

# Analyst

Accepted Manuscript



This is an *Accepted Manuscript*, which has been through the Royal Society of Chemistry peer review process and has been accepted for publication.

*Accepted Manuscripts* are published online shortly after acceptance, before technical editing, formatting and proof reading. Using this free service, authors can make their results available to the community, in citable form, before we publish the edited article. We will replace this *Accepted Manuscript* with the edited and formatted *Advance Article* as soon as it is available.

You can find more information about *Accepted Manuscripts* in the [Information for Authors](#).

Please note that technical editing may introduce minor changes to the text and/or graphics, which may alter content. The journal's standard [Terms & Conditions](#) and the [Ethical guidelines](#) still apply. In no event shall the Royal Society of Chemistry be held responsible for any errors or omissions in this *Accepted Manuscript* or any consequences arising from the use of any information it contains.

1  
2  
3 **Contribution of rotational diffusivity towards the transport of antigens in**  
4  
5  
6 **heterogeneous immunosensors**  
7  
8  
9

10  
11  
12 **Dharitri Rath<sup>1,2</sup> and Siddhartha Panda<sup>1,2,3,\*</sup>**  
13  
14

15  
16 <sup>1</sup>Department of Chemical Engineering,  
17

18 <sup>2</sup>Centre for Environmental Sciences and Engineering,  
19

20 <sup>3</sup>Samtel Centre for Display Technologies,  
21

22 Indian Institute of Technology Kanpur,  
23  
24

25 Kanpur - 208 016, UP, India  
26  
27  
28  
29  
30  
31

32 \* Corresponding author  
33

34 Tel: +91-512-259-6146  
35

36 Fax: +91-512-259-0104  
37  
38

39 E-mail: spanda@iitk.ac.in  
40  
41  
42  
43  
44  
45  
46  
47  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60

**ABSTRACT**

Higher capture efficiency in heterogeneous immunosensors is desirable for the detection of cancer biomarkers at low concentrations. The process of the capture of these antigens is transport limited since the rates of the antigen/antibody reactions are faster. In case of non-flow systems, the diffusive transport has contributions from both translational and rotational phenomena. Since the contribution of the rotational diffusivity is comparatively less explored in literature, we have studied the same for three antigens- bovine serum albumin (BSA), prostate specific antigen (PSA) and C-reactive proteins (CRP). We quantified the rotational diffusivities using the time resolved fluorescence anisotropy method, and further quantified the contribution of the rotational diffusivities to the overall diffusivity of the antigens, and also studied the effect of the process parameters- temperature and pH of the solution. With increase in temperature, the rotational diffusivity increased showing an Arrhenius dependency while with the variation of pH, it showed a non-monotonic behavior having maxima closer to the isoelectric point of the corresponding antigens. This interesting behavior of the pH values could be attributed to lesser electro-viscous effects when the antigen molecule is neutral around its isoelectric point. The optimization of the pH and temperature for the immunosensors could be utilized to design efficient immunosensors.

**Keywords:** Immunosensors; Fluorescence anisotropy; Rotational diffusivity; Antigens.

**Nomenclature**

1		
2		
3		
4		
5		
6		
7	$C$	Concentration of antigen in the solution at any time (mol/m <sup>3</sup> )
8		
9	$D_{eff}$	Effective diffusivity of the antigen in the solution (m <sup>2</sup> /s)
10		
11	$D_{trans}$	Translational diffusivity of the antigen in the solution (m <sup>2</sup> /s)
12		
13		
14	$D_{rot}$	Rotational diffusivity of the antigen in solution (1/s)
15		
16	$D_{rot}'$	Contribution of rotational diffusivity to $D_{eff}$ (m <sup>2</sup> /s)
17		
18	$D_{0,rot}$	Pre-exponential factor in the Arrhenius dependency of $D_{rot}$ (m <sup>2</sup> /s)
19		
20		
21	$E_{a,rot}$	Activation energy for $D_{rot}$ (KJ/mol)
22		
23	$G$	G-factor for the sensitivity of the instrument
24		
25		
26	$k_B$	Boltzmann constant (J K <sup>-1</sup> )
27		
28	$r_1$	Pre-exponential factor for the antigen
29		
30	$r_2$	Pre-exponential factor for FITC
31		
32		
33	$r$	Fluorescence anisotropy of the antigen
34		
35	$r_h$	Hydrodynamic radius (m)
36		
37	$R$	Universal gas constant (J mol <sup>-1</sup> K <sup>-1</sup> )
38		
39		
40	$t$	Time (s)
41		
42	$T$	The absolute temperature (K)
43		
44		
45	$v$	Velocity of the antigen
46		
47	$\eta$	Dynamic viscosity (N s/m <sup>2</sup> )
48		
49	$\theta$	Rotational correlation time-constant for the antigen (s)
50		
51	$\theta_1$	Rotational correlation time-constant for FITC (s)
52		
53		
54		
55		
56		
57		
58		
59		
60		

## 1. Introduction:

Heterogeneous immunosensors can provide specific and reliable detection of life threatening diseases like cancer in the early stages with the help of some signature proteins known as cancer biomarkers<sup>1</sup>. The investigations of physicochemical properties of these clinically relevant biomarkers are of great interest to the scientific community for improving the detection limit by enhancing their capture in an immunosensor<sup>2</sup>. The major challenge associated with the detection of these biomarkers is their extremely low concentration level in the human body. Hence, development of a fast, accurate, and efficient immunosensor is of great importance<sup>3, 4</sup>. The detection process in heterogeneous immunosensors includes two major events - the transport of analytes from the bulk to the surface, and the reaction of these analytes with the surface immobilized antibodies. Since the reaction kinetics of the antigen-antibody interaction is faster compared to the rate of transport of the analytes, the phenomena of the capture of analytes is transport limited<sup>5</sup>. Hence in order to design efficient immunosensors, alleviation of the transport limitations is crucial. Literature contains various reports, wherein efforts have been made to mitigate the mass-transfer limitations such as increasing the advective mixing by mechanical stirring<sup>6, 7</sup>, thermal effects<sup>8</sup>, AC electroosmosis<sup>9</sup>, electrothermal effects<sup>10, 11</sup>, and optimization of the pH<sup>7, 12</sup>. In non-flow systems, diffusion is the major mechanism of transport, and hence effective diffusivity ( $D_{eff}$ ) is an important transport parameter, which combines the contributions from translational and rotational mobility of the travelling molecules. The effect of various process conditions on  $D_{eff}$  have been studied extensively; however the contribution of the rotational diffusivity towards the overall transport is comparatively less explored, and needs attention. We have tried to address this issue in the present study.

1  
2  
3 Rotational diffusion is a manifestation of the rotational degree of freedom of the analyte  
4 molecule which originates from the randomization of the orientations of the molecule, and is  
5 attributed to the nature of the interaction of the same with the surrounding medium (solvents as  
6 well as other solute molecules)<sup>13</sup>. There are studies reported in literature wherein the rotational  
7 dynamics of the molecules have been explored by various techniques for a variety of  
8 applications. The techniques used to measure rotational mobility of the molecules include  
9 phosphorescence anisotropy<sup>14, 15</sup>, fluorescence anisotropy<sup>16, 17</sup>, dynamic light scattering (DLS)<sup>18</sup>,  
10  
11  
12  
13  
14  
15  
16  
17  
18  
19  
20  
21  
22  
23  
24  
25  
26  
27  
28  
29  
30  
31  
32  
33  
34  
35  
36  
37  
38  
39  
40  
41  
42  
43  
44  
45  
46  
47  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60

Rotational diffusion is a manifestation of the rotational degree of freedom of the analyte molecule which originates from the randomization of the orientations of the molecule, and is attributed to the nature of the interaction of the same with the surrounding medium (solvents as well as other solute molecules)<sup>13</sup>. There are studies reported in literature wherein the rotational dynamics of the molecules have been explored by various techniques for a variety of applications. The techniques used to measure rotational mobility of the molecules include phosphorescence anisotropy<sup>14, 15</sup>, fluorescence anisotropy<sup>16, 17</sup>, dynamic light scattering (DLS)<sup>18</sup>,<sup>19</sup>, nuclear magnetic resonance (NMR)<sup>20</sup>, fluorescence correlation spectroscopy (FCS)<sup>21</sup> etc. Molecular dynamics simulation studies have also been used to calculate the rotational diffusivity<sup>22, 23</sup>.

