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The coupling of quasi 2-D MoS$_2$ with substrate on different substrate type has been studied, probed by temperature dependent Raman scattering.
Dependence of Coupling of Quasi 2-D MoS$_2$ with Substrate on Substrate Type, Probed by Temperature Dependent Raman Scattering

Liqin Su,$^a$ Yong Zhang,$^a,^*$ Yifei Yu,$^b$ and Linyou Cao$^b$

This work reports a study on the temperature dependence of in-plane $E_2g'$ and out-of-plane $A_{1g}$ Raman modes of single-layer (1L) and bi-layer (2L) MoS$_2$ films on sapphire (epitaxial) and SiO$_2$ (transferred) substrates as well as bulk MoS$_2$ single crystal in a temperature range of 25 – 500 °C. For the films on the transferred SiO$_2$ substrate, the in-plane $E_2g'$ mode is only weakly affected by the substrate, whereas the out-of-plane $A_{1g}$ mode is strongly perturbed, showing highly nonlinear, sometimes even non-monotonic, temperature dependence in the Raman peak shift and linewidth. In contrast, for the films on the epitaxial sapphire substrate, $E_2g'$ is affected more significantly by the substrate than $A_{1g}$. This study suggests that the 2-D film-substrate coupling depends sensitively on the preparation method, and in particular on the film morphology for the transferred film. These findings are vitally important for the fundamental understanding and application of this quasi 2-D material that is expected to be supported by a substrate in most circumstances.

Introduction

Two-dimensional (2-D) materials such as graphene and hexagonal boron nitride (h-BN) have attracted tremendous attentions because of their extraordinary physical properties. However, graphene is a zero band gap material with vanishing density of states at the Dirac point, making it difficult to be used in electronic devices, particularly in transistors. Although several strategies of band gap engineering have been applied to open the band gap, generating a band gap larger than 400 meV remains a challenge. In contrast, h-BN has a band gap of 5.2 eV, too large for an efficient performance in electronic devices. Recently, single-layer molybdenum disulfide (MoS$_2$), consisting of three atomic layers of one Mo and two S, has been shown to exhibit a direct band gap of ~1.8 eV, while bulk MoS$_2$ has an indirect band gap of 1.29 eV. Since single-layer MoS$_2$ shares a number of common properties with graphene such as 2-D layered structure but has a finite band gap, it is considered to be an alternative to graphene, attracting a significant research interest. By using mechanical exfoliation method, single- and few-layer MoS$_2$ samples have been achieved, showing extremely strong photoluminescence compared to bulk MoS$_2$. Recently, single-layer MoS$_2$ based FETs have been reported to have a mobility of at least 200 cm$^2$ V$^{-1}$ s$^{-1}$ and a current on/off ratio of $1 \times 10^8$. These promising optical and electronic properties can potentially lead to the development of high-quality low-power optoelectronic devices. Synthesis of large area of MoS$_2$ atomic layers has been demonstrated using a vapor-phase deposition method. Recently, it has been reported that a self-limiting approach can produce thin MoS$_2$ films over an area of centimeters with the layer number precisely controllable.

A single-layer MoS$_2$ is formed by the arrangement of a triangular or simple hexagonal plane of Mo atoms sandwiched between two triangular layers of S atoms in a triangular prismatic fashion (see Fig.1(a)). Bulk MoS$_2$ is a periodically stacked S-Mo-S layers through Van der Waals force. The space group of single layer MoS$_2$ is $P6m2$ (point group $D_{3h}$), and the four first-order Raman active modes at the center of Brillouin zone are 32 cm$^{-1}$ ($E_2g'$), 286 cm$^{-1}$ ($E_{1g}$), 383 cm$^{-1}$ ($E_2g'$), and 408 cm$^{-1}$ ($A_{1g}$). The $E_2g'$ mode arises from the relative motion between two MoS$_2$ layers, which will vanish in the single layer sample. The $E_{1g}$ mode is forbidden in back-scattering measurement on the basal plane perpendicular to the c axis. The $E_2g'$ mode is attributed to the in-plane relative motion between the two S atoms and the Mo atom, whereas the $A_{1g}$ mode the out-of-plane vibration of two S atoms in opposite directions. Strictly speaking, the two active Raman modes $E_2g'$ and $A_{1g}$ should be assigned as $E'$ and $A_{1g}'$ in the monolayer MoS$_2$ (in $D_{3h}$). However, to see the evolution
from the bulk to single-layer, the two modes are simply labelled as $E_{2g}^1$ and $A_{1g}$ for all cases, as commonly done in the literature. Raman spectroscopy is a sensitive nondestructive technique to investigate structural and electronic properties of MoS$_2$. Similar to graphene, the Raman peak positions depend on the number of MoS$_2$ single layers, which makes it possible to determine the number of layers from Raman spectra.

