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Deviation from cone geometry significantly influences the ion current rectification through track-etched nanopores with tip radii smaller than 10 nm.
Accurate characterization of single track-etched, conical nanopores

Pavel Yu. Apel, Patricio Ramirez, Irina V. Blonskaya, Oleg L. Orelovitch and Bozena A. Sartowska

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Single track-etched conical nanopores in polymer foils have attracted considerable attention in recent years due to their potential applications in biosensing, nanofluidics, information processing, and other fields. The performance of a nanopore critically depends on the size and shape of its narrowest, nanometer-sized region. In this paper, we reconstructed the profiles of both doubly-conical and conical pores, using an algorithm based on conductometric measurements performed in the course of etching, coupled with SEM data. We showed that pore constriction deviates from the conical shape, and the deviation depends on the energy loss of the particle that produced the track. Funnel-like profiles for tracks of four ions with different atomic numbers were derived from experimental data. The simulations, using a Poisson-Nernst-Planck model, demonstrated that the ion current rectification properties of the funnel-shaped asymmetrical pores significantly differ from those of conical ones if the tip radius of the pore is smaller than 10 nm. Upon subjection to further etching, the pores gradually approach the “ideal” conical geometry, and the ion transport properties of these two pore configurations become almost indistinguishable.

Introduction

Nanopore devices have become an important class of analytical instruments, particularly as sensors for (bio)molecules and nanoparticles. Both biological pores, typically imbedded in a lipid bilayer, and artificial nanopores, produced in an insulating material such as silicon oxide, silicon nitride or an organic polymer, are used in this field of research and development. Nanopores of precise shape and size are also of interest with regard to separation processes, nano- and microfluidics, controlled release, logic gates, energy harvesting and storage. Among the many methods developed for nanopore fabrication, the track-etch technique has proved to be a convenient and relatively simple approach. It entails the creation of damage tracks by bombarding a thin foil with high-energy ions, followed by chemical etching to transform the tracks into mono-disperse hollow channels (pores). Both multi-pore and single-pore membranes can be produced using this technique. An asymmetrical etching procedure has been developed to fabricate the so-called conical pores. These pores are produced in a cell, one half of which is filled with a strong etch solution, typically sodium hydroxide, while a stop-etch solution is added to the other half-cell. The cell is equipped with two gold or platinum electrodes so that a bias voltage can be applied to the system. When the etchant breaks through to the other side of the foil, it is neutralized by the stopping solution. Additionally, the electric field pulls out the hydroxide ions from the new-born pore, thus terminating the growth of the pore. As a result, an asymmetrical pore is obtained, with the large-diameter opening on the order of several nanometers. Such approximately conical pores possess ionic selectivity and diode-like current-voltage characteristics in electrolytic solutions. The ionic selectivity stems from the presence of carboxylic groups, capable of dissociation, on the pore walls, and from the nanometer-sized narrow part of the pore (“tip”). The diode-like behavior directly relates to the geometrical asymmetry of the nanopores with electrical charge on the walls. Asymmetrical track-etched pores have become the subject of extensive study, from both theoretical and experimental viewpoints, with the goal of understanding the transport of electrolytes in confined spaces and developing new nanofluidic devices. Such aspects as the mimicking of biological ion channels, biosensing, ion current rectification, voltage gating, chemical gating, and others have been investigated. In a series of papers, the effects of tip diameter, cone angle, pore shape and length on the ionic current rectification were analyzed theoretically and experimentally. Asymmetrical nanopores of non-conical shapes have been fabricated, studied experimentally and modeled using an approach based on the Poisson-Nernst-Planck equations. It was concluded that the geometry of the narrow part of an asymmetrical pore plays the most important role in its diode-like behavior.