In time-resolved fluorescence anisotropy, the technique used in the present work to measure the rotational diffusivity of antigens, the rotational mobility of a fluorophore attached to the molecule is measured using a technique based on the time evolution of two polarized intensities to measure the fluorescence anisotropy decay<sup>24</sup>, and is used to investigate the physical and chemical properties of these molecules. Since the rotational mobility strongly depends on the solute-solvent interactions as well as the structure of molecule, time-resolved fluorescence anisotropy measurement has been extensively used to capture the information associated with the dynamic nature and structural information of the molecules<sup>25</sup>. For example, Ao-Jin et al. estimated viscosity and the rotational diffusion of bacteriorhodopsin inside membranes to be used to monitor the oligomeric state of the membrane proteins, and showed the temperature dependencies of the viscosity values for the solvents under study<sup>26</sup>. Das et al. measured the rotational time constants of Coumarin-153 in pure 1-(2-methoxyethyl)-1-methylpyrrolidinium tris(pentafluoroethyl)trifluorophosphate (ionic liquid), and its mixture with toluene, and reported

1  
2  
3 that the rotational diffusion becomes faster in the presence of toluene<sup>27</sup>. Zheng et al. studied the  
4 dynamics of the decay of fluorescence anisotropy of free and bound NADH molecules in normal  
5 and cancerous tissues with the change in the environment of the endogenous fluorophore, which  
6 could be used to detect cancers at early stages<sup>24</sup>. Hu et al. reported the rotational time constant of  
7 T4 lysozyme and its dynamical nature pertinent to its physiological environment inside cells,  
8 which are pertinent to the applications in cell signaling<sup>28</sup>. Lavalette et al. reported the rotational  
9 Brownian motion of bovine serum albumin (BSA), hemoglobin and fragmented hemoglobin to  
10 check the validation of the Stokes-Einstein-Debye equation by changing the viscosity of the  
11 solution applied to quantify nonhomogeneity in-vivo<sup>29</sup>. Takahashi et al. studied the effect of  
12 various solvents on lysozyme-lysozyme interactions via fluorescence anisotropy measurements  
13 of the solution to quantify protein-protein interactions for various applications<sup>30</sup>. Further,  
14 anisotropy decay and change in the polarization of the fluorescence emission has also been used  
15 for detection purposes<sup>31-33</sup>. Though there are extensive studies on the quantification of the  
16 rotational time constant in various applications, to the best of our knowledge, the investigation of  
17 rotational time constants to quantify the contribution of rotational diffusion of molecules towards  
18 the overall diffusive transport for immunosensing applications have not been reported.

19  
20  
21  
22  
23  
24  
25  
26  
27  
28  
29  
30  
31  
32  
33  
34  
35  
36  
37  
38  
39  
40  
41  
42 In the present study, we have investigated the effect of the major process parameters on  
43 the rotational diffusivity, which include temperature and pH of the solvent. While there are  
44 reports on the effect of temperature on  $D_{rot}$  for various molecules including bovine serum  
45 albumin (BSA)<sup>34</sup>, the effect of temperature on  $D_{rot}$  for prostate specific antigen (PSA), and C-  
46 reactive proteins (CRP), and the effect of pH of the antigen solution, has not been explored till  
47 now. The motivation for the present study comes from our previous work, where we have  
48 optimized the pH of the solution to obtain the highest capture of the three antigens- BSA, PSA,  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60

1  
2  
3 and CRP<sup>7</sup> for immunosensors. The pH values in the previous study were selected on the basis of  
4  
5 the isoelectric points of the antigen and antibody molecules, and it was observed that maximum  
6  
7 capture of the antigen molecules occurred at a pH value in between the pIs of the antigen and the  
8  
9 antibody. Further, we obtained functional dependencies of transport and reaction parameters on  
10  
11 three process parameters (temperature, extent of mixing and pH). A transport parameter analyzed  
12  
13 for a non-flow system in our previous study through the kinetics of capture of the antigens was  
14  
15  $D_{eff}$ , hence it is of further interest to quantify the contribution of  $D_{rot}$  in the overall rate of  
16  
17 transport, which was not studied in the previous work. We have measured the  $D_{rot}$  of the three  
18  
19 FITC-tagged antigens - BSA, PSA, and CRP in the buffer solution by time-resolved fluorescence  
20  
21 anisotropy method. Our goal is to quantify the contribution of rotational diffusivity to the overall  
22  
23 diffusivity of the travelling molecule before reaching the electric double layer at the interface of  
24  
25 surface immobilized antibodies and the electrolyte. So, the experiments were performed only in  
26  
27 the buffer without any immobilized reacting surface. While BSA is chosen in order to  
28  
29 benchmark our results, to the best of our knowledge, we could not find any report in the  
30  
31 literature related to the measurement of rotational diffusivity of PSA and CRP. Anisotropy  
32  
33 measurements were performed to obtain the rotational time constants, which were further used to  
34  
35 calculate the contribution of  $D_{rot}$  for all three antigens. As the transport of analytes is the rate  
36  
37 limiting step in most of the antigen-antibody interactions, the quantification of the contribution  
38  
39 rotational diffusion towards the overall mass transport will be useful to design efficient  
40  
41 microfluidic immunosensors for early disease detection<sup>35</sup>.  
42  
43  
44  
45  
46  
47  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60



## 2. Theory:

The mass transport of an analyte (the antigen molecules in the present study) is governed by a diffusion-convection phenomenon, described by equation 1.

$$\frac{\partial C}{\partial t} = \nabla \cdot (D_{eff} \nabla C) - \nabla \cdot (\vec{v}C) \quad (1)$$

The first term on the right hand side captures the effect of molecular diffusion on transport, whereas the second term incorporates contribution of convection. In non-flow systems, only the molecular diffusion term accounts for mass transport, hence effective diffusivity,  $D_{eff}$ , becomes an important transport parameter. As discussed above, it combines the contributions from both the translational and rotational degrees of freedom, and is given by equation 2 and 3<sup>36</sup>.

$$D_{eff} = D_{trans} + D'_{rot} \quad (2)$$

where

$$D'_{rot} = \frac{2}{3} r_h^2 D_{rot} \quad (3)$$

where the hydrodynamic radius of the molecules depends on the volume of the solute and their interaction with the surrounding solvent molecules.

Figure 1 shows the schematic to describe the process of the time-resolved anisotropy decay, and how it is utilized to extract the rotational time constants and the  $D_{rot}$ . As presented in the figure, the anisotropy measurements are based on the capture of the intensity of the emitted

1  
2  
3 light by fluorophores attached to the molecules having random orientations excited by linearly  
4 polarized light<sup>37</sup>. The orientation of the molecule plays a crucial role in the depolarization of the  
5 incoming light, and provides information about the rotational degrees of freedom of the  
6 molecule. Polarizers were used in the path of the emitted light to collect the parallel and  
7 perpendicular components of the depolarized emitted light recorded as a function of time. The  
8 collected data were processed by the spectrometer to obtain the anisotropy as a function of time.  
9  
10 A multi-exponential fit to the anisotropy decay data was used to obtain the rotational time  
11 constant of various species present in the solution. For a fluorophore tagged antigen molecule, a  
12 bi-exponential function given by equation 4<sup>30</sup>, was fitted to the anisotropy decay data.  
13  
14  
15  
16  
17  
18  
19  
20  
21  
22  
23  
24  
25  
26  
27

$$r(t) = r_1 \exp(-t/\theta) + r_2 \exp(-t/\theta_1) \quad (4)$$

28  
29  
30  
31  
32 Assuming the antigen molecules to be spherical in shape (Stoke's approximation), the rotational  
33 correlation time constant obtained from the exponential decay fit can be used to calculate the  
34 rotational diffusion coefficient by equation 5<sup>38</sup>.  
35  
36  
37  
38

$$D_{rot} = \frac{1}{6\theta} \quad (5)$$

39  
40  
41  
42  
43  
44  
45  
46 The hydrodynamic radius ( $r_h$ ) was calculated from  $D_{rot}$  by equation 6<sup>38</sup>.  
47  
48  
49  
50

$$r_h = \left( \frac{k_B T}{8\pi\eta D_{rot}} \right)^{1/3} \quad (6)$$

1  
2  
3 The above expression is obtained from the Stokes-Einstein Debye relation, which incorporates  
4 the change in volume due to the change in the environment in which the antigen molecules are  
5 kept.  
6  
7  
8  
9

