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1 **Abstract:** The Ta<sub>3</sub>N<sub>5</sub> semiconductor photocatalyst possesses a 720 nm (about 1.72 eV)  
2 sub-band-gap optical absorption but the mechanism of this optical absorption is still  
3 controversial. In this study, the hybrid density functional theory calculations are  
4 performed to unravel the mechanism of 720 nm sub-band-gap optical absorption of  
5 Ta<sub>3</sub>N<sub>5</sub>. By study of possible optical absorptions initiated by the O<sub>N</sub> impurity and V<sub>N</sub>  
6 defect, we find that the 720 nm sub-band-gap optical absorption of Ta<sub>3</sub>N<sub>5</sub> may be  
7 ascribed to the electrons transition from V<sub>N</sub><sup>•</sup> to V<sub>N</sub><sup>•••</sup>. In addition, we propose that the  
8 720 nm sub-band-gap optical absorption can be used to qualitatively evaluate the  
9 photocatalytic water splitting ability of Ta<sub>3</sub>N<sub>5</sub>.

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## 1 **1. Introduction**

2 Optical properties of semiconductors are very important for understanding and utilizing  
3 their functional properties. For semiconductor-based photocatalysts, the optical  
4 properties are especially important because realizing visible light response is  
5 fundamental for an ideal photocatalyst. In order to absorb the visible portion of solar  
6 light as much as possible, the optical band gap of photocatalyst should be about 2.0 eV.  
7 Among various semiconductor photocatalysts, the tantalum nitride ( $\text{Ta}_3\text{N}_5$ )  
8 semiconductor has recently attracted a great of interest because of its excellent  
9 performance in the photocatalytic water splitting<sup>1-5</sup>. Due to appropriate optical band gap  
10 (about 2.1 eV) and band edges positions, the theoretic maximum solar-to-hydrogen  
11 efficiency of  $\text{Ta}_3\text{N}_5$  is as high as 15.9%<sup>6</sup>, suggesting that  $\text{Ta}_3\text{N}_5$  is one potential  
12 semiconductor photocatalyst to split water into  $\text{H}_2$  and  $\text{O}_2$ .

13 Although  $\text{Ta}_3\text{N}_5$  has been extensively studied from experiments<sup>2-5</sup> and theoretical  
14 calculations<sup>7-10</sup>, most work associated with  $\text{Ta}_3\text{N}_5$  has focused on improving its  
15 photocatalytic activity and chemical stability, while some problems associated with the  
16 optical properties of  $\text{Ta}_3\text{N}_5$  remain to be resolved. Fig. 1 shows the schematic optical  
17 absorption spectrum of  $\text{Ta}_3\text{N}_5$ . It can be seen that, besides the 590 nm (about 2.1 eV)  
18 band gap optical absorption, the  $\text{Ta}_3\text{N}_5$  also has a sub-band-gap optical absorption  
19 around 720 nm (about 1.72 eV)<sup>11,12</sup>. The 590 nm band gap optical absorption is ascribed  
20 to electron excitation from the valence band maximum (VBM) to the conduction band  
21 minimum (CBM), while the origin of 720 nm sub-band-gap optical absorption is still  
22 controversial. Some work attributes the 720 nm sub-band-gap optical absorption to

1 trapping and de-trapping of conduction band electrons at the neutral and reduced Ta  
2 centers<sup>11,13,14</sup>, other work attributes the 720 nm sub-band-gap optical absorption to  
3 nitrogen vacancy ( $V_N$ ) that forms during prolonged nitridation of  $Ta_3N_5$  samples<sup>12</sup>.  
4 Unfortunately, none of the above two explanations of the 720 nm sub-band-gap optical  
5 absorption has been experimentally or theoretically verified.

6 In this study, the hybrid density functional theory (DFT) calculations are  
7 performed to unravel the mechanism of 720 nm sub-band-gap optical absorption of  
8  $Ta_3N_5$ . To our knowledge, the sub-band-gap optical absorption and optical emission of  
9 semiconductors are usually correlated with various defects in semiconductors, but an  
10 in-depth understanding of defects, especially the charged defects in  $Ta_3N_5$  is still  
11 inadequate so far. In  $Ta_3N_5$ , the  $V_N$  is the major intrinsic defect because anion vacancies  
12 such as nitrogen vacancy and oxygen vacancy are usually the most common defects in  
13 metal nitrides and oxides. However, both experimental<sup>15,16</sup> and theoretical<sup>7,8</sup>  
14 investigations have proved that the substitution of oxygen for nitrogen ( $O_N$ ) is another  
15 most important impurity in  $Ta_3N_5$ . Note that, although the nominal constitutional  
16 elements of  $Ta_3N_5$  are only composed of Ta and N, the practical  $Ta_3N_5$  samples naturally  
17 consist of considerable amounts of  $O_N$  impurities, which may come from the residual O  
18 of  $Ta_2O_5$  precursor after nitridation treatment. Furthermore, despite of various  
19 experimental conditions, the  $O_N$  impurities cannot be completely eliminated from  
20  $Ta_3N_5$ <sup>15,16</sup>. The  $O_N$  impurity has an important effect on the optical properties of  $Ta_3N_5$ ,  
21 because the optical band gaps of  $O_N$ -doped  $Ta_3N_5$  are oxygen-concentration dependent<sup>17</sup>.  
22 With the increase of  $O_N$  concentrations, the optical band gap of  $O_N$ -doped  $Ta_3N_5$  first

1 decreases and then increases, agreeing well with the experimental observations<sup>16</sup>. Our  
2 recent theoretical calculations reveal that the  $O_N$  impurities help stabilize  $Ta_3N_5$   
3 surfaces<sup>8</sup> and maintain mechanical stability<sup>9</sup> of  $Ta_3N_5$ , validating that the natural  
4 existence of  $O_N$  impurity is theoretically favorable in  $Ta_3N_5$ . Therefore, besides the  
5 intrinsic  $V_N$  defect, the  $O_N$  impurity is also properly correlated with the 720 nm  
6 sub-band-gap optical absorption and must be considered in this study.

