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## Unexpected origin of the magnetism in monoclinic Nb<sub>12</sub>O<sub>29</sub> from first-principles calculations

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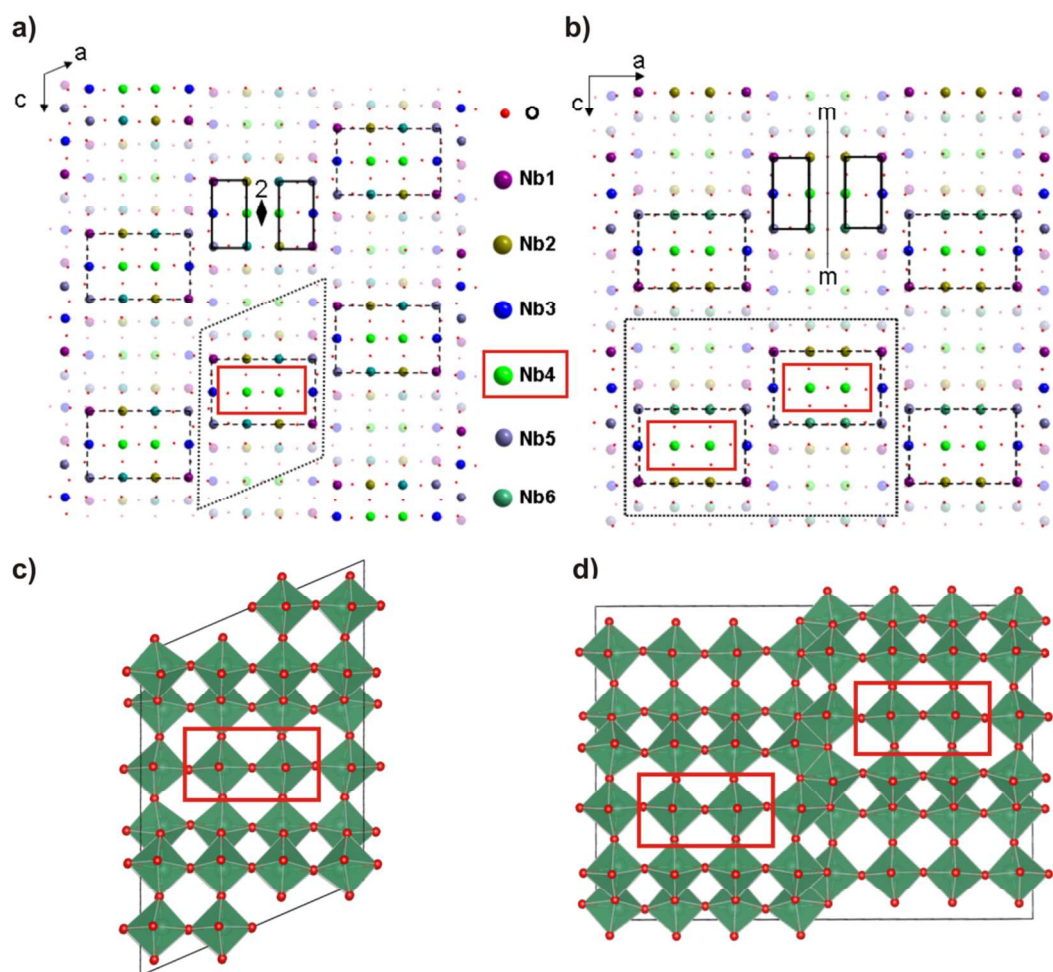
Nb<sub>12</sub>O<sub>29</sub> is a 4d transition metal oxide that occurs in two forms with different symmetries, one being monoclinic (m) and the other orthorhombic (o). The monoclinic form has unusual magnetic properties; below a temperature of 12 K, it exhibits both metallic conductivity and antiferromagnetic ordering. Here, first-principles density-functional theory calculations are used to study the structure, relative stability and electronic properties of Nb<sub>12</sub>O<sub>29</sub>. The optimized crystal structures are in good agreement with experimental observations and total energy calculations show similar stability of the two phases, while a magnetic electronic state is slightly favoured for m-Nb<sub>12</sub>O<sub>29</sub>. The unusual magnetism of the monoclinic phase originates from a Stoner instability that can be attributed to the Nb atoms with valence states close to Nb<sup>3+</sup>, i.e. the atoms with an electronic configuration ~ *d*<sup>0</sup>. This is in clear contradiction to current models in which the magnetism is attributed to the presence of localized Nb<sup>4+</sup> ions with a formal *d*<sup>1</sup> configuration. Our study demonstrates that in complex structures, magnetic properties are best not inferred from ionic models, but require a full quantum mechanical calculation for the whole unit cell.

