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Complete List of Authors:	Teran, Javier; University of A Coruña, Analytical Chemistry Andrade-Garda , Jose Manuel; University of A Corunna, Analytical Chemistry Soto-Ferreiro, R.M.; Universisty of A Corunna, Analytical Chemistry Carlosena, A.; Universisty of A Corunna, Analytical Chemistry Prada-Rodríguez, Darío; University of A Coruña, Analytical Chemistry; University of A Coruña, University Institute of Environment

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# A SIMPLE PROCEDURE TO SELECT A MODEL FOR MASS DISCRIMINATION CORRECTION IN ISOTOPE DILUTION INDUCTIVELY COUPLED

J. Terán-Baamonde<sup>a</sup>, J. M. Andrade<sup>b</sup> (\*), R. M. Soto-Ferreiro<sup>c</sup>, A. Carlosena<sup>d</sup> and D. Prada<sup>e</sup>

PLASMA MASS SPECTROMETRY

A fast, simple and straightforward procedure to decide on the best model to calculate the mass discrimination factor in Isotope Dilution Inductively Coupled Plasma Mass Spectrometry (ID-ICP-MS) is proposed. It is based on the study of the residuals of the different models that are proposed commonly, viz., the linear, the exponential, the power and the Russell's models. However, it can be generalized to evaluate any model proposed to linearize the relationship between the theoretical/measured isotope ratios and the mass. The procedure does not involve laboratory extra work, it is rooted on basic statistics associated to the least squares fit, and can be applied easily by the analysts so that decision-making is fast and reliable. The procedure was exemplified with four different examples where Cd, Cr, Nd and Sm were determined by ID-ICP-MS.

**KEY WORDS** Isotope dilution-ICP, Mass discrimination factor, linearization, residuals, least squares fit

### Introduction

Isotope dilution inductively coupled plasma mass spectrometry (ID-ICP-MS) has become a work horse technique to quantify metals at trace and ultra trace levels, study their species and, more recently, determine proteins (using either inespecific and species-specific methods).<sup>1-3</sup> This can be explained, amongst other considerations, because isotope dilution mass spectrometry (ID-MS) was recognized as a definite primary method, meeting the highest metrological standards, by the 'Comité Consultative pour la Quantité de Matière (CCQM)' and so its results are directly traceable to SI units.<sup>4</sup>

Further, in most ID-MS applications the typical working calibration graphs based on the use of calibration solutions of different quantities of the analyte may be avoided. This saves costly instrument time and makes ID-MS applications much more robust than conventional methodologies so less-careful sample preparation is required. Also, ID-MS procedures are more accurate than conventional methodologies, so that fewer quality-control failures are to be expected.<sup>5</sup>

However, adequate training of laboratory staff is required as ID-ICP-MS needs a careful and laborious optimization in order to look for the best measuring conditions that yield a reliable and traceable working chain. A relevant issue here is to recall that a mass discrimination occurs in ICP-MS when ions of different mass are transmitted through the spectrometer, leading to different efficiencies in the transport of the ions which results in non-uniform sensitivity across the mass range and inaccurate isotope ratio measurements.<sup>6</sup> Following, ICP-MS devices may vield biased isotope amount ratios  $^{7}$  and, therefore, mass discrimination must be corrected for using a correction factor, termed mass discrimination factor, K (it is often presented, simply, as the 'mass bias' or 'mass bias factor', or 'mass bias factor per unit mass'). This is defined as the quotient between the true and the measured mass ratios for a pair of given isotopes and so it underlines that the instrumental system may yield a systematic error regarding the correct mass ratio.<sup>8-10</sup>

It is worth noting that K is defined and determined locally for a specific isotope pair. This raises a further potential difficulty as K may incorporate contributions from unsuspected spectral

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interferences which could vary from sample to sample and, thus, make it unrepresentative of the bias obtained for adjacent masses.<sup>6</sup>