### 10 11 12 **3. Materials and methods:**

#### 13 14 15 *3.1 Chemicals:*

16  
17 Phosphate buffer saline (PBS) of pH 7.4 was obtained from Sigma-Aldrich Inc. Other buffer  
18 solutions of pH 4, 5, 6, 6.5 and 8 were prepared taking appropriate combinations of sodium  
19 dihydrogen phosphate and monosodium phosphate salts, and the final pH was verified using a  
20 calibrated pH meter. The antigens were stored in a stock solution of standard PBS buffer of pH  
21 7.4, and 10  $\mu$ l of this stock solution was mixed with 2 ml of the buffer solution of the specific pH  
22 of interest. Furthermore, the final pH of the combination was measured to be the same (within  
23 the limits of accuracy of the instrument) as earlier. Bovine serum albumin (BSA) was obtained  
24 from Genei Biotech, Bangalore, India. Prostate specific antigen (PSA) was obtained from  
25 Fitzgerald Industries International, USA, and C-reactive proteins (CRP) from Calbiochem, USA.  
26 The tagging of the antigens (BSA, PSA and CRP) with fluorescein isothiocyanate (FITC) was  
27 accomplished in Genetech Laboratory, Biotech. Park, Lucknow, India, and the ratio of the FITC  
28 to antigen was assumed to be 1:1 (based on the manufacturer's information). The different  
29 dilutions for measurement were prepared using stock solutions of the above tagged antigens in  
30 the required buffer solution.  
31  
32  
33  
34  
35  
36  
37  
38  
39  
40  
41  
42  
43  
44  
45  
46  
47  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60

### 3.2 Process conditions used for experiments:

Three different antigens (BSA, PSA and CRP), at three different temperatures (293, 303, and 313 K) were used in the experiments. The antigen solution was added to the buffer of the required pH value, mixed well, and then poured into a clean cuvette for taking measurements. The pH values chosen for each of the antigen molecule on the basis of their isoelectric points, are listed in Table 1. Four/five values of pH, lower as well as higher than the pIs of the corresponding antigens, were used in the experiments.

Table 1. pH values used for measurement for BSA, PSA, and CRP.

Antigens used	pI <sup>7</sup>	pH values used
BSA	4.8	4, 5, 6 and 7.4
PSA	6.8	5, 6, 6.5 and 7.4
CRP	7.2	5, 6, 6.5, 7.4 and 8

### 3.3 Time-resolved anisotropy measurement:

The time-dependent fluorescence anisotropy measurements were performed using a LifeSpec-II luminescence spectrometer (Edinburgh Instruments, Ltd). A pico-second pulsed diode laser of 445 nm was employed as the excitation source, with the emission being recorded at 530 nm. A filter of 500 nm was used in the path of emitted light. Experiments were conducted in triplicates

1  
2  
3 for each process condition mentioned above, and the error bars represent one standard deviation  
4  
5 about the mean.  
6  
7  
8  
9

### 10 3.4 Viscosity measurements:

11  
12 The viscosity of the buffer solutions was measured using a Rolling-ball viscometer (Lovis  
13 2000M Anton Paar microviscometer) at three temperatures (293, 303 and 313 K), where the pH  
14  
15 was kept constant at 7.4. Further the viscosity measurements were taken at pH values of  
16  
17 4,5,6,6.5, and 7.4, with the temperature being kept constant at 303 K.  
18  
19  
20  
21  
22  
23  
24

## 25 4. Results and Discussions:

26  
27  
28 The values of  $D_{rot}$  are expected to be dependent on various parameters associated with a solvent  
29  
30 (viscosity, temperature, pH). So, we have studied the effect of the temperature, and the pH of the  
31  
32 solution on  $D_{rot}$ , and further investigated the choice of the best process condition. Since the  
33  
34 values of viscosity may vary with temperature, and pH of the solution, these were measured for  
35  
36 each experimental condition used, and are reported in Table 2. We first used BSA to benchmark  
37  
38 our results, and then conducted the rotational diffusion measurements of PSA and CRP.  
39  
40  
41  
42  
43  
44  
45  
46  
47  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60

Table 2. Viscosity values of the buffer measured at (a) three temperatures at pH 7.4, and (b) five pH values at 303 K.

$T$ (K)	$\eta$ (Pa.s) $\times 10^{-3}$
293	1.031
303	0.826
313	0.693

pH	$\eta$ (Pa.s) $\times 10^{-3}$
4	0.851
5	0.839
6	0.904
6.5	0.904
7.4	0.826
8	0.909

#### 4.1 Temperature dependency and validation:

Fig. 2 shows the decay of the fluorescence anisotropy with time for BSA tagged with FITC, using PBS as the solvent at 303 K and pH 7.4. The anisotropy as a function of time thus obtained was fitted to a bi-exponential decay function, as shown by the solid line in the figure. The fitting yields the rotational correlation time constants associated with the tagged antigens. Similar anisotropy curves were obtained for BSA at 293 and 313 K, and also for PSA and CRP at all three temperatures, and for all three antigens at the pH values mentioned in Table 1. The

1  
2  
3 corresponding time constants obtained via fitting were used in calculating  $D_{rot}$  and  $r_h$  for each  
4  
5 process condition using equations 4 and 5, respectively.  
6  
7

8  
9 Fig. 3a shows the plot of  $D_{rot}$  of BSA molecules at pH 7.4 and three temperatures- 293,  
10  
11 303, and 313 K. We observed that for all cases, the values of  $D_{rot}$  increases with increase in  
12  
13 temperature. The increase in  $D_{rot}$  with increase in temperature can be attributed to increased  
14  
15 average kinetic energy of the molecules at higher temperature, which manifests in enhancement  
16  
17 of both rotational and translational degrees of freedom. The above trends are also in accordance  
18  
19 with the studies reported earlier. For example, increased rotational diffusivity values for  
20  
21 bacteriorhodopsin with temperature were observed based on faster anisotropy decay, measured  
22  
23 with the help of anisotropy measurements<sup>26</sup>. Temperature dependent studies have also been  
24  
25 performed for 4-methyl-4'-cyanobiphenyl (1CB) and 4-hexyl-4'-cyanobiphenyl (6CB), and the  
26  
27 time constants for the decay were reported to decrease with increase in temperature indicating  
28  
29 increased values of  $D_{rot}$  with temperature<sup>39</sup>.  
30  
31  
32  
33  
34  
35

36 Similar experiments were conducted for PSA and CRP as a function of temperature, and  
37  
38 the results are plotted in Fig. 3b and c respectively. As expected, for all cases,  $D_{rot}$  increases with  
39  
40 increase in temperature and showing an Arrhenius dependency, given by equation 7.  
41  
42

$$D_{rot} = D_{0,rot} \exp(-E_{a,rot}/RT) \quad (7)$$

43  
44  
45  
46  
47 For the Arrhenius fitting shown in the insets of Fig. 3, the mean value of each case was taken  
48  
49 into account, where  $R^2$  represents the regression coefficient, and is used to show how well the  
50  
51 experimental data is fitted to the Arrhenius model. After fitting  $D_{rot}$  vs. *temperature*, we obtained  
52  
53 the values of  $D_{0,rot}$  and  $E_{a,rot}$  for BSA, PSA and CRP respectively, shown in Table 3. The  
54  
55  
56  
57  
58  
59  
60

quantification of the dependencies of  $D_{rot}$  with temperature would be useful in selecting the temperature range for the respective antigen solution. Arrhenius dependencies of the rotational motion was earlier reported for BSA, with an activation energy of 13 KJ/mol<sup>34</sup>. The difference with our results could be due to the different experimental conditions used. To the best of our knowledge, such quantification for PSA and CRP have not been reported in the literature so far. After obtaining the data for the temperature dependencies of  $D_{rot}$  for the three antigens, we proceed to obtain the pH dependencies.

Table 3. Fitting parameters obtained from  $D_{rot}$  vs.  $T$  for all three antigens.

