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The Angular Overlap Model extended for two-open-shell f and d electrons

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We discuss the applicability of Angular Overlap Model (AOM) to evaluate the electronic structure of lanthanide compounds, which are currently the subject of incredible interest in the field of luminescent materials. The functioning of phosphors is well established by the f-d transitions, which requires the investigation of both the ground $4f^n$ and excited $4f^{n-1}5d^1$ electron configurations of the lanthanides. The computational approach to the problem is based on the effective Hamiltonian adjusted from ligand field theory, but not restricted to it. The AOM parameterization implies chemical bonding concept. Focusing our interest on this interaction, we take the advants offered by modern computational tools to extract AOM parameters, which ensure the transparency of the theoretical determination and convey chemical intuitiveness of the non-empirical results. The given model contributes to the understanding of lanthanides in modern phosphors with high or low site symmetry and presents a non-empirical approach using less sophisticated computational procedure for the rather complex problem of ligand field of both 4f and 5d open shells.

Introduction

Before entering the central issues of our computational and modelling approach we mention several topics where the simulation is important as property engineering tool. The functioning of phosphor-converted-light-emitting-diodes (pc-LEDs) deserves strong interest since the ban on incandescent light bulbs. At the first stage of the development of LEDs, white light is produced by lanthanide Ce^{3+} doped inorganic phosphors,¹ taking advantages of the strong dipole allowed f-d transitions in Ce^{3+} . Given the limit of the trial-and-error experiments of new phosphors synthesis, the future of our domestic lighting relies also on the theoretical modelling. The theoretical modelling gives prospect of the optical manifestations of the phosphors together with a reliable understanding of their microscopic origin. *Ergo*, it contributes to the design of modern phosphors. Attention is particularly paid to the optical properties of the lanthanides ions Pr^{3+} or Eu^{2+} especially as activator for warm-white light source.²⁻⁴ The theoretical modelling of such phosphors is not free of puzzling technical concerns. Numerous works related not only to the gigantic size-problem encountered,⁵ like in the case of Eu^{2+} , but also the non-negligible issues due to low symmetry constrain.⁶⁻⁸ We mention also the situation of non-aufbau occupation⁹⁻¹² of the 4f orbitals inasmuch as convergence problems may frequently occur in the self-consistent field (SCF). The calculation of the f - d transitions in lanthanide phosphors is

addressed with respect to the ligand field theory^{13,14} but not restricted its classical empirical frame.¹⁵ The model Hamiltonian is parameterized in terms of few quantities such as the Slater-Condon parameters, the spin-orbit coupling constants and the ligand field potential. The Slater-Condon parameters represent the many electron interaction in the Hamiltonian, while the spin-orbit coupling and ligand field potential account to the one-electron part. The task of computational approach consists in the determination of these parameters in a non-empirical way.¹⁶⁻²⁰ Therefore, we do not aim in this paper to describe the electrostatic interaction part of the Hamiltonian, *i.e.* the Slater-Condon parameters relevant for multi-electron problem, for which our theoretical model has been already improved¹⁹ and revised²¹ in previous works. The calculation of the spin-orbit coupling is placed in the growing efforts devoted nowadays to the relativistic quantum chemistry tools.²²⁻²⁵

On the other hand, the formulation of the one-electron ligand field interaction may partly confusing since effective two-electron components may effectively participate to the parameters. A simple representation of the ligand field interaction is obtained by the perturbation approach of the one-electron wave function of the lanthanide ion ($|l, ml\rangle$). Within this approach the actual system of two-open-shell f and d electrons has a ligand field Hamiltonian, which is constructed in the basis of the merged 4f ($l=3$) and 5d ($l=2$) orbitals of the lanthanide ion, *i.e.* seven plus five $|l, ml\rangle$ functions (see Fig. 1).

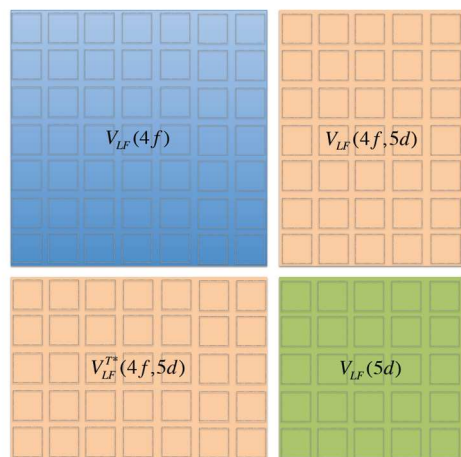


Fig. 1 Schematic representation of the ligand field matrix V_{LF} corresponding to the merged 4f and 5d orbitals in the problem of two-open-shell 4f and 5d electrons.

Dorenbos²⁶ has taken the relative simplicity of this representation (Fig. 1), and the related eigenvalues, to create a model widely applied in some empirical-to-semi-empirical studies. One can recognize from Fig. 1 the shape of the actual ligand field Hamiltonian, where diagonal sub-blocks of 7 by 7 ($V_{LF}(4f)$) and 5 by 5 elements ($V_{LF}(5d)$) are a direct perturbation of the 4f and 5d orbitals of the lanthanide ion. A off-diagonal sub-block of 7 by 5 elements is also present. This $V_{LF}(4f, 5d)$ block matrix is a perturbation in a second order, whose presence is governed by basic group theory rules, *i.e.* $V_{LF}(4f, 5d)$ vanishes if the local symmetry of the lanthanide coordination exhibits inversion center. Without going into details since the theory has been already described in different textbooks,^{27,28} Wybourne has defined the ligand field potential as a linear combination of spherical harmonics $Y_{k,q}$ up to a given order. Accordingly, a general expansion expression of each sub-block in Fig. 1 is presented in Eq. 1.

$$V_{LF}(4f) = \sum_{k=0,2,4,6} \sum_{q=-k}^k B_q^k(4f) C_q^{(k)}, \quad (1a)$$

$$V_{LF}(5d) = \sum_{k=0,2,4} \sum_{q=-k}^k B_q^k(5d) C_q^{(k)}, \quad (1b)$$

$$V_{LF}(4f, 5d) = \sum_{k=1,3,5} \sum_{q=-k}^k B_q^k(4f, 5d) C_q^{(k)}, \quad (1c)$$

where $C_q^{(k)}$ are the solid spherical harmonic tensor operators (Eq. 2) and B_q^k 's are the Wybourne-normalized crystal field parameters.

