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Low thermal conductivity and rapid synthesis of n-type cobalt skutterudite via hydrothermal method

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Abstract

We report low thermal conductivity for n-type cobalt skutterudites synthesized via a rapid hydrothermal procedure combined with evacuated-and-encapsulated heating. Different synthesis temperatures are investigated to obtain the single phase of CoSb₃. The resulting samples are characterized using x-ray diffraction pattern, scanning electron microscopy, Hall and density measurements. A remarkably low thermal conductivity of 1.33 - 1.46 Wm⁻¹K⁻¹ at room temperature can be attained for the pristine CoSb₃, which is comparable with or even lower than the filled CoSb₃ obtained from solid state reaction. Regarding the requirement of lengthy annealing and reaction at high temperature using solid state reaction, our remarkably rapid and low temperature procedure fabrication together with the significantly low thermal conductivity presents major progress in fabricating cobalt skutterudites using hydrothermal synthesis methods.
**Keyword:** Rapid Synthesis, Hydrothermal Methods, Cobalt Skutterudite, Thermal Conductivity, Thermoelectric Properties.

1. **Introduction**

Waste energy recovery via novel technologies such as thermoelectric generators has recently received great attention especially due to wane of petroleum resources and environmental pollution problems. Energy harvesting from the exhaust heat for practical applications is feasible by using thermoelectric devices. The efficiency of a thermoelectric material is evaluated from its figure of merit $zT = \frac{\sigma S^2 T}{\kappa}$, where $S$ is the thermopower (Seebeck coefficient), $\sigma$ is the electrical conductivity, $\kappa$ the thermal conductivity, and $T$ the absolute temperature.

Among potential thermoelectric materials, skutterudites have attracted great research interests.\(^1\) Skutterudites with TPn\(_3\) (T= Co, Rh, or Ir and Pn=P, As, or Sb) structure crystallize in the cubic lattice of CoAs\(_3\)-type with space group Im\(_3\).\(^2\) CoAs\(_3\)-type structures possess two intrinsic voids per unit cell. The voids especially for the CoSb\(_3\) skutterudite are large enough to accommodate guest ions of alkaline earth or rare earth elements as filled skutterudites.\(^3,4\) The rattling motion of the filler atoms inside the Sb-icosahedral voids could decrease the lattice thermal conductivity by broadening the spectrum of scattered phonon modes.\(^5\) One of the objectives for
lowering the lattice thermal conductivity of skutterudites is to reduce the $\text{Im}^3 \left( T_b^5 \right)$ space group symmetry by distorting the pnictogen ring (Sb-ring) via substituting Pn ion with Ge, Sn, Te or Se elements. $^4,6-9$

Nanostructured fabrication has been proven an effective approach to reduce lattice thermal conductivity. It is a common practice now to reduce the lattice thermal conductivity through scattering heat-carrying phonons at interfaces by introducing nanoparticles in the matrix. Based on the Callaway formalism, the effect of particle size on the lattice thermal conductivity can be described in terms of the phonon relaxation rates as $^{10-12}$

$$
\tau_C^{-1} = \tau_U^{-1} + \tau_N^{-1} + \tau_{p-d}^{-1} + \tau_{e-ph}^{-1} + \tau_b^{-1}.
$$

where $C$ denotes combined scattering rate, $U$, $N$, $p-d$, $e-ph$, and $b$ represent phonon umklapp processes, phonon Normal, point-defect, electron-phonon, and boundary, respectively. Phonon scattering rate on the boundaries depends on the grain size as $\tau_b^{-1} = 3 x v_s / 2 R$; where $x$, $v_s$, and $R$ are the content of nanoparticles in the matrix, the speed of sound, and nanoparticle size, respectively. $^{13}$ The shape and size of nanoparticles ($R$), and their content are some crucial parameters in phonon scattering rate. Therefore the fabrication condition plays an important role in reducing thermal
conductivity with the objective to enhance $zT$ values. Developing nanostructured thermoelectric materials in minimizing heat transport without deteriorating the electrical properties may require fine tuning the synthetic conditions. A good nanostructured thermoelectric material needs to possess endotaxial characteristic.$^9,^{14}$ The endotaxially dispersed nanoparticles need to be coherent with embedded fine-grains in their vicinity.

