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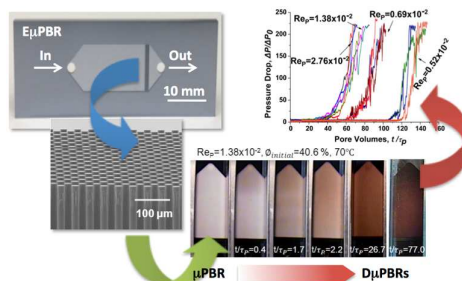
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## Microfluidic investigation of the deposition of asphaltenes in porous media

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The deposition of asphaltenes in porous media, an important problem in science and macromolecular engineering, was for the first time investigated in a transparent packed-bed microreactor ( $\mu$ PBR) with online analytics to generate high-throughput information. Residence time distributions of the  $\mu$ PBR before and after loading with  $\sim 29\mu\text{m}$  quartz particles were measured using inline UV-Vis spectroscopy. Stable packings of quartz particles with porosity of  $\sim 40\%$  and permeability of  $\sim 500\text{mD}$  were obtained. The presence of the packing materials reduced dispersion under the same velocity *via* estimation of dispersion coefficients and the Bodenstein number. Reynolds number was observed to influence the asphaltene deposition mechanism. For larger Reynolds numbers, mechanical entrapment likely resulted in significant pressure drops for less pore volumes injected and less mass of asphaltenes being retained under the same maximum dimensionless pressure drop. The innovation of packed-bed microfluidics for investigations on asphaltene deposition mechanisms could contribute to society by bridging macromolecular science with microsystems.

### Introduction

Miniaturization has broadly advanced the physical and chemical rate principles of organic chemistry, in large part, by providing high-throughput knowledge that bridges molecular-level and laboratory-scale understandings. The ultimate goal of integrating online analytical analyses with microscale devices that yield directly scalable knowledge to real-world scenarios, albeit maturing, remains a vital limitation of the field. High molecular weight aromatics, such as asphaltenes, are difficult to characterise because of the complexity of their chemistry. Deciphering the science of such macromolecular aromatics impacts the sustainability of upstream conventional and unconventional energy production, chemicals manufacture, transportation systems, and the residential and commercial building industries. Tremendous potential exists for lab-on-a-chip devices to discover science that directly scales-up to make societal contributions.

Asphaltene is a macromolecular aromatic, and similar to amino acid derived macromolecules (*e.g.*, proteins, DNA, etc.) they are challenging to characterise due to their thermodynamic and functional complexities. They are the most complex component of crude oil. As a result, asphaltene is commonly defined as the toluene-soluble, light *n*-alkanes-insoluble component of a specific crude oil or other carbonaceous materials such as bitumen and coal<sup>1,2</sup>. They are the heaviest and most polarisable components. Asphaltene obtained from crude oil using *n*-heptane as a precipitant are usually dark-coloured, fragile solids with C:H ratios of  $\sim 1:1.2$  and specific gravity of  $\sim 1.2$ . They consist primarily of aromatic polycyclic clusters and heteroatoms (*e.g.*, N, S, O), as well as trace amount of metals such as V, Fe, and Ni. Similarities exist between asphaltene

and some lower molecular weight fine chemicals and pharmaceuticals. Merit exists for the green hydrothermal cracking of asphaltene into fine chemical and pharmaceutical precursors. Even after decades of academic investigations, understandings of asphaltene structures<sup>2-11</sup>, behaviours at heterogeneous interfaces<sup>10, 12-15</sup>, aggregation and solubility<sup>4, 11, 16-26</sup>, precipitation and depositions<sup>26-39</sup>, dissolutions<sup>40-42</sup>, and the characterization of asphaltene bearing media<sup>37, 43-45</sup>, all remain essential topics of research in this important area of science.

Many factors, such as changes in the temperature, pressure, composition, and shear rate cause asphaltene to precipitate and deposit on heterogeneous surfaces<sup>1</sup>. In upstream petroleum and natural gas production, instabilities of asphaltene within subterranean porous media creates the potential to adversely affect production rates<sup>46-48</sup>. Two recognized models describe asphaltene deposition in porous media: adsorption and mechanical entrapment<sup>47</sup>. Adsorption is reversible with asphaltene desorbing from siliceous and/or carbonate surfaces as their bulk concentrations decrease. Mechanical entrapment (*e.g.*, hydrodynamic bridging) is a physical blocking process of pore throats by precipitated asphaltene particles. Remediation techniques have been studied in order to understand how to mitigate the outcomes of either mechanism on production rates<sup>49</sup>. Conventional macroscale laboratory techniques, however, mask the intrinsic mechanisms and their relationship to asphaltene science.

Microfluidic systems allow for the precise control of conditions to study chemistry<sup>50-57</sup>. The high surface-to-volume ratios attainable in microscale devices and their reduced characteristic length scales within heterogeneous systems minimize the heat and mass transfer resistances, which suggests that microfluidic systems offer advantages in studying intrinsic

flow and reaction behaviour relative to conventional macroscopic systems<sup>51</sup>. The nature of porous media itself represents highly parallelized nanofluidic and microfluidic chemical reactors. Macroscale systems are commonly used to capture the science of chemical reactions in porous media, yet their non-invasive design overlooks key molecular and microscale, mechanistic information. Engineering packed-bed microreactors potentially creates a way to study chemical reactions in situ when unsteady-state time scales are magnitudes less than geological equilibrium conditions. The precipitation of asphaltenes in continuous flow, microchemical reactors<sup>58-61</sup>, in our example, offers a novel approach to overcome the transport limitations while discovering the scalable nature of the kinetic parameters that characterise their deposition mechanisms in porous media.

In the present work, microfluidic devices were designed and fabricated in silicon and Pyrex, for the first time, to develop high-throughput understanding of the deposition of asphaltenes in porous media. Our quartz packed-bed microreactor with online analyses provides a ubiquitous platform to study the deposition of asphaltenes in micro-scale tortuous flows, which bridges the knowledge gap between molecular level events and macro-scale reservoir productions. The porosity loss and permeability impairment of the porous media before and after damages were also studied. The results of asphaltene deposition demonstrate packed-bed microreactors as promising microfluidic tools that could yield mechanistic understanding of high molecular weight aromatics for a broad cross-section of science.

