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Ferroelectric hexagonal and rhombic monolayer ices

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Two new phases of water, the mid-density hexagonal monolayer ice and the high-density flat rhombic monolayer ice, are observed in our molecular dynamics simulations of monolayer water confined between two smooth hydrophobic walls, in addition to the two monolayer ices reported previously, namely, the low-density 4·8° monolayer ice and the high-density puckered rhombic monolayer ice (HD-pRMI). Stabilities of the structures are confirmed by the ab initio computation. Importantly, both new phases and the HD-pRMI are predicted to be ferroelectric. An in-plane external electric field can further stabilize these ferroelectric monolayer ices.

Methods

The simulation system consists of 400 water molecules confined between two hydrophobic planar walls. The wall separation D is set within the range of 0.51 to 0.65 nm, in which only one layer of water can be accommodated. The TIP5P potential 32 is used to describe water-water interaction, as used previously by Zangi and Mark 16 to simulate electrofreezing of a water slab under an in-plane electric field (5 V/nm) and by Qiu and Guo 33 to study the electromelting of confined monolayer ice. The water-wall interactions are described by the Lennard-Jones (L-J) 9-3 potential function with the parameters $\sigma_{\text{coul}} = 0.25$ nm and $\varepsilon_{\text{coul}} = 1.25$ kJ/mol (following Refs. 20 and 28), namely, the integral of the L-J 12-6 potential for a structureless wall. This is because our previous study demonstrates that the formation of LD-48MI is insensitive to the atomic structure of the wall surface by using two structureless walls and two single graphene layers, and our new MD simulations reinforce this point (see Fig. S1 in ESI for detail). All the MD simulations are performed in the constant lateral pressure ($P_L$) and constant temperature ($T$)
ensemble with periodic boundary conditions in the lateral directions (x and y), using the GROMACS 4.5 package. Temperature and pressure are controlled by the Nosé-Hoover thermostat and Parrinello-Rahman barostat, respectively. A cutoff of 1 nm is used for the LJ interactions, and the long-range electrostatic interactions are treated by the slab-adapted Ewald sum method.

Results and discussion

First, we perform molecular dynamics simulations for given \( D = 0.557 \text{ nm} \), a value used in previous molecular dynamics simulations of monolayer water but with a switching function to cut off all interaction at 0.875 nm. The confined water is cooled from 320 K to 210 K at 10 K. At each temperature, the simulation lasts 20 ns. Then the system is equilibrated at 200 K and \( P_L = -50 \text{ MPa} \) for 60 ns. A monolayer crystalline structure consisting of tetragons and octagons (with some voids) is formed spontaneously, which is the LD-48MI (with some voids). Fig. 1a displays its inherent structure (obtained by applying the steepest-descent method to the final configuration of the system).

Taking the LD-48MI at \( D = 0.557 \text{ nm} \) as the initial configuration, thirteen additional independent simulations are performed for \( D = 0.51, 0.52, 0.53, 0.54, 0.55, 0.57, 0.58, 0.59, 0.6, 0.62, 0.63, 0.64, \) and 0.65 nm, respectively, all at \( P_L = -50 \text{ MPa} \) and \( T = 200 \text{ K} \). The LD-48MI structure is still intact in most cases except for \( D = 0.64 \) and 0.65 nm, at which the LD-48MI melts into monolayer liquid (MLiq). Next, for all fourteen \( D \) values, we compress isothermally the monolayer water stepwise from 50 to 800 MPa, scanning through 11-14 state points of \( P_L \) (20 ns for each state point). In these sequential simulations, three other monolayer crystalline phases are attained, including the two new structures MD-HMI (Fig. 1b) and HD-RMI (Fig. 1c), and the known structure HD-pRMI (Fig. 1d). Structural features and properties of these monolayer ices are discussed below.

Fig. 2 shows the area density \( \rho \) of monolayer water versus the lateral pressure \( P_L \) for various given \( D \) at 200 K.