Preparation cost also receives special attention as one of the key factors in evaluating the thermoelectric materials for practical usages. Developing synthesis procedure with short duration would be one of the objectives to reduce the fabrication costs. Recently, Uher et al. have reported a rapid procedure for producing cobalt skutterudite using the melt spinning method, which takes about 20 h.$^{15}$ Their method is promising for practical application as compared with those traditional solid state reaction methods that usually requires long annealing time of 7 to 10 days.$^{16-19}$ We have recently reported a rapid synthesis of cobalt skutterudite using modified polyol process.$^{25}$ However, there are some disadvantages of the polyol methods. The triethylene glycol (TEG) used as the solvent in polyol synthesis is costly; the synthesized powders requires 750 ml ethanol to rinse off viscous TEG. Besides, in the course of polyol synthesis, it requires special attention to avoid the formation of $\text{Sb}_2\text{O}_3$. Compared with solid state reaction methods, the hydrothermal synthesis
process is not particularly common for fabricating CoSb$_3$.$^{20}$ In this work we have developed a hydrothermal synthesis procedure to produce CoSb$_3$ compound at low temperatures. Various hydrothermal synthesis temperatures with a short duration of 12 h are investigated aiming at finding optimum condition of producing pure CoSb$_3$ phase. As a result, we are able to obtain nearly single phase of CoSb$_3$ at the synthesis temperature of 290°C using the hydrothermal method for the first time. For those synthesized at lower temperatures, it requires heating hydrothermally synthesized powders at 580°C for a short period of 5 h in an evacuated-and-encapsulated ampoule. In particular, all these samples exhibit low thermal conductivity ranging from 1.33 Wm$^{-1}$K$^{-1}$ to 1.46 Wm$^{-1}$K$^{-1}$. The thermal conductivity reported for the pristine CoSb$_3$ synthesized from solid state reaction methods falls in the range of 3 and 10 Wm$^{-1}$K$^{-1}$ at room temperature.$^{2, 21-23}$ Yang et al. reported a low thermal conductivity of 1.94 Wm$^{-1}$K$^{-1}$ around room temperature for nano-sized p-type CoSb$_3$ synthesized using modified polyol process.$^{24}$

2. Experimental Procedure

Cobalt skutterudites CoSb$_3$ were synthesized using hydrothermal methods. Powders of SbCl$_3$ and CoCl$_2$·6H$_2$O were weighted and loaded into a Teflon cup (~185 mL volume) containing 110 mL deionized water. For the present container volume
and solvent amount, 10.65 millimole SbCl$_3$ and required amount of CoCl$_2$·6H$_2$O (with Sb:Co ratio 3:1) was used. The solution was then sonicated at 47°C for 30 min, followed by adding 74.26 millimole of NaOH and sonicated for another 15 min. To create a reductive environment, 78.56 millimole NaBH$_4$ was added to above solution, followed by sonication at 47°C for 30 min and then loaded into an autoclave and heated in an oven with heating rate of 2.6°C/min at various temperatures for 12 h. The resulting product was then washed using ethanol and deionized water. Drying of the powders was carried out using a rotary evaporator vacuum dryer. To avoid oxidation of as-synthesized powders, the Ar gas was used to purge the flask before drying and introduced into the flask while breaking the vacuum after drying. The dried powders were then cold-pressed at 16.88 MPa to form a parallelepiped. The prepared parallelepiped was then loaded into a Pyrex ampoule, which was evacuated using a diffusion pump to reach 10$^{-5}$ Torr to 10$^{-6}$ Torr and then sealed.$^{26}$ The parallelepiped in the encapsulated ampoule was then heated in a tubular furnace at a rate of 2.6 °C/min to 580°C, and hold for 5 h. The phase identification of as-synthesized powders and as-sintered samples was carried out using a Shimadzu XRD-6000 diffractometer equipped with Fe Kα radiation. The morphology of the samples was examined using a Zeiss AURIGA field emission scanning electron microscope (FE-SEM). Electrical resistivity and thermopower measurements were
simultaneously carried out from room-temperature down to liquid nitrogen temperature. Thermopower measurements were carried out using steady-state techniques. A type E differential thermocouple connected to a Keithley 2000 multimeter was used to measure the temperature difference between the hot and cold ends of the sample. The thermally generated Seebeck voltage across the sample was measured using a Keithley 2182 nanovoltmeter.\textsuperscript{27} The thermopower of sample was obtained by subtracting the thermopower of the Cu. Electrical resistivity measurements were performed using standard four-probe techniques, reversing the current sources to cancel thermoelectric voltages. Thermal conductivity measurements were carried out using transient plane source techniques with very small temperature perturbations of the sample material by the Hot Disk thermal constants analyzer as described in detail elsewhere.\textsuperscript{26} The uncertainty for the electrical resistivity, thermopower, and thermal conductivity is about ±3%, ±4% and ±4%, respectively. Hall measurements was performed using the van der Pauw method under an applied magnetic field of 0.55 T (ECOPIA:HMS -3000). The relative density of all the samples was measured using the Archimedes’ method.