7

## 8 **2. Computational methodology**

9 The hybrid-DFT calculations are performed using the VASP<sup>18</sup> code, implemented with  
10 the projector augmented wave (PAW<sup>19</sup>) method. The Hyde-Scuseria-Ernzerhof (HSE<sup>20</sup>)  
11 hybrid functional, which is good at reproducing the accurate electronic structures of  
12 semiconductors, is adopted for the hybrid-DFT calculations. The accuracy of HSE  
13 functional is determined by two critical parameters,  $\alpha$  and  $\omega$ , which are the fraction of  
14 semilocal Perdew-Burke-Ernzerhof (PBE<sup>21</sup>) functional replaced by a screened nonlocal  
15 functional and the inverse screening length, respectively. In our calculations,  $\alpha$  and  $\omega$   
16 are 25% and  $0.2 \text{ \AA}^{-1}$ , respectively, which refer to the HSE06<sup>22</sup> functional. For N, O and  
17 Ta, the  $2s^22p^3$ ,  $2s^22p^4$  and  $5p^65d^46s^1$  orbital, respectively, are treated as the valence  
18 states. The cutoff energy for basis functional is 400 eV. Geometry relaxations are  
19 performed until the residual forces on each ion converged to be smaller than  $0.02 \text{ eV \AA}^{-1}$ .  
20 Based on the above computational parameters, the calculated band gap of pure  $Ta_3N_5$  is  
21 2.2 eV, which is close to the experimental band gap of  $Ta_3N_5$  (about 2.1 eV). The  
22 relaxed lattice constants of pure  $Ta_3N_5$  are  $a=3.87$ ,  $b=10.25$  and  $c=10.27 \text{ \AA}$ , which are

1 also in good agreement with the experimental values ( $a=3.89$ ,  $b=10.21$  and  $c=10.26$   
2  $\text{\AA}$ )<sup>23</sup>.

3 The inset in Fig. 1 shows the conventional cell of bulk  $\text{Ta}_3\text{N}_5$ . The Ta atom is  
4 coordinated with six neighboring N atoms, while N atoms are coordinated with three or  
5 four Ta atoms. Since both experiments<sup>16</sup> and theoretical calculations<sup>8</sup> have proved that  
6 the 3-coordinated N atom is easily substituted by O atom, only the 3-coordinated N  
7 atom is removed and substituted by one O atom to build  $\text{Ta}_3\text{N}_5$  with  $\text{V}_\text{N}$  (denoted as  
8  $\text{Ta}_3\text{N}_5+\text{V}_\text{N}$ ) and  $\text{O}_\text{N}$ -doped  $\text{Ta}_3\text{N}_5$  (denoted as  $\text{Ta}_3\text{N}_5+\text{O}_\text{N}$ ), respectively. We construct a  
9  $3\times 1\times 1$  ( $11.61\times 10.25\times 10.27 \text{\AA}^3$ )  $\text{Ta}_3\text{N}_5$  supercell which contains 60 N and 36 Ta atoms.  
10 Doping with one  $\text{O}_\text{N}$  impurity into this supercell corresponds to about 1.7% doping  
11 concentration, which is in agreement with the about 5%  $\text{O}_\text{N}$  concentration in  
12 experiments<sup>15,16</sup>. Due to the large supercell size and rather time-consuming HSE  
13 calculations, only one Gamma centered  $k$ -point is used for the Brillouin zone integration.  
14 However, this does not affect the reliability of our calculated results because (a) the  
15 same  $k$ -point set is also adopted for the HSE calculations of the  $\text{TaON}$ <sup>24</sup> supercell which  
16 has nearly the same cell sizes as the  $\text{Ta}_3\text{N}_5$  supercell in this study, and (b) we recalculate  
17 some critical results with a dense  $2\times 2\times 2$   $k$ -point meshes (8  $k$ -points) to ensure the  
18 reliability of our results.