$$C_q^{(k)} = \sqrt{\frac{4\pi}{2k+1}} Y_{k,q} \quad (2)$$

Analogous representations related by simple convention factors with the above formalism also exist *e.g.* following the definition of $A_{k,q}$'s given by Stevens^{27,29} for instance. However the main idea of the representation in Eq. 1 is the treatment of the interaction having an electrostatic origin, avoiding any overlap between the 4f and 5d orbitals of the lanthanide ion with the ligands. The Eqs. 1 resemble the initial electrostatic form of crystal field theory³⁰ but the parameters tacitly incorporate other contributions to the metal-ligand bonding. A formal drawback of spherical Harmonics expansion is that the total Hamiltonian cannot be formulated as the sum of contributions Eq. 1a + Eq. 1b + Eq. 1c but must conceive separate operators for the 4f and 5d blocks. This is because we cannot prevent a given $C_q^{(k)}$ (with $k \leq 4$) from the Eq. 1a (4f block) to interact with the spherical harmonics with appropriate symmetry originating from the 5d block. This would make the 5d ($B_q^k(5d)$) parameters identical with the $k \leq 4$ subset of the 4f ones. However this formal drawback is tacitly neglected, considering directly the parameterized blocks instead of a primordial common Hamiltonian. A part of such conceptual drawbacks is circumvented working with models explicitly based on different type of bonding effects, as it is the case of Angular Overlap Model (AOM).

In this paper, we extend the traditional concept of the AOM designed by Schäffer and Jørgensen³¹ and Urland³² for single-open-shell d and f electrons, respectively, to tackle the actual ligand field potential for two-open-shell f and d electrons necessary for the reliable understanding of the f-d transitions in lanthanide phosphors. We use the advances of our previously developed Ligand Field Density Functional Theory (LFDFT)¹⁹ method extending it to the f-d transitions. We take the advantages given by the AOM formalism to reconsider more explicitly the ligand field interaction in the LFDFT Hamiltonian to provide general information about the chemistry of the interaction between the lanthanide ion and the ligands. This outline treatment due to AOM implies chemical intuitiveness and allows validation of the theoretical work.

Theory

In our conceptual formulation of the ligand field theory into Density Functional Theory (DFT),¹⁶⁻²⁰ LFDFT presents an effective Hamiltonian, which acts only in the subspace of the microstates originating from the ground $4f^n$ and excited $4f^{n-1}5d^1$ electron configurations of the lanthanide ion subject to perturbations due to 1/ electrostatic interaction inter-electron repulsion, 2/ spin-orbit coupling interaction and 3/ ligand field interaction from the chemical environment. Every interaction is parameterized according to the LFDFT methodology in the way given detailed in ref. 19. Considering especially the ligand field interaction, its representation as shown in Eq. 1 yields 28 $B_q^k(4f)$, 15 $B_q^k(5d)$ and 21 $B_q^k(4f, 5d)$ parameters (altogether, 64 parameters), where most of them may vanish due to symmetry. For instance within the octahedral ligand field, like in the case of Pr^{3+} doped into the trivalent site of the Cs_2KYF_6 crystallizing in the elpasolite structure type,¹⁹ the ligand field potential (Eq. 1) reduces to the following scheme (Eq. 3):

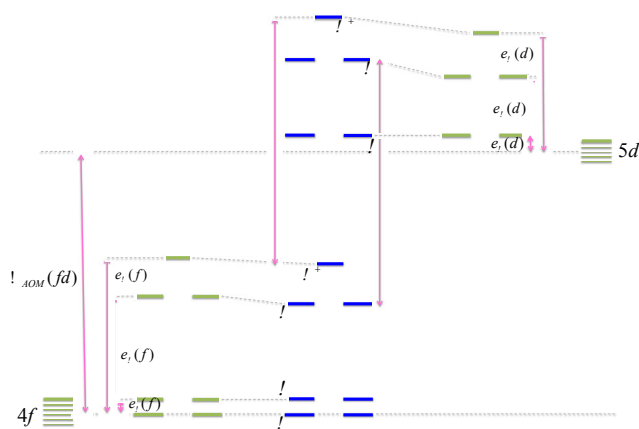


Fig. 2 Representation of the AOM parameters adjusted from the interaction of a lanthanide ion with one ligand. The first order energy splitting of the 4f and 5d orbitals is presented in green and the second order energy splitting in blue.

$$V_{LF}(4f) = B_0^4(4f) \left[C_0^{(4)} + \sqrt{\frac{5}{14}} (C_4^{(4)} + C_{-4}^{(4)}) \right] + B_0^6(4f) \left[C_0^{(6)} - \sqrt{\frac{7}{2}} (C_4^{(6)} + C_{-4}^{(6)}) \right] \quad (3a)$$

$$V_{LF}(5d) = B_0^4(5d) \left[C_0^{(4)} + \sqrt{\frac{5}{14}} (C_4^{(4)} + C_{-4}^{(4)}) \right] \quad (3b)$$

$$V_{LF}(4f, 5d) = 0 \quad (3c)$$

In fact only the parameters $B_0^4(4f)$, $B_0^6(4f)$ and $B_0^4(5d)$ are symmetry independent in O_h ligand field, since $B_4^4(4f)$, $B_4^6(4f)$ and $B_4^4(5d)$ can be defined in terms of the previous ones (Eqs. 3). Because we are often confronting with low site symmetry of the lanthanide coordination obtained from the experimental synthesis of modern phosphors,³³⁻³⁵ the tractability of the Wybourne-normalized crystal field parameters is cumbersome, while the AOM representation seems to be more adequate. The theory of AOM has been already described and reviewed³⁶ for d-³¹ and f-electrons,³² respectively. Hereafter, we are just giving a short description of the model if extended for two-open-shell f and d electrons.