3. Results and Discussion

Fig. 1 shows the x-ray diffraction (XRD) patterns of the as- synthesized CoSb\textsubscript{3}
powders at 170°C, 230°C, and 290°C, respectively. The phase evolution of CoSb, CoSb$_2$ and CoSb$_3$ can be readily seen for hydrothermal reaction carried out at various temperatures. The samples synthesized at 170°C shows CoSb and Sb as the major phases. At the synthesized temperature of 230°C, the desired phase of CoSb$_3$ coexists with CoSb$_2$, CoSb, and Sb. Nearly single phase of CoSb$_3$ can be obtained at 290°C. The CoSb$_3$ phase, however, can be achieved by heating the powders, which are synthesized below 290°C, in evacuated-and-encapsulated ampoules at 580°C for a short period of 5 hours. Fig. 2 displays the powder XRD patterns of all the as-heated samples. It can be seen that all the samples exhibit the CoSb$_3$ phase as the major phase with tiny amount of CoSb$_2$. The lattice constant is refined from the XRD data for all the three samples. The obtained values are 9.030(2), 9.034(2), and 9.038(2) Å for samples synthesized at 170°C, 230°C, and 290°C, respectively, which are in good agreement with other reports for the title system.\textsuperscript{2,28}

Fig. 3 shows the FE-SEM micrographs from fractured samples heated at 580°C and synthesized at 170°C (Fig. 3a) and 290°C (Fig. 3b), respectively. Porosity and various grain sizes in the range of 30 and 200 nm can be readily seen. The bulk density of all the three samples is measured about 71 to 78 % of the theoretical density (Table I), indicating porous nature as seen in Fig. 3. The carrier concentration and mobility obtained from Hall measurements at room temperature are presented in
Table I. The results of these measurements confirm that electrons are the majority charge carriers for all the samples. The low electron mobility might be associated with their porous microstructures and relatively small particle sizes.

Now we turn to the effects of synthetic condition on the transport properties. Fig. 4 shows the temperature dependence of electrical conductivity from 300 K down to liquid nitrogen temperature for samples synthesized at various temperatures of 170°C, 230°C and 290°C. The electrical conductivity decreases with decreasing temperature for all the samples. Fig. 5 displays the temperature dependence of thermopower from room temperature down to liquid nitrogen temperature for samples synthesized at various temperatures of 170°C, 230°C, and 290°C. Negative thermopower observed for all the samples indicates that electrons are the majority charge carriers, being consistent with the Hall measurements (Table I). The absolute value of thermopower decreases with decreasing temperature for all the samples. The sample synthesized at 290°C displays the smallest absolute value of thermopower among all the samples within the whole measured temperature range, while the one synthesized at 170°C displays the largest magnitudes of thermopower in the whole measured temperature range. By assuming acoustic phonons as predominant electron scattering resources for materials with a single parabolic conduction band, the thermopower and carrier concentration can be respectively expressed as $^{29-31}$
\[
S = \pm \frac{k_B}{e} \left( 2 \frac{F_1(\eta)}{F_0(\eta)} - \eta \right) \text{ and } (2)
\]

\[
n = \frac{4}{\sqrt{\pi}} \left( 2\pi m^* k_B T / h^2 \right)^{3/2} F_{1/2}^1(\eta), \text{ (3)}
\]

where \( \eta = E_F/k_B T \) is the reduced Fermi energy, \( F_j \) the Fermi-Dirac integrals of order \( j \), \( k_B \) is the Boltzmann’s constant, \( h \) Planck’s constant, and \( m^* \) the electron effective mass.