### I. Introduction

Nb<sub>12</sub>O<sub>29</sub> has been of interest due to its unique phase relationships, interesting crystal structures, and above all its unusual magnetic properties.<sup>1-10</sup> It has two crystallographic forms at ambient temperature, one being monoclinic (m-) and another orthorhombic (o-). Both Nb<sub>12</sub>O<sub>29</sub> forms have similar short range (local) crystal structures, consisting of perovskite-like 4×3 blocks of corner-sharing NbO<sub>6</sub> octahedra that then share edges with other blocks to fill space. The difference between the two forms is the long-range ordering of the blocks,<sup>1-3,5</sup> which is schematically shown in Figure 1. The chemical representation of the 12 NbO<sub>6</sub> octahedra in the building blocks (there are 6 pairs of symmetrically equivalent octahedra per block) can be written in both the m- and o-forms as Nb<sup>4+</sup><sub>2</sub>Nb<sup>5+</sup><sub>10</sub>O<sup>2-</sup><sub>29</sub> in the commonly used ionic model.<sup>4-7</sup>

As an early 4d transition metal oxide, it is unusual that Nb<sub>12</sub>O<sub>29</sub> is experimentally found to display Curie-Weiss behaviour of the magnetic susceptibility in both forms. The o-form does not order magnetically, while the m-form does, with a Neel temperature of 12 K,<sup>3-9</sup> despite the fact that

both forms have very similar local structures.<sup>1-3</sup> Experimental measurements also show that m-Nb<sub>12</sub>O<sub>29</sub> is a metallic conductor.<sup>3-7</sup> Therefore, m-Nb<sub>12</sub>O<sub>29</sub> can be classified as only one of a handful of transition metal oxides, such as CaRuO<sub>3</sub><sup>11</sup> and Na<sub>0.7</sub>CoO<sub>2</sub><sup>12-14</sup> that are metallic conductors and yet show antiferromagnetic Curie-Weiss-like behaviour of the magnetic susceptibility.<sup>5,15</sup> Many efforts have been made to understand the origin of the magnetism of the m-form of Nb<sub>12</sub>O<sub>29</sub>.<sup>3-9</sup> In the currently accepted ionic picture, the magnetic ordering in m-Nb<sub>12</sub>O<sub>29</sub> has been attributed to the ordering of distinct *d*<sup>1</sup> (*s*=1/2) Nb<sup>4+</sup> ions in the perovskite blocks, as Nb<sup>4+</sup> formally has one unpaired *d*-electron and the other Nb ions present are Nb<sup>5+</sup>, with the non-magnetic electronic configuration *d*<sup>0</sup>. Why the m-phase magnetically orders at 12 K while the o-phase shows similar magnetic susceptibility and yet does not magnetically order remains one of the interesting puzzles in Nb<sub>12</sub>O<sub>29</sub>. Though the long range arrangements of the blocks in the o-form has been credited as frustrating the magnetic ordering in that phase<sup>6</sup>, this would be surprising



**Figure 1.** Schematic crystal structures of the monoclinic- $\text{Nb}_{12}\text{O}_{29}$  (**a,c**) and orthorhombic- $\text{Nb}_{12}\text{O}_{29}$  (**b,d**) phases, both shown in [010] projection. Atoms are depicted using collared spheres as indicated in the figure. Atoms at  $y=1/2$  are plotted half-transparent. Both structures contain similar blocks of  $3 \times 4$   $\text{NbO}_6$  octahedra, outlined by rectangular dashed lines. The monoclinic (m-) phase is a consequence of the ‘staircase’ stacking of the blocks, while the orthorhombic (o-) phase is a consequence of ‘zigzag’ stacking of the blocks. The resulting unit cells are indicated with dotted lines. The 12  $\text{NbO}_6$  octahedra in the  $3 \times 4$  blocks consist of 6 pairs of symmetry-equivalent octahedra: the pairs of octahedra are related by 2-fold symmetry in the monoclinic phase and mirror symmetry in the orthorhombic phase. The Nb4 atoms are at the centre of the  $3 \times 4$  blocks and are indicated with red rectangles. Only the Nb4 atoms in the monoclinic phase satisfy the criterion for the Stoner mechanism (Table 2).