In the AOM formalism, each ligand is assigned with parameters e_σ , e_π , e_δ and e_ϕ classified according to its overlap with the lanthanide ion to give a $\tilde{\sigma}$, $\tilde{\pi}$, $\tilde{\delta}$ and $\tilde{\phi}$ bond, respectively. In Figure 2, we present the AOM parameters in their original definitions, *i.e.* interaction between a lanthanide ion and a ligand within $C_{\infty v}$ symmetry. Chemical bonding up to $\tilde{\delta}$ and $\tilde{\phi}$ bond is rarely reached by the ligand orbitals, allowing us to neglect by convenience the effect of e_δ and e_ϕ in the representation given in Fig. 2 either for the 4f or the 5d energy splitting. The definition of the parameter $\Delta_{AOM}(fd)$ (Fig. 2) is connected to the $\Delta(fd)$, which is already discussed in refs. 19 and 21. This parameter represents the energy shift of the 5d orbitals with respect to the 4f ones (Fig. 2). In cases with more than one electrons it cannot be discriminated in the spectral terms from a gap due to the the

Slater-Condon $F_0(ff)$ and $F_0(fd)$ parameters. Thus for the Pr3+ complexes^{19, 21} taken as examples in the following, we obtain:

$$\Delta(fd) = F_0(fd) - F_0(ff) + B_0^0(5d) - B_0^0(4f) \quad (4a)$$

where, the one-electron ligand field interaction intervenes in Eq. 4a in a spherical average $B_0^0(4f)$ and $B_0^0(5d)$.

Hence the ligand field potential according to Eq. 1 becomes a traceless block without $\Delta(fd)$ in line with the Wybourne formalism,^{27,28} which is not the case in the formalism of AOM.^{31,32} The mapping between both formalisms is obtained by adjusting the trace of the ligand field matrix obtained in the AOM with $\Delta_{AOM}(fd)$ (Eq. 4b).

$$\Delta_{AOM}(fd) = \Delta(fd) + \frac{1}{7} \text{Trace}(\langle 3 | V_{LF} | 3 \rangle) - \frac{1}{5} \text{Trace}(\langle 2 | V_{LF} | 2 \rangle) \quad (4b)$$

This $\Delta_{AOM}(fd)$ parameter will appear in the diagonal element of the $V_{LF}(5d)$ block matrix. Within the first order approximation for a given ligand donor, we define $e_\sigma(f)$, $e_\pi(f)$ and $e_\pi(d)$ parameters in line with the AOM formalism. Taking however the inclusion of a second order perturbation, each ligand donor obtains a novel set of AOM parameters. We define $e_\sigma(fd)$ and $e_\pi(fd)$ as it is represented Fig. 2. Anisotropy in the $\tilde{\pi}$ interaction allows to distinguish between $e_{\pi,x}$ and $e_{\pi,y}$ in the definition of the AOM parameters.^{31,32} Therefore the general matrix element V_{LF} corresponding to the covalent interaction of both the 4f and 5d orbitals with the ligands is developed (Eq. 5), following the earlier approach of single-open-shell d electrons by Schäffer and Jørgensen³¹ and f electrons by Urland.³²

$$\langle 3, \mu | V_{LF} | 3, \nu \rangle = \sum_{k=1}^{\text{ligands}} \sum_{\lambda=\sigma,\pi} D_{\mu\lambda}^{4f}(k) D_{\nu\lambda}^{4f}(k) e_{\lambda,k}(f) \quad (5a)$$

$$\langle 2, \mu | V_{LF} | 2, \nu \rangle = \sum_{k=1}^{\text{ligands}} \sum_{\lambda=\sigma,\pi} D_{\mu\lambda}^{5d}(k) D_{\nu\lambda}^{5d}(k) e_{\lambda,k}(d) \quad (5b)$$

$$\langle 3, \mu | V_{LF} | 2, \nu \rangle = \sum_{k=1}^{\text{ligands}} \sum_{\lambda=\sigma,\pi} D_{\mu\lambda}^{4f}(k) D_{\nu\lambda}^{5d}(k) e_{\lambda,k}(fd) \quad (5c)$$

where D^{4f} and D^{5d} are the matrix elements defined in terms of the Euler angles (Wigner's Darstellungsmatrizen) or direction cosines already described in refs. 31 and 32, respectively, and k is the running index for the ligand system. The eigenvalues of the V_{LF} matrix in the way it is calculated from Eq. 5 can be determined analytically for the interaction between a lanthanide ion and a ligand within $C_{\infty v}$ symmetry (Fig. 2). These eigenvalues are presented in Eq. 6 and Eq. 7, respectively, for the perturbation of the 4f and 5d orbitals.

$$\langle 3, \lambda | V_{LF} | 3, \lambda \rangle = \frac{1}{2} (\Delta_{AOM}(fd) + e_\lambda(d) + e_\lambda(f)) - \frac{1}{2} \sqrt{(\Delta_{AOM}(fd) + e_\lambda(d) - e_\lambda(f))^2 + 4e_\lambda^2(fd)} \quad (6)$$

$$\langle 2, \lambda | V_{LF} | 2, \lambda \rangle = \frac{1}{2} (\Delta_{AOM}(fd) + e_\lambda(d) + e_\lambda(f)) + \frac{1}{2} \sqrt{(\Delta_{AOM}(fd) + e_\lambda(d) - e_\lambda(f))^2 + 4e_\lambda^2(fd)} \quad (7)$$

where, $\lambda = \sigma, \pi x$ and πy .

One can see that the mixed parameters $e_\sigma(fd)$ and $e_\pi(fd)$ have to be small without impinging on the first order AOM parameters. The absence of them leads to the formulation of the eigenvalues (Eq. 6 and Eq. 7) in their original representations given in refs. 31 and 32, respectively. We map the ligand field matrix obtained from the LFDFT calculation with Eq. 5 in order to extract AOM parameters ($e_\sigma(f)$, $e_\pi(f)$, $e_\sigma(d)$, $e_\pi(d)$, $e_\sigma(fd)$, $e_\pi(fd)$ and $\Delta_{AOM}(fd)$) in their definitions described in this section. The presented model is applied next for the calculation of the electronic structure of eightfold coordinated trivalent Pr^{3+} complexes: $(\text{PrX}_8)^{5-}$, with $\text{X} = \text{F}^-$, Cl^- and Br^- having an arrangement either with D_{4h} and D_{4d} symmetry, respectively.