By substituting the room-temperature thermopower and carrier concentrations values (Table I) together with the tabulated magnitudes for Fermi-Dirac integrals in Eq.(2) and (3), \( \eta \) and \( m^* \) are estimated for all the three CoSb\(_3\) samples and results are presented in Table I. The reduced Fermi level is measured from the conduction band edge, and the largest \( \eta \) value of -1.8 is obtained for the sample that was synthesized at 170°C. The estimated \( \eta \) values show that the Fermi level moves towards the conduction band edge by increasing the carrier concentration. The effective mass is extended around the free electron mass \( m_o \) with the largest value of about 1.11 \( m_o \) for the sample synthesized at 170°C (Table I). The number of energy states at the conduction band edge can be estimated by inserting the effective mass into the effective density of states \( 2(2\pi m^* k_B T / h^2)^{3/2} \); the derived values is on the order of \( 10^{19} \) cm\(^3\) and directly rely on the \( m^* \) values for all the three samples (Table I).

The similar curves of both electrical conductivity and thermopower with respect
to temperature might indicate similar conduction mechanism governing the electronic transport for all the three samples. The electrical conductivity for the three samples (Fig. 4) reduces at a faster rate with decreasing temperature in the higher temperature regime ($238 \leq T \leq 300$ K) when compared with that in the lower temperature regime ($77 \leq T \leq 130$ K). Therefore, the activation type conduction mechanism at higher temperatures and the Mott’s $T^{1/4}$ law at the lower temperatures might be responsible for the dominant conduction mechanisms of the title CoSb$_3$ samples. To get insight of probably dominated conduction mechanism, the electrical conductivity curves at $238 \leq T \leq 300$ K and $77 \leq T \leq 130$ K is fitted with the Arrhenius relation and Mott’s model, respectively,$^{32,33}$

$$\sigma(T) = \sigma_o \exp\left(-\frac{E_a}{k_B T}\right) \quad \text{and} \quad \sigma(T) = \sigma_o \exp\left[-\frac{T_o}{T}\right]^{1/4},$$

where $\sigma_o$ is the pre-exponential constant, $E_a$ the activation energy, the characteristic temperature $T_o = \beta \alpha^3/(k_B N_F)$, $\beta$ a constant, $\alpha^{-1}$ the decay length of the localized state wave function, and $N_F$ the density of hopping states at the Fermi level. The fitted results are shown in Figs. 6 and 7. The energy band gap ($E_g = 2E_a$) of each sample is
calculated from the slopes of the Ln ($\sigma$) versus $T^{-1}$ curves and presented in Table I. The obtained $E_g$ for the three samples synthesized at 170°C, 230°C, and 290°C is about 73, 81.8, and 83.6 meV, respectively. These values are in agreement with the theoretical computations for direct and pseudo band gap magnitudes for the CoSb$_3$ cell.$^{34,35}$ As all the three $E_g$ values are larger than $k_B T$ for $T \leq 300$ K, applying the Mott’s theory of variable-range hopping (VRH) at $77 \leq T \leq 130$ K for the title samples should be acceptable.$^{33}$ It can be also seen that the electrical conductivity for all the three samples obeys the Mott’s VRH conduction model at $77 \leq T \leq 130$ K. These results might indicate that the conduction is dominated by variable range hopping process. Based on the decreasing absolute values of thermopower with decreasing temperature for all the three samples, the temperature dependence of thermopower can also be expressed as$^{36,37}$

$$S = \frac{k_B}{2e} \frac{W^2}{k_B T^3} \left( \frac{d \ln N(E)}{dE} \right)_{E=E_F},$$

