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## ARTICLE

# Twin-Driven Thermoelectric Figure-Of-Merit Enhancement Of $\text{Bi}_2\text{Te}_3$ Nanowires

Cite this: DOI: 10.1039/x0xx00000x

Ho Sun Shin<sup>a</sup>, Seong Gi Jeon<sup>b</sup>, Jin Yu<sup>b</sup>, Yong-Sung Kim<sup>a,c</sup>, Hyun Min Park<sup>a,c</sup> and Jae Yong Song<sup>a,c,\*</sup>

Received 00th January 2012,  
Accepted 00th January 2012

DOI: 10.1039/x0xx00000x

www.rsc.org/

Thermoelectric figure-of-merits ( $ZT$ ) are enhanced or degraded by crystal defects such as twins and excess atoms that are correlated with thermal conductivity ( $k$ ) and carrier concentration ( $n$ ). For  $\text{Bi}_2\text{Te}_3$ , it is unclear whether the crystal defects can enhance  $ZT$  without a degradation in thermopower factor. In the present study, n-type  $\text{Bi}_2\text{Te}_3$  nanowires (NWs) are electrochemically synthesized to have twin-free (TF) or twin-containing (TC) microstructures with  $ZT$  of 0.10 and 0.08, respectively, at 300 K. The  $ZT$ s of TF and TC NWs remarkably increase up to 0.21 and 0.31, when heat-treatments cause the  $n$ -reduction and twins induce the phonon scattering, as follows; first, the enhancement of Seebeck coefficient from -70 to -98  $\mu\text{V}\cdot\text{K}^{-1}$  for TF NW and -57 to -143  $\mu\text{V}\cdot\text{K}^{-1}$  for TC NW, by virtue of  $n$ -reduction; secondly, twin-driven  $k$ -reduction from 1.9 to 1.4  $\text{W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$  of TC NW, while the  $k$  of TF NW increases from 2.3 to 2.6  $\text{W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$  due to the enhanced carrier mobility. The lattice thermal conductivities of TC NW are lowered from 1.1 to 0.8  $\text{W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$  by phonon scattering at twins. And density functional theory calculations indicate that twins do not significantly influence the Seebeck coefficient of  $\text{Bi}_2\text{Te}_3$ . It is strongly recommended that twins be incorporated with an optimum carrier concentration to enhance the  $ZT$  of  $\text{Bi}_2\text{Te}_3$ .

## 1 Introduction

Thermoelectric (TE) materials have attracted great attention as promising candidates for clean and sustainable energy conversion. Among the TE materials,  $\text{Bi}_2\text{Te}_3$  is the most efficient material near room temperature, because it has a high figure-of-merit,  $ZT = (S^2\sigma)/(kT)$ , of about 1 at room temperature, where  $S$  is the Seebeck coefficient,  $\sigma$  is electrical conductivity,  $k$  is thermal conductivity, and  $T$  is absolute temperature. Since it was theoretically predicted that  $ZT$  can be drastically enhanced by the size effect and quantum-confinement effect in nanostructures,<sup>1</sup> a plethora of studies have been made to fabricate  $\text{Bi}_2\text{Te}_3$  nanostructures, such as nanowires (NWs),<sup>2-7</sup> superlattice films,<sup>8</sup> coaxial-superlattice NWs,<sup>9,10</sup> and nanotubes.<sup>11,12</sup> However, the Seebeck coefficients (-9 to -70  $\mu\text{V}\cdot\text{K}^{-1}$ )<sup>13-15</sup> of  $\text{Bi}_2\text{Te}_3$  NWs reported elsewhere were much smaller than those (-215 to -255  $\mu\text{V}\cdot\text{K}^{-1}$ ) of  $\text{Bi}_2\text{Te}_3$  in the film and bulk forms near room temperature.<sup>16-19</sup> Even if the reasons have not been clearly understood, one possibility is the carrier concentration, which strongly influences the  $ZT$  of bulk  $\text{Bi}_2\text{Te}_3$ , according to the Pisarenko relation, i.e., thermopower decreases with an increase in carrier concentration.<sup>20</sup> The effects of carrier concentration on the Seebeck coefficient in nanowires have not been intensively investigated for  $\text{Bi}_2\text{Te}_3$  NWs, although limited studies were recently reported for  $\text{Bi}_x\text{Te}_y$ , InAs, InSb NWs.<sup>14,21</sup>

Although the Wiedemann-Franz law, i.e., that electrical conductivity and thermal conductivity cannot be decoupled, limits  $ZT$  values, nanostructuring opens up the possibility that transport of phonons and electrons can be separately controlled by generating phonon scattering without significant degradation of electron

mobility.<sup>22,23</sup> For example, internal defects such as superlattices, nanograins, and nanoprecipitates can increase  $ZT$  effectively through phonon scattering at the internal boundaries.<sup>8,24,25</sup> Recently, (001) basal twins were observed and analyzed in bulk  $\text{Bi}_2\text{Te}_3$  by high-angle annular dark field (HAADF) scanning transmission electron microscopy (STEM) and a theoretical calculation.<sup>26</sup> The twin boundary, i.e. a well-ordered interface like a superlattice, is particularly interesting in view of the phonon-glass-electron-crystal, because electrical transport would be little affected by such interfaces where the phonon scattering occurs.<sup>27</sup> To the authors' knowledge, the effects of twins on the thermopower and lattice thermal conductivity of  $\text{Bi}_2\text{Te}_3$  have not yet been investigated.

Hence, we synthesized twin-free and twin-containing  $\text{Bi}_2\text{Te}_3$  NWs via a potentiostatic electrochemical method. The electrodeposition method, which has often been used to synthesize TE materials in the forms of thin films or NWs, can generate twins in metal deposits of Cu, Ag, Ni-Mn and Ag-Cu.<sup>28-31</sup> The effects of twins and carrier concentration on the TE properties of  $\text{Bi}_2\text{Te}_3$  were experimentally and theoretically investigated using microfabricated TE measurement platform (MTMP) and density-functional theory (DFT) calculation.