In general, two approaches exist to correct for mass discrimination, measured by K.<sup>11</sup> First, external standardisation, where the isotope ratio of interest is measured in a standard solution of exactly known composition of the analyte to be analyzed, and the experimental bias is used to correct for the same ratio in the unknown sample. This allows the mass discrimination factor to be measured at the same masses as the analyte, and approximately at the same abundances. Second, internal standardisation determines the mass discrimination factor of the isotope ratio of interest in the unknown sample solution by means of either a known isotope ratio of an element added to the sample for that purpose, or using a pair of invariant isotopes of the analyte element.<sup>6</sup> Another relevant issue is that K can drift throughout the experiment time and, thus, it must be determined periodically. A standard bracketing sequence is adopted usually, yielding low throughput.<sup>10</sup>

The relative magnitude of mass discrimination can be ascertained using multielemental molar-response curves by which the response observed in the detector is measured as a function of the ion transmission efficiency through the system.<sup>5</sup> In general, these curves have to span through a range of mass/charge values, are complex and depend on the instrument at hand. To make them useful it is necessary to model them functionally. All models calculate a corrected isotope ratio ( $R_{corr}$ ) from an experimentally-measured one ( $R_{exp}$ ), the absolute masses of the isotopes ( $\Delta M$ ), and K (the mass bias factor, which must be determined empirically).

Three functions are of general use; viz. the linear, the exponential and the power ones. They were critiziced somehow by Ingle et al.<sup>6</sup> because they predicted that the bias was dependent on the mass difference and not on the absolute mass. Besides, they have a common origin and the former two may be considered as approximations to the power model<sup>.6,12</sup> Further, in these functions K should be considered as the mass bias per unit mass and it is assumed to be constant across the mass range and proportional, which is not totally correct.<sup>6</sup> This explains why the Russell's model became popular because it avoids these problems as it uses the mass of the two isotopes.

Even though the models might yield similar mass bias factors, inaccuracy may arise from the use of an inappropriate one.<sup>13</sup> Accordingly, the selection of the most suitable functional model is not trivial. Indeed, that calculating the mass bias factor is far from a standardized procedure is demonstrated by the existence of several approaches. Some can be mentioned here (a complete review is out of the scope of this technical note). K was determined as the ratio between the theoretical, or true, isotope ratio and the same ratio measured experimentally.<sup>8</sup> Then, K can be applied using either a bracketing approach or a mathematical model.<sup>4, 6, 14</sup> The use of several internal reference

isotope pairs was compared against the classical approaches mentioned above.<sup>11</sup> This implied the use of a polynomial function and the so-called 'common analyte internal standardization'. The results emphasized the importance of a proper mass discrimination correction (along with the need for a selection of an adequate internal standard).

To complicate things further, the reasons why a model was selected have not always been clarified.<sup>15-17</sup>

Following, this paper aims at presenting a fast and simple procedure to select the best model to calculate the mass discrimination factor in ID-ICP-MS. The key idea is to study and compare the residuals of the different linearized models. Here we will consider the most common ones; viz., the exponential, the linear, the power and the Russell's models, although the procedure can be generalized to any other. Four examples will be considered where Cd, Cr, Sm and Nd were determined.

#### Evaluation of the mass bias factor per unit mass

From a pragmatic viewpoint, the most convenient way to model the instrumental mass discrimination is to relate a suite of theoretical isotope ratios ( $R_{theo}$ ) to their corresponding empirical values ( $R_{exp}$ ), calculate K and, then, use it (along with  $R_{exp}$ ) to calculate a corrected ratio ( $R_{corr}$ ) for the unknown. In general, K is involved in an algebraic equation describing a curve but it can be calculated straightforwardly whenever a linear model is used instead.<sup>6, 8</sup>

As discussed in the previous section, the empirical relationship between  $R_{theo}$ ,  $R_{exp}$  and the two isotope masses can be described in different ways, among which four outstand in literature: the linear (straight line), the exponential, the power and the Russell's models. They are depicted in the second column of Table 1. As their direct use is not trivial, common practice is to linearize them to get simpler and more straightforward equations (see third column of Table 1). To select the best model for a particular problem it was proposed to fit the four linearized models and to study the straight lines obtained by plotting the  $R_{theo}/R_{exp}$  ratio (or a logarithmic form) against the mass difference (or logarithm of the masses, in the Russell's model).<sup>5</sup> However, this approach is subjective and prone to errors because the significance of those plots is not immediate and a sound decision-making is not possible.