since magnetic ordering is normally expected to be mainly determined by the local magnetic interactions. Due to limitations of the experimental characterization that arise from distinguishing the complex structures, the weak magnetism, and the intergrowths of the two forms during

materials synthesis, theoretical approaches, especially those based on parameter-free first-principles techniques, can be helpful to elucidate the electronic properties. Until now, however, the only theoretical work in this system is by Llundell, Alemany and Canadell, who discussed the dual

localized/delocalized nature of the Nb  $4d$  electrons using the tight-binding extended Hückel method.<sup>16</sup> In the present study, first principles electronic structure calculations are used to determine the electronically most stable crystal structure and the electronic properties of m-Nb<sub>12</sub>O<sub>29</sub>. Those calculations show that the magnetism of the m-phase originates from the Stoner instability of the electronic structure for the Nb atoms that have valences closer to Nb<sup>5+</sup>, in contrast with present beliefs. The information obtained here is not only helpful for understanding the structural, electrical transport and magnetic properties of the niobium oxides and related phases, but also has implications for understanding the magnetic properties of other  $4d$  or  $5d$  transition metal compounds and their surfaces, such as was demonstrated recently for the origin of magnetism on the clean and oxygen covered (110) surfaces of nonmagnetic bulk RuO<sub>2</sub>.<sup>17</sup>

## II. Details of computational techniques

In the present work, the first-principles Vienna *Ab initio* Simulation Program (VASP)<sup>18,19</sup> employing the density functional theory (DFT) within the Projector-Augmented Wave (PAW) method was used.<sup>20,21</sup> Both the Generalized Gradient Approximation (GGA) and the Local Density Approximation (LDA) were employed for the exchange and correlation energy terms.<sup>22,23</sup> In our calculations we employ the potential Nb<sub>sv</sub> which contains the Nb  $4p$  semicore electron ( $4s^2 4p^6 5s^2 4d^5$ ).

The cut-off energy of the wave functions was 500.0 eV. The cut-off energy of the augmentation wave functions was 650.0 eV. The electronic wave functions were sampled on a  $2 \times 16 \times 2$  grid with 36 irreducible  $k$ -points, and  $1 \times 16 \times 2$  grid with 16 irreducible  $k$ -points in the Brillouin zone (BZ) of the m- and o-Nb<sub>12</sub>O<sub>29</sub> forms, respectively, using the Monkhorst and Pack method.<sup>24</sup> The magnetism of the m-phase was calculated for different types of magnetic ordering. The Wigner-Seitz radii were set to 1.4 Å for O and 1.0 Å for Nb, respectively. Tests of  $k$ -mesh density and cut-off energies showed a good convergence (well within 1 meV/atom).

## III. Results and discussions

### III.A Crystal structure and chemical bonding in Nb<sub>12</sub>O<sub>29</sub>

Table 1 lists the results of the structural optimizations for the m- and o-Nb<sub>12</sub>O<sub>29</sub> phases using DFT-GGA and DFT-LDA, with

comparisons to the experimental observations. The lattice parameters from the GGA calculations are slightly larger than the experimental values, while the lattice parameters from the LDA calculations are slightly smaller than the experimental values, within 1.2%. Such results are not unusual for calculations using the DFT approximation. In the remainder of this paper we focus on the DFT-GGA results, as they are considered to be more accurate for electronic properties.

**Table 1** Calculated results (lattice parameters, energy relative to the non-magnetic (NM) o-phase) for Nb<sub>12</sub>O<sub>29</sub> using the DFT methods in comparison with experimental values. The AFM ordering is along the (100) orientation with the FM domain in one unit-cell anti-ferromagnetic to the neighbouring cell in a  $2a \times b \times c$  supercell (see text).

a) Crystal structure, formation energy and magnetic moment of m-Nb<sub>12</sub>O<sub>29</sub>, space group A2/m (nr. 12).

