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Modeling the multiple shape memory effect and temperature memory effect in amorphous polymers

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Amorphous polymers achieve the shape memory effect from the tremendous change in the chain mobility of the glass transition. The span of the glass transition region has a direct influence on the shape recovery behavior. In this paper, we investigated the shape memory behavior of Nafion, which has an extremely broad glass transition region. We measured the influence of the shape memory programming temperature on the recovery response and multiple shape memory effect. We applied a finite deformation, nonlinear viscoelastic model with a discrete spectrum of relaxation times to describe the shape memory behavior of the material. The parameters of the relaxation spectrum was determined from the master curve of the relaxation modulus. The model was implemented for finite element analysis and applied to design the multiple switchable pattern transformation of a Nafion membrane.

1 Introduction

Amorphous cross-linked polymers achieve their shape memory behavior through the reversible glass transition. When the temperature is high, the amorphous networks are in their mobile rubbery state and can be easily deformed to a temporary programmed shape. The programmed shape can be fixed under either force or displacement constraint by cooling to the immobile glassy state. The polymer can recover the permanent shape when heated above the glass transition temperature ($T_g$). The temperature range of the glass transition temperature region strongly influences the temperature range of the shape recovery region\textsuperscript{1–3}. Amorphous shape memory polymers (SMPs) typically exhibit a glass transition region spanning 15$^\circ$–20$^\circ$C. A narrower glass transition temperature span is desired for a shorter recovery time. In Safranski and Gall\textsuperscript{4}, the authors systemically investigated the influence of chemical structure and cross-linker density on the glass transition region and the shape recovery behavior. By tailoring the chemical compositions, the temperature span of glass transition region of the acrylate family of polymers can be varied from 20$^\circ$C to 50$^\circ$C.

Xie\textsuperscript{5} demonstrated that the commercially available Nafion PFSA membrane has a broad glass transition that spans $T = 55^\circ$C – 130$^\circ$C. By employing this broad glass transition region, multiple shape recovery behavior can be achieved by successively programming the material at different temperatures. The authors showed that the activation temperature for shape recovery of Nafion correlated with the deformation temperature of the programming step\textsuperscript{6,7}. This phenomena is known as the temperature memory effect (TME)\textsuperscript{8}. The multiple and temperature memory behaviors have also been demonstrated by Li \textit{et al.}\textsuperscript{9,10} using a versatile copolymer with a tailorable broad glass transition behavior. The broad glass transition region can be used to program multiple shapes at distinct temperatures in the glass transition and provide a more complex shape recovery response. In a recent work, Yu and Qi\textsuperscript{11} demonstrated the TME also exists for an acrylate-based SMP with a relative narrow glass transition region.

Numerous works\textsuperscript{2,12–17} have investigated the shape memory behavior of amorphous networks by modeling the glass transition. These models typically assume a temperature dependent relaxation time or viscosity. The tremendous change in relaxation time during the glass transition allows the material to store a temporary shape and recover a permanent shape. Our group developed generalized finite deformation models, where the relaxation time is dependent on the temperature, nonequilibrium structure through the fictive temperature, and solvent concentration. The models were used to the study the effect of the deformation temperature\textsuperscript{3}, physical aging\textsuperscript{14}, solvent absorption\textsuperscript{18} and stiff inclusions\textsuperscript{19} on the shape recovery response. We also developed thermomechanical experiments and analysis methods to determine the model parameters and validate the modeling assumptions. The

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generalized models were able to predict the shape memory behavior under a wide variety of shape programming and recovery temperature and mechanical conditions, but required multiple experiments to obtain the model parameters. Yu et al. developed a one dimensional viscoelastic model with a small number of parameters for the multiple shape memory behavior. The model was able to reproduce well the experimental data, but the authors assumed an even distribution of relaxation times. Here, we present a method for measuring the relaxation spectrum to accurately model the multiple and temperature memory effect.