Fortunately, basic statistics associated to the straight line (or firstorder) least squares fit yield very simple and reliable criteria to judge on the adequacy of each linearized model.<sup>18-20</sup> Note that the expression 'straight line fit' will be used throughout the text to denote that the models are converted to a straight line function. The term 'linear fit' and the like are not of sufficient quality to assure traceability of the calculations because, after all, any mathematical relationship is 'a line'. Analogously, the term 'linearization' is used to denote an algebraic transformation from a (usually) complex mathematical expression to a straight line equation, whose parameters are of interest (here, the slope K).

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58 59 60 Although the conceptual idea is really simple, it is worth remembering some basic statistics. More details and extensive explanations can be found in the references given herein.

### Review of some concepts associated to the straight line fit

In a typical model, two variables are related as  $y=f(x) + \varepsilon$ , where f(x)is a mathematical function that relates y to x (it is common practice to select a straight line function but other possibilities exist, and the choice is under the analyst's responsibility based on his/her experience and/or experimental data). Note that the model is a mere working hypothesis, which must be modified if the experimental data are against it. Finally,  $\varepsilon$  is the random error, or information not modelled by the calibration function, which is associated to the variable response and denotes how closely the model resembles the measured signals. It is reasonable to accept that the smaller the random errors are, the better the model is. Therefore, how can we fit the best model through a swarm of points? A quite intuitive solution is to look for a model that adheres as much as possible to each and every experimental point so that minimizes the average difference between the experimental signals and those predicted by the model. Hence, the common criterion by which the sum of the squared differences between the measured signal (yexp) and that predicted by the model (ypred) is minimal was accepted as a natural fitting criterion.<sup>18-20</sup> The differences  $(y_{pred} - y_{exp})$  are referred to as 'residuals'. This is the (ordinary) least squares criterion (OLS or LS). Despite its widespread and ubiquitous usage the OLS criterion has three basic mathematical assumptions that are less broadly known:<sup>18-</sup> 22

- i) the experimental errors occur only in the direction of the signal to be measured, y.
- ii) the errors in the y-direction are normally distributed. This means that the resulting errors associated with the analytical signals should follow a normal distribution.
- iii) the errors in the y-direction are independent and of the same magnitude regardless the x values. This property is referred to as 'homoscedasticity' (the opposite situation is called 'heteroscedasticity'). Its presence simplifies the calculations and gives rise to the usual unweighted least-squares line.

Statements ii) and iii) above constitute two cornerstones to assure whether a model fit is acceptable. Since the OLS criterion is a universal procedure to fit functions, it does not guarantee by itself that the model under scrutinity is correct. In order to accept it, we must assess that these two requisites hold on. There are different statistical tests to evaluate the models but most of them should not be used due to the usual low number of data points employed to fit the model<sup>23</sup> (this will be considered later). Therefore, a suitable alternative consists of a graphical visualization and evaluation of the residuals associated to our (temptative) model.

Homoscedasticity of the fit must be assured and, fortunately, can be visualized easily. First, the absence of outlying points must be checked as they may strongly bias any model in different ways,<sup>24</sup> see Figure 1a and Figure 1b for a general, conceptual idea on how strongly an outlier will influence the regression. In general, outliers

situated in extreme positions affect more the fit (rotational effects).<sup>22</sup> Check that all points do follow a unique trend; in case a point behaves anomalously, consider rejecting it and recalculating the model. Sometimes, decisions are not immediate and plotting the residuals will help. This can be done straightforwardly in any spreadsheet, less than a minute, and it may yield enormous benefits. Any data point with a too high residual is suspicious (more formally, a point whose standardized residual is around 3, or higher, should be considered as an outlier<sup>23</sup>). Next, check for the absence of visual trends in the residuals (Figure 1c and Figure 1d). In particular, parabolic trends are frequent (Figure 1d) and they mean that a straight line does not fit the experimental data properly. If a clear trend is not visualized, all residuals are more or less randomly distributed, and are of the same magnitude (Figure 1c), it can be reasonably assured that they are normally distributed and that they have common variance (another requisite of the OLS methodology).<sup>20</sup> Normality can be studied more formally using statistical tests, as those described in the next section, where more details are presented.