## Experimental

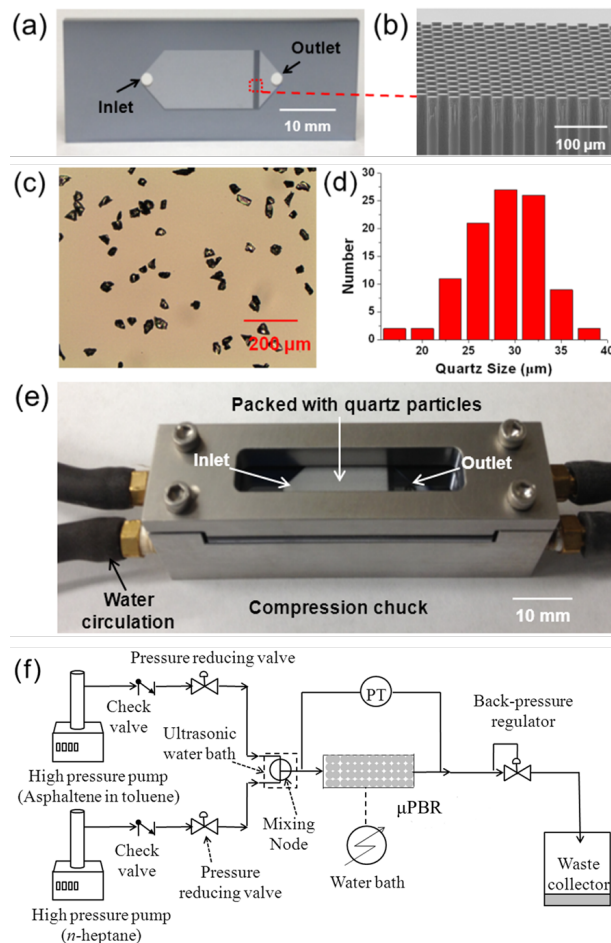
### Chemicals

Toluene and acetone (HPLC grade) were obtained from EMD (Millipore, USA). Ethanol (absolute) and *n*-heptane (HPLC grade) were purchased from Alfa Aesar (Ward Hill, MA, USA). Quartz sand (30~40 mesh) was acquired from VWR International (West Chester, PA, USA). All liquids were used without further purification.

### Device fabrication, layout, and analytics

Empty microreactors (E $\mu$ PBR) were fabricated from 1mm polished single-crystal silicon wafers and capped with 1.1mm Pyrex wafers. The fabrication process primarily included photolithography (spin-coating, exposure, and development), deep reactive ion etching (DRIE), cleaning, anodically bonding of silicon wafers to Pyrex, and dicing into chips, as shown in Fig. S1a of the Electronic Supplementary Information (ESI)<sup>†</sup>. Fig. 1a illustrates a fabricated E $\mu$ PBR with dimensions of 5.0x1.8x0.21cm. Here, the microchannel is 300 $\mu$ m in depth and 9mm in width. Near the outlet, 30 rows of cylindrical pillars of 20 $\mu$ m in diameter were etched 20 $\mu$ m apart, as depicted in the SEM micrograph of Fig. 1b. Quartz particle sizes were designed such that the largest particle size was less than one fourth of the minimum microchannel depth of 300 $\mu$ m to avoid aspect ratios that lead to bridging<sup>61</sup>, *i.e.*, less than 75 $\mu$ m. The starting material, 30–40mesh quartz sands, was grinded by mortar and pestle in the presence of water. Particles were separated and collected using 635mesh and 500mesh sieves. The remaining ultrafine particles were removed by ultrasonic bath treatments. Microscope photographs, *e.g.*, Fig. 1c, acquired using an optical microscope, were used to calculate the quartz particle size number distribution, as shown in Fig. 1d.

From Fig. 1d, mean particle sizes of 29 $\mu$ m were estimated ranging from 17–38 $\mu$ m. The packed bed was prepared by injecting the ~29 $\mu$ m quartz particles dispersed in absolute ethanol into the E $\mu$ R using a 5mL syringe. Fig. 1e shows the packaged system loaded with quartz particles, which creates a native packed-bed microreactor ( $\mu$ PBR). Fig. S1b further illustrates the underside fluidic connections the packaged system.



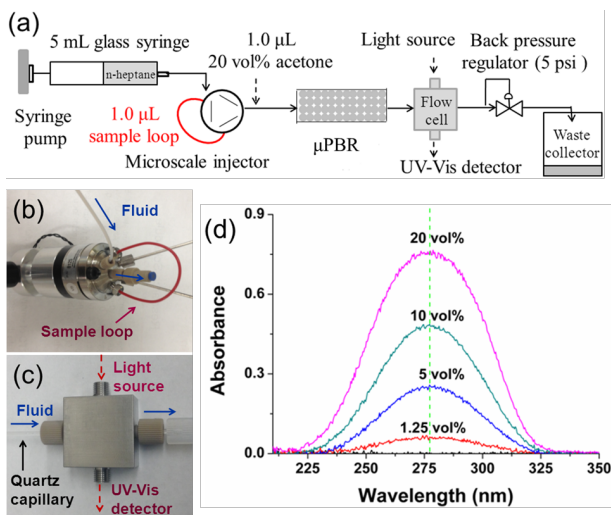
**Fig. 1** (a) Photograph of the E $\mu$ PBR with dimensions of 5.0x1.8x0.21cm. (b) SEM micrographs of 20 $\mu$ m pillars. (c) Microscope photograph and (d) estimated size distribution of the quartz particles. (e) Photograph of the packaged system with water circulation connections. (f) Schematic flow diagram of the experimental setup used to study the deposition of asphaltenes in the  $\mu$ PBR.