	GGA	LDA	Exp.
$a$ (Å)	15.9011	15.5955	15.66* <sup>2</sup> 15.6920 <sup>9</sup>
$b$ (Å)	3.8362	3.7907	3.832 <sup>2</sup> 3.8303 <sup>9</sup>
$c$ (Å)	20.9743	20.6548	20.72 <sup>2</sup> 20.7171 <sup>9</sup>
$\beta$ (°)	113.12	113.12	112.93 <sup>2</sup> 113.11 <sup>9</sup>
$V$ (Å <sup>3</sup> /fu)	588.33	561.51	572.57 <sup>2</sup> 572.64 <sup>9</sup>
$\Delta E$ (eV/f.u)	0.025(NM) 0.010(FM) 0.012(AF)		Co-existence of o- and m- phases
$M$ ( $\mu_B$ /fu)	0.82		0.84 <sup>4,5</sup>

b) Crystal structure, formation energy and magnetic moment of o-Nb<sub>12</sub>O<sub>29</sub>, space group Amma (nr. 62).

	GGA	LDA	Exp.
$a$ (Å)	29.2428	28.6550	28.90 <sup>1</sup> 28.8901 <sup>3</sup>
$b$ (Å)	3.8355	3.7991	3.835 <sup>1</sup> 3.8320 <sup>3</sup>
$c$ (Å)	20.9766	20.6041	20.72 <sup>1</sup> 20.7400 <sup>3</sup>
$V$ (Å <sup>3</sup> /fu)	588.19	560.77	574.11 <sup>1</sup> 574.02 <sup>3</sup>
$\Delta E$ (eV/f.u)	0.0		

Accurate total energy calculations find that the lowest energy solution for the o-form of Nb<sub>12</sub>O<sub>29</sub> is not magnetically ordered (NM, non-magnetic). For the m-phase, an anti-ferromagnetic (AFM) ordering is along the (100) orientation with the FM domain in one unit-cell anti-ferromagnetic to the neighbouring cell in a 2*a*×*b*×*c* supercell. All solutions found for the m-form (non-magnetic, NM, ferromagnetic, FM, and antiferromagnetic, AF) have slightly higher energies than those for the o-form, but the two polymorphs are nearly degenerate in energy from the electronic perspective (energy differences are less than 1 meV/atom). This is consistent with the experimental results, which show that it is difficult to prepare samples with only one form present. With respect to the energy of the o-phase, the nonmagnetic (NM) solution is the least favourable for m-Nb<sub>12</sub>O<sub>29</sub>, with an excess energy of 25 meV per formula-unit (f.u.) compared to the o-form. The ferromagnetic (FM) and antiferromagnetic (AF) solutions for the m-form are slightly more favourable, with energies of 10 meV/f.u. and 12 meV/f.u. in excess of that of the o-form. Thus for the m-phase, within the present computational accuracy, the ferromagnetic solution has almost the same energy as the antiferromagnetic solution. The calculated magnetic moment for the m-phase is about 1.65 μ<sub>B</sub> per unit cell, in good agreement with the experimental values of 1.64–1.80 μ<sub>B</sub> per unit cell.<sup>5-7,15</sup> Antiferromagnetic input parameters for the m-form confining the system to one chemical unit cell result in non-magnetic or ferromagnetic solutions; the antiferromagnetically ordered m-phase is predicted to have a magnetic supercell with a doubled *a*-axis. To date, magnetic supercell reflections have not been observed experimentally by neutron diffraction in m-Nb<sub>12</sub>O<sub>29</sub> due to the weakness of the expected magnetic scattering.

All the Nb ions in Nb<sub>12</sub>O<sub>29</sub> have six O neighbours in distorted octahedral coordination. The valence of Nb ion *i* is determined from the calculated Nb<sub>*i*</sub>-O<sub>*j*</sub> distances using Brown's bond valence approach:<sup>25,26</sup>

$$V_i = \sum v_{ij} = \sum \exp[(R_{ij} - R_0)/A_0], \quad (1)$$

where  $A_0=0.37$  is a universal parameter and  $R_0=1.91\text{\AA}$  is a scaling bond-length obtained for the structure optimization of rutile NbO<sub>2</sub>. The crystal structure and coordination of atoms have been discussed in detail in the literature<sup>1-3,5</sup> The local bonding of typical Nb atoms in the NbO<sub>6</sub> octahedrons is depicted in Figure S1 and all Nb-O bond lengths are listed in Table S1. Magnetic Nb atoms in the m-phase have a short Nb-O bond with bond length small or equal to 1.80 Å (see Table S1 in SI). The Nb6-O bond lengths in o-Nb<sub>12</sub>O<sub>29</sub> is quite similar to that of Nb4 in the m-phase. However, as shown in Figure S1, the distortion of the Nb6 octahedron in the o-phase, with the smallest O-Nb-O angle of about 74°, is significantly larger than

the distortion of the Nb4 octahedron in the m-phase (the smallest O-Nb-O angle is about 82°). Furthermore, the smallest O-Nb-O angle for Nb1 in the m-phase is also about 74° (Figure S1).