19

### 20 **3. Results and discussion**

#### 21 **3.1 Electronic structures**

22 We firstly calculate the density of states (DOS) to study electronic structures of charged

1  $O_N$  and charged  $V_N$  in  $Ta_3N_5$ . For comparison purpose, the DOS of pure  $Ta_3N_5$  is also  
 2 calculated and shown in Fig. 2a. The  $O_N$  impurity can be theoretically presented in the  
 3 neutral ( $Ta_3N_5 + O_N^\times$  in Fig. 2b) and singly positive ( $Ta_3N_5 + O_N^\bullet$  in Fig. 2c) charge  
 4 states. Comparisons between Fig. 2a and 2b reveal that, the CBM of  $Ta_3N_5 + O_N^\times$   
 5 shifts left compared with that of pure  $Ta_3N_5$ . Integral DOS of the left shift part of CBM  
 6 is one, suggesting that one electron is localized at the CBM of  $Ta_3N_5 + O_N^\times$ . Partial  
 7 charge density of the CBM of  $Ta_3N_5 + O_N^\times$  (Fig. 2h) further reveals that this electron is  
 8 uniformly distributed only on Ta atoms, indicating that the neutral Ta ( $Ta_{Ta}^\times$ ) atoms in  
 9  $Ta_3N_5 + O_N^\times$  are reduced by electrons donated from  $O_N^\times$ . Note that, although the  
 10 valence state of reduced Ta can not be precisely determined, the reduced Ta hereinafter  
 11 is expressed by singly negative ( $Ta_{Ta}'$ ) charged state. This is merely for the convenience  
 12 of discussion and will not affect any qualitative analyses in this study. In  $Ta_3N_5 + O_N^\bullet$ ,  
 13 where the electron donated from  $O_N^\times$  is removed, the  $Ta_{Ta}'$  returns to the neutral  
 14  $Ta_{Ta}^\times$  state which is essentially equal to the CBM position. Since the Ta atom is no  
 15 longer reduced, the left shift of CBM disappears in  $Ta_3N_5 + O_N^\bullet$  and the DOS of  
 16  $Ta_3N_5 + O_N^\bullet$  becomes almost the same as that of pure  $Ta_3N_5$ .

17 The above DOS results reveal that, in  $O_N$ -doped  $Ta_3N_5$ , the  $O_N^\times$  can be  
 18 qualitatively regarded as the combination of one  $O_N^\bullet$  and one  $Ta_{Ta}'$ . This means that,  
 19 the variation of  $O_N$  valence states, *i.e.*, the electron transition between  $O_N^\times$  and  $O_N^\bullet$ , is  
 20 merely trapping and de-trapping of conduction band electrons at the  $Ta_{Ta}^\times$  and  $Ta_{Ta}'$   
 21 centers. In addition, the above DOS results also provide a proper explanation to the poor  
 22  $H_2$  evolution ability of  $Ta_3N_5$ . Experiments<sup>2,25</sup> reveal that, although  $Ta_3N_5$  is



1 theoretically an excellent photocatalyst, its practical H<sub>2</sub> evolution ability is poor. Since  
2 the CBM position of one semiconductor reflects its reduction ability to split water into  
3 H<sub>2</sub>, the more negative CBM position of Ta<sub>3</sub>N<sub>5</sub> + O<sub>N</sub><sup>x</sup> suggests that the O<sub>N</sub> impurity is  
4 one possible source of the poor H<sub>2</sub> evolution ability of Ta<sub>3</sub>N<sub>5</sub>.

5 Compared with the O<sub>N</sub> impurity, the V<sub>N</sub> defect is able to donate up to three  
6 electrons to the lattice of Ta<sub>3</sub>N<sub>5</sub>. Then, the V<sub>N</sub> defect can be theoretically presented in  
7 the neutral (Ta<sub>3</sub>N<sub>5</sub> + V<sub>N</sub><sup>x</sup> in Fig. 2d), singly positive (Ta<sub>3</sub>N<sub>5</sub> + V<sub>N</sub><sup>•</sup> in Fig. 2e), doubly  
8 positive (Ta<sub>3</sub>N<sub>5</sub> + V<sub>N</sub><sup>••</sup> in Fig. 2f) and triply positive (Ta<sub>3</sub>N<sub>5</sub> + V<sub>N</sub><sup>•••</sup> in Fig. 2g) charge  
9 states. In Ta<sub>3</sub>N<sub>5</sub> + V<sub>N</sub><sup>x</sup>, where three electrons are donated from V<sub>N</sub><sup>x</sup>, there is a defect  
10 state in the band gap. Integral DOS of this defect state is two, indicating that two of the  
11 three electrons are localized in the in-gap defect state. Partial charge density of this  
12 in-gap defect state (Fig. 2i) shows that these two electrons are mainly localized in the  
13 V<sub>N</sub> site. The left one electron is localized at the CBM of Ta<sub>3</sub>N<sub>5</sub> + V<sub>N</sub><sup>x</sup> and induces the  
14 left shift of CBM, suggesting that the V<sub>N</sub> defect is another possible source of the poor  
15 H<sub>2</sub> evolution ability of Ta<sub>3</sub>N<sub>5</sub>. Partial charge density of the CBM of Ta<sub>3</sub>N<sub>5</sub> + V<sub>N</sub><sup>x</sup> (Fig.  
16 2j) reveals that this electron is uniformly distributed only on Ta atoms, indicating that  
17 the V<sub>N</sub><sup>x</sup> defect is also able to reduce the Ta atoms from Ta<sub>Ta</sub><sup>x</sup> to Ta<sub>Ta</sub><sup>•</sup>. In  
18 Ta<sub>3</sub>N<sub>5</sub> + V<sub>N</sub><sup>•</sup>, where one electron is removed, the in-gap defect state and the  
19 corresponding partial charge density (Fig. 2k) are not changed but the left shift of CBM  
20 disappears. In Ta<sub>3</sub>N<sub>5</sub> + V<sub>N</sub><sup>••</sup>, where two electrons are removed, the defect state remains  
21 in the band gap but only one electron is localized in the V<sub>N</sub> site (Fig. 2l). If all the three  
22 electrons are removed, the in-gap defect state disappears from the band gap of

1  $Ta_3N_5 + V_N^{\bullet\bullet\bullet}$ .