## 2 Experimental Section

### 2.1 Synthesis of $\text{Bi}_2\text{Te}_3$ nanowires

Anodic aluminum oxide membrane (AAM) was prepared through a two-step anodization process at 274 K using aluminum

foils (99.99%, Alfa aesar).<sup>32</sup> After the anodization process, Au electrode layer (150 nm thick) was deposited on the AAM by RF sputtering deposition. The remaining aluminum was etched out in a mixed solution of 1 M CuCl<sub>2</sub> and 0.1 M HCl. The barrier layer of aluminum oxide was dissolved in 0.5 M phosphoric acid (323 K) for the electrodeposition process. The final pore size of AAM was approximately 55 nm in diameter. Electrochemical deposition was potentiostatically conducted at 298 K using a three-electrode setup composed of the Au-coated AAM as a working electrode, a saturated Ag/AgCl as a reference electrode, and a Pt wire as a counter electrode. The potential unit (V) versus a saturated Ag/AgCl electrode was used in this study. Cyclic voltammetry was performed to determine the reduction potential using a potentiostat/galvanostat (Solatron 1280c) at a scan rate of 20 mV·s<sup>-1</sup>. The aqueous electrolyte was composed of 0.004 M Bi<sup>3+</sup> [Bi(NO<sub>3</sub>)<sub>3</sub>, Sigma-Aldrich, ACS grade], 0.004 M HTeO<sub>4</sub><sup>2+</sup> (TeO<sub>2</sub>, Acros Organics), and 0.35 M HNO<sub>3</sub> (Junsei Chemical, GR grade). The pH of the electrolyte was 0.5. The reduction potentials ( $V_R$ ) of +0.017 V and +0.120 V were used for the TF and the TC Bi<sub>2</sub>Te<sub>3</sub> NWs, respectively. The nominal growth rate was estimated as 6.5 μm·h<sup>-1</sup> at  $V_R$  of +0.017 V and 0.8 μm·h<sup>-1</sup> at  $V_R$  of +0.120 V. The Bi<sub>2</sub>Te<sub>3</sub> NWs within the AAM were heat-treated at 673 K for 2 hours in a vacuum ( $2 \times 10^{-6}$  Torr).

### 2.2 Microstructural analyses

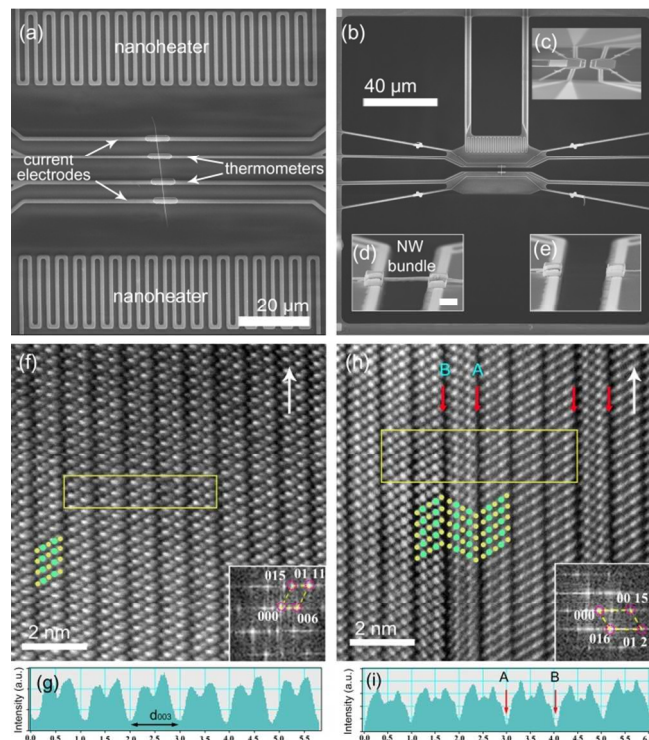
The morphology and length of the electrodeposited Bi<sub>2</sub>Te<sub>3</sub> NWs in the AAM were investigated using a scanning electron microscopy (SEM, Hitachi, S4800). An atomic-scale microstructure analysis was conducted using aberration-corrected scanning transmission electron microscopy (CS-STEM, JEOL ARM200). For the sake of TEM analysis, the NWs-containing AAM was immersed in a 2 M NaOH aqueous solution to remove the AAM. Then, the NaOH solution was copiously rinsed out in deionized water and then ethanol. Finally, the NWs dispersed in ethanol were obtained after sonication for a few seconds. The NWs-containing ethanol was dropped onto a TEM grid and completely dried.

### 2.3 Measurement of TE properties

To characterize the thermopower factor of the Bi<sub>2</sub>Te<sub>3</sub> NWs, we fabricated a membrane-type microfabricated TE measurement platform (MTMP) comprising a symmetric pair of Pt nanoheaters, current carrying electrodes, and four-point thermometers on a suspended low-stress silicon nitride of 500 nm thickness (Figure 1(a)). Ni/Al (10 nm/100 nm) layer was used as the electric and thermal contacts between Bi<sub>2</sub>Te<sub>3</sub> NW and Pt electrode. The Pt thermometers had the electrical resistance of the two orders of magnitude smaller than the NWs. A temperature gradient was generated by resistive heating one of the Pt nanoheaters. The Seebeck voltage and electrical conductivity were measured under a vacuum (approximately  $2 \times 10^{-6}$  Torr) in the temperature range of 40 to 300 K. For the sake of measuring the thermal conductivity of NWs, we used a different micro-platform, *i.e.* suspended bridge-type MTMP (Figure 1(b)). As the heat generated from the nanoheater might be dissipated through the thin Si nitride (500 nm thick) bridges of the bridge-type MTMP, the measurements were conducted under the high vacuum. This enabled us to use one-dimensional heat conduction model ignoring thermal convection and thermal radiation.