Antigen	$D_{0,rot}$ (1/s)	$E_{a,rot}$ (KJ/mol)	$R^2$
BSA	$8.90 \times 10^6$	36.08	0.99
PSA	$2.16 \times 10^6$	32.40	0.95
CRP	$7.76 \times 10^4$	18.74	0.93

#### 4.2 Effect of pH:

Fig. 4a shows the plot of  $D_{rot}$  at 303 K, and four different pH values of the solution for BSA. It can be observed from the figure that the  $D_{rot}$  shows maxima at pH 5, which is close to the isoelectric point of BSA having a value of 4.8<sup>40</sup>. Similarly Fig. 4b and c show the plots of the  $D_{rot}$  at 303 K, and four different pH values for PSA, and five different pH values for CRP respectively. It was observed that the maxima in both the cases are at about pH values of 6.5 and 7.4, close to their pIs at 6.8 and 7.2 respectively<sup>7</sup>. The occurrence of maxima of  $D_{rot}$  close to the



1  
2  
3 pI of the antigens can be attributed to minimal surface charge on the antigen molecules at this  
4  
5 pH, which leads to weakening of the electrostatic interactions of the antigens with the  
6  
7 surrounding (which includes other similar molecules as well as molecules of the solvent).  
8  
9 However, at a pH away from the isoelectric point, the net surface charge of the molecules is  
10  
11 either positive or negative which facilitates the electrostatic interactions of the molecules with  
12  
13 other similar molecules and electrolyte carrier molecules (solvent molecules). This leads to  
14  
15 electro-viscous effects that ultimately result in hindrance to the motion of the antigen molecules.  
16  
17 Since the rotational mobility originates from the Brownian diffusivity of particles, we  
18  
19 hypothesize that the electro-viscous effects result in lower values of  $D_{rot}$ . There are reports of  
20  
21 similar observations to support our hypothesis. For example, Nesmelova et al. reported that  
22  
23 protein molecules do not form aggregates due to absence of interaction at pH values where they  
24  
25 have very small amount of surface charge, and hence leading to enhanced Brownian motion<sup>41</sup>.  
26  
27 Tawari et al. studied Brownian diffusivity of Laponite clay particle in association with the  
28  
29 electric double layer of the solute molecules<sup>42</sup>, and reported that the charged disks have 50%  
30  
31 smaller diffusivity than that of hard disks (no double layer) with the same diameter. They  
32  
33 explained it in terms of electro-viscous drag offered to a charged solute particle by the  
34  
35 surrounding cloud of the counter ions. Hence, we conclude that the maximum rotational mobility  
36  
37 at the isoelectric point can be attributed to the least hindrance pertaining to low surface charge on  
38  
39 the antigen molecules.  
40  
41  
42  
43  
44  
45  
46  
47  
48

49 The above observations associated with pH variation suggest that at the pI of the antigen  
50  
51 molecules, the maximum diffusivity is expected to result in the higher rate of transport, and  
52  
53 hence higher capture of the analytes in the immunosensor. However, it is to be noted that the  
54  
55 capture strongly depends on the affinity of two binding species along with the rate of transport of  
56  
57

1  
2  
3  
4  
5  
6  
7  
8  
9  
10  
11  
12  
13  
14  
15  
16  
17  
18  
19  
20  
21  
22  
23  
24  
25  
26  
27  
28  
29  
30  
31  
32  
33  
34  
35  
36  
37  
38  
39  
40  
41  
42  
43  
44  
45  
46  
47  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60

1  
2  
3 antigens. Since opposite charges on the binding species enhances the probability of binding, one  
4 has to maintain a pH different from the pI values of both the species to get the maximum capture.  
5  
6 These results seems to indicate that there is tradeoff between maximizing the rate of transport  
7  
8 rate and the rate of capture of the antigens. However, in case of the immunosensors since one of  
9  
10 the binding species (antibodies) is already immobilized on the reacting surface, the incoming  
11  
12 antigen has to travel through the solvent onto the surface for the reaction to happen. Hence, a  
13  
14 higher rate of transport may play a crucial role here. To make the above point more clear we  
15  
16 discuss the present work in the context of our previous work. In our previous work, we had  
17  
18 observed the maximum capture efficiency at a value of pH in between the isoelectric points (pI)  
19  
20 of antigen and antibody<sup>7</sup>, where our goal was to maximize the amount of the bound complex. So,  
21  
22 we had studied the interaction between the incoming antigen and the immobilized antibody  
23  
24 surface, and obtained maximum capture where the antigens and antibodies have opposite charges  
25  
26 induced on their surfaces, which leads to the maximum electromigration when the antigen comes  
27  
28 into the electrical double layer (EDL) associated with the immobilized antibody. However,  
29  
30 before coming into the EDL, the antigens have to travel through the bulk solution where the  
31  
32 various solvent conditions affect the motion of the antigen molecules, which could affect the  
33  
34 transport. Thus while the maxima of the capture of antigens as a function of pH of the solution  
35  
36 for the previous investigation was focused within the EDL of immobilized layer (i.e., closer to  
37  
38 the surface), the maxima of the  $D_{rot}$  reported in the present work is pertinent when the antigens  
39  
40 are outside EDL of the immobilized antibodies, and traveling through the solvent in the bulk  
41  
42 layer. So, all the measurements are taken in the buffer solution for this work to quantify the  
43  
44 diffusivity of the antigen molecules. As the effective diffusivity is contributed by the two degrees  
45  
46 of freedom: translational and rotational, the individual contributions are expected to be higher at  
47  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60

1  
2  
3 this pH value. To the best of our knowledge, pH dependent studies for the three antigens are not  
4 reported in the literature. However, there are reports on the comprehensive studies of the  
5 interactions of different kinds of ionic liquids and their interactions with non-polar, charged and  
6 dipolar solute molecules and the factors that influence their anisotropy behavior<sup>43</sup>. Since, this  
7 interaction is specific to the solute-solvent pair under consideration, there is no unanimity in the  
8 trends obtained for the kind of interactions. For example, the rotational dynamics of a cationic  
9 solute ethidium bromide (EB) and an anionic solute 1-anilinonaphthalene-8-sulfonate (ANS), did  
10 not show any electrostatic interactions in ionic liquids<sup>17</sup>. On the contrary, the rotational diffusion  
11 of a cationic solute Rhodamine 110 in a mixture of solvents including SDS showed the  
12 dependence of the rotational time constants on the solute-solvent electrostatic interactions<sup>16</sup>.  
13 There are also reports of the study of neutral versus charged solutes in ionic liquids, but the  
14 charge components of the solute-solvent interaction were not quantified for the rotational  
15 dynamics<sup>44</sup>.  
16  
17  
18  
19  
20  
21  
22  
23  
24  
25  
26  
27  
28  
29  
30  
31  
32

#### 33 34 35 36 37 38 *4.3 Contribution to the effective diffusivity ( $D_{eff}$ ):*

39  
40  
41 From the experimentally measured time constants for all three antigens, and the process  
42 conditions such as temperature and pH of the solution, the values of  $\tau$  and  $D_{rot}$  were obtained for  
43 each case. The  $D_{rot}$  was used to calculate  $r_h$ , and further  $D_{rot}'$  was calculated which quantifies the  
44 contribution of rotational diffusivity of molecule towards over all transport. Fig. 5a shows the  
45 plot of  $D_{rot}'$  for BSA as a function of temperature and pH. It is observed that the factor  $D_{rot}'$   
46 increases monotonically with temperature in the range studied, while it shows a maxima with the  
47 pH of the solution. These trends observed here resemble that of the observed values for  $D_{rot}$   
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60

1  
2  
3 reported in Fig. 3 and 4, though the absolute values are different for each case. Similar data were  
4  
5 plotted for PSA and CRP as a function of temperature and pH in Fig. 5b and c respectively. The  
6  
7 increment in the values of  $D_{rot}'$  with temperature follows a similar Arrhenius dependency for  
8  
9 both PSA and CRP in the ranges studied whereas a nonmonotonic behavior is observed with the  
10  
11 variation in pH values. However, the variation in  $D_{rot}'$  with pH for CRP, reported in Fig. 5c  
12  
13 shows a maxima at pH 7.4 which is close to pI of CRP while the other data points are within the  
14  
15 statistical limits of error. The values of  $D_{rot}'$  were found to be in the range of the values of  $D_{eff}$  ( $1$   
16  
17  $\times 10^{-9}$  to  $1 \times 10^{-12}$  m<sup>2</sup>/s) reported earlier<sup>2, 45</sup>.  
18  
19  
20  
21  
22  
23  
24  
25

## 26 **5. Conclusions:**

27  
28  
29 Rotational diffusivity is an important transport parameter and needs to be characterized to help  
30  
31 design an efficient immunosensor. In this work, the  $D_{rot}$  is measured for three antigens- BSA,  
32  
33 PSA and CRP in the buffer, using the technique of time-resolved fluorescence anisotropy.  
34  
35 Further, the effects of two important process parameters (temperature and pH) on the values of  
36  
37  $D_{rot}$  were investigated. The values of  $D_{rot}$  increase with temperature showing Arrhenius  
38  
39 dependencies which were quantified through the fitting parameters. The trend with the variation  
40  
41 in pH shows an interesting behavior - a maxima at a pH close to the isoelectric point of the  
42  
43 corresponding antigens. This is attributed to the lesser hindrance due to lesser electro-viscous  
44  
45 effects, leading to higher values of  $D_{rot}$  when the antigen molecules are neutral as compared to  
46  
47 the cases when they are either positively or negatively charged. Furthermore, the contribution of  
48  
49  $D_{rot}$  (given by  $D_{rot}'$ ) was quantified, and it was found to be of the order of  $1 \times 10^{-11}$  m<sup>2</sup>/s, which  
50  
51 also measures the contribution towards the diffusive transport of the antigens in an  
52  
53  
54  
55  
56  
57  
58  
59  
60