2 The above DOS results reveal that, similar to the  $O_N$  impurity, the  $V_N^{\times}$  can also be  
 3 qualitatively regarded as the combination of one  $V_N^{\bullet}$  and one  $Ta_{Ta}^{\prime}$ . Then, the electron  
 4 transition between  $V_N^{\times}$  and  $V_N^{\bullet}$  is still trapping and de-trapping of conduction band  
 5 electrons at the  $Ta_{Ta}^{\times}$  and  $Ta_{Ta}^{\prime}$  centers. When the  $V_N$  valence states vary between  
 6  $V_N^{\bullet}$  and  $V_N^{\bullet\bullet}$  (or  $V_N^{\bullet\bullet\bullet}$ ), electrons in the in-gap defect state will participate in the  
 7 electron transition.

8

### 9 **3.2 Thermodynamic properties**

10 Although  $O_N$  and  $V_N$  can be theoretically presented in different valence states, some  
 11 valence states of  $O_N$  and  $V_N$  may be thermodynamically unstable. Therefore, we  
 12 secondly calculate formation energies of the charged  $O_N$  and charged  $V_N$  to study  
 13 whether  $O_N$  and  $V_N$  in all charge states are thermodynamically stable. The formation  
 14 energy of defect  $\alpha$  in charge state  $q$  is calculated using the following equation<sup>26</sup>:

$$15 \quad E_f(\alpha, q) = E_t(\alpha, q) - E_t(host) + \sum n_i \Delta\mu_i + q(\varepsilon_F + \Delta V) \quad (1)$$

16 where  $E_t(\alpha, q)$  and  $E_t(host)$  are total energies of  $Ta_3N_5$  supercell with the defect  $\alpha$   
 17 in charge state  $q$  and that without defect in the neutral charge state, respectively,  $n_i$  is  
 18 the number of constituent  $i$  ( $i=N, O, Ta$ ),  $\Delta\mu_i$  is the chemical potential of constituent  $i$   
 19 referenced to the total energy per atom of its pure elemental phase (bulk Ta,  $O_2$  gas and  
 20  $N_2$  gas),  $\varepsilon_F$  is the Fermi energy level referenced to the VBM, and  $\Delta V$  is a correction  
 21 to align the reference potential in the defective supercell with that in defect-free  
 22 supercell.

1 Due to the finite size supercell and charged defects, the image charge correction  
 2 proposed by Makov-Payne<sup>27</sup> should be calculated in this study. The image charge  
 3 correction generally contains monopole and quadrupole corrections. Unfortunately, due  
 4 to the non-cubic cell shape of Ta<sub>3</sub>N<sub>5</sub> supercell, only the monopole correction can be  
 5 correctly calculated by the VASP code. Therefore, only the monopole correction is  
 6 calculated for the image charge correction in this study. However, this will not affect  
 7 our calculated results because the quadrupole correction is typically ~30% of the  
 8 monopole correction<sup>28</sup>. This treatment of image charge correction is also adopted in  
 9 other theoretical work<sup>24</sup>.

10 As can be seen in Eqn. (1), the defect formation energy depends on the chemical  
 11 potential  $\Delta\mu_i$ . To ensure the reliability of defect formation energies, the  $\Delta\mu_i$  must be  
 12 carefully calculated. Under thermal equilibrium growth conditions, Ta<sub>3</sub>N<sub>5</sub> should  
 13 satisfy:

$$14 \quad 3\Delta\mu_{Ta} + 5\Delta\mu_N = E_{Ta_3N_5}^f = -9.39eV \quad (2)$$

15 where  $E_{Ta_3N_5}^f$  is the formation energy of the pure Ta<sub>3</sub>N<sub>5</sub>.  $\Delta\mu_i=0$  ( $i=N, Ta$ ) represents  
 16 the limit where the element is so rich that the pure elemental phases will form.  
 17 Therefore, to avoid formation of the pure elemental phases in Ta<sub>3</sub>N<sub>5</sub>,  $\Delta\mu_i < 0$  must be  
 18 satisfied. Then, based on Eqn. (2), the  $\Delta\mu_N$  and  $\Delta\mu_{Ta}$  under different growth  
 19 conditions can be determined: under N-poor growth condition,  $\Delta\mu_N = -1.88$  and  
 20  $\Delta\mu_{Ta} = 0$  eV; under N-rich growth condition,  $\Delta\mu_N = 0$  and  $\Delta\mu_{Ta} = -3.13$  eV. In the  
 21 O<sub>N</sub>-doped Ta<sub>3</sub>N<sub>5</sub>, to avoid the precipitation of secondary phases such as Ta<sub>2</sub>O<sub>5</sub> and  
 22 TaON, as well as the pure O<sub>2</sub> gas, the following inequations should be satisfied

1 simultaneously:

$$2 \quad 5\Delta\mu_O + 2\Delta\mu_{Ta} < E_{Ta_2O_5}^f = -18.59eV$$

$$3 \quad \Delta\mu_N + \Delta\mu_O + \Delta\mu_{Ta} < E_{TaON}^f = -6.26eV \quad (3)$$

$$4 \quad \Delta\mu_O < 0$$

5 where  $E_{Ta_2O_5}^f$  and  $E_{TaON}^f$  are formation energies of  $Ta_2O_5$  and TaON, respectively.