It may surprise that so much emphasis is put on graphical decisionmaking but this can be explained quoting NIST: '*Numerical methods* for model validation are useful, but usually to a lesser degree than graphical methods. The latter have an advantage [...] because they readily illustrate a broad range of complex aspects of the relationship between the model and the data'.<sup>25</sup>

### Experimental

#### Data sets

Four case studies will exemplify the working methodology proposed here. Two of them deal with the determination of Sm and Nd and were used as tutorials in a recent textbook.<sup>5</sup> They present a situation where replicates of the experimental ratios are not considered explicitly to set the model. The other two examples are about determining Cd and Cr by ID-ICP-MS, using a cuadrupole analyzer equipped with a kinetic energy discrimination cell. They correspond to an ongoing study in our laboratory to measure some environmentally relevant metals in sediments. Replicates of the mass isotopes are presented and, therefore, will be applied to illustrate the use of the lack-of-fit test (LOF). In addition, Cr was selected because of the low number of isotopes and their low mass (compared to the other elements in the present work).

The experimental isotope ratios were obtained from measurements carried out on Cd and Cr standard solutions of natural isotope composition for ICP analysis (Sigma Aldrich) whose theoretical isotope abundances were obtained from IUPAC.<sup>26</sup> Table 2 compiles the experimental results.

#### Working methodology

In the following, the different candidate models will be considered in their functional linearized straight line forms and the unweighted OLS fit obtained for each one. The first step in selecting a model is to inspect visually the residuals (potential outliers, relative magnitudes of the residuals and absence of

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clear trends) and to study the statistics associated to the regression line (the standard error of the fit, or residual standard deviation,  $S_{v/x}$ ). A careful inspection and a bit of experience are usually enough to get sound decisions, as it will be shown next. Note that as a referee pointed out, the units of  $S_{v/x}$  depend on the particular transformation undergone by the data. Hence, to compare them it is necessary to get rid of the scales. A natural way would be to divide  $S_{v/x}$  by an average value (like the classical relative standard deviation, RSD). However, this is not possible here because the average value of the residuals is zero. To circumvent this problem, the average absolute error (i.e., the average of the absolute value of the residuals),  $|\overline{y_{res}}|$ , is proposed here to get a sort of 'relative standard deviation of the *fit*', RSDF as: RSDF=100\*(( $S_{v/x}$ ) /  $|\overline{y_{res}}|$ ). As classical RSD, it shows the extent of the variability of the residuals in relation to the average value (of the absolute residuals).

In addition, two traditional scale-independent statistics were also considered: the coefficient of determination (R<sup>2</sup>) and the lack-of-fit test (which must be derived from an Analysis of Variance -ANOVA- study when replicates are available).<sup>27</sup> Both are used to evaluate the adequacy of the model to the experimental data. In simple linear regression, the former equals the squared correlation coefficient (given in percentage), but this cannot be generalized to other situations and it is a rough approach to evaluate goodness-of-fit. The lack-of-fit test is an F-test which determines whether the residual information can be associated to the experimental random errors or to 'something' else (i.e., the model has not been able to capture all the relevant variance in the data points and therefore causes a 'lack-of-fit'). Though both tests can be used to compare among different regression models, they should be used in conjunction with the residual plots because they are not powerful enough to assure by themselves that the model is suitable  $^{28,29}$  (a typical problem is that even curvilinear models can exhibit very good figures in both parameters).

Then, statistical tests can be applied to check for normality of the residuals. A normal probability curve (available in most common software) will also simplify decision-making. However, as mentioned above, usual calibrations in Analytical Chemistry do not imply many experimental points due to work, time and resources constraints. As a consequence, it is difficult (sometimes impossible) to rely on sound statistics for decisionmaking due to the low power of the tests (very few degrees of freedom). Non parametric statistics might constitute a powerful alternative but, again, they are not good enough when very few data are available. A clear example here was the impossible application of the non parametric Wald-Wolfowitz's runs test (to check for a random distribution of the residuals) to the Nd and Sm examples due to a lack of tabulated values for such a small number of runs (because of the few data points).