The paper is arranged as follows. Section 2 describes the experimental methods to characterize the mechanical properties and shape memory behaviors of Nafion. We then extended the standard rheological model to describe the large deformation, nonlinear viscoelastic behavior of Nafion and similar amorphous polymers with a broad glass transition region. The model is composed of one elastic element to represent the hyperelastic behavior at high temperature and multiple Maxwell elements arranged in parallel with a temperature dependent relaxation time to describe the viscoelastic behavior. In the following section, an efficient method is presented to obtain the model parameters through time-temperature superposition stress relaxation test. Finally, the model with obtained parameters was adopted to simulate the shape memory recovery experiments of Nafion sheets programmed and deployed at different temperatures. The model was also implemented for finite element analysis to design a sequence of pattern transformation for a Nafion membrane.

2 Methods

Nafion® PFSA membrane with equivalent molecular weight 1100 was purchased (Dupont, Wilmington, DE, USA) and cut into strips of dimensions 15 mm × 5 mm × 0.25 mm for dynamic mechanical analysis (DMA) measurements described below. Prior to the DMA measurements, the specimens were annealed for 30 minutes at 160°C to remove the water in the specimens.

2.1 Material characterization

2.1.1 Stress relaxation: Stress relaxation experiments were performed using the DMA Q800 (TA Instruments, New Castle, DE, USA). The Nafion strips were equilibrated at 190°C for 15 minutes and then cooled to 40°C in 6°C increments. The specimens were equilibrated at each test temperature for 15 minutes, then subjected to a 0.4% strain and held for 20 minutes for stress relaxation. The relaxation modulus as a function of time was measured at each temperature and then shifted to the reference temperature, $T_0 = 160°C$, using the method described in Ferry. This procedure provided a master curve of relaxation modulus, which was used to determine the parameters of the viscoelastic relaxation spectrum and the temperature-dependence shift factor $a(T)$.

2.1.2 Dynamic temperature sweep: The dynamic temperature sweep test was used to measure the temperature dependent storage modulus, loss modulus and $\tan\delta$ of the Nafion strips. The specimen was equilibrated at 20°C for 20 minutes and then heated to 180°C at 1°C/min. A 0.4% dynamic strain applied at 1 Hz at each temperature to measure the dynamic mechanical properties.

2.2 Shape recovery experiments

2.2.1 Temperature memory: The DMA Q800 was also used to measure free recovery response of Nafion strips programmed at different deformation temperatures, 155°C, 120°C and 85°C. The specimens were equilibrated at the deformation temperature for 15 minutes, then stretched to 50% engineering strain in two minutes. The specimens were cooled to 40°C at 3°C/min at constant strain and held isothermally for 5 minutes to fix the temporary shape before unloading. To recover the permanent shape, the strips were heated to 180°C at 1°C/min. The displacement of the strips were measured using the zero force mode of the Q800. We chose a relatively low cooling and heating rate to reduce the influence of heat conduction on the shape memory performance.
2.2.2 Multi-staged shape recovery: To investigate the influence of the recovery temperature, the specimens were stretched to 80% engineering strain at 155°C and cooled to 40°C. To recover the permanent shape, the specimens were heated in discrete steps at 3°C/min. The temperature steps were 40°C, 100°C, 120°C, 140°C and 160°C. The specimens were held for 20 minutes at each step and the displacement was measured under zero force mode.

2.2.3 Dual programming shape recovery: We performed a two-step shape memory programming test. The specimen was equilibrated at 155°C (the first programming temperature) for 15 minutes and stretched to 40% engineering strain. The specimen was cooled to 120°C (the second programming temperature) at 3°C/min and held for 5 minutes at isostrain condition. The specimen was then stretched another 40% engineering strain before cooling to 40°C at 3°C/min to fix the temporary shape. To recover the permanent shape, the specimens were heated to 170°C at 1°C/min under zero force mode. The experiment investigated two additional sets of programming temperatures: (155°C, 85°C) and (120°C, 85°C).

3 Numerical modeling

3.1 Constitutive modeling

A finite deformation, nonlinear viscoelastic model with multiple parallel relaxation mechanisms was used to describe the shape memory behavior of Nafion. The deformation gradient \( \mathbf{F} \) is defined to map a point in the reference undeformed configuration to a point in the current deformed configuration. To describe viscoelasticity, the deformation gradient is multiplicatively decomposed into elastic and viscous parts as: \( \mathbf{F} = \mathbf{F}^e \mathbf{F}^v \). The total and elastic part of the volumetric deformation ratio are

\[
G = \text{det} \left( \mathbf{F}^v \right), \quad G^e = \text{det} \left( \mathbf{F}^e \right).
\]

where \( G \) is the equilibrium shear modulus, \( G^e \) are the nonequilibrium shear moduli and \( \kappa \) is the bulk modulus.