Apart from asymmetrical nanopores, symmetrical doubly-conical track-etched pores are also of interest. Asymmetrical chemical modification makes it possible to impart useful functions to doubly-conical pores. In all instances, it is important to control and characterize the geometry of the conical nanopores accurately and precisely. The base diameters of conical nanopores can be determined by field-
emission scanning electron microscopy (FESEM), which is a routine procedure. Conversely, it is practically impossible to find and identify a single hole a few nanometers in diameter on the surface of polymer foil using FESEM. Therefore, the size of the tip opening is estimated with the conductometric method. The ionic conductance of the electrolyte-filled nanopore is measured at applied transmembrane potentials of between +100 and -100 mV, where the current-voltage curve is linear. The slope provides the conductance \( G \), from which the tip radius is calculated using the formula\[ G = \frac{k \pi r R}{L}, \] where \( r \) is the tip radius of the pore, \( R \) is the base radius of the pore, \( k \) is the specific conductivity of the electrolyte in the pore and \( L \) is the pore length. Eqn. (1) is valid for both asymmetrical conical pores and symmetrical doubly-conical pores. In the latter case, \( r \) stands for the radius of constriction in the middle of the pore. A serious drawback of this approach stems from the fact that the conical geometry of etched ion tracks is a macroscopic model that ignores the latent track structure.\[49\] The latent track of a heavy ion in polymer is a damage zone of cylindrical shape, within which the material’s properties, both physical and chemical, are significantly altered. The central zone along the ion’s path, called the “track core”, consists of severely damaged polymer molecules. The transverse dimension of the track core is a few nanometers. Due to the release of volatile radiolysis products, the density of the track core is substantially lower than the density of the undamaged polymer.\[50, 51\] The free volume in the track core causes a drastic increase in the etch rate. The etch rate along the track is called “track etch rate”. The etch rate in the transverse direction, the radial etch rate, changes with pore radius in a complex way, which reflects the spatial distribution of radiation effects around the ion’s path. A typical feature of common polymers, such as polyethylene terephthalate, polycarbonate and some others,\[52\] is that radiation-induced cross-linking results in a reduced etch rate at radii between approximately 5 and 50 nanometers, i.e., outside the track core. This zone, in which the etch rate is lower than the bulk etch rate, is called the “track halo”. The covalent links between macromolecules in the track halo make the chain segments less mobile, and thus less susceptible to chemical attack. On the nanometer scale, such a spatial distribution of radiation effects inevitably leads to the non-conical geometry of the etching front, namely, to funnel-like pore tips.\[49\] Moreover, the radius of the zone modified by an ionizing particle depends on its energy loss, \( dE/dx \). The energy loss depends on the effective charge and velocity of the particle. Therefore, etched tracks from ions with different atomic numbers and/or different kinetic energies should have different shapes.

Recently, we suggested a procedure that allows for determination of the geometry of a nanopore, in case the etching front reflects the latent track structure.\[53\] The method is based on the conductometric monitoring of symmetrical etching, i.e., etching with the same etch solution on both sides of the foil. Based on analysis of the time dependence of pore conductance, the profile of the quasi-doubly-conical pore can be reconstructed. In this paper, we apply the developed algorithm to tracks of ions with different atomic numbers, and present quantitative characterization of pores with significantly different shapes of constriction. We also demonstrate how the funnel-like pores gradually approach the “ideal” conical geometry as the etching continues after breakthrough. Finally, we present calculations illustrating the ionic transport properties of pores with the reconstructed funnel-like profile, and compare them to those of conical pores having the same conductance.

### Experimental

#### Ion irradiation

Polyethylene terephthalate (PET) biaxially oriented films (10-μm-thick GOST-24234-80, USSR, and 12-μm-thick Hostaphan RN, Kalle, Germany) were irradiated with single U and Au ions at the UNILAC facility of GSI (Darmstadt). Reference samples were irradiated with the same ions, at fluences of 10⁷-10⁸ cm⁻². Stacks consisting of 4-10 samples were exposed at normal incidence. The initial specific energy of the projectiles was 11.1 or 11.4 MeV/u for many- and single-ion irradiations, respectively. Both types of irradiations with 1.2 MeV/u Xe ions and 4.0 MeV/u Fe ions were performed using the IC-100 cyclotron and the U-400M cyclotron (FLNR JINR, Dubna). The basic parameters of the accelerated ions are shown in Table 1.

<table>
<thead>
<tr>
<th>Ion</th>
<th>Specific energy (MeV/u)</th>
<th>Energy loss in PET foil, dE/dx (keV/nm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>U</td>
<td>5-11.4</td>
<td>19-21</td>
</tr>
<tr>
<td>Au</td>
<td>5-11.4</td>
<td>15-17</td>
</tr>
<tr>
<td>Xe</td>
<td>1.2</td>
<td>8-11</td>
</tr>
<tr>
<td>Fe</td>
<td>4.0</td>
<td>4.6-5.0</td>
</tr>
</tbody>
</table>

The second column presents the specific energy of an ion impinging the polymer foil. Use of ions with atomic numbers from 26 to 92 enabled us to vary the energy loss \( dE/dx \) in the tracks from approximately 5 to 20 MeV/μm.\[54\] The variations of \( dE/dx \), as the ions passed through the foil, were within the limits shown in the third column.