Computational Details

The DFT calculations reported in this paper have been carried out by means of the Amsterdam Density Functional (ADF2010) program package.³⁷⁻³⁹ The local density approximation (LDA) functional based on the Vosko-Wilk-Nussair (VWN)⁴⁰ parameterization has been used for geometry consideration. The LFDFT calculation has been performed using DFT calculation based on the hybrid B3LYP functional as it is implemented in the ADF program package³⁷⁻³⁹ for the exchange and correlation energy and potential. Positive point charges are added to neutralize the highly negative charged structure using the *Efield* keyword available in the ADF program package.³⁷⁻³⁹ The molecular orbitals were expanded using a triple- ζ STO basis sets plus two polarization functions (TZ2P+) for the Pr atom and plus one polarization function (TZP) for the halogen atoms, *i.e.* F, Cl and Br. The LFDFT calculation were achieved following the detailed procedure already described in ref. 19 where the most important step consists to the representation of the density in a totally symmetric form using the approach of the Average of Calculation (AOC)⁴¹ type calculation. The 12 by 12 ligand field matrix (in the same shape as it is presented in Fig. 1) being the representative of the ligand field potential was extracted for the purpose of this work. Matlab/Octave codes for the LFDFT program together with the determination of the AOM and the Wybourne-normalized crystal field parameters from the ligand field matrix are available from the authors upon request. The structures of the theoretical complex $(\text{PrX}_8)^{5-}$, with $\text{X} = \text{F}^-$, Cl^- and Br^- were obtained from the DFT geometry optimization of the cluster $(\text{PrX}_8\text{Na}_8)^{3+}$, with $\text{X} = \text{F}^-$, Cl^- and Br^- . The geometry of this cluster was optimized while the electronic structure was confined to have the AOC occupation of the 4f orbitals of the Pr^{3+} center and the symmetry was constrained to have the arrangement of either the D_{4h} or the D_{4d} symmetry.

Results and Discussion

Pr^{3+} with eight ligands in its coordination sphere is commonly met in inorganic coordination complexes and solid state compounds. In the field of luminescent materials, Pr^{3+} has been doped into various fluoride host lattices such as NaYF_4 ,⁴² CaF_2 or LiYF_4 ,⁴³ *etc.* resulting in eight coordination, in order to

investigate the possibility of quantum cutting process in the optical behavior.⁴³ If doped into the CaF_2 host lattice or the α -cubic phase of NaYF_4 ,⁴² the eight coordination is typically found having a cubic arrangement (O_h point group), which might always be subjected to a slight distortion to D_{4h} symmetry. The occurrence of a D_{4d} arrangement of the eight ligands is not usual in solid state compounds, to the best of our knowledge, although it exists in inorganic coordination complexes whose properties are well recognized in the topic of magnetic anisotropy, being important in single ion magnets.^{44,45} In the application of our AOM extended for two-open-shell f and d electrons, we consider here as theoretical example $(\text{PrX}_8)^{5-}$, with $\text{X} = \text{F}^-$, Cl^- and Br^- , having an arrangement of the D_{4h} or the D_{4d} point group, insofar as the eight ligands are identical and equivalent by symmetry (Fig. 3).

The structures of the eightfold coordinated Pr^{3+} are calculated while the optimization of the geometry is confined within the desired symmetry, *i.e.* dependent of few parameters such as the Pr^{3+} -ligand bond length d and the polar angle θ in spherical coordinates. The azimuthal angle φ are fixed for each of the eight ligands in the arrangement with either D_{4h} or D_{4d} symmetry. We present in Table 1 these spherical coordinates deduced from the optimized structures. The optimized structures in question are calculated as clusters, being representative only in semiquantitative sense, since the full lattice effects are idealized by compensating charges. Accordingly, the theoretical structures (Table 1) might not represent a global minimum of the energy in the adiabatic potential energy surface validated by frequency analysis of all the normal modes.

The optimization of the geometry, if confined to the D_{4h} symmetry under the present computational details, leads to a nearly cubic arrangement (O_h point group) of the eight ligands (Table 1). The bond lengths determined for both structures having D_{4h} and D_{4d} symmetry (Table 1) are in agreement with the Shannon radii⁴⁶ of Pr^{3+} and the ligand ions in such an eight coordination. The D_{4h} ligand field splits the 4f and 5d orbitals of Pr^{3+} into a_{2u} , b_{1u} , b_{2u} , $2e_u$ and a_{1g} , b_{1g} , b_{2g} , e_g (*cf.* Fig. 4), respectively, representative of the irreducible representations (*irreps*) of the D_{4h} point group. These representations can be separately discriminated using the inversion center symmetry operator since the 4f and 5d possess opposite parity in D_{4h} . This particular situation allows no mixing of the two-open-shell 4f and 5d electrons in the investigation of the $4f^15d^1$ electron configuration of Pr^{3+} , *i.e.* the $V_{LF}(4f,5d)$ block matrix has strictly zero elements. On the other hand, the D_{4d} ligand field splits the 4f and 5d orbitals into b_2 , e_1 , e_2 , e_3 and a_1 , e_2 , e_3 *irreps* (*cf.* Fig. 4), respectively. It is obviously seen that the e_2 as well as the e_3 *irreps* allow mixing of some 4f and 5d $|l, m\rangle$ functions. This situation therefore leads us to consider more explicitly the off-diagonal elements of the V_{LF} matrix, being parameterized by the mixed AOM $e_\sigma(fd)$ and $e_\pi(fd)$ parameters.

There are other circumstances under which the elements of the $V_{LF}(4f,5d)$ block matrix may be significant, being therefore important in the analysis of the luminescence of lanthanide phosphors. So for example when Pr^{3+} is doped into $\text{Y}_3\text{Al}_5\text{O}_{12}$ ¹⁵ or LiYF_4 ^{43,47,48} having a local symmetry of D_{2d} and S_4 , respectively, or the frequently occurred C_1 ligand field in $\text{YF}_3\text{:Pr}^{3+}$,^{49,50} for instance.

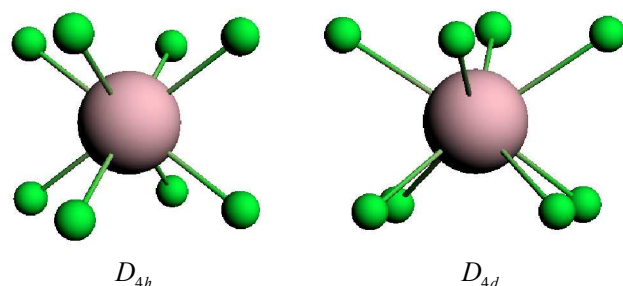


Fig. 3 Spatial representations of the structure of $(\text{PrX}_8)^{5-}$ ($\text{X} = \text{F}^-, \text{Cl}^-, \text{Br}^-$) with D_{4h} (left hand side) and D_{4d} (right hand side) arrangements.

Table 1 DFT calculated geometries of $(\text{PrX}_8)^{5-}$ ($\text{X} = \text{F}^-, \text{Cl}^-, \text{Br}^-$): Pr^{3+} -X bond length d in Å and the polar coordinate θ in ° of one ligand X from which the rest of the ligand coordinates is generated by symmetry.