1. For \( 0.51 \text{ nm} \leq D \leq 0.58 \text{ nm} \), three phase transitions take place in sequence. As \( P_L \) increases from -50 MPa to 50-100 MPa, the LD-48MI transforms into the mid-density hexagonal monolayer ice, i.e. MD-HMI (Fig. 1b). The transition from LD-48MI to MD-HMI exhibits the Oswald staging phenomenon, namely, an unstable intermediate liquid state during the solid-to-solid transition (Movie S1). Interestingly, a stable monolayer liquid (MLiq) can also be observed by increasing the \( P_L \) to 300-400 MPa. The lateral diffusion constant of MLiq is \( D_L \approx 6 \times 10^{-6} \text{ cm}^2/\text{s} \), which is about 30\% of the diffusion constant of bulk water under ambient conditions (2.2 \times 10^{-5} \text{ cm}^2/\text{s})

2. For \( 0.59 \text{ nm} \leq D \leq 0.63 \text{ nm} \), two phase transitions take place in sequence as \( P_L \) increases. First, the MD-HMI phase is bypassed. Next, \( P_L \) increases (we examine more pressure states for this case). In a wider nanoslit (\( D > 0.59 \text{ nm} \)), the MD-HMI is no longer stable.

An approximate \( P_L-D \) phase diagram of monolayer water (under zero external electric field) is plotted based on results of the MD simulations (Fig. 3a). We use the two-phase coexistence simulation method with the NP\( T \) ensemble to determine the phase boundaries (see ESI). More accurate phase boundary can be achieved via the multibaric-multithermal ensemble approach that involves an anisotropic pressure control. A conspicuous feature is that a MLiq domain fully separates two solid phases. On the left side of the MLiq domain, the MD-HMI phase arises in the larger \( P_L \) region; while on the right side of the MLiq domain, the HD-pRMI phase arises in the larger \( P_L \) region. There exist two triple points: one for LD-48MI, MLiq, and MD-HMI, and the other for HD-RMI, MLiq, and HD-pRMI.
Fig. 3. Semi-quantitative phase diagrams of monolayer water confined between two hydrophobic walls at 200 K with the lateral electric field strength $E_L = (a) 0$, (b) 0.01, (c) 0.1, (d) 0.4, (e) 1.0, and (f) 10 V/nm, respectively. Triple points are highlighted by orange circles.

In the inherent structure of LD-k48MI (Fig. 1), it can be seen that the molecular plane of each water molecule is perpendicular to the molecular plane of its nearest-neighbor molecules. Each water molecule has three nearest-neighbors, but entails four hydrogen bonds; namely, LD-k48MI satisfies the ice rule. This is because that the molecule whose molecular plane is perpendicular to the two walls acts as “double donors to a single acceptor”, i.e., its two O-H arms are obliquely oriented towards one O atom in its nearest-neighbor in-plane water molecule, forming two weak hydrogen bonds. Meanwhile, as “double acceptors of double donors”, this molecule forms two strong hydrogen bonds with its two other nearest-neighbor molecules. An in-plane water molecule entails two strong and two weak hydrogen bonds as well, but as “double donors to double acceptors” and “double acceptors of a single donor”. In a plot of the distribution of O-H...O angles of hydrogen bonds (Fig. 4a), the two peaks around $164^\circ$ and $115^\circ$ (for $D \leq 0.55$ nm) correspond to the strong and weak hydrogen bonds, respectively. With the increase of $D$, the libration of the two O-H bonds involved in weak hydrogen bonds with the same O atom becomes stronger. Thus, the peak around $115^\circ$ is lowered and gradually becomes a shoulder peak.