In this work, we report on the temperature dependent Raman spectra of both single- (1L) and bi-layer (2L) MoS$_2$, as well as the bulk sample. The knowledge of temperature dependent vibrational properties is important for further understanding electron-phonon interaction, transport properties, and crystal structure of material, which may largely impact the performance of electronic devices. Furthermore, because the MoS$_2$ is expected to be supported by a substrate in most if not all real applications, thus the coupling with substrate is inevitable, this temperature dependence study offers valuable insights to the effect of substrate, which might not be apparent at a fixed temperature. Since SiO$_2$/Si is widely used as the substrate for fabricating electronic devices after the film being transferred from the original growth substrate, it is of particular interest to investigate the 2-D film with SiO$_2$/Si substrate.

The temperature variations of the Raman frequencies in MoS$_2$ on SiO$_2$/Si have been studied previously, giving the linear temperature coefficients, respectively, for $E_{2g}^1$ and $A_{1g}$ modes: for few layers, -0.0132 cm$^{-1}$/K and -0.0123 cm$^{-1}$/K from 83 to 523 K; for single layer, -0.0179 cm$^{-1}$/K and -0.0143 cm$^{-1}$/K from 300 to 550 K; and for bi-layer on, -0.0137 cm$^{-1}$/K and -0.0189 cm$^{-1}$/K from 300 to 550 K. Apparently, the absolute and relative magnitudes of the temperature coefficients for the two modes differ significantly in these reported values. Furthermore, reliable data for the bulk MoS$_2$, which may serve as the references, are not readily available in the literature. The intrinsic mechanism for the redshift of Raman frequency with increasing temperature, as is known for most materials, is associated with the anharmonic effect due to weakening of the lattice potential energy. In our work, we report the temperature dependent Raman measurements of single- and bi-layer MoS$_2$ in a larger temperature range from 300 to 773 K with small temperature increments, which allows us to accurately examine not only the nonlinearity of the temperature dependence but also the dependence of the film-substrate coupling on the substrate type.

**Experimental Section**

**Samples**

The samples investigated in this work have been obtained by two methods: mechanical exfoliation and chemical vapor deposition as reported in Ref.16. The 1L MoS$_2$ flake was mechanically exfoliated from nature crystalline bulk MoS$_2$ and
transferred onto a silicon wafer covered by a 300-nm-thick thermal oxide (SiO$_2$) layer (Sample 1L-ME-SiO$_2$). The CVD-grown 1L and 2L samples were prepared on two types of substrates, SiO$_2$/Si and sapphire labeled as, respectively, 1L-CVD-SiO$_2$, 1L-CVD-Sa, 2L-CVD-SiO$_2$, and 2L-CVD-Sa. Originally the MoS$_2$ films were grown on sapphire wafers, and then transferred to SiO$_2$/Si wafers by scotch tape. Raman system used in this work is Horiba LabRam HR800 with a spectral resolution smaller than 1 cm$^{-1}$, A 532 nm laser was used with power ~1 mW, low enough to avoid heating of the samples. The temperature dependent measurements were performed with a 50× long-working-distance lens.