6 Then, the  $\Delta\mu_O$  under N-poor and N-rich growth conditions are -4.38 and -3.12 eV,  
7 respectively.

8 Using the above chemical potentials, the defect formation energies of charged  $O_N$   
9 and charged  $V_N$  are calculated and shown in Fig. 3a and 3b, respectively. Fig. 3a reveals  
10 that both  $O_N^\times$  and  $O_N^\bullet$  are thermodynamically stable. Fig. 3b reveals that, except  $V_N^{\bullet\bullet}$ ,  
11 the  $V_N^\times$ ,  $V_N^\bullet$  and  $V_N^{\bullet\bullet\bullet}$  are thermodynamically stable. This means that the  $V_N$  defect  
12 in  $Ta_3N_5$  behaves as a negative- $U$ <sup>29</sup> center which is also found in some metal oxides  
13 with anion defects, for example the oxygen vacancy in  $ZnO$ <sup>30</sup> is a negative- $U$  center. Fig.  
14 3 also reflects the thermodynamic transition levels<sup>26</sup> of  $O_N$  and  $V_N$ . The thermodynamic  
15 transition level  $\varepsilon_\alpha(q/q')$  is the Fermi energy level  $\varepsilon_F$  at which the formation energy  
16 of defect  $\alpha$  in charge state  $q$  is equal to that of the same defect but in charge state  $q'$ .  
17 Since both  $O_N$  and  $V_N$  are electron donors in  $Ta_3N_5$ , the thermodynamic transition levels  
18 of  $O_N$  and  $V_N$  are also called the ionization energies<sup>26</sup>. Fig. 3a and 3b show that  
19  $\varepsilon_{O_N}(0/+1)$  and  $\varepsilon_{V_N}(0/+1)$  are as low as 0.06 and 0.16 eV (below the CBM),  
20 respectively, suggesting that both  $O_N^\times$  and  $V_N^\times$  in  $Ta_3N_5$  are shallow donors. In other  
21 words, the thermodynamic electron transition between 0 and +1 charge state is easily for  
22 both  $O_N$  and  $V_N$ . Since the above DOS results reveal that, for  $O_N$  and  $V_N$ , the electron

1 transition between 0 and +1 charge state is essentially trapping and de-trapping of  
2 electrons at the  $Ta_{Ta}^{\times}$  and  $Ta_{Ta}'$  centers, the small ionization energies of  $O_N^{\times}$  and  $V_N^{\times}$   
3 may be ascribed to the easily electron transition between  $Ta_{Ta}^{\times}$  and  $Ta_{Ta}'$ .

4

### 5 **3.3 Optical properties**

6 Based on the in-depth understanding of electronic structures and thermodynamic  
7 properties of the charged  $O_N$  and charged  $V_N$  in  $Ta_3N_5$ , we finally calculate possible  
8 optical absorptions initiated by the  $O_N$  and  $V_N$  centers to unravel the mechanism of 720  
9 nm sub-band-gap optical absorption of  $Ta_3N_5$ . Before studying the optical properties of  
10  $Ta_3N_5$ , it is worthwhile to make a discussion of the optical transition mechanism in the  
11 defective semiconductors.

12 Using a defect  $D$  in the  $q1$  and  $q2$  ( $q1 < q2$ ) charge states as an example, Fig. 4  
13 shows the schematic diagram of optical transitions for the defect doped semiconductor.  
14 It can be seen that, the optical transitions between  $D^{q1}$  and  $D^{q2}$  involve with two  
15 possible optical absorptions and two possible optical emissions. One optical absorption  
16 occurs through the process  $D^{q1} + h\nu \rightarrow D^{q2} + e$  in which  $D^{q1}$  absorbs a photon and is  
17 converted to  $D^{q2}$  with an electron at the CBM (Fig. 4a). After geometry relaxation, the  
18  $D^{q2}$  is relaxed to the ground state. Then, the optical emission process occurs when the  
19 electron at the CBM is recombined with the hole trapped at  $D^{q2}$  (Fig. 4b). The other  
20 possible optical absorption occurs through the process  $D^{q2} + h\nu \rightarrow D^{q1} + h$  in which  $D^{q2}$   
21 accepts an electron excited from the VBM and is converted to  $D^{q1}$ , with a hole (h)  
22 trapping at the VBM (Fig. 4c). The optical emission process occurs when the electron in

1  $D^{q1}$  is recombined with the hole trapped at the VBM (Fig. 4d). The optical absorption  
 2 energy in Fig. 4a and optical emission energy in Fig. 4b can be derived from the  
 3 following Eqn. (4a) and (4b), respectively<sup>26,31</sup>:

$$4 \quad \varepsilon^{opt}(D^{q1}/D^{q2}) = E^f(D^{q2}/D^{q1}) - E^f(D^{q1}/D^{q1}) \quad (4a)$$

$$5 \quad \varepsilon^{opt}(D^{q2}/D^{q1}) = E^f(D^{q2}/D^{q2}) - E^f(D^{q1}/D^{q2}) \quad (4b)$$

6 where  $E^f(D^x/D^y)$  ( $x,y=q1$  or  $q2$ ) denotes formation energy of  $D^x$  with the relaxed  
 7 geometry of  $D^y$ . The optical absorption energy in Fig. 4c and optical emission energy in  
 8 Fig. 4d can be calculated by the similar method. It is worthy of mentioning that, the  
 9 optical transition level is defined similar to but actually different from the  
 10 thermodynamic transition level calculated in the Section 3.2. More details of the optical  
 11 transition level, as well as the differences between optical transition level and  
 12 thermodynamic transition level, can be found in Ref. 26.