#### Etching and measurement conditions

Etching of single- and multi-track samples was performed in a two-compartment electrolytic cell, to provide identical treatment conditions. Before etching, all samples were exposed to soft (wavelength > 315 nm) ultraviolet radiation for 30 minutes, to stabilize the track-to-bulk etch ratio.\[49\] The foil thickness was measured before and after etching, and its average thickness was used to determine the bulk etch rate. Both halves of the cell were filled with 9 M NaOH. High alkali concentration was used to ensure the fabrication of “doubly-conical” pores by maintaining a relatively low track-to-bulk etch rate ratio. Conductometric monitoring of the etching process for single-track samples was performed in AC mode using a PC-controlled LCR-meter (HiTESTER 3522-50, HIOKI E. E. Corporation, Japan). After filling both compartments with the etchant, the electrical resistance was measured by applying a sine voltage with an amplitude of 0.5 V to the gold electrodes. To avoid interference from 50 Hz noise, a frequency of 1333 Hz was chosen. To avoid overflow of the measuring device in the beginning of the process, a calibrated resistor was connected in parallel with the cell. The
relevant conductance was subtracted from the measured values to obtain the conductance $G$ of the pore itself. The particulars of these measurements were dictated by the following factors: (1) there is no need for a high sensitivity because the electrical current through a conical pore filled with a concentrated electrolyte solution is relatively high; (2) the current should be monitored for a long time, up to values of $10^{-5} - 10^{-4}$ A; (3) polarization of electrodes should be eliminated; (4) the applied voltage should be low, to avoid influencing the etching process.

Pore breakthrough was identified by a sharp onset of the electrical current. Electron microscopy investigations were performed on multi-track samples. These reference samples, containing many ion tracks, were etched under identical concentrations and temperatures. Depending on the required resolution and magnification, samples were examined using either an SEM (JSM-840, JEOL; TM3000, Hitachi, Japan) or an FESEM Ultra Plus (Zeiss, Germany) instrument. Pore diameters on both foil surfaces were measured. Embrittled samples were fractured to observe the inner pore structure. Pores that cleaved exactly along their longitudinal axes were selected for imaging. Details of the sample preparation and FESEM examination have been reported previously.\textsuperscript{42}

**Results and discussion**

Conductometric measurements and their interpretation

Experimentally measured pore conductivity curves, $G^{1/2}(t)$, for different bombarding ions are shown in Fig. 1. For comparison, a theoretical dependence of the square root of conductance vs. etching time is also plotted in Fig. 1.

\begin{equation}
G(t) = \frac{k \pi V_B^2 (t-t_b)}{I_0 - 2V_B t},
\end{equation}

where $L_0$ is the initial thickness of the foil, $t$ is etching time, and $t_b$ is breakthrough time.

**Fig. 2** Two models for two-sided ion track etching: a) double-cone, b) quasi-doubly-conical pore consisting of two funnel-like halves symmetrical to each other with respect to the central plane. The cross-linked zone around the track core is marked with crosses. For other designations, see the text.

The calculated shape of $G^{1/2}(t)$ for the doubly-conical pore was obtained using typical input parameters ($9$ M NaOH, $k = 0.25$ S cm$^{-1}$, $V_B = 2$ nm/min, $t_b = 78$ min, and $L_0 = 12$ $\mu$m). This idealized function is a monotonically increasing curve. The experimental curves for all the tracks distinctly differ from the theoretical curve for $G^{1/2}$ between $5 \times 10^{-3}$ and $2 \times 10^{4}$ S$^{1/2}$. The observed dynamics of pore growth is not that of a double cone. As we have already mentioned in the introduction, one must consider the structure of the latent track to explain the observed dynamics of pore growth. At small radii the etching process cannot be described by a unique etch rate $V_B$. Within a cylinder of approximately 100 nm in diameter, the polymer is substantially modified by ion-induced radiolytic reactions. In the track core (radius < 5 nm), the etch rate $V_T$ is typically several orders of magnitude higher than the bulk etch rate. In the halo (radii between 5 and 50 nm), the track etch rate is slower than the bulk etch rate. The diameters of both the track core and the track halo depend on the energy dissipated around the ion path.\textsuperscript{52} With increasing pore diameter, the local etch rate recovers gradually and reaches the bulk etch rate at the outer halo diameter. As a result, double-funnel-shaped (or “quasi-doubly-conical”) pores form after breakthrough. Fig. 2b shows the quasi-doubly-conical pore geometry. The longitudinal profile of the pore is determined by the spatial distribution of radiation effects in the latent track. It
is essential that the pore be symmetrical with respect to the center plane of the foil and that its evolution can be regarded as an imaginary (virtual) movement of its two halves towards each other at a speed \( V_T \). Such a consideration allowed us to derive the following equation, which relates the measured conductance of the pore to its geometrical parameters \( R \) and \( r \):

\[
\frac{(1-V_B/V_T)}{R^2(t)} - \frac{1}{r^2(t)} = \left( \frac{k\pi}{2V_T} \right) \frac{d}{dt} \left( 1/G(t) \right).
\]

(3)

Using eqn. (3), the constriction radius \( r(t) \) can be calculated using the measured values of \( R(t) \), \( G(t) \), \( V_B/V_T \), and \( k \).