The experimental setup used to study asphaltene depositions is shown schematically in Fig. 1f. Two high-pressure pumps (Teledyne ISCO, Lincoln, NE, USA) were used to inject 4g/L asphaltene in toluene (40vol%) and *n*-heptane (60vol%) at constant flow rates. Inline check valves (IDEX Heath & Science, Oak Harbor, WA, USA) prevented back flows of the liquids. Two pressure-reducing valves (IDEX Heath & Science, Oak Harbor, WA, USA) were installed inline as relief devices. Asphaltenes dissolved in toluene and *n*-heptane were mixed in a stainless steel T-union within an ultrasonic bath (VWR International, West Chester, PA, USA) to ensure no accumulations upstream of the  $\mu$ PBR. Inline pressure transducers (500psi, Honeywell Sensing & Control,

Golden Valley, MN, USA), connected to the entrance and exit of the microreactor, enabled online analyses of pressure drops. The packaged  $\mu$ PBR interconnected to a heated circulating bath (Honeywell Sensing & Control, Golden Valley, MN, USA) maintained the  $\mu$ PBR temperature on-chip of 70.0°C. A 5 psi back-pressure regulator (IDEX Heath & Science, Oak Harbor, WA, USA) maintained constant pressure at the  $\mu$ PBR outlet, and it established fluidic resistance in order to minimize the possibility of microchanneling within the  $\mu$ PBR.

### Measurements of residence time distributions (RTDs)

Residence time distributions were measured using a continuous inline UV-Vis spectroscopy system, as shown in Fig. 2. As shown in Fig. 2a, a syringe pump (PHD 2000, Harvard Apparatus, Holliston, MA, USA) and 5 mL SGE glass syringes were used to inject *n*-heptane (carrier solvent) at flow rates of 10.00, 20.00, 40.00, 80.00, and 160.0  $\mu$ L/min. A microscale injector (Fig. 2b, IDEX Heath & Science, Oak Harbor, WA, USA) with a 1.0  $\mu$ L sample loop of acetone (20 vol% in *n*-heptane) delivered the tracer inline and upstream of the  $\mu$ PBR. Axial dispersion of the tracer was measured using inline UV-Vis spectroscopy (Fig. 2c, Ocean Optics, Dunedin, FL, USA) at the outlet of the  $\mu$ PBR. The peak absorbance wavelength of 277 nm (Fig. 2d) was chosen to maximize the signal-to-noise ratio, which improved the resolution of dilute tracer concentration measurements. The microscale injector, packaged  $\mu$ PBR, and UV-Vis spectroscopy were interconnected by 0.005" tubing in order to reduce the dead volume. The light source was allowed to warm-up for at least 20 min before performing RTD experiments.



**Fig. 2** (a) Schematic diagram of continuous inline UV-Vis spectroscopy used to obtain RTD measurements. (b) The microscale injector with a 1.0  $\mu$ L sample loop (8 cm of 0.005" I.D. red tubing), and (c) flow cell integrated with a 400  $\mu$ m I.D. quartz capillary. (d) Measurements of the UV-Vis absorbance (at 277 nm) of acetone in *n*-heptane for varying concentrations.

### Preparation of asphaltenes

Asphaltenes used in the present study were the *n*-heptane insoluble fraction of a Wyoming crude oil deposit provided by Nalco Energy Services. The insoluble fraction was then dissolved in toluene. Passing the solution through a ceramic filter fitted with Whatman No.1 filter paper separated the

insoluble organic and inorganic material. Next, *n*-heptane was combined with the filtrate, the insoluble material collected, and the procedure repeated until no asphaltene precipitating out of the solution. The filtered asphaltene precipitates were then dried at 60.0°C for 24 hrs. The dried asphaltene (dark-coloured, friable solids) were used in the present work.

## Theoretical

### Axial dispersion model

Residence time distribution theory and dispersion models in laminar flow microreactors have been previously described<sup>62</sup>. Under open-open boundary conditions a molecule can pass the boundary several times<sup>63</sup> and the system deviates from plug flow. The dimensionless residence time distribution function is given as<sup>64, 65</sup>,

$$E(\theta) = \frac{1}{\sqrt{4\pi(D^*/uL)\theta}} \exp\left[-\frac{(1-\theta)^2}{4(D^*/uL)\theta}\right] \quad (1)$$

where  $D^*$  is the dispersion coefficient,  $u$  the superficial velocity, and  $L$  the axial length of the microreactor. The maximum peak heights of  $E(\theta)$  curves yield estimations of  $D^*$ , and hence the ratio of convection to diffusion (*i.e.*, the Bodenstein number,  $Bo = uL/D$ ) is estimated for known  $L/d_E$  ratios of magnitude  $10^2$  by combining into<sup>64</sup>,

$$\mathcal{D} = \frac{u^2 d_E^2}{192D^*} \quad (2)$$

Here,  $d_E$  is the effective cross-sectional diameter of the microchannel, and  $\mathcal{D}$  is the molecular diffusivity. Equations (1) and (2) characterise the extents of axial dispersion and molecular diffusion within  $\mu$ PBRs.

### Porosity, permeability, and skin factor of porous media

In packed-beds, important parameters that characterize the porous media include the length of the packed-bed,  $L$ , the mean particle size,  $d_p$ , and the interstitial fluid velocity,  $u_i$ ,

$$u_i = u/\phi \quad (3)$$

where  $u$  is the superficial velocity, and  $\phi$  is the porosity of the porous media (*i.e.*, the void fraction).<sup>66</sup>

Permeability describes how well a given liquid flows through a porous media, and it is controlled by pore sizes and their interconnectivity. The one-dimensional empirical equation discovered by Darcy continues to be widely adopted by engineers and scientists in their descriptions of porous media<sup>67</sup>. Permeability can be estimated by Darcy's law<sup>68</sup>,

$$Q = \frac{\kappa A \Delta P}{\mu L} \quad (4)$$

which describes the relationship between the flow rate in porous media,  $Q$  (*e.g.*,  $m^3/s$  or barrels per day, bpd), the cross-sectional area normal to the axial direction of flow,  $A$  ( $m^2$ ), the permeability,  $\kappa$  ( $m^2$  or mD, and  $1 \text{ mD} = 9.869233 \times 10^{-16} m^2$ ), the dynamic viscosity of the fluid,  $\mu$  ( $Pa \cdot s$  or Cp), and the pressure drop across the packed-bed,  $\Delta P$  ( $Pa$  or Psi).