The Cauchy stress response \( \sigma \) is described as the sum of a time-independent equilibrium distortional component, \( N \) time-dependent nonequilibrium distortional components and a time-independent volumetric component:

\[
\sigma = \frac{1}{J^e} G^e \left( \mathbf{b} - \frac{1}{3} \text{tr} (\mathbf{b}) \right) + \sum_{i} \frac{1}{J^i} G^i \left( \mathbf{b}^e - \frac{1}{3} \text{tr} (\mathbf{b}^e) \right) + \frac{1}{2J^p} \kappa (J^2 - 1) \mathbf{1},
\]

where \( G^e \) is the equilibrium shear modulus, \( G^i \) are the nonequilibrium shear moduli and \( \kappa \) is the bulk modulus.

The following nonlinear evolution equation is adopted for the internal strains \( \mathbf{b}^e \).

\[
- \frac{1}{2} \mathbf{L} \mathbf{b}^e \mathbf{b}^{-1} = \frac{s^e}{2 \nu^e} a(T),
\]

where \( \mathbf{L} \mathbf{b}^e = \mathbf{F} \left( \mathbf{F}^e \mathbf{F}^v \right)^{-1} \mathbf{F}^v \mathbf{F}^e \mathbf{F}^v \mathbf{F}^v \) and \( \mathbf{L} \) is the Lie time derivative. The parameter \( \nu^e \) is the shear viscosity at the reference temperature and \( a(T) \) is the temperature-dependent shift factor. The stress relaxation time is related with the shear viscosity as \( \tau^e = \nu^e / G^e \).

3.2 Parameter determination

As described in Sec. 2.1.1, the master curve of the relaxation modulus was obtained as shown in Fig. 1(a). Linearizing the viscoelastic model to small strain, the uniaxial tension stress relaxation modulus at the reference temperature can be expressed as,

\[
E(t) = E^e + \sum_{i} E^i \exp \left( - \frac{t}{\tau^i} \right)
\]
where $E^{eq}$ is the equilibrium Young’s modulus and $E_{i}^{neq}$ are the nonequilibrium Young’s moduli. Because the master curve is extremely broad, it is difficult to fit eq. (3) directly to the master curve of the relaxation modulus to obtain the relaxation spectrum $(\tau_{i}^{ref}, E_{i}^{neq})$. Instead, we first evaluated a continuous relaxation spectrum $h(\tau)$ from the master curve \(^20\),

$$E(t) = \int_{-\infty}^{\infty} h(\tau) \exp \left(-\frac{t}{\tau}\right) d\ln \tau.$$  

(4)

According to Schwarzl and Staverman \(^23\), the continuous relaxation spectrum can be calculated using the following second order accurate approximation method,

$$h(\tau) = -E(t) \left[ \frac{d}{d(t)} \left( \frac{d \log E}{d \log t} \right)^2 - \frac{1}{\ln(10)} \frac{d^2 \log E}{d (\log t)^2} \right]_{\tau = 2\tau}.\text{(5)}$$

To evaluate eq. (5) for $h(\tau)$, we expressed $\log E$ as a function of $\log t$ by fitting a 7th order polynomial to the master curve of the relaxation modulus plotted on a log-log scale. We next evaluated the continuous cumulative relaxation spectrum as,

$$H(\tau) = \int_{0}^{\ln \tau} h(z) d(\ln(z))$$  

(6)

The discreet cumulative relaxation spectrum was evaluated by combining eq. (3), (4) and (6) as,

$$H_{disc}(\tau) = E^{eq} + \sum_{i} E_{i}^{neq} \left( \tau - \tau_{i}^{ref} \right)$$  

(7)

where $\langle \tau - \tau_{i}^{ref} \rangle = 1$ for $\tau < \tau_{i}^{ref}$.