The density distribution of oxygen atoms in the z direction (normal to the walls), i.e. the transverse density profile of LD-k48MI ($P_L = -0.50$ MPa, for $0.51 \text{ nm} \leq D \leq 0.63$ nm), is unimodal, as shown in Fig. 5a. As a measure of the planarity of monolayer ices, the width of the unimodal peak is less than 0.05 nm. This width increases with $D$, and as $D$ reaches 0.64 nm, the distribution becomes bimodal, corresponding to the MLiq. As shown by the lateral oxygen-oxygen radial distribution function (RDF) $g_{OO}(r_{OO})$ in Fig. 6, the nearest neighbor O-O distance in LD-k48MI is 0.28 nm, close to the nearest neighbor distance for the bulk water. The second peak is at 0.39 nm, corresponding to the diagonal distance of a tetragon ($\sqrt{2} \times 0.28$ nm). The third peak is at 0.51 nm, corresponding to the distance between a molecule and its second nearest-neighbor in an octagon ($2 \times \sin(135^\circ/2) \times 0.28$ nm). Because each molecule has a para-position in a tetragon and two meta-positions in an octagon, the height of the third peak is about twice of that of the second peak. The position and height of the following peaks can be also understood based on the Archimedean 4·8·2 truncated square tiling.

Fig. 4. Hydrogen-bond angle distributions at $T = 200$ K for (a) LD-k48MI at $P_L = -0.50$ MPa, (b) MD-HMI at $P_L = 100$ MPa, and (c) HD-RMI and HD-pRMI at $P_L = 800$ MPa, respectively.

Fig. 5. The transverse density profile for different slit width $D$ at $P_L = (a) -0.50$ MPa, (b) 200 MPa, (c) 500 MPa, and (d) 800 MPa, respectively. The filled squares indicate LD-k48MI, unfilled squares MLiq, filled circles MD-HMI, unfilled diamonds HD-RMI, and filled diamonds HD-pRMI.
program being ferroelectric (Fig. 7a). Interestingly, the hexagonal molecule is also perpendicular to those of its three nearest neighbors, and the plane of each water HMI. Like LDk48MI, every water molecule in MDkHMI also exhibits spontaneous polarization. For MDkHMI (at $P_L = 200$ MPa) is also characterized by a Gaussian-like distribution with a width $< 0.05$ nm, and this width also increases with $D$. For $D = 0.58$ nm, the MD-HMI melts into MLiq, and the density distribution starts to develop two peaks, while the value of the density profile at $z = 0$ (the central plane parallel to the two walls) is still significant. For $D = 0.62$ nm, the value at $z = 0$ drops to almost zero, reflecting a phase transition from MLiq to HD-pRMI. The first peak in the lateral O-O RDF of the MD-HMI is at $-0.27$ nm (Fig. 6), a value again close to that of the nearest-neighbor distance in bulk water.

As Fig. 5b shows, the transverse density profile of the MD-HMI (at $P_L = 200$ MPa) is also characterized by a Gaussian-like distribution with a width $< 0.05$ nm, and this width also increases with $D$. For $D = 0.58$ nm, the MD-HMI melts into MLiq, and the density distribution starts to develop two peaks, while the value of the density profile at $z = 0$ (the central plane parallel to the two walls) is still significant. For $D = 0.62$ nm, the value at $z = 0$ drops to almost zero, reflecting a phase transition from MLiq to HD-pRMI. The first peak in the lateral O-O RDF of the MD-HMI is at $-0.27$ nm (Fig. 6), a value again close to that of the nearest-neighbor distance in bulk water.

Third, we turn our attention to the two high-density monolayer ices HD-RMI and HD-pRMI. As shown in Figs. 1c and 1d, both HD-RMI and HD-pRMI are composed of rhombic rings. The primary structural distinction between them can be seen from the side view shown in Figs. 1c and 1d: the oxygen atoms of the HD-RMI are essentially in the same plane parallel to the walls, while those of the HD-pRMI are in alternate ridges with different $z$ coordinates. As shown in Figs. 5c and 5d, the transverse density profile of the HD-RMI is unimodal, while that of the HD-pRMI is bimodal, which is why we name this ice as “puckered”. Still, one may wonder whether both ice structures belong to the same phase. To address this question, we carry out additional 32 independent molecular dynamics simulations at $P_L = 800$ MPa and $T = 200$ K for increasing $D$ stepwise from 0.55 nm (HD-RMI) to 0.58 nm (HD-pRMI) and then for the reverse (decreasing $D$) process. As shown in Fig. 9, when $D$ increases, the potential energy $U$ first slowly decreases and then drops steeply by about 1.5 kJ/mol for $D$ from 0.570 nm to 0.574 nm. Meanwhile, the area density $\rho$
first increases gradually, and then jumps up by about 0.8 nm². Upon decreasing D, U and $\rho$ also show abrupt changes in the reverse process, but with a clear hysteresis. So we conclude that the HD-fRMi is a new phase different from the HD-pRMi, and the transition between the two phases is first-order upon changing D.