where $W$ is the hopping energy, $N(E)$ density of hopping states, and $E_F$ the Fermi level. In the framework of VRH process, $W \sim k_B (T_0 T^3)^{1/4}$, and the temperature dependence of thermopower in Eq. (6) can be expressed more clearly as
The thermopower curves of all the three samples in Fig. 5 are fitted with $T^{1/2}$ using Eq. (7) for the same temperature region as in the electrical conductivity curve fitting (Fig. 7). Fig. 8 shows that the absolute value of thermopower increases linearly with $T^{1/2}$ for $77 \leq T \leq 130$ K. For the Mott’s model of hopping conduction to be applicable for the title system, the energy independency of density of hopping states near the Fermi level is assumed. Based on the fitting results for both the electrical conductivity and thermopower, we assume the variable range hopping is the dominate conduction mechanism for as-synthesized CoSb$_3$ samples at $77 \leq T \leq 130$ K. By inserting the obtained $T_o$ values from the fitted curves of Fig. 7 into Eq.(7) together using the slope obtained from thermopower fitting in Fig. 8, we can estimate the magnitude of the hopping energy $W$ and derivative of the logarithmic density of hopping states at the Fermi level, $\left[ \frac{d \ln N(E)}{dE} \right]_{E=E_F}$. The hopping energy at $T=100$ K is calculated and presented in Table II.

Fig. 9 shows the temperature dependence of power factor, $PF=\sigma S^2$, for all the CoSb$_3$ samples synthesized at various temperatures. It can be readily seen that the largest power factor value of 0.72 $\mu$W/cm-K$^2$ is attained at 300 K for the sample synthesized at 170°C. The power factor of all the samples turns smaller and levels off
to low values at about 77 K.

Fig. 10 shows the temperature dependence of the total thermal conductivity ($\kappa$) for the CoSb$_3$ samples. The room-temperature thermal conductivity for the samples synthesized at 170°C, 230°C, and 290°C is 1.34 Wm$^{-1}$K$^{-1}$, 1.46 Wm$^{-1}$K$^{-1}$, and 1.33 Wm$^{-1}$K$^{-1}$, respectively. The room-temperature thermal conductivity is markedly smaller than those reported for the parent CoSb$_3$ system.$^{2,21,40}$ In addition, the low thermal conductivity of our samples is also comparable with or even lower than that of doped, filled, or nanostructured CoSb$_3$ prepared using solid state reaction.$^{9,39-43}$

The thermal conductivity increases with decreasing temperature for all the three samples, which might arise from increasing phonon mean free path upon cooling.$^{44}$ The thermal conductivity at 122 K is 2.95 Wm$^{-1}$K$^{-1}$ for the sample synthesized at 230°C. The electronic component of the thermal conductivity $\kappa_e$ can be obtained using the Wiedemann-Franz law $\kappa_e/\sigma = LT$, where $\sigma$ being the electrical conductivity and $L$ the Lorenz number. The Lorenz number can be expressed as a functional Fermi-Dirac integrals, $F_j(\eta)$, as Eq. (8)$^{2,29,30}$

$$L = \left(\frac{KB_e}{e}\right)^2 \left[ \frac{3F_0(\eta)F_2(\eta) - 4F_1^2(\eta)}{F_0^2(\eta)} \right],$$  \hspace{1cm} (8)

The magnitude of $L$ for all the three samples is estimated using the tabulated
amounts for Fermi-Dirac integrals and the results are presented in Table I. The obtained $L$ values show that the Lorenz number is slightly increased by decreasing the magnitude of $\eta$. By inserting the estimated $L$ value into the Wiedemann-Franz law, we have calculated $\kappa_e$ component and the related results is displayed in Fig. 11a. These results indicate that the electronic contribution to the thermal conductivity is quite small for all the three samples due to their relatively small electrical conductivity. The largest and smallest room-temperature $\kappa_e$ is $2.65 \times 10^3$ Wm$^{-1}$K$^{-1}$ and $2.41 \times 10^3$ Wm$^{-1}$K$^{-1}$ for the samples synthesized at 290°C and 230°C, respectively. The $\kappa_e$ component decreases with decreasing temperature for all the three samples such that its value at 122 K is about 5-times smaller than the related amount at 300 K. The lattice component of thermal conductivity ($\kappa_L$) is obtained by subtracting $\kappa_e$ from the total thermal conductivity ($\kappa = \kappa_L + \kappa_e$) and shown in Fig. 11b. It can be readily seen that the total thermal conductivity $\kappa$ mostly comes from the lattice contribution. While the correlation between $\kappa_L$ and temperature indicates the characteristics of crystalline solids with dominate phonon contribution to the thermal conductivity, efforts for modeling the lattice contribution solely with umklapp phonon-phonon scattering did not show acceptable fitting. For the present CoSb$_3$ structure, assumption of combined-scattering process seems more reasonable, especially for $T \leq 240$ K. According to Callaway,$^{45}$ the lattice thermal conductivity can be expressed as
\[ \kappa_L = \frac{k_B}{2\pi^2 v_s} \left(\frac{k_B T}{\hbar}\right)^3 \int_0^{\theta_D/T} \frac{y^4 e^y}{\tau_C^{-1} (e^y-1)^2} \, dy, \]  