13 Fig. 5 shows the possible optical absorption and optical emission energies initiated  
 14 by  $O_N$  and  $V_N$  centers in the form of configuration coordinated diagram<sup>26</sup>. It can be seen  
 15 that:

16 (i) In Fig. 5a and 5b, the optical absorption energies  $\varepsilon^{opt}(O_N^x/O_N^{\bullet})$  and  
 17  $\varepsilon^{opt}(O_N^{\bullet}/O_N^x)$  are 0.10 (12400 nm) and 2.16 (574 nm) eV, respectively, which are in  
 18 disagreement with the 720 nm sub-band-gap optical absorption. The optical absorption  
 19 in Fig. 5a corresponds to the optical transition mechanism in Fig. 4a. Since the electron  
 20 transition between  $O_N^x$  and  $O_N^{\bullet}$  corresponds to that between  $Ta_{Ta}^{\prime}$  and  $Ta_{Ta}^x$  (equal  
 21 to the CBM position), the 0.10 eV optical absorption energy initiated from  $O_N^x$  to  $O_N^{\bullet}$   
 22 is attributed to the electron excitation from  $Ta_{Ta}^{\prime}$  to CBM, which needs a very small

1 energy because  $Ta_{Ta}^{\cdot}$  just locates at the bottom of CBM. The optical absorption in Fig.  
 2 5b corresponds to the optical transition mechanism in Fig. 4c. The 2.16 eV optical  
 3 absorption energy initiated from  $O_N^{\bullet}$  to  $O_N^{\times}$  is attributed to the electron excitation  
 4 from VBM to  $Ta_{Ta}^{\times}$ . Since  $Ta_{Ta}^{\times}$  is equal to the CBM position, the 2.16 eV optical  
 5 absorption occurs through the electron excitation from VBM to CBM, which is nearly  
 6 equal to the band gap of  $Ta_3N_5$ ;

7 (ii) In Fig. 5c and 5d, the optical absorption energies  $\varepsilon^{opt}(V_N^{\times}/V_N^{\bullet})$  and  
 8  $\varepsilon^{opt}(V_N^{\bullet}/V_N^{\times})$  are 0.21 (5905 nm) and 2.07 (599 nm) eV, respectively, which are not  
 9 equal to the 720 nm sub-band-gap optical absorption. Since the electron transition  
 10 between  $V_N^{\times}$  and  $V_N^{\bullet}$  is also trapping and de-trapping of electrons at the  $Ta_{Ta}^{\times}$  and  
 11  $Ta_{Ta}^{\cdot}$  centers, the optical transition mechanisms between  $V_N^{\times}$  and  $V_N^{\bullet}$  is similar to  
 12 that between  $O_N^{\times}$  and  $O_N^{\bullet}$ . This is also the reason why both the optical absorption and  
 13 optical emission energies in Fig. 5c and 5d are close to that in Fig. 5a and 5b,  
 14 respectively;

15 (iii) In Fig. 5e and 5f, the optical absorption energy  $\varepsilon^{opt}(V_N^{\bullet}/V_N^{\bullet\bullet\bullet})$  and  
 16  $\varepsilon^{opt}(V_N^{\bullet\bullet\bullet}/V_N^{\bullet})$  are 1.98 (626 nm) and 2.15 (577 nm) eV, respectively. The 1.98 eV (626  
 17 nm) optical absorption energy is close to 720 nm, suggesting that the 720 nm  
 18 sub-band-gap absorption of  $Ta_3N_5$  is likely attributable to electrons transition from  $V_N^{\bullet}$   
 19 to  $V_N^{\bullet\bullet\bullet}$ . After increasing the  $k$ -point from single Gamma point to the dense  $2 \times 2 \times 2$   
 20  $k$ -point meshes (8  $k$ -points), the recalculated  $\varepsilon^{opt}(V_N^{\bullet}/V_N^{\bullet\bullet\bullet})$  is 1.74 eV (713 nm), which  
 21 is in good agreement with the experimental observed 720 nm sub-band-gap absorption.  
 22 Although  $V_N^{\bullet\bullet}$  is a thermodynamically unstable charge state, we also calculate the

1 optical absorption associated with  $V_N^{**}$ . As can be seen in Fig. 5g to 5j, all the four  
2 possible optical absorption energies associated with  $V_N^{**}$  are not equal to 1.72 eV (720  
3 nm), further confirming that the 720 nm sub-band-gap optical absorption may be  
4 ascribed to the electron transition from  $V_N^*$  to  $V_N^{***}$ .

5 Based on the relationship between  $V_N$  defect and 720 nm sub-band-gap optical  
6 absorption, we propose that the 720 nm optical absorption can be treated as a fingerprint  
7 of the  $V_N$  defect in  $Ta_3N_5$ . More importantly, since the  $V_N$  defect may lower the  $H_2$   
8 evolution ability of  $Ta_3N_5$ , we can further use the 720 nm optical absorption to  
9 qualitatively predict or evaluate the photocatalytic water splitting ability of  $Ta_3N_5$ . For  
10 example, experiments<sup>11</sup> reveal that, the  $H_2$  evolution ability of  $Ta_3N_5$  with the weak 720  
11 nm optical absorption intensity is much better than that with the strong 720 nm optical  
12 absorption intensity, which may be ascribed to the less  $V_N$  defects in the former  $Ta_3N_5$   
13 semiconductor photocatalyst. We hope that the future investigations of the  $Ta_3N_5$   
14 semiconductor photocatalyst may be enlightened from this study.