Characterization of Samples

Fig.2(a) shows the optical image of an exfoliated 1L MoS$_2$ film on the SiO$_2$/Si wafer, with an AFM image in Fig.2(b), confirming the one-layer thickness which is ~0.7 nm. The Raman frequency difference (Δω) between the $E_{2g}$ and $A_{1g}$ modes has been shown to correlate with the layer number, with Δω = 19 cm$^{-1}$ for 1L and 22 cm$^{-1}$ for 2L$^{21}$ Raman mappings of exfoliated films were carried out to examine the thickness distribution of the MoS$_2$ film at room temperature, and the spatial variation of the frequency difference Δω is shown in Fig.2(c). All the Δω values are found less than 20 cm$^{-1}$, indicating it is indeed single-layer MoS$_2$. Room temperature Raman and photoluminescence (PL) spectra of all the samples, including a bulk MoS$_2$ sample, used in this work are shown in Fig.2(d) and 2(e), respectively. With increasing number of layers, the $E_{2g}$ peak shows a redshift in Raman frequency while $A_{1g}$ peak blueshift. There are small shifts in the peak position among samples of the same thickness but on different substrates, due to residue strain, suggesting some coupling between the film and substrate. In addition, the linewidths of 1L and 2L samples are somewhat larger than those of the bulk sample, which could be an indication of inhomogeneity of the strain. It has been reported that the PL of MoS$_2$ has two peaks that correspond to A1 (1.85 eV) and B1 (1.98 eV) direct excitonic transitions of MoS$_2$.$^{13}$ The A1 and B1 transitions are, respectively, at 1.82 eV and 1.98 eV for sample 1L-ME-SiO$_2$, 1.87 eV and 2.0 eV for single-layer CVD samples, and 1.85 eV and 1.99 eV for bi-layer CVD samples. The variation of PL peak positions of MoS$_2$ samples could be due to the interaction between the film and the substrate and possibly impurities in the films. Additionally, the 1L MoS$_2$ samples show the strongest PL signal, while bulk MoS$_2$ negligible, as expected due to the electronic band structure change.

Experimental Setup

For the temperature dependent study, a Linkam TS1500 heating system, with a temperature control accuracy of 1 °C, was used to heat the samples with a step of 25 °C, and heating rate of 10 °C/min. Five minutes was applied to hold the temperature at each temperature step, allowing sufficient time for stabilization. An extremely low flow rate of nitrogen gas was purged to avoid the oxidation of MoS$_2$ into MoO$_3$. After the sample temperature stabilized, Raman spectra were acquired by the

Horiba Raman system. A few 1L samples were heated in the ambient environment, and no Raman signals of $E_{2g}$ and $A_{1g}$ modes were observed when the temperature > 350 °C, implying total oxidization of MoS$_2$ films.

Results and discussion

Temperature dependence of Raman scattering

The temperature dependences of both $E_{2g}$ and $A_{1g}$ peak positions were performed in the range from room temperature (25 °C) to 500 °C, shown in Fig.3(a)-(d). The upper temperature range in this work is substantially higher than those in the previous works < 250 °C.$^{23, 24}$ The results of bulk MoS$_2$ are used as a reference. Empirically, the temperature dependence of Raman shift can be described by:

$$\omega(T) = \omega_0 + \chi_1 T + \chi_2 (T - T_r)^2 + \chi_3 (T - T_r)^3,$$

where $\omega_0$ is the frequency at room temperature, Δ$T$ is the temperature change relative to room temperature, and $\chi_1$ is the first-order temperature coefficient. The second ($\chi_2$), third ($\chi_3$) or higher order temperature effects are usually assumed to be small in the literature. In reality, the nonlinear effects are found to be quite significant for 1L or 2L MoS$_2$ even in a temperature...
range where the linear dependence might be expected to be adequate, for instance, below 200 °C, depending on the substrate. Even for bulk MoS$_2$, the nonlinearity occurs at around 200 °C for both $E_{2g}$ and $A_{1g}$, though rather weak, but nevertheless evident in our data. It is perhaps reasonable to assume that the temperature shift for a free standing few-layer MoS$_2$ should be rather close to that of the bulk material, despite the difference in the absolute position. Therefore, to show more clearly the substrate effect, we can take the temperature shifts of the bulk sample as references. Figs.3(e)-(h) plot the difference in the Raman frequency shifts between the thin film sample and the bulk, $\delta \omega (T) = | \omega (T) - \omega_0 | _{\text{thin film}} - | \omega (T) - \omega_0 | _{\text{bulk}}$, for $E_{2g}$ and $A_{1g}$ and for 1L and 2L samples. Below we discuss separately $E_{2g}$ and $A_{1g}$ to examine the effects of two types of substrates.

(1) $E_{2g}$: For both the 1L and 2L samples, as shown in Fig.3(a) and (c), Fig.3(e) and (g), the $E_{2g}$ mode exhibits relatively weak nonlinearity or in general appears to be close to the temperature dependences of the bulk sample. The temperature dependences of the deviations from the bulk mode are qualitatively similar for the same type of substrate: 1L-CVD-Sa and 2L-CVD-Sa, and 1L-CVD-SiO$_2$ and 2L-CVD-SiO$_2$, which is more apparent in Fig.3(e) and (g), due to subtle differences in the film-substrate coupling (to be discussed later). The deviations of 1L-ME-SiO$_2$ are somewhat different from the other samples, as shown in Fig.3(e).