(9)

where \( y = \hbar \omega / k_B T \) is dimensionless parameter of integration, \( \omega \) the phonon frequency, \( \theta_D \) the Debye temperature, \( v_s \) the velocity of sound, and \( \tau_C^{-1} \) the combined phonon scattering rate. Recalling Eq. (1) and ignoring the normal phonon scattering rate, \( \tau_N^{-1} \), the \( \tau_C^{-1} \) in Eq. (9) can be expressed as follows

\[ \tau_C^{-1} = A T \omega^2 \exp \left(-\frac{\theta_D}{\alpha T}\right) + B \omega^4 + C \omega^2 + 3xv_s/2R, \]  

(10)

where \( A, B, \) and \( C \) are constants, and \( \alpha \) equal to about 2. The terms in Eq. (10) represents umklapp phonon-phonon scattering, point-defect scattering, electron-phonon scattering, and grain boundary scattering rates, respectively. The parameter \( x \) and the particle size \( R \) are already explained in Eq. (1). Since the temperature region in our collected data is not that low for grain boundary scattering to dominate the lattice thermal conductivity of the title CoSb\(_3\) samples, the main contribution might well be associated with the umklapp phonon-phonon scattering, point-defect scattering, and electron-phonon scattering at 122 \( \leq T \leq 300 \) K. Similar thermal conductivity behavior associated with the mixed phonon scattering
mechanism has been reported for the CoSb₃ system at the same temperature region.²¹,⁴⁴

The thermoelectric figure-of-merit $zT$ is calculated using the values of the power factor ($\sigma S^2$) and the total thermal conductivity obtained for all the three samples and is shown in Fig. 12. The largest $zT$ magnitude of about 0.016 is attained at 300 K for the sample synthesized at 170°C, which is comparable with earlier reports for the pristine CoSb₃ system.⁴²,⁴⁷,⁴⁸ The room-temperature $zT$ for the samples synthesized at 230°C and 290°C display almost the same value of about 0.008. For all the three samples, the $zT$ decreases with decreasing temperature.

4. Conclusion

Rapid synthesis of n-type CoSb₃ can be achieved using hydrothermal methods combined with evacuated-and-encapsulated sintering. The pure CoSb₃ phase can be attained at 290°C for the duration of 12 h. The phase impurities for samples synthesized at lower temperatures can be removed by heating at 580°C for a short period of 5 h in an evacuated-and-encapsulated ampoule. The electrical conductivity data are analyzed to facilitate the understanding of the dominate conduction mechanism for hydrothermally synthesized CoSb₃. It is found that the activated type conduction dominates for $238 \leq T \leq 295$ K. The variable-range hopping model of
conduction can be well fitted to both the electrical conductivity and thermopower curves for $77 \leq T \leq 130$ K. The thermal conductivity displays remarkably low room-temperature values for all the three CoSb$_3$ samples. The lowest room-temperature lattice thermal conductivity is about 1.33 Wm$^{-1}$K$^{-1}$ for the sample synthesized at 290°C, which by comparison is as low as the filled cobalt skutterudite compounds. The largest $zT$ of 0.016 is attained at room temperature for the sample synthesized at 170°C.