1  
2  
3 immunosensor. In this work, we have obtained  $D_{rot}$  through anisotropy measurements for PSA  
4 and CRP, which we believe is reported for the first time. Further, the quantification of  $D_{rot}$  for  
5 the antigens with variation in the process parameters (temperature and pH) was studied.  
6  
7 Delineating the contributions of each of the parameters in the diffusive transport processes  
8 involved would help optimize the transport parameters for immunosensors.  
9  
10  
11  
12  
13  
14  
15  
16  
17

### 18 **Acknowledgement**

19  
20 The authors gratefully acknowledge the financial support from the DST Science and Engineering  
21 Research Board, India (Grant No. SB/S3/CE/055/2013). Kind support for measurement of  
22 fluorescence anisotropy by Ms. B. Sengupta and Prof. P. Sen in the Department of Chemistry,  
23 IIT Kanpur, is acknowledged.  
24  
25  
26  
27  
28  
29  
30  
31  
32  
33

### 34 **References:**

- 35  
36  
37 1. V. Kulasingam and E. P. Diamandis, *Nat. Rev. Clin. Oncol.*, 2008, **5**, 588-599.  
38  
39 2. D. Rath, S. Kumar and S. Panda, *Mater. Sci. Eng., C*, 2012, **32**, 2223-2229.  
40  
41 3. A. Bange, H. B. Halsall and W. R. Heineman, *Biosens. Bioelectron.*, 2005, **20**, 2488-  
42 2503.  
43  
44 4. R. Chepyala and S. Panda, *Appl. Surf. Sci.*, 2013, **271**, 77-85.  
45  
46 5. T. M. Squires, R. J. Messinger and S. R. Manalis, *Nat. Biotech.*, 2008, **26**, 417-426.  
47  
48 6. G. Wang, J. D. Driskell, M. D. Porter and R. J. Lipert, *Anal. Chem.*, 2009, **81**, 6175-  
49 6185.  
50  
51 7. D. Rath and S. Panda, *Chem. Eng. J.*, 2015, **260**, 657-670.  
52  
53  
54  
55  
56  
57  
58  
59  
60

- 1
  - 2
  - 3
  - 4
  - 5
  - 6
  - 7
  - 8
  - 9
  - 10
  - 11
  - 12
  - 13
  - 14
  - 15
  - 16
  - 17
  - 18
  - 19
  - 20
  - 21
  - 22
  - 23
  - 24
  - 25
  - 26
  - 27
  - 28
  - 29
  - 30
  - 31
  - 32
  - 33
  - 34
  - 35
  - 36
  - 37
  - 38
  - 39
  - 40
  - 41
  - 42
  - 43
  - 44
  - 45
  - 46
  - 47
  - 48
  - 49
  - 50
  - 51
  - 52
  - 53
  - 54
  - 55
  - 56
  - 57
  - 58
  - 59
  - 60
8. H. S. Fogler, *Elements of Chemical Reaction Engineering*, fourth edn., Prentice Hall International series, 2005.
9. R. Harta, R. Leca and H. M. Noh, *Sens. Actuators, B*, 2010, **147**, 366–375.
10. M. Sigurdson, D. Wang and C. D. Meinhart, *Lab Chip*, 2005, **5**, 1366–1373.
11. K. R. Huang, J. S. Chang, S. D. Chao, K. C. Wu, C. K. Yang, C. Y. Lai and S. H. Chen, *J. Appl. Phys.*, 2008, **6**, 064702–064711.
12. N. Gan, L. Jia and L. Zheng, *Int. J. Mol. Sci.*, 2011, **12**, 7410–7423
13. M. A. Charsooghi, E. A. Akhlaghi, S. Tavaddod and H. R. Khalesifard, *Comput. Phys. Commun.*, 2011, **182**, 400–408.
14. G. H. Koenderink, D. G. A. L. Aarts and A. P. Philipse, *J. Chem. Phys.*, 2003, **119**, 4490–4499.
15. G. H. Koenderink, M. P. Lettinga and A. P. Philipse, *J. Chem. Phys.*, 2002, **117**, 7751–7764.
16. K. S. Mali, G. B. Dutt and T. Mukherjee, *J. Phys. Chem. B*, 2007, **111**, 5878–5884.
17. D. C. Khara and A. Samanta, *Phys. Chem. Chem. Phys.*, 2010, **12**, 7671–7677.
18. R. Piazza and V. Degiorgio, *J. Phys.: Condens. Matter*, 1996, **8**, 9497–9502.
19. R. Pecora, *J. Nanopart. Res.*, 2000, **2**, 123–131.
20. S. Ravindranathana, C. H. Kimb and G. Bodenhausen, *J. Biomol. NMR*, 2005, **33**, 163–174.
21. A. Loman, I. Gregor, C. Stutz, M. Mund and J. Enderlein, *Photochem. Photobiol.*, 2010, **9**, 627–636.
22. G. F. Schroder, U. Alexiev and H. Grubmuller, *Biophys. J.*, 2005, **89**, 3757–3770.
23. V. Wong and D. A. Case, *J. Phys. Chem. B*, 2008, **112**, 6013–6024.

- 1  
2  
3  
4  
5  
6  
7  
8  
9  
10  
11  
12  
13  
14  
15  
16  
17  
18  
19  
20  
21  
22  
23  
24  
25  
26  
27  
28  
29  
30  
31  
32  
33  
34  
35  
36  
37  
38  
39  
40  
41  
42  
43  
44  
45  
46  
47  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60
24. W. Zheng, D. Li and J. Y. Qu, *J. Biomed. Opt.*, 2010, **15**, 037013.
  25. M. Ameloot, M. VandeVen, A. U. Acuna and B. Valeur, *Pure Appl. Chem.*, 2013, **85**, 589–608.
  26. W. Ao-Jin and H. Kun-Sheng, *Chin. Phys. Lett.*, 2002, **19**, 1727-1729.
  27. S. K. Das and M. Sarkar, *J. Mol. Liq.*, 2012, **165**, 38-43.
  28. D. Hu and H. P. Lu, *J. Phys. Chem. B*, 2002, **107**, 618-626.
  29. D. Lavalette, C. Tetreau, M. Tourbez and Y. Blouquit, *Biophys. J.*, 1999, **76**, 2744-2751.
  30. D. Takahashi, E. Nishimoto, T. Murase and S. Yamashita, *Biophys. J.*, 2008, **94**, 4484-4492.
  31. A. P. Demchenko, *Introduction to Fluorescence Sensing*, Springer Science & Business Media B.V. , 2009.
  32. S. J. Zhen, Y. Yu, C. M. Li and C. Z. Huang, *Analyst*, 2015, **140**, 353-357.
  33. W. Li, K. Wang, W. Tan, C. Ma and X. Yang, *Analyst*, 2007, **132**, 107-113.
  34. M. L. Ferrer, R. Duchowicz, B. Carrasco, J. de la Torre and A. U. Acuna, *Biophys. J.*, 2001, **80**, 2422-2430.
  35. R. Chepyala and S. Panda, *Microfluid. Nanofluid.*, 2015, DOI 10.1007/s10404-014-1532-6, 1-11.
  36. G. Gros, D. Lavalette, W. Moll, H. Gros, B. Amand and F. Pochon, *Proc. Natl. Acad. Sci.*, 1984, **81**, 1710-1714.
  37. J. R. Lakowicz, *Principles of Fluorescence Spectroscopy*, Third edn., Springer Science & Business Media, 2007.
  38. Y. Y. Kuttner, N. Kozler, E. Segal, G. Schreiber and G. Haran, *J. Am. Chem. Soc.*, 2005, **127**, 15138-15144.