### 2.4 Theoretical calculation

The TE properties of TF and TC Bi<sub>2</sub>Te<sub>3</sub> were investigated by DFT calculations. Vienna Ab Initio Simulation Package (VASP) code was used.<sup>33,34</sup> We used the projector augmented wave (PAW) pseudopotentials.<sup>35</sup> The kinetic energy cutoff for the plane-wave



**Figure 1.** SEM images of (a) the membrane-type MTMP with a NW, (b) the bridge-type MTMP with NW bundle, (c) perspective view of the bridge-type MTMP, (d) suspended NW bundle bridging between hot and cold junctions, and (e) NW bundle after AFM cutting. HAADF-STEM results of (f) TF and (h) TC NWs. The atomic arrangement of Bi (bright) and Te (dark) atoms is distinguished by Z-contrast. (g) and (i) the atomic contrast profiles obtained from the yellow marked area of (f) and (h), respectively. The white arrows in (f) and (h) indicate the [110]-longitudinal growth direction of Bi<sub>2</sub>Te<sub>3</sub> NWs. Twin boundaries are indicated by red arrows shown in (h). The insets in (f) and (h) indicate the FFT results of the corresponding HAADF-STEM images.

basis set expansion was 250 eV, and the generalized-gradient approximation (GGA) for the exchange correlation energy was used.<sup>36</sup> The spin-orbit coupling was included in the DFT Hamiltonian. The theoretical lattice constants of  $a=0.4478$  nm and  $c=3.091$  nm were used for the hexagonal three quintuple-layers unit cell (rhombohedral ( $R\bar{3}m$ ) space group) of Bi<sub>2</sub>Te<sub>3</sub> without twins. The  $4 \times 4 \times 2$  k-point mesh in the Brillouin zone for the three quintuple-layers unit cell was used for the geometry optimization and the total energy calculations. The Seebeck coefficients were calculated using the DFT band structures combined with the semiclassical theory of conduction under the energy-independent relaxation time approximation.<sup>37</sup> The  $24 \times 24 \times 2$  k-point mesh was used for the Seebeck coefficient calculation. With the theoretical lattice constants, the calculated electronic band structure has been known to agree well with the experiments.<sup>38</sup> The thickness of a quintuple layer (the distance between two nearby Van der Waals layers) is calculated to be 1.030 nm, whereas the experimentally obtained value is 1.036 nm, measured from HAADF image (Figure 1).

## 3 Results and discussion

The Seebeck coefficients ( $S$ ) and the electrical conductivities ( $\sigma$ ) of the Bi<sub>2</sub>Te<sub>3</sub> NWs were measured using a membrane-type MTMP in the range of 40 to 300 K. Figure 1(a) shows a SEM image of the

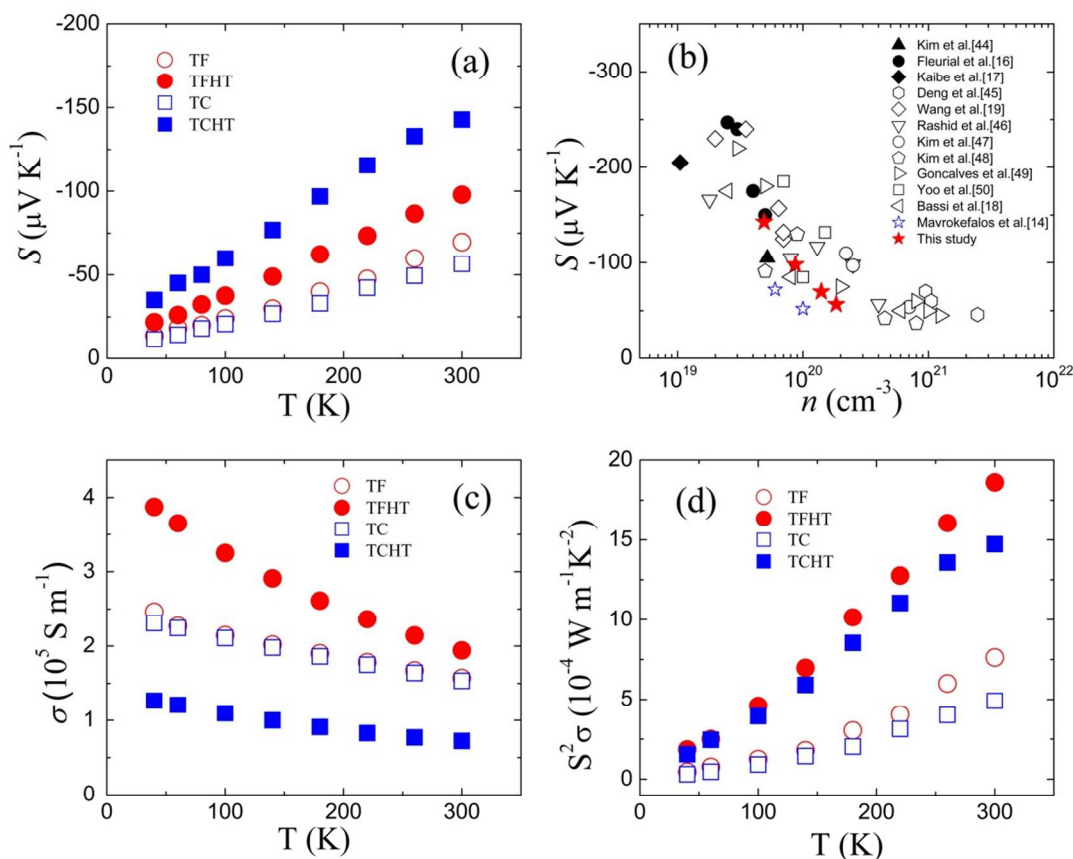
membrane-type MTMP where a single  $\text{Bi}_2\text{Te}_3$  NW was located on the four Pt electrodes in the center of the MTMP. In order to measure the thermal conductivity ( $k$ ), we used a bridge-type MTMP, shown in Figs. 1(b) and 1(c), which was similar to the previously reported method for measuring the thermal conductivity of Si NWs.<sup>39</sup> We used a  $\text{Bi}_2\text{Te}_3$  NW bundle to measure the thermal conductivity because a single  $\text{Bi}_2\text{Te}_3$  NW has too low thermal conductance to ensure measurement accuracy in our measurement system. Therefore, the thermal conductance of a single NW was averaged from that of the NW bundle. The thermal conductances of the NW bundle were determined by comparing the results obtained before and after cutting the  $\text{Bi}_2\text{Te}_3$  bundle, respectively, as shown in Figs. 1(d) and 1(e). The detailed procedure of measuring  $S$ ,  $\sigma$  and  $k$  is described in the method section (also see Supporting Information).