Why such a transition is first order? To answer the question, we analyze the hydrogen-bonding networks of the two high-density ice phases. Note that the coordination number of every water molecule in the HD-fRMi and HD-pRMi is four, as opposed to three in the LD-48MI and MD-HMI. As such, water molecules can meet the ice rule more easily without invoking the “double donors to a single acceptor” mechanism. Nevertheless, another issue arises: the O–H–O angles of the hydrogen bonds, i.e., where the H atoms between the two O atoms of neighboring molecules are located. Normally, the strength of a hydrogen bond increases with its O–H–O angle, and a linear hydrogen bond would be the most ideal. At the outset, the HD-fRMi can make a stable hydrogen-bonding network by arranging all atoms of every water molecule in the same plane and the two H atoms of each molecule roughly in two lines between the two O atoms of neighboring molecules are located. Normally, the strength of a hydrogen bond increases with its O–H–O angle, and a linear hydrogen bond would be the most ideal. At the outset, the HD-fRMi can make a stable hydrogen-bonding network by arranging all atoms of every water molecule in the same plane and the two H atoms of each molecule roughly in two lines connecting with its own O atom and with its two neighbor O atoms, respectively (we call this arrangement as “all-atom planar structure”). As the H–O–H bond angle of water molecules (104.5°) is close to the inner rhombus angle of HD-fRMi (108°), all the O–H–O angles would be close to 180°. However, analysis on the electronic structure indicates that this all-atom planar arrangement is unfavorable. The O atom in water molecule is sp³ hybridized, and its four molecular-orbital lobes yield two covalent bonds and two lone electron pairs. When forming hydrogen bonds, the two lone pairs of the O atom act as H acceptor. As such, the two O-H covalent bonds and associated two O–H vectors of the hydrogen bonds tend to point to the four vertices of a tetrahedron centered from the O atom. If the hydrogen bonds are in the same plane as the covalent bonds, they would cause too much energy penalty. Our ab initio density-functional calculations indeed show that the all-atom planar structure is unstable.

An ideal hydrogen-bonding network of water should satisfy the three requirements simultaneously: (1) four hydrogen bonds for every water molecule, (2) tetrahedral orientation for the four hydrogen bonds, as well as (3) nearly linear hydrogen bonds. Ice structures with the coordination number of three cannot meet the first and the third requirement at the same time. Hence, both LD-48MI and MD-HMI favor the first and the second requirements while compromise on the third requirement, resulting in two nearly linear and two bent hydrogen bonds for each water molecule.

In the HD-fRMi, the geometric constraints to meet the three requirements are even stronger. Suppose there are three O atoms in a linear row (O0, O1, and O2 where O1 is between O0 and O2) with distance being ~ 0.28 nm between O1 and its two neighbour O atoms, forming a linear hydrogen bond O0-H1-O1 (ESI Fig. S3). Under the requirement of tetrahedral orientation, we now consider the geometry of the other hydrogen bond O1-H2-O2. Since the H1O1H2 angle is ~ 109.5°, the H2O1H2 angle must be ~ 70.5°. The distance from O2 to the line O1H2 is ~ 0.28 nm \times \sin(70.5°) = 0.26 nm. This value is much larger than the O-H bond length of a water molecule (~ 0.096 nm), therefore H2 cannot make a covalent bond with O2. In other words, O1 must be the proton-donor. So the O1H2 length is ~ 0.096 nm, the O2H2 length is ~ 0.263 nm, and the O1H2O2 angle is ~ 88°. However, the latter two values do not satisfy the definition of normal hydrogen bonding. Therefore, we can draw a rather general conclusion that linear hydrogen bonds are highly unlikely to exist within a linear row of O atoms.