15

#### 16 **4. Conclusions**

17 In summary, based on the hybrid-DFT calculations, we unravel the mechanism of 720  
18 nm sub-band-gap optical absorption of  $Ta_3N_5$ . By study of possible optical transitions  
19 initiated by  $O_N$  and  $V_N$  centers, we find that the 720 nm sub-band-gap optical absorption  
20 may be ascribed to the electron transition from  $V_N^*$  to  $V_N^{***}$ . Moreover, the electronic  
21 structures and thermodynamic properties of the charged  $O_N$  and charged  $V_N$  have been  
22 intensively investigated in this study. This will provide significant indications for future



1 investigations of the Ta<sub>3</sub>N<sub>5</sub> semiconductor photocatalyst.

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### 3 ACKNOWLEDGMENT

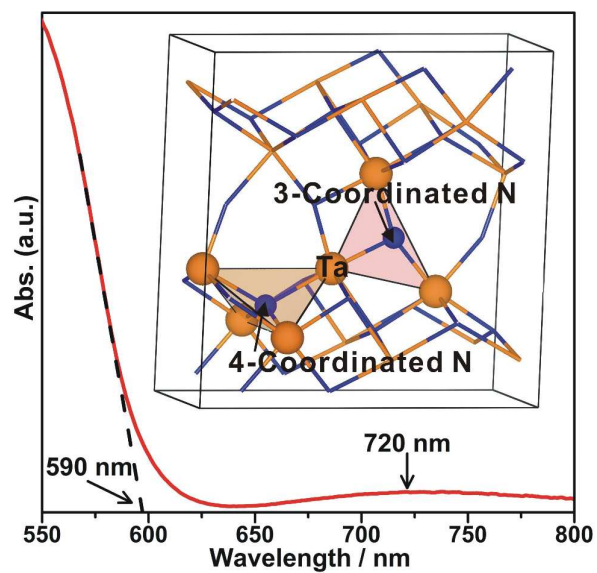
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12

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2 **Fig. 1** The schematic optical absorption spectrum of the Ta<sub>3</sub>N<sub>5</sub> semiconductor. Inset is3 the conventional cell of the bulk Ta<sub>3</sub>N<sub>5</sub>.

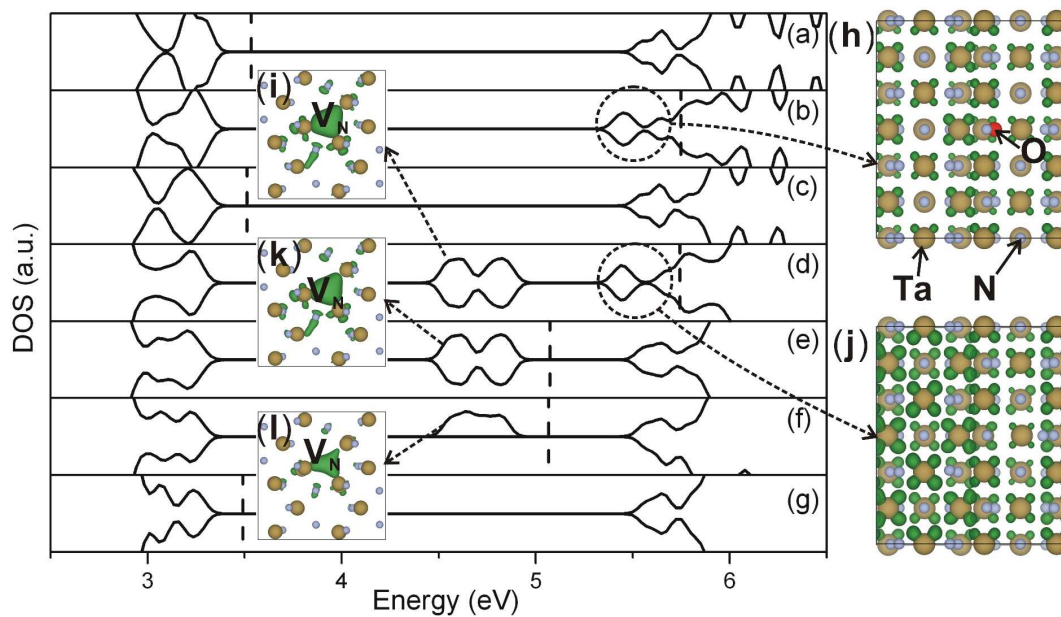
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2 **Fig. 2** The DOS of (a) pure  $\text{Ta}_3\text{N}_5$ , (b)  $\text{Ta}_3\text{N}_5 + \text{O}_\text{N}^\times$ , (c)  $\text{Ta}_3\text{N}_5 + \text{O}_\text{N}^\bullet$ , (d)  $\text{Ta}_3\text{N}_5 + \text{V}_\text{N}^\times$ ,3 (e)  $\text{Ta}_3\text{N}_5 + \text{V}_\text{N}^\bullet$ , (f)  $\text{Ta}_3\text{N}_5 + \text{V}_\text{N}^{\bullet\bullet}$  and (g)  $\text{Ta}_3\text{N}_5 + \text{V}_\text{N}^{\bullet\bullet\bullet}$ . In each case, the vertical