Acknowledgments

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References


Figure Captions

**Fig. 1**, Powder XRD pattern of hydrothermally reacted samples at various temperatures (insets) for 12 h. Herein $hkl$ indices denote CoSb$_3$ phase, (+), (*) and ($) symbols represent CoSb$_2$, CoSb and Sb impurity phases, respectively.

**Fig. 2**, Powder XRD patterns of as-hydrothermally reacted samples (Fig. 1) after heating at 580°C for 5 h into evacuated ampoules; thereat $hkl$ indices denote CoSb$_3$ phase and (+) symbol represents CoSb$_2$ impurity phase.

**Fig. 3**, SEM micrographs from the polished surface of samples hydrothermally synthesized at (a) 170°C and (b) 290°C for duration of 12 h, followed by heating at 580°C for 5 h into evacuated ampoules.

**Fig. 4**, Electrical conductivity of CoSb$_3$ samples hydrothermally synthesized at various temperatures (inset of figure) followed by heating into evacuated ampoules at 580°C for 5 h.

**Fig. 5**, Thermopower of CoSb$_3$ samples hydrothermally synthesized at various temperatures (inset of figure) followed by heating into evacuated ampoules at 580°C.
for 5 h.

**Fig. 6.** Plot of $\ln\sigma$ versus $T^{-1}$ for CoSb$_3$ samples hydrothermally synthesized at various temperatures (inset); the activation energies are calculated using the slopes.

**Fig. 7.** Plot of $\ln\sigma$ versus $T^{-1/4}$ in the framework of the Mott’s variable-range hopping model for CoSb$_3$ samples hydrothermally synthesized at various temperatures (inset).

**Fig. 8.** Plot of thermopower versus $T^{1/2}$ in the framework of the Mott’s variable-range hopping model for the CoSb$_3$ samples hydrothermally synthesized at various temperatures (inset).

**Fig. 9.** Power Factor for CoSb$_3$ samples hydrothermally synthesized at various temperatures (inset) followed by heating into evacuated ampoules at 580°C for 5 h.

**Fig. 10.** Total thermal conductivity ($\kappa$) of CoSb$_3$ samples hydrothermally synthesized at various temperatures (inset of figure) followed by heating into evacuated ampoules at 580°C for 5 h.

**Fig. 11.** (a) Electronic component ($\kappa_e$) and (b) the lattice component ($\kappa_L = \kappa - \kappa_e$) of
the total thermal conductivity ($\kappa$) calculated for the title CoSb$_3$ samples.

**Fig. 12.** Figure-of-merit, $zT$, attained for CoSb$_3$ samples hydrothermally synthesized at various temperatures (inset) followed by heating at 580°C for 5 h.
Table Captions

**Table I.** Room-temperature physical and transport properties for CoSb$_3$ samples hydrothermally synthesized at various temperatures of 170°C, 230°C and 290°C for 12 h, followed by heating at 580°C for 5 h.

**Table II.** Some physical properties calculated from curve fitting of electrical conductivity and thermopower of the title CoSb$_3$ samples in the framework of the Mott’s model of variable-range hopping conduction.
Powder XRD pattern of hydrothermally reacted samples at various temperatures (insets) for 12 h. Herein hkl indices denote CoSb$_3$ phase, (+), (*) and ($) symbols represent CoSb$_2$, CoSb and Sb impurity phases, respectively.
Powder XRD patterns of as-hydrothermally reacted samples (Fig. 1) after heating at 580°C for 5 h into evacuated ampoules; thereat hkl indices denote CoSb₃ phase and (+) symbol represents CoSb₂ impurity phase.

289x203mm (150 x 150 DPI)
Fig. 3 (a & b)

120x193mm (96 x 96 DPI)
Electrical conductivity of CoSb3 samples hydrothermally synthesized at various temperatures (inset of figure) followed by heating into evacuated ampoules at 580°C for 5 h.