We next assumed a power law distribution of the relaxation times at the reference temperature as \(^2\),

$$\tau_{i}^{ref} = \tau_{max} \left( \frac{\tau_{max}}{\tau_{min}} \right)^{\frac{i-1}{N-1}},$$  

(8)

where $\tau_{max}$ and $\tau_{min}$ are the maximum and minimum relaxation time chosen based on the relaxation region and $N$ is the number of relaxation processes. The choice of $N$ is a trade off between accuracy and computational cost.

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**Fig. 1** Characterizing the stress relaxation behavior of Nafion: (a) master curve of the relaxation moduli, and (b) the discrete stress relaxation spectrum
Haupt et al. 24 presented a detailed discussion of the effect of $N$ on the error of the discrete approximation of the relaxation spectrum. The nonequilibrium moduli $E_{i}^{\text{neq}}$ were calculated such that $H_{\text{disc}}(\tau)$ in eq. (7) formed a staircase approximation for $H(\tau)$ in eq. (6)\textsuperscript{24}:

$$E_{1}^{\text{neq}} = \frac{1}{2}(H(\tau_{1}^{\text{ref}}) + H(\tau_{2}^{\text{ref}})) - E^{\text{eq}},$$

$$E_{i}^{\text{neq}} = \frac{1}{2}(H(\tau_{i}^{\text{ref}}) - H(\tau_{i-1}^{\text{ref}})), \quad 1 < i < N - 1,$$

$$E_{N}^{\text{neq}} = E^{\text{neq}} - \sum_{i=1}^{N-1} E_{i}^{\text{neq}}.$$  

As shown in Fig. 1a, the relaxation modulus continuously decreased with increasing time, though at a very slow rate and did not exhibit a clear rubbery plateau. We chose $E^{\text{eq}}$ to be the smallest measured stress relaxation modulus. The results for $(\tau_{i}^{\text{ref}}, E_{i}^{\text{neq}})$ were applied to eq. (3) to calculate the master curve for the discrete viscoelastic model. The results, plotted in Fig. 1(a), showed good agreement with experimental data. The shear moduli were calculated from the Young’s moduli as $G_{i}^{\text{eq}} = E_{i}^{\text{eq}}/2(1 + \nu_{i})$ and $G_{i}^{\text{neq}} = E_{i}^{\text{neq}}/2(1 + \nu_{i})$, where the rubbery Poisson’s ratio was $\nu_{i} = 0.5$ and glassy Poisson’s ratio was $\nu_{g} = 0.35$. The bulk modulus was calculated as, $k = E^{\text{eq}}/3(1 - 2\nu_{g})$. The results gave $G_{3}^{\text{eq}} = 0.087$ MPa and the bulk modulus $\kappa = 744.4$ MPa. Figure 1b plots the relaxation spectrum $(\tau_{i}^{\text{ref}}, G_{i}^{\text{eq}})$. The relaxation moduli $G_{i}^{\text{eq}}(\tau)$ decays very slowly, decreasing only 3 order of magnitude over $10^{24}$ s range of relaxation times.

The temperature-dependent shift factor shift factor was described by a third order polynomial function,

$$a(T) = 2.76 \times 10^{-6} T^{3} - 4.78 \times 10^{-4} T^{2} - 0.171 T + 28.2,$$

which provided a good fit to the experimental data as shown in Fig. 2. Finally, the temperature-dependent storage modulus, loss modulus, and tan$\delta$ can be evaluated for the linearized viscoelastic model as,

$$E'(\omega, T) = E^{eq} + \sum_{i=1}^{N} E_{i}^{\text{neq}} \omega^{2} (\tau_{i}^{\text{ref}} a(T))^{2},$$

$$E''(\omega, T) = \sum_{i=1}^{N} E_{i}^{\text{neq}} \omega \tau_{i}^{\text{ref}} a(T),$$

$$\tan \delta(\omega, T) = \frac{E''(\omega, T)}{E'(\omega, T)},$$

where $a(T)$ is the shift factor in eq. (10).