Here, the standardized Kurtosis and Skewness were calculated as a way to describe whether the distribution of the residuals is symmetric and without tails. Then, the non parametric sign test and the Wilcoxon's signed rank test were used to check whether the residuals are distributed randomly. Finally, the Kolmogorov-Smirnov's and the Shapiro-Wilk's tests (the latter is more powerful than the Kolmogorov-Smirnov's one when few data are available) were used to check whether the distribution of the experimental residuals is compatible with a Gaussian one.<sup>22</sup>

Figure 2 resumes the working procedure conceptually.

#### Software

The statistical studies were performed using Excel® and Statgraphics (StatPoint Technologies, Inc., Warrenton, VA, USA).

#### **Results and Discussion**

# Case study 1 and 2: selection of the model when determining Cd and Cr

Table 3 resumes the results of several statistical tests calculated on the residuals of the different models whereas Figure 3 and Figure 4 depict the residuals associated to each model and each example, along with the standard error of the calibration ( $S_{y/x}$ ), the relative standard deviation of the fit (RSDF), the coefficient of determination ( $R^2$ ) and the lack-of-fit test (LOF).

With respect to Cd, a replicate was rejected because it had an outlying behaviour throughout the studies (see Table 2). The linear (straight-line) fit presents a rather clear parabolic pattern (Figure 3) and, so, it has to be discarded. This model shows also a significant lack-of-fit (95% confidence) and, accordingly, it is not suitable for our purposes. The other models do not exhibit a clear trend and, thus, are considered further. The exponential and power models (whose behaviour is almost equal) present a borderline lack-of-fit (LOF). Although, strictly speaking, the test is not significant the experimental p-value associated to the F test is too close to the critical one (0.05, 95% confidence). Finally, the residuals for the Russell's method do not have a definite pattern, the LOF test is clearly not significant, the RSDF is comparable to the other models and the R<sup>2</sup> statistic is marginally better. Therefore, the latter model should be selected.

This conclusion was assured by studying the residuals of the models deeper and calculating the statistics mentioned above. Table 3 reveals that any model has either a skewed distribution or a tailed shape (standardized skewness and kurtosis lower than  $\pm 2$ ). Thus, those statistics do not help deciding on the best model.

The null hypotheses of the sign test and of the Wilcoxon's signed rank test (in both cases,  $H_0$ : the data derives from a population with a median value of zero) cannot be rejected for any model, hereby revealing that the sets of residuals are compatible with a symmetric distribution whose median is zero. However, this does not guarantee that they are normally distributed.<sup>22</sup>

The other tests are intended to check whether the distribution of the residuals is Gaussian ( $H_0$ : the distribution of residuals follows a normal distribution); namely, the Shapiro-Wilk's and the Kolmogorov-Smirnov's tests. In Table 3 no rejection can be made so all models are compatible with the normal distribution of the residuals. The other tests yielded the same conclusion (but for a borderline situation of the straight line model when the Shapiro-Wilk's test was used).

Finally, the Russell's method leaded to the lowest dispersion of the residuals (Figure 5). Therefore, there are not additional evidences against the selection of the Russell's model for Cd.

With respect to Cr, the low number of isotopes yields only three different calibration levels, which complicates decision-making. However, the linear model shows a clear trend (Figure 4) which makes it unsuitable (Figure 2). This was confirmed by the high skewness of the residuas (Table 3), a bad normal probability plot (figure not shown) and a high dispersion of its residuals (Figure 5). Further, the R<sup>2</sup> and LOF revealed that it is the model that fits the experimental data worst. Hence, it should be discarded definitely.

The other three models performed very similar, with good statistics for the residuals (Table 3). The  $R^2$  and LOF tests where almost equal and only marginal best RSDF values were obtained for the exponential and power models. The LOF test was not significant for any of these three models (95% confidence) although it was better for the power and exponential models than for the Russells'one. As the dispersion of the residuals (Figure 5) was slightly better for the power than for the Russell's method, the former was selected for Cr.

# Case study 2 and 3: selection of the model when determining Nd and Sm

Analogous studies were carried out to select the best model to determine K when studying Nd and Sm. These examples do not include replicates for the isotope ratios and, so, the lack-of-fit test cannot be calculated. Previous studies concluded that all models, but the straight-line one, may be acceptable and the exponential method was preferred (although there was a somehow marginal best performance of the Russell's method when determining Nd).<sup>5</sup>

When the residuals plots were considered for Nd (Figure 6) it was concluded that any one showed a particularly cumbersome behaviour as all models had a quite random distribution. The model with the best RSDF was the exponential one, which agreed with the conclusion obtained elsewhere, although following a more elaborate procedure.<sup>5</sup> The R<sup>2</sup> statistic was almost the same for all models and it did not allowed drawing sound conclusions.