	D_{4h}		D_{4d}	
	\square	θ	d	θ
$(\text{PrF}_8)^{5-}$	2.372	54.75	2.368	56.95
$(\text{PrCl}_8)^{5-}$	2.853	54.78	2.825	57.91
$(\text{PrBr}_8)^{5-}$	3.007	54.74	2.973	58.34

The AOM extended for two-open-shell f and d electrons provides: both a perturbation correction of the ligand field potential for the 4f and 5d open-shells, and an additional mechanism that has to affect the multiplet energy levels and more importantly their intensities. A graphical representation of the energy splitting pattern of the 4f and 5d orbitals of Pr^{3+} together with the molecular orbital diagram is shown in Fig. 4 considering the $4f^1 5d^1$ electron configuration, in both arrangements of D_{4h} and D_{4d} symmetry, respectively.

Taking the structures given in Table 1 as input, we perform the LFDFT calculation and extract the ligand field potential on which we focus our interest. The Slater-Condon parameters are also obtained from the LFDFT calculation and presented in Table 2.

We use the procedure as it is described in ref. 21, using the radial functions of the 4f and 5d Kohn-Sham orbitals of Pr^{3+} to extract the Slater-Condon parameters. These radial functions are graphically presented in Fig. 5 considering the free Pr^{3+} ion and its complex with eight fluoride, chloride and bromide ligands forming a D_{4h} arrangement. Since the Slater-Condon parameters are not treated prior to the ligand field potential in this paper, we present them in Table 2 as average between the quantities obtained for the D_{4h} and D_{4d} arrangements of $(\text{PrX}_8)^{5-}$, with $\text{X} = \text{F}^-, \text{Cl}^-, \text{Br}^-$. It is noteworthy that the parameters (Table 2) are not strongly sensitive to the change of the spatial arrangement of the eight ligands around Pr^{3+} . The quantities given in Table 2 are in the magnitude of known experimental fitted parameters.⁵¹ The Slater-Condon parameters $G_1(fd)$, $F_2(fd)$, $G_3(fd)$, $F_4(fd)$, and $G_5(fd)$ appropriate to the splitting of terms sharing the $4f^1 5d^1$ electron configuration parentage diminish in the series F^-, Cl^- and

Br^- ligands, in line with the increasing of the nephelauxetic effect obtained for the same series of ligands. The nephelauxetic effect denominates an expansion of the electron cloud as it is presented in Figure 5. The radial function of the 5d Kohn-Sham orbital, but also the 4f one although the effect is weaker, is expanded toward the ligands. This expansion is weak in case of the 5d in $(\text{PrF}_8)^{5-}$ but becomes stronger for chloride and bromide systems. However in the same series of ligands, the $F_2(ff)$, $F_4(ff)$, and $F_6(ff)$ parameters ($4f^2$ electron configuration) are almost invariant showing the relative shielding of the 4f orbitals by the outer shells in contrary to the 5d ones (cf. Figure 5). The spin-orbit coupling constants ζ_{4f} and ζ_{5d} are also calculated using the approach of ZORA relativistic available in the ADF program package,³⁷⁻³⁹ where we obtain (in cm^{-1}) 760 and 945, respectively. The AOM parameters are calculated by mapping the matrix elements of V_{LF} given by Eq. 5 to the ligand field potential obtained by the LFDFT procedure. These quantities are presented in Table 3, where only one set of the AOM parameters appears since the eight ligands are identical and equivalent by symmetry in the structures being investigated. Although the Pr^{3+} -ligand bond lengths obtained in the DFT optimization of the D_{4h} structures are slightly elongated if compared to the D_{4d} ones (cf. Table 1), we expect no significant changes of the AOM parameters as depicted in Table 3. The difference between the D_{4h} and D_{4d} ligand field potentials is essentially made by the mixed AOM parameters $e_\sigma(fd)$ and $e_\pi(fd)$ in the $V_{LF}(4f, 5d)$ block matrix elements.

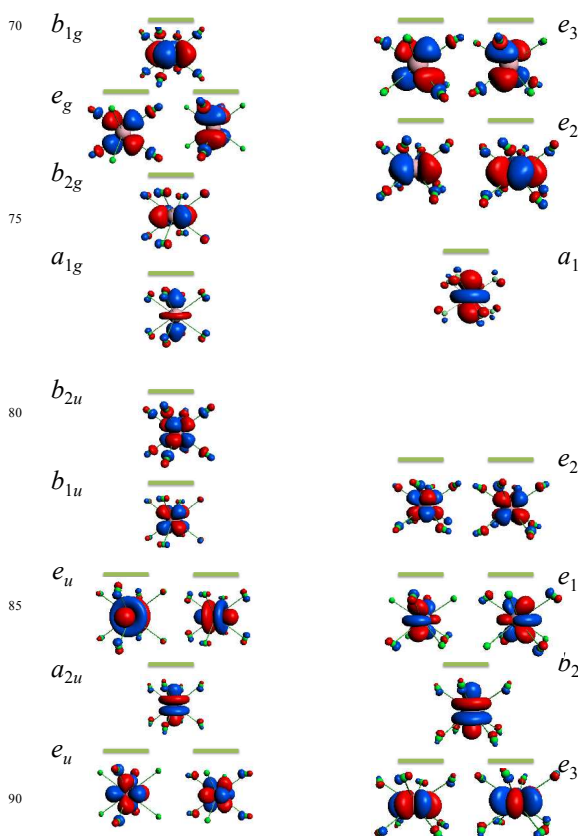


Fig. 4 Splitting pattern of the seven 4f and five 5d orbitals of Pr^{3+} in the presence of a ligand field of D_{4h} (left hand side) and D_{4d} (right hand side) symmetry.

Table 2 LFDFT calculated Slater-Condon parameters in cm^{-1} obtained for the system $(\text{PrX}_8)^{5-}$, with $\text{X} = \text{F}^-, \text{Cl}^-, \text{Br}^-$.