The same model of pore growth as the movement of two mirror halves makes it possible to obtain the longitudinal profile \( r_s(x) \) of the pore from the \( r(t) \) function. The desired \( r_s(x) \) function can be found, based on the fact that the time dependence and the distance dependence are linked to each other via the parameter \( V_T \). For any time \( t_i \geq t_0 \) the quasi-doubly conical shape is given by the pair of parametric equations with parameter \( t \):

\[
r_s(t) = r(t)
\]

(4)

\[x(t) = L_0 / 2 \pm V_T \left( t - t_i \right)
\]

(5)

Here \( x \) is the distance along the pore axis (see Fig. 2b); the length \( x = L_0/2 \) corresponds to the middle plane of the foil. The plus and minus signs in eqn. (5) correspond to the right and left halves of the pore in Figure 2b, respectively. Values of \( r(t) \) within the time interval between \( t_i \) and \( t_i + (1 - V_B/V_T)t_i \) are needed to calculate the pore profile at the time \( t = t_i \). In a typical experiment, pore evolution was monitored for a time exceeding \( t_0 \) by a factor of 2 to 3, which was necessary to reconstruct the whole pore. The average pore opening diameters were determined by SEM within the same time interval, and were approximated with a linear function to obtain the required dependence \( R(t) \).

Fig. 3a shows the result of an experiment performed with a single Fe ion track. A sharp decrease in foil resistance was observed at \( t = 481 \) min (marked with a vertical arrow). The constriction radius of the growing pore was calculated in two different ways. Using eqn. (1), the radius \( r_c \) of this critical part of the pore was estimated within the framework of the double-cone model. Eqn. (3) was employed to calculate the constriction radius \( r \) without presumptions as to the particular shape of the two symmetrical halves of the pore. Both \( r_c \) and \( r \) increase nonlinearly with etching time during the first 20-30 minutes after breakthrough, thus demonstrating the radial dependence of the local etch rate in the latent track. The radius \( r_c \) grows more or less smoothly, while the radius \( r \) increases sharply, beginning at a delay of approximately 1-2 minutes after the drop in resistance. This short phase, characterized by a current of a few nA, appears to signify a transition between the under-etched latent track and the open channel. It is known that electrolytes can penetrate the excess free volume of latent tracks created by heavy ions. Due to this process, the electrical current flowing between two etched cones (or, more appropriately, funnels), through the short residual segment of the latent track, is high enough to be distinguished from the background. Fig. 3b illustrates such an under-etched ion track in a simplified form. In this intermediate phase, the radius of constriction calculated by eqn. (1) takes a value of \( \sim 1 \) nm. Its physical meaning is questionable because the specific conductivity of the etch solution-soaked latent track is not equal to the bulk value. At the time \( t = 482.5 \) min, the radius \( r_c \) of the potentially conical pore remains as small as 1.5 nm, while the radius calculated by eqn. (3) jumps to 3.5 nm. We interpret this moment as the formation of an open channel, free of polymer fragments in the middle of the pore, as shown in Fig. 3c. Taking into account the typical values of track etch rate and the duration of the intermediate phase, one can conclude that the current of \( \sim 1 \) nA corresponds to a residual latent track length of several tens of nanometers. It should be noted that the electrical current through the under-etched pore was especially high in the case of the Fe ion because of the large cone angle of the two mirror halves. The wide cones (i.e., funnels) have a low electrical resistance, which is connected in series with the resistance of the residual part of the latent track. Conversely, the funnel-shaped parts of the uranium track pore are much narrower (due to a much shorter breakthrough time), and the electrical current, both during the transition phase and thereafter, is proportionally smaller, mostly due to the higher resistance of the etched part of the pore. As a result of the smaller current, the formation of an open channel cannot be identified as clearly.
The question arises as to whether the slow radial growth of the pores at small radii is caused by diffusion limitations of the etch solution into the pores. The same phenomenon could affect the specific conductivity of the solution in the new-born narrow channels. To check the possibility that the measured conductance vs. time curves were influenced by diffusion, we performed an experiment on single track etching at a significantly lower temperature. The curve U-LT in Fig. 1 shows the results of the etching of a uranium ion track at 0.5 °C. The 20-degree decrease in temperature resulted in a 20-fold increase in breakthrough time (note the time scale on top). Such a significant change in the track etch rate suggests that the chemical reaction was not diffusion limited. Actually, the 20-fold difference corresponds to the activation energy of approximately 100 kJ/mol, which is typical of reaction rate limited kinetics. The specific conductivity of the working solution decreased from 0.27 S cm⁻¹ at 22 °C down to 0.085 S cm⁻¹ at 0.5 °C, i.e., by three times. Because conductivity directly relates to diffusivity, it is obvious that in the low-temperature experiment the rate of the chemical reaction was significantly reduced, while the rate of diffusion was not seriously altered. However, the shape of the G²₁⁻² vs. time curve remained the same. Therefore, we concluded that the dynamics of pore growth and the electrolyte conductivity in the pore were not limited by diffusion.