4 Results

The constitutive model was applied first to simulate the dynamic temperature sweep experiments described in Sec. 2.1.2 using the relaxation spectrum obtained from the stress relaxation tests in Fig. 1. The temperature dependent storage modulus and tan$\delta$ were calculated using (11) for $\omega = 2\pi$ and $T = 40^\circ\text{C} - 172^\circ\text{C}$. The results are compared to experimental measurements in Fig. 3. Good quantitatively agreement across the glass transition region. We observed from the tan$\delta$ that the glass transition region spanned $T = 50^\circ\text{C} - 140^\circ\text{C}$.

We applied the model to study the shape recovery of specimens deformed at different programming temperatures describe in Sec. 2.2.1. Fig 4.a shows the experimental and simulation results of the free recovery response of the specimens programmed at 155, 120 and 85$^\circ\text{C}$. The activation temperature for strain recovery increased with the programming temperature. The simulations showed good agreement with the experimental data especially for specimens programmed at 155$^\circ\text{C}$ and 120$^\circ\text{C}$. For specimens programmed at 85$^\circ\text{C}$, the simulation predicted a lower
Fig. 2  The temperature-dependent shift factor $a(T)$.

Fig. 3  Comparing experimental measurements and model predictions of dynamic temperature sweep measurements of: (a) the storage modulus, and (b) tan$\delta$
temperature recovery region. The discrepancy was likely caused by structural relaxation, which is a pronounced
effect at the onset of the glass transition and was not included in the model. To illustrate the physical mechanism
behind the effect of the programming temperature, the normalized distribution of nonequilibrium stresses at end of
the cooling period was plotted as a function of the characteristic relaxation time in Fig. 4b for each relaxation time
\( \tau_{ref} \) in the discrete relaxation spectrum. The distribution of nonequilibrium stresses was narrow compared to the
distribution of relaxation moduli in Fig. 1b because faster processes were able to relax to equilibrium for the pro-
gramming temperature and applied strain rate. The breadth of the distribution of nonequilibrium stresses decreased
with increasing programming temperature, and the peak of the distribution shifted towards smaller relaxation times
for lower programming temperatures. This allowed for faster shape recovery. These results were consistent with
the observation in Yu et al., where the authors used the concept of the reduced time to investigate the influence
of the programming temperature and recovery temperature on the shape memory performance.

Fig. 4 Influence of the deformation temperature on shape recovery. (a) Comparison of experimental and simulation results
for the unconstrained recovery behavior at different deformation programming temperature, (b) The distribution of
nonequilibrium stresses at the end of the programming process before unloading.

Fig. 5 shows the experimental and simulation results for the multi-staged shape recover experiments described
in Sec. 2.2.2. The simulations showed good agreement with the experimental results. At each recovery tempera-
ture, the specimens achieved a partial shape recovery, though the results showed that recovery continued to persist
at a significantly reduced rate. This demonstrated that multi-staged shape-recovery at discrete temperatures is a
manifestation of the very broad relaxation spectrum with relaxation times. The distribution of relaxation times for
Nafion was significantly larger than laboratory time scale, which allowed the material to obtain the quasi-stable
nonequilibrium shape at each recovery temperature.

Fig. 6 plots the recovery behavior of specimens programmed at two different temperatures (Sec. 2.2.3), show-
ing good agreement between experiments and simulations. The initial recovery of the specimens programmed
at 155°C and 85°C coincided with the recovery curve of the specimen programmed at 120°C and 85°C. The
two curves separated at 80°C, which corresponded to the activation temperature for shape recovery of specimens
programmed at 120°C in the single-step programming experiment (Fig. 4). In contrast, the recovery curves of
the specimens programmed at 155°C and 120°C and at 155°C and 85°C were initially different, but merged at
130°C. The 130°C coincided with the temperature at which specimens programmed at a single 120°C temperature
achieved fully recovery (Fig. 4).

The nonlinear viscoelastic model was implemented for finite element analysis (Tahoe®, Sandia National
Laboratories) and applied to describe the multiple shape memory effect of a membrane with a period array of
holes (Fig 7a). A series of pattern transformations was programmed in the membrane at different temperatures

† http://sourceforge.net/projects/tahoe/
Fig. 5 Comparing the experimental results and model predictions for the free shape recovery response at multiple temperature steps.