**Table 2** Calculated Nb bond-valences (*V* in valence units, V.U.), number of 4*d* electrons on the Nb atoms, and local magnetic moments (*M* in Bohr magnet, μ<sub>B</sub> per Nb). The indexing of the Nb atoms in the crystal structures (Nb1 ... Nb6) is shown in Figure 1. The Nb4 atom, which satisfies the criterion for Stoner magnetism (Eq. (2) in the text) is printed in bold.

o-Nb <sub>12</sub> O <sub>29</sub>				
	<i>x/a, y/b, z/c</i>	<i>V</i> (V.U.)	<i>Q</i> <sub>4<i>d</i></sub> ( <i>e</i> )	<i>M</i> <sub>Nb</sub> (μ <sub>B</sub> )
Nb1	0.0507, 0.0, 0.0362	4.77	1.22	0
Nb2	0.0505, 0.0, 0.6687	4.82	1.23	0
Nb3	0.0484, 0.0, 0.8514	4.68	1.23	0
Nb4	0.1849, 0.0, 0.0336	4.88	1.18	0
Nb5	0.1845, 0.0, 0.6675	4.87	1.18	0
Nb6	0.1848, 0.0, 0.8508	4.92	1.13	0
m-Nb <sub>12</sub> O <sub>29</sub>				
Nb1	0.1019, 0.0, 0.0667	4.77	1.22	0.01
Nb2	0.3709, 0.0, 0.1445	4.87	1.18	0.05
Nb3	0.0968, 0.0, 0.8804	4.72	1.23	0.02
Nb4	0.3695, 0.0, 0.9613	<b>4.90</b>	1.14	<b>0.10</b>
Nb5	0.1005, 0.0, 0.6988	4.82	1.22	0.02
Nb6	0.3679, 0.0, 0.7774	4.88	1.18	0.06

Using these values, the calculated total valence of the 6 unique Nb ions in Nb<sub>12</sub>O<sub>29</sub> is +28.98, closely matching the expected value of +29. As shown in Table 2 (the indexing of the Nb atoms (Nb1...Nb6) is shown in Figure 1), the calculated valences of the individual Nb ions range from +4.68 to +4.92; they do not extend down to values of +4. It is also possible to obtain information about the Nb ion charge directly from the electronic distributions within the spheres of the atoms; this

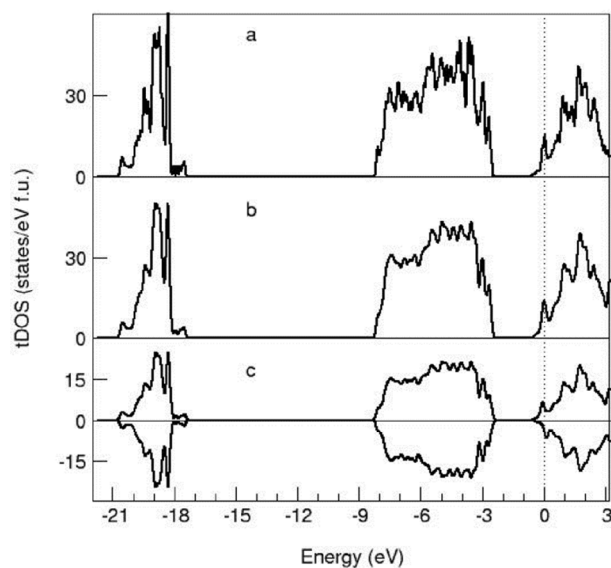
charge counting is convenient, but we note all the valence electrons in  $\text{Nb}_{12}\text{O}_{29}$ , due to their band-like character, belong to the whole crystal and are not actually localized at individual ions. That this is the case can be seen in Figures 2 and 3, where the Nb  $4d$  states are shown to form bands with widths of 2 to 4 eV with details discussed in next section; if the electron states were localized on the ions then the band widths would be much narrower. We also note that there is no unique definition of the size of atoms in solids - the number of electrons integrated in the sphere of an atom strongly depends on the sphere size. However, here we are interested only in the relative number of  $4d$  electrons in the Nb spheres. We find that the number of electrons occupying Nb  $4d$  states ranges from 1.13 to 1.22 e within the Wigner-Seitz spheres of Nb ( $R_{\text{W.S.}} = 1.0 \text{ \AA}$ ).