Reconstructed pore profiles

Fig. 4 shows the profiles of symmetrical pores obtained via the two-sided etching of single tracks, produced by different high-energy ions. The profiles were reconstructed using the arrays of measured data for G(t) and R(t) and the algorithm described by eqns. (3)-(5). The pore’s central segments, with a length of 2,000 nm, are shown at three or four different etching times, each exceeding the breakthrough time by 2-20 minutes. In the case of the heaviest ion, U, the deviation from the ideal double-cone geometry extends in an axial direction for up to ± 500 nm from the center plane. The inscribed triangles serve to locate the region where the deviation is significant. It is clearly seen from Figs. 4a-c that the pores obtained by etching Fe ion tracks are much closer in shape to the double cone than those produced from the tracks of heavier ions. As the pore widens, its geometry gradually approaches the doubly-conical shape. Five minutes after breakthrough, when the constriction radius reaches 7-9 nm, the critical region still has a double-funnel geometry (see Fig. 4a). A prolonged etching is required to approach a conical geometry, which is attained at a constriction radius of approximately 15-20 nm. In reality, however, the geometrically ideal double cone could hardly form even at long etching. Due to faster removal of short fragments of polymer chains, the ridge between the two conical surfaces tends to be smoothed. This tendency is clearly seen in the SEM images of pores etched up to radii significantly larger than the size of the latent track. The smoothed constrictions with a radius of approximately 40 nm are shown in Fig. 5a, where the fracture of a multi-pore sample is imaged.

The tip profiles for U and Xe ion tracks, calculated for the time t = t₀ + 1 min, are shown in Figs. 5b and 5c and compared with the SEM images of real pore tips, obtained by one-sided etching tracks of the relevant bombarding particles. Each pair of plots and micrographs has the same scale. The calculated and directly observed profiles are in good agreement. Other experimental confirmations of this pore shape are the scanning electron microscope images of the metal replicas and fractured membrane samples that have recently been published.

![Reconstructed pore profiles](image_url)

**Fig. 4** Central part of reconstructed pore profiles of the U (a), Xe (b) and Fe (c) ion tracks, etched from both sides. Center plane: x = 6000 nm. The numbers at the curves denote the etching time after breakthrough, in minutes. Inscribed triangles are intended to show the deviation from double-cone geometry.

The pore radius as a function of the distance from the tip, for tracks of four different ions, is presented in Fig. 6. The regions with rₑ < rₘ ≈ 100 nm are shown, where the effect of dEdx on pore shape is most pronounced. These profiles can be considered as simulations of pores produced by asymmetrical etching, followed by a short additional etching (which is often used to obtain a pore with reproducible and stable properties). The reconstruction algorithm accounts for the movement of the etching front towards the tip and the simultaneous small shortening of the pore, due to bulk etching on both sides. The resulting reconstructed profiles resemble elongated funnels, whose tip lengths (defined here as the abscissa xₘ, where rₑ(xₘ) = rₘ) systematically decrease with decreasing atomic number of the track-forming ion. Surprisingly, the radius of the narrowest part of the tip does not vary much and is randomly valued at around r ≈ 4 nm. This scatter in radius length is most likely due to an uncertainty in determination of the...
breakthrough time. The length of the funnel tip correlates much better with the ion atomic number than does the tip radius. The half angles of the conical parts of the pores also correlate well with \( dE/dx \) and take the values of 2.6, 2.9, 3.4 and 7.5° for U, Au, Xe and Fe ions, respectively. The half angle directly reflects the decrease in the track etch rate \( V_T \) with continuing energy loss of the track-forming particle.

![Xe Ion Track](image1)

**Fig. 5** Confirmation of pore profiles using scanning electron microscopy. (a) Fracture of PET foil, 12-\( \mu \)m-thick, with Xe ion tracks etched from both sides, approximately 20 minutes after breakthrough. (b, c) Reconstructed tip profiles of asymmetrical pores obtained by one-sided etching of single Xe (b) and U (c) ion tracks, in true proportion. Insets: FESEM images of pore tips in fractured many-pore samples, irradiated with the same ions. Both insets are to scale.