$\text{Bi}_2\text{Te}_3$  NWs with about 15  $\mu\text{m}$  in length were electrochemically deposited into the anodic aluminum oxide membranes (AAMs) in potentiostatic mode by referring to the cyclic voltammogram (Figure S1). Two types of  $\text{Bi}_2\text{Te}_3$  NWs were synthesized, to have twin-free (TF) and twin-containing (TC) microstructures at the reduction potential ( $V_R$ ) of +0.017 and +0.120 V, respectively. The TF and TC NWs had diameters of  $67 \pm 5$  nm and  $75 \pm 10$  nm, respectively. Typical cross-sectional SEM images of the TF NWs and TC NWs showed that the NWs had smooth and void-free surfaces (Figures S2(a) and S2(c)). The bright-field TEM images of TF and TC NWs and the corresponding selected area electron

diffraction (SAED) pattern for the whole nanowire showed that both  $\text{Bi}_2\text{Te}_3$  NWs grew along the  $[110]$ -longitudinal direction (Figures S2(b) and S(d)). The TF NWs seemed to have almost single-crystalline structure, while the split diffraction pattern indicates that the TC NW was composed of several grains. The XRD results supported the stronger  $[110]$ -texturing along the longitudinal direction for TF NWs than TC NWs (Figure S3).

The HAADF-STEM images shown in Figures 1(f) and 1(h) indicate the quintuple atomic arrangements of the TF and TC NWs and the inset shows the corresponding fast Fourier transform (FFT) images. Figures 1(g) and 1(i) reflect the contrast profile for the marked area (yellow square) where the bright atoms (indicated by green color) represent the atomic columns of Bi atoms, while the dark ones (indicated by yellow color) correspond to the atomic columns of Te atoms. TF NW consisted of five repeating quintuple layers in the order of  $[-\text{Te}^{(1)}-\text{Bi}-\text{Te}^{(2)}-\text{Bi}-\text{Te}^{(1)}-]$  along the  $c$ -axis in a hexagonal structure (Rhombohedral ( $R\bar{3}m$ ) space group). As the quintuple layers are weakly bonded to each other by Van der Waals force, it is shown that the repeating quintuple layers are widely separated by Van der Waals bonds (seen as dark stripes vertically appearing in the Figures 1(f) and 1(h)) between the  $\text{Te}^{(1)}$  atomic layers. The distance between dark stripes was 1.036 nm, which agrees well with the (003) plane spacing of  $\text{Bi}_2\text{Te}_3$ .<sup>40</sup>

The HAADF-STEM image and corresponding FFT image of the TC NW clearly show that (001) basal twins (indicated by the red arrows) existed parallel to the longitudinal direction, as shown in



**Figure 2.** Variations of (a) Seebeck coefficients of  $\text{Bi}_2\text{Te}_3$  NWs with temperature and (b) the Seebeck coefficients with carrier concentration for n-type  $\text{Bi}_2\text{Te}_3$  including the literature data (solid symbols: bulk, open symbols: thin film, asterisk symbols: nanowire). Variations of (c) electrical conductivities and (d) thermopower factors of  $\text{Bi}_2\text{Te}_3$  NWs with temperature. Here, TF, TFHT, TC, and TCHT denote twin-free, heat-treated twin-free, twin-containing, and heat-treated twin-containing NWs, respectively.



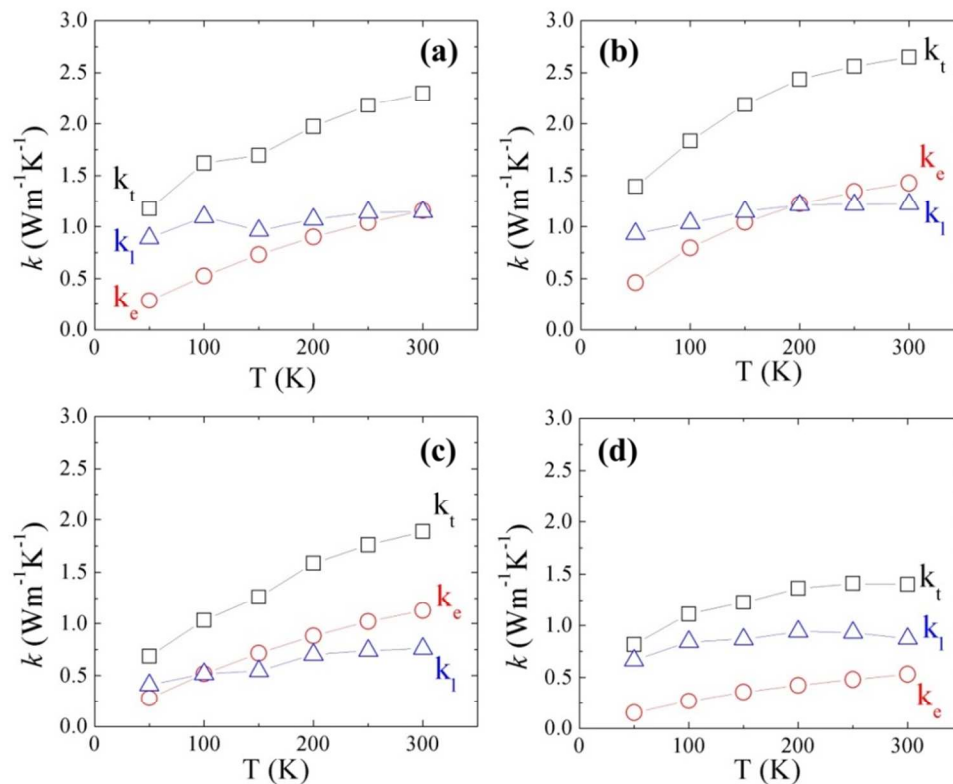
Figure 1(h). It was previously reported that the (001) basal twin terminated at the Te<sup>(1)</sup> layer in Bi<sub>2</sub>Te<sub>3</sub> has the lowest interfacial energy among the possible twin structures.<sup>26</sup> Although the formation mechanism of twins in the NWs is not yet completely understood at the moment, the twin formation might be related to the electrodeposition parameters (e.g. reduction potential), as discussed in the references.<sup>41,42</sup> From the HAADF-STEM observation of six TC NWs, the number of twins was counted and the twin density was estimated to be approximately 1.2±0.9 twins per ten quintuples. And several stacking faults were locally found in both the TF and TC NWs.