In the LD-48MI and MD-HMI, there is no such a linear row, and the angle between two linear hydrogen bonds of an O atom is around 90°. In the HD-fRMi, however, every nearest neighbor O–O pair is in a linear row, so there is no room for a single linear hydrogen bond. In other words, the hydrogen bonding in the HD-fRMi is highly frustrated. This behavior is reflected in the broad and featureless distribution of hydrogen bond angles (Fig. 4c): Most O–H–O angles are in the range from 120° to 150°. In the HD-pRMi, the ridges are still linear rows, but the O atoms aligned in the direction normal to the ridges form zigzag lines instead of linear rows. Therefore, a half number of hydrogen bonds between nearest-neighboring ridges can be nearly linear (and they are indeed so), leading to notable energy drop from the formation of HD-fRMi to HD-pRMi (Fig. 9a), while the other half number of hydrogen bonds along the ridges are still frustrated. The latter feature can be seen from the snapshot (Fig. 1d) and the hydrogen-bond angle distribution (Fig. 4c), which shows two peaks around 169° and 138°. This is the reason for the first-order transition between the two rhombic monolayer ices.

Besides the TIP5P model, we have also examined several other three-site and four-site water models (SPC, SPC/E, TIP3P, TIP4P, and TIP4P/2005). Additional simulations show that all these models give rise to the all-atom planar structure. Our analysis above and results of ab initio calculations demonstrate that the frustrated HD-fRMi structure is more sensible, whereas the all-atom planar structure appears to be unphysical. The key difference between the TIP5P and other models considered may lie in their representation to the electronic structure of O atoms. The TIP5P model entails two negative charge centers in the directions of the two lone pairs, thus mimicking the sp³ hybridization. Other three-site and four-site models lack the similar feature, and therefore the planar arrangement of four H atoms around an O atom results in no energy penalty. This might be a reason why previous simulations on this system did not yield the new structures presented here. One may question why other models can still predict the tetrahedral structure of bulk ice, even though they incur no energy penalty for the flat geometry. An answer is that the bulk ice is still favored by these models because of the formation of local tetrahedral structures. However, under the highly confined environment for the monolayer water, the tetrahedral orientation of H atoms can be energetically favoured over the planar arrangement only if the energy penalty for the latter is implemented into the water model.

As shown in Fig. 1c, water molecules in HD-fRMi exhibit two distinct orientations, both tilted to the walls. The orientation of each molecule is different from that of its four neighbors, rendering the 2D network chessboard-like. Nevertheless, the molecular dipoles with the two orientations result in a net total dipole parallel to the longer diagonal of a rhombus. In HD-pRMi, again there are two
orientations, while the molecules with the same height have the same orientation. The two orientations are also tilted, and also result in a net total dipole parallel to the longer diagonal of a rhombus. Their polarizations are 18 µC/cm² (HD-kfRMI, D = 0.52 nm) and 19 µC/cm² (HD-pRMI, D = 0.59 nm) and the corresponding ab initio values are 22 µC/cm² (D' = 0.52 nm) and 23 µC/cm² (D' = 0.59 nm), respectively (Fig. 8). The ferroelectricities of HD-RMI and HD-pRMI are also confirmed by the strong ferroelectric hysteresis loops (Figs. 7b and 7c). Also, importantly, the “probably ferroelectric” monolayer ice upon an exposed mica surface observed by Spagnoli et al.31 using atomic force microscopy, which appear to exist in a puckered film arrangement, consistent with this HD-pRMI we observed.

To study effect of an in-plane electric fields on phase behavior of monolayer water, we perform the same series of simulations for the system subject to a lateral electric field with strength $E_L = 0.01$, 0.1, 0.4, 1, and 10 V/nm, respectively. These values are comparable to those experienced by water within the crevices of polar crystals,55 from the surfaces of biopolymers46,47 or nanoelectrodes48. Figures 3b-3f show the $P_x$-$D$ phase diagrams with different $E_L$ or 2D cross-sections of the 3D $P_x$-$D$-$E_L$ phase diagram. The corresponding raw data are given in Fig. S4 as the $\rho$ - $P_L$ curves.