To quantitatively characterize the shape of the tip in each particular case, the profiles for \( x < x_m \) were fitted by the equation

\[
r_x(x) = \frac{r_m - r}{1 - \exp \left( -\frac{x_m}{h} \right)^n} - \frac{r_m - r}{1 - \exp \left( -\frac{x}{x_m} \right)^n} \left( \frac{x_m}{h} \right)^n.
\]

where the geometrical parameters \( n \) and \( x_m/h \) control the shape of the pore (the limit \( x_m/h \to 0 \) and \( n = 1 \) gives a conical pore). For \( x_m < x < L \), where \( L \) is the pore length after etching, a linear profile \( r_x(x) \) was assumed. Table 2 summarizes the results obtained. In all cases, parameters \( r \), \( R \), \( x_m \) and \( L \) were taken directly from the experiments, while parameters \( n \) and \( h \) were calculated from least square fitting. As expected from the curves presented in Fig. 6, the radius of the pore base increases with decreasing \( dE/dx \). As in the case of the pore tip length \( x_m \), parameter \( h \) decreases with decreasing \( dE/dx \). However, at etching time \( t = t_b + 2 \) min, neither the ratio \( x_m/h \) nor the parameter \( n \) vary noticeably with \( dE/dx \), and they attain values of approximately 0.8 and 1.5, respectively.

**Table 2** Geometrical parameters characterizing the reconstructed profiles of asymmetrical pores obtained with the four ions indicated, at etching time \( t = t_b + 2 \) min.

<table>
<thead>
<tr>
<th>Ion</th>
<th>( r ) (nm)</th>
<th>( R ) (nm)</th>
<th>( L ) (nm)</th>
<th>( x_m ) (nm)</th>
<th>( h ) (nm)</th>
<th>( x_m/h )</th>
<th>( n )</th>
</tr>
</thead>
<tbody>
<tr>
<td>U</td>
<td>4.5</td>
<td>466</td>
<td>11560</td>
<td>2375</td>
<td>2790</td>
<td>0.85</td>
<td>1.53</td>
</tr>
<tr>
<td>Au</td>
<td>4.5</td>
<td>540</td>
<td>11505</td>
<td>2154</td>
<td>2520</td>
<td>0.85</td>
<td>1.47</td>
</tr>
<tr>
<td>Xe</td>
<td>4.0</td>
<td>597</td>
<td>11327</td>
<td>1791</td>
<td>1920</td>
<td>0.93</td>
<td>1.48</td>
</tr>
<tr>
<td>Fe</td>
<td>4.0</td>
<td>1220</td>
<td>10240</td>
<td>784</td>
<td>1060</td>
<td>0.74</td>
<td>1.46</td>
</tr>
</tbody>
</table>

A similar characterization of the pore shapes obtained with U ions at different etching times was performed. The results obtained are presented in Table 3. Again, parameters \( r \), \( R \), \( x_m \) and \( L \) were measured directly, while parameters \( n \) and \( h \) were determined from least square fitting. We see that increasing the etching time results in the increase of the pore radii \( r \) and \( R \), and parameter \( h \), while the pore tip length \( x_m \) and the parameters characterizing the pore shape, \( x_m/h \) and \( n \), decrease with the etching time and approach the limit \( x_m/h \to 0 \) and \( n \to 1 \), corresponding to the conical pore.

**Table 3** Geometrical parameters characterizing the reconstructed profiles of asymmetrical pores obtained with U ions at the etching times indicated.

<table>
<thead>
<tr>
<th>Etching time</th>
<th>( r ) (nm)</th>
<th>( R ) (nm)</th>
<th>( L ) (nm)</th>
<th>( x_m ) (nm)</th>
<th>( h ) (nm)</th>
<th>( x_m/h )</th>
<th>( n )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( t_b + 2 ) min</td>
<td>4.5</td>
<td>466</td>
<td>11560</td>
<td>2375</td>
<td>2790</td>
<td>0.85</td>
<td>1.53</td>
</tr>
<tr>
<td>( t_b + 5 ) min</td>
<td>9.0</td>
<td>475</td>
<td>11543</td>
<td>2133</td>
<td>3203</td>
<td>0.67</td>
<td>1.31</td>
</tr>
<tr>
<td>( t_b + 8 ) min</td>
<td>16</td>
<td>484</td>
<td>11526</td>
<td>1891</td>
<td>4374</td>
<td>0.43</td>
<td>1.14</td>
</tr>
<tr>
<td>( t_b + 12 ) min</td>
<td>29</td>
<td>496</td>
<td>11504</td>
<td>1569</td>
<td>6127</td>
<td>0.26</td>
<td>1.05</td>
</tr>
</tbody>
</table>