(2) $A_{1g}$: For both 1L-ME-SiO$_2$ and 1L-CVD-SiO$_2$, as shown in Figs.3(b) and (f), the temperature dependence of $A_{1g}$ mode is drastically different from that of the bulk, showing strong nonlinearity starting at temperature near 100 °C and an overall ‘S’ shape dependence. The Raman spectra of 1L-ME-SiO$_2$ at a few representative temperatures are shown in Fig.4. The FWHM of $A_{1g}$ mode is 5.7 cm$^{-1}$ at room temperature, increasing to a maximum of 10.3 cm$^{-1}$ at around 125 °C, then it decreases to 6.3 cm$^{-1}$ at the temperature reaches 500 °C, whereas the FWHM of $E_{2g}$ mode increases from 2.2 cm$^{-1}$ at room temperature monotonically to 4.8 cm$^{-1}$ at 500 °C. However, 1L-CVD-Sa shows only small deviation from the bulk dependence, with an average slope of -0.0159 cm$^{-1}$/K by using linear fitting, up to 425 °C, then an obvious change occurs, becoming nearly flat with a slope of -0.0027 cm$^{-1}$/K. As for the 2L samples, Figs.3(d) and (h), similar to 1L-CVD-SiO$_2$, 2L-CVD-SiO$_2$ exhibits more significant deviation from the bulk sample than 2L-CVD-Sa when temperature < 400 °C. For 2L-CVD-Sa, the slope changes significantly when T > 400 °C from -0.0162 cm$^{-1}$/K to -0.0102 cm$^{-1}$/K. Again, one may notice that the temperature dependences of the deviations from the bulk mode are qualitatively similar for the same type of substrate: 1L-CVD-Sa and 2L-CVD-Sa vs. 1L-CVD-SiO$_2$ and 2L-CVD-SiO$_2$, which is more apparent in Fig.3(f) and (h).

Similarly it is reasonable to expect that in MoS$_2$ the in-plane mode ($E_{2g}$) will be less affected by the interaction between film and substrate than the out-of-plane mode ($A_{1g}$). Thus, it is not difficult to understand that the $E_{2g}$ mode typically shows more linear temperature dependent Raman shift than $A_{1g}$ mode for both 1L and 2L samples. The difference between the SiO$_2$ and sapphire substrate also indicates that the coupling between the film and substrate depends on the substrate type and/or how the film and substrate is bound.

The temperature coefficients of all the samples are fitted to third order with polynomial function according to Eq.(1), listed in Table 1. The linear temperature coefficients of $E_{2g}$ and $A_{1g}$ in bulk MoS$_2$ are $\chi_1 = -0.0211 \pm 8.9 \times 10^{-4}$ cm$^{-1}$/K and $-0.0197 \pm 8.9 \times 10^{-4}$ cm$^{-1}$/K, respectively. Bulk MoS$_2$, as the reference, can be treated as a stacking of single-layered MoS$_2$ films, and each layer has the same properties. With increasing temperature, all layers expand with the same rate without introducing any strain, leading to a nearly linear redshift of the Raman peak position for both $E_{2g}$ and $A_{1g}$ modes. Although the interlayer coupling has led to significant frequency shifts for the two modes between 1L and bulk, the changes in temperature coefficients are expected to be relatively small. For the $E_{2g}$ mode, the first-order temperature coefficients ($\chi_1$) of SiO$_2$ samples, both 1L and 2L, are close to that of bulk MoS$_2$, while those of the sapphire samples are much smaller. For $A_{1g}$, all the SiO$_2$ samples yield much larger $\chi_1$’s than that of bulk MoS$_2$, while sapphire samples are close to bulk MoS$_2$. Our results for the films on SiO$_2$/Si are contradicting to or significantly different from those reported in the literature, because the improved data accuracy allows to examine the nonlinear effect that was neglected.