In porous media, the presence of solid particles themselves causes the diffusion paths of molecules to deviate from their original trajectories. Tortuosity should be considered to

accurately estimate the role of porosity on diffusion, which is defined by<sup>69,70</sup>,

$$\mathcal{T} = \frac{L_e}{L_s} \quad (5)$$

where  $L_e$  and  $L_s$  are the actual length and the straight length of the molecule flow paths. Unlike  $\Phi$ ,  $\mathcal{T}$  values are challenging to directly measure. An empirical tortuosity-porosity relationship for unconsolidated sands has previously been described by<sup>70</sup>,

$$\mathcal{T}^2 = (A\Phi^{1-m})^n \quad (6)$$

where the parameter values in Equation (6) are  $A=1$ ,  $n=1$  and  $m=2.14$ .

The hydraulic radius between the sand grains can be estimated by<sup>71</sup>,

$$r_H = \frac{\Phi}{(1-\Phi)} \frac{d_p}{6} \quad (7)$$

where  $d_p$  is the mean particle size of the sand grains.

The dimensionless van Everdingen-Hurst Skin Factor,  $s$ , commonly used to describe the extent of subterranean well-bore damage, is defined as<sup>71</sup>,

$$s = \Delta P \frac{7.08\kappa_{\text{initial}}h}{Q\mu} \quad (8)$$

where  $h$  is the thickness of production zone.

Reynolds number in a packed-bed,  $Re_p$ , is defined as<sup>72</sup>,

$$Re_p = \frac{d_p u \rho}{(1-\Phi)\mu_i} \quad (9)$$

where  $\rho$  is the density of the solvent. Fully laminar conditions exist for  $Re_p < 10$ , while fully turbulent from  $> 2000$ . Equations (3) through (9) characterise the extent asphaltene deposition within  $\mu$ PBRs has on fluid flow through the porous media.

## Results and discussion

### Porosity, permeability, and tortuosity of the $\mu$ PBR

Characterisations of an E $\mu$ PBR free of quartz particles were first performed to establish the dimensionless constraints that govern the microfluidic system. Table 1 summarizes the experimental conditions achieved in the E $\mu$ PBR and the corresponding dimensionless quantity estimates based on 40vol% toluene and 60vol% *n*-heptane solvent injections. In empty reactors (Table 1a), Reynolds number ranged from 0.25 to 4.1, and as a consequence laminar flow was established for residence times ranging from 0.28 to 4.50min. Viscosities and densities of toluene and *n*-heptane at 70°C were obtained from the work of others<sup>73-76</sup>. Capillary numbers ( $Ca = \mu u / \gamma$ , where  $\gamma$  is the interfacial tension of the liquid) were estimated on the order of  $10^{-5}$ , while the Weber number ( $We = d_E \rho u^2 / \gamma$ ) ranged from 0.02 to  $6.09 \times 10^{-5}$ . Therefore, surface tension dominated over the inertial forces within the E $\mu$ PBR. The ratio of  $Ca/Re = \mu^2 / (d_E \rho \gamma)$  was estimated to be  $0.37 \times 10^{-5}$  (see Fig. S2), which is much smaller than a previously reported value of mineral oil-seawater systems<sup>62</sup> due to the small viscosity and larger effective microchannel diameter. Estimation of the same quantities of  $\mu$ PBRs required first understanding the porosity of the porous media.

**Table 1.** Experimental conditions and dimensionless quantity estimates for the E $\mu$ PBR and  $\mu$ PBR.

		(I)	(II)	(III)	(IV)	(V)	(VI)
(a) E $\mu$ PBR	Total flow rate, $F_T$ ( $\mu\text{L}/\text{min}$ )	-	10.00	20.00	40.00	80.00	160.0
	Mean velocity, $u$ ( $\times 10^{-4}$ m/s)	-	0.62	1.23	2.46	4.92	9.84
	$Re$	-	0.25	0.51	1.02	2.04	4.08
	$Ca$ ( $\times 10^{-5}$ )	-	0.09	0.19	0.38	0.76	1.52
	$We$ ( $\times 10^{-5}$ )	-	0.02	0.09	0.38	1.52	6.09
	$\tau$ (min)	-	4.50	2.25	1.13	0.56	0.28
(b) $\mu$ PBR	Total flow rate, $F_T$ ( $\mu\text{L}/\text{min}$ )	8.00	10.00	20.00	40.00	80.00	160.0
	Interstitial velocity, $u_i$ ( $\times 10^{-4}$ m/s)	1.23	1.54	3.09	6.17	12.3	24.7
	$Re_p$ ( $\times 10^{-2}$ )	0.55	0.69	1.38	2.76	5.52	11.0
	$\tau_p$ (min)	2.25	1.80	0.90	0.45	0.23	0.11

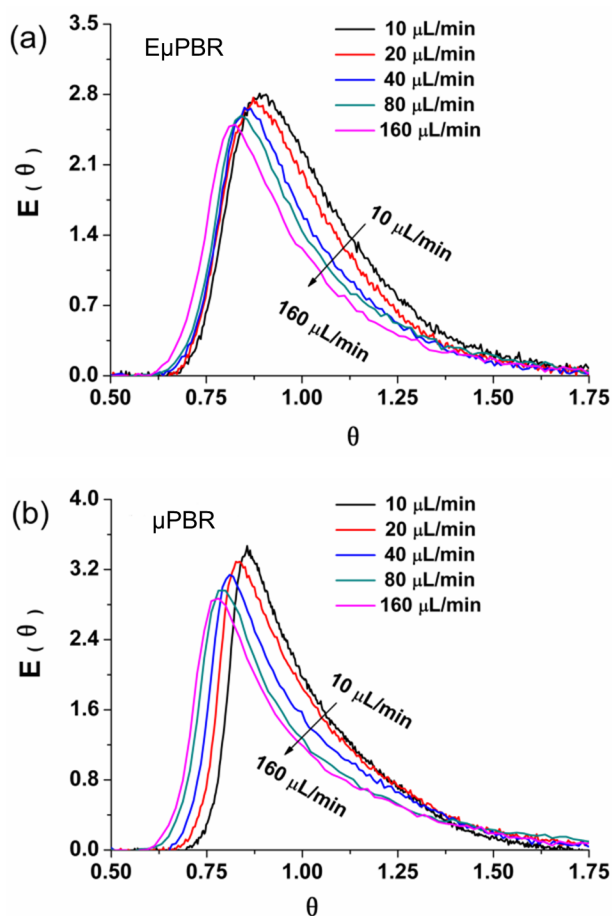
**Table 2.** Porosity, permeability, and tortuosity estimations of the  $\mu$ PBRs.