4 dash line is the Fermi level. The horizontal axes of (b) to (g) are aligned with that of (a)

5 by the electrostatic potentials. (h) to (l) are partial charge densities of the labeled CBM

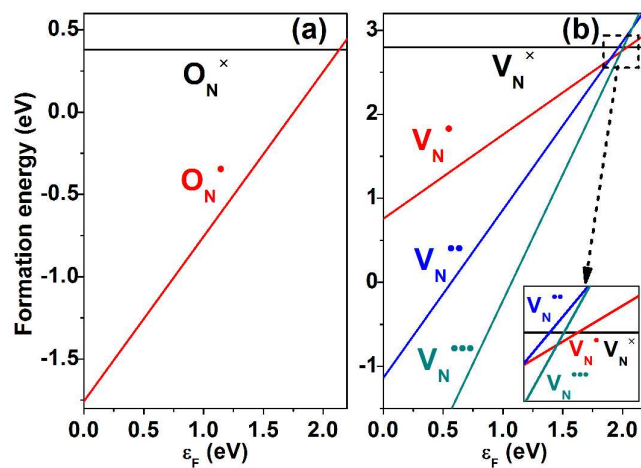
6 or in-gap defect state (isosurface level=0.001 electron/ $\text{\AA}^3$ ).

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2 **Fig. 3** Defect formation energies as a function of the Fermi level ( $\epsilon_F$ ) for (a)  $O_N$  and (b)3  $V_N$  defects under the N-rich growth condition.

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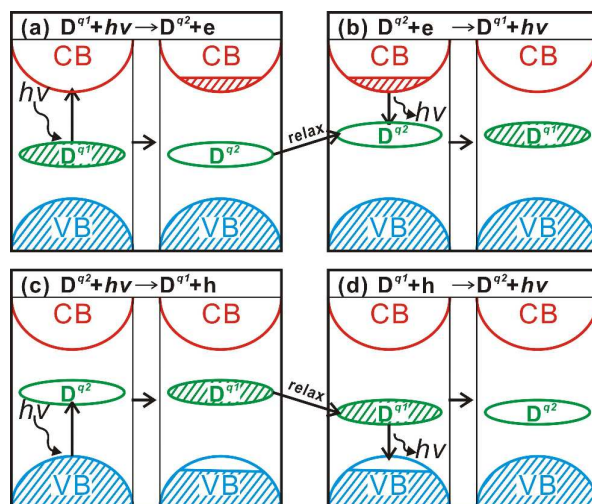
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2 **Fig. 4** Two optical absorption [(a) and (c)] and two optical emission [(b) and (d)]3 processes in a semiconductor when the valence states of the defect  $D$  vary between  $q1$ 4 and  $q2$  ( $q1 < q2$ ) charge state. The shaded and blank areas denote electron occupied and

5 electron unoccupied states, respectively.

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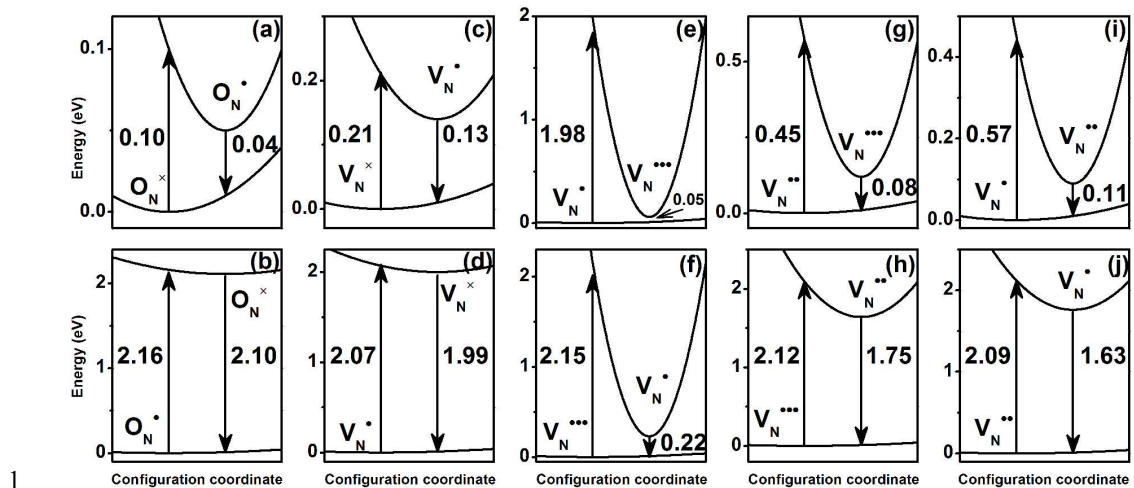
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2 **Fig. 5** Calculated configuration coordinate diagram for the  $O_N$  [(a) and (b)] and  $V_N$  [(c)  
3 to (j)] defects in  $Ta_3N_5$ . The charged defect formation energies, which are used to obtain  
4 the configuration coordinate diagram, are calculated with the Fermi level locating at the  
5 CBM and under the N-rich growth condition.