- 1  
2  
3 39. H. Matsuzawa, K. Watanabe and M. Iwahashi, *J. Oleo Sci.*, 2007, **56**, 579-586.  
4  
5  
6 40. C. Wang, J. Wang and L. Deng, *Nanoscale Res. Lett.*, 2011, **6**, 579.  
7  
8 41. I. V. Nesmelova, V. D. Skirda and V. D. Fedotov, *Biopolymers*, 2002, **63**, 132-140.  
9  
10 42. S. L. Tawari, D. L. Koch and C. Cohen, *J. Colloid Interface Sci.*, 2001, **240**, 54-66.  
11  
12 43. K. S. Mali, *J. Chem. Sci.*, 2009, **121**, 7-21.  
13  
14  
15 44. N. Ito, S. Arzhantsev and M. Maroncelli, *Chem. Phys. Lett.*, 2004, **396**, 83-91.  
16  
17 45. R. A. Vijayendran, F. S. Ligler and D. E. Leckband, *Anal. Chem.*, 1999, **171**, 5405-5412.  
18  
19  
20  
21  
22  
23  
24  
25  
26  
27  
28  
29  
30  
31  
32  
33  
34  
35  
36  
37  
38  
39  
40  
41  
42  
43  
44  
45  
46  
47  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60



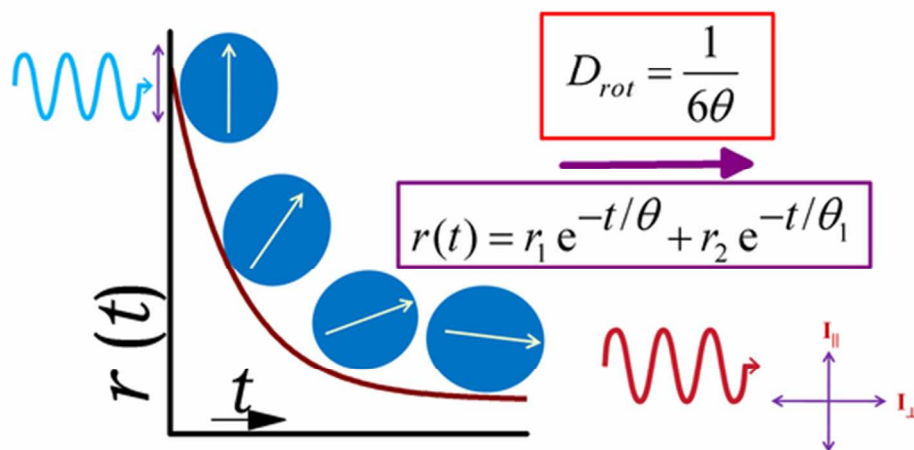


Figure 1  
49x24mm (300 x 300 DPI)

1  
2  
3  
4  
5  
6  
7  
8  
9  
10  
11  
12  
13  
14  
15  
16  
17  
18  
19  
20  
21  
22  
23  
24  
25  
26  
27  
28  
29  
30  
31  
32  
33  
34  
35  
36  
37  
38  
39  
40  
41  
42  
43  
44  
45  
46  
47  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60

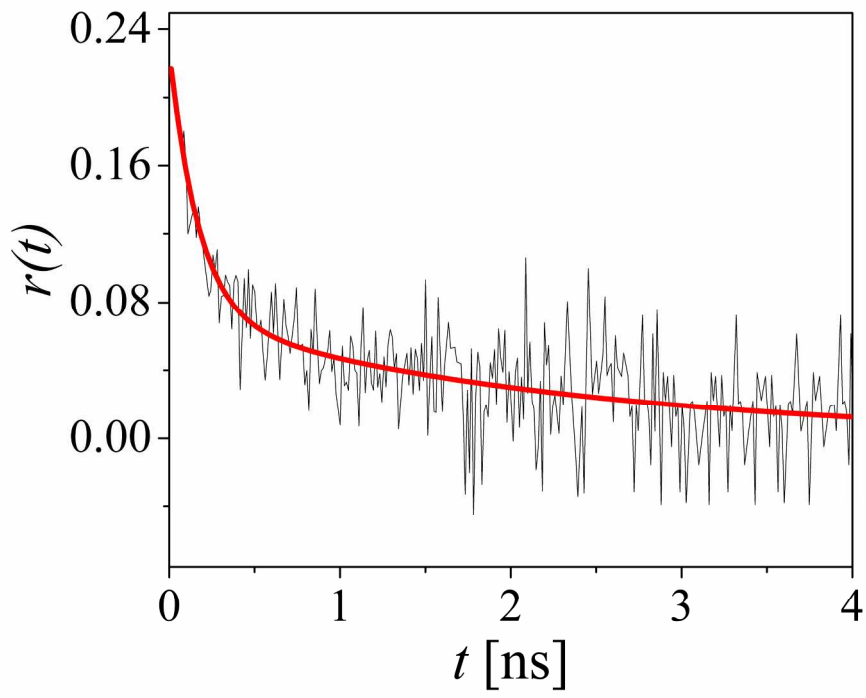


Figure 2  
215x166mm (300 x 300 DPI)

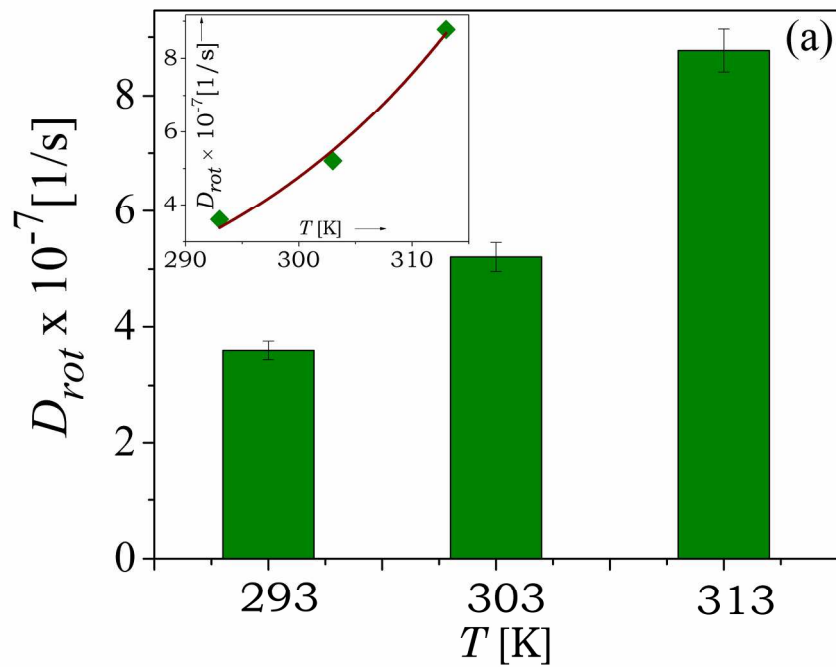


Figure 3  
207x158mm (300 x 300 DPI)

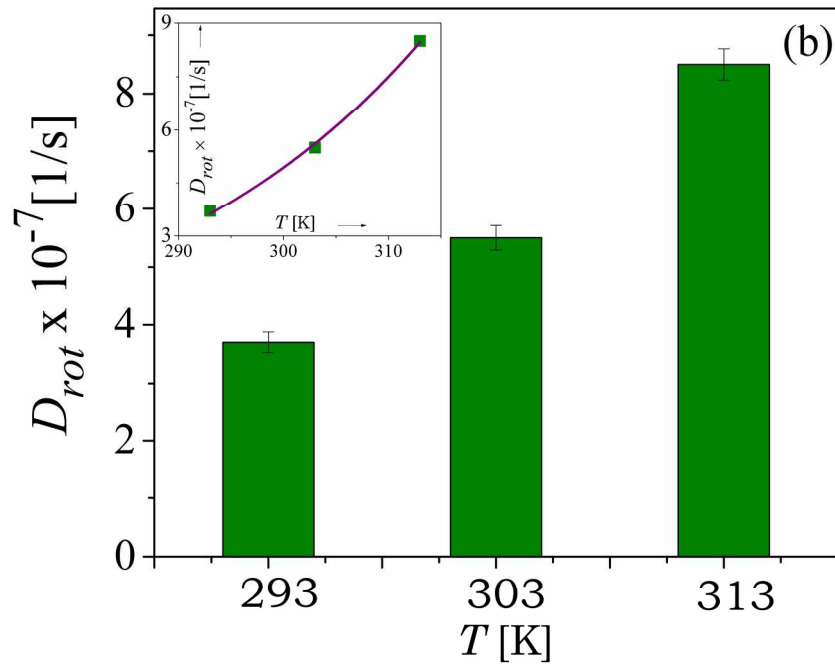


Figure 3b  
207x158mm (300 x 300 DPI)