Reactor	$V$ ( $\mu\text{L}$ )	$\Phi_{RTD}$ (%)	$m$ (mg)	$\Phi_{\text{mass}}$ (%)	$\kappa$ (mD)	$\mathcal{T}$	$r_H$ ( $\mu\text{m}$ )
E $\mu$ PBR	80.2 $\pm$ 0.6	-	0	-	-	1	-
$\mu$ PBR 1	53.8 $\pm$ 0.3	41.3	71.2	40.3	575	1.68	3.37
$\mu$ PBR 2	52.8 $\pm$ 0.4	39.1	73.6	38.3	501	1.73	3.11
$\mu$ PBR 3	53.5 $\pm$ 0.4	40.6	71.7	39.9	557	1.69	3.31
$\mu$ PBR 4	53.1 $\pm$ 0.2	39.7	72.4	39.2	524	1.71	3.23

A  $\mu$ PBR was characterised in order to establish the dimensionless constraints that govern the microfluidic systems via RTD measurements. Figs. 3 and S3 show the dimensionless RTDs of the E $\mu$ PBR and the  $\mu$ PBR. As the flow rates through

the E $\mu$ PBR increased from 10.00 to 40.00 $\mu\text{L}/\text{min}$ , the mean residence times decreased from  $7.97 \pm 0.05$  to  $2.02 \pm 0.02$  min, and from  $5.35 \pm 0.03$  to  $1.35 \pm 0.02$  min for the  $\mu$ PBR (see Table S1). The variance  $\sigma^2$  decreased from 2.13 to 0.17 for the

$E_{\mu\text{PBR}}$ , and it decreased from 1.51 to 0.16 for the  $\mu\text{PBR}$  (see Table S2). The magnitudes of variances are indications of the “spread” of the distributions. Fig. S3a confirmed the shrinkage. The mean volume obtained from RTD measurements was  $80.2 \pm 0.6 \mu\text{L}$  for the  $E_{\mu\text{PBR}}$  and  $53.8 \pm 0.3 \mu\text{L}$  for the  $\mu\text{PBR}$ , as reported in Table 2 for “ $\mu\text{PBR 1}$ ”. The difference between the two,  $26.4 \mu\text{L}$ , corresponds to the volume occupied by quartz particles. The resulting packing efficiency and the porosity of the  $\mu\text{PBR}$  were 58.7% and 41.3%, respectively. The corresponding Reynolds number calculated using Equation (9) is reported in Table 1b. As is evident in Table 1, the interstitial velocity within the  $\mu\text{PBR}$  was much larger than the mean velocity in the  $E_{\mu\text{PBR}}$  for the same volumetric flow rate. Reynolds number in the  $\mu\text{PBR}$  ranged from 0.55 to  $11.0 \times 10^{-2}$  (*i.e.*,  $< 10$ ), and thus laminar flows were confirmed for residence times ranging from 0.11 to 2.25 min.



**Fig. 3** Residence time distribution measurements of the  $E_{\mu\text{PBR}}$  and the  $\mu\text{PBR}$ .  $E(\theta)$  values as a function of dimensionless time ( $\theta$ ) for (a) the  $E_{\mu\text{PBR}}$  and (b) the  $\mu\text{PBR}$ . The volumetric flow rates ranged from 10.00 to 160.0  $\mu\text{L}/\text{min}$ .

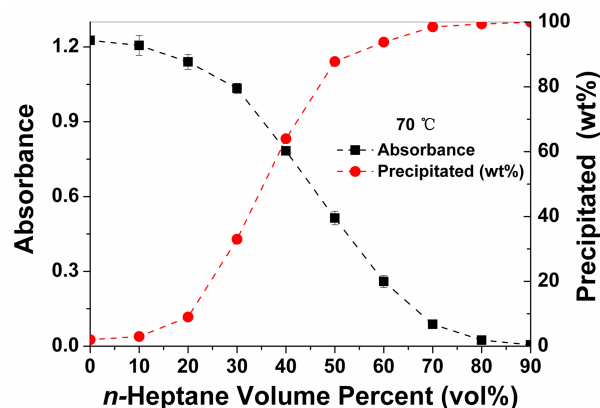
The extent of dispersion was evaluated in both the  $E_{\mu\text{PBR}}$  and the  $\mu\text{PBR}$ . Tracer experiments in *n*-heptane single-phase flows report the dimensionless RTDs of Fig. S3b, which compares  $E(\theta)$  values as a function of dimensionless time ( $\theta$ ) for both microreactors given the same velocity of  $1.23 \times 10^{-4}$  m/s. The maximum peak heights of 3.55 (for the  $\mu\text{PBR}$ ) and 2.73 (for the  $E_{\mu\text{PBR}}$ ) yield estimations of ( $D^*/uL$ ) using Equation (1). As shown in Table S2, ( $D^*/uL$ ) is  $1.24 \times 10^{-2}$  within the