The Nb4 ions in  $m\text{-Nb}_{12}\text{O}_{29}$  are calculated have the largest local magnetic moment ( $\sim 0.1 \mu_{\text{B}}$ /atom). The isosurfaces of the spin-densities for the Nb atoms in the FM  $m$ -phase are shown in Figure S2). Significant magnetic moments ( $\sim 0.06$ ) can also be found for the Nb2 and Nb6 ions. These are substantially lower than the moments expected for 1 localized unpaired electron on a particular site. Interestingly, all the moment-bearing Nb ions are calculated to also have the highest chemical valence ( $\sim 4.9$ ) and correspondingly the smallest  $d$  electron orbital occupancy. This is in contrast to the expectation that the magnetism should originate from the Nb ions that are closest in formal valence to  $\text{Nb}^{4+}$ . This shows the failure of the simple ionic model, i.e.  $\text{Nb}^{4+}_2\text{Nb}^{5+}_{10}\text{O}^{2-}_{29}$ , to correctly describe the system. The results clearly point to an itinerant electron origin for the observed antiferromagnetism.

### III.B Electronic and magnetic properties of the $\text{Nb}_{12}\text{O}_{29}$ phases

Figure 2a shows the calculated total density of states (tDOS) for the o- (upper), and m- (middle and lower) forms of  $\text{Nb}_{12}\text{O}_{29}$ ; both non-magnetic (middle) and magnetic (lower) solutions are shown for  $m\text{-Nb}_{12}\text{O}_{29}$ . Figure 2b compares the partial density of Nb  $4d$  states in the  $\text{Nb}_{12}\text{O}_{29}$  phases. The strong overall similarity between the tDOS curves of the o- and m- phases is apparent, corresponding to the strong relationship between the two structures. Considering the full energy range, a simple chemical model can describe the general features of the tDOS plots (Figure 2a). At energies far below the Fermi Energy ( $E_{\text{F}}$ , 0 eV), a band with a bandwidth of about 3.3 eV (from about  $-20.8 \text{ eV}$  to  $-17.5 \text{ eV}$ ) is composed of O  $2s$  states. There is a gap of about 9.3 eV separating this O  $2s$  sub-band from another sub-band (from about  $-8.2 \text{ eV}$  to  $-2.3 \text{ eV}$ ) that is dominated by O  $2p$  states with some admixture of Nb  $4d$  states. The band at positive

energies that begins just below  $E_{\text{F}}$  is dominated by Nb  $4d$  states, separated by a gap of about 1.8 eV from the O  $2p$  sub-band below it. This is the mostly empty Nb  $4d$  band manifold. Distinct peaks in the total density of states are seen at  $E_{\text{F}}$  in both phases.



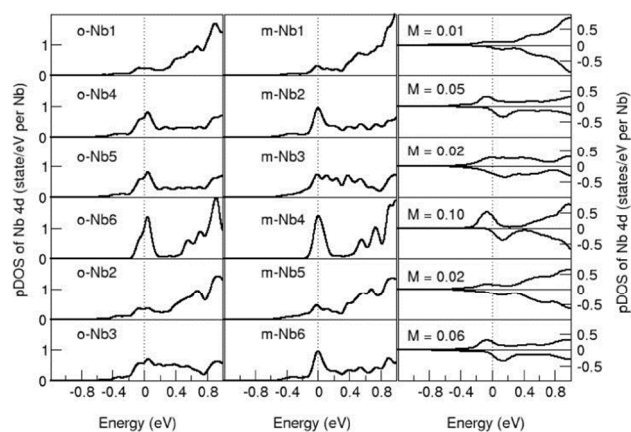
**Figure 2.** Total calculated density of states (tDOS) over a wide energy range for non-magnetic o- $\text{Nb}_{12}\text{O}_{29}$  (a), and non-magnetic (b) and ferromagnetic (FM) (c)  $m\text{-Nb}_{12}\text{O}_{29}$ .