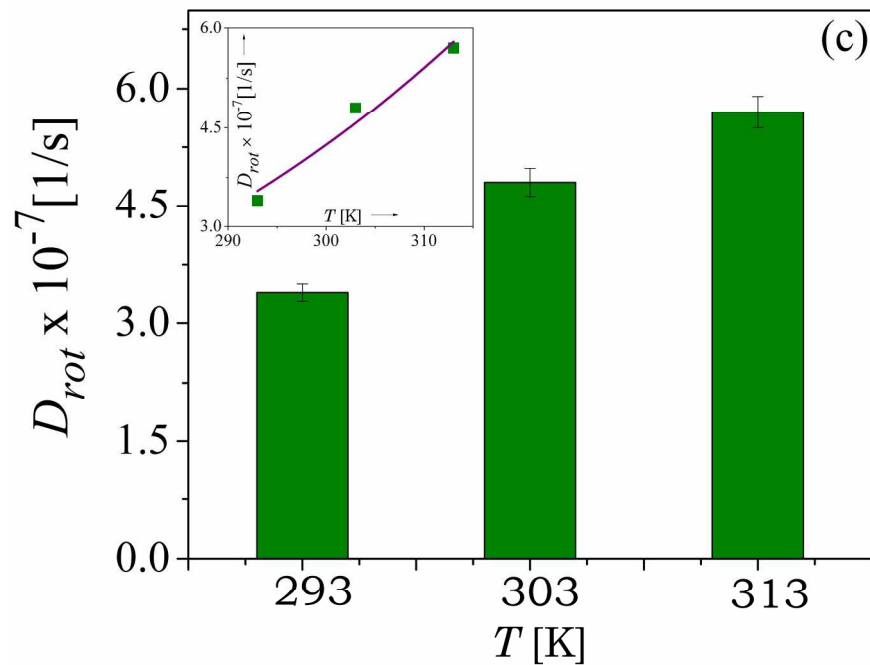
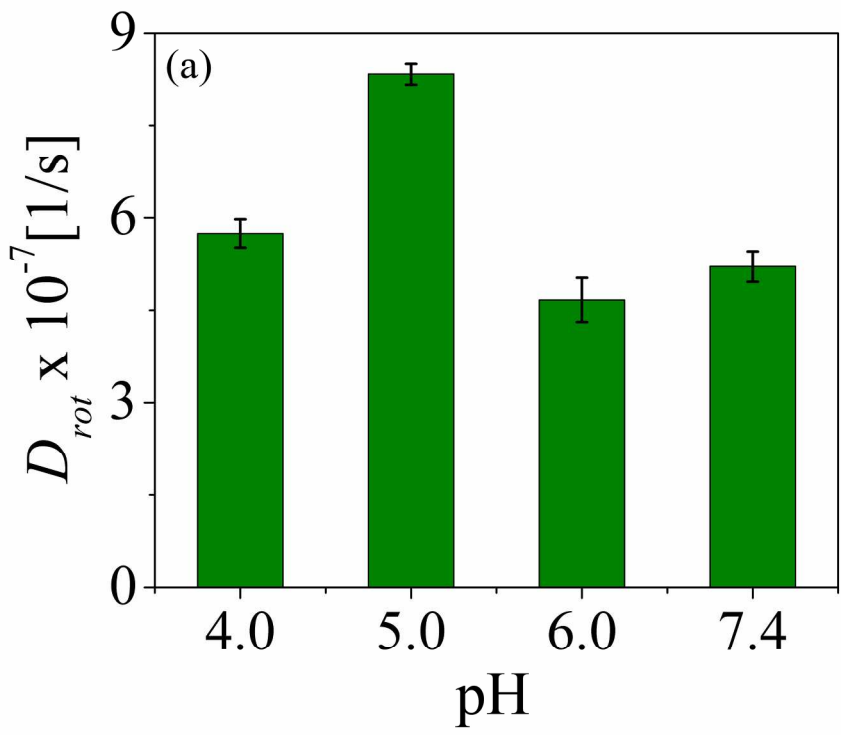
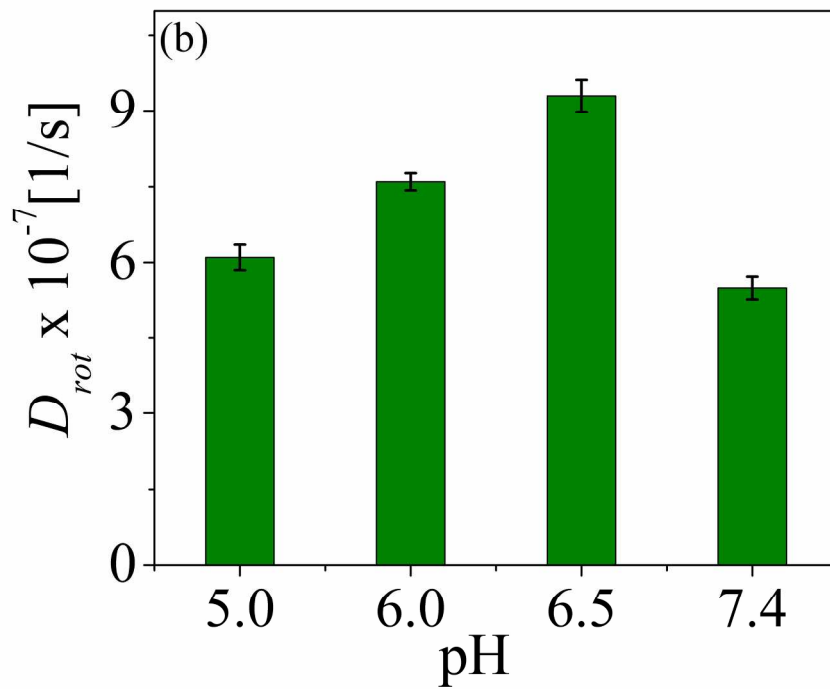


Figure 3c  
207x158mm (300 x 300 DPI)

1  
2  
3  
4  
5  
6  
7  
8  
9  
10  
11  
12  
13  
14  
15  
16  
17  
18  
19  
20  
21  
22  
23  
24  
25  
26  
27  
28  
29  
30  
31  
32  
33  
34  
35  
36  
37  
38  
39  
40  
41  
42  
43  
44  
45  
46  
47  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60

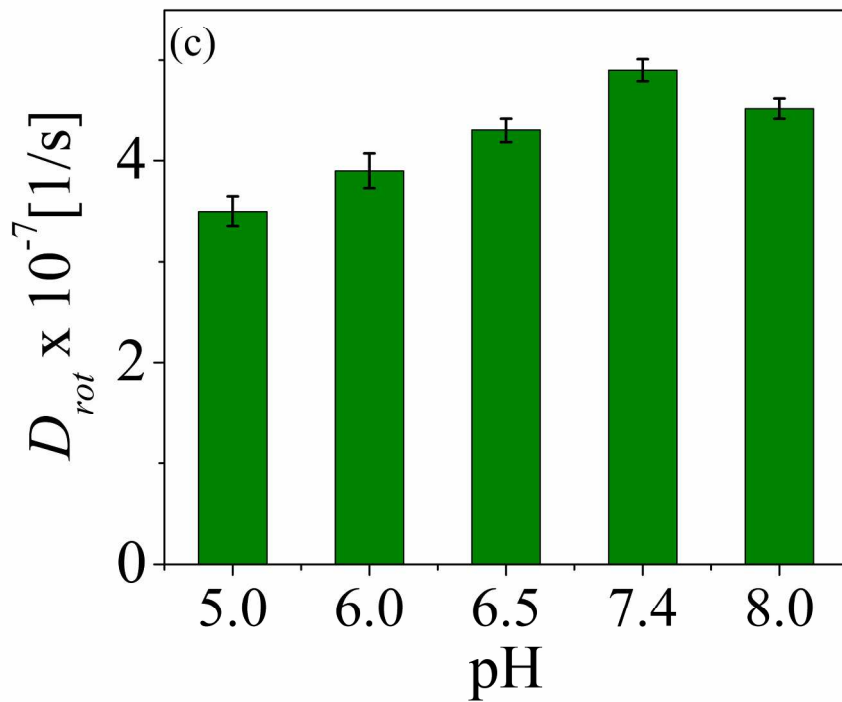


215x166mm (300 x 300 DPI)