**Modeling of ion transport in funnel-shaped pores**

Figs. 7-9 show the calculated current vs. voltage (\( I-V \)) and rectification ratio (defined as \( |I(V)/I(-V)| \)) vs. electrolyte concentration for the asymmetric pores, based on the reconstructed profiles characterized in Tables 2 and 3. The simulations have been performed using a Poisson-Nernst-Planck (PNP) model developed previously. Although this model was originally proposed for conical nanopores, it has been applied successfully to pores with a variety of shapes and fixed charge distributions, and constitutes a standard tool for the characterization of the ionic transport through long and narrow pores, such as those produced in organic polymers by track-etching. In spite of the nanoscale nature of the pore radii, this continuum electrostatics model can explain most of the transport phenomena observed because the nanopore diameters are larger than the Debye length in the range of electrolyte concentrations used in the experiments. All calculations have been performed assuming that the pores separated two identical KCl solutions. We have also considered the (infinite dilution)
The $I-V$ curves of the pores with the reconstructed profiles in Figure 6 are presented in Fig. 7a. All curves show rectification of the electric current, with a high conducting state for positive applied voltages, in which the current enters the pore through the narrow opening, and a low conducting state for negative applied voltages, in which the current enters the pore through the wide opening. We see also that, at a given voltage, the current increases with decreasing atomic number of the track forming ion, as a result of the increasing radius of the wide opening with decreasing $dE/dx$. Fig. 7b shows the rectification ratio at $V = 1$ V. For the sake of clarity, only the curves for pores obtained with U and Fe ions have been plotted. In spite of the different $I-V$ curves shown in Figure 7a, the rectification ratio vs. KCl concentration $c$ curves obtained through the pores are very similar for the four reconstructed profiles, showing a maximum value around $c \approx 0.1$ M. The maximum value increases slightly with decreasing $dE/dx$, due to the increase in the pore angle at the region of the pore tip. In accordance with this result, previous experiments on PET samples irradiated by different single heavy ions have not revealed any explicit relationship between the type of bombarding ion and the diode-like properties of the asymmetrical pores fabricated by one-sided etching.

As discussed in the introduction, experimentalists who use conical pores frequently employ SEM techniques to estimate the base radius of the pores, and use eqn. (1) to calculate the radius of the pore tip. This procedure can lead to severe errors if the pore geometry deviates from the conical shape, as illustrated in Figs. 8 and 9. The continuous curves of Fig. 8a correspond to the $I-V$ curves of the funnel-shaped pore produced by the tracks of U ions at etching time $t = t_0 + 2$ min, and the dashed curves represent the $I-V$ curves of the equivalent conical pore with the same surface charge concentration, base radius and conductance at $V = 0.1$ V and $c = 1$ M KCl. The curves are parametrical in the electrolyte concentration. At this etching time, the radius of the pore tip of the equivalent conical nanopore is $r \approx 2.2$ nm, which deviates significantly from the value $r = 4.5$ nm found for the tip of the funnel. We see that the equivalent conical pore overestimates the electric currents obtained assuming the reconstructed profile at the three KCl concentrations analyzed. This is also the case for the rectification ratio vs. KCl concentration curves, shown in Fig. 8b. Again, the rectification ratios corresponding to the equivalent conical pore are significantly higher than those obtained assuming the reconstructed profile, due to the reduction of the tip radius in the case of the equivalent conical pore. We also find also significant differences in the concentration where the maximum value is attained: $c \approx 0.1$ M in the case of the pore with the reconstructed profile and $c \approx 0.2$ M for the equivalent conical pore.

![Fig. 7](image7.png)

*(a) Calculated $I-V$ and (b) rectification ratio vs. KCl concentration curves for asymmetrical pores etched for 2 minutes after breakthrough. Profiles are obtained from single U, Au, Xe and Fe ion tracks.

![Fig. 8](image8.png)

*(a) Calculated $I-V$ and (b) rectification ratio vs. KCl concentration curves for asymmetrical pores etched for 2 minutes after breakthrough from single U ion tracks (continuous lines) and equivalent conical pores with the same surface charge concentration, pore base radius, and electrical conductance at 100 mV (dotted lines). The curves are parametrical in the KCl concentration.*
Fig. 9 illustrates how, with increasing etching time, the properties of the pores with reconstructed profiles approach those of the equivalent conical pores. We have considered again the case of the pores obtained with U ions and the shape described by the parameters summarized in Table 3. Fig. 9a shows the I-V curves of the pores with the reconstructed profile (continuous lines), and the I-V curves of the equivalent conical pores (dashed lines). The curves are parametric in the etching time. The calculated pore tip radii of the equivalent conical pores at the different etching times are $r = 2.2$ nm ($t = t_b + 2$ min), 9 nm ($t = t_b + 5$ min), 16 nm ($t = t_b + 8$ min), and 29 nm ($t = t_b + 12$ min). Therefore, the estimation of the pore tip radius using the conical pore assumption equals that of the reconstructed profile at $t = t_b + 5$ min, and the calculated I-V curves using the two models practically coincide above this etching time. The rectification ratio vs. concentration curves of Fig. 9b show greater differences between the two models because the rectification ratio is very sensitive to small differences in the I-V curves. Nevertheless, the curves corresponding to the equivalent conical pores match those of the reconstructed profile at etching times higher than $t_b + 8$ min.