Detailed information about the electronic structures of the phases around  $E_{\text{F}}$  is presented in Figure 3, which compares the partial DOS (pDOS) of the Nb  $4d$  states for o- and  $m\text{-Nb}_{12}\text{O}_{29}$  without spin polarization. There are significant differences in the shapes of the  $4d$  pDOS curves for the different Nb sites. The pDOS for the Nb2, Nb4, and Nb6 atoms in  $m\text{-Nb}_{12}\text{O}_{29}$  without spin-polarization have much higher peaks around  $E_{\text{F}}$  than the other atoms in this phase; the pDOS for Nb4 is especially distinct and high;  $E_{\text{F}}$  is exactly positioned at this peak of the Nb4 pDOS. The resulting high density of electronic states at  $E_{\text{F}}$  results in a higher calculated energy for the non-magnetic solution of the  $m$ -phase. The difference is primarily that the peaks in the o-form near  $E_{\text{F}}$  are slightly split in energy. The result is that the Nb pDOS are not as sharply peaked in the o-form, with the highest pDOS calculated to be actually very slightly above  $E_{\text{F}}$ .

In the 1930s, Stoner investigated the relationship between the exchange interaction and kinetic contribution for a band structure and proposed the well-known Stoner criterion:<sup>27-29</sup>

$$I \cdot D(E_F) \geq 1 \quad (2)$$

Where  $D(E_F)$  is the density of states at the Fermi level. The Stoner parameter which is a measure of the strength of the exchange correlation is denoted  $I$ . The Stoner criterion has been successfully applied to predict the magnetism of different compounds.<sup>17, 30-32</sup>

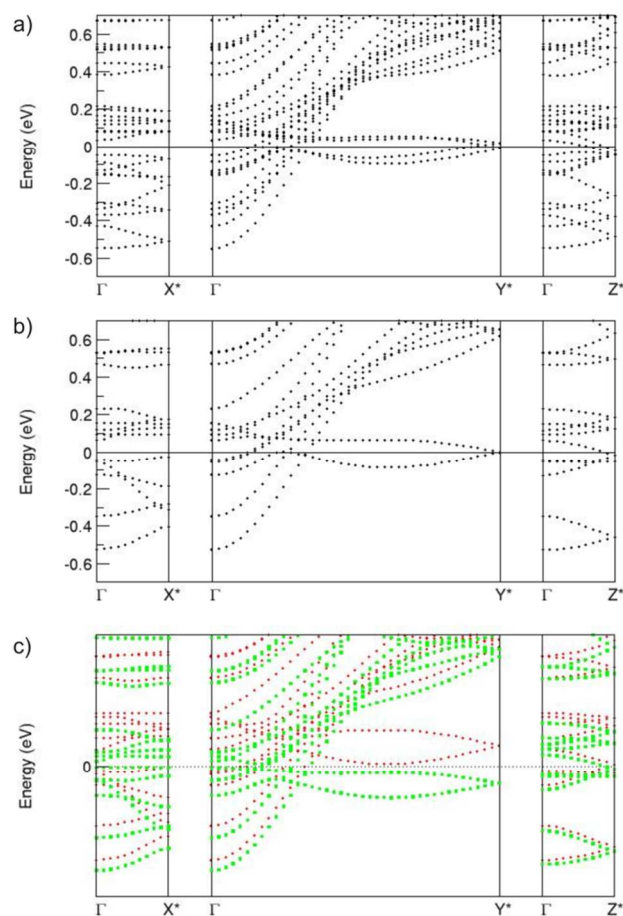


**Figure 3.** Partial density of states (pDOS) near  $E_F$  for the Nb atoms in  $\text{Nb}_{12}\text{O}_{29}$ , as calculated for the o-phase (left), and the m-phase in the non-spin-polarized solution (center) and in the ferromagnetic solution (right). Only states close to the Fermi level (set at 0 eV) are shown.

The Nb4 atom in  $\text{m-Nb}_{12}\text{O}_{29}$  has a large  $D(E_F)$  value of about 1.6 states/eV per atom while the  $D(E_F)$  values for rest of the Nb atoms as well as all the Nb atoms in  $\text{o-Nb}_{12}\text{O}_{29}$  are significantly smaller (0.8 states/eV per atom) (see Figure 2). Unfortunately, there are no data on the Stoner parameter for Nb. If we use  $I = 0.9$ , the value for Fe,<sup>31</sup> the Stoner criterion is satisfied for the Nb4 atom in  $\text{m-Nb}_{12}\text{O}_{29}$ ,  $I \cdot D(E_F) \sim 1.45, \geq 1$ , whereas for the other Nb atoms  $I \cdot D(E_F) \sim (0.2 \text{ to } 0.7) < 1$ . This is in agreement with the local moment of the Nb4 atom in the m-phase as shown in Table 2. The Nb4 atoms are the Nb atoms located at the center of the blocks of  $3 \times 4$   $\text{NbO}_6$  octahedra, indicated with red rectangles in Figure 1.