Subsequently, the TF and TC NWs within the AAM were heat-treated at 673 K for 2 hours in a vacuum ( $2 \times 10^{-6}$  Torr) and, hereafter, are termed TFHT and TCHT NWs, respectively. The microstructures of TFHT and TCHT NWs were not significantly changed after the heat-treatments. The single crystallinity of TFHT was maintained and the TCHT had similar twin-containing structure after the heat-treatment, as shown in the HAADF-STEM image and XRD data (Figures S4 and S5). This indicates that the present Bi<sub>2</sub>Te<sub>3</sub> NWs had stable crystalline structure, which was different from the disproportionation (Bi<sub>2</sub>Te<sub>3</sub> to Bi<sub>4</sub>Te<sub>3</sub> via Bi<sub>4</sub>Te<sub>5</sub>) occurring due to Te sublimation in unstable Bi<sub>2</sub>Te<sub>3</sub> crystalline structure.<sup>4</sup>

Figure 2(a) shows the variations of Seebeck coefficient over the temperature range of 40 to 300 K for TF, TC, TFHT, and TCHT NWs. The negative sign of the Seebeck coefficients indicates that all the NWs have *n*-type carriers. It is noted that the Seebeck coefficients linearly decreased with decreasing temperature, which was due to the contribution of diffusive thermopower rather than phonon drag effect.<sup>43</sup> At 300 K, the *S* ( $-70 \mu\text{V}\cdot\text{K}^{-1}$ ) of TF NW, is comparable to the previous result ( $-70 \mu\text{V}\cdot\text{K}^{-1}$  at 300 K) for the electrodeposited Bi<sub>2</sub>Te<sub>3</sub> NWs,<sup>14</sup> but lower than that of Bi<sub>2</sub>Te<sub>3</sub> thin films ( $-240 \mu\text{V}\cdot\text{K}^{-1}$ )<sup>19</sup> or bulk values ( $-250 \mu\text{V}\cdot\text{K}^{-1}$ ).<sup>16</sup> And, it should be noted that the *S* ( $-57 \mu\text{V}\cdot\text{K}^{-1}$ ) of TC NW was slightly smaller

than that of TF NW. Therefore, we carried out a density functional theory (DFT) calculation in order to investigate the effects of twins on the thermopower of the Bi<sub>2</sub>Te<sub>3</sub> phase. The twin density in our calculations was one twin per three quintuple layers. We found that lattice expansion of +0.55% occurred along the *c* axis with the twin insertion (Figure S6) and that the Te-Bi inter-layer spacing was barely changed, while the Te(1)-Te(1) Van der Waals inter-layer spacing was enlarged from 2.749 Å (TF Bi<sub>2</sub>Te<sub>3</sub>) to 2.896 Å (TC Bi<sub>2</sub>Te<sub>3</sub>) by +5.3%, which is in good agreement with the recent TEM measurement (+4.4%).<sup>26</sup> The calculated twin formation energy (the interface energy) was 22.7 mJ·m<sup>-2</sup> per twin boundary, which was lower than the previous calculation (40.7 mJ·m<sup>-2</sup>).<sup>26</sup> According to the calculations of electronic density-of-states (DOS) and Seebeck coefficient (*S*) (at 300 K) of the TF and TC Bi<sub>2</sub>Te<sub>3</sub> as a function of the Fermi level, the calculated *S* was +164 μV·K<sup>-1</sup> (maximum value) in *p*-type and -156 μV·K<sup>-1</sup> (maximum value) in *n*-type (see Figure S7), of which the absolute values were lower than those of the experimental values of +230 and -250 μV·K<sup>-1</sup> (Figure S7).<sup>16,18</sup> For TC Bi<sub>2</sub>Te<sub>3</sub>, the calculated *S*'s were found to be lower, i.e., +129 μV·K<sup>-1</sup> in *p*-type and -142 μV·K<sup>-1</sup> in *n*-type. Approximately, 21% (*p*-type) and 9% (*n*-type) reductions of the *S*'s were found. The smaller gradients of the DOS at both the valence and conduction band edges for the TC Bi<sub>2</sub>Te<sub>3</sub> might be ascribed to the smaller Seebeck coefficients. As a result, the calculation result (9% *S*-reductions of *n*-type) supports the measurement result of 19% *S*-reduction for TC NW.