The exact determination of nanopore size and shape is a challenge associated with numerous potential applications of nanopore-based devices. Very often, the nanopores are employed in electrolyte solutions, and the electrical conductance is taken to be a measure of the nanopore dimensions. However, the shape of the pore cannot be determined solely from conductance measurements in the absence of any additional information or reasonable presumptions. In the present work, we applied a previously introduced method for the characterization of so-called conical track-etched pores. The method includes conductance measurements performed during the chemical etching of an ion-irradiated foil. The analysis of conductance vs. time, in combination with the time dependence of the pore size on the foil surface, made it possible to determine the whole longitudinal profile of the pore. The implied presumptions are (a) the pore etches symmetrically from both sides; (b) the etching front subsequently reproduces itself when moving along the track axis; and (c) the specific conductivity of the etching solution in the pore is equal to the bulk value. The symmetry was ensured in our experiments by the use of bombarding ions (U, Au, Fe), the kinetic energy of which was high enough so that the energy loss was nearly constant in the 12-µm-thick foils (see Table 1). The only exception was the Xe ion with an energy of 1.2 MeV/u: its energy loss was reduced by 27% as the ion passed through the foil. Nevertheless, this has lead to only a slight asymmetry. As seen in Figure 5a, the constriction is shifted, relative to the center plane of the foil, by a distance of 0.5-1 µm. For all the other ions, the etched pores were symmetrical. As to points (b) and (c), these conditions are fulfilled as long as the concentration of etchant in the pore is constant. A very high concentration of electrolyte suggests that the effect of surface charge on the specific conductivity in the pores is negligible. We also performed etching experiments at sufficiently different temperatures to show that the process was not diffusion-limited, ensuring a homogeneous distribution of etchant concentration in the pores. Note that this is not the case when the etch solution contains surfactant, the adsorption front of which moves slower than the alkali ions diffusing into the pores. Therefore, the reconstruction algorithm is not applicable to surfactant-controlled track etching. It should be mentioned that the surfactant-controlled etching provides another interesting geometry, namely, spindle-shaped pores.

The presence of two nanoscale-sized pore mouths, which can be functionalized individually, opens the door to a wide variety of nanofluidic circuits. Compared to the double-cone geometry, the situation is opposite, with the small radius at pore ends, and the large radius in the pore middle. In this case the SEM technique seems to be the only reliable method to determine the pore geometry while the etching conductometric measurements can serve for a rough estimate of the inside pore radius. The information hidden in the $G(t)$ function cannot be extracted to provide quantitative determination of the pore axial profile until significant progress is made in the understanding of the diffusion, adsorption and surface protection effect of surfactant in narrow channels.

The long-standing question about the fluctuating and voltage-gated behavior of asymmetrical pores with apparent small radii of a few nanometers remains open, though new experimental findings provide credible explanations. The analysis of the conductometric data for ion tracks with a relatively low track-to-bulk etch rate ratio suggests that the extremely narrow, unstable pores in PET may contain parts that have not been etched out completely. This hypothesis has been made before; electrical conductivity studies of under-etched ion tracks in polymers seem to support this point of view. Another relevant problem is the specific conductivity in channels as narrow as 1-2 nm, which has been reported to be different from the bulk value even for highly concentrated solutions.
Conclusions and outlook

The accurate reconstruction of the pore shape, with the focus on the tip region, shows that the asymmetrical pores produced by one-sided etching have a larger critical radius and a longer narrow part than previously thought. This finding should be taken into account when studying ion and molecule transport processes, the application of nanopores in resistive-pulse sensing and in other cases. Such important parameters as electrical field, dwell time, and ionic selectivity critically depend on the pore constriction geometry. An example is the modeling of photo-triggered and pH-tunable membranes, which has been refined with the use of the corrected nanopore shape.\textsuperscript{38} The calculations performed in the present paper show that the ion current rectification properties of funnel-shaped pores significantly differ from those of conical pores, provided the tip radius is smaller than ~10 nm. For larger tip radii, i.e., when the pore is subjected to additional two-sided etching after breakthrough, the ion transport properties of these two pore configurations become almost indistinguishable.

Based on the data for two-sided (symmetrical) track etching, we reconstructed the pore profiles for one-sided etching. We assumed that contact of the opposite side of the foil with a stop-etch solution did not affect the tip shape, as long as the etchant had not broken through the foil. Strictly speaking, this is in actuality not true. The neutralizing agent can diffuse along the latent track and change, at least slightly, the etching conditions in the tip region.\textsuperscript{31} In this context, the development of a method for estimating the geometry of the asymmetrical nanopore, exactly as it is after fabrication, would be of considerable importance.

Recently, new approaches to the quantitative characterization of nanopores drilled in thin inorganic films have been suggested.\textsuperscript{59-61} The dependence of nanopore conductance on ionic strength, in combination with selective surface functionalization, can be used to accurately determine the nanopore shape and size. Application of this concept to asymmetrical track-etched pores could be the next step towards comprehensive knowledge of their geometry.

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