Because all the SiO$_2$ samples were produced by mechanical exfoliation, it is possible that wrinkles or ripples were introduced to the films, resulting in a considerable strain in the film. Fig.5 gives the spatial maps of the Raman frequencies of $E_{2g}$ and $A_{1g}$ modes for mechanically exfoliated single-layer MoS$_2$ film on SiO$_2$/Si (1L-ME-SiO$_2$) at room temperature. The maps demonstrate that the frequency of $A_{1g}$ shows a larger increase.
variation than that of $E_{2g}^1$, indicating that the morphology of the film impacts the Raman frequency of $A_{1g}$ more than that of $E_{2g}^1$. On the other hand, both 1L and 2L MoS$_2$ films were originally grown on sapphire. It has been reported, for graphene, the possibility of forming bonds between mechanically exfoliated graphene and substrate is quite low; however, such bonds are possible with high-temperature growth. It is reasonable to believe that the CVD growth of MoS$_2$ films at the temperature higher than 800 °C could produce somewhat stronger bonding between the MoS$_2$ film and sapphire substrate than in the case of transferred film. With increasing temperature, the chemical bonding would influence the in-plane vibration, giving rise to a

### Table 1 Temperature coefficients of bulk, 1L and 2L samples with polynomial fitting to third order.

<table>
<thead>
<tr>
<th></th>
<th>$\chi_1$</th>
<th>$\chi_2$</th>
<th>$\chi_3$</th>
</tr>
</thead>
<tbody>
<tr>
<td>bulk</td>
<td>$-0.0221 \pm 8.9 \times 10^{-4}$</td>
<td>$2.12 \times 10^5 \pm 4.4 \times 10^{-6}$</td>
<td>$-2.94 \times 10^8 \pm 6.1 \times 10^{-9}$</td>
</tr>
<tr>
<td>1L-ME-SiO$_2$</td>
<td>$-0.0241 \pm 0.0015$</td>
<td>--</td>
<td>--</td>
</tr>
<tr>
<td>1L-CVD-SiO$_2$</td>
<td>$-0.0217 \pm 0.0017$</td>
<td>$2.04 \times 10^5 \pm 8.4 \times 10^{-6}$</td>
<td>$-2.68 \times 10^8 \pm 1.2 \times 10^{-8}$</td>
</tr>
<tr>
<td>1L-CVD-Sa (till 425 °C)</td>
<td>$-0.0143 \pm 5.7 \times 10^{-4}$</td>
<td>$-1.44 \times 10^5 \pm 3.4 \times 10^{-6}$</td>
<td>$7.71 \times 10^9 \pm 5.6 \times 10^{-9}$</td>
</tr>
<tr>
<td>2L-CVD-SiO$_2$ (till 400 °C)</td>
<td>$-0.0233 \pm 0.0018$</td>
<td>$3.00 \times 10^5 \pm 1.1 \times 10^{-5}$</td>
<td>$-4.61 \times 10^8 \pm 2.0 \times 10^{-8}$</td>
</tr>
<tr>
<td>2L-CVD-Sa (till 425 °C)</td>
<td>$-0.0135 \pm 8.4 \times 10^{-4}$</td>
<td>$-2.54 \times 10^5 \pm 5.0 \times 10^{-6}$</td>
<td>$2.93 \times 10^8 \pm 8.2 \times 10^{-9}$</td>
</tr>
<tr>
<td>1L ME SiO$_2$ Ref.</td>
<td>$-0.0179$</td>
<td>--</td>
<td>--</td>
</tr>
<tr>
<td>2L ME SiO$_2$ Ref.</td>
<td>$-0.0137$</td>
<td>--</td>
<td>--</td>
</tr>
<tr>
<td>few layer Ref.</td>
<td>$-0.0132$</td>
<td>--</td>
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Fig. 5 Spatial maps (6 µm x 6 µm) of the Raman frequencies of (a) $E_{2g}^1$ and (b) $A_{1g}$ modes for 1L-ME-SiO$_2$ sample, and the unit is cm$^{-1}$. 
damping of Raman frequency redshift to $E_{2g}^l$ mode at the low temperature region, as manifested on the reduced magnitude of $\chi_1$ for the CVD-grown MoS$_2$ films on sapphire. Furthermore, the film-substrate coupling leads to the sign changes for both $\chi_2$ and $\chi_3$ compared to the bulk for the $E_{2g}^l$ mode of the on-sapphire samples. In contrast, mechanically transferred MoS$_2$ films on SiO$_2$/Si do not form the chemical bonding between film and substrate other than Van der Waals force, leading to the temperature dependence of Raman shift of $\chi_2$ of the $E_{2g}^l$ mode similar to bulk MoS$_2$. However, the MoS$_2$ films on SiO$_2$/Si are more likely to be affected by the changes in the film morphology such as wrinkles and ripples when temperature increases, due to thermal expansion coefficient mismatch between MoS$_2$ and SiO$_2$. These changes of morphology in turn will have a large impact on out-of-plane vibration ($A_{1g}$), causing not only the nonlinear effect of temperature coefficient but also the large deviation of $\chi_2$ from bulk MoS$_2$ for the SiO$_2$/Si samples. As for the sapphire samples, the chemical bonding restricts the MoS$_2$ film from morphology change, and the coupling with the substrate has a relatively small influence on the $A_{1g}$ mode. Therefore, we can conclude that the morphology of MoS$_2$ films plays a significant role in temperature dependence of $A_{1g}$ mode, which leads to the large and highly non-linear deviation from the bulk, while the bonding between film and substrate introduces weaker effects, in similar magnitudes, to both $E_{2g}^l$ and $A_{1g}$ modes on their temperature induced Raman shifts.