However, according to the Pisarenko relation of *S* and carrier concentration (*n*) for highly-doped semiconductors,<sup>20</sup> the Seebeck coefficient is strongly affected by carrier concentration which is correlated to DOS. We estimated the carrier concentration of Bi<sub>2</sub>Te<sub>3</sub> NWs using the linear relationship of *S* and *T* following the Mott formula,



**Figure 3.** Variations of thermal conductivities of (a) TF, (b) TFHT, (c) TC, and (d) TCHT NWs with temperature. Open squares indicate the total thermal conductivity ( $k_t$ ), open circles the electronic thermal conductivity ( $k_e$ ), open triangles the lattice thermal conductivity ( $k_l$ )

$$\frac{S}{T} = -\frac{\pi^2 k_B^2 m^*}{(3\pi^2)^{2/3} \hbar^2 |e|} \frac{1}{(n^{2/3})}$$

Under assumptions of a simple parabolic electronic band structure and a constant effective mass ( $m^*$ ), the carrier concentrations were calculated as  $1.4 \times 10^{20}$  and  $8.7 \times 10^{19} \text{ cm}^{-3}$  for TF and TFHT NWs while those of TC and TCHT NWs were estimated as  $1.8 \times 10^{20}$  and  $4.9 \times 10^{19} \text{ cm}^{-3}$ , respectively. Here,  $m^* = 0.58m_0$  was used, where  $m_0$  is electron rest mass.<sup>20</sup> Despite the similar carrier concentrations for TF and TC NWs, the TC NW had a lower  $S$  than the TF NW. This supports the premise that the lower  $S$  can be mainly attributed to the twin effect, as described by the above DFT calculation.

The carrier concentrations ( $n$ ) of TF, TC, TFHT, and TCHT NWs were plotted with the previously reported results for  $\text{Bi}_2\text{Te}_3$  film and bulk, as shown in Figure 2(b). It is noted that the  $S$  at room temperature decreased with the increasing  $n$  in the range of  $10^{19}$  to  $10^{21} \text{ cm}^{-3}$ , indicating strong correlation between  $S$  and  $n$ .<sup>14,16-19,44-50</sup> The measured  $S$  for  $\text{Bi}_2\text{Te}_3$  NWs agreed well with the  $S$  vs.  $n$  variations reported in the literature implying that the  $S$  of NWs might also be enhanced by optimization of  $n$ .

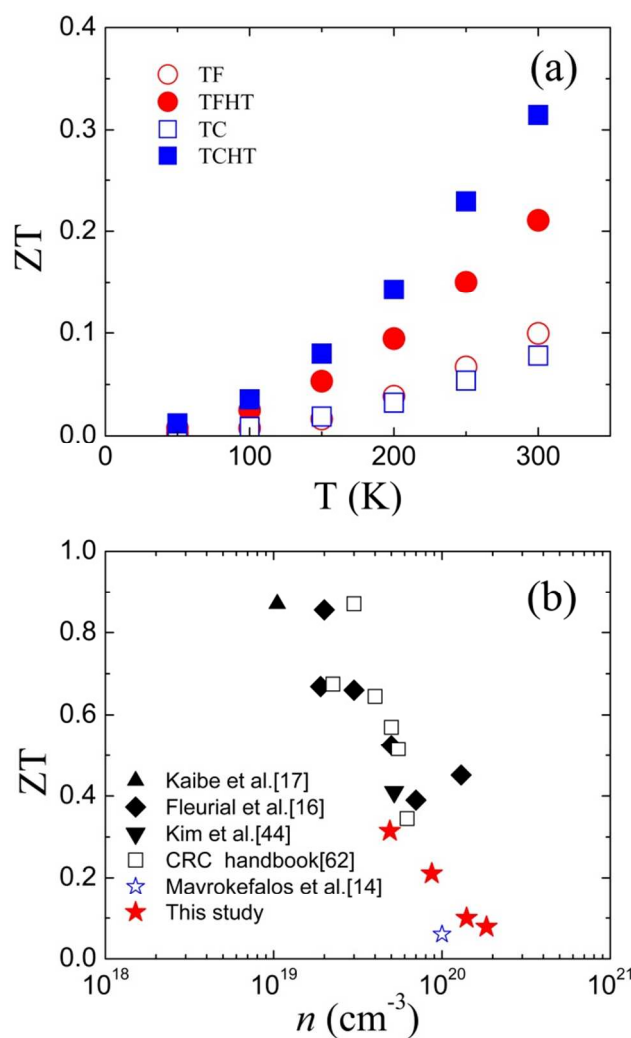
Figure 2(c) shows the variations of the electrical conductivities ( $\sigma$ ) with temperature, and illustrates that all the NWs had increasing  $\sigma$  with decreasing temperature. This is presumed to be due to the increasing electron-phonon scattering with temperature. TF and TC NWs showed very similar  $\sigma$  variation ( $1.5 \times 10^5 \text{ S}\cdot\text{m}^{-1}$  at 300 K). It is known that excess Te atoms occupying Bi sites play the role of  $n$ -type dopant and reduce the thermopower and mobility of  $\text{Bi}_2\text{Te}_3$ .<sup>51</sup>

Using the carrier concentrations ( $1.4 \times 10^{20}$  and  $1.8 \times 10^{20} \text{ cm}^{-3}$ ), the carrier mobilities ( $\mu$ ) were calculated from the relation of  $\sigma = nq\mu$ , where  $q$  is electron charge. The  $\mu$  ( $52 \text{ cm}^2\cdot\text{V}^{-1}\cdot\text{s}^{-1}$ ) of TC NW was slightly lower than that ( $70 \text{ cm}^2\cdot\text{V}^{-1}\cdot\text{s}^{-1}$ ) of TF NW (see Figure S8). The mobilities increased with decreasing temperature due to the diminishing scattering of carriers. The higher  $\sigma$  ( $1.94 \times 10^5 \text{ S}\cdot\text{m}^{-1}$  at 300 K) of TFHT was due to the highly increased mobility, from 70 to  $140 \text{ cm}^2\cdot\text{V}^{-1}\cdot\text{s}^{-1}$ , despite the lowered carrier concentration, from  $1.4 \times 10^{20}$  to  $8.7 \times 10^{19} \text{ cm}^{-3}$  after the heat-treatment, indicating that the lattice defects (e.g. anti-site defect) decreased and the crystallinity was enhanced by the heat-treatment. And the lower  $\sigma$  ( $0.59 \times 10^5 \text{ S}\cdot\text{m}^{-1}$  at 300 K) of TCHT was ascribed to the decreased carrier concentration despite the small increase of mobility from 52 to  $92 \text{ cm}^2\cdot\text{V}^{-1}\cdot\text{s}^{-1}$  (at 300 K) after the heat-treatment. The lower mobility of TCHT might be related to the carrier scattering at twin boundaries.