For $E_L = 0.01$ V/nm, the topology of the phase domains is the same as that in Fig. 3a, but the phase boundaries are relocated. For $E_L = 0.1$ V/nm, the phase boundaries are moved further away. A qualitative change occurs for $E_L = 0.4$ V/nm; the domain of MLiq becomes an “island-like” region, and can no longer separate the two solid-phase regions. For $D \geq 0.557$ nm or $D \geq 0.59$ nm, MD-HMI can directly transform to either HD-RMI or HD-pRMI (Movies S2 and S3). The domain of LD-48MI is now fully separated from the MLiq phase by MD-HMI. For $E_L = 1$ V/nm, both MLiq and LD-48ML domains disappear, and only the three ferroelectric phases remain. At $E_L = 10$ V/nm, only the two high-density rhombic phases survive. Obviously, the reason for these behaviors is that the polarization energy under electric field stabilizes the ferroelectric phases.

For given $D$ and $E_L$, increasing $P_L$ favors phases with higher area density $\rho$. The order of $\rho$ (LD-48MI < MD-HMI < MLiq < HD-RMI < HD-pRMI) is indeed a general sequence of phases in the $P_L$ direction. Moreover, the area density of the monolayer structure is positively correlated with its coordination number ($N_C$). The $N_C$ is 3 for LD-48MI and MD-HMI, 4 for HD-RMI and HD-pRMI, and about 3.5 for MLiq. Hence, the two solids with $N_C = 3$ arise at low pressure region and are next to one another, while the two solids with $N_C = 4$ arise at high pressure region and are next to one another. The MLiq separates the two groups. Because the difference in $\rho$ between HD-RMI and HD-pRMI is very small, the phase boundary line between them is quite flat.

Among the five 2D phases, three are flat (LD-48MI, MD-HMI, and HD-RMI), and two are nonplanar (MLiq and HD-pRMI). When increasing $D$ while fixing $P_L$ and $E_L$, each phase would rearrange its structure to lower its free energy, and the nonplanar phases have more flexibility than the planar phases in the structural relaxation. Hence, the domain of HD-pRMI is above that of HD-RMI. Moreover, since both LD-48MI and MD-HMI are relatively less sensitive to change in $D$, their boundary is nearly vertical. Because MLiq is nonplanar, increasing $D$ would widen its domain in both directions of $P_L$. Therefore, the slopes of the (MD-HMI)-MLiq and MLiq(HD-RMI) boundaries are negative and positive, respectively. In the two nonplanar phases, HD-pRMI is more favorable with increasing $D$ due to its long-range ordering, so the slope of the phase boundary is negative. The MLiq(HD-RMI)-HD-pRMI triple point is the turning point of the two liquid-solid lines.

Conclusions

In conclusion, four monolayer ice phases, including two new ones, are predicted based on molecular dynamics simulations. Moreover, both new phases (MD-HMI and HD-RMI) and the HD-pRMI are predicted to be ferroelectric. The latter appears to be relevant to the prediction of “probable ferroelectricity” from the experiment.31 Stabilities and ferroelectricities of the 2D monolayer ices are supported by the ab initio density-functional theory calculations, as well as by the strong tendency of satisfying the ice rule in a monolayer of water. Both evidences suggest that the existence of 2D ferroelectric ices is highly plausible and thus warrants future experimental confirmation and more simulations with improved water models (e.g. WAIL water model56). Finally, we find that an in-plane external electric field can stabilize the ferroelectric phases and eliminate the nonpolarized phases. In contrast, a perpendicular external electric field can melt the monolayer ice.33 Thus, an external electric field may be used to alter phase behavior of confined water.

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Notes and references

39. The CASTEP software code is distributed and maintained by Accelrys Inc.