The integrated Raman intensity for both $E_{2g}^l$ and $A_{1g}$ modes has been found to decrease in all CVD-grown samples when $T$ is greater than 400 °C, possibly due to the decomposition of MoS$_2$ films. The thermal decomposition temperature for most samples including bulk is somewhere > 500 °C, except for 2L-CVD-SiO$_2$ being near 450 °C. For all CVD-grown MoS$_2$ films on sapphire, no Raman signal is detected when the temperature reaches 575 °C, indicating the decomposition of MoS$_2$ films. The Raman spectrum does not recover at room temperature after reaching the maximum temperature. The main change is that the frequency difference between $A_{1g}$ and $E_{2g}^l$ modes increases by 2.5 cm$^{-1}$ for 1L-ME-SiO$_2$. In addition, their peak intensities decrease. There are at least two possible reasons: (1) the strain or morphology has changed, as expected, (2) the sample might be partially oxidized or decomposed. Similar results have been reported for graphene.\cite{30}

Simulation model for temperature dependence of Raman shift

The intrinsic temperature dependence of the Raman shift can be divided into thermal expansion of the lattice ($\Delta \omega_R$) and anharmonic effect ($\Delta \omega_A$) which causes the change of phonon self-energy.\cite{27,31,32} In addition, thermally induced strains due to thermal expansion coefficient mismatch ($\Delta \omega_M$) between MoS$_2$ film and substrate should be considered.\cite{28} Thus, the measured frequency change can be written as

$$\Delta \omega(T) = \Delta \omega_R(T) + \Delta \omega_A(T) + \Delta \omega_M(T). \quad (2)$$

where $T$ is the sample temperature. Firstly, with increasing temperature, the lattice constant of MoS$_2$ structure increases due to thermal expansion of the film, leading to the Raman shift which is commonly expressed as\cite{32}

$$\Delta \omega_R(T) = \omega_0 \exp \left( -n \int_{T_1}^{T} \alpha \, dT \right) - \omega_0, \quad (3)$$

where $\omega_0$ is the room temperature frequency, $n$ is the degeneracy, 1 for $A_{1g}$ mode and 2 for $E_{2g}^l$ mode, $\gamma$ is the Gruneisen parameter, and $\alpha$ is the thermal expansion coefficient of the material. The Gruneisen parameters of both $E_{2g}^l$ and $A_{1g}$ modes for bulk MoS$_2$ are $\gamma(E_{2g}^l) = 0.21$ and $\gamma(A_{1g}) = 0.42$, respectively. The in-plane and out-of-plane thermal expansion coefficients for bulk MoS$_2$ have been derived from the results of Ref.\cite{33}.

$$\alpha_x(T) = \frac{0.6007 \times 10^{-3} + 0.6958 \times 10^{-3}}{a} \left( \frac{T}{1 \degree C} \right),$$

$$\alpha_y(T) = \frac{0.1064 \times 10^{-3} + 1.5474 \times 10^{-3}}{c} \left( \frac{T}{1 \degree C} \right), \quad (4)$$

where $T$ is the temperature in °C, $a$ and $c$ are the lattice constants of MoS$_2$ in Å. They are calculated to be $2.48 \times 10^{-6}$ /°C and $9.14 \times 10^{-6}$ /°C, respectively, for in-plane and out-of-plane thermal expansion coefficients at room temperature. The second term of right-handed side in Eq.(2) is related to pure temperature effect, so called “self-energy” shift due to anharmonic coupling of multiple phonons, which can be written as\cite{31}

$$\Delta \omega_A(T) = A \left[ \frac{2}{e^{x-1} - 1} \right] + B \left[ \frac{3}{e^{x-1} - 1} \right]^3, \quad (5)$$