All gradients of  $\mu$  vs.  $T$  increased in the sequence of TC, TF, TCHT, and TFHT, indicating that phonon scattering played an important role in decreasing  $\mu$  with temperature for TFHT NW.

Figure 2(d) shows the variations of thermopower factor ( $S^2\sigma$ ) with temperature, and that the  $S^2\sigma$  increased after the heat-treatment;  $7.6 \times 10^{-4}$  to  $18.6 \times 10^{-4} \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-2}$  for TFHT and  $4.9 \times 10^{-4}$  to  $14.7 \times 10^{-4} \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-2}$  for TCHT. The improvement was due to the enhancement of Seebeck coefficient caused by the lowered carrier concentration of the heat-treated NWs.

We measured the thermal conductivity of the  $\text{Bi}_2\text{Te}_3$  NWs by using the bridge-type MTMP shown in Figure 1(b). Practically, the thermal conductivity of  $\text{Bi}_2\text{Te}_3$  NWs cannot be directly measured with a steady state method.<sup>14,39</sup> Rather, we measured the thermal conductance of NWs and converted it into thermal conductivity using the geometrical parameter (length and diameter) of the NWs provided by SEM observation. Considering the measurement reliability, we used a  $\text{Bi}_2\text{Te}_3$  NW bundle composed of 5 to 6 NWs to enhance the sensitivity of measurement. To understand the effect of twinning on the lattice thermal conductivity ( $k_l$ ) of NWs, we



**Figure 4.** Variations of (a) ZTs of  $\text{Bi}_2\text{Te}_3$  NWs with temperature and (b) the ZTs with the carrier concentration ( $n$ ) of  $n$ -type  $\text{Bi}_2\text{Te}_3$  including the literature data. (solid symbols: bulk, open symbols: thin film, asterisk symbols: nanowire). Here, TF, TFHT, TC, and TCHT denote twin-free, heat-treated twin-free, twin-containing, and heat-treated twin-containing, respectively.

extracted the electronic contribution ( $k_e$ ) from the total thermal conductivity ( $k$ ). The  $k_e$  was calculated by Wiedemann-Frantz law with the non-degenerated Lorentz number of  $2.45 \times 10^{-8} \text{ W}\cdot\Omega\cdot\text{K}^{-2}$  and electrical conductivity.<sup>52</sup> Here, the bipolar contribution to thermal conductivity was not considered because of the large contribution of electrons to thermal conductivity in highly  $n$ -doped  $\text{Bi}_2\text{Te}_3$  NWs ( $>10^{19} \text{ cm}^{-3}$ ).<sup>53</sup>

Figure 3 shows the  $k$ -variations of the  $\text{Bi}_2\text{Te}_3$  NWs with temperature. At 300 K, the  $k$  of TF NW was measured to be  $2.3 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ , and of the TC NW to be  $1.9 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ . After the heat treatment at 673 K, TFHT showed the slightly increased  $k$  of  $2.6 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ , while TCHT exhibited the lowered  $k$  of  $1.4 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$  at 300 K. The  $k$  values of all NWs decreased with decreasing temperature; this was in contrast to the phenomena for the bulk sample, which shows increasing  $k$  with decreasing temperature. This implies that phonon-phonon umklapp scattering diminished while phonon-boundary and phonon-impurity scattering dominated in  $\text{Bi}_2\text{Te}_3$  NWs.<sup>54,55</sup> In addition, although the electrodeposited  $\text{Bi}_2\text{Te}_3$  NWs had a smooth surface apparently, they had an atomically rough surface, after heat treatment (Figure S4). The

rough surface serves as a strong phonon scattering site,<sup>56</sup> and even a phonon backscattering site.<sup>57</sup>

Generally, thermal conductivity is influenced by the microstructure and the carrier concentration. Mavrokefalos et al. reported that electrodeposited Bi<sub>2</sub>Te<sub>3</sub> NWs had thermal conductivities ( $k$ ) of 1 to 3 W·m<sup>-1</sup>·K<sup>-1</sup> depending upon the microstructure and the carrier concentration.<sup>10</sup> In their study, the calculated  $k_e$  values were 0.35 and 1.51 W·m<sup>-1</sup>·K<sup>-1</sup> for Bi<sub>2</sub>Te<sub>3</sub> NWs with the carrier concentration of 6 × 10<sup>19</sup> cm<sup>-3</sup> and 1 × 10<sup>20</sup> cm<sup>-3</sup>, respectively. Chen et al. also reported the low  $k$  (0.75 W·m<sup>-1</sup>·K<sup>-1</sup>) of electrodeposited Bi<sub>2</sub>Te<sub>3</sub> NWs with a [100]-preferred orientation in an amorphous alumina matrix,<sup>13</sup> but they did not investigate the effects of  $n$  on thermoelectric transport. Higher  $n$  leads to higher electrical conductivity, whereby the thermal conductivity will be increased by the increasing electronic component  $k_e$ . The calculated  $k_e$  (1.4 W·m<sup>-1</sup>·K<sup>-1</sup>) for TFHT increased in comparison with that (1.1 W·m<sup>-1</sup>·K<sup>-1</sup>) of TF despite the decreased  $n$ , while the  $k_e$  for TCHT decreased due to the decreased  $n$ . The increased  $k_e$  for TFHT was attributed to the increased  $\mu$  (Figure S8). On the other hand, the decreased  $k_e$  for TCHT was due to a larger decrease of the  $n$ .