The statistics associated to the residuals, Table 3, revealed that the Russell's method yielded a somehow worst distribution (skewness and kurtosis, although not statistically significant), whereas the exponential and the power methods performed best. The latter one was selected finally for Nd because of the lowest dispersion of the residuals (Figure 5).

When Sm was considered (Figure 7) the Russell's and the straightline methods were not acceptable as they showed a parabolic residual pattern and, therefore, the models do not fit the data properly. Hence, they are discarded at the first step of Figure 2. Noteworthy, the approach presented here allows for an immediate and clear rejection of the Russell's model, which was not so simple when calculating relative errors.<sup>5</sup> The exponential and power models behave totally similar (as noticed previously)<sup>5</sup> although with a marginal better RSDF for the power method. With regards to the residuals statistics (Table 3) they reinforce the graphical conclusions. Notice that it is not possible to select between the methods (once the Russell's and straight-line ones were discarded) considering the statistics alone (as for most models in previous section, the null hypotheses of the statistical tests could not be rejected and they were of little value to select a model). The power model was selected owing to the smallest scattering of the residuals (Figure 5).

Two final notes can be given. First, most statistics shown in Table 3 can be visualized in a common box and whiskers plot (Figure 5). Although -strictly speaking- such a plot is not a graphical representation of the tests, the symmetry of the residuals, their distribution and the closeness of the mean and the median can be observed easily. So, for a reduced dataset (as is usually the case), it is possible to take advantage of this plot for decision-making: i) the smaller the box and the whiskers are, the lower the standard error of the regression is; ii) the closer the mean (in the plot this is shown by a cross) and the median (the bar within the box) are, the less likely the existence of outliers will be; iii) the more symmetrical the box and the whiskers are, the less skewed the distribution will be and, likely, the more Gaussian the distribution of the residuals will become. Second, the RSDF was always greater than 100% because it is derived from the residuals. These, in turn, follow essentially a random distribution and, therefore, their variability is expected to be large when compared to the average (of the absolute values, because the arithmetic average is zero). The relevant issue here is to look for models with the lowest RSDF values.

## Conclusions

It was shown that simple plots derived from the residuals of the least squares fit provide a powerful, simple and rather objective criterion to decide on the suitability of a model to calculate the mass discrimination factor (K) in ID-ICP-MS. Visualization of the residuals of the fit for the different models allows deciding on the existence of both outliers and non random (typically, parabolic) patterns.

Then, the lack-of-fit test (if replicates are available) will further test the adequacy of the model. In the examples studied in this paper, the classical coefficient of determination  $(R^2)$  and the

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relative standard error of the fit (RSDF) were not critical to select among different candidate models. However their calculation is straightforward and it is recommended to keep them in order to gather additional information on the models. Further, a box and whiskers plot yields good clues on the symmetry (likely, on the Gaussian distribution) and scattering of the residuals, which can help selecting amongst two very similar candidate models.

It was also observed that in some occasions non parametric statistics were not conclusive enough for decision-making. Thus, the graphical study of the residuals and the lack-of-fit test constitute the cornerstones to differentiate among several models to calculate the mass discrimination factor and to select a suitable one.

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## Notes and references

<sup>a, b, c, d, e</sup> Dept. Química Analítica, Universidade da Coruña, Campus da Zapateira, s/n, E-15071, A Coruña, Spain. (\*) Corresponding author: andrade@udc.es, fax: +34-981167065.

<sup>†</sup>Footnotes should appear here. These might include comments relevant to but not central to the matter under discussion, limited experimental and spectral data, and crystallographic data.

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**Table 1** Models to determine the mass discrimination factor (K) in ID-ICP-MS.  $R_{corr}$  is the corrected isotope ratio,  $R_{exp}$  is the measured isotope ratio,  $R_{theo}$  is the theoretical isotope ratio,  $m_i$  and  $m_j$  are the absolute masses of the selected isotopes and  $\Delta M$  the mass difference between them.