	$(\text{PrF}_8)^{5-}$	$(\text{PrCl}_8)^{5-}$	$(\text{PrBr}_8)^{5-}$
$F_2(ff)$	330.0	323.1	322.1
$F_4(ff)$	43.0	41.9	41.8
$F_6(ff)$	4.6	4.5	4.4
$G_1(fd)$	296.3	227.5	179.8
$F_2(fd)$	210.7	144.3	117.5
$G_3(fd)$	26.7	18.5	14.5
$F_4(fd)$	16.0	10.5	8.3
$G_5(fd)$	4.2	2.8	2.2

The strength of the ligand field is directly related to the AOM parameters (Table 3), where the fluoride ligands exert the largest energy splitting of both the 4f and 5d orbitals. This is perfectly in line with the spectrochemical series for ligands. The definition of the novel mixed parameters $e_\sigma(fd)$ and $e_\pi(fd)$ in the present theoretical section leads to quantities which are lying between the $e_\sigma(f)$, $e_\sigma(d)$, and $e_\pi(f)$, $e_\pi(d)$, respectively, as shown in Table 3. Although in this paper we address theoretical examples based on Pr-halides complexes, the AOM parameters have the recognized advantages to be transferable giving further insight into their comparison to available experimental deduced parameters. Urland⁵² experimentally deduced $e_\sigma(f) = 552 \text{ cm}^{-1}$ in the system $\text{LiYF}_4:\text{Pr}^{3+}$ (eightfold coordinate $(\text{PrF}_8)^{5-}$ having S_4 arrangement)⁵² with a ratio $e_\sigma(f)/e_\pi(f) = 5.34$, in the magnitude of our calculated parameters (Table 3). For a chloride system, $e_\sigma(f) = 235 \text{ cm}^{-1}$ was deduced experimentally in Pr^{3+} -doped LaCl_3 ,⁵³ also in line with the calculated parameters given in Table 3. Experimentally deduced Wybourne-normalized crystal field parameters for bromide systems (Pr^{3+} -doped ThBr_4) are also available in ref. 54, which indicate a priori AOM parameters in the magnitude of Table 3, providing validation of the calculated parameters.

We carried out the investigation by focusing more deeply upon the D_{4d} ligand field, for which the presence of the mixed AOM parameters is attested. To obtain the eigenvalues of the V_{LF} matrix in their representation given in Fig. 4, we calculate analytically the V_{LF} matrix elements for the case of the D_{4d} ligand field. The given analytical expressions are rigorously adequate for any practical example since we present them also in terms of the polar angle θ (cf. Table 1), the AOM parameters containing by definition information about the metal-ligand bond length.^{31,32} In the D_{4d} ligand field, the split of the 4f orbitals in the b_2 , e_1 , e_2 , e_3 irreps follows the classification of $ml = \{0, \pm 1, \pm 2, \pm 3\}$ components. In the same way, the split of the 5d in the a_1 , e_2 , e_3 irreps gets $ml = \{0, \pm 2, \pm 1\}$. Within the first order perturbation, most elements of the V_{LF} matrix are zero, the non-vanishing elements remaining only in the diagonal as given in Eqs. 8 and 9.

$$\langle 3, b_2 | V_{LF} | 3, b_2 \rangle = 2e_\sigma(f) (5\cos^3\theta - 3\cos\theta)^2 + 3e_\pi(f) (4\sin\theta - 5\sin^3\theta)^2 \quad (8a)$$

$$\langle 3, e_1 | V_{LF} | 3, e_1 \rangle = \frac{3}{2}e_\sigma(f) (4\sin\theta - 5\sin^3\theta)^2 + \frac{1}{4}e_\pi(f) (225\cos^6\theta - 305\cos^4\theta + 111\cos^2\theta + 1) \quad (8b)$$

$$\langle 3, e_2 | V_{LF} | 3, e_2 \rangle = 15e_\sigma(f) (\cos\theta - \cos^3\theta)^2 + 10e_\pi(f) \left(\frac{9}{4}\sin^6\theta - 4\sin^4\theta + 2\sin^2\theta \right) \quad (8c)$$

$$\langle 3, e_3 | V_{LF} | 3, e_3 \rangle = \frac{5}{2}e_\sigma(f) \sin^6\theta + \frac{15}{4}e_\pi(f) (\sin^4\theta + (\cos\theta - \cos^3\theta)^2) \quad (8d)$$

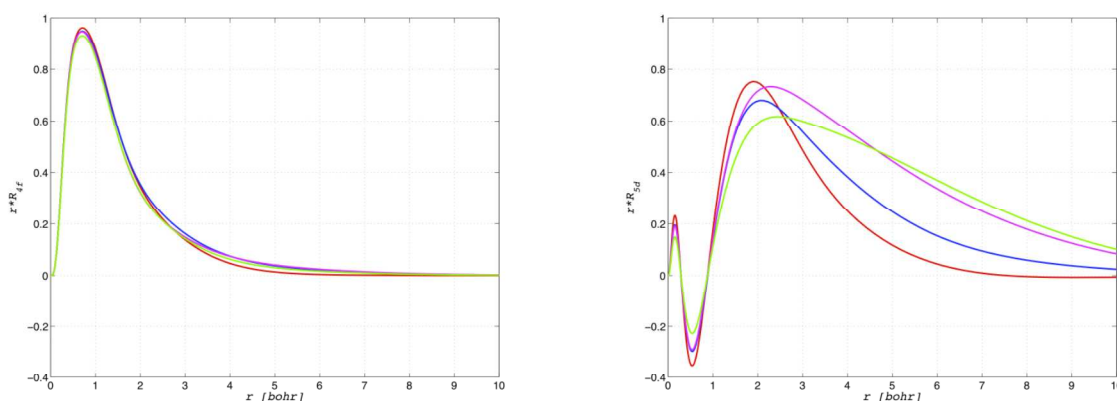
**Fig. 5** Graphical representation of the radial functions of the 4f (left hand side) and 5d (right hand side) Kohn-Sham orbitals of the free Pr^{3+} ion (in red) and the complexes $(\text{PrF}_8)^{5-}$ (in blue), $(\text{PrCl}_8)^{5-}$ (in magenta) and $(\text{PrBr}_8)^{5-}$ (in green), forming a D_{4h} arrangement.

Table 3 DFT calculated AOM parameters in cm^{-1} for the ligand field potential of $(\text{PrX}_8)^{5-}$ ($\text{X} = \text{F}^-, \text{Cl}^-, \text{Br}^-$) with arrangement in D_{4h} and D_{4d} symmetry.