$E_{\mu\text{PBR}}$  and  $7.5 \times 10^{-3}$  within the  $\mu\text{PBR}$  for a velocity of  $1.23 \times 10^{-4}$  m/s. As a consequence, the packing reduced axial dispersion. From Figs. 3a and b, one observes the maximum peak height decreased with increasing volumetric flow rate for both the  $E_{\mu\text{PBR}}$  and the  $\mu\text{PBR}$ . The corresponding values of ( $D^*/uL$ ) are reported in Table S2. From Equation (2), values of  $D$  were calculated to be  $0.85 \times 10^{-8}$  m<sup>2</sup>/s (for the  $E_{\mu\text{PBR}}$ ) and  $0.32 \times 10^{-8}$  m<sup>2</sup>/s (for the  $\mu\text{PBR}$ ), which yielded  $Bo$  values. Values of  $Bo$ , ranged from 10 to  $10^3$  in both the  $E_{\mu\text{PBR}}$  and the  $\mu\text{PBR}$ , which confirms that convective forces dominated over diffusive forces. One observes in Figs. 3a and b that the maximum peaks shifted left for both the  $E_{\mu\text{PBR}}$  and the  $\mu\text{PBR}$  as the flow rates increased. Some degree of back-mixing, by dispersion, was likely present within the microreactors<sup>64, 77</sup>.

To confirm the reproducibility of the packing efficiency, four  $\mu\text{PBR}$  were prepared and the porosities determined by estimations of their RTDs ( $\phi_{RTD}$ ). Values of  $\phi_{RTD}$ , ranging from 39.1 to 41.3%, were estimated and reported in Table 2. Quartz masses within each  $\mu\text{PBR}$  were also measured, and the corresponding porosity ( $\phi_{mass}$ ) estimated from 38.3 to 40.3%. Using Equations (4) and (6), permeability and tortuosity were also estimated to range from 501–575 mD and 1.68–1.73, respectively. The resultant diffusivity within  $\mu\text{PBs}$  (*i.e.*,  $0.32 \times 10^{-8}$  m<sup>2</sup>/s) is less than that within the  $E_{\mu\text{PBR}}$  (*i.e.*,  $0.85 \times 10^{-8}$  m<sup>2</sup>/s), yet of the same order of magnitude. As shown in Table 2, the hydraulic radii calculated from Equation (7) were  $\sim 3.2 \mu\text{m}$ . The preparation of  $\mu\text{PBRs}$  with quartz particles was highly reproducible.

#### The solubility of the asphaltenes and their deposition in $\mu\text{PBRs}$

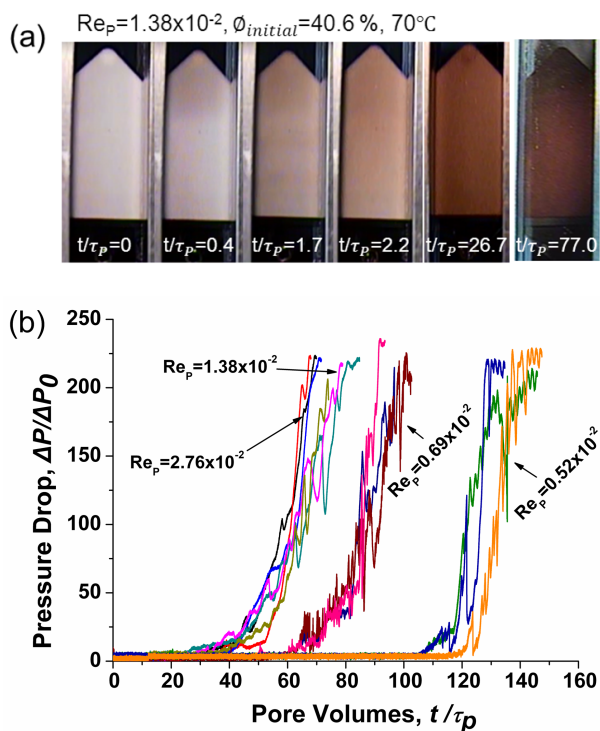
As a next step in understanding asphaltene deposition, their solubility in *n*-heptane was measured using inline UV-Vis spectroscopy. The solubility of asphaltenes in *n*-heptane (0 to 90 vol%) in toluene was investigated. Mixtures of *n*-heptane and 4g/L asphaltenes in toluene at varying ratios were stirred and maintained for 24hr at 70.0 °C before filtration using Whatman No.3 filter paper. The absorbance of asphaltenes in the filtrates were measured using UV-Vis spectroscopy (at 286nm) and the results shown in Fig. 4 (black squares).



**Fig. 4** UV-Vis absorbance of asphaltenes at 286nm in the filtrates, and the corresponding precipitated weight percent of asphaltenes (wt%) for different *n*-heptane volume fractions (vol%).

Contaminated filter papers were dried and the mass measured. As seen in Fig. 4, the precipitated wt% corresponds to different *n*-heptane volume fractions. The absorbance of asphaltenes

decreased from 1.23 to  $5.0 \times 10^{-3}$  as the volume fraction of *n*-heptane increased from 0 to 90vol%. The precipitated asphaltenes were 93.8wt% for an *n*-heptane volume fraction of 60vol% at 70.0 °C. The relationship between the anticipated solubility of the asphaltenes for different volume fractions was therefore established, which enabled the design of experiments for asphaltene depositions in  $\mu$ PBRs.



**Fig. 5** (a) Photographs of the deposition of asphaltenes in the D $\mu$ PBRs obtained using a CCD camera for different pore volumes. (b) Influence of the flow rate on the dimensionless pressure drop as a function of the pore volumes of 4g/L asphaltenes in toluene injected.