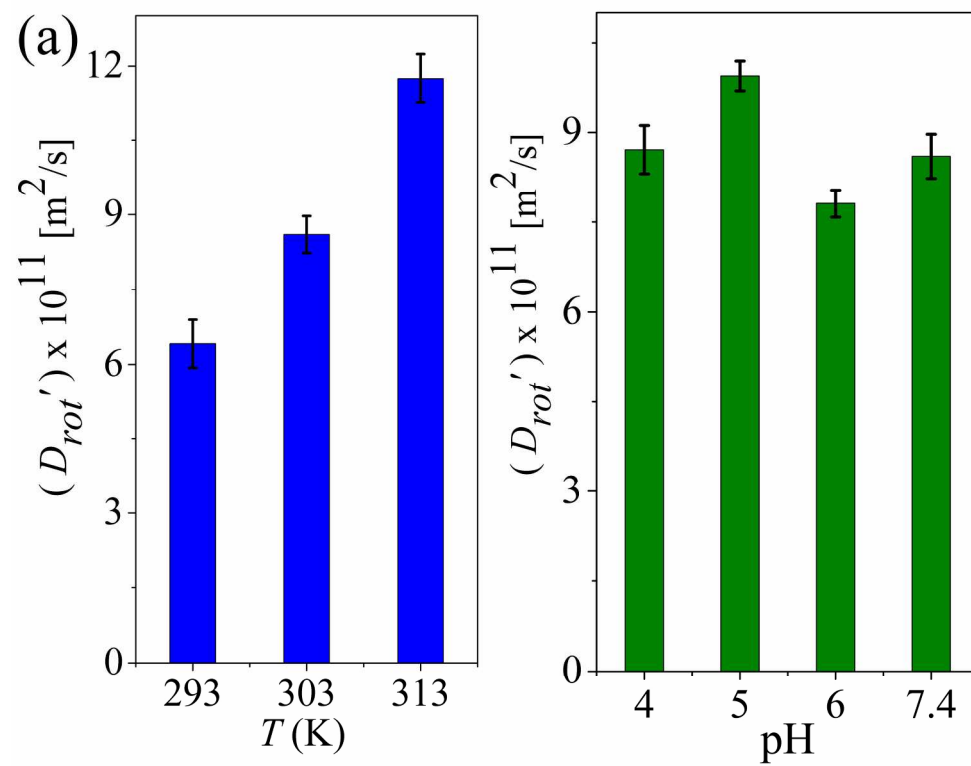
215x166mm (300 x 300 DPI)

1  
2  
3  
4  
5  
6  
7  
8  
9  
10  
11  
12  
13  
14  
15  
16  
17  
18  
19  
20  
21  
22  
23  
24  
25  
26  
27  
28  
29  
30  
31  
32  
33  
34  
35  
36  
37  
38  
39  
40  
41  
42  
43  
44  
45  
46  
47  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60

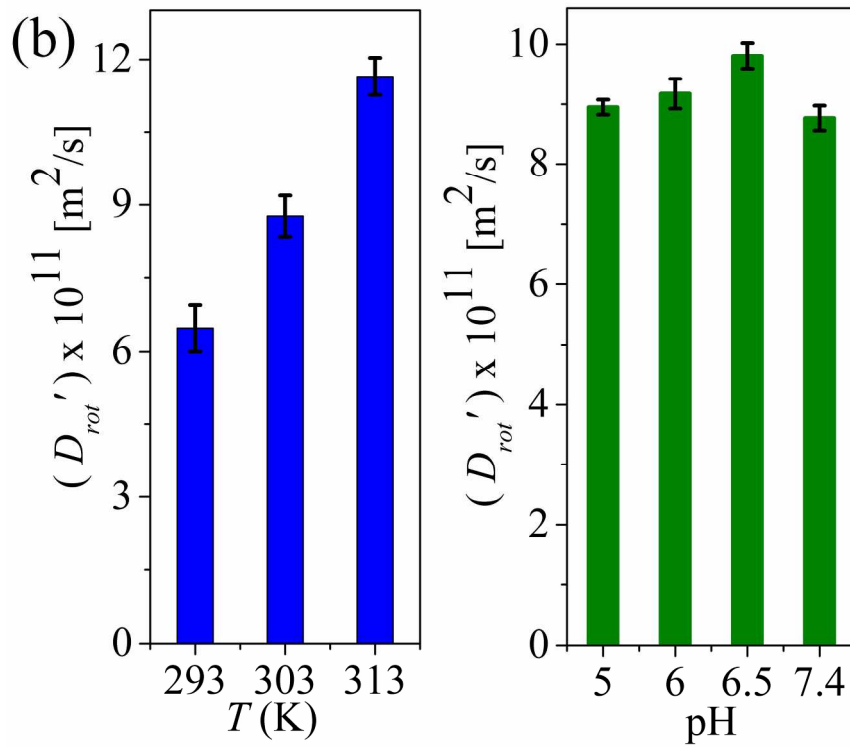


215x166mm (300 x 300 DPI)

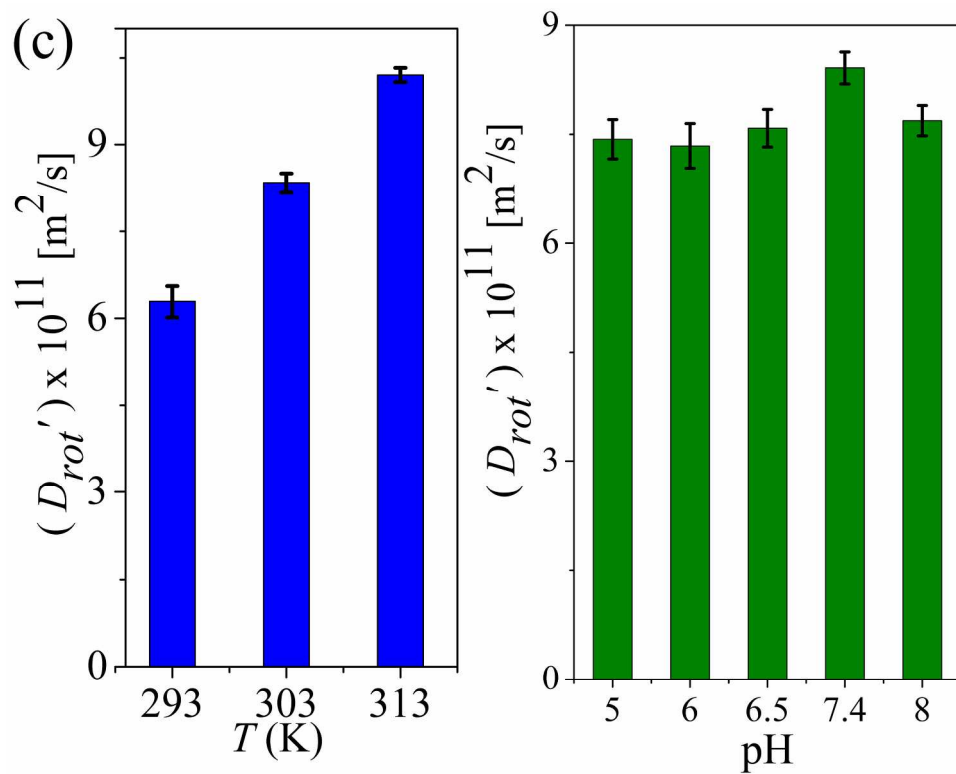




215x166mm (300 x 300 DPI)



215x166mm (300 x 300 DPI)



215x166mm (300 x 300 DPI)

## List of Tables:

1. pH values used for measurement for BSA, PSA, and CRP
2. Viscosity values of the buffer measured at (a) three temperatures at pH 7.4, and (b) five pH values at 303 K.
3. Fitting parameters obtained from  $D_{\text{rot}}$  vs. T for all three antigens

## List of Figures:

1. Schematics representing the overall process of the time-resolved anisotropy decay.
2. Time-resolved anisotropy decay curve for BSA at 30 °C and pH 7.4. The solid line represents the bi-exponential fit to the experimental anisotropy decay data.
3. The values  $D_{\text{rot}}$  at pH 7.4 and three temperatures- 293, 303 and 313 K, and the corresponding Arrhenius fitting is presented in the inset for (a) BSA (b) PSA and (c) CRP.
4. The values  $D_{\text{rot}}$  as a function of pH at T= 303 K for (a) BSA, (b) PSA, and (c) CRP.
5. The values of  $D_{\text{rot}}'$  as a function of temperature (keeping pH constant at 7.4), and pH (keeping temperature constant at 303 K) for (a) BSA, (b) PSA, and (c) CRP.