try}$  attributes were extracted randomly as candidate attribute between each of the internal nodes in the
- 100 decision tree ( $m_{try} \ll M$ ). ntree and  $m_{try}$  for the RF model can be optimized by the OOB error estimation. Moreover,  $m_{try} =$  $\sqrt{M}$  was found to be the best choice based on the OOB error rate.21

A significant characteristic of RF is able to calculate and rank 105 the importance of each variable(the LIBS spectral peaks). For each tree grown in RF, OOB was put down and the number of votes cast for the correct class was counted. The value of variable m in OOB was randomly permuted and these samples

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**Fig. 1** Representative LIBS spectra of slag samples, black line for HTS; red line for OHFS; green line for CS.

were put down the tree. The numbers of votes were counted for 5 the correct class in the variable-m-ranked OOB data; and then, we again count the number of votes for the correct class in the untouched OOB data. Subtracting the two counts, and averaging this number over all the trees in the forest is the raw importance score for the variable. Finally, the important scores were

10 computed depending on the correlations between the trees, in other words, it was obtained depend on the contribution of input variable to classification result. The process of random forest based on variable importance(VIRF) model as follows: (1) Suppose there is original spectra *A*, and original spectra is used

- 15 to construct random forest classification model. (2) Calculate variable importance of each variable for classification analysis based on OOB error. (3) Remove the variable of variable importance is zero, and generate a new input variable **B**. (4) Input variable **B** is used to construct VIRF classification model.
- 20 The averaged OOB error, sensitivity, specificity and accuracy are the statistical parameters to evaluate the performance of RF model for slag samples. Averaged OOB error are calculated by an estimate of the error rate (ER) for classification analysis of RF.<sup>26</sup> The sensitivity is the percentage of the samples of a
- 25 category accepted by the class model. The specificity is the percentage of the samples of the categories which are different from the modeled one, rejected by the class model. The accuracy of classification procedure is expressed as fraction of correctly classified samples to the total samples.<sup>28</sup>

#### 30 3. Results and discussion

#### 3.1. LIBS spectra of three types of slag samples

Fig 1 shows the averaged spectrum of three types of slags in the range of 200-800nm, which includes the emission lines of the major component in slag. Slag is complex sample containing 35 many chemical elements and thus related to LIBS spectra characterized by hundreds of atomic lines. There is obvious difference between the averaged LIBS spectrum with the range of 200-500nm and 580-650nm on three types of slags, which contributes to classification and identification of three types of

40 slags. The differences among three types of slags come from the concentration of TiO<sub>2</sub>, CaO, MnO<sub>2</sub> and Al<sub>2</sub>O<sub>3</sub>. Spectral lines of major element(Ca, Si, Al, Mg, Fe, Mn and Ti) in slag sample were detected and identified based on NIST atomic database.<sup>29</sup> For high titanium slag, the concentration of its major component-

45	Table 2	2 The	RF	training	model	for	the	classification	of slags	
	with dif	ferent	pre-	processir	ng meth	od				

Pre-processing method	Averaged OOB error	Sensitivity	Specificity	Accuracy
without pre-processing	0.0050	0.9952	0.9976	0.9968
Normalization	0.0001	1.0000	1.0000	1.0000
first-order derivative	0.0011	1.0000	1.0000	1.0000
second-order derivative	0.0016	1.0000	1.0000	1.0000

 Table 3 The RF training model for the classification of slags with different input variables

Input variable	Averaged OOB error	Sensitivity	Specificity	Accuracy
200-300nm	0.0097	0.9905	0.9952	0.9937
200-400nm	0.0012	1.0000	1.0000	1.0000
200-500nm	0.0002	1.0000	1.0000	1.0000
200-600nm	0.0046	0.9952	0.9972	0.9968
200-700nm	0.0052	0.9952	0.9976	0.9968
200-800nm	0.0050	0.9952	0.9976	0.9968

TiO<sub>2</sub> is over than 80%; the convert slag is given priority to CaO,

50 and there are no  $TiO_2$  and  $MnO_2$  in convert slag; the proportion of MgO and  $MnO_2$  of open-hearth slag is larger than high titanium slag and convert slag. Therefore, classification analysis of slags could be brought out by the differences of specific components for each type slag.

## 55 3.2. RF model with different pre-processing methods and input variables

An excellent training model with appropriate pre-processing methods and input variables is essential for the classification analysis of slag using LIBS and RF. In order to improve the

- 60 classification performance of RF model, the input variables addressed by pre-processing method(i.e. normalization) was used to decrease the differences comes from laser pulse energy fluctuations and increase the comparability among the different types of slags. Normalization is an effective method for
- 65 eliminating the differences comes from laser pulse energy fluctuations, and derivation can be used to increase the comparability among the different types of slags. In this work, the RF training model for the classification of slags with the whole spectra(200-800nm) as input variable by different pre-
- 70 processing methods was shown in Table 2. As seen from Table 2, sensitivity, specificity and accuracy of RF training model with three pre-processing methods(Normalized by maximum integrated intensity, First-order derivative and Second-order derivative) were higher than the RF model without pre-
- 75 processing, meanwhile, the averaged OOB error of RF training model with three pre-processing methods is lower than the RF model without pre-processing. For three pre-processing method, all of three RF models show well classification performance, sensitivity, specificity and accuracy were 1.0000, 1.0000 and
- 80 1.0000, respectively; however, the averaged OOB error of RF model with normalized by maximum integrated intensity is lower than with first-order derivative and second-order derivative. Therefore, the LIBS spectra with normalized by maximum integrated intensity as input variable were employed to construct
- 85 RF training model for the classification analysis of three types of slags.