Depositions of the asphaltenes within  $\mu$ PBRs (*i.e.*, damaged  $\mu$ PBRs, denoted by D $\mu$ PBRs) were next studied using microscopy. The influence of Reynolds number ( $Re_p$ ) was investigated in the next set of experiments for constant temperature. Asphaltenes dissolved in toluene (concentration of 4 g/L) and *n*-heptane were delivered into the  $\mu$ PBR at an *n*-heptane concentration of 60vol% for varying total flow rates

from 7.50 to 40.00  $\mu\text{L}/\text{min}$  and  $Re_p$  ranging from 0.52 to  $2.76 \times 10^{-2}$ . Fig. 5a shows an example photograph of the deposition of asphaltenes in the D $\mu$ PBR for different pore volumes ( $t/\tau_p$ ) obtained by CCD camera. Values of  $Re_p = 1.38 \times 10^{-2}$  and the initial porosity of 40.6% within the  $\mu$ PBR were estimated. As seen in Fig. 5a, no obvious channelling was observed up to 77.0 pore volumes, as the colour of the D $\mu$ PBR changed uniformly. Uniform deposition of asphaltenes was observed under these conditions and before plugging.

Analyses of fluidic resistances and  $\mu$ PBR-characterisations further revealed the deposition of the asphaltenes within D $\mu$ PBRs. Fig. S4 shows the influence of the flow rate on the pressure drop as a function of time, and Fig. 5b illustrates the corresponding dimensionless pressure drop as a function of the pore volumes of 4g/L asphaltenes in toluene injected. One observes in Fig. 5b that Reynolds number influenced the number of pore volumes necessary to obtain dimensionless pressure drop values of 225. The D $\mu$ PBRs plugged in less pore volumes injected as the ratio of the inertial-to-viscous forces increased. Interestingly, Table 3 shows that as  $Re_p$  decreased from  $2.76 \times 10^{-2}$  to  $0.52 \times 10^{-2}$  the mass of asphaltenes deposited increased from 1.1 to 2.1mg. The corresponding damaged porosities were estimated to range from 0.949–0.902 of the original. The porosity of the D $\mu$ PBR was calculated from the mass of deposited asphaltenes, which was measured by closing the mass balance (*i.e.*, the difference between the mass flow rate of asphaltenes in and out of each D $\mu$ PBR). The mass of asphaltenes in the waste collector and tubing were also measured by flushing with toluene. Reynolds number clearly plays an important role on the mechanism of asphaltene deposition with  $\mu$ PBRs.

#### The deposition mechanisms and dispersion within D $\mu$ PBRs

The mechanism of the deposition process and its impact on permeability impairment are evident upon further evaluation of their relationships to Reynolds number. Statistically, a larger number of asphaltene particles passed through pore throat entrances along stream lines for a given number of pore volumes at larger  $Re_p$  compared to smaller  $Re_p$ , which ultimately lead to hydrodynamic bridging<sup>78</sup>. At smaller  $Re_p$ , precipitated asphaltenes likely penetrated further into D $\mu$ PBRs and uniformly, resulting in gradual dimensionless pressure drop increases. The porosity loss ( $\phi_{damage}/\phi_{initial}$ ) of Table 3 was more severe at smaller  $Re_p$  under the same dimensionless pressure drop of 225.

**Table 3.** Influence of Reynolds number on  $\mu$ PBR impairments that generated D $\mu$ PBRs.

Test	Pore volumes	$Re_p$ ( $\times 10^{-2}$ )	$\phi_{initial}$	$\kappa_{initial}$ (mD)	$m_{total}$ (mg)	$m_{waste}$ (mg)	$m_{deposited}$ (mg)	$\frac{\phi_{damage}}{\phi_{initial}}$	$\frac{\kappa_{damage}}{\kappa_{initial}}$	$s$ ( $\times 10^3$ )	$\frac{\Delta P}{\Delta P_0}$
1	68	2.76	39.7 $\pm$ 0.6	520 $\pm$ 5	4.9	3.8 $\pm$ 0.1	1.1	0.949	0.005	3.46	225
2	68	1.38	41.7 $\pm$ 0.5	580 $\pm$ 4	5.1	4.1 $\pm$ 0.2	1.0	0.956	0.004	4.19	134
3	68	0.69	40.7 $\pm$ 0.3	556 $\pm$ 3	5.0	4.6 $\pm$ 0.3	0.4	0.982	0.020	0.85	13
4	68	0.52	40.4 $\pm$ 0.7	557 $\pm$ 7	5.0	4.8 $\pm$ 0.1	0.2	0.991	0.050	0.33	3.7
5	77	1.38	40.6 $\pm$ 1.0	560 $\pm$ 10	5.5	4.1 $\pm$ 0.2	1.4	0.936	0.002	6.86	225
6	77	0.69	40.5 $\pm$ 0.6	556 $\pm$ 5	5.5	4.9 $\pm$ 0.2	0.6	0.973	0.007	2.46	37
7	77	0.52	39.9 $\pm$ 0.5	529 $\pm$ 5	5.4	5.2 $\pm$ 0.2	0.2	0.991	0.048	0.35	3.9
8	96	0.69	40.3 $\pm$ 0.6	550 $\pm$ 5	7.0	5.3 $\pm$ 0.3	1.7	0.922	0.001	12.7	225
9	96	0.52	41.1 $\pm$ 0.4	570 $\pm$ 3	7.1	6.8 $\pm$ 0.2	0.3	0.986	0.045	0.37	4.2
10	115	0.52	40.5 $\pm$ 0.3	550 $\pm$ 4	8.4	7.1 $\pm$ 0.4	1.3	0.941	0.012	3.21	15.3
11	133	0.52	39.7 $\pm$ 0.7	524 $\pm$ 6	9.5	7.4 $\pm$ 0.4	2.1	0.902	0.001	17.2	225



**Table 4.** Dispersion within  $\mu$ PBR and  $D\mu$ PBRs for different Reynolds numbers.

	$u_i$ ( $\times 10^{-4}$ m/s)	$Re_{P(RTD)}$ ( $\times 10^{-2}$ )	$\sigma^2$ ( $\text{min}^2$ )	$\sigma_{\sigma^2}$	$D^*/(uL)$	$D^*$ ( $\times 10^{-8}$ m <sup>2</sup> /s)	$Bo$
(a) $\mu$ PBR	2.46	0.86	0.85	0.018	0.0086	3.60	90
	9.84	3.44	0.07	0.023	0.0112	18.8	360
	15.4	5.38	0.04	0.025	0.0120	31.4	563
(b) $D\mu$ PBR	2.46	0.86	1.02	0.016	0.0079	3.31	85
	9.84	3.44	0.09	0.021	0.0101	16.9	340
	15.4	5.38	0.04	0.024	0.0113	29.6	531