	D_{4h}			D_{4d}		
	$(\text{PrF}_8)^{5-}$	$(\text{PrCl}_8)^{5-}$	$(\text{PrBr}_8)^{5-}$	$(\text{PrF}_8)^{5-}$	$(\text{PrCl}_8)^{5-}$	$(\text{PrBr}_8)^{5-}$
$e_\sigma(f)$	534	214	105	417	186	101
$e_\pi(f)$	71	88	34	194	84	45
$e_\sigma(d)$	13040	4536	3997	13091	4558	3965
$e_\pi(d)$	3732	2405	2365	2341	2365	2514
$e_\sigma(fd)$	0	0	0	3456	429	248
$e_\pi(fd)$	0	0	0	2179	257	123
$\Delta_{\text{AOM}}(fd)$	19351	16741	11339	22075	17397	11755

$$\begin{aligned} \langle 2, a_1 | V_{LF} | 2, a_1 \rangle &= \Delta_{\text{AOM}}(fd) \\ &+ 2e_\sigma(d)(3\sin^2\theta - 2)^2 \\ &+ 24e_\pi(d)\cos^2\theta\sin^2\theta \end{aligned} \quad (9a)$$

$$\begin{aligned} \langle 2, e_2 | V_{LF} | 2, e_2 \rangle &= \Delta_{\text{AOM}}(fd) \\ &+ 12e_\sigma(d)\cos^2\theta\sin^2\theta \\ &+ 4e_\pi(d)(4\cos^4\theta - 3\cos^2\theta + 1) \end{aligned} \quad (9b)$$

$$\begin{aligned} \langle 2, e_3 | V_{LF} | 2, e_3 \rangle &= \Delta_{\text{AOM}}(fd) \\ &+ 3e_\sigma(d)\sin^4\theta \\ &+ 4e_\pi(d)\sin^2\theta(1 + \cos^2\theta) \end{aligned} \quad (9c)$$

Furthermore, within the second order perturbation, the e_2 and e_3 *irreps*, being present in the transformation of both f and d, allow mixing of the 4f and 5d functions as stated earlier, leading to the formation of off-diagonal elements located in the $V_{LF}(4f, 5d)$ block matrix (Eq. 10).

$$\langle 3, e_2 | V_{LF} | 2, e_2 \rangle = \sqrt{30} \cos\theta \sin^4\theta (e_\sigma(fd) - \sqrt{2}e_\pi(fd)) \quad (10a)$$

$$\langle 3, e_3 | V_{LF} | 2, e_3 \rangle = 3\sqrt{5} \cos\theta \sin^4\theta (e_\sigma(fd) - \sqrt{2}e_\pi(fd)) \quad (10b)$$

To ensure the double degeneracy of the e_1 , e_2 and e_3 *irreps*, the matrix elements given in Eqs. 8b, 8c, 8d, 9b, 9c, 10a and 10b are always multiplied by an identity matrix of dimension 2. Amongst the thirty-five elements of the $V_{LF}(4f, 5d)$ block matrix, four elements are non-zero in the D_{4d} ligand field, which are two by two equivalents as shown in Eq. 10. Although the e_2 and e_3 *irreps* are well distinguished in the D_{4d} point group, the AOM formalism up to second order does not differentiate them in the perturbation considering the isotropic π -interaction of the Pr^{3+} -ligand bond. Indeed Eq. 10a can be obtained from Eq. 10b by multiplying it with a factor of $\sqrt{6}/3$. Therefore the slight

stabilization of the eigenvalue of the $|3, e_2\rangle$ function due to the presence of the off-diagonal elements in the V_{LF} matrix (Eq. 10), which is equal to the destabilization of the eigenvalue of the $|2, e_2\rangle$ function, are connected to the energy stabilization of the $|3, e_3\rangle$, which is also equivalent to the destabilization of the $|2, e_3\rangle$, weighted with a constant factor. This factor is not in reality fixed as we obtain from the non-empirical DFT calculation. It can be definitely dismissed in the AOM considering the formulation of two different $e_\pi(fd)$ parameters such as $e_{\pi x}(fd)$ and $e_{\pi y}(fd)$, respectively. These two parameters, while different, will conserve an intrinsic degeneracy of either e_2 or e_3 *irrep* in the D_{4d} point group. This is intriguing but without any doubt in the definition of the second order AOM perturbation. Hence we present in Table 3 one of those $e_\pi(fd)$ parameters since the another one is set to zero in the mapping of AOM to the DFT results (Eq. 5). It is noteworthy to emphasize that the exact consideration of the AOM for two-open-shell f and d electrons requires too many parameters, which by convenience we enforce to fit with only seven parameters ($e_\sigma(f)$, $e_\pi(f)$, $e_\sigma(d)$, $e_\pi(d)$, $e_\sigma(fd)$, $e_\pi(fd)$, $\Delta_{\text{AOM}}(fd)$). The non-considered parameters do not vanish but their influence are subtly engulfed into the active list in Table 3, the V_{LF} matrix from Eq. 5 being as accurate as the calculated non-empirical DFT one.

Since most of the theoretical and experimental works are adopting the Wybourne-normalized crystal field formalism, we present for comparison by means of Eq. 11 the B_q^k 's values (Eq. 1) obtained from the computed matrix elements of V_{LF} (see Eq. 5):

$$\langle l, ml | V_{LF} | l', ml' \rangle = \sum_k \sum_{q=-k}^k B_q^k(l, l') \langle l, ml | C_q^{(k)} | l', ml' \rangle \quad (11)$$

where $\langle l, ml | C_q^{(k)} | l', ml' \rangle$ is a coupling coefficient.

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Table 4 DFT calculated Wybourne-normalized crystal field parameters in cm^{-1} for the ligand field potential of $(\text{PrX}_8)^{5-}$ ($\text{X} = \text{F}^-, \text{Cl}^-, \text{Br}^-$) with D_{4h} and D_{4d} symmetry.

	D_{4h}			D_{4d}		
	$(\text{PrF}_8)^{5-}$	$(\text{PrCl}_8)^{5-}$	$(\text{PrBr}_8)^{5-}$	$(\text{PrF}_8)^{5-}$	$(\text{PrCl}_8)^{5-}$	$(\text{PrBr}_8)^{5-}$
$B_0^2(4f)$	-3	-3	0	-346	-217	-133
$B_0^4(4f)$	-2634	-1148	-550	-2068	-871	-459
$B_4^4(4f)$	1577	689	329	0	0	0
$B_0^6(4f)$	1391	268	175	511	260	148
$B_4^6(4f)$	2595	498	328	0	0	0
$\Delta(fd)$	51285	31249	25104	49592	31853	25926
$B_0^2(5d)$	-82	-79	1	-8929	-5697	-6059
$B_0^4(5d)$	-45129	-7433	-4725	-50719	-6773	-2875
$B_4^4(5d)$	27012	4458	2823	0	0	0
$B_0^1(4f, 5d)$	0	0	0	-5399	-835	-700
$B_0^3(4f, 5d)$	0	0	0	6380	861	580
$B_0^5(4f, 5d)$	0	0	0	1613	366	441

The B_q^k 's are presented in Table 4 for comparison purpose considering the eightfold complexes of Pr^{3+} ion under consideration. In total this formalism requires ten parameters in the actual problem of D_{4d} ligand field, which is by far superseded by our seven parameters obtained from the AOM formalism.