Input variables are also significant for the training model of slags. In this work, the RF training model for the classification of





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Fig. 2 The relationship between the variable importance of RF model and LIBS spectra(200-500nm) of slags

Table 4 Classification result of PLS-DA, SVM, RF and VIRF 5 model for slags

19 20	RF model	OOB error	Sensitivity	Specificity	Accuracy
20 21	PLS-DA	0.0733	0.9253	0.9189	0.9227
22	SVM	0.0511	0.9364	0.9344	0.9353
23	RF	0.0333	0.9667	0.9833	0.9778
24	VIRF	0.0111	0.9889	0.9944	0.9926

25 slags with different input variables(200-300, 200-400, 200-500, 26 200-600, 200-700 and 200-800nm) was investigated by averaged 27 OOB error, sensitivity, specificity and accuracy. Table 3 shows 28 the averaged OOB error, sensitivity, specificity and accuracy for **29** 10 RF training model for the classification of slags with different 30 input variables. As seen from Table 3, it can be obtained a well 31 RF training model with different input variables. All of 32 sensitivity, specificity with six RF model were over than 0.9900, 33 and all of averaged OOB error were under 0.01. However, the 34 15 averaged OOB error of RF training model with the input 35 variable(200-500nm) is lowest, and the same time, it takes the relative less time and improves the RF efficiency of 36 classification analysis based on RF. The LIBS spectra with the 37 range of 500-800nm doesn't contribute to the classification for 38 20 slags, there is no change for sensitivity, specificity and accuracy 39 of RF model with the input variables(200-600, 200-700 and 200-40 800nm). Although there are a rich spectral information for the 41 whole spectra(200-800nm), it takes a longer time to construct the 42 RF training model. For the LIBS spectra of 200-300 and 200-43 44 25 400nm, there are less LIBS spectral information, and fails to obtain a better classification result of RF model for slags. 45 Therefore, the LIBS spectra with range of 200-500nm were 46 selected as input variable to construct the RF training model for 47 slag samples. 48

#### 30 3.3. RF model with variable importance for the classification 49 of slags 50

Variable importance of RF model can be obtained by using 51 OOB data. The greater the variable importance of RF model is 52 obtained, the better the classification performance of slags, and 53 35 vice versa. Fig 2 shows the relationship between the variable 54 importance of RF model and LIBS spectra(200-500nm) of slags. 55 The majority variable importance of LIBS spectra(200-500nm) 56 on RF model for classification analysis of slags is 0-0.15. Some 57 variable importance is 0, in other words, the LIBS spectral peaks 58 40 of variable importance equals to zero that doesn't contribute to 59

the classification of slags. Hence, we can remove the LIBS spectral peaks of variable importance equals to zero, and extract the spectral peaks of variable importance over zero in order to improve the classification performance of slags based on RF. In 45 order to validation the classification abilities of VIRF model for

slags, we compared the VIRF model with PLS-DA, support vector machine(SVM) and RF method. Input variables of these four methods for training model are the LIBS spectrum(200-500nm). For the training model based on PLS-DA, the best latent

- 50 variables optimized by 5-fold cross-validation is 10. When the PLS-DA model was trained upon the training set, the averaged classification accuracy is 97%. For SVM training model, the best parameters selected by genetic algorithm(GA) were used as input for an epsilon classification SVM with a radial basis
- 55 function(RBF) kernel. The optimum parameters were set as: penalty parameter C = 98.25 and kernel parameter of RBF g = 0.08. The averaged classification accuracy is 95% for optimized SVM training model. Table 4 lists the classification result of PLS-DA, SVM, RF and VIRF model. The classification
- 60 performance of VIRF model is better than conventional RF model. Sensitivity, specificity and accuracy of VIRF model is larger than other three model, meanwhile, its averaged OOB error is less than other three model. Hence, VIRF model shows a better classification performance for slag samples.

#### 65 **Conclusions**

In summary, LIBS technique coupled with RF has been successfully used for the classification of 60 slag samples. Normalized by maximum integrated intensity LIBS spectra(200-500nm) of slag samples as input variable was constructed the 70 PLS-DA, SVM, RF and VIRF model for the classification analysis of slags. VIRF model shows a better classification performance than other three model. It has been confirms that LIBS technique coupled with RF is promising approach to achieve the online analysis and process control of slag and even

75 industrial waste recycling.

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### Notes and references

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**Analytical Methods Accepted Manuscript** 



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