Model	Instrumental relationship	Functional linearized form	Dependent variable
Exponential	$R_{corr} = R_{exp} \cdot e^{\Delta M \cdot K}$	$y = \Delta M \cdot K$	$y = \ln(R_{theo} / R_{exp})$
Straight line (linear)	$R_{corr} = R_{exp} / (1 + \Delta M \cdot K)$	$y = \Delta M \cdot K$	$y = (R_{exp} - R_{theo})/R_{theo}$
Power	$R_{corr} = R_{exp} \cdot (1+K)^{\Delta M}$	$y = \Delta M \cdot \log_{10}(1+K)$	$y = log_{10}(R_{theo} / R_{exp})$
Russell	$R_{corr} = R_{exp} \cdot (m_i \ / \ m_j)^K$	$y = K \cdot log_{10}(m_i/m_j)$	$y = log_{10}(R_{theo} / R_{exp})$

Casa stud-		Exponential	Straight line	Dowor	Dussell
ase study	Cleanmage			rower 0.14	
Cd	Skewness	0.14	1.41	0.14	-0.48
	Kurtosis	0.01	-0.46	0.01	-0.44
	Sign test	p-value=1.00	p-value=0.39	p-value=1.00	<i>p</i> -value=0.61
	Wilcoxon's test	p-value=1.00	<i>p</i> -value=0.78	p-value=1.00	p-value=0.76
	Shapiro-Wilk's test	<i>p</i> -value=0.99	<i>p</i> -value=0.16	<i>p</i> -value=0.99	<i>p</i> -value=0.54
	Kolmogorov-Smirnov`s test	<i>p</i> -value=0.99	<i>p</i> -value=0.65	<i>p</i> -value=0.99	<i>p</i> -value=0.89
	Skewness	-1.26	2.13	-1.26	-1.61
Cr	Kurtosis	0.53	0.80	0.53	0.57
	Sign test	p-value=1.00	p-value=0.40	p-value=1.00	<i>p</i> -value=0.40
	Wilcoxon's test	p-value=0.75	<i>p</i> -value=0.57	p-value=0.75	<i>p</i> -value=0.70
	Shapiro-Wilk test	<i>p</i> -value=0.30	<i>p</i> -value=0.03	p-value=0.29	<i>p</i> -value=0.21
	Kolmogorov-Smirnov's test	p-value=0.93	p-value=0.71	p-value=0.93	<i>p</i> -value=0.88
	Skewness	-0.05	0.75	-0.05	-1.52
	Kurtosis	-0.22	0.13	-0.22	1.24
Nd	Sign test	p-value=1.00	p-value=0.68	p-value=1.00	<i>p</i> -value=0.68
	Wilcoxon's test	<i>p</i> -value=1.00	<i>p</i> -value=0.83	p-value=1.04	<i>p</i> -value=0.68
	Shapiro-Wilk test	p-value=0.99	<i>p</i> -value=0.53	p-value=0.99	p-value=0.19
	Kolmogorov-Smirnov's test	p-value=1.00	p-value=0.99	p-value=1.00	<i>p</i> -value=0.93
Sm	Skewness	-1.12	0.71	-1.12	-0.56
	Kurtosis	0.57	-0.94	0.57	-0.94
	Sign test	p-value=1.00	<i>p</i> -value=0.68	p-value=1.00	<i>p</i> -value=0.68
	Wilcoxon's test	p-value=1.00	p-value=1.00	p-value=1.04	p-value=1.00
	Shapiro-Wilk's test	<i>p</i> -value=0.34	p-value=0.07	p-value=0.34	<i>p</i> -value=0.14
	Kolmogorov-Smirnov's test	<i>p</i> -value=0.94	<i>p</i> -value=0.75	p-value=0.94	<i>p</i> -value=0.89

**Table 2** Original data for the four case studies considered here. The isotopes selected for each element are shown under the heading 'Isotopes', along with their theoretical (derived from IUPAC  $^{26}$ ) and experimentally measured ratios. The mass difference is denoted as  $\Delta M$ .