Electrical conductivity of CoSb3 samples hydrothermally synthesized at various temperatures (inset of figure) followed by heating into evacuated ampoules at 580°C for 5 h.
Fig. 5

Thermopower (μV/K) vs Temperature (K) for CoSb₃ at different temperatures: 170°C, 230°C, and 290°C.
Fig. 6

CoSb$_3$

$E_a = 36.5$ meV

$E_a = 40.9$ meV

$E_a = 41.8$ meV

170°C

230°C

290°C

289x203mm (150 x 150 DPI)
Fig. 7

CoSb$_3$

287x201mm (150 x 150 DPI)
Fig. 8

![Graph showing thermopower vs. T^{1/2} for CoSb₃ at different temperatures: 170°C, 230°C, and 290°C.](image)

287x201mm (150 x 150 DPI)
Power Factor for CoSb3 samples hydrothermally synthesized at various temperatures (inset) followed by heating into evacuated ampoules at 580°C for 5 h.

Fig. 9

Power Factor (µW/cm-K²) vs Temperature (K)

CoSb3

- 170°C
- 230°C
- 290°C

Power Factor for CoSb3 samples hydrothermally synthesized at various temperatures (inset) followed by heating into evacuated ampoules at 580°C for 5 h.
Total thermal conductivity ($\kappa$) of CoSb$_3$ samples hydrothermally synthesized at various temperatures (inset of figure) followed by heating into evacuated ampoules at 580°C for 5 h.
Fig. 11

289x203mm (150 x 150 DPI)
Fig. 12

![Graph showing zT vs. Temperature for CoSb$_3$ at 170°C, 230°C, and 290°C.](image)

289x203mm (150 x 150 DPI)
Table I. Room-temperature physical and transport properties for CoSb₃ samples hydrothermally synthesized at various temperatures of 170°C, 230°C and 290°C for 12 h, followed by heating at 580°C for 5 h.

<table>
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<tr>
<td>Carrier concentration</td>
<td>10¹⁸ cm⁻³</td>
<td>- 4.6</td>
<td>- 8.2</td>
<td>- 9.1</td>
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<tr>
<td>Hall mobility</td>
<td>cm²/V.s</td>
<td>9.51</td>
<td>6.24</td>
<td>6.27</td>
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<tr>
<td>Electrical conductivity</td>
<td>10²Ω⁻¹m⁻¹</td>
<td>6.51</td>
<td>5.97</td>
<td>6.51</td>
</tr>
<tr>
<td>Thermopower</td>
<td>µV/K</td>
<td>-333</td>
<td>-252</td>
<td>-237</td>
</tr>
<tr>
<td>Lattice thermal conductivity</td>
<td>W/mK</td>
<td>1.342</td>
<td>1.457</td>
<td>1.327</td>
</tr>
<tr>
<td>Reduced Fermi level, η</td>
<td>----</td>
<td>-1.8</td>
<td>-0.75</td>
<td>-0.5</td>
</tr>
<tr>
<td>Electron effective mass (m*/m₀)</td>
<td>----</td>
<td>1.112</td>
<td>0.789</td>
<td>0.797</td>
</tr>
<tr>
<td>Effective density of states</td>
<td>10¹⁹ cm⁻³</td>
<td>2.94</td>
<td>1.76</td>
<td>1.79</td>
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<tr>
<td>Energy band gap</td>
<td>meV</td>
<td>73</td>
<td>81.8</td>
<td>83.6</td>
</tr>
<tr>
<td>Lorenz number, L</td>
<td>(kₑ/e)²</td>
<td>2.038</td>
<td>2.097</td>
<td>2.119</td>
</tr>
</tbody>
</table>
Table II. Some physical properties calculated from curve fitting of electrical conductivity and thermopower of the title CoSb$_3$ samples in the framework of the Mott’s model of variable-range hopping conduction.

<table>
<thead>
<tr>
<th>Synthesis temperature (°C)</th>
<th>$T_o$ (K)</th>
<th>$W \sim k_B(T_o T^3)^{1/4}$ (eV)</th>
<th>$(T=100 \text{ K})$</th>
<th>$\left[ \frac{d \ln N(E)}{dE} \right]_{E=E_F}$ (eV)$^{-1}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>170</td>
<td>123266.9</td>
<td>0.051</td>
<td>20.33</td>
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<tr>
<td>230</td>
<td>80564.15</td>
<td>0.046</td>
<td>15.19</td>
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<tr>
<td>290</td>
<td>76549.97</td>
<td>0.045</td>
<td>13.74</td>
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</tr>
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