Fig. 6 Shape recovery of specimens programmed at two different temperatures, comparing experiments and model predictions.
by applying deformations to trigger a mechanical instability\textsuperscript{25–28}. The numerical examples combined the multiple shape memory effect and mechanical instability to achieve multiple temperature activated pattern transformation. The repeating unit cell shown in Fig. 7 was used to describe a membrane with a periodic array of circular holes. The unit cell was discretized using hexahedral elements and only one layer element was used in the thickness direction as shown in Fig 7.b.

In order to simulate the deformation through the mechanical instability and bias the buckled configuration, the shape of the bottom-left circle was perturbed into an ellipse with a major axis that was 0.14% larger than the minor axis. The displacements were fixed as follows: \(u_z(x, y, 0) = 0, u_x(0, 0, 0) = 0, u_y(0, 0, 0) = 0\). In addition, periodic boundary conditions were applied to the \(x\) surfaces (\(AA'B'B, DD'C'C\)) and \(y\) surfaces (\(AA'D'D, BB'C'C\)). The membrane was deformed in the \(z\) direction to -25\% engineering strain over 100 seconds at 160\(^\circ\)C. The boundary conditions were chosen to simulate the experiments of Li \textit{et al.}\textsuperscript{28}, which used hot-pressing to trigger the pattern transformation of an SMP periodic membrane. The applied programmed shape at different strain level is shown in Fig 8. The mechanical instability transformed the circular holes into alternating horizontal and vertical ellipses. The programmed membrane was cooled to 120\(^\circ\)C at 6\(^\circ\)C/min and stretched from -25\% to 25\% engineering strain in the \(z\) direction. The tension in the \(z\) direction opened the ellipses returning the shape to the original periodic array of circular holes. The third temporary programmed shape was achieved by cooling the membrane to 80\(^\circ\)C at 6\(^\circ\)C/min and then compressing again in \(z\) to -20\% strain at 80\(^\circ\)C. The final shape, an array of alternating horizontal and vertical ellipses, was fixed by cooling the membrane to 40\(^\circ\)C at 6\(^\circ\)C/min under fixed compression strain and unloaded.

The membrane was heated to 170\(^\circ\)C at 1\(^\circ\)C/min to achieve shape recovery under traction-free conditions in \(z\), the thickness direction. The recovered shape is shown in Fig 8 at different temperatures. As shown at \(T = 40\(^\circ\)C\), unloading in \(z\) had negligible effect on the programmed shape. No pronounced recovery occurred until 70\(^\circ\)C. The elliptical holes continuously opened with increasing temperature until 85\(^\circ\)C and then closed to reach the ellipses with larger aspect ratio with increasing temperature to 125\(^\circ\)C. The elliptical holes then opened again, transforming to the permanent circular shape. The membrane achieved fully recovery at 170\(^\circ\)C. As shown, the multiple pattern transformation can be achieved by combining mechanical instability and the multiple shape

\textbf{Fig. 7} (a) Schematic of Nafion membrane with a periodic array of circular holes, (b) finite element model of a representative unit cell of the Nafion membrane.
Fig. 8  The shape memory programming and recovery of the Nafion membrane with a periodic array of circular holes shown multiple switchable pattern transformation.
memory effect. Stretching the thin film in the thickness direction to program the second temporary shape may be difficult to achieve in experiments. Alternatively, pattern transformation can be achieved by deforming the film through uniaxial or biaxial compression in the plane\textsuperscript{26,27}. Stretching the film in the plane would open the collapsed holes to achieve the second temporary shape for this loading configuration.

5 Conclusions

In this paper, we applied a simple finite deformation nonlinear viscoelastic model to describe the complex shape memory behavior of Nafion and similar materials with a broad glass transition temperature region. We also developed a method to obtain the parameters of the relaxation spectrum from the master curve of the relaxation modulus. The model is capable of predicting the influence of the deformation temperature and recovery temperature on the free recovery response of Nafion films. We also demonstrated the application of the multiple shape memory effect to program a series of switchable pattern transformation in Nafion membranes using finite element simulations.

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