Case study 1: Cd											
Isotopes	Theoretical ratio	Experimental ratio	ΔΜ	Isotopes	Theoretical ratio	Experimental ratio	ΔМ	Isotopes	Theoretical ratio	Experimental ratio	ΔΜ
106/114	0.043508528	0.031349113	8	111/114	0.445527323	0.391757742	3	113/114	0.425339367	0.406410177	1
		0.031121068	8			0.391053577	3			0.405081916	1
		0.030958661	8			0.394968971	3			0.406683127	1
		0.030647223	8			0.392116797	3			0.406479036	1
		0.030951996	8			0.393185914	3			0.405911499	1
108/114	0.030978072	0.023971763	6	112/114	0.839888618	0.772383915	2	116/114	0.260703098	0.279916302	-2
		0.023763753	6			0.768285734	2			0.278555226	-2
		0.0247017*	6			0.775911501	2			0.279184221	-2
		0.024381751	6			0.774078028	2			0.281141181	-2
		0.02392011	6			0.772314239	2			0.279164297	-2
110/114	0.434737208	0.365326652	4								
		0.365379831	4								
		0.370625246	4								
		0.36543465	4								
		0.366794537	4								
					Case study	2: Cr					
50/52	0.051456543	0.04146233	2	53/52	0.114016237	0.126390065	-1	54/52	0.028414518	0.035143948	-2
		0.039952749*	2			0.125910941	-1			0.03487478	-2
		0.041939234	2			0.125490294	-1			0.034398109	-2
		0.042557359	2			0.126713427	-1			0.036049048	-2
		0.042027005	2			0.127015489	-1			0.035308014	-2
		0.042005136	2			0.125975986	-1			0.03475144	-2
		0.041460437	2			0.126565896	-1			0.035736555	-2
		0.040932561	2			0.125553057	-1			0.034422643	-2
	Case study 3: Nd (**) Case study 4: Sm (**)										
142/146	1.57961487	1.491953	4					144/147	0.2048032	0.197872	3
143/146	0.70824364	0.679507	3					148/147	0.74983322	0.758822	-1
144/146	1.38449008	1.345698	2					149/147	0.92194797	0.943961	-2
145/146	0.48245971	0.475716	1					150/147	0.49232822	0.510151	-3
148/146	0.33486532	0.34442	-2					152/147	1.78452302	1.891842	-5
150/146	0.32800047	0.346675	-4					154/147	1.51767845	1.647119	-7

(\*) outliers excluded from the studies

(\*\*) Case Studies 2 and 3 stem from reference 5.

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Figure 1 Effect on the regression lines calculated by the ordinary least squares criterion when outliers are present in the dataset (the rotational and translational denominations stem from reference<sup>24</sup>) and a graphical example of homoscedasticity (c) and heteroscedasticity (d) in the residuals.



Figure 2 Conceptual description of the approach proposed to select the most suitable model to calculate the mass discrimination factor, K.



**Figure 3** Case study 1 (Cd): Statistics associated to the calibration and graphical representation of the residuals. Models to calculate the K factor: a) exponential, b) straight-line, c) power, and d) Russell.

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S<sub>v/x</sub>=0.01726 R<sup>2</sup>=99.10%

**TECHNICAL NOTE** 

S<sub>v/x</sub>=0.01231 R<sup>2</sup>=99.54%



60



a)

**Figure 4** Case study 2 (Cr): Statistics associated to the calibration and graphical representation of the residuals. Models to calculate the K factor: a) exponential, b) straight-line, c) power, and d) Russell.

b)

d)

![](_page_12_Figure_3.jpeg)

**Figure 5** Box and Whiskers plot of the residuals for each model (Exp= exponential, Lin= straight line, Pow= power, Rus= Russell). The cross in the middle of the box represents the average value whereas the vertical line within the box represents the median.

![](_page_13_Figure_3.jpeg)

**Figure 6** Case study 3 (Nd): Standard error of the fit  $(S_{y/x})$  and graphical representation of the residuals. Models to calculate the K factor: a) exponential, b) straight-line, c) power, and d) Russell.

![](_page_14_Figure_3.jpeg)

**Figure 7** Case study 3 (Sm): Standard error of the fit  $(S_{y/x})$  and graphical representation of the residuals. Models to calculate the K factor: a) exponential, b) straight-line, c) power, and d) Russell.