Another utility of the two-open-shell approach, which however will be not detailed here, is curing the so-called holohedrization effect⁵⁹ that leads to an artificial increase in symmetry, if traditional single-open-shell ligand field theories are used. Namely, with respect of an inversion center, the d or f block Hamiltonians can include only terms with even parity, because the matrix elements are carrying the respective $g \times g = g$ or $u \times u = g$ products. This means that an asymmetric coordination sphere is accounted non-realistically. For instance, for the case of a single metal-ligand couple, M-L, the ligand field problem in d or f basis looks like the perturbation is smeared in equivalent halves ($L/2$) on the both directions of the coordination, as the ligand field is produced by a *trans*-($L/2$)-M-($L/2$) arrangement.

Or, in the same line of reasoning a *cis*- MX_3 pyramid with X-M-X only at 90° angles will have the same f or d splitting as an octahedron, since each ligand has distributed its perturbation in the *trans* direction too, resulting in an artificial $\text{M}(\text{X}/2)_6$. Such a *cis*- MX_3 does not exist in reality, but is a convincing thought experiment about the limitation of the classical single-open-shell

ligand field Hamiltonian phenomenology. The two-open-shell approach allows the insertion of asymmetric terms, by the $g \times u = u$ parity of the $f \times d$ nondiagonal block. In this way the ligand field treatment is enhanced to more realism. Another outlook of this approach, which also is too large in technical display, being presented now only as seed idea, is that the explicit use of two-electron f-d terms may replace the use of empirical corrections, such as Trees⁶⁰ or Marvin terms,⁶¹ for amending the implication of many body effect in the ligand field Hamiltonian parameterization. The AOM extended for two-open-shell 4f and 5d electrons will therefore provide a useful tool insuring chemical intuitiveness in the currently popular magnetic property design of lanthanide single ion magnet.⁶²⁻⁶⁵

Conclusions

Theoretical modeling is a valuable tool for the understanding of the chemical and the physical properties of molecular, coordination chemistry complexes and solid state compounds. Here we address a practical problem encountered in the non-empirical determination of the $4f^n \rightarrow 4f^{n-1}5d^1$ transitions: the ligand field interaction. We underline the need for a ligand field potential for two-open-shell 4f and 5d electrons, which is important in the formulation of a new generation of theoretical and application problems in lanthanide physical chemistry. As

practical use, the two-open-shell model is of interest for the design and characterization of modern luminescent materials, aiming to provide us hopefully soon with warm-white LED lighting.

We revisit the old concept of the Angular Overlap Model (AOM), originally designed to describe the electronic structures of a single-open-shell d or f electrons, to parameterize the ligand field potential obtained not only from the LFDFT calculation but also from any available computational setting which may deal with the problem. The combination of the AOM along modern quantum chemistry tools enhances the understanding of the chemistry of lanthanides. We define new mixed AOM parameters acting in non-diagonal blocks of the two-open-shell ligand field matrix. The presented model is also appropriate for the calculation of line intensities, where the mixing of both the 4f and 5d wave functions are important. The AOM can be used to parameterize the ligand field potential for two-open-shell f and d electrons, especially in case of low symmetry lanthanide coordination. The AOM parameters are transferable, comparable, and offer chemical insight. In low symmetry environments, the number of AOM parameters is usually smaller than those of the Wybourne-normalized crystal field schemes, a fact that enhances the transparency of the modelling. The given model contributes to the understanding of lanthanides in phosphors and presents a non-empirical approach using less sophisticated computational procedure for the rather complex problem of ligand fields of both 4f and 5d open-shells.

Acknowledgements

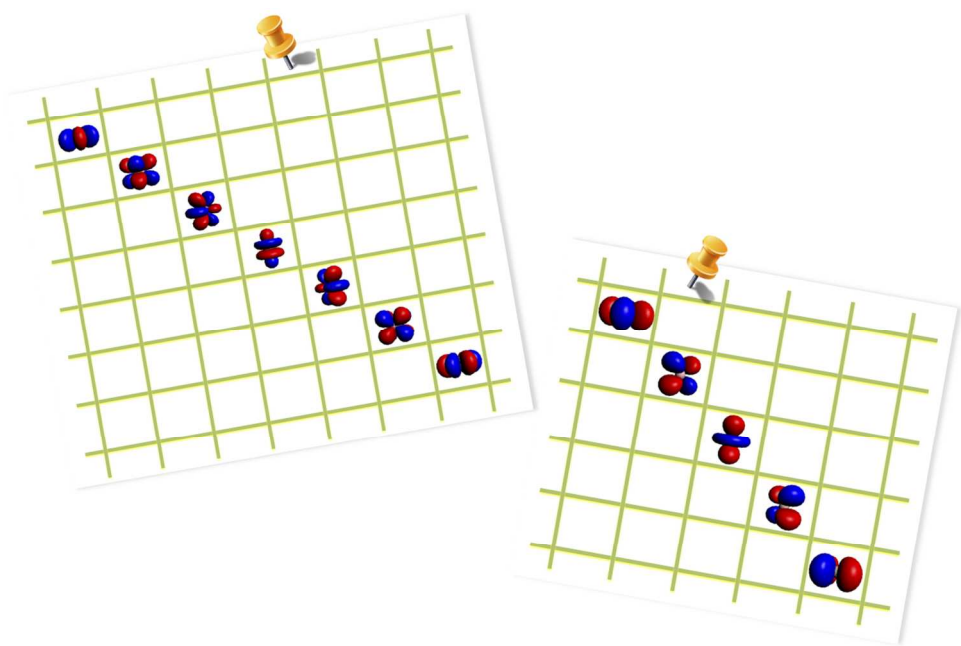
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The Angular Overlap Model is revisited to account for two-open-shell 4f and 5d electrons, important in the interpretation and understanding of the f-d transitions in lanthanide phosphors.
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