where $x = \hbar \omega / 2kT$, $y = \hbar \omega / 3kT$, and the first term corresponds to coupling of the optical phonon to two identical phonons, and the second term represents the coupling to three identical phonons. The coefficients $A$ and $B$ are constants that can be estimated by fitting the frequency shift attributes to anharmonic coupling. The possible remaining change of Raman shift is associated with the thermal expansion coefficient mismatch between film and substrate, introducing strain to the film, which can be expressed as\cite{28}

$$\Delta \omega_M(T) = B \int_{T_1}^{T} \left( \alpha_{Sub} - \alpha_{MoS_2} \right) \, dT. \quad (6)$$

where $\beta$ is the biaxial strain coefficient, $\alpha_{Sub}$ and $\alpha_{MoS_2}$ are the thermal expansion coefficients of substrate and MoS$_2$, respectively. For bulk MoS$_2$, there is no thermal expansion...
coefficient mismatch between MoS$_2$ layers, so that the third term is zero. Eq.(6) assumes that the film and substrate is in coherent strain, which is likely invalid for the transferred film. Fig.6 shows these contributions to the changes in Raman peak positions of both $E_{2g}$ and $A_{1g}$ modes for bulk MoS$_2$ with good agreement to experimental results, Table 2 shows the fitting parameters of $A$ and $B$ for both $E_{2g}$ and $A_{1g}$ modes.

However, this model, which predicts a monotonic behavior, is not appropriate for MoS$_2$ films, either 1L or 2L, on substrates. In the case of MoS$_2$ films on substrates like SiO$_2$/Si and sapphire, according to Eq.(6) with $\beta$ being -2.1 cm$^{-1}$ per % strain, the contribution of the thermal expansion coefficient mismatch is expected to be negligible compared to the thermal expansion of lattice and anharmonic effect in the temperature region of interest.$^{34,35}$ With increasing temperature, the biaxial tensile or compressive strain induced by thermal expansion coefficient mismatch increases significantly over the Van der Waals force, resulting in the slippage or realignment of MoS$_2$ films on the surface of the substrate as well as forming wrinkles or ripples. For 1L-ME-SiO$_2$ sample, the realignment process takes place at $\sim$100 °C where there is an obvious slope transition of $A_{1g}$ peak position. During the realignment process, defects may be introduced into MoS$_2$ film such as the breakdown of Mo-S bonds and the slow decomposition of the film, showing a broadening of $A_{1g}$ Raman peak (Fig.4). After the MoS$_2$ layer adjusts to a stable state on the SiO$_2$/Si substrate at high temperature, the Raman shift of $A_{1g}$ mode again follows what is expected from Eq.(2).

**Table 2** The fitting parameters $A$ and $B$ for both $E_{2g}$ and $A_{1g}$ modes used in three- and four-phonon coupling model.

<table>
<thead>
<tr>
<th>bulk MoS$_2$</th>
<th>$E_{2g}$</th>
<th>$A_{1g}$</th>
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<tbody>
<tr>
<td>$A$ (cm$^{-1}$)</td>
<td>-3.05835</td>
<td>0.04204</td>
</tr>
<tr>
<td>$B$ (cm$^{-1}$)</td>
<td>-5.68777</td>
<td>0.26566</td>
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</tbody>
</table>

Waals force, resulting in the slippage or realignment of MoS$_2$ films on the surface of the substrate as well as forming wrinkles or ripples. For 1L-ME-SiO$_2$ sample, the realignment process takes place at $\sim$100 °C where there is an obvious slope transition of $A_{1g}$ peak position. During the realignment process, defects may be introduced into MoS$_2$ film such as the breakdown of Mo-S bonds and the slow decomposition of the film, showing a broadening of $A_{1g}$ Raman peak (Fig.4). After the MoS$_2$ layer adjusts to a stable state on the SiO$_2$/Si substrate at high temperature, the Raman shift of $A_{1g}$ mode again follows what is expected from Eq.(2).