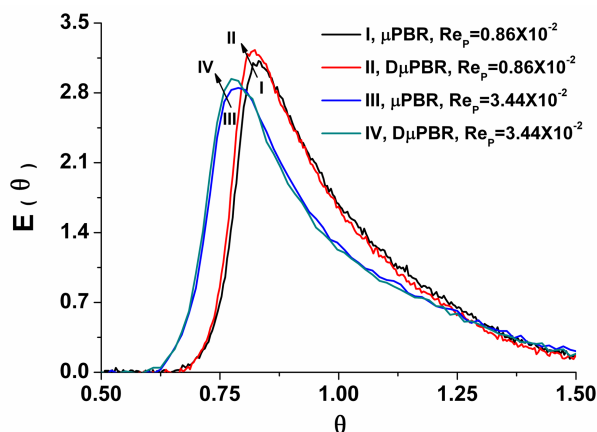
**Fig. 6** Comparison of  $E(\theta)$  values as a function of dimensionless time ( $\theta$ ) for Reynolds numbers of  $0.86 \times 10^{-2}$  (I and II) and  $3.44 \times 10^{-2}$  (III and IV) within  $\mu$ PBR (I and III) and  $D\mu$ PBRs (II and IV).

Table 3 also reports the permeability impairment ( $\kappa_{\text{damage}}/\kappa_{\text{initial}}$ ) ranging from 0.001 to 0.058, and the dimensionless Skin Factor of  $0.33 \times 10^{-3}$  to  $12.7 \times 10^3$  calculated by Equation (8). The viscosity of the mixture at  $70.0^\circ\text{C}$  was obtained from the work of others<sup>73, 74</sup>. Fluctuations of the curves of Fig. 5b at small  $Re_p$  of 0.69 and  $0.52 \times 10^{-2}$  are explained by the relationship between the interstitial velocity and the critical velocity necessary to transport desorbed asphaltene particles at quartz particle surfaces. Under such near equilibrium conditions, previously deposited asphaltene particles desorb from quartz surfaces and begin to move with the flow. The pressure drop then increases when the transported asphaltene particles were trapped or absorbed once again on surfaces. The overall deposition process was the combination of asphaltene absorption and desorption and asphaltene mechanical entrapment<sup>47</sup>. Larger relative ratios of the inertia to the viscous forces favour mechanical entrapment.

Analyses of RTDs of  $D\mu$ PBRs and their comparison to  $\mu$ PBRs reveal the influence of impairments on axial dispersion. The RTDs of  $D\mu$ PBRs were measured after injecting 115 pore volumes for  $Re_p$  of  $0.52 \times 10^{-2}$ . Fig. S5 shows the RTDs of the  $E\mu$ PBR,  $\mu$ PBR, and  $D\mu$ PBRs. One observes in Fig. S5a that the maximum absorbance of a  $D\mu$ PBR shifted left by comparison of the values of the  $\mu$ PBR, which is attributed to the deposition of asphaltenes. The difference in mean volumes between the  $\mu$ PBR ( $53.5 \pm 0.4 \mu\text{L}$ ) and the  $D\mu$ PBR ( $52.5 \pm 0.3 \mu\text{L}$ ) was  $1.0 \mu\text{L}$ , which corresponds to  $\phi_{\text{damage}}/\phi_{\text{initial}}$  values of 94.5%. The result was also approximated from the mass accumulated of 1.3 mg, which corresponds to a volume decrease of  $\sim 1.1 \mu\text{L}$  and  $\phi_{\text{damage}}/\phi_{\text{initial}}$  values of 94.5%. Figure 6 and Table 4

demonstrate that in general axial dispersion increased with increasing  $Re_{P(RTD)}$  values. The same trend was observed for  $Re_{P(RTD)}$  values ranging from  $0.86 \times 10^{-2}$  to  $3.44 \times 10^{-2}$  for  $\mu$ PBRs (I and III) and  $D\mu$ PBRs (II and IV), separately. For a given  $Re_{P(RTD)}$ , however, axial dispersion was reduced by the deposition of the asphaltenes at  $70.0^\circ\text{C}$ . No significant channeling was observed in  $D\mu$ PBRs, as illustrated by the single mode of Figure 6 (*i.e.*, the by-pass model does not accurately describe the system)<sup>66</sup>. The design of  $\mu$ PBRs, their characterization, and integration with online analytics lay the groundwork for understanding nanofluidic by-pass pore throat models that predict  $D\mu$ PBRs. Such information is ubiquitous towards revealing the relationship of the two deposition mechanisms and the dimensionless constraints that describe macroscale scenarios.

## Conclusions

The deposition of asphaltenes in porous media, an important problem in science and macromolecular engineering, was for the first time investigated in transparent packed-bed microreactors with online analytics to generate high-throughput information. Highly reproducible, stable packings of quartz particles with porosity of  $\sim 40\%$  and permeability of  $\sim 500\text{mD}$  were designed. The presence of the quartz particles reduced axial dispersion under the same velocity *via* estimations of the dispersion coefficients and the Bodenstein number. The deposition of asphaltenes decreased axial dispersion.

The high-throughput chemical and microfluidic information revealed the influence of Reynolds number on asphaltene deposition within packed-bed microreactors. For low Reynolds numbers, evidence of asphaltene adsorption onto quartz particle surfaces was revealed. For larger Reynolds numbers, mechanical entrapment likely resulted in significant pressure drops for less pore volumes injected and less mass of asphaltene being retained under the same maximum dimensionless pressure drop. In general, the mass of asphaltene deposited increased as Reynolds number decreased for the same pore volumes injected. As a consequence, the corresponding porosity loss increased and the permeability decreased. No significant channelling was evident in any scenario. The innovation of packed-bed microfluidics for investigations on asphaltene deposition mechanisms promises to contribute to society by bridging macromolecular science with microsystems.

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## Notes and references

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