Figure 4 also shows the dispersion curves of the non-spin-polarized  $\text{Nb}_{12}\text{O}_{29}$  phases. The curves are very similar, except that the number of states for the o-phase is twice as high as the number of states for the m-phase due to the relationship of the

unit cells (the cell volume of the orthorhombic phase is close to double that of the m-phase.) A subtle difference can be found at  $k$ -point  $Y^*$ : the states are degenerate for the m-phase, whereas in the o-phase they are split in two, with the Fermi level set in between. This explains the splitting of the pDOS peaks in Figure 3b. Correspondingly, as is shown in the dispersion curves of the magnetic m-phase in the spin-polarized calculations, the state at  $Y^*$  splits into two due to spin-splitting, correspondingly the density of states dominated by Nb 4d states at the Fermi level is strongly reduced.



**Figure 4.** Dispersion curves of the band structure close to the Fermi level from the centre ( $\Gamma$ ) to the axes  $X^*$ ,  $Y^*$  and  $Z^*$  in the Brillouin zone for (a)  $\text{o-Nb}_{12}\text{O}_{29}$  (non-magnetic solution), (b) the non-magnetic solution for  $\text{m-Nb}_{12}\text{O}_{29}$ , and (c) the ferromagnetic (FM) solution for  $\text{m-Nb}_{12}\text{O}_{29}$ . The red dots represent the states for the majority (spin-up) electrons and green dots represent the minority (spin-down) electrons.

It is also of interest to analyse the anisotropy in charge carrier transport properties. Figure 4 shows clearly a strong anisotropy of the energy-wavevector dispersion curves along the three axes. The bands show very small dispersion along  $a$ , taking the length ratio into account ( $b^*/a^* = 7.7$ , and  $c^*/a^* = 1.4$ , and  $b^*/c^* = 5.5$ ). This indicates a strong anisotropy of effective masses for the charge carriers. The band just below the Fermi level along  $a^*$  has a dispersion of about 0.08 eV, while the some of the bands along  $c^*$  show a dispersion of about 0.2 eV. These states are highly localized. Some of the bands along the  $b^*$ -axis have dispersions larger than 1 eV, while four bands show small dispersions of just about 0.4 eV, reflecting a difference in the localization of the states in this direction, though they are substantially more delocalized than along  $a^*$  and  $c^*$ . Eigen-character analysis reveals that the localized bands are dominated by Nb4  $4d$  states for the m-phase and Nb6  $4d$  states for the o-phase, corresponding to the sharp peaks in the pDOS around  $E_F$  for the non-magnetic o-and m-phases seen in Figure 2.

## V. Conclusions

First-principles DFT calculations have been performed for the two forms of Nb<sub>12</sub>O<sub>29</sub>. The calculations showed only small energy difference (~0.01 eV/fu) between the monoclinic and the orthorhombic forms, with the o-phase slightly favoured. This agrees with experimental observations that the o-form, samples can be prepared with high purity, while the m-form is sometimes found intergrowing with the o-form. For the m-form, a spin-polarized solution is favoured over the non-magnetic solution. The calculated lattice parameters and magnetic moments are in good agreement with the available experimental data. The magnetism in the m-form originates from the high density of states of the itinerant 4d states of the atoms indexed as Nb4 atoms, fulfilling Stoner's magnetic instability criterion. Both electronic configurations and bond valence analysis showed that the spin-polarized Nb atoms (indexed Nb4 in the m-phase) are close to a valence state of 5+. This conclusion is in contrast to the current belief that the magnetism can be attributed to the Nb<sup>4+</sup> ions when an ionic model is considered. Electronic band structure analysis predicts a strong anisotropy in the charge carrier mobility.

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## Unexpected origin of the magnetism in monoclinic Nb<sub>12</sub>O<sub>29</sub> from first-principles calculations

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### TOC

The unusual magnetism of m-Nb<sub>12</sub>O<sub>29</sub> is attributed to the Nb atoms with valence states close to Nb<sup>5+</sup>(*d*<sup>0</sup>). This is in clear contradiction to general belief which the magnetism is attributed to the Nb<sup>4+</sup> (*d*<sup>1</sup>) atoms.