Regarding the  $k_L$ , we found that the  $k_L$ 's for TC (0.8 W·m<sup>-1</sup>·K<sup>-1</sup>) and TCHT (0.9 W·m<sup>-1</sup>·K<sup>-1</sup>) were lower than those of TF (1.1 W·m<sup>-1</sup>·K<sup>-1</sup>) and TFHT (1.2 W·m<sup>-1</sup>·K<sup>-1</sup>). The  $k_L$ 's were comparable to the other report in the literature that  $k_L$  varied depending upon the microstructure of NWs, i.e.,  $k_L$  of 0.35 and 1.5 W·m<sup>-1</sup>·K<sup>-1</sup> for single crystalline and polycrystalline Bi<sub>2</sub>Te<sub>3</sub> NWs at 400 K, respectively.<sup>10</sup> And it was reported that the nanostructuring of Bi<sub>2</sub>Te<sub>3</sub> nanowires (56 nm in diameter) with twins leads to a reduction in the speed of sound, predicting a 13%-reduction in the lattice thermal conductivity.<sup>58</sup> The 25%-lower  $k_L$  for TC and TCHT Bi<sub>2</sub>Te<sub>3</sub> NWs might be related to the higher twin density, considering the similar NW diameters of 67 and 75 nm.

Introducing twins into TE materials has been considered to enhance the ZT by decreasing thermal conductivity by phonon scattering at twin boundaries. It was reported that thermal conductivity was depressed by twin boundaries in an indium-thallium alloying bulk.<sup>59</sup> Considering the higher twin density of TC and TCHT NWs,  $k_L$  reduction for TC by additional phonon scattering at twin boundaries can be expected. If the phonon scattering added by twins is independent of other sources, we can combine the phonon scattering rate of twins ( $\tau_{\text{twin}}^{-1}$ ) into the total phonon scattering rate ( $\tau_{\text{total}}^{-1}$ ) following Mathiessen's rule, as follows:  $\tau_{\text{total}}^{-1} = \Sigma\tau_{\text{other}}^{-1} + \tau_{\text{twin}}^{-1}$ , where  $\tau_{\text{other}}^{-1}$  indicates other scattering process such as phonon-phonon scattering, phonon-point defect scattering, and phonon-boundary scattering. Assuming that the twins can effectively confine the phonon propagation within neighboring quintuple layers, the scattering rate at twins would significantly increase because the effective length scale of scattering is dominated by the interspacing between neighboring twins rather than the NW's diameter. Actually, for the twin density of one twin per ten quintuples, the interspacing between twins was approximately 10 nm. Previously, it was reported that a small confinement dimension below 10 nm would lead to a large suppression in the lattice thermal conductivity.<sup>56,60,61</sup> Thus, it is reasonably supposed that the lower  $k_L$  for TC can be mainly ascribed to the scattering at twins as well as the surface scattering.

The ZTs for the Bi<sub>2</sub>Te<sub>3</sub> NWs are plotted with temperature in Figure 4(a). The ZT was calculated to be 0.10 for TF NW and 0.08 for TC NW at 300 K. Notably, after a heat treatment at 673 K, the TCHT had higher ZT (0.31) than that (0.21) of TFHT. In good agreement with the Pisarenko relation, the lower carrier concentration of TFHT and TCHT NWs leads to the higher Seebeck coefficient. In addition, the thermal conductivity lowered by twin scattering enabled TCHT to have the highest ZT among the present

Bi<sub>2</sub>Te<sub>3</sub> NWs. The ZTs for Bi<sub>2</sub>Te<sub>3</sub> NWs are plotted with other literature data for Bi<sub>2</sub>Te<sub>3</sub> film and bulk in Figure 4(b).<sup>14,16,17,43,62</sup> It is evident that ZT has a strong correlation to carrier concentration. This result implies that the Pisarenko relation still holds regardless of the dimension of TE materials and the maximum ZT of NWs can be obtained when the carrier concentration is carefully optimized.

## 4 Conclusions

Twin-free and twin-containing Bi<sub>2</sub>Te<sub>3</sub> NWs were electrochemically synthesized by controlling the reduction potential, in order to investigate the effects of twins on TE properties. The TE properties of the synthesized Bi<sub>2</sub>Te<sub>3</sub> NWs were characterized by using two types of microfabricated device (the membrane-type and the island-type MTMP) from 40 K to 300 K. The TCHT NW had the highest ZT of 0.31 due to enhanced Seebeck coefficient and lowered thermal conductivity despite lowered electrical conductivity. The enhanced ZT was mainly attributed to the reduction of the carrier concentration, which gives rise to increasing thermopower according to the Pisarenko relation. Although DFT calculations indicated a 9%  $S$ -degradation by twins in  $n$ -type Bi<sub>2</sub>Te<sub>3</sub>, the  $k_L$ -suppression by twins led to the ZT enhancement of Bi<sub>2</sub>Te<sub>3</sub> NWs. The  $k_L$  was lowered for the twin-containing microstructure suggesting that twins effectively reduce the lattice thermal conductivity regardless of the carrier concentration.

According to the roundup of ZTs of Bi<sub>2</sub>Te<sub>3</sub> thin films and bulk in the literature, the correlation between the carrier concentration and ZT is valid for Bi<sub>2</sub>Te<sub>3</sub> NWs. That suggests that the ZT enhancement of NWs can be achieved by optimizing the carrier concentration and nanoengineering twins.

## 5 Acknowledgements

This work was supported by Future-based Technology Development Program (Nano Fields) through the National Research Foundation of Korea (NRF) funded by the Ministry of Education, Science and Technology (Grant No. 20120009623).

## 6 Notes

<sup>a</sup> Center for Nanomaterials Characterization, Korea Research Institute of Standards and Science, Daejeon, 305-340, Republic of Korea. \*E-mail: jysong@kriss.re.kr

<sup>b</sup> Department of Materials Science and Engineering, Korea Advanced Institute of Science and Technology, Daejeon 305-701, Republic of Korea.

<sup>c</sup> University of Science and Technology, Daejeon 305-350, Republic of Korea

†Electronic Supplementary Information (ESI) available [Additional results on microstructural analysis, DFT calculation, carrier mobilities and procedure of measuring TE properties of NW]. See DOI: 10.1039/b000000x/.

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