**Full Width at Half Maximum (FWHM)**

Fig.7 shows the temperature dependent FWHM of both $E_{2g}$ and $A_{1g}$ peak for all samples, by fitting to a Lorentzian lineshape function. Bulk MoS$_2$ has room-temperature FWHMs of 1.6 cm$^{-1}$ and 2.2 cm$^{-1}$, respectively, for $E_{2g}$ and $A_{1g}$. Other samples have greater FWHMs, indicating the film-substrate coupling and defects existing in these samples that cause the peak broadening. The FWHM of $E_{2g}$ mode, in general, increases linearly with increasing temperature. However, the $A_{1g}$ mode does not show a monotonic dependence but with a maximum linewidth in the middle of the temperature range. As it is discussed above, the mismatch of thermal expansion coefficients between MoS$_2$ films and substrates gives rise to changes of morphology e.g. wrinkles or ripples, consequently leading to a significant change of the temperature coefficients of $A_{1g}$ mode. For all 1L and 2L samples, the FWHM of $A_{1g}$ reaches the maximum when the realignment process occurs.

For instance, the anomaly of temperature dependent Raman shift of 1L-ME-SiO$_2$ takes place at the temperatures starting from $\sim$100 °C, while the FWHM reaches the maximum at 125 °C and then starts to decrease afterward. This gives an additional illustration that the change of the morphology by the thermal expansion coefficient mismatch can affect the out-of-plane vibrational mode more than the in-plane mode when the temperature reaches a critical value.

**Conclusions**

In summary, we have reported temperature-dependent Raman studies of the in-plane $E_{2g}$ and out-of-plane $A_{1g}$ modes on single- and bi-layer MoS$_2$ samples prepared by CVD growth and mechanical exfoliation on SiO$_2$/Si and sapphire substrates in a temperature range of 25 - 500 °C. Bulk MoS$_2$ has also been measured to serve as the references, with the first-order temperature coefficients of the Raman frequency shifts given as $\gamma_E(E_{2g}) = -0.0221 \pm 8.9 \times 10^{-4}$ cm$^{-1}$/K and $\gamma_A(A_{1g}) = -0.0197 \pm 8.94 \times 10^{-4}$ cm$^{-1}$/K, respectively, for the $E_{2g}$ and $A_{1g}$ mode. The thermal decomposition temperature is found to be approximately 575 °C for CVD-grown films on sapphire. The film-substrate coupling affects the temperature dependence of Raman frequency, intensity, and linewidth for both $E_{2g}$ and $A_{1g}$ modes in the 1L and 2L MoS$_2$. The impact depends on the substrate type and/or film-substrate binding mechanism. For the CVD grown film on the original sapphire substrate with likely chemical bonding between them, the film-substrate coupling significantly reduces the linear temperature coefficients of the Raman shift of the $E_{2g}$ mode to $-0.0143 \pm 3.7 \times 10^{-3}$ cm$^{-1}$/K for 1L and $-0.0135 \pm 8.4 \times 10^{-4}$ cm$^{-1}$/K for 2L, but has no or small effect on the $A_{1g}$ mode, with $-0.0199 \pm 0.0012$ cm$^{-1}$/K for 1L and $-0.0160 \pm 0.0014$ cm$^{-1}$/K for 2L. For the transferred film on SiO$_2$/Si substrate, originally grown on sapphire by CVD, for the $E_{2g}$ mode, the temperature coefficients were found to be very close to the bulk value as $-0.0217 \pm 0.0017$ cm$^{-1}$/K for 1L and $-0.0233 \pm 0.0018$ cm$^{-1}$/K for 2L; but for $A_{1g}$ mode, they increase substantially to $-0.0301 \pm 0.0023$ cm$^{-1}$/K for 1L and $-0.0310 \pm 0.0024$ cm$^{-1}$/K for 2L, respectively.

![Fig. 7 Temperature dependence of FWHM of $E_{2g}$ and $A_{1g}$ modes in bulk and all other 1L and 2L samples.](image-url)
0.0018 cm\(^{-1}/K\) for 2L. The substrate effects are most pronounced for the \(A_{1g}\) mode, showing as stronger nonlinearity on the temperature shift of the Raman frequency and non-monotonic temperature dependence of the Raman linewidth. Similar or even stronger effects were observed on a mechanically exfoliated 1L film from a bulk single crystal. These results suggest that for the mechanically transferred thin film, due to the mismatch in thermal expansion between the film and substrate, the temperature change can lead to significant changes in the thin-film morphology as a result of realignment of the film on the substrate, which can be most easily probed by the temperature dependence of the \(A_{1g}\) mode associated with the out-of-plane atomic vibration. Temperature dependent Raman study provides an efficient tool for investigating the coupling between the 2D material and substrate either with chemical or mechanical bonding.

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Notes and references